

# **Fast GA-based project scheduling for computing resources allocation in a cloud manufacturing system**

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Received: 30 November 2014 / Accepted: 25 March 2015 / Published online: 8 April 2015 © Springer Science+Business Media New York 2015

**Abstract** Cloud manufacturing is becoming an increasingly popular enterprise model in which computing resources are made available on-demand to the user as needed. Cloud manufacturing aims at providing low-cost, resource-sharing and effective coordination. In this study, we present a genetic algorithm (GA) based resource constraint project scheduling, incorporating a number of new ideas (enhancements and local search) for solving computing resources allocation problems in a cloud manufacturing system. A newly generated offspring may not be feasible due to task precedence and resource availability constraints. Conflict resolutions and enhancements are performed on newly generated offsprings after crossover or mutation. The local search can exploit the neighborhood of solutions to find better schedules. Due to its complex characteristics, computing resources allocation in a cloud manufacturing system is NP-hard. Computational results show that the proposed GA can rapidly provide a good quality schedule that can optimally allocate computing resources and satisfy users' demands.

**Keywords** Resource allocation · Cloud manufacturing · Project scheduling · Genetic algorithm

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## **Introduction**

Cloud manufacturing is a service-oriented, customer-centric, demand-driven manufacturing model that aims at providing low-cost, resource-sharing and effective coordination. According to [Wu et al.](#page-12-0) [\(2013](#page-12-0)), cloud manufacturing requires interaction between three groups: the users, application providers, and physical resource providers. Users are the consumers in cloud manufacturing. They have the need to manufacture a product, but do not possess the capabilities to do so, or they possess the capabilities but can also gain a competitive advantage by using cloud manufacturing. The application providers are responsible for managing all aspects of the cloud manufacturing environment and transfers user requirements into data required for manufacturing the desired products. Physical resource providers own and operate manufacturing equipment, such as forms of machining, finishing, inspection, packaging technology, testing resources, etc. Moreover, physical resource providers have the expertise and experience to utilize these machines effectively and efficiently. Computing resources (such as CPU, processors, I/O, networks, servers, storage, applications, services, etc.) at the physical resource layer is an important part of cloud manufacturing. Through centralized management, the application providers transfer users' demands into virtual access, and assign various heterogeneous computing resources to process those demands.

The current computing resource allocation in cloud manufact[uring](#page-12-1) [faces](#page-12-1) [several](#page-12-1) [difficult](#page-12-1) [problems.](#page-12-1) [Based](#page-12-1) [on](#page-12-1) Wu and Yang [\(2010](#page-12-1)), in order to cope with the quickly changing market requirements in an increasing globalized economic environment, manufacturing enterprises need to develop extensive collaboration among themselves. This includes many kinds of manufacturing resources sharing. These resources are geographically distributed, with morphology

diversity and autonomy, which makes the resource-sharing and management very complicated. Further, the computing resources are made available on-demand and dynamically allocated to the user as needed, to realize scalable integration of all kinds of distributed resources for effective use. Some of the previous studies pointed out that in the cloud manufacturing system, the resource demands are time varying and often has large spikes. How to appropriately select the price and allocate resources for each type of virtual machine services in order to best match the interests of the customers is a key issue of cloud manufacturing [\(Zhang et al. 2011](#page-12-2)). Another key issue is how to minimize the response time of data [processing](#page-12-3) [queries](#page-12-3) [to](#page-12-3) [satisfy](#page-12-3) [customer](#page-12-3) [demands](#page-12-3) [\(](#page-12-3)Lee et al. [2011](#page-12-3)). Further, [Laili et al.](#page-12-4) [\(2012\)](#page-12-4) mentioned that the optimal allocation of computing resources is the core part of implementing cloud manufacturing. High heterogeneity, high dynamism, and virtualization make the optimal allocation of computing resources problems more complex than the traditional scheduling problems in the grid system or cloud computing system. Motivated by these studies, this paper proposed a new and fast hybrid GA method on the proposed model to solve the optimal allocation of computing resources problems.

In this work, we are assuming that there are multiple project planning problems that require computing resources from cloud manufacturing platforms at the same time. Hence, large amount of tasks with different resource requirements that are submitted to the cloud manufacturing platform need to be scheduled heterogeneously under layer clusters. The cloud-based application providers need to centrally manage those demands, and allocate computing resources in order to process them and respond to users promptly.

Figure [1](#page-1-0) shows computing resources allocation in a cloud manufacturing system for resource-constrained project scheduling problems (RCPSPs). We focus on studying the problem of computing resources allocation in a cloud manufacturing system. A GA has been proposed to tackle the problem. The rest of this work is organized as follows. Section [2](#page-1-1) provides the related works; Sect. [3](#page-2-0) introduces resource-constrained project scheduling; the proposed GA is presented in Sect. [4;](#page-3-0) in Sect. [5,](#page-6-0) the computational results are reported; Sect. [6](#page-10-0) presents our conclusions and suggestions for future research.

## <span id="page-1-1"></span>**Related works**

In recent years, cloud manufacturing has been studied by many researchers. Some researchers focused on studying computing resource allocation in a cloud manufacturing system [\(Wu and Yang 2010;](#page-12-1) [Lee et al. 2011](#page-12-3); [Zhang et al.](#page-12-2) [2011](#page-12-2)). [Laili et al.](#page-12-5) [\(2011](#page-12-5)) used a GA to solve the problem of optimal allocation of computing resources in cloud manufacturing systems. In a subsequent study, [Laili et al.](#page-12-4) [\(2012](#page-12-4)) proposed a new and improved niche immune algorithm (NIA) for optimal allocation of computing resources in cloud manufacturing systems. They showed that NIA outperforms other intelligent algorithms in solving computing resources allocation problems. [Tao et al.](#page-12-6) [\(2012\)](#page-12-6) proposed a novel parallel intelligent algorithm, namely, full connection based parallel-adaptive chaos optimization with reflex migration (FC-PACO-RM) for service composition optimization-selection in a cloud manufacturing system. [Laili et al.](#page-12-7) [\(2013\)](#page-12-7) proposed a ranking chaos algorithm for dual scheduling of cloud service and computing resources in a private cloud. [Cheng et al.](#page-11-0) [\(2013](#page-11-0)) established comprehensive utility models, which consider energy consumption, costs, and risks for the three sides (provider, consumer, and



<span id="page-1-0"></span>**Fig. 1** Computing resources allocation in cloud manufacturing system for project scheduling problems

operator) in the resource service scheduling process in a cloud manufacturing system.

Some researchers focused on studying workflow scheduling in cloud computing environment. A cloud workflow system is a type of platform service which facilitates the automation of distributed applications based on the novel cloud infrastructure. [Kaur et al.](#page-11-1) [\(2011](#page-11-1)) provided a comparison of workflow scheduling algorithms in cloud computing. [Varalakshmi et al.](#page-12-8) [\(2011](#page-12-8)) proposed an optimal workflow based algorithm for scheduling workflows in a cloud environment. [Bardsiri and Hashemi](#page-11-2) [\(2012\)](#page-11-2) provided a review of workflow scheduling in the cloud computing environment. [Kim et al.](#page-11-3) [\(2012\)](#page-11-3) developed an adaptive workflow scheduling scheme that optimized the allocation ratio of computing elements to the different datasets in order to minimize the total makespan under certain resource constraints. [Abrishami and Naghibzadeh](#page-11-4) [\(2012](#page-11-4)) proposed an algorithm for workflow scheduling in the software as a service cloud, which minimizes the total execution cost, while meeting userdefined deadlines. Rahman et al. (2013) proposed an adaptive workflow scheduling algorithm for dynamic grid and cloud computing environments. [Lodha and Wadhe](#page-12-10) [\(2013\)](#page-12-10) provided a study on different types of workflow scheduling algorithm in cloud computing. [Yassa et al.](#page-12-11) [\(2013\)](#page-12-11) proposed a multiobjective approach for energy-aware workflow scheduling in cloud computing environments.

From the literature review, we concluded that the optimal allocation of computing resources is one of the urgent issues in cloud manufacturing. Also, prompt response to customers' demands is a requirement in cloud manufacturing. Hence, in this study, we proposed a fast hybrid GA to solve the optimal allocation of computing resources problems.

#### <span id="page-2-0"></span>**Resource-constrained project scheduling problem**

According to [Laili et al.](#page-12-5) [\(2011\)](#page-12-5), cloud manufacturing is a service-oriented networked manufacturing model which aims at achieving low cost resource sharing and coordination. By way of virtual access, various heterogeneous computing resources at the physical layer of cloud manufacturing are assigned to users on-demand. The demand of coordination and computing power on the cloud manufacturing platform is high and varied as manufacturing tasks are usually complex and multi-disciplinary collaborative tasks. To ensure efficient running of manufacturing tasks and to fully utilize computing resources, the optimal allocation of computing resources to manufacturing tasks in cloud manufacturing is important. This poses challenges for optimal allocation of computing resources as computing resources have the characteristics of large scale, high heterogeneity, dynamic interconnection and group collaboration. The practical issues and constraints related to resource allocation are discussed in detail in Laili et al. [\(2011](#page-12-5)). To tackle the challenges, [Laili et al.](#page-12-5) [\(2011\)](#page-12-5) formulated a new optimal allocation of computing resources model based on the uncertain resource topology. The model considered the constrain conditions from all aspects and is closer to reality.

Similar to [Laili et al.](#page-12-5) [\(2011,](#page-12-5) [2012](#page-12-4)), we are assuming that there are multiple project planning problems that require computing resources from cloud manufacturing. Due to the large amount of tasks, there are different resource requirements submitted to a cloud manufacturing platform that need to be scheduled heterogeneously under layer clusters. There is an insufficient amount of practical activity time, so we made some assumptions and set a range for them. Hence, this study only follows one project scheduling. For a given project scheduling problem, we use graphs and record the successors and predecessors of each node by having adjacent lists. Since many tasks are submitted to a resource for service, and the resource is needed to handle the tasks sequentially, we vary the activity times to reflect the situations of resource allocation in cloud manufacturing. The task duration of each node is randomly generated within a certain range. When we complete evaluations, we start from the source (the first) node, and then find its successors step by step, which is followed by recording the whole task durations at the end of the graph (sink node). Project scheduling problem in cloud manufacturing is one type of RCPSPs.

Here, we give a brief literature review of RCPSPs. In recent years, more and more researchers have studied the RCPSPs [\(Brucker et al. 1999](#page-11-5); [Hartmann and Briskorn 2010](#page-11-6)). [Kolisch and Hartmann](#page-12-12) [\(2006](#page-12-12)) have summarized and categorized a large number of heuristics that have recently been proposed in the literature for the RCPSPs. Some researchers have proposed sampling-method based on heuristics [\(Kolisch](#page-12-13) [1995](#page-12-13), [1996a](#page-12-14), [b;](#page-12-15) [Kolisch and Drexl 1996;](#page-12-16) [Shue and Zamani](#page-12-17) [1999](#page-12-17); [Grèze et al. 2014\)](#page-11-7). Amongst the sampling methods, the heuristics are referred to as sampling random (S) and sampling-random (P) corresponding to pure random sampling with serial and parallel scheduling generation scheme (SGS). Some researchers have developed metaheuristic based algorithms to tackle the RCPSPs, which include GA [\(Leon and Ramamoorthy 1995;](#page-12-18) [Hartmann 1998](#page-11-8); [Coelho and Tavares 2003](#page-11-9); [Debels and Vanhoucke 2007](#page-11-10)[;](#page-12-19) Valls et al. [2008](#page-12-19); [Agarwal et al. 2011](#page-11-11); [Ji and Yao 2014\)](#page-11-12), ant colony optimization (ACO) [\(Merkle et al. 2002,](#page-12-20) [Chen et al.](#page-11-13) [2010](#page-12-5)[a](#page-11-13), [b](#page-11-14)), simulated annealing (SA) [\(Bouleimen and Lecocq](#page-11-15) [2003](#page-11-15)), filter-and-fan approach [\(Ranjbar 2008](#page-12-21)), bee colony [\(Shi et al. 2010](#page-12-22); [Jia and Seo 2013b\)](#page-11-16), shuffled frog-leaping algorithm [\(Fang and Wang 2012](#page-11-17)) and particle swarm optimization (PSO) [\(Jia and Seo 2013a](#page-11-18)).

A brief introduction of RCPSP is provided here. The RCPSP can be described as follows. A single project consists of a set  $J = \{0, 1, ..., n, n + 1\}$  of tasks (activities), which have to be processed. Fictitious tasks 0 and  $n + 1$ 

correspond to the "project start" and to the "project end", respectively. The tasks are subjected to two kinds of constraints. First, precedence constraints enforce task *j* to start only after all its immediate predecessors have been completed. Second, performing the tasks requires resources that are limited. Resources may be renewable or non-renewable. Renewable resources are available for each period without being depleted, such as labor and computer memory. Non-renewable resources are depleted as they are used up, such as capital and raw materials. We have *K* renewable resource types, given by the set  $\kappa = \{1, ..., K\}$ . While being processed, task *j* requires  $r_{i,k}$  units of resource type  $k \in \kappa$  during every period of its non-preemptable duration  $p_i$ . Resource type *k* has a limited capacity of  $R_k$  at any point in time. For the project start and end tasks, we have  $P_i = 0$  and  $r_{i,k} = 0$  for all  $k \in \kappa$ . The objective of the RCPSP is to find precedence and resource feasible completion times for all tasks so that the makespan of the project is minimized. We use an instance j301\_5 (we call it Example 1) that is taken from the project scheduling problem library (PSPLIB, [Kolisch and Sprecher 1997](#page-12-23)) to illustrate the ideas of the studied problem. Table [1](#page-3-1) gives an example of a project comprising  $n = 32$  tasks, which have to be scheduled subject to the  $K = 4$  renewable resource type with a capacity of  $R_1 = 11$ ,  $R_2 = 11$ ,  $R_3 = 9$ ,  $R_4 = 11$  units. A feasible schedule with a makespan of 40 periods is represented in Fig. [2.](#page-4-0) Figure [3](#page-4-1) shows resource allocation of Example 1 where a number inside a parenthesis indicates the resource consumption of the task.

## **Genetic algorithms**

GAs are stochastic search techniques that are inspired by the principles of evolution and heredity [\(Holland 1975\)](#page-11-19). The usual form of a GA is described by [Goldberg](#page-11-20) [\(1989](#page-11-20)). GAs have been proven to be a very robust algorithm for solving NP-hard global optimization problems, including scheduling problems. GAs are very effective for its climbing ability and the diversification in search. Besides that, GAs are easy to adapt, implement, and enhance. In the last two decades, there are lots of researchers applied GA-based approaches to solve the RCPSPs successfully [\(Leon and Ramamoorthy](#page-12-18) [1995](#page-12-18); [Hartmann 1998](#page-11-8); [Alcaraz and Maroto 2001](#page-11-21); [Hartmann](#page-11-22) [2002](#page-11-22); [Coelho and Tavares 2003;](#page-11-9) [Kochetov and Stolyar 2003](#page-12-24); [Alcaraz et al. 2004;](#page-11-23) [Valls et al. 2008;](#page-12-19) [Mendes et al. 2009](#page-12-25); [Debels and Vanhoucke 2007;](#page-11-10) [Khanzadi et al. 2011](#page-11-24)[;](#page-11-11) Agarwal et al. [2011;](#page-11-11) [Gonçalves et al. 2011;](#page-11-25) [Zamani 2013](#page-12-26)). GAs are population based algorithms that work iteratively. A single iteration is called a generation. When applying them to scheduling problems, GAs consider a schedule as an individual of a population. A fitness value derived from the objective value of the schedule is assigned to each single individual, called a genome. The individuals of the new generation are obtained from the individuals of the previous generation by applying crossover and mutation procedures. The fittest among populations are selected, and are then carried into the next generation. In this work, we present a GA for optimal allocation of computing resources in a cloud manufacturing system. The proposed GA are described as follows.

<span id="page-3-2"></span><span id="page-3-0"></span>**Table 1** Data of Example 1

<span id="page-3-1"></span>

Task $j$	<b>Successors</b>	Durations $p_j$	$r_{j,1}$	$r_{j,2}$	$r_{j,3}$	$r_{j,4}$	Task $j$	Successors	Durations $p_j$	$r_{j,1}$	$r_{j,2}$	$r_{j,3}$	$r_{j,4}$
	2, 3, 4	$\overline{0}$	$\Omega$	$\overline{0}$	$\overline{0}$	$\overline{0}$	17	26	3	$\Omega$	$\overline{2}$	$\overline{0}$	$\theta$
2	11, 12, 15	6	$\Omega$	$\Omega$	7	$\Omega$	18	19, 23	2		$\Omega$	$\Omega$	$\theta$
3	5, 8, 16	4	$\Omega$	$\Omega$		$\Omega$	19	22		0	8	$\Omega$	$\Omega$
$\overline{4}$	27	2.	$\Omega$	$\Omega$	$\Omega$	2	20	29		$\Omega$	$\Omega$	5	$\Omega$
5	6, 12, 14		$\Omega$	$\overline{0}$	6	$\Omega$	21	31		$\Omega$	$\Omega$	$\Omega$	$\overline{c}$
6			$\mathfrak{D}$	$\Omega$	$\Omega$	$\Omega$	22	24		$\Omega$	$\Omega$	$\Omega$	
7	9, 28		$\Omega$	$\theta$	$\Omega$	6	23	24		$\Omega$	$\Omega$	$\Omega$	
8	10, 20	3	$\Omega$	9	$\Omega$	$\Omega$	24	29		$\Omega$	$\Omega$	$\Omega$	
9	13, 21	5.	0	8	$\Omega$	$\Omega$	25	30		0	9	$\Omega$	$\Omega$
10	17, 25	6	8	$\Omega$	$\Omega$	$\Omega$	26	28		$\Omega$	5	$\Omega$	$\overline{0}$
11	25, 28	6	0	$\Omega$	7	$\Omega$	27	30		$\Omega$	9	$\Omega$	$\theta$
12	25, 29			$\Omega$	$\Omega$	$\Omega$	28	30		0	4	$\Omega$	$\Omega$
13	22, 23, 31		8	$\Omega$	$\Omega$	$\Omega$	29	32		$\Omega$	4	$\Omega$	$\Omega$
14	17	6	0		$\Omega$	$\Omega$	30	32		$\Omega$	9	$\Omega$	$\theta$
15	24		$\Omega$	$\Omega$	$\Omega$	2	31	32		$\Omega$	$\Omega$	$\Omega$	10
16	18	3.	$\overline{0}$	$\theta$	5	$\theta$	32		0	$\Omega$	$\theta$	$\overline{0}$	$\overline{0}$



<span id="page-4-0"></span>**Fig. 2** A feasible solution of Example 1



<span id="page-4-1"></span>**Fig. 3** Resource allocation of Example 1

## **Basic operations of the GA**

### *Genetic representation*

[Wall](#page-12-27) [\(1996\)](#page-12-27) developed a coding scheme that can generate a feasible solution for project scheduling problems. Here, we use the [Wall](#page-12-27) [\(1996](#page-12-27)) coding scheme to represent a solution to the problem at hand, as a genome. A single genome is a single array of integer start times. Each element in the array corresponds to a task in the project plan. The times represent delay times relative to the latest finish time of the task's predecessors. Unlike traditional solution methods which are typically sequence-based, each genome uses representation that encodes scheduling information as an array of relative start times. Each time represents the duration from the latest finish of all predecessor tasks, to the start time of the corresponding task. The times represent delay times relative to the finish time of the predecessors. If the precedence constraints for a task is allowed to overlap, then negative values are permitted for the start time for this particular task. If overlap is not modeled, values are truncated to zero. The elements in the array correspond to the tasks in the project plan, but the order of elements relative to each other is insignificant. This encoding scheme for scheduling is a minimal repre-



<span id="page-5-0"></span>**Fig. 4** Representation of a genome and its mapping to the schedule

sentation that can only represent resource-feasible solutions. Unlike order-based representation, the encoding scheme will assure precedence feasibility for every schedule after any crossover operator, with no schedule repair required. Figure [4](#page-5-0) gives an example of a single project consisting of seven tasks. A possible representation for Fig. [4](#page-5-0) could be  $[t_1, t_2, t_3, t_4, t_5, t_6, t_7]=[0, 2, 3, 3, 3, 1, 4].$ 

## *Initialization*

We use random initialization. The integer start times of the genome are initialized with random numbers. The range of possible values is based upon the average estimated task durations. We sum up all of the task durations and divide them by the number of tasks, excluding the first and last virtual tasks. Based on this average duration, we get the lower and upper durations by multiplying them with certain factors, currently set at 0.1 and 3.0, and then use a random function to generate a random value for each element in the time component of the genome.

## *Crossover*

We use blend crossover [\(Eshelman and Schaffer 1992\)](#page-11-26) to generate new offsprings from two parent values. Each genome is encoded as an array of relative start times. Each time represents the duration from the latest finish of all the predecessor tasks to the start time of the corresponding task. This representation is different from traditional solution methods, which are typically sequence based. By combining the array of relative start times encoding and Blend Crossover, the location of the offspring will depend on the difference in the parent solutions. If the differences between the parent solutions are small, the difference between the offspring and parent solution will be correspondingly small. This property of the search operator constitutes an adaptive search and needs no tuning parameter. The operator enables searching of an entire space, at the initial stage, when a random population over the entire space is initialized, and then it concentrates the search more on the later stages, when the population tends to converge in some region of the search space. The adaptive search property was highlighted in a study by [Mehra et al.](#page-12-28) [\(2014](#page-12-28)). They showed that Blend Crossover performed better than Arithmetic Crossover in their problem domain. The crossover operator is a kind of linear combination of the two parents that uses the following equations for each gene:



where b is a random value between 0 and 1.

#### *Mutation*

Mutation is performed by applying Gaussian noise to each element in the array. A single element in the genome was mutated by replacing it with a number chosen based upon a Gaussian distribution defined by a mean and a standard deviation. The mean and standard deviation are both set equal to the gene's previous value. The mutation probability is genebased, not genome-based.

## *Evaluation and selection*

During each generation, genomes are evaluated using a measure of fitness based on the original objective function. Since we deal with a minimization problem, we convert the genome *i* objective function value into its fitness value by using a  $f_i = 1/m$ akespan, so that a fitter genome has a larger fitness value. In each generation, we select a portion (replacement percentage) of the worst individuals, and then replace them with newly generated good individuals in order to create a new population for the next generation.

## *Termination*

There are two terminating conditions. The first one is based on the number of generations, and the second one is based on the number of generations that cannot achieve a better solution, whichever is earlier.

#### *Parameterization*

We studied the effects of several important parameters on the performance of our proposed GA. Since a rapid response and optimal resource allocation is required for cloud manufacturing, extensive trial runs have been performed to provide practical values for the GA-related parameters. The selected GA parameters are the number of generations = 20, population size = 30, crossover rate =  $0.6$  and mutation rate =  $0.2$ , generations that cannot achieve a better solution = 9, the replacement percentage =  $0.2$ , local search level = 5, and number of best local search at each level = 3.

#### **Enhancement**

A newly generated offspring might not be feasible after crossover or mutation. This is because the encoding of genome has not considered resource constraints. In that case, we will perform enhancements to resolve those problems. After the crossover and mutation, and based on the delay times of genes of a genome, we construct an initial project schedule without considering the resource constraint, and in ascending order of task numbers and by using serial schedule generation scheme (serial SGS). Based on the start times of tasks in the constructed schedule, we sort the tasks in ascending order of their start times. The sorting also ensures the task precedence relationships of tasks satisfied. Based on the sorted task sequence, we then construct a final schedule that takes into consideration of task precedence and resource constraints by using serial SGS.

## **Local search**

Two kinds of neighborhood search approaches are implemented in this research to exploit the neighborhood of solutions. Both neighborhood search approaches have used the concept of a block, in which a move is defined by inserting a task to a block on a critical path. Critical paths play

an important part in a feasible solution. Critical paths are the longest routes from a start node to a sink node in a directed graph. We first try to locate the critical path blocks for a given solution. This is quite similar to job shop scheduling [\(Nowicki and Smutnicki 1996\)](#page-12-29). From the last task, based on predecessor tasks and resource constraints, we traced them backwards. Take Example 1 in Fig. [3](#page-4-1) as an example. Those rectangles highlighted with thicker borders are tasks in the critical path, which include (2, 5, 12, 18, 19, 9, 25, 26, 28, 30). A critical block  $(B)$  is a maximum subsequence of successive tasks, which contains tasks that are processed on the same machine in the critical path. For example, there are five blocks in the critical path, which are  $B_1 = (2, 5)$ ,  $B_2 = (12, 18)$ ,  $B_3 = (19, 9, 25), B_4 = (26, 28), B_5 = (30).$ 

Our first neighborhood search approach (N1) is based on [Nowicki and Smutnicki](#page-12-29) [\(1996\)](#page-12-29). For each critical path, we consider a set of moves that "swaps tasks near the borderline of blocks on a single critical path", as shown in Fig. [5.](#page-6-1) In the first block, we only swap the last two tasks, while in the last block, we only swap the first two tasks. For other blocks, besides the first and last blocks, we swap the first two tasks and the last two tasks, each of which contains at least two tasks.

Our second neighborhood search approach (N2) is based on [Balas and Vazacopoulos\(1998](#page-11-27)). For each critical path, we consider a set of moves that "moves internal tasks to either before the first or after the last task on a critical path" as shown in Fig. [6.](#page-7-0) The size of N2 is quite large and the approach is time consuming. However, our preliminary result shows that it tends to get better makespan than N1 since it considers more moves.

<span id="page-6-0"></span>We test all of N1 (N2) moves, and choose the best *n* defined by the parameter (number of best local search) to go and find another critical path and then repeat the same procedure. This can go on indefinitely, as long as there are still tasks that can be swapped. Hence, we further use another parameter (local search level) to define how many levels (how many critical paths) we want to execute in a local search.



<span id="page-6-1"></span>**Fig. 5** Neighborhood of moves (N1)



**Fig. 6** Neighborhood of moves (N2)

<span id="page-7-0"></span>

<span id="page-7-1"></span>**Fig. 7** The converge curves of the proposed GA

## **Computational results**

In this section, we present several computational results on the performance of the proposed GA. The GA was implemented in C++ using GAlib, a C++ library of GA components developed by [Wall](#page-12-27) [\(1996\)](#page-12-27). Test instances include a variet[y](#page-12-23) [of](#page-12-23) [RCPSPs](#page-12-23) [taken](#page-12-23) [from](#page-12-23) [PSPLIB](#page-12-23) [\(](#page-12-23)Kolisch and Sprecher [1997](#page-12-23)) and ran on an Intel (R) Core (TM) i7-3770 3.4 GHz processor and 16 GB RAM. We have selected the test sets J30, J60, J90, and J120. Each of these sets contains projects with 30, 60, 90, and 120 tasks, respectively, and four resources.

#### **The convergence curves of the proposed GA**

We examined the convergence curves of the proposed GA. We set the maximum generation to 10000 and disabled the terminating conditions for the number of generations that cannot achieve a better solution. Figure [7](#page-7-1) shows five typical convergence curves for some of the benchmark instances of J120. From the curves, the GA has a steep descent for early generations. This is important for a fast GA applicable for resource allocation problems in cloud manufacturing. The GA, in average, takes 2703.4 generations to converge to the best solution for the 20 tested benchmark problem instances of J120.

## **The performance of the proposed GA**

In order to examine the performance of the proposed GA, we first compare it with benchmark problem instances taken from PSPLIB. Two kinds of neighborhoods have been used to evaluate the quality of the proposed GA. GA\_N1 represents GA incorporated with neighborhood search approach N1 while GA\_N2 represents GA incorporated with neighborhood search approach N2. Four sets (J30, J60, J90, and J120) of benchmark instances have been used to evaluate the quality of the proposed GA. For each set of problem sizes, 20 instances have been selected. Since not all of the problem instances in PSPLIB have found optimal solutions, we have selected instances that have provided optimal solutions to be tested (lower bound = upper bound). Table [2](#page-8-0) gives the computational results for benchmark problem instances. For single project scheduling that contains J30, J60, J90, and J120, the GA\_N1 on average deviates 1.1, 2.9, 5.9, and 14.2% from the optimal solution. The average computation times are 0.09, 0.24, 0.51, and 1.77 s for J30, J60, J90, and J120, respectively. The GA\_N2 on average deviates 1.1, 2.4, 4.8, and 13.3% from the optimal solution for J30, J60, J90, and J120, respectively. The average computation times are 0.09, 0.28, 0.81, and 2.88 s for J30, J60, J90, and J120, respectively. As the problem size increases, the average deviation from the optimal solutions increases. Also, as the problem size increases, the computation time increases. Our GA settings are fined tune for problem size 30 and we used the same GA

<span id="page-8-0"></span>

Number of tasks	Opt.	GA N1	$(GA_N1-Opt.)$ Opt.	Computation time(s)	GA N <sub>2</sub>	$(GA N2-Opt.)$ Opt.	Computation time(s)
J30	48.20	48.75	0.011	0.09	48.75	0.011	0.09
J60	71.45	73.55	0.029	0.24	73.20	0.024	0.28
J90	84.05	87.90	0.046	0.50	87.00	0.035	0.76
J120	98.00	111.90	0.142	1.77	111.00	0.133	2.88
Average	75.425	80.813	0.057	0.649	80.25	0.051	1.004

**Table 2** The performance of GA for benchmark problem instances

<span id="page-8-1"></span>**Table 3** Average percent deviations from the critical-path based lower bound for J30



settings for other problem sizes. If GA settings are changed depends on the problem sizes, better results can be achieved for larger problem sizes. Overall, the GA\_N1 deviates 5.7% from the optimal solution, and the average computation time is 0.649 s while the GA\_N2 deviates 5.1% from the optimal solution, and the average computation time is 1.004 s. The GA\_N2 outperforms the GA\_N1 in terms of makespan. However, the GA\_N1 outperforms the GA\_N2 in terms of computation time. This is a tradeoff between solution quality and the time response to the users that a manager needs to consider. Table [2](#page-8-0) shows that the proposed GA can generate good quality solutions quickly, even in large problem instances.

#### **Comparison with other algorithms**

Next, we compare the performance of the GA\_N2 developed in this work with the existing algorithms. We also compare it with benchmark problem instances taken from PSPLIB. We have selected the test sets J30, J60, and J120. Sets J30 and J60 consist of 480 instances. Set J120 consists of 600 instances. The effectiveness of the algorithm proposed is compared with a number of state-of-the-art algorithms for the RCPSP. In order to provide a basis for the comparison, the number of generated and evaluated schedules, has been fixed to 1000 and 5000. Tables [3,](#page-8-1) [4,](#page-9-0) [5](#page-9-1) display the results obtained from our GA and other tested algorithms. In these tables, we present the type of algorithms, the reference of each heuristic and the average percent deviations from the critical-path based lower bound (from the optimal solution for J30 instances) for 1000 and 5000 schedules, respectively. In each table, the algorithms are sorted according to descending performance, with respect to 1000 schedules. Table [3](#page-8-1) summarizes the average percentage deviations from the optimal solution for the instance set J30. The average deviation of the proposed GA from the optimal solution is 0.64 and 0.56% for 1000 and 5000 schedules, respectively. Tables [4,](#page-9-0) [5](#page-9-1) summarized the average percentage deviations from the critical-path based lower bound for the instance sets J60 and J120, respectively. The average deviation of the proposed GA from the criticalpath based lower bound is 12.73 and 12.38% for 1000 and 5000 schedules for J60 set. The average deviations are 41.2 <span id="page-9-0"></span>**Table 4** Average percent deviations from the critical-path based lower bound for J60



<span id="page-9-1"></span>**Table 5** Average percent deviations from the critical-path based lower bound for J120



and 39.52% for 1000 and 5000 schedules for J120 set. These results are competitive with other techniques used in the literature.

# **Results for computing resources allocation in a cloud manufacturing system**

As mentioned above, for a given RCPSP, graphs are used and the successors and predecessors of each node are recorded by adjacent lists. Since many tasks are submitted to a resource for service and the resource is needed to handle the tasks sequentially, we vary the task durations to reflect the situation of resource allocation in cloud manufacturing. The duration of each task is randomly generated from uniform distribution  $[0.5p_j, 2.0p_j]$ . Moreover, we vary the level of parameters to see how they influence the performance of the GA. Instead of comparing all combinations of parameter settings individually, we fix all parameters and change the level of a parameter in one setting at a time. For example, the second row of Table [6](#page-10-1) shows the results of a changing

<span id="page-10-1"></span>

<sup>a</sup> Deviation is calculated by (average makespan- standard setting of GA\_N1)/standard setting of GA\_N1

crossover rate to 0.4, and all the other parameters are kept the same, as defined in Sect. [4.1](#page-3-2) under Parameterization. For each parameter settings, 20 instances have been generated and tested. Table [2](#page-8-0) shows that the GA has a larger deviation from the optimal solution for projects with 120 tasks. We fix problem size to 120 tasks instances since it is more challenging.

<span id="page-10-0"></span>Table [6](#page-10-1) demonstrates the computational results for computing resources allocation in a cloud manufacturing system with different parameter settings of the GA. If we use the parameter settings defined in Sect. [4.1](#page-3-2) under Parameterization, the average makespan obtained is 130.65 for the GA\_N1. We called it standard setting of the GA\_N1. We use it as a benchmark to evaluate the performance of each parameter setting by calculating (average makespan- standard setting of the GA\_N1)/standard setting of the GA\_N1 that is listed under the deviation column. In the deviation column, a positive value represents that the corresponding settings of GA has found solutions that are worse than the standard setting of GA\_N1's solutions (130.65). A negative value represents that the corresponding settings of the GA has found solutions that are better than the standard setting of the GA\_N1's solutions. It is obvious that in all cases GA\_N2 performs equal to or better than GA\_N1 when solution quality is concerned. However, the mangers might prefer GA\_N1 since computation time is an important factor in cloud manufacturing for fast response to customer request. Except for the number of generation, the results show that all parameters have influences on the performance of the GA. The mutation rate, population size, local search level, and number of best local search have significant influences on the performance of the GA. Increasing mutation rate, population size, local search level, or number of best local search can lead to a smaller makespan with the effect of increasing computation time. When local search level (number of best local search) set to 0, it means that local search has been disabled. Both the GA\_N1 and GA\_N2 perform poorly when local search has not been implemented. Among all the settings, the GA\_N2 performs the best when population size is set to 150 and the average computation time for it is 4.26 s. When both local search level and number of best local search set to 5, the computation time for GA\_N2 is the longest.

#### **Conclusions and future works**

Fast optimal allocation of computing resources is one of the most important problems in cloud manufacturing. In this study, a GA-based algorithm has been proposed to solve the problem of computing resource allocation in a cloud manufacturing system. We focus on the computation time which is an important factor in cloud manufacturing for fast response to customer request. Experiments demonstrate the effectiveness of the proposed GA, and show GA's high performance for solving optimally allocated computing resources in the cloud manufacturing system. To further improve the performance of the GA, a full design of experiment should be done for different problem sizes.

Due to the complex characteristics, determining how to find a feasible solution that can satisfy all users' demands with the minimum resources utilization in a short time is the most important matter in resource management in cloud manufacturing system. Hence, future works can study on designing more efficient algorithms that minimize makespan and resources utilization simultaneously.

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