

# CONWIP based control of a lamp assembly production line

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**Abstract** Efficient and effective production control systems are very important for manufacturing plants. CONWIP, one of these production control systems, has a high potential of becoming the best one available because it suits a variety of production environments and is easy to implement. In the following paper, we compare the single-loop and multi-loop CONWIP production control systems for an actual lamp assembly production line producing different kinds of products with discrete distribution processing time and demand. A model is formulated with respect to total cost and service level. A novel rule-based genetic algorithm (GA) approach is proposed for the multi-loop CONWIP system to find the optimum parameter setting. The results have shown that the single-loop CONWIP production control system is more efficient than the multi-loop system. It can greatly decrease the total cost and the WIP (Work-In-Process) with zero shortage probability.

**Keywords** Production control system · Single-loop CONWIP · Multi-loop CONWIP · Simulation · Genetic algorithm

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## Introduction

Production control is so important in manufacturing that it attracts the attention of both researchers and practitioners. In these decades, production control systems are introduced to produce the right parts, at the right time and at a competitive price. They are usually divided into two types: the push and the pull systems (Spearman, Woodruff, & Hopp, 1990). The push systems, such as MRP and its successor MRP II, schedule releases based on the forecast value of lead time, while the pull systems, such as kanban (Sugimori, Kusunoki, Cho, & Uchikawa, 1977), generic kanban (Chang & Yih, 1994) and CONWIP (Spearman et al., 1990) authorize releases based on the rate at which the products have been consumed (Gstettner & Kuhn, 1996; Hopp & Roof, 1998; Kimura & Terada, 1981; Venkatesh, Zhou, Kaighobadi, & Caudill, 1996). The pull systems control the WIP (Work-In-Process) directly, and hence minimize it to facilitate quick responses to changes in demand and production fluctuations. The advantages of pull over push are observability, efficiency, variability, and robustness. All are discussed by researchers (Hopp & Spearman, 1996; Spearman & Zazanis, 1992; Spearman et al., 1990) and supported by firms that have successfully used the pull systems (Hopp & Roof, 1998).

Dr. Taichi Ohno, a manager of Toyota Motors, in order to limit the inventory level at each production stage, developed the kanban control mechanism utilizing a cards based system. The card number of each stage is predetermined so that the WIP is controlled effectively. Due to its efficiency, there is an immense literature about kanban, e.g. the survey papers from Berkley (1992), Price, Gravel, and Nsakanda (1994), Huang and Kusiak (1996) et al. There are many forms

of kanban mechanism such as generic kanban (Chang & Yih, 1994) and extended kanban (Dallery & Liberopoulos, 1995). Some manufacturers, especially Japanese firms, have also successfully used Kanban. However, as it was pointed by Hall (1981), “Kanban is intrinsically a system for repetitive manufacturing.” In order to take into consideration the characteristics of a more complex environment, CONWIP (Spearman et al., 1990) was proposed.

In the CONWIP control mechanism, cards assigned to the whole production line control the WIP. The product can be pulled into the production line when the WIP is smaller than the predetermined card number and then be pushed between machines till the end of the production line. The main difference between CONWIP and kanban system is: CONWIP pulls products into the initial machines of the production line and then pushes them between machines, while kanban pulls products at each machine. Therefore, CONWIP is applicable to a wider variety of production environments and is inherently simpler than kanban (Spearman et al., 1990). Furthermore, it has demonstrated an excellent performance when compared to other types of pull systems (Hopp & Spearman, 1996; Spearman & Zazanis, 1992; Spearman et al., 1990). Nowadays, CONWIP has become the focus of many researchers, including the comparison between CONWIP and other production control systems (Bonvik, Couch, & Gershwin, 1997; Huang, Wang, & Ip, 1998; Muckstadt & Tayur, 1995a, 1995b; Roderick, Toland, & Rodriguez, 1994; Spearman, 1992; Spearman et al., 1990; Spearman & Zazanis, 1992), performance analysis (Ayhan & Wortman, 1999; Duenyas, Hopp, & Spearman, 1993; Duri, Frein, & Lee, 2000; Hopp & Spearman, 1991), generation of the order of backlog list (Golany, Dar-El, & Zeev, 1999; Herer & Masin, 1997; Lee & Chen, 1997; Luh, Zhou, & Tomastik, 2000), and determination of the card number (Golany et al., 1999; Hopp & Roof, 1998).

Little attention has yet been devoted to the assembly line. Duenyas (1994) started to study the problem of estimating the throughput of a cyclic assembly system with general processing time distributions. Closed queueing network approximation is used in this method. Ayhan and Wortman (1999) proposed an approximation for computing the throughput of a closed assembly-type queueing networks by using Markovian analysis. However, they only addressed single-loop CONWIP but not multi-loop CONWIP. Also, none of these researches considered different kinds of products as well as discrete distribution processing time and demands of products, which might be faced in actual production situations. The aim of this paper is to compare single-loop and multi-loop CONWIP with respect of service level and

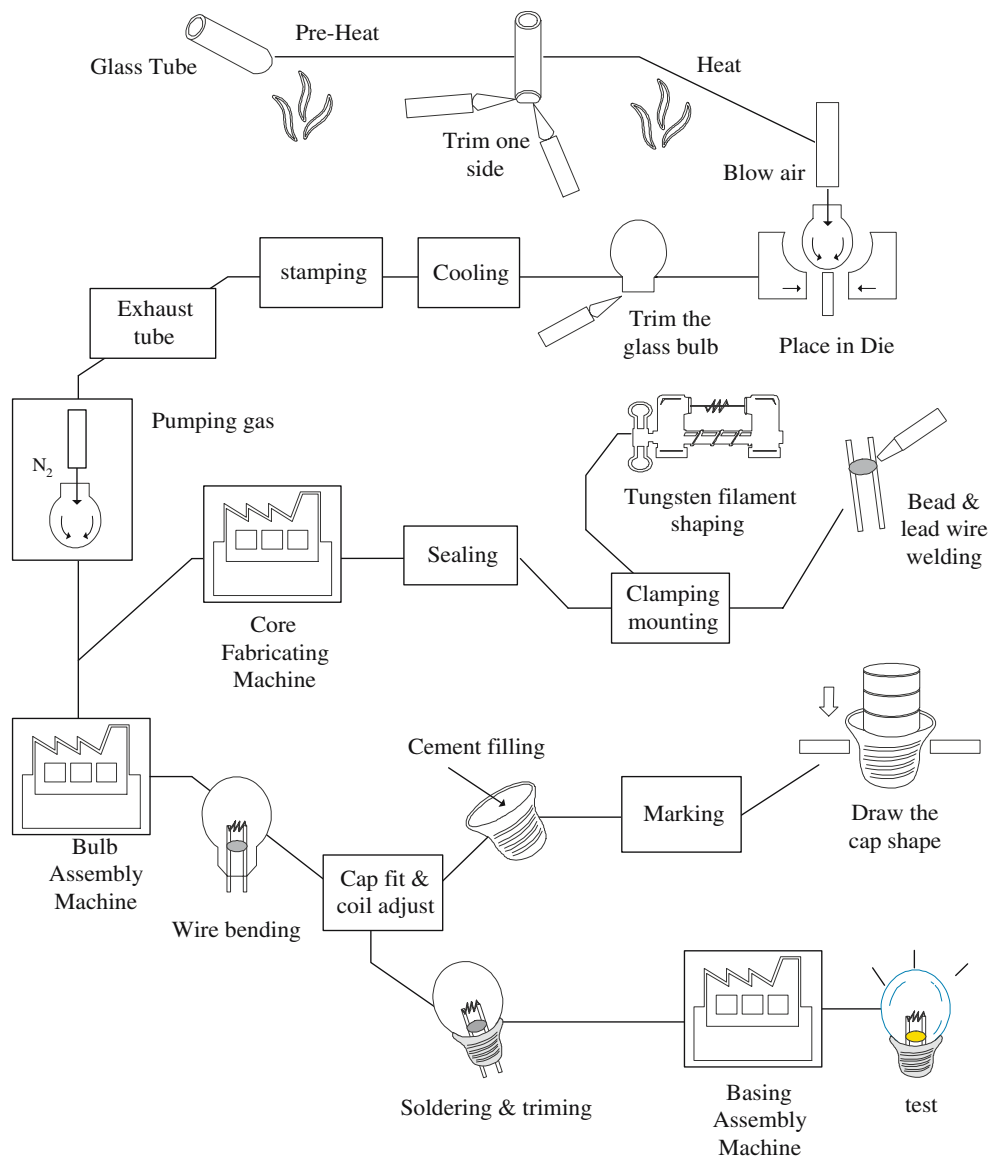
WIP for an actual lamp assembly line that produces different kinds of products with discrete distribution processing time and demands. A novel rule-based genetic algorithm (GA) approach is proposed for the multi-loop CONWIP system aimed at finding the optimum parameter setting where a rule is proposed in order to modify the card number of the loop in the evaluation process of genetic algorithm according to the throughput rate of corresponding loop and the demand rate. These characteristics reflect an actual production situation we met in a lamp company. This study was motivated by the request of a lamp producing company to improve the control on the cost of the assembly line while maintaining high service level performance.

In the following two sections, we describe the background of the lamp company and the control mechanism of both single-loop and multi-loop CONWIP of the production line. The model formulation and approaches for finding the optimum parameter configuration of both control systems are introduced in section “Parameters setting of the CONWIP systems.” The comparison between the single-loop and multi-loop CONWIP system can be found in section “Comparison between the single-loop and multi-loop CONWIP system” while the final section contains the conclusions.

### The background of the lamp company

The lamp company has manufactured miniature and subminiature lamps for about 40 years. The assembly line is a flexible one (Fig. 1). A glass tube is preheated and blown to form a glass bulb. A glass bead, a filament and a lead wire are joined to form a core. Then, an aluminum sheet is drawn out to form a cap-shaped base. Finally, the glass bulb, the core and the base are assembled to form a light bulb.

More than 100 kinds of products are produced by this assembly line. Some of them are: Bicycle Lamp, Energy Saving Lamp, Radio Panel Lamp, Toy Lamp, Pen Torch Lamp, Flashing Lamp, Pre-focusing Radio Panel Lamp, etc. The shape of the light bulb and the method employed classify these products. Three different shapes of bulbs—pear shaped, round or conical shaped, tube shaped—are produced by this manufacturer. Therefore, all products are grouped into three families. In the following part of this paper, we use the word “product” to substitute for the word “family.” The processing times (Tables 1, 2, 3) and the demands per day (Fig. 2) of the products are taken directly from the statistical data of the company and assumed to be a discrete distribution. The basic raw materials used are



**Fig. 1** The lamp assembly line

Boron lead wire, glass rods, glass tubing, electrical wiring and aluminum sheet. The assembly line works 24 h a day. The holding cost of the different products in the assembly line buffer is shown in Table 4, while the shortage cost of the products is shown in Table 5. The relationship between the machines number and the production machines is shown in Table 6.

The lamp company in an effort to improve the control on the cost of the assembly line while maintaining high service level performance considered employing the single-loop and multi-loop CONWIP systems.

**The single-loop and multi-loop CONWIP systems**

The single-loop and multi-loop CONWIP can be distinguished according to the time at which information

about demand at the final buffer is forwarded, and the path that the information takes. In both systems, information about demand at the final buffer is forwarded by means of a card immediately after the demand has occurred. However, the path that the information will take differs from one system to another.

The single-loop CONWIP contains only a single loop. When a product in the final buffer of the production line is consumed, the card is detached from the product. The free card then returns to the initial machine of the system where it joins a queue of cards waiting for subsequent parts to be processed. The single-loop CONWIP for the lamp production line is shown in Fig. 3.

The multi-loop CONWIP contains several loops, each one corresponding to a production or assembly line. When a product in the final buffer of a loop is consumed

**Table 1** Processing time and its probability of product 1

Probability (%)		Processing time (seconds)									
		31	32	33	34	35	36	37	38	39	40
Machine	1	20	25	30	25						
	2		30	15	30		25				
	3		10	25	25	15			25		
	4			30	30	15	25				
	5					10	25	25	15	25	
	6			20	25	30		25			
	7		30	15	30		25				
	8		10	25	25	15			25		
	9			30	30	15	25				
	10					10	25	25	15	25	
	11		25	30		25		20			
	12		30	15	30		25				
	13		10	25	25	15				25	
	14			30	30	15	25				
	15					10	25	25	15	25	
	16	20		30		27		23			
	17		34	15	26		25				
	18		10	25	29	15			21		
	19			30	30	22	18				
	20					10	26	30	15		19
	21		28	25	30		17				

**Table 2** Processing time and its probability of product 2

Probability (%)		Processing time (seconds)									
		31	32	33	34	35	36	37	38	39	40
Machine	1		10	24	26	15			25		
	2			30	24	21	25				
	3					10	25	25	22	18	
	4		25	29		25		21			
	5		30	21	24		25				
	6		10	25	25	14			26		
	7			30	22	23	25				
	8					10	25	27	15	23	
	9	20	25	30		25					
	10		26	17	28		29				
	11		25	30		25		20			
	12		25	30	23		22				
	13		22	23	30		25				
	14		10	25	25	14			26		
	15			20	30	29	21				
	16					10	25	19	21	25	
	17	21	25			25		29			
	18		30	19	26		25				
	19		10	27	23	15			25		
	20			30	28	17	25				
	21					10	23	21	17	29	

by its downstream machine or demand, the card is detached from the product. The free card then returns to the initial machine of the loop where it joins a queue of cards waiting for subsequent parts to be processed. The multi-loop CONWIP for the lamp production line is shown in Fig. 4.

As the comparison of the two CONWIP systems must take place while the two systems are running on optimal

parameters setting, next section presents the methods employed in setting those parameters.

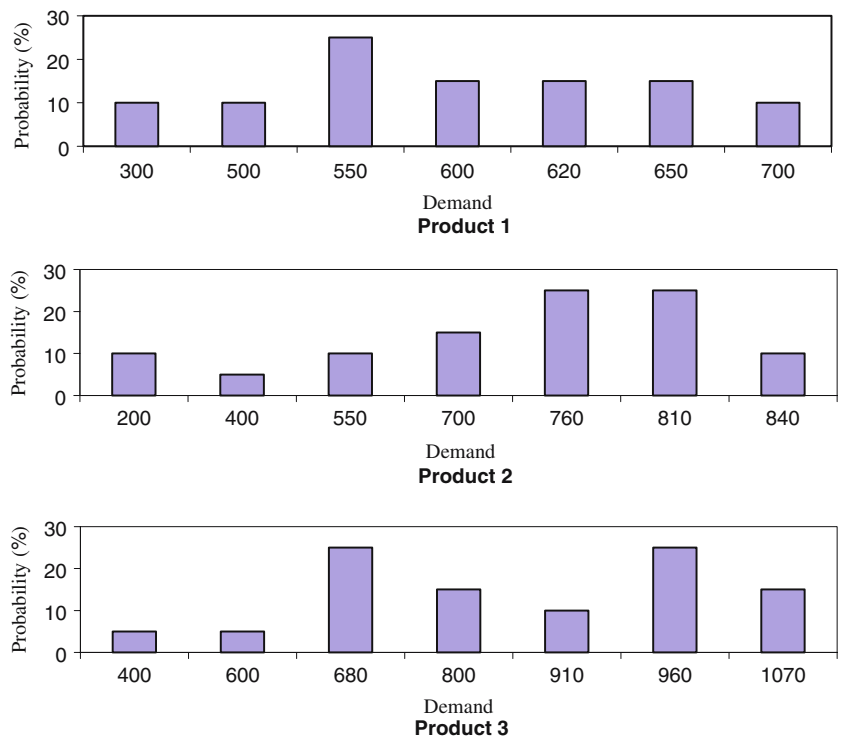
#### Parameters setting of the CONWIP systems

The main parameters for the single-loop and the multi-loop CONWIP systems are the cards. For a

**Table 3** Processing time and its probability of product 3

Probability (%)	Processing time (seconds)									
	31	32	33	34	35	36	37	38	39	40
Machine 1					10	27	28	12	23	
2	22	25	28		25					
3		26	19	29		26				
4		10	23	28	17			22		
5			30	22	23	25				
6					10	28	22	18	22	
7		25	23		25	27				
8		27	18	27		28				
9			28		25		22			25
10		25	27	25		23				
11		22	26		28		24			
12		23	22	27		28				
13		10	25	28	15			27		
14			30	30	15	25				
15		16	25	25	15			19		
16			27	29	18	26				
17	28	23	22		27					
18		27	18	30		25				
19		16	25	19	15			25		
20			23	29	22	26				
21					17	25	18	15	25	

**Fig. 2** The probability distribution of the different products



quantitative comparison between them, approaches that enable the parameters setting of the systems with respect to the goal of the lamp company are needed. An optimization model and methods are proposed in this section.

**Optimization model**

The aim of the production control of the lamp company is to ensure the service level while minimizing the total

**Table 4** The holding cost of different workcenters

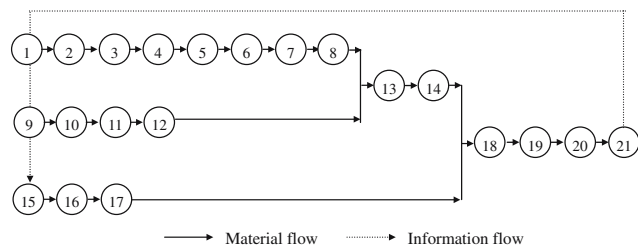
Workcenter	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
Holding cost	5	5	6	6	6	7	8	8	3	3	4	4	15	15	4	4	4	20	20	20	20

**Table 5** The shortage cost of different products

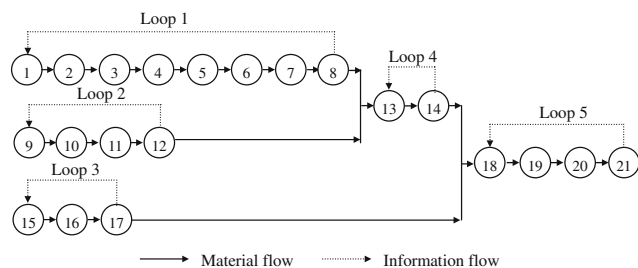
Product	1	2	3
Shortage cost	10	16	8

**Table 6** The workcenters and their numbers

Number	Workcenter
1	Pre-heat
2	Trim one side
3	Heat
4	Blow air and place in Die
5	Trim the glass bulb
6	Cooling
7	Stamping & exhaust tube
8	Pumping gas
9	Bead & lead wire welding
10	Clamping mounting
11	Sealing
12	Core fabricating machine
13	Bulb assembly machine
14	Wire bending
15	Draw the cap shape
16	Marking
17	Cement filling
18	Cap fit & coil adjust
19	Soldering & trimming
20	Basing assembly machine
21	Test



**Fig. 3** The single-loop CONWIP for the lamp assembly line



**Fig. 4** The multi-loop CONWIP for the lamp assembly line

cost of the production process. This is formulated as follows:

$$\min TC(K) \tag{1}$$

$$\text{s.t. } SP(K) \leq b \tag{2}$$

$$k_l \geq 1 \text{ with } l \text{ an integer } l = 1, 2, \dots, L \tag{3}$$

where  $K = (k_1, k_2, \dots, k_L)$  is the cards distribution,  $k_l (l = 1, 2, \dots, L)$  is the card number in the  $l$ th loop of the CONWIP system.  $L$  is the number of loop,  $TC(K)$  is the total cost of the production process,  $SP(K)$  is the shortage probability of the production process,  $b$  is the up bound of the shortage probability.

It can be observed that  $TC(K)$  and  $SP(K)$  are the performance measures of the production line under the setting of cards in the control systems. Therefore, approaches, which enable the modeling of the assembly line with respect to the different control systems and parameter setting, are needed. Although there are some analytical methods proposed for the CONWIP (Bonvik et al., 1997; Bonvik, Dallery, & Gershwin, 2000; Di Mascolo, Frein, & Dalley, 1996; Duenyas 1994; Duenyas & Hopp, 1992a, 1992b), they mainly focus on the single-loop or the multi-loop CONWIP in serial. Therefore, simulation is used here. By simulation, the two performance measures are calculated as follows:

- (1) The total cost,  $TC(K)$ , is composed of the inventory holding cost and the shortage cost of final machine  $n$ . That is:

$$TC = \frac{1}{T} \sum_{t=1}^T \left[ \sum_{j=1}^n \left( IC_j * \sum_{i=1}^m \max \{0, I_{ij}(t)\} \right) + \sum_{i=1}^m (SC_i * \max \{0, -I_{in}(t)\}) \right] \tag{4}$$

where  $n$  is the number of machines,  $m$  is the number of products,  $IC_j$  denotes the unit holding cost of machine  $j$ ,  $SC_i$  denotes the shortage cost of product  $i$ ,  $T$  is the statistic time,  $I_{ij}(t)$  is the inventory of product  $i$  at machine  $j$  in period  $t$ . As the cost of production is independent of the strategy, it is not considered here. The inventory

of finished product  $I_{in}(t)$  can be negative which means that product  $i$  is in short supply.

- (2) Shortage probability,  $SP(K)$ , is measured by the average shortage probability of the demands per unit time.

$$SP = \frac{1}{T} \sum_{t=1}^T \sum_{i=1}^m \frac{\max\{0, -I_{in}(t)\}}{D_i(t)} \tag{5}$$

where  $D_i(t)$  is the demand of product  $i$  in period  $t$ .

**Parameter setting of the single-loop CONWIP system**

For the single-loop CONWIP, the optimum number of cards is determined by enumerating different card number and reading curves of card numbers versus work in process  $WIP(K)$  and  $SP(K)$ .  $WIP(K)$  can also be obtained by simulation:

$$WIP = \frac{1}{T} \sum_{t=1}^T WIP_t \tag{6}$$

On the curve, at the point where  $SP(K)$  reaches the up bound of the short probability, the card number is the optimal one. As when the card number is over this point, the  $SP$  reaches the up bound of the short probability and any additional card only results in higher  $WIP(K)$ .

**Parameters setting of the multi-loop CONWIP system**

For the multi-loop CONWIP, the problem is a combination one and has large search space. The heuristic GA approach is suitable for this kind of problems. Ettl and Schwehm (1994) have presented a GA for optimizing the network partition and kanban allocation. However, their method is for the sequence of workstation. So, a novel rule-based GA approach is brought forth specifically for our problem.

In designing a GA, it is necessary to specify the chromosome description, a fitness function, the initial generation generating method, some genetic operators, a selection strategy, and an ending criterion (Holland, 1975; Michalewicz, 1996; Ostermark, 1999). Considering the characteristics of our problem, a rule is proposed in order to modify the card number of the loops in the evaluation process of genetic algorithm based on the knowledge of production line and demand rate.

*The chromosome description of the GA*

For our GA, the natural number string is selected as the gene description. Let  $K = [k_1, k_2, \dots, k_L]$ , where

$k_l$  is an integer between 1 and  $k_l^u (l = 1, 2, \dots, L)$ .  $k_l^u$  is the up bound of the card number of the loop  $l$ . This stands for the card number of  $k_l$  used for loop  $l$ . Thus,  $K = [k_1, k_2, \dots, k_L]$  refers to a card distribution of the multi-loop CONWIP and represents a chromosome or an individual in the GA. For example, a natural number string of 5 bits:

[5 2 6 5 3]

is a card distribution or a chromosome of a multi-loop CONWIP with 5 loops. This means 5 cards for loop 1, 2 cards for loop 2, and so on.

The up bound of the card number of loop  $l$  is determined by setting the card number of each loop as the same value and enumerating different values. For each value,  $SP(k)$  is recorded. When  $SP(k)$  reaches the pre-determined short probability, the corresponding value is recorded. Then the up bound of the card number of each loop is set to two times this value.

*Fitness function*

For the previous problem, the objective is a minimum one. So it is transferred to the fitness function as follows:

$$F = TC_{\max}(K) - TC(K) + a \tag{7}$$

where  $TC_{\max}(K)$  is the maximum of  $TC(K)$  in the current generation;  $a$  is the adjustment coefficient

*The initial population and ending criterion of the GA*

In order to generate the initial generation, the following INI procedure is introduced for each chromosome:

**Procedure INI:**

- Step 1:  $l=0$ , go to Step 2;
- Step 2:  $l = l + 1$ , if  $l > L$ , record the chromosome and stop; otherwise generate a random variable  $r$  within the interval of  $[0, 1]$ , let  $k = 0$ , go to Step 3;
- Step 3:  $k = k + 1$ , go to Step 4;
- Step 4: if  $k/k_l^u \geq r$ , then let  $k_l = k$  go to Step 2; otherwise, go to step 3;

From the INI procedure, we can see that the initial generation is a legal one, as the partners are selected within the up bound of cards.

The maximum generation is used as an ending criterion.

*The selection in the GA*

Among many selection techniques, the “roulette wheel approach,” one of the fitness-proportional selections, (Michalewicz, 1996) is adopted here.

Moreover, “elitist strategy” (Goldberg, 1989), which preserves the best chromosome in the next generation and overcomes the stochastic errors of sampling, is used too. In the elitist selection, if the best individual in the previous generation is not reproduced in the new generation, it will remove one individual randomly from the new population and add the best one of the previous population onto the new population.

*The genetic operators in the GA*

The one-cut-point crossover and the altering mutation are used as the genetic operators in the GA. The first operator is used to exchange two different sections of the two selected parents to produce two children; and the second operator is used to randomly select a bit and alter its gene value within the up bound (Gen & Cheng, 1996). It is evident that all chromosomes can remain legal when the genetic operations of the above crossover and mutation are implemented. However, they may be infeasible. Hence, the adjusting rule for the infeasible chromosomes is proposed in section “The adjusting rule for the infeasible chromosomes.”

*The adjusting rule for the infeasible chromosomes*

In the evaluation process of genetic algorithm, as the solution may not satisfy the constraint, an adjustment is needed for this kind of chromosome. The adjusting rule is

**Rule:** If  $SP(K) > b$ , then

$$k'_l = k_l + (k'_l - k_l) * \left( \frac{dd - \theta_l}{dd} \right) \tag{8}$$

where  $k'_l$  is the card number of loop  $l$  after adjusting,  $\theta_l$  is the throughput rate of loop  $l$ ,  $dd$  is the demand rate:

$$dd = \sum_{i=1}^m \sum_{w \in D_i} w * p_i(w) \tag{9}$$

where  $D_i = \{D_{i1}, D_{i2}, \dots, D_{ih}\}$  and is the set of possible demands of product  $i$ ,  $p_i(w)$  is the probability that the demand of product  $i$  is equal to  $w$ .

It can be seen that the card number of the loops is modified in the evaluation process of genetic algorithm based on the knowledge of production lines and demand rates in the rule.

*The steps for the GA*

The step-by-step procedure for the GA is:

- Step 1: Specify the parameters: population sizes NP, the maximum number of generations NG, crossover probability  $p_c$  and mutation probability  $p_m$ .
- Step 2: Generate an initial population with NP chromosomes by Procedure INI:  $K(q) = (k_1(q), k_2(q), \dots, k_L(q))$ ,  $q = 1, 2, \dots, NP$ . Set the generation index  $u = 0$ , initial optimal solution  $K^* = K_v$ , where  $K_v = [1, 1 \dots 1]$  and the optimal fitness function value  $F^* = 0$ .
- Step 3: Let  $u = u + 1$ . If  $u > NG$ , go to step 8, otherwise, implement Steps 4 to 7.
- Step 4: For chromosome  $K(q)$ ,  $q = 1, 2, \dots, NP$ , implement the following three sub steps:
  - Substep 4.1: Call the simulation procedure for calculating the statistical values and return the values of  $TC(k_1(q), k_2(q), \dots, k_L(q))$  and  $SP(k_1(q), k_2(q), \dots, k_L(q))$ .
  - Substep 4.2: Call the rule to adjust the infeasible chromosome, calculate and return the fitness function value  $F(q)$ .
  - Substep 4.3: Find  $F_{\min} = \min\{F(q), q = 1, 2, \dots, NP\}$  and  $F_{\max} = \max\{F(q), q = 1, 2, \dots, NP\}$ .  $q^* = \arg\{F(q) = F_{\max}\}$  are the indices of achieving  $F_{\max}$  and the associate card distribution.
- Step 5: If  $F_{\max} > F^*$ , let  $F^* = F_{\max}$  and  $K^* = K(q^*)$
- Step 6: For  $q = 1, 2, \dots, NP$ , calculate the selection probability  $pp_q = F(q) / q \sum_{q=1}^{NP} F(q)$ .
- Step 7: To generate a new population, use the selection probabilities  $pp_q$ ,  $q = 1, 2, \dots, NP$ , to select  $NP_c = p_c \times NP$  chromosomes for one-point crossover,  $NP_m = p_m \times NP$  chromosomes for altering mutation. Go to Step 3.
- Step 8: Output  $F^*$  and  $K^*$  as the optimal solution.

Note that Step 1 initializes the algorithm. Step 2 is used to generate the initial population of the GA. Steps 3–7 are the backbone of the GA. Step 3 checks the stop criterion. Step 4 is the nuclear step of the algorithm. It firstly calls the simulation procedure to calculate the statistical values for a given chromosome in Substep 4.1 and then calls the rule to adjust the infeasible chromosome and calculate the fitness function values in Substep 4.2.



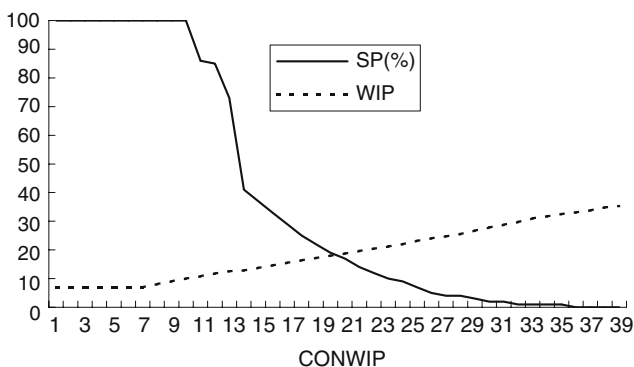
Finally, it obtains the minimum and maximum values of this generation. Step 5 updates the optimum. Step 6 calculates the selection probability. Step 7 is used to calculate the genetic operations. The final step, Step 8, is used to determine the solution.

**Comparison between the single-loop and multi-loop CONWIP system**

In this section, the comparison between the single-loop and multi-loop CONWIP production control systems for the lamp assembly line is summarized. The up bound of the shortage probability *b* is set to be 0.

To optimize the number of cards in the single-loop CONWIP system, various card numbers are enumerated in order to obtain the resultant WIP and SP for corresponding card number. The curves of card numbers versus WIP and SP were plotted as shown in Fig. 5. It is obviously shown that when the card number increases, the WIP also increases while the SP decreases. However, when the card number is over 37, the SP reaches zero and any additional card only results in higher WIP. Thus, 37 is used as the rational number of cards for the CONWIP control system.

The optimum card numbers and allocation in the multi-loop CONWIP system are obtained by using the rule-based GA approach introduced in section “Parameters setting of the multi-loop CONWIP system.” The parameters for the rule-based GA are set as follows: population size  $NP = 50$ ; crossover probability  $p_c = 0.5$ ; mutation probability  $p_m = 0.04$ ; maximum number of generation  $NG = 100$ . Under these parameters for rule-based GA, the “Best Rate” of the algorithm is 100% and the rational card numbers and allocations are obtained (see Table 7). Here, the “Best” stand for the best one of the objective values achieved in 100 runs. The “Best Rate” is the rate that reaches the best value.



**Fig. 5** Determine the card numbers in single-loop CONWIP

**Table 7** Card numbers for the multi-loop CONWIP system

Loop	1	2	3	4	5
Card number	5	2	9	1	5

**Table 8** The comparison of the single-loop and multi-loop CONWIP system for the lamp assembly line

Control system	TC	SP (%)	WIP
Single-loop CONWIP	135.29	0	33.07
Multi-loop CONWIP	152.15	0	34.71

Then we compare different control strategies under the rational card number by simulation. The three performance measures TC, SP, and WIP are recorded for each system. Table 8 demonstrates that the single-loop CONWIP system has a lower TC and WIP, when both systems reach the zero SP. Also, the single-loop CONWIP system is inherently simpler to implement and control. It is an effective system for the lamp assembly production line.

**Conclusion**

In this paper we compared the single and multi-loop CONWIP production control systems for an actual lamp assembly production line that produces a series of products with discrete distribution processing time and demand, a situation that differs from that of other current researches. In order to accomplish this, a model was formulated with respect to total cost and service level. A novel rule-based GA approach was proposed for the multi-loop CONWIP system in order to find the optimum parameter setting.

The model presented here can be easily extended to other production lines with the same control objectives and the rule-based GA approach is potential for this kind of problem. The only thing that needs to change is the analysis model of the production line by which the parameters in the objectives and constraints are obtained.

In conclusion, the results have clearly illustrated that the single-loop CONWIP offers better performances than the multi-loop CONWIP for the lamp assembly production line with respect to total cost and service level. The total cost is lower and the demand service level is guaranteed in the single-loop CONWIP. Therefore, the single-loop CONWIP is a more effective production control system for the lamp assembly production line.

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## References

- Ayhan, H., & Wortman, M. A. (1999). Approximation for computing the throughput of closed assembly-type queueing networks. *European Journal of Operational Research*, *112*(1), 107–121.
- Berkley, B. J. (1992). A review of the kanban production control research literature. *Production and Operations Management*, *1*(3), 393–411.
- Bonvik, A. M., Couch, C. E., & Gershwin, S. B. (1997). Comparison of production-line control mechanisms. *International Journal of Production Research*, *35*, 789–804.
- Bonvik, A. M., Dallery, Y., & Gershwin, S. B. (2000). Approximate analysis of production systems operated by a CONWIP/finite buffer hybrid control policy. *International Journal of Production Research*, *38*, 2845–2869.
- Chang, T. M., & Yih, Y. (1994). Generic kanban systems for dynamic environments. *International Journal of Production Research*, *32*, 889–902.
- Dallery, Y., & Liberopoulos, G. (1995). A new Kanban-type pull control mechanism for multi-stage manufacturing systems. *Proceedings of the 3rd European Control Conference*, Rome, September 5–8, *4*(2), 3543–3548.
- Di Mascolo, M., Frein, Y., & Dalley, Y. (1996). An analytical method for performance evaluation of kanban controlled production systems. *Operations Research*, *44*, 50–64.
- Duenyas, I. (1994). Estimating the throughput of a cyclic assembly system. *International Journal of Production Research*, *32*(6), 1403–1419.
- Duenyas, I., & Hopp, W. J. (1992a). Estimating the throughput of an exponential CONWIP Assembly system. *Queueing Systems: Theory and Applications*, *14*, 135–157.
- Duenyas, I., & Hopp, W. J. (1992b). CONWIP assembly with deterministic process and random outages. *IIE Transactions*, *24*(3), 97.
- Duenyas, I., Hopp, W. J., & Spearman, M. L. (1993). Characterizing the output process of a CONWIP line with deterministic processing and random outages. *Management Science*, *39*(6), 975–988.
- Duri, C., Frein, Y., & Lee, H.-S. (2000). Performance evaluation and design of a CONWIP system with inspections. *International Journal of Production Economics*, *64*(1), 219–229.
- Ettl, M., & Schwehm, M. (1994). A design methodology for Kanban-controlled production lines using queueing networks and genetic algorithms. *Proceedings of tenth international conference on systems engineering, ICSE'94 in Coventry*, UK, Coventry University Press, pp. 307–314.
- Gen, M., & Cheng, R. (1996). *Genetic algorithms and engineering design*. New York: John Wiley & Son Press.
- Golany, B., Dar-El, E. M., & Zeev, N. (1999). Controlling shop floor operations in a multi-family, multi-cell manufacturing environment through constant work-in-process. *IIE Transactions*, *31*(8), 771–781.
- Goldberg, D. E. (1989). *Genetic algorithm in search, optimization & Machine learning*. Reading, MA: Addison-Wesley.
- Gstettner, S., & Kuhn, H. (1996). Analysis of production control systems kanban and CONWIP. *International Journal of Production Research*, *34*, 3253–3273.
- Hall, W. R. (1981). *Driving the productivity machine: production planning and control in Japan*. Falls Church, Virginia: American Production and Inventory Control Society.
- Herer, Y. T., & Masin, M. (1997). Mathematical programming formulation of CONWIP based production lines; and relationships to MRP. *International Journal of Production Research*, *35*(4), 1067–1076.
- Holland, J. H. (1975). *Adaptation in natural and artificial systems*. Ann Arbor: University of Michigan.
- Hopp, W. J., & Roof, M. L. (1998). Setting WIP levels with statistical throughput control (STC) in CONWIP production lines. *International Journal of Production Research*, *36*, 867–882.
- Hopp, W. J., & Spearman, M. L. (1991). Throughput of a constant work in process manufacturing line subject to failures. *International Journal of Production Research*, *29*(3), 635–655.
- Hopp, W. J., & Spearman, M. L. (1996). *Factory physics: Foundations of manufacturing management*. Burr Ridge, IL: Irwin.
- Huang, C.-C., & Kusiak, A. (1996). Overview of Kanban system. *International Journal of Computer Integrated Manufacturing*, *9*, 169–189.
- Huang, M., Wang, D., & Ip, W. H. (1998). Simulation and comparative study of the CONWIP, kanban and MRP production control systems in a cold rolling plant. *Production Planning and Control*, *9*, 803–812.
- Kimura, O., & Terada, H. (1981). Design and analysis of push system, a method of multi-stage production controls. *International Journal of Production Research*, *19*, 26–49.
- Lee, Ch.-E., & Chen, Ch.-W. (1997). Dispatching scheme involving move control and weighted due date for wafer foundries. *IEEE Transactions on Components, Packaging, and Manufacturing Technology Part C: Manufacturing*, *20*(4), 268–277.
- Luh, P. B., Zhou, X., & Tomastik, R. N. (2000). Effective method to reduce inventory in job shops. *IEEE Transactions on Robotics and Automation*, *16*(4), 420–424.
- Michalewicz, Z. (1996). *Genetic algorithms + data structure = evolution programs* (thirded). New York: Springer-Verlag.
- Muckstadt, J. A., & Tayur, S. R. (1995a). Comparison of alternative kanban control mechanisms. I. Background and structural results. *IIE Transactions*, *27*, 140–150.
- Muckstadt, J. A., & Tayur, S. R. (1995b). Comparison of alternative kanban control mechanisms. II. Experimental results. *IIE Transactions*, *27*, 151–161.
- Ostermark, R. (1999). Solving a nonlinear non-convex trim loss problem with a genetic hybrid algorithm. *Computers & Operations Research*, *26*(6), 623–635.
- Price, W., Gravel, M., & Nsakanda, A. L. (1994). A review of optimization models of kanban-based production systems. *European Journal of Operational Research*, *75*, 1–12.
- Roderick, L. M., Toland, J., & Rodriguez, P. (1994). A simulation studies of CONWIP versus MRP at Westinghouse. *Computer Industrial Engineering*, *26*, 237–242.
- Spearman, M. L. (1992). Customer service in pull production systems. *Operations Research*, *40*, 948–958.
- Spearman, M. L., Woodruff, D. L., & Hopp, W. J. (1990). CONWIP: A pull alternative to kanban. *International Journal of Production Research*, *28*, 879–894.
- Spearman, M. L., & Zazanis, M. A. (1992). Push and pull production systems: Issue and comparison. *Operations Research*, *40*, 521–532.

Sugimori, Y., Kusunoki, K., Cho, F., & Uchikawa, S. (1977). Toyota production system and kanban system materialization of just-in-time and respect-for-human system. *International Journal of Production Research*, 15, 553–564.

Venkatesh, K., Zhou, M. C., Kaighobadi, M., & Caudill, R. (1996). A petri net approach to investigating push and pull paradigms in flexible factory automated systems. *International Journal of Production Research*, 34, 595–620.