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Behavior of Geosynthetic Reinforced Ring Footings Supported on Multilayered Soil Strata

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Abstract This study is aimed at analyzing the behavior of ring footings on layered foundation systems. The influence of layer stratification, foundation type, and subgrade strength on the behavior of ring footings was studied. Various laboratory model experiments were performed for the ring and solid circular footings on homogenous and two-layered unreinforced and reinforced foundation systems. The layered system consisted of medium dense sand $(Dr_T = 65\%)$ of varying thickness (H = 0.66 - 2.66D)overlying the subgrade (lower layer) of varying relative density ($Dr_B = 30\%$, 50%, 80%). The results show that the top layer thickness (H), subgrade relative density (Dr_B) , foundation type, and the type of geosynthetic material utilized for reinforcement viz. geogrid, and geotextile considerably influences the performance of footings. As the top layer thickness and subgrade strength increased, the improvement factors for reinforced layered foundation systems decreased due to the lack of strain mobilization for the membrane action. The maximum contribution of the geosynthetic reinforcement to the bearing pressures was witnessed for the top layer thickness of

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M. Y. Shah e-mail: yousuf@nitsri.net H=0.66D and loose subgrade system of $Dr_B=30\%$. The pressure settlement responses for all the cases indicate that the ring footing outperformed the circular footings and hence can be used as an effective and economical alternative to the conventional footings.

Keywords Ring footing · Improvement factor · Unreinforced layered strata · Reinforced layered strata

1 Introduction

The bearing capacity and settlement of a foundation depend on the footing shape, sub-soil conditions, and shear strength parameters (Hanna 1981). Many empirical equations are available in the literature to calculate the carrying capacity and settlement of circular, strip, and square footings on homogeneous and multi-layer soil strata. On the other hand, the behavior of ring foundations, which have proved to be efficient and cost-effective alternatives for axisymmetric loading conditions like silos, chimneys, storage tanks, etc. is yet to be studied extensively. Fisher (1957) was the first to investigate the behavior of ring footings. He presented a method for calculating the settlement of a ring footing in a semi-infinite elastic medium. Egorov (1965) introduced a few relations for calculating the settlements and bearing pressure for the ring footing. Bowles (1997) used the finite element method to calculate the bearing pressure and settlement of ring footings. In a series of laboratory tests on model ring footings, Ohri et al. (1997) discovered that the bearing capacity for dune sand is maximized for an internal to the external radius (r_i/r_o) ratio of 0.38. According to Hataf and Razavi (2003), the radius ratio for the maximum bearing capacity ranges from 0.2 to 0.4. They proposed a semi-empirical relation evaluating the carrying capacity of ring footings on the sand. Verma et al. (2005) investigated the model ring footing behavior subjected to vertical loads while being supported on sand beds reinforced with geocells of varied diameters and heights. Laman and Yildiz (2007) experimenaly investigated the effect of geogrid reinforcement on the ultimate bearing capacity of ring foundations supported by a sand bed.

One of the most promising techniques for increasing the load-carrying capacity of foundation soils is the utilization of soil reinforcement, which dates back to Vidal's study in (1966). The concept of soil reinforcement was advanced further with the development of geosynthetics. Binquet and Lee (1975) carried out the first investigations on the influence of soil reinforcement on the improvement of load carrying capacity, which was later followed by other researchers. Since the advent of ground improvement methods, geotechnical engineers have been very interested in improving the engineering behavior of soil. The use of geosynthetic reinforcement has greatly helped in reducing the cost required for ground improvement and has streamlined the construction processes. Adding reinforcements (such as geosynthetics, discrete fibers arranged randomly or aligned along the weak planes/zone of the soil, metal strips), densifying the weak soil up to a substantial depth, replacing the weak soil with strong soil up to a significant depth, are all ways to improve the engineering properties of soils. A number of studies (Akinmusuru and Akinboladeh 1981; Guido et al. 1986; Huang and Tatsuoka 1990; Khing et al. 1993, 1994; Das et al. 1994; Adams and Collin 1997; Shin et al. 2002; El Sawwaf 2007, 2009) have demonstrated that using soil reinforcement to improve the load settlement behavior of cohesionless soils beneath shallow foundations is an efficient and affordable technique. They used a variety of materials, including geotextiles, geogrids, and aluminum strips for soil reinforcement in their studies. The impact of these materials on the soil's carrying capacity have been examined in nearly all of these studies. The number of reinforcement layers (N), the depth of the first layer of reinforcement (u), and the vertical spacing between the layers (z) have all been varied. The carrying capacity was also examined for varying types of soil, its density, the form, and the size of the footings. The bearing capacity ratio (*BCR*), which compares the bearing capacity of reinforced soil to that of unreinforced soil, is frequently used to assess the increase in bearing capacity. When the reinforcement was inserted at the proper depth, the *BCR* for reinforced soil was found to be greater than unity.

Soils in nature exhibit inherent variability, as a result, foundations are typically built on multi-layered soil profiles. Depending on the thickness of the top layer, the influence zone of the foundation, which includes the potential failure zone, may reach a significant depth, and two or more layers within that depth will therefore have an impact on the foundation behavior. The majority of the experimental and theoretical studies available in the literature have been carried out on ring footings supported on the subsoil of uniform relative density. The influence of many factors affecting the bearing capacity of footings, such as soil layer thickness (Kumar and Walia 2006; Kumar et al 2007; Prasad and Chakraborty 2021; Nguyen et al. 2023), soil properties (Ghazavi 2008; Papadopoulou and Gazetas 2020; Das et al. 2021; Lai et al. 2022), and footing shape (Sawaaf and Nazir 2012; Sharma and Kumar 2017, 2018, 2021) has been a subject of consideration in very few experimental studies. Sawwaf and Nazir (2012) investigated the performance of eccentrically loaded small-scale ring footings on reinforced layered soil strata. They stated that the improvement in the performance of ring footing on reinforced compacted sand is significantly dependent on the relative density of the sand and the radius ratio of the ring footing. The recommended r_i/r_o (where r_i is the internal radius and r_o is the external radius) for optimum ring footing response was reported to be 0.39. The improvement in the behavior of ring footing with increasing depth of replaced top layer was reported to be significant only up to a value of $H/D_{o} = 1.5$. Also, the addition of soil reinforcement resulted in a substantial decrease in the required depth of the replaced sand layer for the same footing settlement and a significant increase in the bearing load, resulting in a cost-effective ring footing design. Sharma and Kumar (2017) studied the effect of relative density on the performance of fiber-reinforced layered soil foundations. For all the evaluated relative density combinations, the greatest increase in terms of bearing capacity and settlement reduction was observed when $r_i/r_o = 0.40$. They concluded that the improvement in bearing capacity and settlement reduction is maximized by increasing the thickness of the top layer reinforced with randomly distributed fibers. Using finite element modeling, Khatri et al. (2022) studied the behavior of ring footings on dense sand underlain by loose sand. The bearing capacity was reported to increase very significantly as the thickness of the dense sand layer increased up to a specific optimum thickness before reaching a constant value.

The majority of the experimental and numerical investigations on ring footings present in the literature were conducted to find the optimum radius ratio and bearing capacity factors for ring footings on homogeneous strata. (Egorov 1965; Haroon and Misra 1980; Al-Sanad et al. 1993; Ismael 1996; Ohri et al. 1997; Hataf and Razavi 2003; Zhao and Wang 2008; Gholami and Hosseininia 2017; Benmebarek et al. 2017). However, the behavior of geosynthetic reinforced ring foundation systems has not been explicitly studied in the context of varying subsoil configurations and subgrade strengths. The present study aims to gain a better insight into the performance of ring and solid circular foundation systems on geosynthetic reinforced two-layer strata. A number of physical tests on model footings have been performed to investigate the effect of the following parameters:

- Effect of the top layer thickness (H)
- Effect of relative density $(Dr_B = 30\%, 50\%, 80\%)$ of the lower layer
- Effect of foundation type i.e. solid circular, and ring footing with radius ratio, $r_i/r_o = 0$ and 0.4 respectively.
- Effect of reinforcement type i.e. geogrid and geotextile on the performance of both ring and solid circular footing.

2 Mechanism of Geosynthetic Reinforcement

2.1 Confinement Effect

Before loading the reinforced soil, there is no relative movement between the soil and the geosynthetic material. Relative displacement between the soil and the geosynthetic material takes place after the application of load which causes the development of friction and subsequent mobilization of tension in the reinforcement. Due to the frictional interaction and interlocking between the fill and the geosynthetic material, the additional shear stresses that would otherwise be imparted to the soft/loose lower layer (subgrade) are absorbed by the reinforcement(Hufenus et al. 2006). This improves the distribution of pressure on the subgrade, which lowers the settlement.

2.2 Pocket Effect

The pocket effect is caused by vertical deformation, which results in a concave shape in the tensioned geosynthetic material (Dash et al. 2001; Rajagopal et al. 1999). The curved reinforced material, due to its stiffness, generates an upward force that sustains the applied pressure and thus improves bearing capacity (Perkins et al. 1999). The material functions as a tensioned membrane, with the pressure on the loose lower layer/subgrade being much lesser than the pressure applied to the top layer on the upper concave side.

3 Test Materials

3.1 Sand

The present study was carried out using locally available river sand. The coefficient of curvature and coefficient of uniformity of sand were 0.76 and 3.67 respectively. The effective size (D_{10}) was 0.2 mm. The sand was classified as poorly graded (*SP*) according to the Unified Soil Classification System. The values of maximum and minimum void ratios were found to be 0.65 and 0.32 respectively. The layer stratification was achieved by varying the relative density of the lower sand layer (Dr_B =30%, 50%, 80%) and the thickness of the top layer (*H*), which was maintained at a constant relative density (Dr_T) of 65%.

3.2 Ring and Circular Footing

Footings made of mild steel plates of 25 mm thickness were utilized in the study. To achieve the radius ratio of 0.4, the external (D_o) and internal (D_i) diameters of the ring footing were kept as 150 mm and

60 mm, respectively. The external diameter of the circular footing (D), was kept the same as the diameter of the ring footing $(D=D_o)$, i.e.150 mm. A thin layer of sand was fixed to the bottom surface of the footing with epoxy glue to create the rough base condition of the footing.

3.3 Geogrid

Geogrid used for testing was supplied by M/S Strata Systems (India) Pvt. Ltd.StratagridTM. Biaxial geogrid was used as reinforcement. These high-performance geo-grids are produced from knitted polyester yarns with high molecular weight and tenacity. The physical and mechanical parameters specified by the manufacturer are listed in Table 1.

3.4 Geotextile

A non-woven geotextile was used as soil reinforcement beneath the footings. The geotextile material (needle punch, HSN Code 5603) was procured from Ganpathi Enterprises Jaipur, India. The properties of geotextile provided by the manufacturer are listed in Table 2.

4 Experimental Setup

A loading frame assembly was used to conduct model tests in a testing tank sized $1 \text{ m} \times 1 \text{ m} \times 1 \text{ m}$. The sand in the testing tank was filled using the "raining" technique. To determine the appropriate height of fall for a specific relative density, the

Table 2 Properties of geotextile

Property	Test method	Units	Value
Mass per unit area	ASTM D 5261	g/m2	≥325
Grab tensile strength	ASTM D 4632	kN/m	≥ 20
Grab elongation	ASTM D 54533	%	≥ 80
Thickness at 20 kPa	EN ISO 9863-1	mm	≥ 2

unit weights obtained were 17.02 kN/m³, 17.80 kN/ m³, 18.4 kN/m³, and 19.04 kN/m³ for the relative densities of 30%, 50%, 65%, and 80%, respectively. The sand was deposited in 100 mm thick layers. For reinforced configurations, geogrid/geotextile was positioned at the interface over which the top layer was rained. The schematic of the layer configurations is presented in Fig. 1 and the experimental setup is shown in Fig. 2. A straight piece of wood was used to level the sand's top surface while taking the necessary precautions to maintain the relative density at the top. The footings were positioned in the middle of the tank once the sand had been filled and leveled. Concentric load application was ensured by carefully aligning the loading arrangement with the centerline. A manually operated loading jack system was used to apply load on the footings. Two linear variable displacement transducers (LVDTs) were stowed on either side (diametrically opposite) of the footing. Two datum bars were also used to position the LVDTs, which were mounted on magnetic bases. The footing's settlement was determined by averaging the settlements recorded by the two settlement transducers. The settlement transducers were linked to a high-precision data

Table 1Properties ofgeogrid	Properties of geogrid	Unit	Value			
	Mechanical properties (ASTM D6673-method A)					
	Tensile strength in the cross-machine direction (CMD)	kN/m	80			
	Tensile strength in the machine direction (MD)	kN/m	80			
	Creep limited strength in the cross-machine direction (CMD)	kN/m	54.5			
	Creep limited strength in the machine direction (MD)	kN/m	54.5			
	Partial factor installation damage in clay, silt, or sand	kN/m	1.07			
	Creep reduction factor		1.47			
	Physical properties					
	Product weight	g/sqm	558			
	Aperture size	mm	20			
	Rib width	mm	6			



acquisition system. The data acquisition system is based on the static measurement program for data collection. The load on the footing was assessed using a pre-calibrated proving ring. A specific load increment was sustained on the footing until the settlement stabilized. The loading continued until failure, which was indicated by excessive settlements for a specific load increment. Details of the experimental program are presented in Table 3.

5 Results

The results of the tests are reported in terms of the pressure-settlement responses for various foundation configurations with differing layer thicknesses (H) and subgrade strengths. To present the analysis and findings, this paper utilizes the normalized forms of footing settlement (S) and top layer thickness (H) in terms of footing diameter (D) as S/D and H/D, respectively. The behavior of footings on layered soil strata compared to the homogeneous strata and that of reinforced layered strata over unreinforced layered soil strata is quantified by analyzing the pressure-settlement responses in terms of improvement factors as $I.F_u$ and I.F respectively. The improvement factors $I.F_u$ and I.F are determined using Eqs. (1) and (2) as the ratio of two bearing pressures at equivalent footing settlement levels (S/D).

$$I.Fu = \frac{Bearing \ pressure \ of \ unreinforced \ layered \ strata \ (qu)}{Bearing \ pressure \ of \ homogeneous \ strata \ (qh)}$$
(1)

$$I.F = \frac{Bearing \ pressure \ of \ reinforced \ layered \ strata \ (qr)}{Bearing \ pressure \ of \ unreinforced \ layered \ strata \ (qu)}$$
(2)

The bearing pressures of unreinforced and geogrid/ geotextile-reinforced layered foundations are represented in the equations by q_u and q_r , respectively, whereas q_h represents the bearing pressure of homogenous beds.

5.1 Pressure–Settlement Responses

5.1.1 Homogeneous Strata

A number of tests on homogenous sand beds with varied relative densities ($Dr_B = 30\%$, 50%, 65%, and 80%) were performed in series A. The tests were performed to compare the performance of footings on homogeneous soil with stratified configurations. Tests were performed for both ring and circular footings, as shown in Fig. 3. Higher bearing pressure values were reported for ring footings. With the improvement in relative density, both the initial stiffness (the initial curvature/slope of the pressure-settlement curves) and the bearing pressure enhanced significantly. The







Fig. 3 Pressure settlement curves of homogeneous sand beds for the ring and circular footings $% \left(\frac{1}{2} \right) = 0$

bearing pressures were found to be 88 kPa, 196 kPa, 336 kPa, and 452 kPa for $Dr_B = 30\%$, 50%, 65%, and 80% respectively for rings at S/D = 10%. The corresponding values of bearing pressure for varied relative densities of sand bed in circular footings were found to be 64 kPa, 168 kPa, 260 kPa, and 420 kPa respectively.

5.1.2 Unreinforced Layered Strata

Model tests on two layered strata with unreinforced medium dense sand layer ($Dr_T=65\%$) of varying thicknesses (H=0.66, 1.33, 2, and 2.66D) overlying sub-grades of various strengths ($Dr_B=30\%$, 50%, and 80%) were conducted in series *B*. Figures 4 and



Fig. 4 Pressure settlement curves of ring footing for varying lower layer relative density (Dr_B) and top layer thickness (H)

5 shows the pressure-settlement curves of the layered strata for ring footings and circular footings respectively. It is evident that there is an increase in the bearing pressure from 88Kpa for H/D=0 (homogeneous) to 192 kPa for H/D=0.66 at S/D=10% due to the introduction of a relatively denser top layer (medium dense, $Dr_T=65\%$) over loose subgrade of $Dr_B=30\%$, for ring footings as shown in Fig. 4a. For a similar configuration, the bearing pressure for



Fig. 5 Pressure settlement curves of circular footing for varying lower layer relative density (Dr_B) and top layer thickness (H)

circular footings increases from 64 to 120 kPa as shown in Fig. 5a. Bearing pressure values were found to increase as the layer thickness (*H*) was increased. For $Dr_B=30\%$ (at S/D=10%), the bearing pressure values were enhanced from 192 to 284 kPa for the ring footing and 120 kPa to 240 kPa for circular footing as the thickness increased from H=0.66 to 2.66*D*. However, on increasing the layer thickness beyond 2*D*, no significant improvement was observed. A perusal of Fig. 4a indicates that due to an increase in H from 2D to 2.66D, the bearing pressure rises marginally from 280 to 284 kPa for ring footing and an increase from 224 to 240 kPa was observed in case of circular footings as shown in Fig. 5a. For subgrades with $D_B^r = 50\%$, a similar variation in foundation performance was observed, as shown in Figs. 4b and 5b. Figures 4c and 5c present the case of a comparatively loose sand layer overlying a very dense sand deposit. A decrease in bearing pressure from 452 to 352 kPa was witnessed for ring footings, and 420 kPa to 276 kPa for circular footings (at S/D = 10%) as the top layer thickness was varied from 0 to 2.66D. The observations are in agreement with the findings of A.M Hanna (1982) in the case of loose sand overlying dense sand.

5.1.3 Reinforced Layered Strata

The behavior of layered foundations with planar reinforcement (geogrid, geotextile) at the two-layer interface was investigated in test series C. The foundation configurations were maintained in the same manner as that of series B. Figures 6a, b present the pressure-settlement responses of geogrid-reinforced foundations with $Dr_B = 30\%$ and 80\% respectively for ring footings, and Figs. 7a, b present the pressuresettlement responses of geogrid-reinforced foundations with $Dr_B = 30\%$ and 80% respectively for circular footings. For similar configurations, the responses of geotextile reinforced layered strata are presented in Figs. 8a, b for the ring footings and Figs. 9a, b for circular footings respectively. The figures also include responses from the corresponding homogeneous beds (series A) and unreinforced layered strata (series B). Both types of reinforcements (geogrids and geotextiles) performed more efficiently for smaller top layer thickness and loose subgrades. A perusal of Figs. 6a and 8a shows that the maximum bearing pressures at H=0.66D for a geogrid-reinforced and geotextile reinforced system with a very loose subgrade $(Dr_B = 30\%)$ were 440 kPa and 272 kPa respectively, whereas the corresponding values for unreinforced layered bed and homogeneous bed were 192 kPa and 88 kPa, respectively. As the top layer thickness increased, the contribution of geosynthetics decrea sed.

For the case of the stiff lower layer ($Dr_B = 80\%$), the contribution of geosynthetics was not significant



Fig. 6 Pressure settlement curves of geogrid reinforced ring footing for varying lower layer relative density (Dr_B) and top layer thickness (H)

and no prominent improvements were observed for both geogrid and geotextile reinforced configurations. The bearing pressure values at H=0.66D were observed to be 528 kPa and 460 kPa for geogrid and geotextile reinforced systems respectively. The corresponding value for the unreinforced system was 416 kPa, indicating comparatively lower improvements as seen in Figs. 6b and 8b.

6 Discussions

The pressure-settlement responses discussed above illustrate that the layer thickness (*H*), subgrade strengths, S/D %, foundation type, and geosynthetic type had a significant impact on the performance of foundations. The implications of these parameters are discussed in this section. To quantify the observations made from pressure settlement curves, results are presented in terms of improvement factors. Compared to



Fig. 7 Pressure settlement curves of geogrid reinforced circular footing for varying lower layer relative density (Dr_B) and top layer thickness (H)

the unreinforced layered soil strata (series B), geosynthetic reinforced strata generally showed a significant improvement in bearing pressures for both types of planar reinforcements used.

6.1 Effect of Layer Thickness

6.1.1 Unreinforced Strata

The typical variations in improvement factors are shown in Fig. 10, which also illustrates the impact of top layer thickness (*H/D*) at *S/D*=10%. With the increase in the thickness of the stiffer top layer, layered soil showed enhanced bearing pressures than homogeneous strata. The improvements were significant only up to H=2D beyond which only marginal improvements were observed. In general, for H=2D, the values of improvement factors for ring footings for $Dr_B=30\%$ and 50%, were 3.18 and 1.63 respectively. For H=2.66D, the values increased marginally



Fig. 8 Pressure settlement curves of geotextile reinforced ring footing for varying lower layer relative density (Dr_B) and top layer thickness (H)

to 3.2 and 1.69, respectively. The values recorded for circular footings for similar soil configuration were 3.5 and 1.61 at H=2D and for H=2.66D the values were observed to be 3.7 and 1.66 respectively. As per the results of the present study, H=2D was found to be the optimum thickness that maximized the contribution from the top layer of the layered configurations. However, $I.F_u$ values for the stiff subgrade of $Dr_B=80\%$ were nearly constant despite variations in H/D. A reduction in the performance of footings on layered soils compared to homogeneous beds was observed as the thickness of the weaker top layer increased. The improvement factors varied between 0.9–0.7 for ring footings and 0.95–0.65 for circular footings.

For a relatively thinner top layer (H=0.66D), the failure zone is primarily (predominantly) formed in the lower layer ($Dr_B=30\%$, loose sand) and the behavior is influenced significantly by the



Fig. 9 Pressure settlement curves of geotextile reinforced circular footing for varying lower layer relative density (Dr_B) and top layer thickness (H)



Fig. 10 I.F_U versus H/D for varying Dr_B

lower layer. As the top layer's thickness increases (H > 0.66D), a significant portion of the failure zone forms in the top layer of higher relative density $(Dr_T = 65\%, \text{ medium dense})$. In other words, as the thickness increases from H = 0.66D to 2.66D, the influence of the top layer dominates. Hence, the improvement is witnessed with increasing top layer

thickness. A similar observation was reported by Azam and Wang (1991).

Figures 4c and 5c present the response of unreinforced layered foundations with dense sand $(Dr_B = 80\%)$ as the lower layer for ring footing and circular footings respectively. As can be observed, regardless of variations in sand layer thickness, bearing pressures for layered strata are less than the homogeneous strata. The failure surface for a relatively thinner top layer (H=0.66D) extends to the dense subgrade beneath it, which offers more resistance. The bottom layer's contribution decreases as the top layer thickness increases, forming a rupture surface inside the top layer. In other words, when the thickness increases, H > 0.66D, the contribution of the top layer, which is relatively weaker, dominates. The stiffness of curves keeps reducing and hence a drop in performance is witnessed. This is a typical foundation behavior for weak sands overlying dense sands, as observed by Hanna (1982).

6.1.2 Reinforced Strata

The reinforcement at the two-layer interface enhanced the bearing pressures compared to the unreinforced systems. The maximum improvement due to reinforcement was witnessed for H/D=0.66 regardless of the type of reinforcement used (geogrid, geotextile). The magnitude of improvement beyond H=0.66Dwas seen to reduce tremendously as seen in Figs. 11 and 12. For H/D>1.33, the effect of reinforcement on the performance of the footing was practically negligible. Hence, the placement of reinforcement below a depth of 1.33D does not contribute to the improvement in performance. Similar findings were



Fig. 11 I.F versus H/D at S/D = 10% (geogrid reinforced ring footings)



Fig. 12 I.F versus H/D at S/D = 10% (geotextile reinforced ring footings)

reported by Guido et al. (1985) and Khing (1993). For H/D > 1, the contribution of geogrid reinforcement decreased. At H=0.66D the overburden due to the overlying soil mass is enough to produce friction at the soil reinforcement interface which means that the reinforcement is present within the effective zone. Reduced *I.F* values for H>0.66D suggest the location of reinforcement outside the effective zone. At $H/D \ge 2$ the *I.F* approached almost 1, indicating no contribution of geosynthetic reinforcement on the performance of the footings as the location of reinforcement is outside the failure zone.

6.2 Effect of Subgrade Strength

6.2.1 Unreinforced Strata

In general, it can be seen that the improvement factors tend to decline as subgrade strength increases. Figure 10 illustrates the impact of different lower layer strengths on the performance of foundations in terms of improvement factors $(I.F_u)$. As Dr_B increased from 30 to 80%, the values of $I.F_u$ declined from 3.22 to 0.78 for rings and 3.75 to 0.65 for circular footings. In this regard, it should be noted that the declining trend only applies to improvement factors, however with increasing subgrade strengths the corresponding bearing pressures are still enhanced as seen in Table 4.

6.2.2 Reinforced Strata

Reinforced strata exhibited higher bearing pressures than the corresponding unreinforced ones irrespective of the reinforcement type for all the subgrade strengths tested. At S/D = 10% and H/D = 0.66, the maximum bearing pressures of an unreinforced layered foundation system were approximately 192 kPa, 248 kPa, and 416 kPa for $Dr_B = 30\%$, 50%, and 80% respectively for ring footings as shown in Table 4. The bearing pressure values for geogrid and geotextile reinforced circular footings are also presented in Table 4. With geogrid reinforcement, the corresponding bearing pressures raised to 440 kPa (I.F=2.29), 440 kPa (I.F = 1.77), and 528 kPa (I.F = 1.26) respectively. The corresponding values for the geotextilereinforced system were observed to be 272 kPa (I.F=1.42), 312 kPa (I.F=1.25), and 460 kPa (I.F=1.10) respectively. The improvement in bearing pressures due to the use of planar reinforcement was more pronounced for loose subgrades.

Figs. 11 and 12 illustrate the variation in *I*.*F* of ring footings for various layer configurations (H=0.66 to 2.66 D) and varying subgrade strengths ($Dr_B=30\%$, 50%, and 80%) at *S*/*D*=10%. The *I*.*F* was observed to decline with increasing subgrade strengths. A similar observation was made for geotextile and geogrid

Tal	ble	3	Experimental	program
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Test series	Foundation configurations	Test parameters	Foundation type	number	
		Variable	Constant		of tests
A	Homogeneous sand beds	<i>Dr</i> =30%, 50%, 65%, 80%	_	$r_i/r_o = 0, 0.4$	8
В	Unreinforced layered strata	$Dr_B = 30\%, 50\%, 80\% H/D = 0.66, 1.33, 2, 2.66$	$Dr_T = 65\%$	$r_{l}/r_{o} = 0, 0.4$	24
С	i. Geogrid reinforced layered strata	$Dr_B = 30\%, 50\%, 80\%, H/D = 0.66, 1.33, 2, 2.66$	$Dr_T = 65\%$	$r_{l}/r_{o} = 0, 0.4$	24
	ii. Geotextile reinforced layered strata	$Dr_B = 30\%, 50\%, 80\%, H/D = 0.66, 1.33, 2, 2.66$	$Dr_T = 65\%$	$r_t / r_o = 0, 0.4$	24

Table 4 Bearing pressuresof the ring and circularfootings at S/D = 10% fordifferent configurationstested

	Bearing pressure (kPa)						
	H/D	$Dr_B = 3$	0%	$Dr_B = 50\%$		Dr _B =80%	
		Ring	circular	Ring	circular	Ring	circular
Homogeneous strata	0	88	64	196	168	452	420
Unreinforced layered	0.66	192	120	248	224	416	404
	1.33	240	152	288	240	368	304
	2	280	224	320	272	352	276
	2.66	284	240	336	280	352	276
Geotextile reinforced	0.66	272	192	312	296	460	480
	1.33	272	192	316	272	400	352
	2	292	228	332	288	372	304
	2.66	292	248	344	304	368	288
Geogrid reinforced	0.66	440	264	440	352	528	500
	1.33	288	216	348	284	416	352
	2	296	248	336	304	376	288
	2.66	308	244	352	308	368	288

reinforced circular footing systems. This is because the geosynthetic materials contribute only when sufficient deformations occur in soil, as in the case of loose subgrades. Hence improvement in the case of loose subgrades (easily deformable soil) is quite significant.

6.3 Effect of S/D Ratio

6.3.1 Unreinforced Strata

With an increase in *S/D* and *H/D* ratios, $I.F_u$ was seen to enhance. As seen in Fig. 13, for ring and circular footings, however, the rate of improvement slows down, and beyond footing settlement of 6%, the slope flattens. This is because of the fact that beyond this point the foundation response is being affected by the loose sand layer below and the denser sand column



Solid markers - ring footing, Empty marker-circular footing

Fig. 13 $I.F_U$ versus S/D% for different top layer thicknesses



Fig. 14 I.F versus S/D% for geogrid reinforced ring footing at H=0.66D

(top layer) is being punched into the loose subgrade. For $Dr_B=80\%$, as shown in Fig. 13, the value of improvement factors was observed to be very less, signifying lower performance compared to homogeneous strata, which is due to the layer of loose sand overlying dense sand. Furthermore, it is evident that the improvement factors nearly remain the same for *S/D* values greater than 6%.

6.3.2 Reinforced Strata

At higher settlement levels, as shown in Fig. 14, a greater improvement in bearing pressure was seen for $Dr_B = 30\%$. In other words, the improvement factors increased with an increase in settlement levels. Since the improvements are more profound at the smaller thickness of the top layer (H=0.66D), it will be more reasonable to present the improvements corresponding to different subgrades at H=0.66D as seen in Fig. 14. The improvement factors increased from 1.6 to 2.29 for $Dr_B = 30\%$ as S/D% increased from 2 to 10%. This is because at higher settlement levels there is greater strain mobilization, which causes friction between the soil and the reinforcement, thereby increasing the contribution of the geosynthetic material. However, for stiffer subgrades, $(Dr_B = 50\%, 80\%)$ the range of *I*.*F* is narrow i.e. 1.5–1.77 for $Dr_B = 50\%$ and 1.15–1.27 for $Dr_B = 80\%$ as S/D varies between 2 and 10%. In other words, the improvement factor curves are flat for stiffer subgrades. The drop in performance for stiffer subgrades is attributed to restrained subgrade deformations, which leads to the insufficient generation of membrane resistance.

The effect of geogrid and geotextile reinforcement on the foundations resting on two layer soil strata was analyzed in this study. The results show that the geogrid reinforcement led to larger improvement in bearing pressures and a considerable reduction in the settlements compared to the geotextile reinforcement as shown in Figs. 15 and 16 respectively.

The settlement reduction ratio is defined as

$$=\frac{(S_u - S_{gg})}{S_u} \times 100, \frac{(S_u - S_{gt})}{S_u} \times 100.$$

Where S_u = settlement of unreinforced layered strata, S_{gg} = settlement of geogrid reinforced strata,

 S_{gt} = settlement of geotextile reinforced strata. The values of S_{gt} and S_{gg} represent the settlement of the geotextile and geogrid reinforced bed, respectively, at a bearing pressure that corresponds to S/D = 10% in unreinforced layered strata.

From Fig. 16, it is evident that with an increase in top layer thickness and lower layer strengths, the effectiveness of geogrid and geotextile decreases. Also, settlement reduction for geogrid is higher than geotextile because of its higher tensile strength. Although both geogrid and geotextile can be used as reinforcement, geogrids can be preferred over geotextiles to serve the purpose of soil reinforcement where a significant improvement in strength is required. This is because the passive resistance is mobilized against the transverse members in geogrids which contributes to higher performances in geogrids.



Fig. 15 Pressure settlement response of ring footing at $\mathrm{H}\!=\!0.66\mathrm{D}$





6.5 Effect of Foundation Type

Both ring and solid footings showed similar responses to various varying parameters. However, in terms of bearing pressures, ring footings, at a radius ratio of 0.4, performed better than circular footing for all the configurations tested and parameters varied in the study as shown in Table 4 and Fig. 17. The enhanced performance of the ring footings at a lower radius ratio is attributed to the "interference effect". Experimental investigations regarding the interference of two interfering footings on cohesion-less soil were done by Stuart (1962) and Nadri and Hataf (2014). It was established that interference occurs within a certain range of the *S/B* ratio (where S denotes the spacing between the footings and B is the footing width). It is well established that beneath a footing three zones are formed, elastic zone (zone I), radial zone (zone II), and passive zone (zone III). For widely spaced footings interference does not occur and the footings behave independently. At a certain spacing, the outer spirals (Zone III, Rankin's passive zone) of the two interfering footings eventually get intersected, and an inverted arch forms in the soil between the two footings. Due to the arching of soil between the footings, the combined system behaves as a single unit during loading. This unit's area is more than the combined area of two individual footings, resulting in an enhancement of bearing capacity. Similarly, when the footings come into contact, the arching effect is lost. The case of ring footings is analogous to the case of two interfering footings. Here, interference occurs due to the internal annular portion of ring footings. At higher radius ratios (r_i/r_0) the interference effect

Fig. 17 Comparison of pressure settlement responses for homogeneous, unreinforced layered (at H=0.66D) and reinforced layered (at H=0.66D) ring and circular footings for $Dr_B=30\%$



disappears in ring footings and hence the performance reduces. The same observation was reported by Sawaaf and Nazir (2012) and Sharma and Kumar (2017)

7 Limitations

The study aimed to investigate the impact of soil stratification and geosynthetic reinforcement on the behavior of ring footings resting on layered strata. However, only one type of geogrid and geotextile, one type of sand, and one radius ratio (0.4) of ring footing were used in the study. Additionally, the laboratory model ring footing was scaled down, which has an impact on the results of the experiment (Vesic 1973; Ovesen 1979). While problems in the field are related to prototype footings, test results obtained in this research are based on small scale laboratory model experiments. Although the practice of using small scale modeling to predict the behavior of a full scale foundation is common, it is also well-recognized that due to scale effects and the nature of soils, especially granular soils, laboratory models and prototypes may not exhibit the same behavior. The main causes of the differences are the variations in stress levels between prototypes and model testing, as well as the impact of the footing width/grain size ratio. The scale effects caused by differences in footing and soil particle size can be ignored as long as the footing dimensions are large enough in comparison to the soil particle size. However, the test results provide a useful insight into the foundation behavior and serve as a valuable reference for additional investigations using full-scale tests, centrifugal model tests, and numerical studies, which adds to the knowledge of the actual behavior.

8 Conclusions

In this study, various laboratory model experiments were performed for the ring and solid circular footings on homogenous and two-layered unreinforced and reinforced foundation systems. The effect of geogrid and geotextile reinforcement on the behavior of footings was also analyzed. The following conclusions can be drawn from the present study.

- 1. The thickness of the top layer has a significant impact on the bearing pressure of the foundations. However, the influence of the top layer thickness on the behavior of foundations is significant up to a value of H=2D. A further increase in the top layer thickness does not exhibit a substantial influence on the foundation behavior.
- 2. The pressure-settlement responses in layered configuration showed improvements in bearing pressures with a layer of dense sand $(Dr_T=65\%)$ overlying the loose subgrades $(Dr_B=30\%)$, however, a detrimental effect was observed for the stiff subgrade of $Dr_B=80\%$, regardless of variations in sand layer thickness (H).
- 3. The geosynthetic reinforcement at the two-layer interface improved the bearing stresses of the multilayer foundation system irrespective of the foundation type i.e. ring/circular footing. Compared to the unreinforced soil system, the improvement factors due to geosynthetic reinforcement was found to be 2.29 and 2.2 for ring and circular footings respectively.
- 4. The optimum top layer thickness for geosynthetic reinforced layered soil systems was found to be to be H=0.66D for $Dr_B=30\%$. As layer thickness and subgrade strength increased, the improvement factors for reinforced layered foundation systems were reduced. This is because of the lack of strain mobilization for the generation of membrane action in geosynthetics.
- 5. Among the two types of planar reinforcements used, geogrids proved to be more effective at enhancing the bearing pressure and reducing the settlements. The maximum value of *I.F* for geogrid and geotextile was found to be 2.29 and 1.42 respectively in the case of ring footings.
- 6. For all the cases of the geosynthetic reinforced and unreinforced soil beds, the ring footing (for $r_i/r_o = 0.40$) performed better than the circular footing. Hence ring footings can be used as an effective and economical alternative to conventional footings.

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Author contribution SF conceptualized and performed experiments and wrote the original draft. Dr. MYS contributed

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Data Availability All the data was generated through experimental tests performed in the laboratory by the author.

Declarations

Conflict of interest The authors declare no competing interests.

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