

Robust optimization in an agricultural closed‑loop supply chain network design with a price and freshness‑dependent demand: hybrid rat with particle swarm optimization algorithm

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Abstract

This study seeks to develop a closed-loop network for managing the pistachio Supply Chain (SC) under uncertainty. Then, a Mixed-Integer Linear Programming model is suggested to achieve optimal costs of the SC such transportation, production costs and $CO₂$ emissions tax. It is assumed that the demand for the product depends on the freshness and price of the product and, to deal with uncertainty, a robust optimization approach is used. Furthermore, GAMS software as an exact solution method and four meta-heuristics algorithms including Whale Optimization Algorithm, Particle Swarm Optimization, Rat Swarm Optimizer and a new hybrid algorithm are used as the solution approach. The accuracy of the planned model is examined using a case study and to more measurement, a sensitivity analysis is performed. Finally, the computational time of the mentioned algorithms and their obtained results are compared. The numerical analysis showed that the hybrid algorithm, although having more computational time, is superior to others, which the results had a diference between 0.9 and 2.7% with the exact method. Therefore, it is showed that the hybrid approach is a valid approach to solve large-scale problems. Our fndings are helpful for pistachio-producing countries.

Keywords Agricultural supply chain optimization · Mathematical modeling · Metaheuristics · Robust optimization

1 Introduction

Nowadays, the agriculture industry has attracted the attention of many governments because of its essential role in nutrition, health, and improving the economy of developing countries (Yaseen et al., [2023](#page-35-0); Abbas et al., [2020](#page-33-0)). In addition, the Agricultural Supply Chain (ASC) is considered an attractive research feld among researchers due to unique attributes such as the sensitivity of product quality, fuctuations in their demand and prices, and the efects of climate change. (Abbas & Dastgeer, [2021;](#page-33-1) Abbas et al., [2021](#page-33-2)). Among all agricultural products, pistachio is one of the most valuable garden products that play

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Fig. 1 Pistachio production between 1994 and 2019 (FAO)

Fig. 2 From left to right: raw pistachios, processing center, pistachio nuts, and the soft shell of pistachio

a crucial role in improving the economy of pistachio-producing countries (Taghizadeh-Alisaraei et al., [2017](#page-35-1)). World pistachio production in 2014 reached more than 638,000 tons (with its soft shell), which showed an increase by 37% and 50% compared to 2013 and 2004, respectively (Dolatabadi et al., [2021](#page-34-0)). In 2018, the top three pistachio farmers in the world were Iran, the USA, and Turkey, which their annual production is 551×10^3 , 447×10^3 447×10^3 447×10^3 , and 240×10^3 tons, respectively (see Fig. 1) (www.fao.org).

Annually, a huge large quantity of wastes is produced in pistachio processing centers (terminals), which can be used in many other industries instead of destruction (see Fig. [2](#page-1-1)). In addition to economic benefts, optimal use of pistachio wastes will have positive environmental impacts. For example, approximately 135,000 tons of pistachio waste is produced annually just in Iran. These wastes, such as the soft shell of pistachio, have great potential for biofuel production in bio-refneries (Taghizadeh-Alisaraei et al., [2017\)](#page-35-1). The soft shell of pistachio also can be recycled to produce large amounts of compost, which is used as fertilizer by farmers (Esmaeili et al., [2020](#page-34-1)). Therefore, reverse logistics utilization in the pistachio case and the optimal use of waste from its processing is essential for producing countries, which has rarely been considered by researchers.

Moreover, uncertainty in decision-making is one of the most important challenges that pistachio farmers face every year. The demand for this products is sensitive to the price and the farmer's yield could experience a signifcant fuctuation rate (Gilani & Sahebi, [2021](#page-34-2)).

Robust optimization is a proper technique to predict future conditions in the unstable environment of pistachio Supply Chain (SC), but literature review shows that this approach has rarely been considered by researchers.

Environmental concern, and the importance of the circular economy have motivated this research group to focus on a Closed-Loop Supply Chain (CLSC) network design in the ASC sector. To fll the abovementioned research gap, a CLSC network is designed for the pistachio SC, and then a new Mixed-Integer Linear Programming (MILP) model is formulated to minimize the chain's costs. A robust optimization approach is used to handle uncertainty of demand and production capacity of farmers. Also, GAMS software and some metaheuristic algorithms including Whale Optimization Algorithm (WOA), Particle Swarm Optimization (PSO), Rat Swarm Optimizer (RSO), and a new hybrid approach based on RSO and PSO (is called RSO-PSO) were used to solve the model, and then their results were compared. Then, the algorithm parameters are adjusted by applying the Taguchi method for achieving better results. Finally, the validation of the model is confrmed by analyzing the obtained results from a case study in Iran.

Therefore, the most important innovations of this research are as follows:

- Designing a CLSC network for pistachio under uncertainty.
- Proposing a new optimization model with a price and freshness-dependent demand.
- Presenting a new hybrid algorithm based on both RSO and PSO to solve the planned model.

The main purposes of this article are to solve the following problems:

- 1. How can mathematical modeling help in better distribution of agricultural products and recycling of their waste with the aim of reducing costs?
- 2. How to get better results in solving SC optimization problems in high dimensions by combining meta-heuristic algorithms?
- 3. How can the robust optimization approach be used in the decision-making and modeling processes in uncertain environments?

The current article has been written in 6 sections, which other sections are organized as the following: Sect. [2](#page-2-0) has a complete literature review. The mathematical formulation of the problem is presented in Sect. [3](#page-5-0). The optimal solution fnding approach and the meta-heuristic algorithm are described in Sect. [4.](#page-13-0) A real case study is implemented on the proposed model to show efficiency, which is described in Sect. [5](#page-23-0). The parameters of the meta-heuristic algorithm are adjusted in this section. Moreover, a comparison between the computational results is performed after obtaining individual results, and then a sensitivity examination is conducted to achieve a further evaluation of the model. Finally, in Sect. [6](#page-30-0), the obtained results are concluded, and new research lines for future studies are described.

2 Literature review

In the recent past decades, several studies have been conducted to evaluate and expand pistachio production and obtain proper use of its wastes due to the high importance of the economic aspect of pistachio for its producing countries (Taghizadeh-Alisaraei et al., [2017\)](#page-35-1). According to our best knowledge, only a few articles have used mathematical models to optimize the pistachio SC. Therefore, some studies related to SC optimization for other agricultural products are described to get to the research gap. This section aims to review and analyze these papers in three subsections, namely ASC optimization, applying meta-heuristic algorithms and considering uncertainty in this feld.

2.1 ASC optimization

There are several studies in the scope of ASC optimization (Abbas et al., [2018](#page-33-3)). As a pioneer of this feld Ahumada and Villalobos [\(2009](#page-33-4)) considered diferent agricultural products, including both perishable and non-perishable, and as well as vegetables. Following this research, a model developed by Bohle et al. ([2010\)](#page-33-5) for red grape via considering correctly determining the amount of harvested crop in each period, transporting way to the fnal product processing site, and planning the factory processing regarding the products, and packaging into the formation of a mixed integer programming model. For considering possible delays in the SC, both costs of harvesting and reducing product quality were included in the objective function of the model.

Asgari et al. [\(2013](#page-33-6)) studied a linear programming model for investigating the optimal quantity of wheat between farmers and consumers, and Lingo optimization software was applied for resolving the presented model. For large-scale problems, a genetic algorithm was also developed. A comparison between the obtained solutions from Lingo software and the obtained results from the genetic algorithm showed that the developed genetic algorithm is more efective by considering the computational time and quality of the obtained results. For SC management of imported fruits and perishable vegetables, Teimoury et al. (2013) (2013) also proposed a multi-objective model. The system dynamics approach was used to analyze the impact of fruit imports in the SC. Subsequently, Nadal-Roig and Plà-Aragonés ([2015\)](#page-34-3) formulated a transport programming model to optimize fruit logistics to meet demands in off-harvest seasons.

Banasik et al. [\(2017](#page-33-7)) studied a multi-objective MILP model by considering diferent recycling technologies for reproduction in the CLSC network of the mushroom product. Their results showed that using such technologies in the CLSC could increase the overall proft by up to 12% and reduce emissions by about 28%. Sazvar et al. ([2018\)](#page-35-3) studied a multi-objective linear mathematical programming model for providing a sustainable SC of perishable agricultural products, which were produced by organic and non-organic methods. In this research, the epsilon constraint approach was applied for solving the model to achieve specifc goals, including maintaining an equilibrium of production and consumption of non-organic and organic foods and reducing prices, reduction of environmental impacts, and improve consumers' health.

Chávez et al. ([2018\)](#page-33-8) investigated the waste of Colombian cofee to produce biofuels in a multi-objective problem. Their multi-period model's objective functions maximized net present value, minimized the cost of carbon pollution and maximized the positive social effects

2.2 Utilizing *meta***‑heuristic algorithms in ASC**

Meta-heuristic algorithms are utilized to resolve the Np-hard optimization problems. These algorithms are applied by several scientists in the feld of ASC optimization (Cheraghalipour, [2021\)](#page-33-9). For instance, Cheraghalipour et al., [\(2018](#page-33-10)) proposed a CLSC network and a multi-objective model for optimizing citrus fruits chain costs and the responsiveness of customers' demand. Several multi-objective evolutionary algorithms, such as NRGA, MOSA, MOKA, and NSGA-II, were also applied in this research to solve the planned model. Their results were compared to each other.

In other research, Cheraghalipour et al. ([2019\)](#page-33-11) formulated a two-level optimization model to optimize total costs in the rice SC. Several meta-heuristic algorithms, including the Genetic Algorithm (GA) and PSO, as well as two unique hybrid algorithms based on them, were used in this study to solve the proposed model. Roghanian and Cheraghalipour ([2019\)](#page-35-4) proposed a multi-objective model for the citrus fruit SC network for minimizing total costs, maximizing the responsiveness of demand, and minimizing $CO₂$ pollution. Some Pareto-based meta-heuristic algorithms were used as the solution methods, i.e., TGA, NRGA, and NSGA-II. The "ideal flter / ideal displacement" method was used to fnd the best algorithm. Finally, MOTGA was selected as the best algorithm. Recently, a multiobjective optimization model was developed by Sahebjamnia et al. [\(2020](#page-35-5)) for minimizing total costs and maximizing total profts in the ASC. Some evolutionary algorithms such as NSGA-II, MOPSO, and MOICA were also used to solve the suggested model. Salehi-Amiri et al. [\(2021](#page-35-6)) designed a CLSC network for walnut industry. They formulated a novel optimization model for optimizing logistics costs. They used some meta-heuristics algorithm and exact methods for solving the planned model. Rajabi-Kafshgar et al. [\(2023](#page-34-4)) considered the environmental impacts of agricultural wastes, and proposed a MILP model for an ASC network to minimize total costs. Some hybrid meth-heuristics algorithms such as KASA and GASA were used to fnd optimal solutions.

Gharye et al., ([2023a\)](#page-34-5) designed a dual-channel SC network for tea industry, and considered the role of traditional and digital advertising rates on demand focusing on social factors. They used some multi-objective algorithms such as MOSA, MOGWO and MOWOA to solve their model. Gholian-Jouybari et al., [\(2023](#page-34-6)) proposed a new sustainable MILP model to optimize the total net profit while monitoring $CO₂$ emissions and the satisfaction of customers for the soybean industry. Some multi-objective optimizers such as MOGWO and MOHHSA were utilized to solve their model.

2.3 Considering uncertainty in ASC optimization models

Since the production of agricultural products is afected by climatic conditions, and the market for agricultural products is susceptible to economic fuctuations, ASC managers should consider the uncertainty in decision-making process. In many studies in the feld of ASC optimization, uncertainty in the model has been considered. For example, Motevalli-Taher et al. ([2020\)](#page-34-7) presented a new model for optimizing wheat production under demand uncertainty. Cost and water consumption minimization, and job opportunity maximization were considered as the objective functions. In addition, the simulation approach was used to estimate demand under uncertainty. In this research, a robust probabilistic optimization approach, and epsilon constraint method were used to handle uncertainty and to solve the model, respectively.

Gilani and Sahebi [\(2021](#page-34-2)) proposed a bi-objective mathematical model for optimizing the proft and the amount of pollutants in the pistachio SC under both demand and cost uncertainty. Clavijo-Buritica et al. (2023) (2023) considered a resilience agro-food SC network during disruptions, and combined optimization and simulation schemes to address the uncertainty. Gharye et al. [\(2023b](#page-34-9)) investigated weather conditions and economic fuctuations in diferent scenarios in date fruit SC using a robust MILP model.

3 Research gap and innovation

Table [1](#page-6-0) shows a summary of related articles to shed light on the research gap. All of these articles are related to the feld of ASC optimization. By reviewing the articles, it can be concluded that mathematical models have been studied in very few articles to achieve an optimized solution for the pistachio SC network. Also, considering uncertainty in ASC optimization model is rarely seen. In addition, the use of reverse logistics in the ASC is infrequent.

In the current research, an innovative mathematical model is introduced to fll the research gap by optimizing the CLSC of pistachio under uncertainty. A robust optimization approach is used to deal with uncertainty. Also, it is assumed that the demand for the product depends on the freshness and price of the product. GAMS software and metaheuristic algorithms are used as solution methods to solve the proposed model. During each period, our model aims to fnd the best location for the construction of new facilities, determine the optimal fow of the product and its waste between the facilities, and the level of inventory of processed product (pistachio nuts) in each warehouse. The structure of the suggested logistics network and the mathematical model are described in the following chapters**.**

4 Problem defnition

A pistachio CLSC network is presented in this work. The network is developed to be a multi-period type, is composed of farmers (producers), distribution (processing) centers, factories, customers areas, recyclers (compost production centers), and compost customers (pistachio farmers) as shown in Fig. [3.](#page-8-0) In the forward fow, the raw products are sent from the farmers to the processing centers for peeling, washing, separating, sorting, and packaging. Because the maximal harvest and processing duration of raw pistachios are two months, forward and reverse fows in the pistachio logistics network are only arranged in two periods. Then, the processed pistachios (pistachio nuts) are packed and transported to a warehouse with a maximum storing time of twelve months. In the next step, the goods are sent from the warehouse to customers to meet their demand.

In the reverse fow, the waste from pistachio processing (i.e., its soft shell) is sent from processing centers to bio-refneries and recyclers to produce biofuels and compost, respectively. Finally, the produced compost in the reprocessing centers is sent to its relevant customer (pistachio producers). Since, farmers (gardeners) are the customers of fertilizers, the network can be regarded as a CLSC.

4.1 Demand function modeling

In our study, the demands of customers are assumed to be sensitive to the price and freshness of product, as follows:

$$
dm_{mt} = \alpha \times pr_{mt}^{-\xi} \times f(t)
$$
 (1)

$$
f(t) = e^{-\sqrt{t}} \tag{2}
$$

CL: Closed loop, F: Forward, MILP: Mixed Integer Linear Programming, LP: Linear Programming *CL:* Closed loop, *F:* Forward, *MILP:* Mixed Integer Linear Programming, *LP:* Linear Programming

Fig. 3 The presented CLSC network of pistachio

In these equations, pr_{mt} is the price of product in market m in period t, α is a constant parameter, and ξ is the price elasticity of demand. Moreover $f(t) = e^{-\sqrt{t}}$ indicates the freshness of the product, which decreases with time period.

4.2 Model assumptions

- The designed CLSC network is multi-period, and has four levels.
- Transportation costs between network facilities are considered per unit of product.
- The location of farmers, processing centers, bio-refneries, existing recyclers and customer zones is predetermined and constant. Some points are potential centers for opening new recyclers.
- All centers have a limited capacity.
- The demand for the product depends on the freshness and price of the product.
- The demand and production capacity of farmers are assumed to be uncertain.
- A time horizon of 1 year is considered.

5 Sets and indicators

5.1 Parameters

5.1.1 The uncertain parameters

5.1.2 Positive decision variables

5.1.3 Binary decision variables

$$
V_{c_2} = \begin{cases} 1 & \text{if new recycler c2 is opened} \\ 0 & O.W \end{cases}
$$

The objective function of the model ([3](#page-10-0)) aims to optimize all related costs to the SC network. These costs include fxed opening cost, transportation cost, maintenance cost for processing centers, production and Co2 emissions tax for farmers, processing and Co2 emissions tax for processing centers, and reprocessing cost for recyclers.

$$
\begin{split} \text{Min } \text{Costs} &= \sum_{c_2 \in C_2} f c_{c_2} \times v_{c_2} + \sum_{t' \in T} \sum_{i \in I} \sum_{j \in J} c t a_{ij} \times X a_{ijt'} + \sum_{t' \in T} \sum_{j \in J} \sum_{w \in W} c t b_{jw} \times X b_{jwt'} \\ &+ \sum_{t \in T} \sum_{w \in W} \sum_{m \in M} c t c_{wm} \times X g_{wmt} + \sum_{t' \in T} \sum_{j \in J} \sum_{b \in B} c t d_{jb} \times X c_{jbt'} + \sum_{t' \in T} \sum_{j \in J} \sum_{c \in C} c t e_{jc} \times X e_{jct'} \\ &+ \sum_{t \in T} \sum_{i \in I} \sum_{c \in C} c t f_{ci} \times X f_{cit} \sum_{t' \in T} \sum_{i \in I} \sum_{j \in J} \left[cp a_{it'} + tx i_{ti} \right] \times X a_{ijt'} + \sum_{w \in W} \sum_{t' \in T} c h w_{wu} \times X h w_{wu} \\ &+ \sum_{i \in I} \sum_{j \in J} \sum_{t' \in T} c p j_j \times X a_{ijt} + \sum_{t \in T} \sum_{i \in I} \sum_{c \in C} \left[cp c_c + tx c_{ci} \right] \times X f_{cit} + \sum_{t \in T} \sum_{w \in W} \sum_{m \in M} pr_{mt} \times X g_{wmt} \end{split} \tag{3}
$$

5.2 Constraints

5.2.1 Capacity constraints

$$
mincap_{ii'} \le \sum_{j \in J} X a_{ijt'} \le \widetilde{cap_{ii'}} \quad \forall i \in I, t' \in T
$$
\n⁽⁴⁾

$$
\sum_{i \in I} X f_{c_1 i t} \leq cap c_{c_1 t}, \quad \forall c_1 \in C_1, \forall t \in T
$$
\n
$$
(5)
$$

$$
\sum_{i \in I} X f_{c_2it} \leq capc_{c_2t} \cdot V_{c_2}, \quad \forall c_2 \in C_2, \forall t \in T
$$
 (6)

$$
\sum_{i \in I} X a_{ijt'} \le capj_j, \quad \forall j \in J, t' \in T
$$
\n(7)

$$
Xhw_{wt} \leq capw_w, \quad \forall w \in W, \forall t \in T
$$
\n
$$
(8)
$$

5.2.2 Balancing constraints

$$
(1 - \beta) \cdot \sum_{i \in I} X a_{ijt'} \ge \sum_{w \in W} X b_{jwt'} \quad \forall j \in J, t' \in T
$$
\n
$$
(9)
$$

$$
(\beta)\cdot\sum_{i\in I}Xa_{ijt'}\geq \sum_{b\in B}Xc_{jbt'}+\sum_{c\in C}Xe_{jct'},\quad\forall j\in J, t'\in T
$$
 (10)

$$
Xhw_{wt'} = Xhw_{wt'-1} + \sum_{j \in J} Xb_{jwt'} - \sum_{m \in M} Xg_{wmt'}, \quad \forall w \in W, t' \in T
$$
\n(11)

$$
\sum_{j \in J} \sum_{t' \in T} X e_{jc_2 t'} \le M \times V_{c_2}, \quad \forall c_2 \in C_2
$$
\n(12)

$$
\varphi \cdot \sum_{t' \in T} \sum_{j \in J} X e_{jct'} = \sum_{t' \in T} \sum_{i \in I} X f_{cit'}, \quad \forall c \in C
$$
\n(13)

$$
\sum_{t' \in \mathcal{T}} \sum_{j \in J} X b_{j \le t'} = \sum_{t \in \mathcal{T}} \sum_{m \in M} X g_{\mathcal{N}m t}, \quad \forall w \in W \tag{14}
$$

5.2.3 Demand constraints

$$
\sum_{w \in W} X g_{wmt} \ge \widetilde{dm_{mt'}} \quad \forall m \in M, t' \in T'
$$
\n(15)

$$
\sum_{j\in J}Xc_{jbi'}\geq db_{bi'},\quad \forall b\in B, t'\in T' \tag{16}
$$

$$
\sum_{j \in J} X e_{jc_1 t'} \geq dc_{c_1 t'}, \quad \forall t' \in T, c_1 \in C_1
$$
\n(17)

$$
\sum_{j \in J} X e_{j c_2 t'} \ge d c_{c_2 t'} \cdot V_{c_2}, \quad \forall c_2 \in C_2, t' \in T
$$
\n(18)

$$
\sum_{c \in C} X f_{ci} \ge di_{it}, \quad \forall i \in I, \forall t \in T
$$
\n(19)

5.2.4 Decision variables types

$$
Xa_{ijt'}, Xb_{jwt}, Xc_{jbt'}, Xg_{wmt}, Xe_{jct}, Xf_{cit'}, Xhw_{wt} \ge 0,
$$

\n
$$
\forall i \in I, \forall t \in T, \forall c \in C, \forall m \in M, \forall w \in W
$$

\n
$$
\forall j \in J, \forall b \in B, \forall c_2 \in C_2, Vc_2 \in \{0, 1\}
$$
\n(20)

Constraint ([4](#page-11-0)) is considered to ensure that the harvest of each farmer is between the minimum and maximum of predicted production. Constraint [\(5\)](#page-11-1) illustrates that the amount of transported compost to pistachio farmers is smaller than or equal to the production capacity of recyclers. Constraint [\(6\)](#page-11-2) indicates that the amount of transported pistachio to the warehouse should be smaller than or equal to the holding capacity of each warehouse. Constraint ([7](#page-11-3)) shows that the amount of transported raw pistachio to processing centers should be smaller than or equal to the holding capacity of each processing center. Constraint [\(8](#page-11-4)) indicates that warehouse inventory in each period must be smaller than or equivalent to its storage capacity.

Constraint [\(9](#page-11-5)) is considered to balance the fow of processing centers. So, all raw pistachios received from farmers multiplied by the conversion rate to the processed pistachio is greater than or equal to the total processed pistachio in warehouses. Constraint (10) (10) is similar to constraint ([9](#page-11-5)), which is considered the amount of raw pistachio in each processing center multiplied by the conversion rate to waste is greater than or equal to the amount of transported waste to recyclers and bio-refineries. Constraint ([11](#page-11-7)) illustrates the balance of the processed pistachio inventory in the warehouse. This constraint states that the amount of inventory in each warehouse in each period is equivalent to the inventory level for the previous period plus the amount of processed pistachio received from processing centers minus the amount of the delivered product to consumers. Constraint ([12\)](#page-11-8) ensures that the waste of pistachio processing is transported to the new recycler only if the new center is opened. Constraint ([13\)](#page-11-9) is defned to ensure that all received pistachio waste from processing centers multiplied by the compost conversion rate equals the total delivered compost to the farmers. Constraint [\(14\)](#page-11-10) balances the flow of warehouses.

Constraints (15) , (16) (16) , (17) (17) , (18) (18) and (19) (19) indicate that the demand for each facility in each period must be met and, fnally, constraint ([20](#page-12-3)) defnes the type of decision variables and their non-negativity.

5.3 Robust counterpart

Here, to deal with the uncertainty of parameters, a robust optimization proposed by Ben-Tal and Nemirovski [\(1998\)](#page-33-14) is employed. In this approach, it is assumed that each of the uncertain parameters changes in an interval uncertainty set, as follows:

$$
\tilde{\tau} = \overline{\tau} + \varphi \hat{\tau} \forall \tilde{\tau} \in R \tag{21}
$$

In this set, $\bar{\tau}$ is the nominal values, $\hat{\tau}$ is a constant deviation and $|\varphi| \leq \sigma$ is the scale of uncertainty in which σ is the radius bound.

Considering the mathematical model with uncertain parameters, including \tilde{a} , \tilde{b} , \tilde{c} and \tilde{d} :

$$
Max \tilde{c}x + \tilde{d} \tag{22}
$$

$$
s.t. \ \tilde{a}x \le \tilde{b} \tag{23}
$$

$$
x \ge 0\tag{24}
$$

To convert mathematical modeling $(Eq. (23))$ $(Eq. (23))$ $(Eq. (23))$ and solve it, the following structure is suggested:

$$
Max \gamma
$$

$$
\gamma - cx + \left[\sigma\left\{\hat{c}x + \hat{d}\right\}\right] \le \overline{d} \tag{25}
$$

$$
\overline{a}x + [\sigma \{\hat{a}x + \hat{b}\}] \ge \overline{b}
$$
 (26)

Here, the deterministic programming model is formulated based on the robust model to embed the uncertainty of demand and production capacity of farmers. The boundaries for uncertain parameters, according to Eq. [\(21\)](#page-13-2), are defned as follows**:**

$$
\widetilde{dm_{mt}} = dm_{mt} + \varphi m_{mt} \overline{dm_{mt}} \quad \forall m \in M, t \in T \tag{27}
$$

$$
\widetilde{cap_{it}} = cap_{it} + \varphi i_{it} \overline{cap_{it}} \quad \forall i \in I, t \in T
$$
\n
$$
(28)
$$

The objective function doesn't include uncertain parameters, so the following constraints are added:

$$
\sum_{w \in W} Xg_{wmt} + \sigma \times \overline{dm_{mt}} \ge \overline{dm_{mt}} \quad \forall m \in M, t \in T
$$
\n(29)

$$
\sum_{j \in J} X a_{ijt'} + \sigma \times \widetilde{cap_{it}} \ge \overline{cap_{it}} \quad \forall i \in I, t \in T
$$
\n(30)

6 Solution approach

A MILP model is presented to optimize the pistachio logistics network costs in this research. To solve this model, GAMS software was used as an exact solution method and some metaheuristic algorithms with priority-based encoding were used as the proposed approach, respectively. In this section, the proposed solution approach is described through several separate subsections including Structure and display of initial solution, WOA, PSO, RSO and, RSO-PSO algorithm. In addition, it is showed that this approach can satisfy the model's limitations.

Segment1					Segment2			Segmaent3		Segment4			Segment ₅							
period	$I=2$		$I=2$		$I=2$			$K=2$	$K=2$		$M=1$		$I=2$		$L + B = 2 + 1$		$L=2$		$I=2$	
	0.72	0.15	0.86	0.9	0.23	0.46	0.84	0.93	0.86	0.84	0.46	035	0.28	0.07	0.59	0.19	0.03	0.08	0.19	0.33

Fig. 4 A schematic diagram of proposed arrays

Segment1 (random key)								
0.72	0.15							
Segment1 (priority)								

Fig. 5 The proposed array, which is composed of random numbers for the frst segment

6.1 Structure and display of the initial solution (encoding)

In this study, the priority-based encoding method introduced by Gen et al. [\(2006\)](#page-34-14) is applied to display a candidate answer. To use this method to two-level SC optimization problems with I origins and J destinations, the structure of a solution will be a string of numbers with the length of $I+J$. Also, $I+J$ random numbers are generated and sorted according to their priority. Then, the minimum amount is transported between the origin's capacity and the demand of the destination from the origin and destination with the highest priority. For more details on this method, see (Gen et al., [2006\)](#page-34-14). The decoding method of the solution for the model of this current research is described here. Also, the structure of the initial solution is more complex due to several periods and several levels of the proposed logistics network, so a small-scale example is described for better understanding. Assume that the total numbers of farmers, processing centers, warehouses, buyers, bio-refneries, and recyclers are 2, 2, 2, 1, 1, and 2, respectively. As shown in Fig. [4,](#page-14-0) the proposed solution is a matrix with twelve rows and $2^*i+3^*j+2^*k+l+m+c$ columns. The cells of this matrix are packed with random numbers between 0 and 1, and these cells are sorted according to their priority in the next step. The sorting procedure of the numbers is performed separately for each section, which the frst part of the proposed array is shown in Fig. [5](#page-14-1) for better understanding. This section corresponds to the product amount transported from farmers (I) to processing centers (J). The constraints of 7, 9 and 10 are satisfed due to the encoding of the frst part as shown in Fig. [6](#page-15-0). In addition, the demands of bio-refneries and recyclers are met using the decoding of the second part. Moreover, inventory can be controlled by using the third part of the encoding. Other constraints can be met by the encoding of the rest of the sections, which are described in Fig. [23](#page-32-0) in appendix.

6.1.1 Whale optimization algorithm

One of the most common and recent population-based algorithms was proposed by Mirjalili and Lewis ([2016\)](#page-34-15) called WOA, which designed based on the social behavior of humpback whales. In WOA, a series of random candidate solutions (population) and three rules is used to update and enhance the location of candidate solutions in each

For $t=1$:T **Inputs:** I=set of producers I=set of DCs $Ca(i, t)$ = production capacity of producer i in period t $D(i, t)$ = capacity of DC j in period t $V(L + N)$ = encode solution of period t $Dis(i, j) = Distance$ between nodes **Outputs:** $Xaloc(i, j, t) = amount ofأbiments between node i and i in period t$ period t $W(i)$ = binary variable shows the DCs j is opened Step1 = $Xaloc(i, j, t) = 0$ $i \in I$, $j \in J$ while \sum Ca(i, t) > 0 or \sum D(j, t) > 0 **Step3**= Xaloc(i, j, t) = min(Ca(i, t), D(j, t)) Update demands and capacities $Ca(i, t) = Ca(i, t) - Xaloc(i, j, t),$ $D(j, t) = D(j, t) - Xaloc(i, j, t)$ **Step4=** if Ca(i, t) = 0 Then, $V(I, J) = 0$; if $D(i, t) = 0$ Then, $V(I, I) = 0$; End while **Step5**= $Em(i, j, t)$ = $Xaloc(i, j, t)/Cap_v \times RF_f \times Dis_{ii}$ $For i \in I$ \sum Xaloc(i, j, t) > 0 Then, W(j) = 1 **End if End for End for**

Fig. 6 The process of the priority-based decoding procedure for segment 1

step that is common in other population-based algorithms. Indeed, these three rules are including encircling prey, spiral updating location and searching for prey. A list of them is presented in the following:

• Encircling prey: if $(p < 0.5$ and $|A| < 1$).

The position of the candidate solution $\vec{X}(t + 1)$ is updated according to Eqs. ([31\)](#page-15-1) and ([32\)](#page-16-0):

$$
\vec{D} = \left| C \cdot \vec{X} * (t) - X(t) \right| \tag{31}
$$

$$
\vec{X}(t+1) = \vec{X} \cdot \vec{\ast} (t) - \vec{A} \cdot \vec{D}
$$
\n(32)

where $\vec{X}(t + 1)$ is used to show the best candidate solution for the current generation. \vec{A} *and* \vec{D} are calculated according to Eqs. ([33](#page-16-1)) and [\(34\)](#page-16-2):

$$
\vec{A} = 2\vec{a} \cdot r - \vec{a} \tag{33}
$$

$$
\vec{C} = 2 * r \tag{34}
$$

where a linearly decrease from 2 to 0, and r is a random vector in [0,1] interval.

• Search for prev: if $(p < 0.5$ and $|A| < 1$)

Both searching for prey and encircling prey are very similar, but instead of using \vec{X} ^{*}*, in searching for prey, a random candidate solution \overrightarrow{Xrand} is chosen. The process is showed by Eqs. (35) (35) (35) and (36) .

$$
\vec{D} = \left| C \cdot \vec{X} \text{rand}(t) - X(t) \right| \tag{35}
$$

$$
\vec{X}(t+1) = \overrightarrow{Xrand}(t) - \vec{A}.\vec{D}
$$
\n(36)

Searching for prey is applied during performing of the exploration phase, in which WOA is enabled to conduct a full global search (Mirjalili & Lewis, [2016\)](#page-34-15).

• Spiral updating position: if $p < 0.5$

During the WOA's exploitation process, two methods including encircling prey and spiral updating position are also used. Individual positions are modifed by the spiral updating position, according to Eq. (37) (37) (37) :

$$
\vec{X}(t+1) = \vec{D} * e^{bt} * \cos(2\pi l) + \vec{X}(t)
$$
\n(37)

where $\vec{D} = |\vec{X} * (t) - X(t)|$ is specified to show the distance among ith candidate solution and the best solution in the current iteration. Figure [7](#page-17-0) shows the pseudo-code of the WOA algorithm.

6.2 Rat swarm algorithm

RSO was introduced by Dhiman et al. [\(2020](#page-34-16)) which is a population-based algorithm that mimics the mechanism of social behavior of rats in nature, such as chasing. Chasing prey and aggressive behavior of rats caused the death of some animals which is simulated as follows:

6.2.1 Chasing prey

Prey is chased by a group of rats. To model this mechanism, it is assumed that the best search agent knows the location of the prey and that other rats update their position relative to it. The following formulas are used to model this behavior:

Input data, Number of Maxiter and Population *Initialize* the Whales population *Xi* $(i = 1, 2, ..., n)$ *Initialize a. A. C. l and p.* Calculate the fitness of each search agent X^* = the best search agent While (it < Maxiter) For each search agent If $(p < 0.5)$ *If* (|A| < 1) Update the position of the current search agent by the equation (32) Else if $(|A| \ge 1)$ Update the position of the current search agent by the equation (36) End Else if $(p \ge 0.5)$ Update the position of the current search by the by the equation (37) End End Calculate the fitness of each search agent Update X^* if there is a better solution $it=it+1$ Update a, A, C, l and p **End while** Return X^*

Fig. 7 Pseudo-code of the WOA algorithm (Mirjalili & Lewis, [2016](#page-34-15))

$$
P = A \cdot \vec{P}_i(x) + C \cdot (\vec{P}_r(x) - \vec{P}_i(x))
$$
\n(38)

where $\vec{P}_i(x)$ and $\vec{P}_i(x)$ represent the position of the rats and the best answer, respectively. In this equation, parameters A and C are defned as follows:

$$
A = R - x \times \left(\frac{R}{\text{MaxIteration}}\right) \tag{39}
$$

$$
C = 2 \times rand \tag{40}
$$

where R and C are random numbers between $\begin{bmatrix} 1 \\ 5 \end{bmatrix}$ and $\begin{bmatrix} 0.2 \\ 0.2 \end{bmatrix}$, respectively. These parameters are used for better exploration and exploitation in each iteration.

6.2.2 Fight against prey

To simulate a group of rats that fghts against prey, the following equation is used:

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Fig. 8 3D position vectors of rats

Initialize the Rats population $Xi(i = 1, 2, ..., n)$ Initialize A, C, and R Calculate the fitness of each search agent Pr = the best search agent **While** (it \langle Maxiter) For each search agent Update the position of the current search agent by the equation (41) **End** for Initialize A, C, and R Check if there is any search agents which goes beyond the given search space Calculate the fitness of each search agent Update Pr if there is a better solution $it=it+1$ **End while** Return Pr

Fig. 9 The pseudo code of RSO algorithm

$$
\overrightarrow{P_i}(x+1) = \left| \overrightarrow{P_i}(x) - P \right| \tag{41}
$$

where $\overline{P}(x+1)$ shows the next position of the rats in the next iteration so that the others update their positions using this variable. The simulation of these equations is shown in Fig. [8](#page-18-0). According to this figure, rat (A, B) can update their location to the location of their prey. By setting the parameters, a number of diferent situations can be achieved in the current position. Thus, exploration and exploitation can be guaranteed by parameters A and C. The pseudo-code of this algorithm is shown in Fig. [9.](#page-18-1)

6.2.3 Time complexity

- 1. The initialization of RSO population needs O ($n \times d$) time where n indicates the number of iterations and, d defnes the dimension of a test function to adjust the solutions within the boundary.
- 2. In the next step, the fitness calculation of each search agent requires O (MaxIteration \times n \times d) time where MaxIteration is the maximum number of iterations to simulate the proposed RSO algorithm.
- 3. Repeat Steps 1 and 2 until the satisfactory results is found which needs O (N) time. Therefore, the overall time complexity of RSO algorithm is O (MaxIteration $\times n \times d \times N$) (Dhiman et al., [2020\)](#page-34-16).

6.3 Particle swarm optimization

The PSO is a meta-heuristics algorithm proposed based on the social behavior of birds' flocks (Coello Coello & Lechuga, 2002). Particles as a population of candidate solutions move across the search space in this algorithm, which is following basic mathematical formulae over the particle's position and corresponding velocity, as below formulation:

$$
V_{ij}(t+1) = W \times V_{ij}(t) + c_1 r_{1j}(t) [p_{ij}(t) - x_{ij}(t)] + c_2 r_{2j}(t) [g_j(t) - x_{ij}(t)]
$$
\n(42)

$$
x_{ij}(t+1) = x_{ij}(t) + V_{ij}(t+1)
$$
\n(43)

where $V_{ii}(t + 1)$, $x_{ii}(t)$ are particle velocity and particle position, respectively; $p_{ii}(t)$ is the individual local of best position and $g_j(t)$ *is* the global best solution at that iteration. Moreover, W is the inertia weight factor that has a great impact on the dynamic fy of the particle, and C_1 and C_2 represent the acceleration constants and $x_{ii}(t+1)$ is the new position of the particle. In this Algorithm, the particle best position (*pbest*) and the global best position (*gbest*) are updated by Eq. ([44](#page-19-0)).

$$
pbest(t + 1) = x_{i,j}(t + 1)
$$

\n
$$
gbest(t + 1) = x_{i,j}(t + 1)
$$
\n(44)

The process will continue till obtaining the best possible solution, otherwise particles' velocity and, position must be updated. The time complexity of PSO is O (DN) (D and N are the dimensionality and population size, respectively.

6.4 RSO‑PSO hybrid algorithm

In this subsection, a new hybrid algorithm of PSO and RSO is presented. In this algorithm, a combination of diferent formulas and operators are used based on these algorithms. The algorithm starts with a population of candidate rats that have random positions and speeds in the search space. They can memorize their positions and the best position (*pbest*) and the best global position (*gbest*) similar to the PSO algorithm. For each primary iteration, the RSO is performed for a specifc number of secondary iterations, and the best rat qualifcation is considered as *gbest*. Next, for some sub-third-party iterations, the PSO algorithm starts by updating the position, velocity, *pbest*, and *gbest* using the PSO mechanism and Eqs. [8](#page-11-4) and [9](#page-11-5). Finally, a comparison is performed between the two diferent best answers obtained by the PSO and the RSO, and a more appropriate answer is considered as *gbest*. This process continues till ending the initial iterations. The fowchart and Pseudo-code of the proposed RSO-PSO hybrid algorithm is demonstrated in Figs. [10](#page-20-0) and [11.](#page-21-0)

6.4.1 Time complexity of RSO‑PSO

1 The initialization of RSO-PSO population needs O $(n \times m \times d)$ time where n and m indicate the number of RSO and PSO iterations and d defnes the dimension of a test function.

Fig. 10 Flowchart of the hybrid RSO-PSO

Inputs: The population size N and maximum number of iterations T **Outputs:** The location of Rats and its fitness value While (stopping condition is not met) do Calculate the fitness values of Rats Set Pr as the best search agent Initialize Phest and Ghest For (each Rats) do Update the position of the current search agent by the equation (41) Initialize A.C and R Check if there is any search agents which goes beyond the given search space Update Pr if there is a better solution While PSO sub-iter <Max PSO sub-iter Set Pr as the new Phest and Ghest Calculate Rats velocity according equation (43) Update Rats position according equation (44) Calculate fitness value of the Rats (fp) Updating Rat's best fitness value so far. Set Pr as the new Phest and Ghest **End While End** for **End While**

Fig. 11 Pseudo-code of the hybrid RSO-PSO algorithm

- 2 In the next step, the ftness calculation of each search agent requires O (RSOMaxIteration \times PSOMaxIteration \times n \times d) time where RSOMaxIteration and PSOMaxIteration are the maximum number of iterations in RSO and PSO.
- 3 Repeat Steps 1 and 2 until the satisfactory results is found which needs O (M) time. Therefore, we can conclude that the overall time complexity of RSO-PSO algorithm is O (RSOMaxIteration \times PSOMaxIteration \times n \times d \times M).

6.5 Evaluation of metaheuristics using benchmark functions

This section employs a benchmark outline to analyze the capability of meta-heuristics algorithms. A set of constrained problems from DTLZ (Deb et al., [2005\)](#page-34-18), which are represented in Table [9](#page-32-1) in Appendix are selected to evaluate the performance of the proposed

Fig. 13 Customer zones locations highlighted in blue color

metaheuristics. The numerical results are available in Table [2.](#page-21-1) According to the obtained results, it can be concluded that RSO-PSO outpaced the other optimizers.

Table 4 The cost of transportation between the mentioned cities (unit: dollar per ton)

	Rafsanjan	Zarand	Kerman	Ravar	Sirjan	Anar
(a)						
Rafsanjan	5					
Zarand	8	5				
Kerman	8	8	5			
Ravar	9	$\overline{7}$	10	5		
Sirjan	12	11	13	15	5	
Anar	8	9	14	11	15	5
	Tehran	Isfahan	Mashhad		Shiraz	Tabriz
(b)						
Rafsanjan	50	40	50		36	62
Zarand	52	41	45		40	62
Kerman	53	45	53		37	68
Ravar	53	44	44		45	65
Sirjan	55	35	55		33	64
Anar	45	35	40		35	62

7 Case study and results

The correctness of the presented model is investigated through a real case study in Kerman province, Iran. At present, the pistachio cultivated area in Iran is approximately more than 300,000 hectares, and Kerman province, with a total of 200,000 hectares, provides 67% of the total pistachio in Iran (Taghizadeh-Alisaraei et al., [2017\)](#page-35-1). In this study, information was collected as input data from some pistachio farmers to close the case study to reality. Some

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cities of Kerman province including Rafsanjan, Ravar, Zarand, Anar, Kerman, and Sirjan, are selected to collect data, which are considered as farmers, processing centers, recyclers and warehouses. The location of these cities is shown in Fig. [12.](#page-22-0) In addition, consumers are considered among other provinces of Iran, which are highlighted in Fig. [13](#page-22-1). Besides, as shown in Table [3,](#page-23-1) ten test problems are created depending on the number of network facilities for evaluating the efectiveness of the proposed model. In addition, Table [4](#page-23-2)a and 4b show the transportation costs between the mentioned facilities. These costs are calculated using the distance between the abovementioned cities (kilometers) and Iranian fare rates (dollars per kilometer). The conversion rate of raw pistachio to processed pistachios is approximately determined to 0.7 according to the collected information. Therefore, the conversion rate of raw pistachio to waste is about 0.3. Moreover, the conversion rate of waste pistachio to compost is 1.3. The price of product per Kg is between 7\$ and 8\$).There was a challenge to fnd exact data concerning the amount of demand, capacity and costs of related companies in the pistachio industry. For these reasons, the required data are mostly approximated, which are presented in Table [5](#page-24-0).

7.1 Parameter adjustment

The efficiency and effectiveness of any meta-heuristic algorithms depended on the proper adjustment of their parameters. Several methods have been proposed to adjust these parameters that the Taguchi method is used in this study. In this method, a group of factors is classifed into two main subclasses based on orthogonal arrays, namely control and perturbation factors (Roghanian & Cheraghalipour, [2019\)](#page-35-4). The infuence of control and perturbation factors simultaneously is changed to maximum and minimum amounts, respectively.

Algorithms	Parameter	Parameter level	Best level		
		Level 1	Level ₂	Level ₃	
RSO-PSO	Maximum iteration (MI)	50	100	150	150
	Population size (PS)	40	50	60	60
	R	0.4	0.5	0.6	0.6
	C	0.4	0.5	0.6	0.6
	C_1	1.9	$\overline{2}$	2.1	\overline{c}
	C_2	2.1	2.2	2.3	2.3
WOA	Maximum iteration (MI)	50	100	150	150
	Population size (PS)	40	50	60	60
	Pe	0.4	0.5	0.6	0.5
PSO	Maximum iteration (MI)	50	100	150	150
	Population size (PS)	40	50	60	60
	C_1	1.9	2	2.1	\overline{c}
	C_2	2.1	2.2	2.3	2.1
RSO	Maximum iteration (MI)	50	100	150	150
	Population size (PS)	40	50	60	60
	\mathbb{R}	0.4	0.5	0.6	0.6
	C	0.4	0.5	0.6	0.6

Table 6 Algorithm's parameters and their levels

Fig. 14 Diagram of the S/N ratio for WOA

Fig. 15 Diagram of the S/N ratio for PSO

Fig. 16 Diagram of the S/N ratio for RSO

Fig. 17 Diagram of the S/N ratio for RSO-PSO

The optimum level for a factor is the one that produces the highest signal-to-noise ratio (S/N) (Liao et al., [2020\)](#page-34-19). This ratio measures the level of changes during the process, which is calculated using the following formula.

$$
SN = -10 \log \left(\frac{\sum_{i=1}^{n} Y^2}{n} \right) \tag{45}
$$

where the response value in this equation is showed by *Y* and the number of orthogonal arrays is showed by *n* (Cheraghalipour et al., [2018](#page-33-10)).

Three levels for each parameter are considered to obtain better performance of the algorithms, which are shown in Table [6.](#page-25-0) According to these levels, the Taguchi design method presents the L9 orthogonal array for PSO and WOA and the L27 for RSO and hybrid RSO-PSO. After performing the Taguchi experiment in the Minitab software, the best level for each parameter is obtained using the diagrams of the S/N ratio (Figs. [14](#page-26-0), [15,](#page-26-1) [16](#page-26-2), [17\)](#page-27-0). The best value for each level is the value that the diagram reaches its maximum value. The best values for the algorithm's parameters are shown in the right column of this table. For example, the best value for the maximum repetition parameter is 150. These optimal values are usable in all sample problems.

Test	GAMS	WOA		PSO		RSO		RSO-PSO	
		Sol	RPD	Sol	RDP	Sol	RPD	Sol	RPD
1	20,262	21,074	0.039	21,762	0.074	20,955	0.034	20,872	0.027
2	23,835	24,864	0.041	25,209	0.058	24,506	0.028	24,009	0.007
3	45,648	46,393	0.016	47,023	0.03	46,301	0.014	46,293	0.014
$\overline{4}$	62,018	64,474	0.038	69.328	0.118	63,371	0.022	62.850	0.013
5	85.190	90.281	0.056	95,361	0.119	89.179	0.047	87.419	0.025
6	103.719	107,857	0.038	112,964	0.089	105,194	0.014	104,921	0.011
7	126,890	129,562	0.021	137,783	0.086	128,455	0.012	128,041	0.009
8	152.451	158.593	0.039	162,790	0.068	157,741	0.035	155,677	0.021
9	179,008	184,422	0.029	191,317	0.069	183,630	0.026	181,237	0.012
10	206,449	209.962	0.017	214.541	0.039	208,842	0.012	208,321	0.009

Table 7 The obtained computational results via solving the model

Fig. 18 Graphical diagram of the obtained results via GAMS and the proposed solution approach

7.2 Analysis and comparison of results

In this sub-section, the suggested model is examined on ten sample problems designed in the previous section. Hence, sample problems 1–5 and 6–10 are considered as small- and mediumsize problems, respectively. Then the proposed model and the meta-heuristic algorithm are encoded in GAMS software and MATLAB software, respectively. For performing calculations, a computer with 4 GB of RAM and a 2.2 GHz CPU was used. The numerical and graphical results obtained from solving the model are demonstrated in Table [7](#page-27-1) and Fig. [18,](#page-28-0) respectively. The diference between GAMS and the proposed hybrid approach (RSO-PSO) results in all sample problems is acceptably between 0.009 and 0.028. According to the obtained results, this solution approach is valid for solving large-scale problems. Moreover, Table [8](#page-28-1) and Fig. [19](#page-29-0) display the running time of the described meta-heuristic algorithms. This table illustrates that the running time of the algorithm increases following an increase in the problem size. Overall, according to these tables, although the hybrid algorithm has more execution time, it provides better results.

Table 8 Metahe
Algorithms' run

Fig. 19 Graphical diagram of the execution time

7.3 Sensitivity analysis

For further evaluating the proposed model, sensitivity analysis is conducted on diferent values of the demand parameter, and Co2 emissions tax for recyclers. It should be remembered that the frst sample problem is subjected to sensitivity analysis.

7.3.1 Demand

The diagram of the objective function values for diferent demands of pistachio (between 1400 and 1500 kg) is presented in Fig. [20.](#page-29-1) As can be shown, when the demand increases from 1450 to 1460, the total costs will also increase by 4.4%. The higher the demand, the more product will be moved, which leads to an increase in costs.

Fig. 20 The effect of increasing demand parameter on the objective function

7.3.2 Co2 emissions tax for recyclers

Here, we perform a sensitivity analysis on Co2 emissions tax fuctuations. After solving with GAMS software, the obtained outcomes are shown in Fig. [21.](#page-30-1) Sensitivity analysis shows that with a 10% increase in Co2 tax, the total costs will also increase by 0.4.4%, but when the demand value increases from 10 to 20%, total costs will increase slowly.

7.3.3 The scale of uncertainty (q)

In this section, the efect of changing the scale of uncertainty on the objective function is investigated. Figure [22](#page-30-2) assesses the presented robust model with several values of uncertainty levels in the frst test problem. As seen in this fgure, the objective function increases with an increase in this parameter.

8 Conclusions, managerial insights and suggestions for future studies

Optimal use of pistachio waste is one of the signifcant challenges in the pistachio SC, which these wastes are produced after pistachio processing. In this paper, a CLSC network was frstly organized for pistachio products, which is rarely considered by researchers. The proposed network structure was a four-level network, in which farmers were defned as the lowest level. The second layer is processing centers for processing raw pistachio products that are received from farmers. Then they sent the processed and packaged pistachios to

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the warehouse for storing in the third layer. Besides, produced waste in processing centers was sent to bio-refneries and recyclers for producing biofuel and compost. In the fourth layer, processed pistachios were shipped from the warehouse to the consumer points, and the produced composts were sent to the farmers to meet their demand in the last level. In the present problem, a MILP model was developed to optimize the total costs under uncertainty of demand and capacity of farmers. These costs included transportation costs between network layers, production costs and Co2 emissions tax for farmers and recyclers, storing costs of warehouses, and fxed costs for opening new recyclers. The mathematical model was proposed to address strategic and several operational decisions such as the construction of recyclers, product fow rate, and the amount of inventory level. The demand for the product was sensitive to the freshness and price of the product. Then, GAMS software and some metaheuristic algorithms including WOA, PSO, RSO, and also a new hybrid algorithm based on RSO and PSO called RSO-PSO were used to solve this model in low and medium dimensions. Besides, parameters of the meta-heuristic algorithm were adjusted via the Taguchi method for obtaining better results and performance, and the obtained results from solving the model were analyzed. In addition, to more measurement, a sensitivity analysis was performed on some key parameters. In this paper, ten test problems with different sizes were used to evaluate the efficiency of the presented solution approach, and the obtained results indicated that this hybrid approach can be used to solve large-scale problems.

8.1 Managerial insights

The results of this research can be used by decision-makers and managers in agricultural felds. Besides, the applications of the presented model can be expanded to optimize the SC of some other agricultural products such as citrus, crops, etc. The planed model can assist marketing executives, and production directors in their economic decision-making process. Correspondingly, the planned model can help relevant managers in the agricultural sector to better distribute products in local markets when faced with demand uncertainty.

8.2 Limitations and future directions

Although this research designed a framework to optimize the pistachio SC, it seems to have many limitations. For example, collecting real data was beyond the author's ability. Therefore, some of model's parameters were generated based on existing information. Considering water resources or pistachio production methods were not considered in this research. In addition, pricing or advertising decisions in modeling or disruption efects were ignored.

For developing this study in the future, the proposed model can be turned into a multiobjective model and, sustainability aspects must be integrated with it. Considering other robust optimization to deal with uncertainty are among the future suggestions that must be considered by researchers in this feld. Furthermore, solving the proposed model by using heuristic methods and other meta-heuristic algorithms and, comparing their results can raise some motivation for researchers to follow this research feld. Finally, due to the expansion of the Internet, it seems that the integration of ASC management with new concepts such as the Internet of Things or machine learning could improve it, which has rarely received the attention of researchers. Therefore, these issues could also be investigated in the future.

Appendix

See Figs. [23](#page-32-0) and Table [9](#page-32-1).

For $t=1$ to T **Inputs** W=set of warehouses $K =$ set of markests $D(w, t)$ = capacity of warehouse w in period t $Ca(k, t) =$ capacity of market k in period t V(W+K)=encode solution of period t $Dis(w, k)$: distance between nodes **Outputs:** $valoc(w, k, t)$ = amount of shipments between node w and k in period t $INV(w, t)$ = amount of remained goods in warehouse w at period t $D(w, t) = D(w, t) + INV(w, t - 1)$ step1 = yaloc(w, k, t) = 0 w \in W, $k \in K$ while $\sum_i Ca(k, t) > 0$ or $\sum_i D(w, t) > 0$ step2:select the value of first column of first sub-segment W for w index) select the value of first column of first sub-segment K for k index step3: $\text{valoc}(w, k, t) = \min(Ca(k, t), D(w, t))$ Update demands and capacities $Ca(k, t) = Ca(k, t) - value(w, k, t)$, $D(w, t) = D(w, t) - value(w, k, t)$ step4: *if* $Ca(k, t) = 0$ Then, $V(W, K) = 0$; *if* $D(w, t) = 0$ Then, $V(W, K) = 0$; **End while** step6: INV(w, t) = $Ca(w, t)$ **End for**

Fig. 23 The procedure of presented priority-based decoding in segment 3

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Declarations

Confict of interest The authors declare that they have no confict of interest.

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