

Channel coordination and proft distribution in a three‑echelon supply chain considering social responsibility and product returns

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Abstract

By developing markets and increasing world competition, today, companies' success is not only related to their performance but also the interaction and performance of their entire supply chain and distribution. In the supply chain strategy, operational functions, such as planning, purchasing, and fnancial afairs are considered all together. In the meantime, the coordination between manufacturers, distributors, and retailers is of great importance. Coordination through cooperation between distribution channels is necessary because of their potential for realizing signifcant profts. This study presents a mathematical model for a three-echelon supply chain. In this model, the efect of the strategy of returning goods on the amount of proft as well as on the optimal amount of wholesale-retail prices is determined. The three-echelon supply chain is represented by manufacturers, distributors, and retailers. In this study, social responsibility is considered in the model and channel coordination in this three-echelon supply chain is also considered. Hence, in addition to maximizing total proft, social responsibility is also taken into consideration. Channel coordination and optimization of the supply chain are considered in both centralized and decentralized modes. In the results, it was found that the quality of products in a consistent manner is always at a higher level than in a decentralized state. Also, it was found that if decisions are made on a coordinated basis, customers who return their goods will beneft from higher earnings than decentralized. Therefore, this model helps the frms to fnd out the structure, which has a better performance in terms of product quality, return policy, and social responsibility impact while reducing confict between supply chain members. Also, through a coordinated system, frms can enhance the quality of products and return policy, which in turn improves customer satisfaction and profts.

Keywords Supply chain coordination · Pricing · Return strategy · Social responsibility

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1 Introduction

In today's market wherein frms are competing fercely, each frm aims to enhance its proft using diferent tools and methods. Applying coordination methods can be considered as one of the most efective methods in an increment of profts of supply chain members and the whole supply chain. Coordination between supply chain participants can be obtained through designing an appropriate contract between members of the supply chain such that they decide on optimal centralized decisions instead of decentralized ones. The primary objective of the coordination contract is to instigate supply chain members to make their decisions coherently. To decline channel confict between supply chain decision-makers, diferent kinds of side-payment contracts have been applied by the previous scholars. Two-part tarif (Modak et al., [2016](#page-31-0)), sales rebate (Wong et al., [2009](#page-32-0)), quantity discount (Li & Liu, [2006](#page-30-0)), buy-back (Ding & Chen, [2008](#page-30-1)), and revenuesharing (Cachon & Lariviere, 2005) are examples of payment contracts.

Corporate social responsibility (CSR) is an evolving concept, which indicates that frms are responsible to their stakeholders for the efect of its measures and decisions on society as well as the environment. Thus, as far as CSR is concerned, the frm is liable for the variety of expectations such as social, environmental, health, ethical expectations placed by society (Carroll & Buchholtz, [2014](#page-29-1)). Over time and with the emergence of the global supply chain, CSR has been becoming growingly popular so much so that it has turned into a deciding factor for making a purchase decision, so it cannot be disregarded by the organization anymore. The result of an empirical study indicates that consumers are inclined to pay a greater price for products characterized by CSR attributes (Auger et al., [2003](#page-29-2); Trudel & Cotte, [2009\)](#page-32-1), leading to the creation of shareholder value. As a result, CSR helps companies with the improvement of their competitiveness through cost-saving. Therefore, in today's market, a lot of frms are voluntarily employing CSR to enhance their corporate image (Fombrun, [2001,](#page-30-2) [2005](#page-30-3)), control their risk (Fombrun et al., [2000;](#page-30-4) Husted, [2005\)](#page-30-5), build customer royalty (Bhattacharya & Sen, [2004](#page-29-3); Sen & Bhattacharya, [2001\)](#page-31-1), to name but a few. Consequently, many prestigious companies such as Wal-Mart, Nike, Gap, and Adidas have applied a CSR strategy in their corporate through a series of codes of conduct (Amaeshi et al., [2008\)](#page-29-4).

As an important aspect of product features, the quality of products signifcantly infuences the customers' preferences and subsequently market demand. Therefore, the quality of products plays a strategic role in the supply chain competitiveness, and consequently, this factor remarkably afects the marketing strategies. Apart from the market demand, the quality of products correlates with the return quantity. In other words, the low quality of products results in consumer dissatisfaction and subsequently a lot of returns. On the other hand, when products have high quality, the consumers are satisfed with the quality of products, and consequently, the return quantity decreases. Products that have a high quality merit high sales price, because the higher price of products indicates that products are of higher quality (Kirmani & Rao, 2000 ; Whitfield & Duffy, [2013](#page-32-2)). Nevertheless, a high price of products results in falling market demand, in particular when market demand is highly dependent on the price of the product. On the other hand, when market demand does not depend on price, the frm tries to enhance the quality, and therefore the price of the product. Thus, there is a trade-of between the price and quality of products afecting the pricing and quality investment strategies of supply chain participants.

A centralized, decentralized model, based on the Stackelberg model, and a coordinated model are formulated to address the below questions regarding optimal solutions in diferent models.

- What are the optimal quality level, wholesale, selling, and buy-back prices in a CSR supply chain?
- How does the responsibility of the supply chain afect wholesale price, selling price, quality level, and buy-back price?
- How does the manufacturer make a reaction against the price-quality trade-off?
- What is the effect of the return policy on optimal quality and price solutions?
- How can a contract be designed to eliminate channel confict between participants of the supply chain and increase their profts?

This paper aims to incorporate return policies into a socially responsible three-level supply chain by considering a channel coordination mechanism. In a manufacturer-led supply chain, contract bargaining is applied to eliminate the channel friction and share surplus proft among supply chain participants. Unlike, most previous works, which considered CSR and channel coordination issues separately, this paper considers CSR and channel coordination issues at the same time. Recently, Panda et al. [\(2015](#page-31-2)) explored the channel coordination issue in a socially responsible supply chain. However, they ignored the return policy and the efect of the quality of products on a demand function. Therefore, this paper develops the work of Panda et al. (2015) (2015) by considering the return policy and the quality of products. Also, although few studies in the literature have considered the efect of the return policy on a demand function, this factor is taken into consideration in this paper.

The rest of this study is outlined as follows. Section [2](#page-2-0) reviews the previous works. In Sect. [3](#page-6-0), model formulation is presented. In Sect. [4,](#page-11-0) we analyze the behavior of the model regarding the change of diferent parameters. Finally, concluding remarks are provided in Sect. [5.](#page-17-0)

2 Literature review

By reviewing the literature, it is noted that there are a lot of two-level supply chain models exploring coordination contracts for the elimination of double marginalization. However, a limited number of papers have been developed for solving channel confict in a three-level supply chain. Elimination of channel confict through coordination contracts is more diffcult in a three-level supply chain than that in a two-level supply chain. By increasing the levels of a supply chain, designing a coordination contract gets more complex as a result of the increment of the solution space dimension. By considering a quantity discount contract, Munson and Rosenblatt [\(2001](#page-31-3)) explored the coordination issue in a multi-level supply chain containing a manufacturer, a retailer, and a supplier. Jaber et al. [\(2005](#page-30-7)) developed the previous work in terms of discount-dependent demand function and proft-sharing. Jaber and Goyal ([2008\)](#page-30-8) discussed order quantity contract to coordinate a multi-echelon supply chain which is consist of multiple suppliers and buyers and a single manufacturer. With consideration of the buy-back contract, Ding and Chen [\(2008](#page-30-1)) achieved a coordinated three-tire supply chain in which the members of the supply chain divide their profts freely. Panda ([2014\)](#page-31-4) coordinated a three-level supply chain including disposal cost-sharing for perishable items. They assumed that there is a coalition between the distributor and the

manufacturer indicating that the disposal cost of the retailer should be divided between them. Using a quantity discount contract, Modak et al. [\(2014](#page-31-5)) developed a coordinated dual-channel supply chain by considering a CSR strategy. With consideration of a quality and marketing efort, Ma et al. ([2013\)](#page-31-6) designed a new contract for the coordination of the manufacturer and the retailer. Recently, Choi et al. [\(2013](#page-30-9)) used two-tarif and new revenue-sharing contracts to achieve coordination in a closed-loop supply chain (CLSC) by considering diferent formats for supply chain leadership. By considering diferent channel formats in CLSC, Taleizadeh et al. [\(2018a\)](#page-32-3) optimized pricing, quality, efort decisions in a three-level supply chain. By considering a price and marketing-dependent demand function, Zerang et al. ([2018\)](#page-32-4) studied pricing decisions in a closed-loop supply chain under both centralized and decentralized decisions.

As far as an individual frm is concerned, the practice of CSR has a rich history in the context of the supply chain. However, the application of CSR in the whole supply chain has been emerging in recent years. By introducing social issues into the traditional economy, Murphy and Poist [\(2002](#page-31-7)) explored the responsibility approach in a supply chain characterized by CSR. Carter and Jennings [\(2004](#page-29-5)) did a case study research to explore the role of CSR in decisions made in a supply chain. Cruz ([2008\)](#page-30-10) explored the CSR issue in a dynamic supply chain where supply chain participants act based on multi-criteria decisionmaking. Hsueh and Chang ([2008\)](#page-30-11) applied CSR strategy in a three-level supply chain for coordination of the supply chain. Their results indicate that using CSR benefts the entire supply chain. Savaskan et al. [\(2004](#page-31-8)) extended the concept of CSR into the closed-loop supply chain. Using quantity discount, Panda et al. (2016) (2016) coordinated a two-level supply chain wherein either the retailer or the manufacturer employs a CSR strategy. Ni et al. ([2010\)](#page-31-10) examined the CSR issue in a two-echelon supply chain. They applied a wholesale price contract to share the CSR cost between upstream and downstream members of the supply chain. Ni and Li (2012) (2012) extended a CSR two-level supply chain by considering separate CSR cost for each supply chain member. They developed a game theory model to analyze the impact of strategic interactions between supply chain participants. Crifo et al. ([2016\)](#page-30-12) analyzed the French data set to investigate the impact of diferent CSR approaches on the economic performance of the frm. Then, regarding the quality and quantity of CSR, they compared the results. By designing a new revenue-sharing contract, Hsueh [\(2014](#page-30-13)) coordinated a two-echelon socially responsible supply chain. Recently, Panda et al. [\(2015](#page-31-2)) interestedly studied channel coordination, and CSR issues in a supply chain. They assumed the CSR cost is imposed on the manufacturer only. However, in their paper, they did not consider the return policy.

Modak et al. [\(2019a\)](#page-31-12) considered social work donation to practice CSR in a two-level closed-loop supply chain. They investigated a centralized and three-decentralized scenarios two-part tarif contract to mitigate channel confict between a manufacturer and a retailer. Unlike our model, they did not consider a return policy and quality considerations. Recently, Modak and Kelle ([2021\)](#page-31-13) applied a social work donation and a recycling policy to practice social responsibility in the CLSC. They incorporated carbon emissions tax and obtained the optimal prices, investment in recycling, the amount of donation, and replenishment. Unlike our paper, they did not consider the quality factor and coordination mechanisms to mitigate channel confict. Also, in the same direction, Subramanian and Gunasekaran [\(2015](#page-31-14)), Ding et al. [\(2015](#page-30-14)), and Chen and Slotnick [\(2015](#page-29-6)) did worthwhile research studies. Azevedo et al. ([2017\)](#page-29-7) examined the sustainability of individual frms and their corresponding upstream frms by considering economic, social, and environmental aspects. Hosseini-Motlagh et al. ([2020\)](#page-30-15) investigated the coordination mechanism for acquisition price by incorporating CSR in a closed-loop supply chain. Gang et al. [\(2020](#page-30-16))

discussed CSR in the context of the global supply chain consisting of Chinese suppliers and multinational companies. Modak et al. [\(2019b](#page-31-15)) developed a three-echelon CLSC consisting of a manufacturer, several retailers, and a third party for collecting used products. They examined the relationship between CSR policy and product recycling under the manufacturer Stackelberg model and indicated that considering the CSR policy, thresholdbased recycling decision is optimal. Unlike our model, they did not consider the quality level and buy-back price decisions. Also, in this paper, a discount contract is applied for mitigating channel confict, which was not considered in their paper.

Panda et al. [\(2017](#page-31-16)) investigated a socially responsible two-echelon CLSC by considering the recycling policy and examined CSR through recycling practice. To resolve the channel friction in the decentralized model, they considered a revenue-sharing contract. Unlike the work of Panda et al. (2017) (2017) , in this paper, we consider a three-echelon CLSC consisting of a manufacturer, a distributor, and a retailer. Also, in this paper, we incorporate the quality level of products in a demand function and investigate the impact of CSR and the return policy on the optimal quality as well as the price of the products. Also, Modak et al. [\(2019b](#page-31-15)) considered a return policy as a given parameter, while in this paper, we aim to optimize the rate of refund as a decision variable. Moreover, this paper develops a kind of discount contract between a manufacturer, a distributor, and a retailer to attain channel coordination, which was not investigated by Panda et al. ([2017\)](#page-31-16).

As an important factor in the determination of consumers' preferences, quality issues have earned incredible attention in couples of recent years. Singer et al. ([2003](#page-31-17)) optimized the supplier's and retailer's quality investment in a distribution channel of disposable items. By considering three kinds of contracts, Gurnani and Erkoc ([2008](#page-30-17)) extended a pricing model in a decentralized distribution channel where market demand associates with the selling efort and quality. Based on four game theory models, Hsieh and Liu ([2010\)](#page-30-18) optimized the best investment strategy in quality improvement with different levels of available information. Considering cooperation and non-cooperation in a dynamic supply chain, De Giovanni ([2011](#page-30-19)) derived the optimal pricing, advertising, and quality investment decisions. In a just-in-time setting, Diaby et al. ([2013\)](#page-30-20) developed a multi-product optimization model of setup time reduction and quality improvement. Yu and Ma ([2013](#page-32-5)) explored how diferent sequences of decision-making can afect pricing and quality improvement decisions in a two-tire supply chain wherein demand is uncertain. In recent years, Moshtagh and Taleizadeh ([2017\)](#page-31-18) developed a production/reproduction model in an imperfect closed-loop supply chain in which produced and reproduced items are not perceived equally, and returned items are of variable qualities. Also, Taleizadeh and Moshtagh ([2019\)](#page-32-6) extended a four-level CLSC by considering a quality-dependent return, imperfect production, and diferent qualities of produces and reproduced items. Maiti and Giri [\(2015\)](#page-31-19) optimized pricing and quality-level decisions under fve diferent channel power structures of three-tire CLS. Recently, Taleizadeh et al. ([2017\)](#page-32-7) developed a pricing model to optimize selling and buyback prices, quality level, and eforts based on diferent game models. By considering a price- and quality-dependent demand, Modak et al. ([2018\)](#page-31-20) developed a pricing model in a two-level CLSC. They examined diferent alternatives for collection activities and showed that collecting products using third-party logistics is disadvantageous. Based on a collection efort threshold, they determined the optimal solutions and applied two strategies to overcome channel confict. It should be mentioned that, unlike our model, they did not consider the CSR policy and coordination mechanisms for the return policy. Zhalechian et al. [\(2017](#page-32-8)) considered a multi-objective hub location problem with economic, responsiveness and social issues under uncertainty. In their model, they considered an *M*/*M*/*c* queuing system and social responsibility measures. To solve the model, they proposed the possibilistic programming, fuzzy multiobjective programming and self-adaptive diferential evolution algorithm.

In addition to the quality of products that afect the return quantity, buy-back price and return policy exert signifcant infuence on return quantity. Most works in the literature studying product return investigated a business to business (B2C) return policies that mainly occur between a retailer and a manufacturer. They primarily studied the supply chain coordination obtained through the return contract (Cai et al., [2009;](#page-29-8) Emmons & Gilbert, [1998;](#page-30-21) Pasternack, [1985;](#page-31-21) Webster & Weng, [2000;](#page-32-9) Yao et al., [2005\)](#page-32-10). Few works in the literature studied return strategies between a business and a customer. The previous researches mainly focused on the impact of return policies on consumers' reactions in a general sense. However, the buyback price of the products can directly afect the return quantity of the products. In a direct sales model, Mukhopadhyay and Setoputro [\(2004](#page-31-22)) examined the efect of return strategies on customers' decisions regarding return and buying. However, they disregard the impact of product quality. They further developed a multi-stage model of pricing in an online selling setting to investigate the optimal prices, quality level, and return policy (Mukhopadhyay & Setaputra, [2007](#page-31-23)). Yu and Wang ([2008](#page-32-11)) optimized marketing and return policies in a direct selling framework. By considering an online-selling model, Bonifeld et al. ([2010\)](#page-29-9) studied the correlation between return policies and quality level. Li et al. ([2013](#page-30-22)) incorporated a return policy in a direct selling system to investigate the optimal price and quality level. Taleizadeh et al. ([2018b](#page-31-24)) studied a green chain with both coordination and pricing strategies. Keyvanshokooh et al. ([2013](#page-30-23)) considered a multi-period, multi-product, multi-echelon supply chain with forward/reverse logistics and returned products. They developed a dynamic pricing approach to fnd the acquisition price for the products. Fadaei et al. ([2019\)](#page-30-24) considered the partial and full coordination in serial *N*-echelon supply chains with a proft-sharing contract and uncertain demand.

On the whole, reviewing the highlighted literature review, we can notice that there is no work in the literature considering the CSR, channel coordination, bargaining, return policy, and quality factor jointly. More specifcally, this paper contributes to the literature by developing the work of Panda et al. (2015) (2015) in the following ways:

- 1. They did not consider the return policy in their paper, although in today's market, the possibility of returning products by customers plays an important role in the competitiveness of a frm and can be considered as an inseparable part of a supply chain.
- 2. In this paper, the efect of the return policy is incorporated in a demand function.
- 3. Despite the undeniable efect of the quality level of product on market demand, Panda et al. [\(2015](#page-31-2)) ignored this very important factor. Therefore, we discuss the efect of the quality level of products by considering its efect on both market demand and return quantity functions in our research.

Also, this paper contributes to the work of Panda et al. ([2017\)](#page-31-16) by considering a three-level supply chain and using a discount contract to mitigate channel confict between three supply chain members. Furthermore, unlike Panda et al. [\(2017](#page-31-16)), this work optimizes the quality of the products and refund rates, which was considered as a parameter in Panda et al. [\(2017](#page-31-16)).

3 Model formulation

This chapter deals with defning the problem, after introducing the notation used in mathematical models and using the game theory strategy to obtain optimal decision variables followed by developing mathematical models.

3.1 Notations

The symbols and signs used in this study including parameters, decision variables, and dependent variables, are presented below.

Parameters

 ρ^b **b** Optimal discount rate at the distributor's wholesale price under coordinated decision-making mode

3.2 Assumptions

To model the described problem, the following assumptions were considered.

Assumption 1 The demand of customers referring to the retailer for supplying goods follows a linear function, relative to the price of the fnal product, the quality of the products, and the sale price of the returned goods, and it is written by:

$$
D = \alpha - \beta p + \delta q + \gamma r \tag{1}
$$

where α , β , δ , γ \geq 0. In this equation, α is the basic market demand for this product, β is the customer's sensitivity to the price of this product, δ is the degree of sensitivity of demand to the quality of products, and γ is the sensitivity parameter for the refund of a returned item. Assuming that the demand function must be non-negative, then we have:

$$
p \in (0, (\alpha + \delta q + \gamma r)/\beta).
$$

Assumption 2 Moreover, the return value (R) is a linear function dependent on the purchase price of the returned goods and product quality, which is presented by.

$$
R = \phi + \varphi r - vq \tag{2}
$$

where φ , ν . In this equation, ϕ is the basic return value for this product, which is independent of the amount of the returned goods refund and the product quality, φ is the sensitivity of the number of returning products to the refund (the higher the sale price of a retrogressive product, the more customers are willing to return the purchased goods), and ν is the sensitivity of the number of returned goods to the quality of products. The higher the quality of the products, the fewer customers willing to return them.

Assumption 3 Deficiency is not allowed at any level.

Assumption 4 The delivery time from producer to the distributor and from the distributor to the retailer was considered zero.

Assumption 5 The demand for manufactured goods is considered fxed and constant.

3.3 Modeling

Consider a three-level supply chain consisting of a manufacturer, a distributor, and a retailer. The producer produces goods with the quality of *q* and a cost of *c* and sells them to a distributor at a wholesale price of ω_m . Then, the distributor sells these products to the retailer at a wholesale price of ω_d , and ultimately, the retailer meets customer demand by selling these products at the final price of p . In this model, the manufacturer promises to customers that if they are dissatisfed with the quality of the products, they can return them at any time and receive r amount of money as a refund $0 \le r \le p$. If $r = 0$, it means that the retailer does not pay any money for returning the goods from the customers, and if $r = p$, it means that customers receive the refund at the same purchased price.

In this model, the manufacturer tries to increase the quality of the product by controlling the failure rate at the production stage and reducing defective items. The greater the cost of increasing the quality of products, the higher the quality of the goods will be. Hence, similar to the studies of Hosseini-Motlagh et al. ([2020\)](#page-30-15) and Gang et al. [\(2020](#page-30-16)), in this thesis, it was assumed that the costs of increasing the quality follow the convex function of $C = \lambda q^2$.

As mentioned, this strategy model is called CSR. Most of the world's leading and dominant brands and companies are struggling with extreme pressure to manage a socially responsible supply chain. A common strategy to reduce these pressures is to provide a set of behavioral codes by the core company for its business partners. As a result, other members of the supply chain are involved in the CSR strategy, while the producer is the main member of the supply chain.

Therefore, in this research, it is assumed that the producer is investing based on the CSR strategy and adjusts the CSR according to the performance of the channel. The cost of CSR is divided among the supply chain members through transitional pricing. In this thesis, the impact of CSR is modeled based on the consumer's surplus.

When a company employs CSR regardless of the competing companies, it improves its goodwill, since it largely indicates the intention to increase stakeholder satisfaction. As a result, customers are willing to pay a higher price than the base price for the products. Consequently, similar to the study of Panda et al. [\(2015](#page-31-2)), we consider consumer surplus in the proft function as an efect of the CSR strategy. The consumer's surplus is the diference between the maximum price the consumer is willing to pay and the market price that the customer pays. Thus, the consumer surplus is written by:

$$
\int_{p_{\min}}^{p_{\max}} Ddp = \int_{(\alpha + \delta q + \gamma r - D)/\beta}^{(\alpha + \delta q + \gamma r)/\beta} (\alpha + \delta q + \gamma r) dp = \frac{D^2}{2\beta}
$$
(3)

If $\theta \in [0, 1]$ is a ratio of CSR related to producer social responsibility, then the producer puts $\theta D^2/\beta$ as a consumer's surplus in the profit function. $\theta = 0$ means that the producer maximizes net proft, indicating that he/she maximizes the total welfare. In this research, since the producer is socially responsible, it is assumed that his/her proft function includes net proft from selling the products to the distributor and the consumer's surplus obtained by using the CSR strategy.

3.4 Centralized decision‑making system

Assume that all members of the channel are willing to cooperate and make a decision. Therefore, under this system, there will be only one marketing channel, in which a product category is produced and sold to customers at a price of p_C . Moreover, in this system, socalled the CSR strategy is used. Thus, the surplus of the consumer from the shareholders is accumulated in the channel and is calculated in the total proft function. The total proft function in the centralized system is written by:

$$
\pi_C = (p_C - c)(\alpha - \beta p_C + \delta q_C + \gamma r_C) - \lambda q^2 - r(\phi + \varphi r_C - vq_C) + \frac{\theta}{2\beta}(\alpha - \beta p_C + \delta q_C + \gamma r_C)^2
$$
\n(4)

Proposition 1 *When the following conditions are established,* π_c *in p_C*, *q_C*, *and r_C is concave, and there is a single optimal solution for the single decision-maker*.

$$
\theta < 2 - \max\left\{\frac{\delta^2}{2\beta\lambda}, \frac{2\delta^2\varphi + 2\delta\gamma v + 2\gamma^2\lambda}{\beta\left(4\varphi\lambda - v^2\right)}\right\} \tag{5}
$$

By solving the first derivative of the π_C function for p_C , q_C , and r_C , the equilibrium optimal response for this centralized system is obtained by:

$$
p_C^* = \frac{\left[\alpha(1-\theta) + \beta c\right]\left(v^2 - 4\varphi\lambda\right) + \phi(1-\theta)(\delta v + 2\gamma\lambda) + 2c\left(\delta^2\varphi + \gamma^2\lambda + \delta\gamma v\right)}{\beta(2-\theta)\left(v^2 - 4\varphi\lambda\right) + 2\delta^2\varphi + 2\gamma^2\lambda + 2\delta\gamma v}
$$
(6)

$$
q_C^* = \frac{\delta[\phi\gamma - 2\varphi(\alpha - \beta c)] + \upsilon[\beta\phi(2 - \theta) - \gamma(\alpha - \beta c)]}{\beta(2 - \theta)(\upsilon^2 - 4\varphi\lambda) + 2\delta^2\varphi + 2\gamma^2\lambda + 2\delta\gamma\upsilon}
$$
(7)

$$
r_C^* = \frac{(\beta c - \alpha)(\delta v + 2\gamma \lambda) + 2\beta \phi \lambda (2 - \theta) - \delta^2 \phi}{\beta (2 - \theta)(v^2 - 4\varphi \lambda) + 2\delta^2 \varphi + 2\gamma^2 \lambda + 2\delta \gamma v}
$$
(8)

Furthermore, by substituting the optimal values of p_C , q_C , and r_C in π_C the optimal total proft rate is obtained.

3.5 Decentralized decision making‑system

In a decentralized supply chain, unlike the centralized supply chain, where a single decisionmaker exists, each member of the supply chain makes optimal decisions. When members of the channel act independently and optimize their individual goals, it is essentially a non-cooperative decision-making process. Here, a decentralized system was developed that the Stackelberg game is used to solve. The Stackelberg game is a kind of strategic game, in which at least one member of the supply chain is the frontrunner (leader), who makes the decisions based on optimal decisions of the other members of the chain, and the rest of the members are identifed as followers.

In this research, a Stackelberg-producer game is considered in which the distributor is the frst follower of the producer and the retailer is a follower of the distributor. This game is a kind of sequential game in which the manufacturer applies his/her optimal strategy to the distributor. Accordingly, the distributor fnds the optimal strategy and communicates with the retailer.

Ultimately, based on the distributor's optimal strategy, the retailer determines its optimal strategy. The decision-making process consists of two Stackelberg games, one between the producer and the distributor and the other between the distributor and the retailer. In this study, to obtain the optimal solutions for these two games, the retrogressive inference method is used.

The proft functions of the supply chain members are expressed by:

$$
\pi_m = (\omega_m - c)(\alpha - \beta p + \delta q + \gamma r) - \lambda q^2 \tag{9}
$$

$$
\pi_d = (\omega_d - \omega_m)(\alpha - \beta p + \delta q + \gamma r) \tag{10}
$$

$$
\pi_r = (p - \omega_d)(\alpha - \beta p + \delta q + \gamma r) - r(\phi + \varphi r - \upsilon q) \tag{11}
$$

Therefore, the total proft of the producer is written by:

$$
v_m = \pi_m + \frac{\theta}{2\beta} (\alpha - \beta p + \delta q + \gamma r)^2
$$
 (12)

As mentioned, in this research, a retrogressive method is used to solve the Stackelberg model. Therefore, frst, the retailer's optimal decisions (which are followed by the second) are obtained.

• **Retailer's optimal decisions**

By considering the optimal values related to the distributor and producer as a parameter, the retailer makes the optimal decisions as follows:

Proposition 2 *When the condition* (13) *exists*, π *, is concave in p and r, and there is a single optimal answer for the retailer*.

$$
\varphi \ge \frac{\gamma^2}{4\beta} \tag{13}
$$

By solving the first-order conditions, $\frac{\partial \pi_r}{\partial p} = 0$ and $\frac{\partial \pi_r}{\partial r} = 0$, the retailer's optimal decisions are obtained by:

$$
p^* = \frac{2\alpha\varphi - \phi\gamma + \omega_d(2\beta\varphi - \gamma^2) + q(2\delta\varphi + \gamma v)}{4\beta\varphi - \gamma^2}
$$
(14)

$$
r^* = \frac{\alpha \gamma - 2\beta \phi + q(\delta \gamma + 2\beta v) - \beta \gamma \omega_d}{4\beta \varphi - \gamma^2}
$$
 (15)

• **Distributor's optimal decisions**

After obtaining the retailer's optimal decisions, substituting the optimal solutions of p^* and r^* in the distributor's profit function (π_d) the optimal solution of the distributor is obtained.

Proposition 3 *Existing condition* (16), π_d *is concave in* ω_d *, and there is a single optimal solution for the distributor*.

$$
\varphi \ge \frac{\gamma^2}{4\beta} \tag{16}
$$

By solving $\frac{\partial \pi_d}{\partial \omega_d} = 0$, the optimal value of ω_d is obtained by:

$$
\omega_d^* = \frac{2\alpha\varphi - \phi\gamma + q(2\delta\varphi + \gamma v) + 2\beta\varphi\omega_m}{4\beta\varphi}
$$
\n(17)

• **Producer's optimal decisions**

After obtaining optimal feedback from retailers and distributors and placing them in the producer's profit function (v_m) , we obtain the producer's optimal decisions.

Proposition 4 Once the condition (18) exists, π_m is concave in ω_m and q and there is a sin*gle optimal decision for the producer*.

$$
\phi < \frac{(\alpha - \beta c) \left[-2\delta^2 \varphi \theta (2\delta \varphi + \gamma v) + 4\beta \varphi \gamma \lambda v \right] + 2\beta c \delta (2\delta \varphi + \gamma v)^2 - 8\beta \delta \varphi^2 \lambda [9\beta c + \alpha (7 - 2\theta)] + 16\delta \varphi \gamma^2 \lambda}{2\gamma^2 \lambda (4\delta \gamma + \beta v) - \delta^2 \gamma \theta (2\delta \varphi + \gamma v) - 4\beta \delta \varphi \gamma \lambda (7 - 2\theta)}\tag{18}
$$

Therefore, by solving the first-order conditions, $\frac{\partial v_m}{\partial \omega_m} = 0$ and $\frac{\partial v_m}{\partial q} = 0$ the producer's optimal decisions are written as follows:

$$
\omega_m^* = \frac{8\varphi\lambda(\alpha + \beta c)(\gamma^2 - 4\beta\varphi) + 4\beta\varphi\varphi\gamma\lambda(4 - \theta) - 8\beta\varphi^2\lambda[4(\alpha + \beta c) - \alpha\theta] + \beta c(2\delta\varphi + \gamma v)^2 - 4\varphi\gamma^3\lambda}{\beta[16\varphi\gamma^2\lambda + (2\delta\varphi + \gamma v)^2 - 8\beta\varphi^2\lambda(8 - \theta)]}
$$
\n(19)

$$
q^* = \frac{(2\delta\varphi + \gamma v)[\phi\gamma - 2\varphi(\alpha - \beta c)]}{\beta \left[16\varphi\gamma^2\lambda + (2\delta\varphi + \gamma v)^2 - 8\beta\varphi^2\lambda(8 - \theta)\right]}
$$
(20)

Moreover, by placing ω_m^* and q^* in Eqs. [\(14\)](#page-10-0), ([15](#page-10-1)) and ([17](#page-10-2)) the optimal values of p^* , r^* , and ω_d^* are obtained by:

$$
p^* = \frac{4\varphi\gamma^2\lambda(3\alpha + \beta c) - 8\beta\varphi^2\lambda[\alpha(7-\theta) + \beta c] + 4\beta\varphi\varphi\gamma\lambda(7-\theta) + \beta c(2\delta\varphi + \gamma v)^2 - 6\varphi\gamma^3\lambda}{\beta[16\varphi\gamma^2\lambda + (2\delta\varphi + \gamma v)^2 - 8\beta\varphi^2\lambda(8-\theta)]}
$$
(21)

$$
r^* = \frac{4\beta\phi\varphi\lambda(8-\theta) - (\alpha - \beta c)\left[\gamma(v^2 + 4\varphi\lambda) + 2\delta\varphi v\right] - \phi\gamma(6\gamma\lambda + \delta v) - 2\delta^2\phi\varphi}{16\varphi\gamma^2\lambda + (2\delta\varphi + \gamma v)^2 - 8\beta\varphi^2\lambda(8-\theta)} \tag{22}
$$

$$
\omega_d^* = \frac{4\varphi\lambda(3\alpha + \beta c)\left(\gamma^2 - 4\beta\varphi\right) + \beta c(2\delta\varphi + \gamma v)^2 + 4\beta\varphi\varphi\gamma\lambda(6 - \theta) - 6\varphi\gamma^3\lambda + 8\alpha\beta\varphi^2\lambda\theta}{\beta\left[16\varphi\gamma^2\lambda + (2\delta\varphi + \gamma v)^2 - 8\beta\varphi^2\lambda(8 - \theta)\right]}
$$
\n(23)

Furthermore, by placing the optimum values of ω_m^* , q^* , p^* , r^* , and ω_d^* in Eqs. [\(12\)](#page-10-3), ([10](#page-9-0)) and [\(11\)](#page-10-4), the optimal proft rate of producer, distributor, and retailer is obtained.

3.6 Supply chain coordination

The producer as a member of the supply chain, with the social responsibility, always wants to receive larger size orders from the retailer, since the producer will be able to act more competitively in line with CSR. On the other hand, the retailer has no reason to order at larger sizes than the decentralized decision-making mode. Therefore, the retailer will leave the optimal model in the centralized decision-making structure provided that the manufacturer provides an incentive scheme to compensate for the cost of getting out of the optimality through the distributor. Consider that as a motivational

scheme, the manufacturer will offer a discount at the wholesale price to the distributor, which is the middle and the intermediary member between the producer and the retailer.

In response to this, the distributor would force the retailer to increase the order quantity, by providing a discount on the wholesale price. Members of the supply chain will participate in such schemes, and such discounts will be practical if there are two conditions:

- The retailer must order based on the optimal decision-making mode (the custom value that is desirable throughout the supply chain, not just for the retailer),
- Under any discount scheme at wholesale prices, each member of the supply chain must attain at least some of their proft in decentralized decision-making mode (by leaving their optimal decisions and participating in the discounts scheme, they will not be in a worse position in terms of proftability).

In general, in multi-level supply chains, each member establishes a one-to-one relationship only with the member directly associated and assumes that there are no other members in the chain. The producer can provide a discount on the wholesale price to the distributor, as long as the decentralized profts are guaranteed.

Similarly, retailers will accept the discount offer at wholesale prices from the distributor's proft and will order based on centralized decision-making mode provided that the cost of leaving the optimality is compensated by outperforming by a discount at wholesale price.

In the process of discounts, the distributor plays a central role, since he/she preserves the role of mediator to maintain the fow of the incentive discounts scheme from the manufacturer to the retailer, and the flow of the order quantity from the retailer to the manufacturer. In this way, the distributor will receive more proft than the decentralized model. Therefore, when a discount plan is provided at wholesale prices to resolve the conficts between targets in the supply chain, the distributor decides on two maters:

- The minimum discounts at wholesale prices from the manufacturer to the distributor
- The maximum discounts on wholesale prices from the distributor to the retailer.

Allowed values for these two matters depend on each other. The fow of determining the discount values can be assessed under two scenarios. In the frst scenario, the decisionmaking process is from the manufacturer to the retailer, and in the second scenario, the decision-making fow is from the retailer to the manufacturer. In the frst scenario, the producer and distributor decide on the minimum and maximum discount rate on the wholesale price of the manufacturer. Then, in this specifed range, they decide on the distribution of the generated surplus. Based on the decisions made at this stage, the distributor and retailer will also achieve a certain range for discounts in distributor wholesale quantities so that the winning-winning state is guaranteed. In the second scenario, retailers frst decide on discounts and proft-sharing, and then based on this, the distributor will deal with the manufacturer. These two scenarios will produce diferent results and responses.

Nevertheless, the frst approach is to examine, from producer to retailer, since it is assumed that the producer is the leader of the supply chain. Another reason is that in the real world, any discounts from the manufacturer will fow through the supply chain to the customers, and these types of schemes will begin with manufacturers. Therefore, in general, a plan for supply chain coordination will include two coordination and two negotiation (bargaining) agreements.

In the process of coordinating the supply chain, the sequence of activities will be as follows:

Step 1 The manufacturer and distributor fnd discount rates on the wholesale price to achieve the winning-winning state, provided that the distributor must compensate the retailer losses for the change in order quantity.

Step 2 Within the determined discount range set in the first step, the manufacturer will bargain with the distributor for a certain share of the generated proft. The decentralized proft plus the proft share here is the producer's optimal proft. Similarly, the proft in the decentralized mode plus the proft share in this step represents the distributor's total proft.

Step 3 Given the created intermediary profit (additional profit reached by the distributor), the distributor and the retailer will determine the winning-winning range for a discount at the distributor's wholesale prices.

Step 4 Distributors and retailers will determine the profts share through bargaining.

Suppose that the manufacturer suggests a discount of $\mu \omega_m^*(\mu \ge 0)$ to the distributor. The total proft of the manufacturer under this discount will be as follows:

$$
v_{m}^{wd} = (\omega_{m}^{*} - c)(\alpha - \beta p_{C}^{*} + \delta q_{C}^{*} + \gamma r_{C}^{*}) + \frac{\theta}{2\beta}(\alpha - \beta p_{C}^{*} + \delta q_{C}^{*} + \gamma r_{C}^{*})^{2} - \lambda q_{C}^{*2}
$$

- $\mu \omega_{m}^{*}(\alpha - \beta p_{C}^{*} + \delta q_{C}^{*} + \gamma r_{C}^{*})$ (24)

The manufacturer can offer a discount on the wholesale price as long as at least the decentralized profits are maintained. In other words, $v_m^{\text{wd}} \ge v_m^*$. If μ is assumed as the maximum discount rate that satisfies the mentioned inequality, $\bar{\mu}$ is computed by:

$$
\bar{\mu} = \frac{(\omega_m^* - c + \frac{\theta}{2\beta})(D_C^* - D_D^*) - \lambda(q_C^{*2} - q_D^*)}{\omega_m^* D_C^*}
$$
(25)

where $D_C^* = \alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*$ and $D_D^* = \alpha - \beta p_D^* + \delta q_D^* + \gamma r_D^*$.

Therefore, the minimum amount of retailer that the manufacturer can ofer to the distributor is as follows:

$$
\underline{\omega_m} = \left(1 - \overline{\mu}\right)\omega_m^* \tag{26}
$$

Similarly, the distributor may accept a discount ofer from the manufacturer, as long as the proft is provided and the loss is compensated in the decentralized decision-making system.

If the distributor requests the minimum discount of $\mu \omega_m^*$. There should be $\pi_d^{wd} = \pi_d^* + [\pi_r^* - \pi_r^{wd}],$ then by placing this phrase.

$$
\begin{split} \left(\omega_{d}^{*} - \omega_{m}^{*}\right)\left(\alpha - \beta p_{C}^{*} + \delta q_{C}^{*} + \gamma r_{C}^{*}\right) + \underline{\mu}\omega_{m}^{*}\left(\alpha - \beta p_{C}^{*} + \delta q_{C}^{*} + \gamma r_{C}^{*}\right) \\ & = \left(\omega_{d}^{*} - \omega_{m}^{*}\right)\left(\alpha - \beta p_{D}^{*} + \delta q_{D}^{*} + \gamma r_{D}^{*}\right) \\ & + \begin{bmatrix} \left(p_{D}^{*} - \omega_{d}^{*}\right)\left(\alpha - \beta p_{D}^{*} + \delta q_{D}^{*} + \gamma r_{D}^{*}\right) - r_{D}^{*}\left(\phi + \varphi r_{D}^{*} - \upsilon q_{D}^{*}\right) \\ - \left(\left(p_{C}^{*} - \omega_{d}^{*}\right)\left(\alpha - \beta p_{C}^{*} + \delta q_{C}^{*} + \gamma r_{C}^{*}\right) - r_{C}^{*}\left(\phi + \varphi r_{C}^{*} - \upsilon q_{C}^{*}\right)\right) \end{bmatrix} \end{split} \tag{27}
$$

By simplifying the above expression, the value of μ will be as follows:

$$
\underline{\mu} = \frac{(\omega_d^* - \omega_m^*) (D_C^* - D_D^*) + (p_D^* - \omega_d^*) D_D^* - (p_C^* - \omega_d^*) D_C^* - r_D^* (\phi + \varphi r_D^* - \upsilon q_D^*) + r_C^* (\phi + \varphi r_C^* - \upsilon q_C^*)}{\omega_m^* D_C^*}
$$
\n(28)

Therefore, the manufacturer can have the maximum wholesale price demand as follows:

$$
\overline{\omega_m} = \left(1 - \underline{\mu}\right)\omega_m^* \tag{29}
$$

According to the presented explanation, for each $\omega_m \in \left(\omega_m, \overline{\omega_m}\right)$, the producer's profits are in the winning-winning mode, and after compensating for the loss of the retailer, the distributor's proft is also obtained in the winning-winning mode. In this wholesale price range, the manufacturer and the distributor will bargain over a certain amount of the wholesale price that effectively distributes the generated surplus profit.

Here, we use the concept of Nash equilibrium to calculate the ideal amount for the wholesale price under the discounts. One of the important features of the Nash equilibrium is that the output will be in the random form since it depends on the bargaining of the members participating in equilibrium. In the Nash bargaining model, the objective function of the product model is to beneft the members of the cooperation which should be maximized. Each member's beneft means the diference between profts from co-operation and proft in decentralized decision-making mode. Hence, we will have:

$$
Max_{\underline{\mu} \le \mu \le \overline{\mu}} [v_m^{wd} - v_m^*] [\pi_d^{wd} - (\pi_d^* + (\pi_r^* - \pi_r^{wd}))]
$$
(30)

By replacing the terms we will have:

$$
Max_{\underline{\mu} \leq \mu \leq \overline{\mu}} \left[(\omega_m^* - c) (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) + \frac{\theta}{2\beta} (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*)^2 - \lambda q_C^{*2} - \mu \omega_m^* (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) - \nu_m^* \left[(\omega_d^* - \omega_m^*) (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) \right] + \mu \omega_m^* (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) - \left(\pi_d^* + \left(\pi_r^* - \left(\frac{(p_C^* - \omega_d^*) (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*)}{-r_C^* (\phi + \varphi r_C^* - \upsilon q_C^*)} \right) \right) \right) \right]
$$
\n(31)

By solving the above model, the optimal value of μ is obtained as follows:

$$
2c\beta (D_D^* - D_C^*) + 2D_D^* \beta p_D^* - 2\beta D_C^* (p_C^* - 2\omega_m^*) - 4\beta D_D^* \omega_m^* + \theta (D_C^{*2} - D_D^{*2})
$$

$$
\mu^b = \frac{+2\beta \lambda (q_D^{*2} - q_C^{*2}) + 2\beta v (q_D^* r_D^* - q_C^* r_C^*) + 2\beta \phi (r_C^* - r_D^*) + 2\beta \phi (r_C^* - r_D^*) (r_C^* + r_D^*)}{4D_C^* \omega_m^* \beta}
$$
(32)

Therefore, the rate of the wholesale price, in this case, is as follows:

$$
\omega_m^b = \left(1 - \mu^b\right)\omega_m^* \tag{33}
$$

In this case, the distributor's proft is as follows:

$$
\pi_d^{ib} = \left(\omega_d^* - \omega_m^b\right) \left(\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*\right) \tag{34}
$$

Accordingly, the distributor and the retailer will disclose the discount at the distributor's wholesale price. If $\bar{\rho}\omega_d^*$ expresses the maximum discount on the wholesale price that the distributor provides for the retailer, we will have:

$$
\pi_d^{ib} - \bar{\rho}\omega_d^* \left(\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^* \right) = \pi_d^* \tag{35}
$$

Then, we have:

$$
\bar{\rho} = \frac{(\omega_d^* - \omega_m^b) D_C^* - (\omega_d^* - \omega_m^*) D_D^*}{\omega_d^* D_C^*}
$$
\n(36)

Thus, the minimum wholesale price for a distributor under a discount policy is as follows:

$$
\underline{\omega}_d = (1 - \bar{\rho})\omega_d^* \tag{37}
$$

If the distributor provides such a minimum discount for the retailer, the retailer's proft will be formulated as follows:

$$
\pi_r^{wd} = (p_C^* - \omega_d^*) (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) - r_C^* (\phi + \varphi r_C^* - \upsilon q_C^*) + \rho \omega_d^* (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*)
$$
\n(38)

Given the $\pi_r^{wd} \geq \pi_r^*$, ρ will be the minimum acceptable discount as follows:

$$
\underline{\rho} = \frac{(p_D^* - \omega_d^*)D_D^* - (p_C^* - \omega_d^*)D_C^* - r_D^*(\phi + \varphi r_D^* - \varphi q_D^*) + r_C^*(\phi + \varphi r_C^* - \varphi q_C^*)}{\omega_d^* D_C^*} \tag{39}
$$

Therefore, the maximum acceptable value for the wholesale price that the distributor provides to the retailer is as follows:

$$
\overline{\omega_d} = \left(1 - \underline{\rho}\right) \omega_d^* \tag{40}
$$

For each $\omega_d \in (\omega_d, \overline{\omega_d})$, the retailer and distributor benefit under a winning-winning policy. In the range provided for the distributor's wholesale price, the two parties will bargain to earn a share of the generated proft. As in the previous section, we also use the Nash bargaining model here. Then, the model will be as follows:

$$
\text{Max}_{\underline{\rho}\leq\rho\leq\overline{\rho}}\left[\pi_d^{ib}-\rho\omega_d^*\left(\alpha-\beta p_C^*+\delta q_C^*+\gamma r_C^*\right)-\pi_d^*\right]\left[\pi_r^{wd}-\pi_r^*\right] \tag{41}
$$

Solving the presented Nash model, the optimal value of ρ is obtained by:

$$
\rho^{b} = \frac{D_{D}^{*}(p_{D}^{*} - 2\omega_{d}^{*} + \omega_{m}^{*}) - D_{C}^{*}(p_{C}^{*} - 2\omega_{d}^{*} + \omega_{m}^{b}) - vq_{C}^{*}r_{C}^{*} + r_{C}^{*}(\phi + r_{C}^{*}\phi) + r_{D}^{*}(-\omega_{D}^{*} + \phi + r_{D}^{*}\phi)}{2\omega_{d}^{*}D_{C}^{*}}
$$
\n
$$
\tag{42}
$$

As a result, the optimal wholesale price of the distributor to the retailer is also obtained under the discount contract as follows:

$$
\rho^b = \omega_d^b = \left(1 - \rho^b\right)\omega_d^*
$$
\n(43)

Finally, in general, the profts of the supply chain members in the discount contracts are given by:

$$
\pi_m^b = (\omega_m^b - c)(\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) - \lambda q_C^{*2}
$$
\n(44)

$$
\pi_d^b = \left(\omega_d^b - \omega_m^b\right) \left(\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*\right) \tag{45}
$$

$$
\pi_r^b = (p_C^* - \omega_d^b) (\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) - r_C^* (\phi + \varphi r_C^* - \nu q_C^*)
$$
(46)

$$
v_m^b = (\omega_m^b - c)(\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*) + \frac{\theta}{2\beta}(\alpha - \beta p_C^* + \delta q_C^* + \gamma r_C^*)^2 - \lambda q_C^{*2} \tag{47}
$$

It should be considered that it means eliminating the contradiction in the goals of the supply chain.

4 Model solving and analysis

In this chapter, to illustrate the application of the proposed models in this research, the sample problems were designed and solved. In the next chapter, the sensitivity of the model to some more important and infuential parameters will be analyzed.

4.1 Numerical example

This section deals with the problem design for the developed model and then the problem analysis. Numerical examples for centralized, decentralized, and coordinated systems are solved.

In a production system considering the return policy and CSR, the following parameters are considered as: $\alpha = 100$, $\beta = 10$, $\delta = 5$, $\gamma = 5$, $\phi = 10$, $\varphi = 3$, $\nu = 5$, $\theta = 0.5$, $c = 50$, $\lambda = 350$.

By placing the above values in the concavity conditions, it is seen that the proft functions of the producer, the distributor, the retailer, and the total proft function are

concave. Therefore, using the optimal solutions presented in the preceding sections, the optimal decisions of the producer, distributor, and retailer are made in the Stackelbergproducer system as well as optimal decisions under concentrated and coordinated conditions. The optimal solutions obtained from these models are presented in Table [1.](#page-16-0)

4.2 Sensitivity analysis

In this section, for each centralized, decentralized, and coordinated model, several numerical experiments were performed separately to evaluate the sensitivity of the optimal response to changes in the values of some parameters. To evaluate the behavior of the model by changing the key parameters, the sensitivity analyses to the parameters of α , β , θ , ϕ , ϕ , λ and *v* are presented in Tables [2](#page-18-0), [3](#page-19-0), [4](#page-20-0), [5,](#page-21-0) [6](#page-22-0) and [7.](#page-23-0) Moreover, changes in the variables of the diferent decision and proft functions are shown in Figs. [1,](#page-24-0) [2](#page-25-0), [3](#page-26-0), [4,](#page-27-0) [5](#page-28-0) and [6.](#page-29-10) Note that the changes to the decentralized state were shown with *D* and changes to the coordinated mode were indicated by *Co*.

According to Table [2](#page-18-0) and Fig. [1,](#page-24-0) when the base demand for manufactured goods (*α*) increases ω_m^* , π_a^* , π_m^* , r^* , q^* , ω_d^* , and π_r^* also are increased. When the demand for manufactured goods increases, the optimal production policy moves toward the production of higher quality goods and higher prices. Moreover, the retailers purchase the returned goods from the customers at a higher price. The results show that by increasing α , the proft of the producer, distributor, and retailer and total supply chain is increased. The results of Table [3](#page-19-0) and Fig. [2](#page-25-0) show that by increasing the customer's sensitivity to the price of products, the producer prefers to produce products with a lower price and quality. Moreover, the retailer returns the returning products at a lower price. Thus, the proft of the producer, distributor, retailer, and the total supply chain proft will be reduced.

According to Table 4 and Fig. [3,](#page-26-0) by increasing the social responsibility coefficient (θ) , the wholesale price of the distributor, the producer, and the sales price of the products is decreased slightly and the quality of the products is increased. Similarly, the retailer pays more money for returning the returned goods. Based on the results, with increasing social responsibility, all the decision variables change to increase the customer's satisfaction. Furthermore, according to the consumer's surplus function, with increasing θ , the profit of the members of the supply chain increases. In a practical point of view, achieving the appropriate social responsibility level helps the frm to increase the content of customers, which in turn can generate higher demand for products and higher profits.

According to Table [5](#page-21-0) and Fig. [4,](#page-27-0) with the increased sensitivity of the number of returning goods to the refund rate (φ) , the price of the produced goods is reduced slightly. Moreover, the manufacturer reduces the quality of manufactured goods. Given the fact that the objective of the supply chain is to reduce the purchased goods returning, with the increase in the sensitivity of the number of returned items to the refund, the retailer reduces the sale price of returning goods.

As seen in Table 6 and Fig. 5 , the increase in the quality cost coefficient does not have a signifcant efect on wholesale prices. However, it reduces the wholesale price of the producer and distributor in both centralized and decentralized decision-making systems very slightly. Moreover, with increasing λ , the discounts offered in the centralized decision-making mode increase. In other words, to reach the Nash equilibrium point, the manufacturer and retailer should give more discounts to their downstream member. This can be caused by the fact that as the quality of the product decreases by

 $\overline{}$

0.8 37.41 43.68 62.75 0.83 52.14 0.4736 0.4871 7983.25 3996.18 3693.51 15,672.94

43.68

0.4736

15,672.94

3693.51

3996.18

 \mathbf{v}

 ∞

10 53.93 60.48 68.16 0.32 8.66 0.2624 0.3004 4691.6 2379.61 1967.44 9038.66

8.66

0.32

68.16

60.48

53.93

 $\overline{10}$

0.2624

9038.66

1967.44

2379.61

4691.6

0.3004

400 51.49 57.73 72.91 0.52 36.95 0.2900 0.3278 5824.46 2859.48 2586.9 11,270.84 500 51.46 57.70 72.87 0.41 36.79 0.2903 0.3280 5811.69 2853.55 2584.25 11,249.49 600 51.44 57.69 72.84 0.34 36.68 0.2904 0.3281 5802.66 2854.37 2578.29 11,235.34

36.95 36.79 36.68

0.52 0.41 0.34

72.91 72.87
 72.84

57.73 57.70 57.69

 $rac{1}{2}$

500 600

0.2900 0.2903 0.2904

11,270.84
11,249.49 11,235.34

> 2584.25 2578.29

2859.48
2853.55
2854.37

2586.9

5824.46 5811.69 5802.66

0.3278 0.3280 0.3281

Parameter Parameter value

State

𝜔∗ *m*

200

 \prec

Decentralized

 300

 400 500 600 200

 \prec

Coordinated

Fig. 1 Changes in the decision and profit variables of members in terms of the parameter α change

an increase in the quality cost, consequently, and consequently the demand decreases, to compensate this efect, more discount is ofered at wholesale prices. This will reduce the retail price and, as a result, partially compensate for the reduced number of customers. The important thing regarding the table is that, as expected, all three members of the supply chain in a coordinated manner will be more proftable than the decentralized state, which is a prerequisite for acquiring a coordination mechanism. Furthermore, the proft of the entire supply chain in a coordinated mode (i.e., the total proft of the producer, distributor, and retailer) is exactly equal to the supply chain proft in the centralized decision-making mode. This fact means that the contradiction in goals and decisions is resolved. The implication is that the frm should try to coordinate supply chain members to make centralized decisions, while they do not lose proft.

According to Table 7 and Fig. 6 , an increase in the quality impact coefficient in the quantity of the returned goods means that the quality of the goods will play a more important role in the number of the returned goods. In Table [7,](#page-23-0) it can be observed that by increasing the quality impact coefficient in the number of returned goods, the retail price will increase slightly in either decentralized or centralized mode. On the other hand, in these circumstances, the wholesale prices of goods also show a

Fig. 2 Changes in the decision and profit variables of the members according to the parameter β change

non-signifcant growth rate. One important point in Table [7](#page-23-0) is that the proposed discount decreases with increasing *𝜐*. Similar to the preceding tables, and as expected, the proft of each member of the supply chain in 4.1 coordinated manners is always higher than the decentralized mode for any amount of v , and it makes the provided coordinating mechanism efficient.

5 Concluding remarks

In this research, the intention is to study the mathematical model of a supply chain consisting of producer, distributor, and retailer to determine wholesale and retail prices under the policy of returning goods. The decision variable is wholesale and retail the price, quality of manufactured products, and the buy-back price of the returned goods to the customer. Therefore, the goal is to determine the optimal value of decision variables in such a way that the total proft of the system is maximized. One of the tools used in this study is the theory of games in a collaborative model. After formulating each model, the Stackelberg-producer game is used to obtain optimal answers. Then, a numerical example was presented to illustrate the presented model numerically, and fnally, by analyzing

Fig. 3 Changes in the decision and profit variables of the members according to the parameter θ change

the sensitivity, we examined the efect of diferent parameters on optimal values and total proft. In this research, the efect of parameters such as the basic demand of manufactured goods, customer sensitivity to price, social responsibility coefficient, the amount of the base of the returned goods, the sensitivity of the number of returning goods to the amount of refund, the coefficient of cost of quality and the coefficient of quality impact on the amount of returned goods reviewed.

By comparing two decentralized and coordinated systems, in the coordinated mode, the quality of the products and the price paid to customers for the returned goods (the price of the refows) are always higher than the decentralized ones now. Thus, according to the sensitivity analysis, the application of the coordinated system is not only for the beneft of each member of the supply chain (the proft of each member in the coordinated mode is at least equal to or greater than the proft of the same member in the decentralized decisionmaking mode) but also for the beneft of customers. In other words, because the quality of goods and the amount of the refund are factors that afect customer satisfaction, customers are also coordinated by the stakeholders. The result of sensitivity analysis and numerical

Fig. 4 Changes in the decision and profit variables of members in terms of change in φ

example indicates the following important managerial insights: (1) As the market base for goods increases or sensitivity of customers to price decreases, the manufacturer increases the price, quality, and refund amount increases because by increasing the demand and popularity of the product, decreasing the sensitivity of customers to the price of products, or increasing the efect of quality, the frm increases the price and the quality of products to increases its profit. (2) By increasing the social responsibility coefficient (θ) , decision variables change in the favor of consumers' satisfaction. In other words, the price of sales of products decreases, and the quality of products increases. Also, the retailer pays more money for the return of returning goods. Also, with the increase in social responsibility, the proft of the members of the supply chain will increase. Therefore, a higher level of social responsibility helps the frm to increase its popularity and customer satisfaction as well as profits. (3) When the value of the base of returning goods (ϕ) or the sensitivity of the number of returning goods increases to the amount of refund (φ) , the price of the products, as well as the amount of the refund, will be reduced. Supply chain members decide in a way that the number of return items will be reduced. (4) An increase in the cost-of-quality ratio results in a reduction in the wholesale price of the producer and the distributor in either

Fig. 5 Changes in the decision and profit variables of members in terms of change in λ

centralized or decentralized decision making. Also, the discounts ofered in the centralized decision-making mode increase. In other words, to reach the Nash equilibrium point, the manufacturer and retailer should give more discounts to their downstream member.

There are some limitations involved in this paper, which can be considered a future study. First, this model assumed that the supply chain has only one retailer. However, in reality, a supply chain consists of multiple retailers. Apart from the coordination mechanism investigated in this paper, other coordination mechanisms (e.g., buy-back policy) can be further discussed and compared with the introduced contracts. Further possible future study direction is to consider diferent game theory models in addition to manufacturer-Stackelberg investigated in this research.

Fig. 6 Changes in the decision and profit variables of the members in terms of the change in v parameter

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