# **Mining distinguishing subsequence patterns with nonoverlapping condition**

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Received: 27 October 2017 / Revised: 20 December 2017 / Accepted: 28 December 2017 / Published online: 9 January 2018 © Springer Science+Business Media, LLC, part of Springer Nature 2018

#### **Abstract**

Distinguishing subsequence patterns mining aims to discover the differences between different categories of sequence databases and to express characteristics of classes. It plays an important role in biomedicine, feature information selection, time-series classification, and other areas. The existing distinguishing subsequence patterns mining only focuses on whether a pattern appears in a sequence, regardless of the number of occurrences of the pattern in the sequence and the proportion of the pattern in the entire sequence database, which affects the discovery of the distinguishing patterns when there are a large number of irrelevant occurrences. Therefore, the nonoverlapping conditional distinguishing subsequence patterns mining algorithm is proposed. In this paper, we focus on the number of nonoverlapping occurrences that effectively reduce the number of irrelevant or redundant occurrences, and in this way, the number of occurrences can be better grasped. At the same time, we use a specially designed data structure, namely, a Nettree, to avoid backtracking. In addition, we use the distinguishing patterns as classification features, and carry out classification experiments on DNA sequences and time-series data with two classes. Extensive experimental results and comparisons demonstrate the efficiency of the proposed algorithm and the correctness of the feature extraction.

**Keywords** Nonoverlapping occurrences · Distinguishing subsequence pattern · Nettree · Feature extraction

## **1 Introduction**

Data mining, as an important means of data analysis and information extraction [\[1](#page-11-0)], has received extensive attention from researchers. As an important branch of data mining, sequence pattern mining [\[2\]](#page-11-1) is widely used in mining information [\[3](#page-11-2)], time-series analysis and prediction [\[4](#page-11-3)], and other fields [\[5\]](#page-11-4), and has become one of the focuses of various studies. Distinguishing subsequence patterns [\[6\]](#page-11-5) and other new types of subsequence patterns proposed provide a new direction for sequential pattern mining. To satisfy user demand better, a gap constraint has been introduced in traditional sequential pattern mining. A gap constraint exists in sequence

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pattern mining [\[7](#page-11-6)] that makes the occurrences of patterns more flexible. The wide use of a gap constraint enhances the expressiveness and applicability of patterns. Sequential pattern mining with a gap constraint plays an important role in information retrieval [\[8](#page-11-7)], computational biology [\[9](#page-11-8)], feature extraction [\[10](#page-11-9)], and emergency medical recognition [\[11](#page-11-10)], among others.

Distinguishing subsequence patterns mining aims to discover differences between different categories or conditions, and has become a hotspot in the field of data mining, and is commonly applied in real life [\[12](#page-11-11)], such as shareholders determining whether to buy a stock by comparing changes in the stock market index. By comparing the price and quality of products, customers choose products with a high costperformance. In an enterprise, an HR chooses applicants who meet the requirements by comparing their abilities.

Ji et al. [\[6\]](#page-11-5) first proposed the concept of distinguishing patterns and used the ConSGapMiner algorithm to solve the problem of the minimum distinguishing pattern mining with a gap constraint, which laid an important foundation for future studies. Based on [\[6\]](#page-11-5), Wang et al. [\[13](#page-11-12)] proposed the concept of a density constraint, and introduced it into dis-



<span id="page-1-0"></span>**Table 1** Occurrences of pattern *P* in sequence *S*

S	S <sub>1</sub> G	$s_2$	$s_3$ G	$S_4$	s <sub>5</sub> G
1st occurrence	G,		G	٠	
2nd occurrence	G	т	٠	٠	G
3rd occurrence	G		٠	т	G
4th occurrence			G		G

tinguishing pattern mining to mine patterns that satisfy the density and gap constraints. Yang et al. [\[14](#page-11-13)] added the topk concept to distinguishing pattern mining to avoid pattern loss caused by an improper threshold. Wang et al. [\[15\]](#page-11-14) proposed a minimum distinguishing pattern mining algorithm with a compact gap constraint without a pre-set gap constraint to avoid an improper threshold owing to insufficient prior knowledge. Our previous studies showed that nonoverlapping subsequence patterns mining with a gap constraint can make full use of the characteristics of the elements in the sequence. In addition, Wu et al. [\[16](#page-11-15)] proposed a nonoverlapping subsequence patterns mining with a gap constraint algorithm that balances completeness with the Apriori property [\[17](#page-11-16)].

<span id="page-1-2"></span>*Example 1* Suppose that the sequence  $S = s_1 s_2 s_3 s_4 s_5$ GTGTG and pattern  $P = G[0, 2]T[0, 2]G$  are given. The occurrences of *P* in *S* are shown in Table [1.](#page-1-0) The elements of the same position for any two occurrences cannot be the same in a sequence with the nonoverlapping condition. There are thus two occurrences,  $\langle 1,2,3 \rangle$  and  $\langle 3,4,5 \rangle$ , and the support is 2.

Suppose that a positive database  $D+$  is  ${S_1 = G TGTG}$ ,  $S_2$  = GTGGTG,  $S_3$  = GGTTGGGTG}, negative database *D*− is  ${S_4 = \text{GTATC}, S_5 = \text{ACGTC}}$ , positive support threshold is 2, and negative support threshold is 1. A distinguishing subsequence pattern is a pattern whose support in a positive database is greater than the positive support threshold, whereas support in a negative database is less than the negative support threshold, and that satisfies the gap constraint. Because the supports of G[0,2]T[0,2]G are 3 and 0 in *D*+ and *D*−, respectively, pattern *P* is a distinguishing subsequence pattern.

This will cause a loss of distinguishing patterns if we adopt the density threshold method in [\[13](#page-11-12)]. Let us follow the same example. In [\[13](#page-11-12)], the density calculation method is *density* = *the number of occurrences in sequence*  $C_1(0.21T10.21G)$  occurrences *the number of possible occurrences in sequence* . G[0,2]T[0,2]G occurs four times in  $S_1$ , namely,  $\langle 1,2,3 \rangle$ ,  $\langle 1,2,5 \rangle$ ,  $\langle 1,4,5 \rangle$ , and  $\langle 3,4,5 \rangle$ , and there are nine possible occurrences,  $\langle 1,2,3 \rangle$ ,  $\langle 1,2,4 \rangle$ ,  $(1,2,5), (1,3,4), (1,3,5), (1,4,5), (2,3,4), (2,3,5),$  and  $(3,4,5)$ . If we agree that the density threshold is  $0.5$ ,  $S_1$  cannot satisfy the *gd*-*support* count of pattern *P*, which should be greater than the threshold. In addition,  $S_2$ , and  $S_3$  are also not satisfied in this way. Continuing to assume that the positive support threshold is 0.5, according to the calculation method *sup* <sup>=</sup> *the number of sequences whose density is greater than threshold in database the number of sequences in datasbase* then  $sup(P, D+) = 0$ , which is less than the positive class support threshold of 0.5, and thus *P* will not be a distinguishing pattern. It can be seen that *P* occurs frequently in a positive class, and the cause of a loss of *P* is due to the fact that a large number of irrelevant patterns under no-condition have a reduced pattern density, and thus, the sequence cannot be a *gd*-*support* count. In addition, when calculating the support, a sequence that satisfies the density threshold is simply used as a *gd*-*support* count, weakening the relationship between the patterns and database, and ignoring the proportion of patterns in the entire database.

To solve the above problems, we conducted the following in this study:

- (1) We used a Nettree to solve distinguishing subsequence patterns with the nonoverlapping condition to improve the algorithm efficiency, and proposed the nonoverlapping conditional distinguishing subsequence patterns mining (NOCM) algorithm to reduce redundancy.
- (2) We employed the average support rate, which takes the number of occurrences in a sequence and the ratio in the entire database into account, making the mining results more reasonable.
- (3) We designed an approach for applying distinguishing subsequence patterns as classification features, and verified its effectiveness and efficiency on some binary datasets.

The remainder of this paper is organized as follows. Section [2](#page-1-1) introduces the related work. Section [3](#page-2-0) provides a definition of the problem and describes it through concrete examples. Section [4](#page-4-0) proposes the NOCM algorithm based on a Nettree, and illustrates the working principle of NOCM through some examples. Section [5](#page-7-0) shows the mining effect of NOCM and the effect of distinguishing subsequence patterns for sequence classification. Finally, we conclude the paper and discuss the future work in Sect. [6.](#page-10-0)

## <span id="page-1-1"></span>**2 Related work**

Subsequence pattern mining has laid the foundation for research in many fields and plays an important role in practical applications. For example, Zhang et al. [\[18\]](#page-11-17) addressed sequence pattern mining with periodic gap constraints, to apply in mining DNA sequence. Zhang et al. [\[19\]](#page-11-18) proposed a method of mining frequent patterns with occupancy, which is used in the print-area recommendation and the travellandscape recommendation. The two methods do not take the classification issue into account. Li et al. [\[10\]](#page-11-9) proposed

an efficient algorithm for mining the closed frequent patterns with gap constraints and applied them to the feature selection of classification or clustering [\[20](#page-11-19) [,21\]](#page-11-20). This research adopted the frequent patterns as the features. However, it is difficult to treat these features as distinguishing features. The following researches focused on mining distinguishing patterns for the classification issues. Wang et al. [\[13](#page-11-12)] proposed a new method of distinguishing pattern mining based on density-aware, and used it to identify human genetic variations. Yang et al. [\[14](#page-11-13) ] and Wang et al. [\[15](#page-11-14)] also mined distinguishing subsequence patterns. And [\[14](#page-11-13)] introduced top-k to reduce the output of the patterns, while [\[15\]](#page-11-14) adopted an idea which is without a predefined gap constraint. Therefore, these methods can achieve better performance for the classification issues. However, all these above methods employ no-condition to find the frequent patterns or the distinguishing patterns.

Our previous research showed that subsequence pattern mining with nonoverlapping condition is a better strategy than that with no-condition since the former method meets the Apriori property while the latter is difficult to meet the Apriori property [\[16](#page-11-15)]. One of our previous works [\[22\]](#page-11-21) is a pattern matching task which is one of the key issues of sequence pattern mining task [\[16](#page-11-15)] since calculating the support of a pattern actually is pattern matching task. In research [\[16](#page-11-15)], we investigated subsequence pattern mining with nonoverlapping condition which does not focus on feature selection. However, this paper focuses on mining the distinguishing patterns.

Considering that the relevance and differences of this paper with these papers, we therefore make a comparison of related research in Table [2](#page-2-1) .

It can be seen from Table [2](#page-2-1) that the research work in this paper is the closest to the research [\[13](#page-11-12)]. The difference is that, research [\[13](#page-11-12)] focused on sequence pattern mining with nocondition, while this paper studies sequence pattern mining with nonoverlapping condition.

It is not difficult to find through Table [2](#page-2-1) that this paper is characterized by the mining of distinguishing subsequence patterns with nonoverlapping condition. Such mining is of great importance in practice. For example, the study of [\[23](#page-11-22)] stipulated the order of occurrence of events, but from the background analysis, the same event can only occur in one event sequence at a time, but not in several different event sequences. If there is nonoverlapping sequence of events, there will be more significance in the practical application.

## <span id="page-2-1"></span><span id="page-2-0"></span>**3 Problem definition**

In this section, the definitions about distinguishing subsequence patterns with nonoverlapping condition are presented



and several examples are given to illustrate the definitions clearly.

**Definition 1** (*sequence*) A sequence *S* with length *n* is an ordered list of events, which can be denoted as  $S =$  $s_1 s_2 \dots s_i \dots s_n$ , where  $1 \leq i \leq n$  and  $s_i \in \Sigma$ . Here,  $\Sigma$ represents a set of events, where the number of events in the set is denoted as  $|\Sigma|$ .

For example, in the DNA sequences,  $\Sigma$  is  ${A, T, C, G}$  and  $|\Sigma|$  is 4.

**Definition 2** (*pattern with gap constraints*) A pattern with gap constraints can be denoted as  $P = p_1[a_1, b_1]p_2...$  $p_j[a_j, b_j]p_{j+1} \dots [a_{m-1}, b_{m-1}]p_m(1 \leq j \leq m)$ , where  $p_j \in \Sigma$ ,  $a_j$  and  $b_j$  are two given non-negative integers that represent the minimal and maximal gap constraints between  $p_j$  and  $p_{j+1}$ , respectively. The length of *P* is *m*.

**Definition 3** (*occurrence*) If there exists a group of *m* integers  $I = \langle i_1, i_2, \ldots, i_m \rangle$  that satisfies:  $1 \leq i_1 \leq i_2 < \ldots$  $$  $p_m = S_{i_m}$ , then *I* is an occurrence of pattern *P* in sequence *S*.

**Definition 4** (*nonoverlapping occurrences*) Let  $I = \langle i_1, i_2, \rangle$ ...  $i_m$  and  $I' = \langle i'_1, i'_2, \ldots, i'_m \rangle$  be two occurrences. If and only if ∀1  $\leq$  *j*  $\leq$  *m*:  $i_j \neq i'_j$ , *I* and *I'* are two nonoverlapping occurrences.

In Example [1,](#page-1-2)  $I_1 = (1, 2, 3)$  and  $I_2 = (3, 4, 5)$  are two nonoverlapping occurrences of *P* in sequence *S*4. Although  $I_1$  and  $I_2$  both use a character at position 3,  $I_1$  and  $I_2$  are two nonoverlapping occurrences because position 3 differs in *I*<sup>1</sup> and  $I_2$ .

**Definition 5** (*support*) With the nonoverlapping condition, the support of pattern  $P$  in sequence  $S$  is the total number of occurrences of *P* in *S*, denoted by *sup*(*P*, *S*).

**Definition 6** (*offset occurrence*) If there exists a sequence  $L = \langle l_1, l_2, \ldots l_n \rangle$  that satisfies  $1 \leq l_1 \leq l_2 < \cdots < l_m \leq n$ ,  $a \leq l_{j+1} - l_j - 1 \leq b$ , then *L* is an offset occurrence of pattern *P* in sequence *S*.

**Definition 7** (*nonoverlapping offset occurrences*) Let *L* =<  $l_1, l_2,...l_j$  > and  $L' = \langle l'_1, l'_2,...l'_j \rangle$  be two offset occurrences. If and only if  $\forall 1 \le j \le m$ :  $l_j \ne l'_j$  when  $j = j', l$ and *I'* are two nonoverlapping offset occurrences. Using  $ofs(P, S)$  represents the number of nonoverlapping offset occurrences of pattern *P* in sequence *S*.

**Example 2** Following Example [1,](#page-1-2) occurrences not only need to satisfy the gap constraints, they also need to ensure that the corresponding position in the sequence of elements is the same as the pattern, whereas the offset occurrences that only need to satisfy the gap constraint, regardless of whether the element at the position is the same as the pattern. Therefore, the nonoverlapping offset occurrences of *P* in sequence *S* are:  $\langle 1, 2, 3 \rangle$ ,  $\langle 2, 3, 4 \rangle$ , and  $\langle 3, 4, 5 \rangle$ . In addition, its *ofs*(*P*, *S*) is 3.

**Lemma 1** *Under the nonoverlapping condition, given sequence*  $S = s_1 s_2 \cdots s_n$  *and pattern*  $P = p_1 p_2 \cdots p_m$ *, the total number of nonoverlapping offset occurrences of pattern P* in sequence *S* is  $n - m + 1$ .

*Proof* Compared with the definition of occurrence,  $p_i$  can be different with  $S_{i_j}$ . Therefore, the nonoverlapping offset occurrences of pattern *P* in *S* should be  $\langle 1, 2, ..., m \rangle$ ,  $\langle 2, 3, \ldots, m + 1 \rangle, \langle 3, \ldots, m + 1, m + 2 \rangle, \ldots, \langle n - m + 1 \rangle$  $1, \ldots, n-1, n$ , for a total of  $n - m + 1$ .

**Definition 8** (*support rate*) The support rate of pattern *P* in sequence *S* can be written as  $\text{rate}(P, S) = \text{sup}(P, S)$ / *ofs*(*P*, *S*).

**Definition 9** (*binary classification sequence database*) A binary classification sequence database is a collection of sequences in two mutually exclusive classes database, which can be expressed as  $D = \{S_1, S_2, ..., S_M, S_{M+1}, ..., S_N\},\$ where  $S_1 \cdots S_M$  comes from the database of  $D+$ , and *S<sub>M+1</sub>* ··· *S<sub>N</sub>* comes from the database of *D*−. The number of sequences contained in the sequence database can be denoted as |*D*|.

<span id="page-3-0"></span>**Definition 10** (*nonoverlapping occurrences between multiple sequences*) Let  $D = \{S_1, S_2, \ldots, S_M\}$  be a multi-sequence database, the occurrences  $I = \langle i_1, i_2, \dots, i_m \rangle$  and  $I' =$  $\langle i'_1, i'_2, \ldots, i'_m \rangle$  of pattern P in any two sequences  $S_j$  and  $S_j$ can be two nonoverlapping occurrences between multiple sequences.

<span id="page-3-1"></span>**Example 3** Suppose sequence database  $D = \{S_1 = \text{GTGTG}\}$ ,  $S_2$  = GGTTGG}. The nonoverlapping occurrences of pattern *P* = G[0,2]T[0,2]G in *S*<sub>1</sub> are then  $\langle 1,2,3 \rangle$  and  $\langle 3,4,5 \rangle$ , and are  $\langle 1,3,5 \rangle$  and  $\langle 2,4,6 \rangle$  in  $S_2$ . According to Definition [10,](#page-3-0) the occurrence  $\langle 1,2,3 \rangle$  in  $S_1$  and the occurrence  $\langle 1,3,5 \rangle$  in *S*<sup>2</sup> are two nonoverlapping occurrences between multiple sequences. Similarly, so are  $\langle 2,3,4 \rangle$  and  $\langle 2,4,6 \rangle$ . The supports  $sup(P, S_1)$  and  $sup(P, S_2)$  of pattern  $P = G[0, 2]T[0, 2]G$ in *S*<sup>1</sup> and *S*2, respectively, are both 2.

**Definition 11** (*average support rate*) Let sequence database  $D = \{S_1, S_2, ..., S_M\}$ , then  $|D| = M$ . The average support rate can be denoted as  $r(P, D)$ , and  $r(P, D) = \sum_{n=0}^{n} r^{at}(P, D)$  $\frac{\sum_{i=1}^{n} rate(P, S)}{M}$ . Given the average support rate threshold *minsup*(*D*), if *r* is not less than the given *minsup*(*D*), then pattern *P* is said to be frequent.

**Example 4** Continuing to example [3,](#page-3-1) the average support rate of *P* in *D* is  $r(P, D) = 0.583$ . Supposing that the average support rate threshold  $minsup(D) = 0.3$ , because  $r > minsup(D)$ , then *P* is frequent.

<span id="page-4-1"></span>

<b>Table 3</b> Example of sequence database	ID	Sequence	Class
		<b>GTGTG</b>	D+
	$\mathfrak{D}$	<b>GTGGTG</b>	$D+$
	3	GGTTGGGTG	$D+$
	4	<b>GTATC</b>	$D-$
	5	<b>ACGTC</b>	$D-$

**Definition 12** (*nonoverlapping conditional distinguishing subsequence pattern*) Given the positive sequence database *D*+ and the negative sequence database *D*−, the positive average support rate threshold  $minsup(D+)$  and negative average support rate threshold *minsup*(*D*−), gap constraints is [*a*, *b*]. The pattern  $P = p_1[a, b]p_2 \cdots [a, b]p_m$  is the nonoverlapping conditional distinguishing subsequence pattern (NOCP) that satisfies the gap constraint if *P* satisfies the following conditions:

- (1) *P* is frequent in positive sequence database  $D+$ , that is,  $r(P, D+) \geq minsup(D+).$
- (2) *P* is not frequent in negative sequence database *D*−, that is,  $r(P, D-) \leq maxsup(D-).$

The average support rate *r* is used as the threshold criterion because the average support rate takes into account the number of occurrences of patterns in each sequence and the proportion of the entire sequence database at the same time, and will not be affected by the number of positive and negative sequences. Let us combine the following examples:

**Example 5** Given the sequence database shown in Table [3,](#page-4-1) the positive support rate threshold is 0.5, and the negative support rate threshold is zero. Here,  $P = G[0, 2]T[0, 2]G$  is not a distinguishing subsequence pattern when adopting the method in [\[13\]](#page-11-12). Because  $sup(P, D+) = 0$  and  $sup(P, D-) = 0$ ,  $sup(P, D+)$  is less than 0.5 and  $sup(P, D-)$  is equal to zero. It is clearly unreasonable to state that G[0,2]T[0,2]G is not a distinguishing subsequence pattern because G[0,2]T[0,2]G occurs frequently in a positive sequence database, and *P* occurs in a positive sequence database far more than a negative sequence database.

Using the method proposed in this paper, we first calculate the support rate of the pattern in each sequence, and then calculate the ratio in the positive and negative databases separately, that is, the average support rate,  $r(P, D+) = 0.532$ ,  $r(P, D-) = 0$ . It can be seen that the average support ratio of *P* in a positive database is much larger than in a negative database. This method reduces redundant occurrences and avoids interference with patterns of excessive possible occurrences, and takes into account the contribution of occurrences in the individual sequence and the entire database. This, therefore, makes the evaluation criteria more reasonable.

**Definition 13** (*maximum prefix and maximum suffix*) Given a pattern  $R = r_1 r_2 \cdots r_m (m \ge 2)$ , if  $P = r_1 r_2 \cdots r_{m-1}$ , then *P* is the maximum prefix sub-pattern of *R*. This can be denoted as  $prefix(R) = P$ , and has  $R = P \cup r_{m-1}$ . If  $Q =$  $r_2 \cdots r_{m-1}r_m$ , then *Q* is the maximum suffix sub-pattern of *R*, and is denoted as *suffix*( $R$ ) =  $Q$ , and  $R = r_1 \cup Q$ .

**Definition 14** (*prefix–suffix connection method*) Suppose that pattern  $A = ar_1r_2 \cdots r_{m-1}$  and  $B = r_1r_2 \cdots r_{m-1}b$ , from Definition [16](#page-5-0) we know that  $\text{suffix}(A) = \text{prefix}(B) = R$ , and thus, *A* and *B* can be connected to generate a superpattern *T* whose length is  $m + 1$  using the operator  $\oplus$ , and  $T = A \oplus B = aRb.$ 

**Example 6** Given pattern  $P = ACTA$  and  $Q = CTAC$ , the maximum prefix sub-pattern and maximum suffix subpattern of *P* are the same as CTA. Therefore, super-pattern  $T = \text{suffix}(A) \oplus \text{prefix}(B) = \text{ACTAC}$  can be generated.

## <span id="page-4-0"></span>**4 Mining distinguishing subsequence patterns with the nonoverlapping condition**

In this section, we introduce the special designed data structure at first. Then we present our algorithm. Finally, we analyze the space and time complexities of our algorithm.

Under the nonoverlapping condition, there are two problems: (1) how to effectively identify the character in a sequence that can be reused by applying a nonoverlapping support, and (2) how to quickly prune out candidate patterns that cannot exist to avoid calculating a large number of irrelevant patterns. To solve these two problems, we use a feature of a Nettree to calculate the support, that is, we allow the same node label to appear many times at different levels, which can effectively identify whether characters in the sequence can be reused. We use the pattern growth approach to minimize the support calculation of irrelevant patterns.

**Definition 15** (*Nettree*) A Nettree [\[24](#page-11-23)[–26\]](#page-11-24) is a type of data structure that is similar to a tree, and consists of a root, leaf, level, parent, child, and so on. Nevertheless, a Nettree is clearly different from a tree data structure based on the following characteristics:

- (1) A Nettree may have one or more roots, where  $n > 1$ .
- (2) Any node except a root may have more than one parent, but all parents must appear at the same level.
- (3) The same node label can appear at different levels. Node *i* in the *j*th level can be described as  $n_j^i$ .

(4) There may be more than one path from one node to its ancestor.

<span id="page-5-0"></span>**Definition 16** (*root-leaf* path) A path from a root to the termination of the leaf is called a root-leaf path.

**Lemma 2** *An occurrence of pattern P in sequence S can be expressed as a root-leaf path in a Nettree.*

*Proof* Our previous work [\[24](#page-11-23)] proved that each occurrence of pattern *P* in sequence *S* can be transformed into a root-leaf path in a Nettree, that is, each occurrence can be expressed as a root-leaf path. 

<span id="page-5-3"></span>**Lemma 3** *Let A and B be two root-leaf paths that do not contain any of the same nodes. The corresponding occurrences of A and B are two nonoverlapping occurrences.*

*Proof A* and *B* are <  $n_1^{a_1}$ ,  $n_2^{a_2}$ , ...,  $n_m^{a_m}$  > and <  $n_1^{b_1}$ ,  $n_2^{b_2}$ , ...,  $n_m^{b_m}$  >, respectively. For all  $i(1 \le i \le m)$ ,  $a_i$  is not equal to  $b_i$ , because  $A$  and  $B$  do not contain the same node. Therefore,  $\langle a_1, a_2, ..., a_n \rangle$  and  $\langle b_1, b_2, ..., b_n \rangle$  are two nonoverlapping occurrences. 

#### <span id="page-5-4"></span>**Lemma 4** *If a non-leaf node does not have any children, it can be safely pruned.*

**Proof** Supposing node  $n_j^i$  is a non-leaf node in a Nettree without any children, then node  $n_j^i$  cannot reach the leaf. Therefore,  $n_j^i$  is an invalid node and should be pruned. After pruning  $n_j^i$ , we should also check whether its parent nodes have other children. A node with no child should also be  $p$ runed.  $\Box$ 



<span id="page-5-2"></span>**Fig. 1** The corresponding Nettree of Example [7](#page-5-1)

<span id="page-5-1"></span>We use the following example to illustrate how the algorithm works.

*Example 7* Given sequence  $S = s_1 s_2 s_3 s_4 s_5 s_6 s_7 s_8 s_9 s_{10} s_{11} s_{12}$  $s_{13} s_{14} s_{15}$  = ATTCGATGCAATGAG and pattern  $P =$ A[0, 2]T[0, 2]G[0, 2]A, the Nettree shown in Fig. [1](#page-5-2) can be created.

Using the Nettree in Fig. [1,](#page-5-2) we can obtain three root-leaf paths:  $\langle n_1^1, n_2^2, n_3^5, n_4^6 \rangle$ ,  $\langle n_1^6, n_2^7, n_3^8, n_4^{10} \rangle$  and  $\langle n_1^{10}, n_2^{12}, n_3^{13},$  $n_4^{14}$ . According to Lemma [3,](#page-5-3) there are three nonoverlapping occurrences. As can be seen from Fig. [1,](#page-5-2) node  $n_2^3$  has no child and is an invalid node. Hence,  $n_2^3$  can be pruned by combining with Lemma [4.](#page-5-4) As we can see, the character at position 6 are reused in  $\langle n_1^1, n_2^2, n_3^5, n_4^6 \rangle$  and  $\langle n_1^6, n_2^7, n_3^8, n_4^{10} \rangle$  since position 6 is different in the two occurrences with nonoverlapping condition. Namely, if a character appears at different levels in the Nettree, then it can be reused.

An algorithm, called Support, which computes the support of *P* in *S*,*sup*(*P*, *S*), is shown in Algorithm 1. Because Support is used for calculation support, in other words, it is used for mining occurrences, we prune the invalid nodes while mining the occurrences of *P*.



The NOCM algorithm first scans a sequence at a particular time to generate the event set  $\Sigma$ . It then generates candidate patterns in positive database using the prefix-suffix connection method on the basis of  $\Sigma$ , and uses Nettree to calculate the support. Based on the nature of the Nettree, it is known that the number of levels in the Nettree is equal to the length of the patterns, and a complete path from the root to the leaf represents an occurrence of *P* in the sequence with the root to the leaf satisfying the gap constraint. Frequent patterns generated in the positive database are used as the candidate patterns of the negative mining, and the distinguishing sequence patterns are finally generated.

<span id="page-6-0"></span>**Theorem 1** *During the process of frequent pattern mining, if pattern P is infrequent, then any of its super patterns is infrequent.*

*Proof* Mining in a positive database is the mining of frequent patterns of the nonoverlapping condition. Suppose that  $sup(P)$  is the support of pattern *P*, *minsup*(*D*) is the average support rate threshold. If *P* is infrequent, namely,  $sup(P)$  < *minsup*( $D$ ), then when element  $e$  is added to pattern  $P$ , the generated super pattern (*eP* or *Pe*) occurrences cannot be more than the original pattern *P*, and must be less than or equal to the occurrences of the original model. 

The following example illustrates the principle of the NOCM algorithm.

**Example 8** We mine the distinguishing subsequence patterns with the nonoverlapping condition in sequence database *D* shown in Table [3](#page-4-1) and the selected parameters are the gap  $\text{constant} = [0,2]$ ,  $\text{minsup}(D+) = 0.25$ , and  $\text{maxsup}(D-) =$ 0.1.

First, we compute the average support rate for the patterns in  $\Sigma$ . We know that  $r(A, D+) = 0.22$  is less than *minsup*( $D+$ ). According to Theorem [1,](#page-6-0) all super patterns of "A" are also infrequent, thereby pruning "A" and its super patterns. Since  $r(T, D+) = 0.37$  is greater than  $minsup(D+)$ , pattern "T" which is stored is a frequent pattern in positive class. Similarly, we prune pattern "C" and its super patterns, and store pattern "G" since  $r(C, D+)$  and  $r(G, D+)$  are 0 and 0.63, respectively. Then we can generate the candidate patterns in positive class {TG, TT, GG, GT} with length of 2 by "T" and "G". We know that  $r(TG, D+) = 0.40$ ,  $r(TT, D+) = 0.20, r(GG, D+) = 0.56$ , and  $r(GT, D+) =$ 0.44. Therefore, pattern "TT" and its supper patterns are pruned since  $r(TT, D+)$  is less than  $minsup(D+)$ . Repeat this process until there is no new frequent pattern in positive class generated. After that, we compute the support rate for these negative candidate patterns. The pattern will be a distinguishing subsequence pattern if its average support rate is less than  $maxsup(D-)$ . Here,  $r(G, D−)$  and  $r(T, D−)$  are 0.2 and 0.3 separately which are more than *maxsup*(*D*−), so they are not distinguishing patterns. Both *r*(TG, *D*−) and  $r(GG, D-)$  are 0 which are less than  $maxsup(D-)$ , thus "TG" and "GG" are distinguishing patterns. Using this method, we find eight distinguishing patterns: "GG", "TG", "GGG", "GGT", "GTG", "TGG", "GGTG" and "GTGG".

We describe the detailed procedures of the NOCM algorithm in Algorithm 2 which employs the Apriori property to prune candidate patterns in *D*+.



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Algorithm 3 is proposed to generate candidate patterns in positive class.

to *Lemma* [4,](#page-5-4) in the  $(m - 1)$ th level we may prune w nodes at most since each node has at most w parents. Similarly, at



**Theorem 2** *Let m, n, w, l<sub>pos</sub>, l<sub>neg</sub> and r be the maximal length of a pattern, the maximal length of a sequence in the database SDB, b* −*a* +1 *(where a and b are the minimal and maximal gap constraint), the number of the positive class candidate patterns, the number of the negative class candidate patterns,* and the size of  $\Sigma$ , respectively. Then the space complexity of *NOCM is*  $O(m \times (n \times w + l_{pos}))$  *in the worst case and*  $O(m \times (n \times w/r/r + l_{pos}))$  *in the average case.* 

*Proof* The maximal length of candidate and mined pattern is  $O(m)$ . The space complexity of frequent and candidate patterns in positive class is  $O(m \times l_{pos})$ . *Algorithm* 1 employs a Nettree to calculate the support of a pattern in a sequence. In the worst case, the Nettree has no more than *m* levels, each level has no more than *n* nodes, and each node has no more than w children. Thus it can be concluded that the space and time complexities of creating a Nettree are both  $O(m \times n \times w)$ . So the space complexity of NOCM mined in positive class is  $O(m \times (n \times w + l_{pos}))$  in the worst case. The space complexity of mined patterns in negative class which is  $O(m \times l_{\text{neg}})$  can be neglected compared with the space complexity of frequent patterns in positive class since *lneg* is less than *l pos*. Therefore, the space complexity of NOCM is  $O(m \times (n \times w + l_{pos}))$ . In addition, each level has no more than  $n/r$  nodes and each node has no more than  $w/r$  children in the average case. Hence, the space complexity of NOCM is  $O(m \times (n \times w/r/r + l_{pos}))$  in the average case.  $\Box$ 

**Theorem 3** *The time complexity of NOCM is*  $O(m \times m \times n \times n)$  $w \times l_{pos}$ ) in the worst case and  $O(m \times m \times n \times w \times l_{pos}/r/r/r)$ *in the average case, where m, n,* w*, l pos, and r are given above.*

*Proof* The complexity of *Algorithm* 3 is  $O(l_{pos} \times \log l_{pos})$ since it employs binary search. We know that the time complexity of creating Nettrees is  $O(m \times n \times w)$  from the above theorem and the nonoverlapping occurrences are no more than *n*. Apparently, the depth of the Nettree is *m*. According most 2  $\times$  w nodes in the  $(m - 2)$ th level could be pruned. Thus, there are  $O(m \times m \times w)$  nodes could be deleted at most. Therefore, the time complexity of lines 5 to 12 in NOCM is  $O(m \times n \times w + m \times m \times n \times w) = O(m \times m \times n \times w)$ . There are *l pos* candidate patterns in positive class, so the time complexity is  $O((n \times m \times n \times w + \log l_{pos}) \times l_{pos}) =$  $O(n \times m \times n \times w \times l_{pos})$  in the worst case. Similarly, the time complexity of computing negative candidate patterns which is  $O(n \times m \times n \times w \times l_{neg})$  can be neglected compared with  $O(n \times m \times n \times w \times l_{pos})$  since  $l_{neg}$  is less than  $l_{pos}$ . Hence, the complexity of NOCM is  $O(n \times m \times n \times w \times l_{pos})$ . Moreover, as mentioned in the space complexity, the time complexity of NOCM is  $O(m \times m \times n \times w \times l_{pos}/r/r/r)$  in the average  $\Box$ case.  $\Box$ 

### <span id="page-7-0"></span>**5 Experimental results and analysis**

In this section, we will demonstrate the correctness and efficiency of our algorithm with extensive experiments. All experiments were conducted on a computer with an Intel(R) Core(TM) i5-3210M 2.50 GHz CPU and 8.0 GB of RAM running the 64-bit version of Windows 7. VC++ 6.0 was used in the development of all algorithms applied, including NOCM and NOSEP. The data used in the experiments are DNA sequences and time-series data. The real DNA sequences were extracted from [http://dbtss.hgc.jp/,](http://dbtss.hgc.jp/) and original time-series data can be obtained from [www.cs.ucr.edu/](www.cs.ucr.edu/~eamonn/time_series_data/) [~eamonn/time\\_series\\_data/.](www.cs.ucr.edu/~eamonn/time_series_data/)

#### **5.1 Efficiency**

We conducted several experiments on five groups of timeseries data and a set of DNA sequences. NOCM is compared with NOSEP based on the number of patterns and the running time. Each group of experiments uses the same length

<span id="page-8-0"></span>



Number of patterns mined using the two algorithms

constraint. Because NOSEP mines frequent patterns, for all sequences under a single class, only the minimum average support threshold *minsup* needs to be set. NOCM needs to set the positive average support rate threshold  $minsup(D+)$ and negative maximum support rate threshold *maxsup*(*D*−). To unify the standard and make the experiment comparable, it is necessary to keep *minsup* and  $minsup(D+)$  consistent.

Figure [2](#page-8-0) shows the number of patterns mined using NOSEP and NOCM with gap constraint [0,2], using the threshold of each parameter shown in Table [4.](#page-8-1)

From Fig. [2,](#page-8-0) we can see that the number of distinguishing patterns is generally much less than the number of frequent patterns. In addition, with a decrease in  $minsup(D+)$ , the number of distinguishing patterns gradually increases. For WormsTwoClass, NOSEP mines 99 frequent patterns when *minsup* is 0.01, whereas NOCM mines eight distinguishing patterns at the corresponding threshold. Under a condition in which the parameter setting is reasonable, the number of patterns mined by NOCM is less than NOSEP. Thus, redundant patterns can be effectively reduced, and the secondary selection of features in the sequence classification is avoided.

It is possible for the number of distinguishing patterns to be greater than or equal to the number of frequent patterns under certain threshold conditions. For dataset inp100 in Fig. [2,](#page-8-0) NOCM mines eight distinguishing patterns, whereas NOSEP mines nine frequent patterns when *minsup*/*minsup*( $D$ +) is 0.12 and *maxsup*( $D$ −) is 0.1. This is due to patterns appearing in a positive class far more frequently than in a negative class when the difference between the positive and negative classes is obvious, and thus its support will be averaged in frequent pattern mining, leading to a frequent decrease in support. Thus, the pattern cannot be a frequent pattern. However, it is precisely in line with a distinguishing pattern, resulting in the above phenomenon. In most cases, NOCM can be very good at finding significant distinguishing patterns.

Figure [3](#page-9-0) shows the running time of NOSEP and NOCM with a gap constraint of [0, 2], and the threshold parameters shown in Table [4.](#page-8-1)

From Fig. [3,](#page-9-0) we can see that NOCM is fast when the gap constraint and *minsup*/*minsup*(*D*+) are the same, and takes far less time than NOSEP. As *minsup*(*D*+) increases, the time required for mining becomes increasingly shorter. This illustrates that the speed of NOCM has a significant advantage owing to the use of a Nettree, which avoids backtracking in the mining process and reduces the time consumption.

<span id="page-8-1"></span>**Table 4** Threshold parameter table used in the comparison experiment



*len*<sup>1</sup> and *gap*<sup>1</sup> are the length and gap constraints of NOSEP respectively, and *len*<sup>2</sup> and *gap*<sup>2</sup> are the length and gap constraints of NOCM

<span id="page-9-0"></span>

<span id="page-9-1"></span>**Table 5** Corresponding number of features of different feature extraction approaches



– indicates that this threshold does not need to be set

#### **5.2 Classification effect**

A distinguishing subsequence pattern can show well how things change under the different classes or conditions, and focuses on the differences in different datasets. Therefore, in this paper, we propose a feature extraction approach based on a distinguishing subsequence pattern. Breaking from a single situation of frequent patterns as the classification features [\[27](#page-11-25)[–29](#page-11-26)], a new direction for feature extraction is provided.

The number of features used in the experiment and the corresponding feature extraction thresholds are shown in Table [5.](#page-9-1)

To verify the classification effect, we use the K-NN classifier to conduct experiments on a binary classification sequence database and compare it with the frequent patterns as features. The classification effect is evaluated based on the training and prediction accuracies, shown in Figs. [4](#page-10-1) and

[5,](#page-10-2) respectively. Clearly, the feature extraction approach with NOCM obtains a better classification effect and has a higher accuracy in different datasets. In general, the accuracy of its classification is better than feature extraction with NOSEP.

It can be seen from Figs. [4](#page-10-1) and [5](#page-10-2) that the classification accuracy of the two feature extraction approaches is basically the same, but training accuracy and prediction accuracy have significantly improved with choosing distinguishing subsequence patterns as classification features. For example, from the BeetleFly dataset in Figs. [4](#page-10-1) and [5,](#page-10-2) we can know that the training accuracy of the two feature extraction methods of NOSEP and NOCM is 95.0 and 100.0% respectively, and the prediction accuracy is 70.0 and 95.0% respectively. Mean-while, combined with Table [5,](#page-9-1) we can see that NOCM only used 11 features, whereas NOSEP used 34 features. Experimental results on each data set show that a relatively small number of distinguishing subsequence patterns can be used

<span id="page-10-1"></span>**Fig. 4** Comparison of the classification accuracy in

training sets



BirdChicke

 $\mathbf n$ 

70.0%

80.0%

**BeetleFly** 

70.0%

95.0%

<span id="page-10-2"></span>**Fig. 5** Comparison of the classification accuracy in testing sets

to achieve higher accuracy. Therefore, NOCM which can find the most distinguishing patterns is an effective feature extraction than the competitive method.

80.0%

70.0%

60.0%

NOSE<sub>P</sub>

NOC<sub>M</sub>

inp100

73.6%

76.0%

## <span id="page-10-0"></span>**6 Conclusion**

Existing distinguishing subsequence patterns mining algorithms pay less attention to the sequences in a database, and if long sequences appear in a database, or if the number of positive and negative sequences is not equal, the mining result will be unreasonable. In view of this problem, an effective distinguishing mining algorithm with the nonoverlapping condition, called NOCM, was proposed in this paper. NOCM not only can reduce redundant patterns, it can also pay attention to the proportion of patterns in each sequence and the entire database. This prevents the number or length of the sequences to have impact on the patterns, and makes distinguishing subsequence patterns more significant and reasonable. We also proposed a new feature extraction approach that employs nonoverlapping distinguishing subsequence patterns as features of a sequence classification. Extensive experimental results demonstrate the efficiency of NOCM, and a good classification effect was shown on a standard binary classification database.

Earthquake

78.3%

81.1%

As future work, more effective mining algorithm could be studied and better pattern mining method for feature extraction could be investigated, so as to improve the performance of classification.

WormsTw

oClass

71.5%

73.5%

Gun Point

76.1%

78.0%

**Acknowledgements** The work was supported in part by the National Natural Science Foundation of China under Grant 61673159, in part by the Natural Science Foundation of Hebei Province under Grant F2016202145, in part by the Science and the Technology Project of Hebei Province under Grant 15210325, and in part by the Graduate Student Innovation Program of Hebei Province under Grant CXZ-ZSS2017037.

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