ORIGINAL PAPER

# Idealized powder diffraction patterns for cellulose polymorphs

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Received: 3 May 2013 / Accepted: 13 August 2013 / Published online: 25 August 2013 © Springer Science+Business Media Dordrecht (outside the USA) 2013

Abstract Cellulose samples are routinely analyzed by X-ray diffraction to determine their crystal type (polymorph) and crystallinity. However, the connection is seldom made between those efforts and the crystal structures of cellulose that have been proposed with synchrotron X-radiation and neutron diffraction over the past decade or so. In part, this desirable connection is thwarted by the use of different conventions for description of the unit cells of the crystal structures. In the present work, powder diffraction patterns from cellulose I $\alpha$ , I $\beta$ , II, III<sub>I</sub>, and  $III<sub>II</sub>$  were calculated based on the published atomic coordinates and unit cell dimensions contained in modified "crystal information files" (.cif) that are supplied in the Supplementary Information. The

Manuscript prepared for Cellulose, Special Issue from the symposium, "100 Years of Cellulose Diffraction," 245th National Meeting, American Chemical Society (presented in part at the symposium, ''From Cellulose Raw Materials to Novel Products: Anselme Payen Award Symposium in Honor of Hans-Peter Fink'').

Electronic supplementary material The online version of this article (doi[:10.1007/s10570-013-0030-4\)](http://dx.doi.org/10.1007/s10570-013-0030-4) contains supplementary material, which is available to authorized users.

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calculations used peak widths at half maximum height of both 0.1 and  $1.5^{\circ}$  2 $\theta$ , providing both highly resolved indications of the contributions of each contributing reflection to the observable diffraction peaks as well as intensity profiles that more closely resemble those from practical cellulose samples. Miller indices are shown for each contributing peak that conform to the convention with  $c$  as the fiber axis, a right-handed relationship among the axes and the length of  $a < b$ . Adoption of this convention, already used for crystal structure determinations, is also urged for routine studies of polymorph and crystallinity. The calculated patterns are shown with and without preferred orientation along the fiber axis. Diffraction intensities, output by the Mercury program from the Cambridge Crystallographic Data Centre, have several uses including comparisons with experimental data. Calculated intensities from different polymorphs can be added in varying proportions using a spreadsheet program to simulate patterns such as those from partially mercerized cellulose or various composites.

Keywords Cellulose crystal structure - Miller indices - Powder diffraction patterns - Convention

## Introduction

Not only is cellulose arranged in small crystals, but there are several different crystal forms (polymorphs)

that depend on the history of the sample. Diffraction studies, which depend on more or less periodic arrays of atoms, are one of the most common analyses conducted on cellulose. These studies are used for many purposes, ranging from refinement of atomic positions and delineation of the hydrogen bonding systems to routine determination of the polymorph or degree of crystallinity.

The detailed refinements of atomic positions based on more than a hundred diffraction intensity values taken from fiber diffraction patterns (Nishiyama et al. [2002,](#page-10-0) [2003](#page-10-0); Langan et al. [2001](#page-10-0); Wada et al. [2004,](#page-10-0) [2009\)](#page-10-0) have been of great benefit to the knowledge of cellulose. By replicating the unit cells of these crystals, three-dimensional models of the crystals can be readily constructed and subjected to calculations of various sorts, allowing comparisons of observed experimental properties with those calculated on the basis of the model cellulose structures. For example, vibrational and NMR spectra can be calculated (Kubicki et al. [2013](#page-10-0)), perhaps for validation or attempts at resolution of the structure of remaining non-crystalline material. Another use of such models would be for calculation of various mechanical properties such as deformability that allow determination of ideal values (Wohlert et al. [2012\)](#page-10-0). Such calculations, however, can be regarded as topics for specialists who are expected to be competent users of the various tools for manipulating data from crystal structure studies.

More often, perhaps thousands of times per year, powder diffraction data are collected from cellulose for determination of the sample's specific polymorph or its degree of crystallinity. The resulting information provides important characterization and information on the consequences of various applied treatments. These analyses are conducted with varying levels of effort and understanding. One task that often accompanies these analyses is the assignment of Miller indices to the various peaks. Assignment is complicated to a degree because various conventions have been used over the years to designate the unit cell dimensions. Early work (Meyer and Misch [1937\)](#page-10-0) proposed a unit cell for cellulose I with  $a = 8.35$  Å, b (fiber axis) = 10.3 Å,  $c = 7.9$  Å and a monoclinic angle of  $\beta = 84^{\circ}$ . However, perhaps to facilitate comparative discussions of polymers that have several space groups, the molecular axis for cellulose is now

considered to be  $c<sup>1</sup>$ . In both small molecule and polymer crystallography, the convention now is to use an obtuse monoclinic angle  $(\gamma$  for polymers), but early cellulose structures were instead based on an acute  $\beta$ angle. Even within the convention with an obtuse monoclinic angle and c as the fiber axis, Gardner and Blackwell ([1974\)](#page-10-0) defined their unit cell with  $a = 8.17 \text{ Å}$  and  $b = 7.86 \text{ Å}^2$ , whereas the work of Woodcock and Sarko  $(1980)$  $(1980)$  used 7.78 Å for a and 8.20  $\AA$  for  $b$ . These differing conventions result in varying Miller indices being assigned to most peaks on the diffraction pattern. From an editor's perspective, both authors and reviewers have been caught up in these varied conventions, to the extreme point that reviewers have demanded rejection of a manuscript because the authors had used a convention different from the one that the reviewers had seen somewhere along the way. Some current submissions to Cellulose and other journals regarding polymorph identification and crystallinity measurements continue to base their Miller indices for cellulose I on the conventions used by Meyer and Misch, while some others use the also obsolete one of Gardner and Blackwell.

It would seem to be an improvement if there were adoption of a single convention by both the fiber and powder diffraction communities, with the understanding that the selection of convention is a choice and that other choices were made in the past. Perhaps a more important consequence from standardizing on one convention that is used in both routine powder patterns and advanced fiber crystallography is that it expedites conversations between those two spheres of scientific endeavor. Zugenmaier ([2008\)](#page-11-0) has seconded our earlier proposal (French et al. [1987](#page-10-0); French and Howley [1989\)](#page-10-0) that shows the unit cell with the  $c$ -axis vertical. the a-axis directed towards the viewer and the b-axis towards the right, with  $a$  being shorter than  $b$ . In turn

 $1$  Consider the conversion of a structure with twofold molecular symmetry to one with fourfold symmetry. In the case of the twofold axis and monoclinic space group, there would be no logical problem with using b, but for the fourfold case and a tetragonal space group, two of the axes are the same. There, the undisputed convention is to have  $a$  and  $b$  equal, with  $c$  unique (Klug and Alexander [1974\)](#page-10-0). If the monoclinic structure also uses the  $c$ -axis as parallel to the molecular axis, then one can compare the  $c$ -axis dimensions of the two different molecules.

<sup>2</sup> Their reported dimensions were for an 8-chain unit cell although their reported structure has a two-chain cell. Their values have been divided by two in this work to represent their two-chain cell.

that was grounded in statements by Klug and Alexander [\(1974](#page-10-0)) and used by Woodcock and Sarko [\(1980](#page-10-0)).

In the past few years, we (Nishiyama et al. [2012\)](#page-10-0) have taken advantage of the availability of the x, y, and z atomic coordinates from the crystal structures to calculate both powder and fiber diffraction patterns for cellulose. These calculations were based on different sizes of crystals, either from the coordinates of one asymmetric unit in the unit cell, using the Mercury program (Macrae et al. [2008](#page-10-0)) or from crystal models that had various shapes, sizes and amounts of water or deviation from a perfect lattice that resulted from molecular dynamics studies. The latter calculations were carried out with either the Debyer software for powder patterns (Wojdyr [2011\)](#page-10-0), or custom software by Dr. Nishiyama for fiber patterns (Nishiyama et al. [2012\)](#page-10-0). These efforts are beginning to provide an atomistic visualization of cellulosic materials.

The present work is based only on the Mercury 3.0 program, which is available in both free download and full-capability versions (Macrae et al. [2008](#page-10-0)). This program requires the unit cell dimensions and the fractional atomic coordinates of the asymmetric unit to instantly produce a powder pattern. The primary goal here is simple, namely to present the calculated diffraction patterns from the different polymorphs with the recommended indexing. With an input peak width at half maximum height (pwhm) of  $1.5^{\circ}$  2 $\theta$ , a pattern can be calculated that resembles an experimental pattern from a fairly crystalline sample of practical interest. By also using the Mercury's default pwhm value of  $0.1^{\circ}$  2 $\theta$ , a pattern is calculated that is much sharper than will be attained with any cellulose sample, but it resolves the peaks to show them mostly without overlap. Powder diffraction patterns are sometimes subjected to deconvolution during analysis, with arbitrary choices of the contributing peaks. A secondary goal of the present work is to show, based on the calculated patterns having narrow peak widths, which peaks should be considered during deconvolution.

Another facility of the Mercury program (paid licenses only) is to account for preferred orientation of the sample. Because of the aspect ratio of cellulose fiber fragments that are used as samples for powder diffraction, it is difficult to avoid some degree of preferred orientation. Therefore, patterns were calculated both with and without preferred orientation along the c-axis. Not only is preferred orientation difficult to avoid in experiments on cellulose, but it was originally recommended when calculating the Segal crystallinity index analysis (Segal et al. [1959](#page-10-0); French and Santiago Cintro $(2013)$  $(2013)$ . In the latter paper, the pattern from the oriented cellulose  $I\beta$  sample was indicated to have a slightly higher Segal Crystallinity Index than for the random pattern. None of the information herein is particularly novel or unique, but the idea here is to present a practical visual indication of the Miller indices of the often overlapped peaks and their approximate proportions.

#### Input information

Crystal information files (.cif) for cellulose I $\alpha$  and I $\beta$ were obtained from the Supplementary Information accompanying the original reports (Nishiyama et al. [2002,](#page-10-0) [2003](#page-10-0)). Those files contain both X-ray and neutron structures. (These structures are also found in the Cambridge Crystallographic Database with Refcodes PADTUL and PADTUL01 (cellulose Ia) and JINROO01 and JINROO02 (cellulose  $I\beta$ ).) The X-ray coordinates have no hydroxyl hydrogen atoms present and the neutron diffraction coordinates have deuterium atoms in the positions of the hydroxyl hydrogen atoms. The Supplementary Information includes modified.cif files for cellulose  $I\alpha$  and I $\beta$  that eliminate the coordinates from the X-ray study and other information not needed for the calculation of powder patterns. The deuterium atoms of the neutron studies are renamed as hydrogen atoms. That was done to avoid any effect on the pattern from the presence of deuterium. Because the original.cif for Ia was reported with  $a$  as the fiber axis (the main original article reported  $c$  as the fiber axis), the revised.cif file in Supplementary Information has coordinates that were transformed so that  $c$  is the fiber axis. If the.cif file were to be used for constructing models to be studied with energy calculations, only the A or B scheme hydrogen atoms should be used. For calculations of the X-ray pattern, the A and B atoms should be used. Small differences can be observed in the calculated patterns when they are not included.

A .cif file for the cellulose II structure (Langan et al. [2001\)](#page-10-0) was kindly sent by Dr. Langan and a shortened version is supplied in Supplementary Information. The .cif files for cellulose  $III_I$  and  $III_{II}$  were created manually from the published coordinates (Wada et al.

[2004,](#page-10-0) [2009](#page-10-0), respectively) and the minimum of information needed for a functional .cif. Those files are also provided as Supplementary Information.

The default calculated powder patterns were customized with a CuK $\alpha$  wavelength of 1.5418 Å, typically used in powder diffractometers. Pwhm values of 0.1 and  $1.5^{\circ}$  2 $\theta$  were used. The intensity vs. 2 $\theta$  data were saved and re-plotted with plotting software to make combined plots. The cropped bitmap image of the expected peak positions from the Mercury powder plots was copied and pasted onto the plots in a drawing program. Miller indices were obtained from a list of reflections produced by Mercury and manually added to the expected peak positions. Preferred orientation was also part of the customization process in Mercury, with a March-Dollase factor of 1.8 (Dollase [1986](#page-10-0)) applied to the (001) plane for the monoclinic structures. In the case of triclinic I $\alpha$ , specification of the (001) plane resulted in increases in many of the intensities relative to the main (110) peak. Earlier versions of this paper attempted to explain this behavior that was opposite to the results for the monoclinic structures. Ultimately it was realized that the problem was that the (001) plane was not normal to the molecular axis for the triclinic structure, unlike the situation for the monoclinic structures. Specifying the (001) plane in the Mercury customization data window did not therefore result in preferred orientation of the fiber axes as intended. Instead, the plane to specify was  $(11-4)$ , which has an interplanar spacing of 2.596  $\AA$ , very close to c/4. Thus, the only preferred orientation modeled was for fibrous samples where the fiber axes were in a plane parallel to the sample surface, and the crystallites were randomly oriented about the fiber axes. Samples of bacterial cellulose, for example, can have additional orientation about the fiber axis, causing the (100) peak to be nearly absent from I $\alpha$  patterns.

### Results and discussion

Figure [1](#page-4-0)a, b show the calculated patterns from cellulose Ia, based on the modified .cif file in the Supplementary Information. Unit cell dimensions were:  $a = 6.717 \text{ Å}, b = 5.962 \text{ Å}, c = 10.400 \text{ Å},$  $\alpha = 118.08^{\circ}, \beta = 114.80^{\circ}, \text{ and } \gamma = 80.37^{\circ}$  (Nishiyama et al. [2003\)](#page-10-0). The modifications involved interchange of the unit cell dimensions to match a convention with the c-axis parallel to the molecular axis. Although the unit cell dimensions listed in their published report (Nishiyama et al. [2003](#page-10-0)) are the same as used herein, their structure determination was carried out with the a-axis parallel to the molecular axis, and the coordinates in their supplementary .cif file are based on that convention. The three main peaks for the I $\alpha$  one-chain triclinic unit cell have Miller indices of (100), (010) and (110) (which are the counterparts to the  $(1-10)$  (110) and (200) peaks of the cellulose  $I\beta$  pattern).

The simulated patterns from the randomly oriented and preferred orientation samples are noticeably different, but after simulating the orientation of the (11–4) plane (see last paragraph of Input information, above) set the pattern for the effects of preferred orientation for the other samples. The intensities of the non-equatorial reflections, mostly weak in the random pattern, nearly disappear. Note also that the weak (001), (002), and (003) peaks on the I $\alpha$  pattern at 10.48°, 21.05°, and 31.8 $^{\circ}$  2 $\theta$ , have d-spacings of 8.44, 4.22, and 2.81 Å, respectively. They do not correspond to divisions of the 10.40  $\AA$  c-axis dimension by 1, 2, and 3, as would be the case for a monoclinic structure. The (004) reflection is beyond the  $40^{\circ}$  2 $\theta$  cut-off. Finally, the present unit cell admittedly does not conform to conventions that call for all triclinic cell angles to be greater than 90°. Here, priority was given to having the  $c$ -axis match the molecular dimension.

Figure [2a](#page-5-0) shows the calculated diffraction patterns for randomly oriented powder samples of cellulose  $I\beta$ , and Fig. [2](#page-5-0)b presents the patterns for  $\iota$ B samples with preferred orientation along the c-axis. Unit cell dimensions were:  $a = 7.784 \text{ Å}, b = 8.201 \text{ Å},$  $c = 10.380$  Å, and  $\gamma = 96.55^{\circ}$  (Nishiyama et al. [2002\)](#page-10-0). As previously stated (French and Santiago Cintrón, [2013](#page-10-0)), both simulated diffraction curves correspond to perfect crystals. The difference in the simulated intensity profiles is strictly the result of different crystallite sizes, and the ''background'' level around  $18^{\circ}$  2 $\theta$  for the curves with  $1.5^{\circ}$  2 $\theta$  pwhm results from overlap of the diffraction peaks. On these simulated patterns, there is no modeling of amorphous scattering. Therefore, in various calculations of cellulose crystallinity, it is generally not appropriate to position a background intensity curve (attributed to amorphous scattering) as high as the minimum intensity at 18° 2 $\theta$ . The shoulder at about 20.5° 2 $\theta$ for the (012) and (102) reflections on the random pattern is not obvious on the pattern with preferred

<span id="page-4-0"></span>

Fig. 1 a Simulated cellulose Ia powder pattern for randomly oriented crystallites with  $0.1^{\circ}$  and  $1.5^{\circ}$  peak widths at half maximum intensity. Magenta lines indicate the positions of the calculated peaks, and the black vertical lines on the scale correspond to the 5° intervals. The image was prepared with the

orientation. The positions of the absent, odd-order  $[(001)$  and  $(003)]$  meridional reflections are indicated by green lines above their green Miller indices instead aid of the Mercury program (see text) which output files with the intensities and the Miller indices; the magenta lines were taken from the saved image of the powder pattern from the Mercury program. b Cellulose Ia with crystallites having preferred orientation along the fiber axis

of the purple lines for the other reflections. The main contributors of intensity to the three main peaks have Miller indices of  $(1-10)$ ,  $(110)$  and  $(200)$ . The

<span id="page-5-0"></span>

Fig. 2 a Cellulose I $\beta$  with random (a) orientation of the crystallites. b Cellulose I $\beta$  with preferred orientation of the crystallites along the fiber axis

moderate peak on the random  $1.5^{\circ}$  pwhm curve near  $34.5^\circ$  is seen to be a composite of several reflections and (004) is not the dominant contributor.

These Miller indices  $[(1-10)$  and  $(110)]$  for the peaks at  $14.88^{\circ}$  and  $16.68^{\circ}$  2 $\theta$  are the same as those used by Gardner and Blackwell ([1974\)](#page-10-0) despite their assignment of the  $a$ -axis to the 8.20 Å repeat and the  $b$ -axis to the 7.88  $\AA$  dimension. However, their assignments do interchange the indexing for the major peak, with Miller indices of (020) instead of the (200)

values promoted herein. Because of this difference, it was not immediately obvious that the chain packing in their unit cell was different from that in the monoclinic (MM subcell) unit cell from Syracuse (Sarko and Muggli [1974\)](#page-10-0). The packing in the Gardner and Blackwell cell corresponds to a ''down'' instead of ''up'' orientation of the molecules (French and Howley [1989\)](#page-10-0) for the unit cell used herein, whereas the packing is parallel up in Sarko and Muggli's structure and in the Nishiyama et al. ([2002\)](#page-10-0) structure.

Figure [3](#page-7-0)a, b show the patterns for cellulose II samples with random and preferred orientation. Unit cell dimensions were:  $a = 8.10 \text{ Å}, b = 9.03 \text{ Å},$  $c = 10.31$  Å, and  $\gamma = 117.10^{\circ}$  (Langan et al., [2001](#page-10-0)). Both the  $0.1^{\circ}$  and  $1.5^{\circ}$  patterns from the sample with preferred orientation are considerably simplified, compared to the random model, by the near absence of reflection intensities from upper layer lines. The three main peaks have Miller indices of  $(1-10)$ ,  $(110)$ and (020). The peak for the latter reflection, at about  $22.1^\circ$  2 $\theta$ , has contributions from two adjacent reflections. To ascertain which reflection is responsible for the majority of the intensity it was helpful to plot the diffraction pattern for only a small range, say from 19 to  $23^{\circ}$  2 $\theta$ , along with a step size of  $0.01^{\circ}$  2 $\theta$ . The window with the calculated diffraction patterns in the Mercury program can be stretched to the full width of the monitor as well. Note that this reflection (020) is often mistakenly labeled as (200)—e.g. Yue et al. [\(2012](#page-11-0)). The .hkl file that is output from Mercury also lists the intensities of the various reflections. For example, it gives the calculated intensity for the  $(1–10)$  reflection as 2480.7, and a value of 1.1 for the  $(100)$  peak, easily resolving that  $(1-10)$  is the dominant contributor to the peak at about  $12.2^{\circ}$   $2\theta$ .

The simulated patterns for cellulose  $III<sub>I</sub>$  are shown in Fig. [4](#page-8-0), based on unit cell dimensions of  $a = 4.45$  Å,  $b = 7.85$  Å,  $c = 10.33$  Å, and  $\gamma = 105.1^{\circ}$  (Wada et al. [2004](#page-10-0)). Because the cellulose  $III<sub>I</sub>$  structure has only a one-chain unit cell with twofold screw-axis symmetry, the number of reflections is limited, with only ten peaks possible before  $25^{\circ}$  2 $\theta$  (cellulose II has 19 and I $\alpha$  has 14). The difference between the patterns for random (Fig. [4a](#page-8-0)) and oriented samples (4b) is dramatic because of the strong presence of the (002) reflection on the random pattern, and its near absence on the pattern from the sample with preferred orientation. Because the peak at about  $21^{\circ}$  2 $\theta$  comprises the (100), (012) and (1–10) reflections with very strong contributions from (100) and (1–10), it is not well-suited for line profile analyses for crystallite size determinations.

Figure [5](#page-9-0) shows the results from the study of cellulose  $III_{II}$  by Wada et al. [\(2009](#page-10-0)). This one-chain unit cell with  $a = 4.45 \text{ Å}, b = 7.64 \text{ Å}, c = 10.36 \text{ Å},$ and  $\gamma = 106.96^{\circ}$  has fractional occupancy, with either an ''up'' or ''down'' chain in any given unit cell. The calculated patterns show very low intensity except for the peak at 12.1 $\degree$  2 $\theta$  and the composite of (1–10) and (100) peaks at  $20.863^{\circ}$  and  $20.869^{\circ}$  2 $\theta$ , respectively.

These results underscore the need to report the details of the sample preparation that would affect the orientation, such as whether the sample was a pressed pellet, or sprinkled onto sticky tape. Also, the presentation of the sample to the incident beam (transmission or reflection) should be stated as that can also affect the relative intensities of the various peaks.

The intensities and spacings on these calculated patterns will not totally agree with experimentally observed patterns for several reasons. The peak positions will not agree exactly, possibly because of crystallite size variations resulting in different longrange compressive forces on the crystals and unit cells (Nishiyama et al. [2012\)](#page-10-0). Knowing that the crystallographic discrepancy index (the  $R$  factor) values are about 20 % in the original crystallographic studies, the observed and calculated intensities are expected to differ. (A better indicator of expected differences in this case would be the discrepancy index  $wR^2$  based on the structure factors squared and weighted, values of which are about 45 %.) This expected deviation is why the title ''idealized powder diffraction patterns'' was chosen. The patterns calculated by Mercury are isotropic; there is no way to input crystallite shape information. That can affect the relative peak heights and widths. If the crystal structures are re-determined in the future, the appropriate figures herein should be replaced.

From the experimental side, it is almost impossible to obtain powder pattern samples with completely random orientation or complete orientation in a given direction. That could be compensated for by calculating patterns with varying values of the March-Dollase orientation parameter (Dollase [1986\)](#page-10-0). Another factor is the sample itself. It may not be pure, it may have minor amounts of another polymorph, and, especially when sample sizes are marginal, signals from the sample presentation system, such as adhesive tape may also occur. The latter problem should be easily corrected once identified. Some diffuse scattering

<span id="page-7-0"></span>

Fig. 3 a Simulated powder diffraction patterns for cellulose II crystallites having random orientation. b Simulated powder diffraction pattern for cellulose II with preferred orientation of the crystallites along the fiber axis

from non-crystalline material is also going to be present that is not taken into account by these calculations.

Of course, many samples of interest are likely to contain more than one crystal form, such as partially mercerized samples that would be mixtures of cellulose I and II. It is important to not try to interpret such patterns with an assumption that only one form is present. However, given the ability to calculate intensity versus  $2\theta$  data for the various polymorphs

<span id="page-8-0"></span>

Fig. 4 a Simulated powder diffraction pattern for cellulose  $III<sub>I</sub>$  with random orientation of the crystallites. b Simulated powder pattern for cellulose  $III_I$  with preferred orientation for the crystallites along the fiber axis

with a range of peak width values, it is simple to add together the intensity data (perhaps with a spreadsheet program) to obtain theoretical patterns for mixtures of either cellulose of different polymorphs or cellulose with other polysaccharides such as xylan (Nieduszynski and Marchessault [1972\)](#page-10-0) in composites.

<span id="page-9-0"></span>

Fig. 5 a Simulated powder diffraction pattern for cellulose  $III<sub>II</sub>$  with random orientation of the crystallites. b Simulated diffraction pattern for cellulose  $III<sub>II</sub>$  with preferred orientation of the crystallites about the fiber axis

## **Conclusions**

Ideal diffraction patterns were readily calculated with the Mercury program using as input the crystal information files (.cif) that are provided in the Supplementary Information. The patterns were presented for both very narrow, well-resolved peaks and for the broader peaks that are found for the most crystalline practical higher plant cellulose such as cotton. This graphical representation shows which <span id="page-10-0"></span>reflections are contributing to a given peak. Indexing for these peaks conforms to the modern nomenclature, with  $c$  as the fiber axis, an obtuse monoclinic angle, and the  $a$ -axis shorter than the  $b$ -axis. The Mercury program and the .cif files in Supplementary Information make it easy for even the novice to create calculated patterns for various purposes. For example, the calculated intensity versus  $2\theta$  data from various structures can be added in varying proportions to simulate diffraction patterns from partially mercerized samples or composite materials.

#### Supplementary information

Crystal information files (.cif) are provided for the five cellulose polymorphs described in this work. These files were either modifications of published or unpublished .cif files or created from the published unit cell parameters and coordinates by putting them into the .cif format. Readers are advised to copy the entire contents, starting with the line ''#Modified Crystal Information File for Ia cellulose'' into a text editor such as Microsoft Notepad and saving the file as e.g., "all\_cellulose.cif". The Mercury program will then allow any of the structures to be selected.

Acknowledgments Paul Langan kindly provided the .cif file for cellulose II. The research was partly inspired by collaborative efforts with Cotton, Incorporated. Drs. Santiago Cintrón, Seong Kim and Xueming Zhang kindly commented on preliminary versions of the manuscript. Dr. Edwin Stevens consulted on the effects of preferred orientation on the cellulose Ia pattern.

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