CRYOGENIC ENGINEERING, PRODUCTION AND USE OF INDUSTRIAL GASES, VACUUM ENGINEERING

VAPOR-LIQUID EQUILIBRIUM OF THE ETHYLENE–BUTANE MIXTURE

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The article deals with the investigation of the ethylene-butane natural gases mixture that is promising for practical application. A unit with a small volume cell created to obtain data on phase equilibria and thermal properties of binary mixtures of little investigated and rare substances using several experimental methods was presented. It is shown that it was possible to use non-standard measuring equipment to obtain sufficiently reliable results in a wide range of temperatures, pressures and compositions. Application of a new method to determine two-component gas mixtures concentration was demonstrated. The method of experimentation was described as well. The experimental results of ethylene–butane mixture thermal properties and vapor-liquid equilibrium that have expanded our knowledge in relation to this two-component natural refrigerant behavior in the low-temperature region and at high dilutions were tabulated. The comparison of the experimental and calculated data showed the possibility of applying the three-parameter cubic equation of state to simulate the thermodynamic properties of the ethylene–butane mixture without using test data of the mixture.

Keywords: vapor-liquid equilibrium, ethylene–butane mixture, natural refrigerant, equation of state, static method.

Modern low-parametric equations of state make it possible with limited initial information to predict the thermodynamic properties of substances for solving a number of technical problems [1]. However, in order to adequately describe the thermodynamic properties of the working fluid and to verify the quality of its model, experimental data are required in the temperature and pressure range typical for the production process.

The object of the study was a binary ethylene–butane ($C_2H_4-C_4H_{10}$) mixture of natural gases, which is a promising two-component working fluid of vapor-compression refrigeration systems to provide a cooling level of 190 K [2]. An analysis of published sources showed that the ethylene–butane system was experimentally studied mainly in the region of critical temperatures [3–5].

The limited field of research of this mixture and the promise of its use as a working fluid make it expedient to experimentally study its thermal properties at lower temperatures (173 to 273 K).

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Fig. 1. Experimental setup diagram: 1) vacuum pump; 2, 25) thermocouple pressure transducer; 3) gauge tank; 4) expansion tank; 5) nitrogen trap (cryogenic pump); 6, 11, 23) pressure transducer DD2.5; 7) pressure transducer D100; 8) thermocompressor (cryopump); 9, 24) gauge cylinder; 10) mass converter S-05; 12, 14, 16) pressure transducer D16; 13) cylinders with clean components; 15) separation vessel and mercury displacer; 17) equilibrium chamber; 18) cryostat; 19) mercury collection; 20) nitrogen-oil separator; 21) deadweight tester; 22) cylinder with liquid; 26) cylinder with CGS (calibration gas mixture); 27) nitrogen cylinder.

Experimental study. *Equipment*. The experimental setup (Fig. 1) allows to investigate the vapor-liquid equilibrium in a wide range of pressures (0.01 to 15 MPa), temperatures (77 to 450 K) and concentrations (from 0.0001 mol/mol). The measuring cell of the apparatus is a metal cylindrical vessel 17 with a volume of 15 cm³ with a magnetic stirrer, placed in a stabilizing copper block of the cryostat 18.

The design of the measuring cell is shown in Fig. 2. The vessel 2 is an austenitic chromium-nickel stainless steel (Kh18H9T) 18×1.5 mm tube with spherical bottoms, enclosed in a copper sheath 3 and placed in a copper temperature stabilizer 2 with sectional heaters 7, 21, 23 bifilarly wound around its cylindrical surface. The temperature is maintained and equalized by height by analog temperature controllers. The temperature sensor is a copper resistance thermometer 20, the unbalance signal source is a copper-constant differential thermocouple with junctions 17, 26.

The heat-stabilizing block is cooled by two copper coils 5, 9 (shown in Fig. 2) bifilarly wound around the copper shell 8 (top and bottom). In evaporator coils, liquid nitrogen is bubbled out from the Dewar flask. The flow rate of the evacuated vapors of the cryogen is regulated by means of the valves 11, 13. The heater 7 is used for heating and temperature maintenance. The axial gradient of the block is eliminated with an accuracy of ± 0.01 K by heaters 21, 23.



Fig. 2. Diagram of the cryostat with the measuring cell: *1*) liquid nitrogen supply tube; *2*) corrosion-resistant steel vessel; *3*) copper sheath; *4*) spiral stirrer; *5*, *9*) upper and lower coolers; *6*) platinum resistance thermometer; *7*, *21*, *23*) heaters; *8*) copper shells; *10*) funnel cryogenic agent supply; *11*, *13*) valves; *12*) vacuum pump; *14*) magnet pull; *15*) guide; *16*) cooled screen; *18*, *27*) covers; *17*, *19*, *26*) points of installation of differential thermocouple junctions; *20*) copper resistance thermometer; *22*) magnet; *24*) heat stabilizer; *25*) thermal bridge.

For better thermal stabilization of the equilibrium chamber, copper thermal bridges 25 are provided to reduce the heat inflow through the filling and analysis lines, the magnet 22 pull 14 of the stirrer 4 (see Fig. 2). The use of copper cooled lids 18, 27 helps to reduce the radiant and convective components of heat inflows. Cylindrical copper thermal bridge 25 provides adjustable compensation of heat influx and cooling of the copper block in the temperature range of 150–250 K. The correspondence of the temperature of the stabilizing block to the temperature of the equilibrium chamber with an error of ± 0.01 K is estimated from the EMF of the differential thermocouple with junctions at 17, 19, periodically measured by a voltmeter.

The temperature of the block is determined using a universal digital voltmeter V7-78/1 and a platinum resistance thermometer PTSV-2-1, calibrated in ITS-90 with an error of ± 0.01 K. The measured temperature corresponds to the cell temperature with an error not exceeding ± 0.03 K.

The pressure in the cell is calculated from the electric signal of the strain gauge D16 *14* (see Fig. 1), measured by the same voltmeter. The strain gauges DD2.5, D16, D100 (*6*, *23*, *12*, *16*, *7*), used for measurement and mutual monitoring, are calibrated in accordance with the deadweight testers MP6, MP60, MP600 class 0.05.



Fig. 3. Diagram of the device for determining the concentration of two-component gas mixtures by the gravimetric static method: 1, 2) cylinders with clean components; 3) pressure transducer; 4) support pier; 5) thermostat; 6) gauge tank; 7) counterweight; 8) mass tensor; 9) digital voltmeter; 10, 11) sources of constant voltage; 12) voltage comparator; 13) filling valve; 14) vacuum pump; 15) cylinder with a stirred mixture of components.

The total composition of the mixture is calculated from the mass values of the components, obtained with an error of ± 1 mg from the difference in mass of the respective filling cylinders 9 (see Fig. 1) weighed on the analytical balance ADV-200 before and after filling the substance into the cell. Small or fractional amounts of the dissolved component are determined with an error of $\pm 1\%$ by the volumetric method from the pressure of the substance, determined using the transducer 6, in a temperature-controlled filling line of a constant volume. The density of the saturated liquid phase is calculated from the values of the mass of the components and the known volume of the cell at the boiling point with an error of $\pm 0.2\%$.

With the created device (Fig. 3), the molar concentration of the volatile component of the binary gas mixture can be determined (based on the gravimetric static method [6]) with an error of 0.001–0.01 mol/mol.

The device (see Fig. 3) makes it possible to make measurements of a gas sample with a mass of 5-50 mg at a pressure of 0.005–0.1 MPa. For this, all cylinders and tubing are evacuated through the nitrogen trap 5 by the pump 1 with a thermocouple pressure transducer 2 (see Fig. 1). The vapor phase sample is carried to the tubing and, if necessary, to the expansion vessel 4. The sample is then heated to ambient temperature and fed to the temperature-controlled measuring constant volume 3, where the values of the corresponding quantities are determined from the strain 10 and pressure 11 gauges.

The molar concentration of gas mixture components is calculated from the results of measurements obtained in the temperature-controlled constant volume ($T_{\text{mix}} = T_1 = T_2$, $V_{\text{mix}} = V_1 = V_2$):

$$N = \frac{U(m_{\text{mix}})/U(p_{\text{mix}}) - U(m_1)/U(p_1)}{U(m_2)/U(p_2) - U(m_1)/U(p_1)}$$

where p_{mix} , p_1 , p_2 represent the absolute pressure of the mixture and its components; m_{mix} , m_1 , m_2 represent the mass of the gas mixture and its components; and U is the measurement signal proportional to the indicated values.

Experiment methodology. The pre-evacuated cell was filled to 95–99% with the first component (less volatile) from the measuring cylinder. The vapor volume $V_v \approx 0.03-0.3$ ml was set by overheating of the saturated liquid followed by the release of its excess amount, by determining the density at the point of inflection on the temperature–pressure relationship curve and the subsequent cooling to the initial state. The amount of the substance remaining in the cell was determined by weighing the measuring cylinder before and after filling. The second component (more volatile) was added from another measuring cylinder. Small amounts of the component, the precise weighing of which on the analytical balance was difficult, were determined

	1		1				
p, MPa	x, mol/mol						
283.15 K		303.15 K		322.04 K		348.15 K	
0.1475	0	0.2715 0		0.4669	0	5.572	0.523
0.1501	0.00062	0.2729	0.00026	0.4675	0.00011		
0.1521	0.00120	0.2757	0.00082	0.4683	0.00021		
0.1560	0.00211	0.2804	0.00178	0.4698	0.00047		
0.1632	0.00409	0.2899	0.00363	0.4735	0.00101		
0.1804	0.00857	0.3071	0.00711	0.4779	0.00185		
0.2107	0.01716	0.3677	0.01947	0.4927	0.00384		
0.2419	0.02558	0.3681	0.01992	0.5183	0.00854		
0.2696	0.03385	0.4247	0.03074	0.5745	0.01678		
3.399	0.745	0.4815	0.04169	0.6628	0.02983		
3.474	0.759	0.5028	0.04579	0.8225	0.05467		
5.152	1	0.5585	0.05644	0.9259	0.07030		
		0.6181	0.06716	1.0368	0.08598		
		0.6726	0.07768	1.1205	0.10124		
		0.7218	0.08758	1.2303	0.11612		
		3.434	0.562	1.4358	0.14458		
		4.847	0.764	1.6514	0.17365		
				1.8146	0.20021		
				4.218	0.527		
				6.344	0.779		

TABLE 1. Results of Measuring the Boiling Curves of the Ethylene–Butane Mixture on Different Isotherms

from the pressure in the filling line (the dependence of the mass of the gas on the pressure in the line was obtained previously by experiment). The gas was dosed via the filling capillary to the lower part of the cell. The gas flow rate was determined using a digital voltmeter from the pressure drop in the filling line and was set according to the nature of the pressure change in the cell. The sensitivity of the change in the measuring signal of the pressure transducer $\Delta U_p = 1 \mu V$ corresponds to the change in pressure in the lines $\Delta p = l_2 \Delta U_p = 14$ Pa and to the change in the total composition $N \approx 0.1$ ppm. Equilibrium in this case was established within 20–60 min. Pressure for the next 10 min remained unchanged within $\delta p = \pm 0.001$ MPa and was recorded by the measuring system. Then the refueling of the component and the subsequent measurement were carried out.

After filling the cell with the second component in several stages, its residues in the lines were frozen into a measuring cylinder, the weight of the charged substance and the total molar concentration of the mixture were determined by weight, and the calculated intermediate masses and compositions were corrected.

Further studies were carried out by a static method, measuring the compositions of the equilibrium liquid and vapor phases by the gravimetric static technique. Before sampling the liquid phase, the capillaries were blown into a preliminary measuring cylinder of the filling lines, and then evacuated. Then, the sample was heat-stabilized and fed into an evacuated measuring volume, where its mass and pressure were determined at the beginning and end of the process. After evacuation of the measuring volumes, the sample was re-sampled with subsequent measurements, the measurement cycle was repeated until stable results were obtained within the error of determining the composition of the gas mixture (generally, two or three attempts were sufficient).



Fig. 4. Graphs of solubility of ethylene in butane: —) calculation; \circ) experimental data, Rainwater and Lynch [3]; ∇) experimental data, Efremova and Sorina [4]; \triangle) experimental data obtained by the authors.

The flow rate for sampling the vapor phase was chosen so that the total pressure did not decrease by more than 1%, in order to avoid a significant disruption of the composition. For purging the capillary, it was necessary to have 2–5 ml of the vapor phase. 5–15 ml were used for the measurements. With such a quantity of the selected vapor phase, the equilibrium total pressure changed with the corresponding concentration of the liquid phase. The reference pressure in this case was the arithmetic mean equilibrium pressure measured at the beginning and at the end of the last sampling.

The vapor phase with a low content of the volatile component was sampled while equally replenished (flow rate G = 2-10 mg/h) through the lower filling capillary.

In studies over a wide range of compositions, a predetermined amount of the component was determined only by weighing, and refilling with the second component was carried out after measuring the equilibrium pressure at all temperature levels. When calculating the concentration of components in a liquid, their content in the vapor phase was taken into account.

The testing of the installation in a wide range of temperatures, pressures and densities was carried out by measuring the thermal properties of pure substances N₂ (99.995%), C₂H₄ (99.88%), C₄H₁₀ (99.95%), C₄F₈ (99.99%) on the vapor pressure curve and in the single-phase region. The compositions of the equilibrium phases were measured on isotherms: 89.68 K for the nitrogen–neon mixture; 310.95 K for the nitrogen–butane mixture and compared with the corresponding literature data. The consistency of the measurement results with true values confirmed reliability of the measuring techniques.

Results of simulation and experiment. The solubility of gaseous ethylene in liquid butane was studied at 283.15, 303.15, 322.04, 348.15 K in a range of compositions, respectively, 0.0006–0.76, 0.0003–0.76, 0.0001–0.78, 0.52 mol/mol by the static method, where the content was specified and the concentration by weight of the charged components was determined (Table 1, Fig. 4).

The presented calculated data are consistent with the results presented by Rainwater and Lynch [3] in the critical region and diverge at low pressures, approaching the values presented by Efremova and Sorina [4].

The low-temperature range on the boiling and condensation curves, supplementing studies in the critical region, was extended by measurements at temperatures of 173.15, 193.15, 213.15, 233.15, 253.15, and 273 K (Table 2) by the static method. The total composition of the mixture was set. The concentration in the liquid was determined from the masses of the charged components and using the volumetric method, and the concentration of the components in the vapor was determined only by the volumetric method (gravimetric static method). The homogeneity of the liquid phase was confirmed up to the melting curve.

p, MPa	x, mol/mol	p, MPa	y, mol/mol	p, MPa	x, mol/mol	p, MPa	y, mol/mol		
	173.	15 K		193.15 K					
0.0002	0	0.0002	0	0.0011	0	0.0011	0		
0.0069	0.063	0.0131	0.953	0.0188	0.063	0.025	0.857		
0.0123	0.12	0.0134	0.903	0.0352	0.120	0.0394	0.899		
0.0185	0.186	0.0649	0.992	0.0525	0.186	0.0427	0.905		
0.0512	0.48	0.0957	0.997	0.1332	0.480	0.1639	0.987		
0.1260	1	0.1260	1	0.223	0.710	0.2428	0.995		
				0.3407	1	0.3407	1		
	213.	15 K		233.15 K					
0.0050	0	0.0050	0	0.0168	0	0.0168	0		
0.0437	0.063	0.0336	0.805	0.0599	0.05	0.0765	0.721		
0.0795	0.120	0.0429	0.701	0.5286	0.459	0.0875	0.753		
0.1210	0.186	0.0952	0.874	0.802	0.664	0.1653	0.850		
0.7537	1	0.3475	0.979	0.990	0.771	0.630	0.966		
		0.5181	0.974	1.071	0.817	0.978	0.978		
		0.7537	1	1.454	1	1.454	1		
	253.	15 K		273.15 K					
0.0468	0	0.0468	0	0.1032	0	0.1032	0		
0.1392	0.040	0.0731	0.401	0.2124	0.037	0.2099	0.487		
0.2648	0.112	0.1066	0.515	1.145	0.334	0.2706	0.637		
0.6556	0.322	0.1625	0.556	1.659	0.465	0.4289	0.740		
1.084	0.523	0.4030	0.883	2.292	0.632	1.091	0.900		
1.533	0.684	0.8169	0.951	2.314	0.639	1.568	0.929		
1.629	0.695	1.216	0.965	2.995	0.797	1.666	0.941		
1.751	0.735	1.562	0.979	4.113	1	2.277	0.962		
1.887	0.812	1.612	0.981			4.113	1		
2.532	1	1.813	0.989						
		2.532	1						

TABLE 2. Results of Measurements of Liquid and Vapor Compositions of the Ethylene–Butane Mixture on Isotherms of the Two-Phase Region

The characteristics of the ethylene–butane system in the single-phase region are represented as p-T dependences on liquid isochores of mixtures of constant compositions (Table 3). Confidence limits for the determination of temperatures were $\Delta_{0.95}T = 0.02-0.05$ K; compositions – $\tilde{\Delta}_{0.95}x = 0.1-8\%$, $\tilde{\Delta}_{0.95}y = 2-6\%$; specific volumes of liquid – $\tilde{\Delta}_{0.95}v' = 0.2-0.8\%$ and pressure – $\tilde{\Delta}_{0.95}p = 0.1-0.5\%$.

Simulation of the thermodynamic properties of the ethylene–butane mixture was carried out using a three-parameter cubic equation of state (TCEOS), which for the *i*th component of the mixture is written in the form [7, 8]:

$$p = RT \left[\frac{1}{v - b_i} - \frac{a_i(T)}{v(v + c_i)} \right],$$

ТК	n MPa	v' liters/kg	ТК	n MPa	v' liters/kg	ТК	n MPa	v' liters/ka				
<i>1</i> , K	<i>p</i> , wi a	v, mers/kg	1, K	p, wh a 0 mol/mol	V, IIICIS/Kg	1, K	<i>p</i> , wii a	V, IIICI5/Kg				
273.36	0.120	1.658	284.73	7.722	1.622	279.72	3.905	1.621				
287.12	9.518	1.622	282.13	5.742	1.621	277.41	2.135	1.620				
						272.39	0.518	1.658				
	0.0468 mol/mol											
252.55	0.162	1.618	292.34	0.470	1.730	322.46	0.817	1.844				
255.32	0.453	1.618	297.96	4.108	1.731	323.30	1.234	1.844				
257.74	1.729	1.618	303.43	7.707	1.732	325.28	2.245	1.845				
260.05	4.078	1.619	308.48	11.03	1.733	329.11	4.203	1.846				
263.28	6.889	1.620	322.36	0.782	1.844	334.51	6.955	1.847				
						342.13	10.82	1.848				
0.3467 mol/mol												
172.31	0.129	1.492	211.93	0.568	1.588	267.58	13.36	1.708				
174.86	1.491	1.493	216.61	4.260	1.589	286.85	6.000	1.811				
175.76	2.624	1.493	219.68	7.092	1.590	289.94	7.977	1.811				
177.28	4.574	1.494	222.22	9.841	1.591	292.82	9.809	1.812				
179.83	7.423	1.494	224.95	12.80	1.591	295.72	11.66	1.813				
181.85	10.32	1.495	253.33	1.900	1.705	299.16	13.84	1.813				
183.99	13.38	1.496	255.61	4.148	1.705	283.87	4.108	1.810				
213.77	1.584	1.588	259.46	8.762	1.707	280.98	2.267	1.809				
215.02	2.635	1.589	263.11	9.792	1.707	279.52	1.671	1.809				
						275.97	1.349	1.809				
				0.4975 mol/mo	1							
175.38	3.224	1.531	218.68	7.105	1.64	283.22	2.700	1.917				
174.49	2.266	1.531	221.67	11.21	1.640	286.56	4.593	1.918				
171.07	0.562	1.530	225.08	13.82	1.641	290.86	7.060	1.919				
175.00	2.323	1.531	250.57	1.123	1.776	295.90	9.882	1.920				
176.92	4.444	1.531	251.05	1.127	1.776	303.10	13.94	1.922				
178.78	7.077	1.532	252.81	2.076	1.776	277.91	1.993	1.916				
180.82	9.969	1.533	256.03	4.250	1.777	283.22	2.700	1.917				
183.72	14.05	1.533	259.89	7.162	1.778	286.56	4.593	1.918				
210.17	0.356	1.637	263.51	9.882	1.779	290.86	7.060	1.919				
213.95	2.474	1.637	268.57	13.65	1.780	295.90	9.882	1.920				
215.79	4.072	1.638	277.91	1.993	1.916	303.10	13.94	1.922				
	0.6203 mol/mol											
177.48	0.566	1.576	217.83	7.059	1.691	270.38	14.04	1.861				
179.09	4.416	1.577	220.70	10.01	1.692	274.59	2.313	2.030				

TABLE 3. Results of p, v, T, x Measurements of Ethylene–Butane Mixture of Constant Compositions in the Single-Phase Region

TABLE 3. Continued

Т, К	p, MPa	v', liters/kg	Т, К	p, MPa	v', liters/kg	<i>T</i> , K	p, MPa	v', liters/kg		
181.15	7.190	1.578	224.59	13.90	1.693	283.53	3.230	2.031		
183.24	10.051	1.578	249.06	1.341	1.856	286.51	4.733	2.032		
185.98	13.75	1.579	254.84	3.222	1.857	294.04	7.021	2.033		
209.36	0.427	1.689	257.93	5.375	1.858	296.49	9.773	2.034		
214.01	3.220	1.690	260.45	7.126	1.859	304.29	13.71	2.036		
215.81	5.052	1.690	264.37	9.876	1.860					
1 mol/mol										
171.21	0.118	1.604	252.91	3.309	2.411	283.15	7.595	2.846		
171.99	0.316	1.604	258.19	5.656	2.418	283.15	7.250	2.886		
173.03	2.633	1.605	262.42	7.533	2.419	283.15	6.891	2.935		
176.40	5.307	1.606	266.44	9.382	2.420	283.15	6.623	2.977		
179.00	7.988	1.606	271.00	11.40	2.421	283.15	6.389	3.025		
181.02	10.46	1.607	277.05	14.02	2.423	283.15	6.180	3.072		
183.94	14.05	1.608	283.15	10.27	2.650	283.15	6.008	3.119		
212.89	3.109	2.001	283.15	9.645	2.684	289.96	7.606	3.120		
216.38	5.769	2.007	283.15	8.902	2.732	294.99	8.799	3.121		
221.24	9.591	2.005	283.15	8.415	2.769	301.01	10.27	3.123		
226.41	13.84	2.010	283.15	7.986	2.807	306.88	11.70	3.124		
						315.56	13.83	3.127		

where *v* is the molar volume; *R* is the gas constant; b_i , c_i are the parameters of the TCEOS for the *i*th component; and $a_i(T)$ is the temperature function for the *i*th component.

Algorithms for calculating the vapor-liquid equilibrium and the solubility of gas in a liquid are given in [9, 10]. To compare the experimental and published data on the solubility of this mixture, graphs were constructed (see Fig. 4). The results of the comparison testify to the possibility of using the TCEOS for thermodynamic calculations of process units operating on ethylene–butane mixture.

Conclusions

1. The developed gravimetric static method for measuring the concentration of two-component gas mixtures allows, with an accuracy proportional to the mass of the sample and the difference in the molecular masses of the components, to determine their content in the entire concentration range at pressures an order of magnitude lower than the atmospheric pressure after measuring the masses of samples of pure starting materials only once.

2. The obtained experimental data on the phase equilibrium for the ethylene–butane system can be used in the development of refrigeration devices and methods for the highest degree of purification of substances.

3. Approbation of the three-parameter cubic equation of state gives grounds for its use in modeling the thermodynamic properties of the ethylene–butane mixture.

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