RESEARCH ARTICLE

Evapotranspiration over Land from a Boundary-Layer Meteorology Perspective

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Abstract

The precise determination of evapotranspiration rate is challenging because it is a quantity that is difficult to measure and to parametrize. Direct estimates include the determination of the change of mass of a volume of soil and vegetation that evapotranspirates using lysimeters, or direct measurements of turbulent water vapour fluxes by eddy-covariance systems. Parametrized estimates that make use of the Monin–Obukhov similarity theory use vertical gradient measurements of temperature and moisture at one point, and line or area averages by means of scintillometers operating at high frequency. A relation for the evapotranspiration from well-watered surfaces was initially developed by Penman and later expanded for vegetated surfaces and for heterogeneous croplands. A popular simplified expression was obtained by Priestley and Taylor. The current challenge is to find expressions for the evapotranspiration in non-saturated conditions, which are common in arid and semi-arid climates, and for heterogeneous terrain. In numerical models, the estimated actual evapotranspiration over land is obtained as the result of the explicit representation of the different involved sub-processes taking place in the soil and the canopy, using so-called land-surface models. Usually these mechanisms are described in a simplified manner and rely on a number of adjustable parameters. The improvement of such descriptions relies in the availability of experimental measurements to make the physical models more complete and robust.

Keywords Evapotranspiration · Eddy-covariance systems · Lysimeters · Heterogeneous surfaces · Land-surface models

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1 Introduction

1.1 Evapotranspiration as a Key Process in the Earth System

The evapotranspiration rate is the flux of water vapour from the surface to the atmosphere, traditionally expressed in kg s⁻¹ m⁻² or an equivalent unit such as mm day⁻¹ or mm year⁻¹, in which 1 mm represents 1 kg m⁻². We will denote it through the variable *E* as the sum of the evaporation from the soil (E_g) and the transpiration of plants (E_{tr}) ,

$$
E = E_g + E_{tr} \tag{1}
$$

Water evaporation requires energy, denoted by the latent heat flux λE , which is the product of the enthalpy of vaporization of water λ and *E*, expressed in W m⁻².

From an energy point of view, evapotranspiration is the most important non-radiative process transmitting heat from the surface to the atmosphere globally, and it is larger than direct heating of the air due to the surface sensible heat flux (Bosilovich et al[.](#page-27-0) [2011\)](#page-27-0). Furthermore it is the branch of the water cycle transporting water upwards feeding clouds and hence the origin of precipitation. The process links the energy and water budgets, and it is quantitatively very significant in both from a global perspective (Trenberth et al[.](#page-31-0) [2007\)](#page-31-0).

There is intense research on evapotranspiration in the fields of plant physiology (Jone[s](#page-29-0) [2013](#page-29-0)), agronomy (Pereira et al[.](#page-30-0) [2015](#page-30-0)), soil physics (Or et al[.](#page-30-1) [2013\)](#page-30-1), global and regional climate (Hagemann et al[.](#page-28-0) [2004](#page-28-0); Katul et al[.](#page-29-1) [2012](#page-29-1)), remote sensing (Zhang et al[.](#page-32-0) [2016](#page-32-0)), and hydrology (Liu et al[.](#page-29-2) [2016\)](#page-29-2), and for these subjects we refer the reader to the referenced works and citations within. Furthermore, there are other important processes related to the phase changes at the Earth's surface, such as interception of precipitation and the corresponding evaporation (van Dijk et al[.](#page-32-1) [2015\)](#page-32-1), sublimation from solid to vapour (Bliss et al[.](#page-26-0) [2011\)](#page-26-0), or condensation, taking place mostly on clear and calm nights (Jacobs et al[.](#page-29-3) [2008;](#page-29-3) Cuxart et al[.](#page-27-1) [2015](#page-27-1)).

A quantification of the importance of evapotranspiration at the global scale is made by Miralles et al[.](#page-30-2) [\(2011\)](#page-30-2) using satellite information. The biome types for which evapotranspiration is maximum include low latitude tropical forests (1182 mm year⁻¹) and savannas $(806 \text{ mm year}^{-1})$. Mid-latitude biome types have larger evapotranspiration in greener areas, such as croplands (542 mm year⁻¹), temperate forests (512 mm year⁻¹) and grasslands $(462 \text{ mm year}^{-1})$, than in semi-arid biomes such as shrublands (315 mm year⁻¹). High latitude boreal forests evaporate 372 mm year⁻¹, while deserts (122 mm year⁻¹) and permanent snow (57 mm year⁻¹) are areas with less evapotranspiration. Their maps show that transpiration is the dominant process in vegetated areas, while soil evaporation prevails in desert areas and is significant in semi-arid climates. Snow sublimation is important in the Northern Hemisphere and interception is especially relevant in the forested areas, being maximal in the tropics[.](#page-31-1) Trenberth et al. [\(2009\)](#page-31-1) estimate a global $\lambda E = 80$ W m², which is much larger than the average sensible heat flux (*H*) of $H = 17$ W m², and the average λE values over land (39 to 52 W m² depending on the source) are also larger than H (25 to 27 W m²). In the current global evolution of temperature and $CO₂$ concentration in the atmosphere, Sikma et al[.](#page-31-2) (2019) indicate that, for vegetated terrain, increases solely in $CO₂$ concentration would enhance H and decrease λE , whereas increases solely of temperature would have the opposite effect, and the combined increases of both factors would depend on their relative importance.

Considering the atmospheric boundary layer (ABL), the evapotranspiration is constrained by the net radiation (R_n) , and is often a major term in the surface energy budget (SEB). When the terrain is dry, the incoming solar energy is employed in warming the soil and the ABL, whereas when it becomes wet the energy used in the phase change results in a lesser warming in both media. The atmosphere is fed by evapotranspiration, thereby increasing the buoyancy of the plumes that may result in ABL clouds, which, in turn, enhance the exchange of mass and energy with the free atmosphere. In addition, the amount of water vapour in the ABL and above modulates the terrestrial longwave radiation captured and re-emitted, influencing the surface radiation and energy budgets (Edward[s](#page-28-1) [2009](#page-28-1)). Dry air from above the ABL is entrained across the convective boundary layer (CBL) capping inversion, and its transport by turbulence to the surface layer increases evapotranspiration (de Brui[n](#page-27-2) [1983;](#page-27-2) van Heerwaarden et al[.](#page-32-2) [2009\)](#page-32-2).

1.2 Physical Mechanisms and Interactions

The main physical processes that are involved in determining evapotranspiration at one location are usually considered to be: (a) *Rn*, which provides most of the energy for the phase change; (b) the turbulence intensity, which favours the renewal of the air close to the surface; (c) the water demand of the atmosphere; (d) the amount of water in the soil–vegetation system and its ability to reach the interface with the atmosphere; (e) the lateral transport of atmospheric moisture related to the surrounding surface heterogeneities; (f) large-scale advection of heat and moisture, and (g) the entrainment of dry air across the ABL top, with the latter three modifying the local atmospheric conditions. The coupling of the water and energy balances at the land surface induces feedbacks that must be considered for a proper representation of the mechanisms in play (Brubaker and Entekhab[i](#page-27-3) [1996](#page-27-3); Kim and Entekhab[i](#page-29-4) [1998](#page-29-4)). For a review of the history and the state of the art on determining evapotranspiration some fifteen years ago, see Shuttlewort[h](#page-31-3) [\(2007](#page-31-3)).

As we depart from the classical idealized picture of an homogeneous terrain covered by grass on a clear-sky day, more processes have to be taken into account. This complex system involves a large number of interactions, as described in Ek and Holtslag [\(2004,](#page-28-2) see their Fig. 1), and it is difficult to inspect analytically. A substantial part of the progress in understanding evapotranspiration dynamics is based in the conceptual model of Raupac[h](#page-31-4) [\(2000\)](#page-31-4), which has inspired large-eddy simulation (LES) studies, especially when coupled with land-surface models (LSMs). This coupled framework provides a more complete description of the soil– vegetation processes and their interaction with the atmosphere (as in Lohou and Patto[n](#page-29-5) [2014\)](#page-29-5). The parametrization of the process depends on the spatio-temporal scales under study, which is discussed in Sect. [5.](#page-17-0) This is complemented with new strategies of data acquisition and analysis, often in synergy with numerical studies. The different ABL processes affecting evapotranspiration over land are shown schematically in Fig. [1.](#page-3-0)

The effect of entrainment can be formally analyzed using the framework set by Raupac[h](#page-31-4) [\(2000](#page-31-4)), who summarized the effect of the external environment through a generic conductance *ge*. This allowed the formal treatment of lateral advection and top entrainment in what is defined as a thermodynamically partly-open system, which provides a solution for the steady state that depends on the ratio of environmental and surface conductances. A CBL over a well-watered grassland may reach equilibrium evaporation, which occurs when the evaporative fraction (taken as $\lambda E/(H + \lambda E)$) remains approximately constant. This is the case when the atmospheric water demand increases with temperature at a similar rate at with humidity, as the result of surface evaporation and entrainment at the top of the CBL. van Heerwaarden et al[.](#page-32-2) [\(2009\)](#page-32-2) determined an expression for the evaporative fraction in the CBL using Raupach's framework by combining three feedback mechanisms: "heating" as

Fig. 1 A schematic of the ABL mechanisms related to evapotranspiration. Orange arrows reflect the components of the solar radiation, dark red arrows the longwave radiation, yellow arrows the net radiation. The radiation budget at the surface is in the orange circle, which can be transient due to cloud passing. Blue arrows are evapotranspiration, dark brown sensible heat flux and light brown ground flux. Black lines with arrows represent circulations. The green circle summarizes the feedbacks as explained in van Heerwaarden et al[.](#page-32-2) [\(2009\)](#page-32-2)

evapotranspiration increases with increasing temperature of the atmosphere, "moistening" as evapotranspiration is reduced as humidity builds up in the CBL, and "drying" as entrainment brings drier air into the CBL.

As the spatial complexity of the vegetation increases, more detailed analyses are needed. Continuous forest canopies act as porous elevated surfaces with complex turbulent motions above and across the canopy top, and the surface can be decoupled from the above-canopy dynamics if the leaf-area index is large (Belcher et al[.](#page-26-1) [2012](#page-26-1)). In the case of patches of forest and open terrain, the terrain heterogeneities induce circulations (Garcia-Carreras et al[.](#page-28-3) [2010\)](#page-28-3) that may have significant effects on the local evapotranspiration (Simó et al[.](#page-31-5) [2019](#page-31-5)). An adequate physical description of the effects of surface heterogeneity is still lacking, although it has been postulated that patches on scales of around a few hundreds of metres may explain part of the organized transport in the lower ABL (De Roo and Maude[r](#page-28-4) [2018](#page-28-4); Mauder et al[.](#page-30-3) [2020](#page-30-3)). The scale of the surface heterogeneities has an impact on the entrainment rate at the top of the CBL and, consequently, on the evolution of the ABL (van Heerwaarden et al[.](#page-32-3) [2014](#page-32-3)). The vegetation density, typically characterized by the leaf-area index, relates to the amount of transpiration and modifies the incident solar radiation as it penetrates the canopy (Pedruzo-Bagazgoitia et al[.](#page-30-4) [2017\)](#page-30-4).

The presence of stratified clouds affects evapotranspiration depending on their optical thickness. Dense clouds essentially prevent solar radiation from reaching the surface, in contrast to thin clouds, which may be associated with larger evapotranspiration than on a cloudless day because of an increase in the amount of diffuse light and a decrease of direct light, resulting in a reduced canopy resistance (Pedruzo-Bagazgoitia et al[.](#page-30-4) [2017](#page-30-4)). Passages of cumulus clouds decrease both the surface latent and sensible heat fluxes, but $\lambda E/R_n$ is larger under the cloud because the atmospheric water demand is not changing while the ground flux *G* is directed upwards causing more evaporation from the upper soil (Lohou and Patto[n](#page-29-5) [2014](#page-29-5)). The effect of a cloud passage affects the leaf response since the opening/closing of the stomata has a mechanical response time on the order of several minutes (Sikma and Vilà-Guerau de Arellan[o](#page-31-6) [2019\)](#page-31-6) leading to a decoupling between *Etr* and the incoming solar radiation. The treatment of such transient conditions is a challenge for current methods used to determine surface turbulent fluxes since they assume stationarity. Conditional sampling strategies have been developed over forests with dense canopies by Kivalov and Fitzjarral[d](#page-29-6) [\(2019](#page-29-6)): they found that evapotranspiration takes between 5 to 10 min to respond to a change in solar radiation, in contrast to the air and leaf temperatures that change more rapidly.

For the sake of completeness, the main concepts relating soil physics to evaporation are summarized here (Or et al[.](#page-30-1) [2013\)](#page-30-1). Soil evaporation, E_g , is usually considered as a two-stage process for a porous material provided that the necessary supply of energy for the phase change is available, and that the atmosphere in contact with the wet surface is not saturated. As long as there is a film region (with pore spaces occupied by air or water) between the surface and the underlying saturated region forming a continuously connected hydraulic network, water will flow from the saturated region to the surface by capillarity. This stage is termed 'constant rate period', as it is controlled by the atmospheric evaporative demand, and it is close to the evaporative rate of a free water surface under the same conditions. The second stage is starting as a dry region is formed in the upper part of the soil, driving the film region downward, as the capillary rise is not sufficient to reach the surface. The top of the film region is termed the 'secondary drying front', and evaporation proceeds to the surface by vapour diffusion through the pore spaces in the soil, with a significant drop of *Eg*. The soil evaporation rate depends on the physical properties of the soil, essentially its porosity and texture, as well as the adsorptive capacities of the soil materials (Verhoef et al[.](#page-32-4) [2006\)](#page-32-4) that may reduce the amount of vapour reaching the surface. A summary of equations describing the transport of water vapour in the soil can be found in Garcia-Gonzalez et al[.](#page-28-5) [\(2012](#page-28-5)), and a discussion on the parametrization of these processes is given in Sect. [5.3.](#page-20-0)

1.3 The Scope

The current status of the determination of evapotranspiration over land is presented, with a focus on its experimental measurement, parametrization and representation in numerical models. We restrict ourselves to estimations for a period of time of the order of an hour or less, taking into account the diurnal cycle, refering to daily values when appropriate. The explicit treatment of sublimation from ice or of condensation of water over surface elements are not part of this work. The evaporation from rain or irrigation water intercepted by the vegetation will be commented upon in Sect. [5.2,](#page-18-0) within the framework of LSMs.

The discussions are intended for a precise location and the effects of terrain heterogeneities will be limited to those related to the immediate surroundings at the scale of a few hectometers, since typically lateral transport related to surface variabilities is already relatively small for the kilometre scale (Cuxart et al[.](#page-27-4) [2016\)](#page-27-4). Sustained synoptic or mesoscale advection is typically of longer spatial and temporal scales. The estimation of areal values, such as drainage basins, satellite pixels or model grid elements, are their relation to values at a single station or of a network of stations, are not addressed here. However, the use of the approaches presented here within the framework of numerical modelling and the associated large range of space scales, are discussed in Sect. [5.](#page-17-0)

It is worth also mentioning the relation between the actual evapotranspiration and a theoretical concept, the potential evapotranspiration (E_p) , which is widely used in applications. It is assumed to represent the amount of water vapour arising from a surface without any restriction on water availability. This concept is a good approximation to evapotranspiration when the soil–vegetation system is close to water-holding field capacity, which is the common case in mid-latitudes, except in a dry summer, and in the tropics in the wet season. Note that when the soil is not saturated, E_p may not be a suitable representation of evapotranspiration, which should be determined either by direct or approximate measurements, by LSMs or by a specific theory on the actual evapotranspiration.

In Sect. [2](#page-5-0) the current methodologies for the experimental estimation of evapotranspiration are revisited, going from the most direct determinations to those that are highly parametrized. Sect. [3](#page-10-0) gives a review of the E_p formulations which are currently most used, since it is a concept of wide application as long as the soil–vegetation system is charged with water. In Sect. [4,](#page-13-0) the challenges of determining the actual evapotranspiration for non-saturated terrain and for heterogeneous surfaces are discussed, with a succinct description of some recent propositions. Section [5](#page-17-0) summarises LSM-based representations of evapotranspiration with information on the current limitations of this approach. Finally, Sect. [6](#page-24-0) contains a description of the perspectives related to evapotranspiration in ABL-related research.

2 Experimental Determination of Evapotranspiration

The experimental determination of evapotranspiration is not straightforward. When it is considered as a flux of matter from the surface to the atmosphere, eddy-covariance systems are considered to be the reference method. This approach is expensive and its use is subject to certain constraints (Hicks and Baldocch[i](#page-29-7) [2020](#page-29-7)). A common surrogate method uses vertical gradients of temperature, humidity and wind speed to estimate the turbulent fluxes using empirical functions depending on the thermal stability. From a surface point of view, evapotranspiration may be considered as the loss of water mass from a volume of soil and vegetation, which can be determined using lysimeters, which monitor the change in mass. The comparison between both methods must take into account that they may be sampling the evapotranspiration process at different spatial and temporal scales depending on their configuration.

2.1 Direct Methods

An eddy-covariance (EC) system measures the fluctuations in velocity, the sonic temperature, and the water vapour concentration at high frequency (typically 10 or 20 Hz). The wind vector is obtained by a three-dimensional sonic anemometer; the speed of sound can be derived and from it the so-called 'sonic temperature', which is very similar to the virtual temperature. High-frequency series of water vapour are obtained using an open-path optical system, which emits infrared radiation that is absorbed depending on the water vapour density (Lee et al[.](#page-29-8) [2004](#page-29-8); Foke[n](#page-28-6) [2017\)](#page-28-6).

Averages and fluctuations of these atmospheric variables can be obtained, from which turbulence covariances (including vertical fluxes) are computed. If the flow is not stationary, the concept of the average is compromised, and if the surroundings are heterogeneous, the conditions required to apply the Reynolds axioms of averaging may not be fulfilled (Mauder et al[.](#page-30-3) [2020](#page-30-3)). Therefore the turbulent flux values as provided by an EC system would be valid as a reference only in the conditions described. Water drops on the transducers, from rain or dew, alter the measurements and may give values that do not comply with the quality control criteria, therefore often water vapour fluxes are not provided during these events, even if they seem to be significant (Hirschi et al[.](#page-29-9) [2017](#page-29-9)). Dust may have a similar effect and regular cleaning and maintenance are necessary.

It is assumed that the EC system is located in the surface layer, where the turbulent fluxes are considered to vary little with height, making the values of the fluxes relatively insensitive to the actual position of the system above the surface. This hypothesis is usually not fulfilled on stably stratified nights, when the fluxes may change significantly in the first few metres over the surface (Mahr[t](#page-29-10) [2014\)](#page-29-10). Besides, nocturnal strong stable stratification may cause evaporation or condensation close to the ground and below the level of the EC system, questioning the representativeness of the measured fluxes.

Lysimeters provide the changes in mass (assumed to be water changes) of a control volume, allowing to an estimate of evapotranspiration if rainfall, seepage and changes in the soil-water storage are monitored (López-Urrea et al. [2006\)](#page-29-11). They are considered a reference system in agronomy, but are expensive to set up. With surfaces typically ranging between 0.5 and 10 $m²$ and depths between 1 and 2 m, lysimeters can measure small changes in mass using several load cells with high precision (Seneviratne et al[.](#page-28-7) [2012;](#page-31-7) Groh et al. [2018](#page-28-7)). A recent strategy to estimate rainfall is to make high frequency measurements (e.g. every 1 min), assuming that there is no evapotranspiration when precipitation occurs (Schrader et al[.](#page-31-8) [2013](#page-31-8)).

In principle, the depth of the lysimeter should be scaled with the level to which moisture changes at the temporal scale of interest. Therefore, for daily monitoring, the depth could be less than that used for yearly monitoring, as long as most of the root system is included (Diaz-Espejo et al[.](#page-28-8) [2005](#page-28-8); Heusinkveld et al[.](#page-29-12) [2006\)](#page-29-12). On the other hand, lysimeters may be isolated from their surroundings and neglect lateral runoff, which may be substantial and difficult to estimate, especially in complex terrain (Girona et al[.](#page-28-9) [2002\)](#page-28-9). However, it is possible to maintain the lysimeter with similar water table depth to the immediate outside soil by means of a bi-directional pumping system and suction candles, so that the lysimeter water dynamics evolve as the field dynamics (Groh et al[.](#page-28-10) [2016;](#page-28-10) Pütz et al[.](#page-30-5) [2016](#page-30-5)). The so-called 'oasis effect', related to differences of the lysimeter surface with its immediate surroundings, is also a source of uncertainty that must be considered (Gebler et al[.](#page-28-11) [2015](#page-28-11)).

Comparing EC systems with lysimeters is an interesting exercise, since both approaches are usually taken as reference methods. When the systems are very close to each other, in the same terrain plot, the differences between them depend on the variability of the surface and the surroundings, in particular the footprint effects on the EC system, or to the presence of persistent hectometre-scale motions not well accounted for in the computation of the turbulent vapour flux (Mauder et al[.](#page-30-3) [2020\)](#page-30-3). Furthermore, lysimeters provide estimations of evapotranspiration and condensation in clear and calm nights, whereas EC systems often have difficulties due to the formation of droplets on the transducers (Groh et al[.](#page-28-12) [2019](#page-28-12)). Gebler et al[.](#page-28-11) [\(2015](#page-28-11)) found, for a well-watered grass site, that lysimeter-based evapotranspiration monthly averages are very close to E_p estimations and that the annual-averaged value obtained from the EC system is 5% smaller than the lysimeter value[.](#page-29-9) Hirschi et al. (2017) showed acceptable correspondance between both methods for measurements in nearby locations for monthly averages, whereas large dispersion was found when comparing hourly values.

Plant physiological measurements are intended to quantify transpiration from a plant. For example, gas chambers measure the amount of water vapour released at the leaf level (Pérez-Priego et al[.](#page-30-6) [2015\)](#page-30-6). Plants in transparent isolated containers with controlled air inflow and outflow, along with monitoring the other components of the water balance, allow a quantification of the amount of water transpired by the plant physiological activity (Escalona et al[.](#page-28-13) [2013\)](#page-28-13). These methods can be used to calibrate sap flow measurements determining its speed in the xylem by heating at one point and detecting the heated flow at another point (Dragoni et al[.](#page-28-14) [2005\)](#page-28-14), which depend on the plant type. Extensively employed in plant physiology studies, these techniques may be of interest for ABL studies in the case of wide dense crop fields, for which transpiration is dominant. They are more difficult to apply for natural vegetation, since it is usually a mixture of several plant species. A recent attempt to combine these methods with standard micrometeorological measurements is the CloudRoots field experiment (Vila-Guerau de Arellano et al. [2020\)](#page-31-9), which shows that information at the leaf level is necessary to obtain accurate parameters for the mechanistic representation of photosynthesis and stomatal aperture, and that sun-induced fluorescence data can be used to estimate the spatial variability of evapotranspiration.

2.2 Methods Based on the Similarity Theory

Estimating evapotranspiration when EC systems or lysimeters are not available is a necessity. Traditionally, Monin–Obukhov similarity theory (MOST, Monin and Obukho[v](#page-30-7) [1954;](#page-30-7) Foke[n](#page-28-15) [2006](#page-28-15)) is used, which relates turbulent fluxes and vertical gradients through an eddy diffusivity coefficient. Empirical formulations for stability correction in the surface layer were provided by Businger et al[.](#page-27-5) [\(1971\)](#page-27-5), and they are currently used in the revised form of Högströ[m](#page-29-13) [\(1988\)](#page-29-13).

Monin–Obukhov theory assumes that surface conditions are horizontally homogeneous and stationary, and defines dimensionless gradients that are a function of a stability parameter, using the Obukhov length, *L*, or the Richardson number, *Ri*. In the particular case of computing *E* using *L*, this relation can be written as

$$
E = \rho_a \overline{w'q'} = -\rho \kappa z u_* \frac{\partial \overline{q}}{\partial z} \frac{1}{\phi_e(z/L)}
$$
(2)

where u_* is the friction velocity, ρ_a the density of air, and $\phi_e(z/L)$ the flux–gradient universal stability function. The overline stands for the average values for the selected interval to compute the statistics of interest. The function can be different between moisture and other variables (momentum or temperature) in unstably stratified conditions $(L < 0)$, but they are usually taken as identical in stable conditions $(L > 0)$. The classical expressions, which are identical to those for the temperature, according to Högströ[m](#page-29-13) [\(1988](#page-29-13)) are

$$
\phi_e(z/L) = 0.95 \left(1 - 11.6 \frac{z}{L}\right)^{-\frac{1}{2}} \qquad -2 < z/L < 0 \tag{3}
$$

$$
\phi_e(z/L) = 0.95 + 7.8 \frac{z}{L} \qquad 0 < z/L < 1 \tag{4}
$$

which have a range of validity restricted to moderate values of stability and unstable stratification (Foke[n](#page-28-15) [2006\)](#page-28-15).

An alternative way to express the fluxes uses the inverse of the eddy diffusivity (called conductance in this framework, see Jone[s](#page-29-0) [2013](#page-29-0)) as an analog to the electrical resistance, usually taking differences, as

$$
E = -\rho_a \frac{\overline{q}(z_2) - \overline{q}(z_1)}{r_{ae}} \tag{5}
$$

where r_{ae} is the aerodynamic resistance for water vapour (in s m⁻¹), with z_1 and z_2 the levels of measurement of *q*. The integration of Eq. [2](#page-7-0) yields

$$
\overline{q}(z_2) - \overline{q}(z_1) = -\overline{w'q'} \left\{ \frac{1}{\kappa u_*} \left[\ln \left(\frac{z_2}{z_1} \right) - \Phi_e \left(\frac{z_2}{L} \right) + \Phi_e \left(\frac{z_1}{L} \right) \right] \right\}
$$
(6)

in which the terms in large brackets are r_{ae} , while Φ_e are the integrated forms of Eq. [3](#page-8-0) and Eq. [4](#page-8-0) as given by Paulso[n](#page-30-8) [\(1970\)](#page-30-8)

$$
\Phi_e(z/L) = 2 \ln \left(\frac{1+x^2}{2} \right) \qquad z/L \le 0 \tag{7}
$$

$$
\Phi_e(z/L) = -5 \frac{z}{L} \qquad z/L \ge 0 \tag{8}
$$

in which $x = (1 - 16z/L)^{1/4}$. Similar equations can be written for the momentum and the sensible heat fluxes (Moene and Van Da[m](#page-30-9) [2014](#page-30-9)). This approach is simple to implement and makes use of an iterative method with an arbitrary initial value of *L* until convergence is reached, since *L* is a function of the three aforementioned turbulent fluxes.

In terms of data availability, the surface-layer variables at the screen level and estimations for the ground level are taken. The wind speed is considered zero at the height of the roughness length *z*0, whereas the land-surface temperature and a related moisture value, are used for the gradients of temperature and humidity. The surface temperature determined from radiation measurements has uncertainties of a few K (Simó et al[.](#page-31-10) [2018\)](#page-31-10) and strong hypotheses are imposed to obtain a value of humidity at the surface, especially when the soil is not saturated. Therefore, the computation of the turbulent fluxes in the surface layer is likely less accurate using estimated data at the surface than it would be actually using two levels of measurement.

The similarity theory has been recently adapted for airflow over forests with homogeneous canopies, since the presence of large coherent structures above the canopy top represent a large part of the turbulent transport (Finnigan et al[.](#page-28-16) [2009](#page-28-16)). This "roughness sublayer" has a length scale for the turbulent mixing which is approximately constant (not increasing with height as in the surface layer), with modified wind profiles that are different to those described by MOST. The interaction with the canopy is made through the prescription of a penetration depth scale that depends on the leaf-area index and the Stanton number that quantifies the difference between scalar and momentum transport efficiency and the subsequent modification of the MOST expressions (Harma[n](#page-29-14) [2012](#page-29-14)).

Scintillometers provide an alternative experimental estimation of evapotranspiration also relying on MOST. A combination of microwave and optical signals travelling between an emitter and a receiver located in the surface layer allows the determination of the humidity and temperature structure parameters (Meijninger et al[.](#page-30-10) [2002;](#page-30-10) Ward et al[.](#page-32-5) [2013](#page-32-5)). These quantities, combined with MOST (Kooijmans and Hartogensi[s](#page-29-15) [2016](#page-29-15)), give estimations of the temperature and moisture fluxes over heterogeneous terrain. The 3D spatial distribution of water vapour can be estimated using Raman lidars, obtaining evapotranspiration from the profiles combined with MOST (Eichinger et al[.](#page-28-17) [2006](#page-28-17); Wulfmeyer et al[.](#page-32-6) [2010](#page-32-6)). The elevated cost of these remote-sensing instruments so far is not conducive to their widespread use.

2.3 Evapotranspiration as the Residual of the Surface Energy Budget

Estimating one term in the SEB equation as the residual of the sum of the others is a common technique. In numerical models, the SEB closure is imposed as a constraint and therefore it is a legitimate approach to determining a term in the budget as the residual, as in Noilhan and Planto[n](#page-30-11) [\(1989](#page-30-11)), where the ground flux *G* is equivalent to the net flux into or out of the combined soil–vegetation–surface scheme.

Experimental estimations of λE by remote sensing from satellite or aircraft widely use this approach. Net radiation (R_n) at the surface is determined with an atmospheric radiative transfer model, together with estimations of surface temperature and emissivity (Roerink et al[.](#page-31-11) [2000](#page-31-11)). The ground flux is usually given as a function of *Rn* and some surface parameters, while H is estimated using the radiatively-derived surface temperature, the air temperature from some external source and a computation of the aerodynamic resistance. The large uncertainties involved in these estimations make residual estimates of λE not very precise. To reduce the uncertainties, experimental validation campaigns are needed for calibration, using λE experimental estimations (Jia et al[.](#page-29-16) [2012](#page-29-16)) or surface temperature over homogeneous terrain (Coll et al[.](#page-27-6) [2005\)](#page-27-6).

From the point of view of the ABL experimentalist, the lack of closure of the SEB is an unavoidable fact that has to be dealt with (Mauder et al[.](#page-30-3) [2020\)](#page-30-3). Usually the sum of the turbulent latent and heat fluxes is smaller than the so-called 'available energy' *Rn*−*G*. The imbalance is usually closed by distributing it between λE and *H* following some proportionality, typically the Bowen ratio ($B = H/\lambda E$) or the evaporative fraction. The validity of this assumption is unclear, as Wang et al[.](#page-32-7) [\(2004\)](#page-32-7) showed that evapotranspiration is maximized in balancing the surface energy budget. Gebler et al[.](#page-28-11) [\(2015\)](#page-28-11) chose to attribute all the energy imbalance to λE (in what they call the worst-case scenario), finding increases in the monthly averages of evapotranspiration up to 25% in the summer and up to 37% in the winter, resulting in values very similar to those provided by a lysimeter.

On the other hand, if *H* is available from a sonic anemometer, but not λE (a very common situation), then λE can be estimated directly as the residual if we proceed as Gebler et al[.](#page-28-11) [\(2015](#page-28-11)), or corrections can be made using the Bowen ratio computed with the vertical gradients of temperature and humidity.

2.4 Section Summary

Figure [2](#page-10-1) summarizes the methods described in this section. The direct determinations of evapotranspiration by EC systems or lysimeters each have their own limitations, but it is commonly accepted that, for monthly averages, EC systems tend to underestimate evapotranspiration while lysimeters (if they are properly set) provide more reliable values at the scale of their plot. Flux chambers give direct estimations at ground and leaf level, but at the price of modifying the measurement conditions, which implies a need to define accurate sampling strategies. The plant physiology methods provide estimations of transpiration and

need to be calibrated against eddy covariance or lysimeters while monitoring the other components of the water balance. The SEB residual method usually requires calibration and can be considered a direct determination of evapotranspiration if λE is made equal to the energy imbalance with *H* provided by an EC system, with corrections if necessary.

The experimental estimation with MOST using temperature and humidity at the screen level and at the surface is the most widely used technique because of its simplicity and low cost. However, the strong hypotheses imposed on the surface and the range of validity of the empirical relations usually reduce the applicability of this approach. Experimental estimations of evapotranspiration in heterogeneous terrain, such as those using scintillometers and Raman lidars, rely fully on MOST and therefore share the same limitations.

3 Estimation of Evapotranspiration for Well-Watered Surfaces

3.1 The Basic Equations

As mentioned in the Introduction, the potential evapotranspiration E_p (or λE_p in terms of energy) is a good approximation to the actual evapotranspiration when there is no limitation on the water availability for the evaporating surface. This is the case when the soil has enough moisture to allow water to reach the surface or when it is covered by vegetation and the root system has access to sub-surface water, even if the upper soil is not saturated, as long as stomata are open.

A number of expressions have been derived to estimate E_p . The simplest ones correlate *Ep* with solar irradiation, or with temperature as its surrogate. Thornthwait[e](#page-31-12) [\(1948\)](#page-31-12) computed an annual heat index using the mean monthly temperature and then estimated the monthly value of E_p using the average temperature of the month weighted by the number of daylight hours. A member of this class of approaches, the equation of Hargreaves (Hargreaves and Alle[n](#page-29-17) [2003](#page-29-17)) is recommended by the Food and Agricultural Organization when only basic meteorological data are available and a daily E_p value is needed. Its computation requires the daily average air temperature T_d and the daily temperature range, the global daily solar radiation, expressed in terms of the radiation at the top of the atmosphere *Ro*, and an adjustable coefficient c_H , while λ is taken at 20 °C

$$
\lambda E_p = c_H R_o (T_d + 17.8) \sqrt{T_{max} - T_{min}} \tag{9}
$$

If the focus is placed on the representation of the relevant processes, the traditional approach has made use of the SEB concept, from which the Penman–Monteith, Priestley–Taylor, or Makkink–DeBruin relations are derived.

Fig. 3 The two conceptual terms in Penman–Monteith equation. Left: the radiation term (E-rad) as a function of the available energy $(R_n - G)$; right: the aerodynamic term (E-aero) as a function of the atmospheric conditions, the aerodynamic and the canopy resistances

The basic idea was given by Penma[n](#page-30-12) [\(1948](#page-30-12)), who wrote a four-term SEB equation involving R_n , *G*, *H* and λE_p , taking $R_n - G$ as the available energy and expressing *H* and λE_p in resistance form as in Eq. [5](#page-8-1) using the surface as the bottom level. To isolate λE_p from this equation he needed to, (i) assume a saturated surface so that the saturation vapour pressure is used, i.e. $e_s = e_{sat}(T_s)$, (ii) a local linear variation of e_{sat} with temperature allowing estimates of $e_{sat}(T_s)$ from $e_{sat}(T_a)$, an approximation that holds for small vertical temperature gradients, (iii) take the aerodynamic resistances equal for heat and moisture, (iv) expect that a value for the available energy was at hand. The formula is usually written as

$$
\lambda E_p = \frac{s \ (R_n - G)}{s + \gamma} + \frac{\rho \ C_p}{r_{ae}} \frac{[e_{sat} \ (T_a) - e_a]}{(s + \gamma)} \tag{10}
$$

in which *s* is the slope of the saturated vapour pressure curve with air temperature T_a , C_p is the specific heat capacity of air at constant pressure, $\gamma = C_p/\lambda$ is the psychrometric constant, ρ is the air density, *ea* is the vapour pressure, and *rae* is the aerodynamic resistance for heat and moisture. The first term is customarily called the "radiation term" as it represents the effect of the radiation available for evapotranspiration. The second term is noted "aerodynamic" as it depends on the state of the atmospheric surface layer, namely the turbulence intensity and the atmospheric water vapour deficit at screen level (Fig. [3\)](#page-11-0).

Recently McCol[l](#page-30-13) [\(2020](#page-30-13)) has revised elements of this derivation, in particular substituting the linearized form of the Clausius–Clapeyron equation by the expression proposed by Vallis et al. [\(2019\)](#page-31-13), leading to improvements when using EC values from the FLUXNET database [\(http://fluxnet.ornl.gov\)](http://fluxnet.ornl.gov).

3.2 The Treatment of Vegetation

As indicated in Moene and Van Da[m](#page-30-9) [\(2014\)](#page-30-9), the expansion for fully-vegetated surfaces was proposed independently by Monteit[h](#page-30-14) [\(1965](#page-30-14)) and by Rijtem[a](#page-31-14) [\(1965\)](#page-31-14). The big-leaf approach represents the actual vegetation as one leaf with one stomatal cavity, for which the water phase change takes place in saturated conditions, by adding an extra canopy resistance *rc* to represent vapour flowing to the leaf surface that is in series with the aerodynamic resistance. The resulting equation for transpiration is identical to Penman's except that γ is substituted by $\gamma^* = \gamma (1 + \frac{r_c}{r_{ae}})$.

A widely used expression for the canopy resistance (Jarvi[s](#page-29-18) [1976](#page-29-18); Stewar[t](#page-31-15) [1988\)](#page-31-15) takes it proportional to a minimum value depending on the vegetation type and to four factors that are, respectively, functions of the incident solar radiation, the soil moisture, the atmospheric water vapour deficit and the temperature of the air, and inversely proportional to the leaf-area index. A more elaborate approach makes use of plant physiology concepts, known as the 'A–g*s*' model (Farquhar et al[.](#page-28-18) [1980;](#page-28-18) Goudriaa[n](#page-28-19) [1986;](#page-28-19) Ball et al[.](#page-26-2) [1987;](#page-26-2) Jacobs et al[.](#page-29-19) [1996\)](#page-29-19). There the net assimilation of carbon *A*, taken as proportional to the difference of carbon concentration between the air in contact with the leaf and the intercellular space, is related to the stomatal conductance g_s , the inverse of the stomatal resistance, and this value is then related to *rc*. Another development was the use of two big leaves in one layer, one sunlit, the other shaded, introduced by Sinclair et al[.](#page-31-16) [\(1976\)](#page-31-16) for which Wang and Leunin[g](#page-32-8) [\(1998\)](#page-32-8) incorporated an A–g*^s* model and a radiative transfer model.

The transpiration of a vegetated surface depends on its canopy resistance, which is determined by the physiology, structure and root system of the plants composing the canopy, each of which has its own particular stomatal resistance. As indicated above, stomata take several minutes to react to light changes (Woods and Turne[r](#page-32-9) [1971](#page-32-9)) and cumulus clouds produce alternating direct and diffuse light that may decouple evapotranspiration from actual changes in photosynthetically-active radiation illumination, as explored by Pedruzo-Bagazgoitia et al[.](#page-30-4) [\(2017](#page-30-4)) using a scheme with two big leaves.

The canopy resistance is considered minimal when water availability and solar radiation are plentiful and the atmospheric demand is not very high. Typical r_c values range from 30 s m^{-1} for short and well-watered vegetation to more than 100 s m^{-1} for tall vegetation. Wh[e](#page-31-17)n bare and vegetated surfaces coexist, Shuttleworth and Wallace [\(1985\)](#page-31-17) proposed a twosource scheme (or "combination" model) in which the total E_p is the sum of the potential evaporation from the soil E_{gp} and the potential transpiration from the vegetation E_{trp} , each obtained using the Penman–Monteith equation, as

$$
E_p = C_s E_{gp} + C_c E_{trp}
$$
\n(11)

in which the multiplying coefficients are combinations of the aerodynamic, soil and canopy resistances. This approach can be expanded to more combinations of sources and layers as described in Zhang et al[.](#page-32-0) [\(2016\)](#page-32-0).

3.3 Variations of the Penman–Monteith Equation

In the case of a non-turbulent saturated surface layer over a well-watered surface, only the radiation term in the Penman equation would remain, an expression that is commonly called "equilibrium evaporation". Nevertheless, turbulent mixing usually removes the saturated air from near the surface and transports drier air from above, allowing the evaporation rate to increase as the aerodynamic term stays active. Priestley and Taylo[r](#page-30-15) [\(1972](#page-30-15)) took the aerodynamic term as proportional to the radiation term for a well-watered surface and expressed λE_p as proportional to the equilibrium evaporation,

$$
\lambda E_p = \alpha \, \frac{s \, (R_n - G)}{s + \gamma},\tag{12}
$$

and they proposed $\alpha = 1.26$, in the absence of significant advection, implying that the aerodynamic term is about one-fourth of the radiation term.

Later de Bruin [\(1983](#page-27-2)) showed that when dry entrainment at the top of the CBL equilibrates with the surface evaporation, α varies with the canopy resistance r_c , and has a diurnal cycle. For well-watered surfaces $(r_c = 0)$ the estimated values are between 1.2 and 1.4, in good agreement with Priestley and Taylor, whereas α diminished with increasing r_c , taking values close to 1 for well-watered grass ($r_c = 60 \text{ m s}^{-1}$) and down to 0.6 for surfaces with $r_c =$ 250 m s⁻¹[.](#page-27-7) In accordance with these findings, Cristea et al. [\(2013\)](#page-27-7) summarized the values for α obtained experimentally for a number of sites, showing the lowest values for dry ventilated sites and the highest for wet locations. The values of α for wet surfaces are in good agreement with van Heerwaarden et al[.](#page-32-2) [\(2009\)](#page-32-2).

Another simplified expression conceptually derived from Penman's equation is found in the Makkink–de Bruin approach for the daily evaporation. Makkin[k](#page-29-20) [\(1957](#page-29-20)) showed that for a well-watered surface in the Netherlands, the daily λE_p scaled with the incoming shortwave solar radiation as

$$
\lambda E_p = a \left(\frac{s}{s + \gamma} \right) S_d + b \tag{13}
$$

where S_d is the downwelling global shortwave radiation at the surface, $a = 0.9$ and $b =$ $30 \,\mathrm{W\,m^{-2}}$. This expression is consistent with the Priestley–Taylor equation in the sense that *G* is approximately zero averaged over a daily cycle and that for wet surfaces R_n is roughly proportional to the global radiation. de Brui[n](#page-27-8) [\(1987\)](#page-27-8) showed that the relation could be [s](#page-27-9)implified by taking $a = 0.65$ and $b = 0$, as later proven by de Bruin and Lablans [\(1998\)](#page-27-9) when comparing it to the Penman relation.

An alternative expression proposes that $b = 20$ W m⁻² (noted β) as an expression of the dry entrainment at the top of the ABL (de Bruin and Holtsla[g](#page-27-10) [1982\)](#page-27-10), with $a = 1$ and, using the solar radiation S_d as a surrogate of R_n , as (de Bruin et al[.](#page-28-20) [2016\)](#page-28-20),

$$
\lambda E_p = \frac{s}{s + \gamma} \left[(1 - A)S_d - C_s \frac{S_d}{S_{dta}} \right] + \beta \tag{14}
$$

in which *A* is the albedo of the surface, S_{dta} is the incident shortwave radiation at the top of the atmosphere, and *Cs* is an adjustable parameter taken as 110 W m−2. This relation is currently applied to estimate daily λE_p values from satellite-derived fields (Trigo et al[.](#page-31-18) [2018](#page-31-18)).

4 Estimations of Evapotranspiration in General Conditions

4.1 Non-saturated Surfaces and Heterogeneous Terrain

When the surface is not well-watered, E_p may not be a suitable approximation to the actual value of evapotranspiration, since it will be limited by the availability of water in the soil. Furthermore, if the terrain is heterogeneous, evapotranspiration will vary between adjacent parcels and lateral transport of humidity will take place by turbulent motions or semipermanent small-scale circulations between areas at different temperature, a process that is not included in the derivation of the E_p equation.

The strategy to extend the Penman-type equations for non-saturated surfaces usually faces the challenge of prescribing the surface moisture for the partially-dry upper soil (the film and the dry regions) and incorporating the response of plant transpiration in these conditions (Verhoef and Ege[a](#page-32-10) [2014\)](#page-32-10). Trugman et al[.](#page-31-19) [\(2018](#page-31-19)) show that the empirical modifications of surface conductivity due to changes in soil moisture cause large uncertainties that are the major cause of inter-model variability in the determination of the carbon cycle, indicating that progress is still needed.

A pragmatic approach in applications is to use the Priestley–Taylor equation with the α coefficient adju[s](#page-28-21)ted to the type of terrain. Flint and Childs [\(1991\)](#page-28-21) related α to soil moisture

Fig. 4 The effect of terrain heterogeneity on evapotranspiration: humidity advection from parcel "1" changes the air humidity over parcel "2" and subsequently its evaporation rate and the upper soil moisture

to determine the actual evapotranspiration for a specific set of atmospheric conditions. Jiang and Isla[m](#page-29-21) [\(2001\)](#page-29-21) adjusted α to a linear variation between 1.26 and zero for well-watered and dry conditions respectively for remote-sensing applications.

Over heterogeneous terrain, the soil moisture distribution is uneven depending to a large extent on the soil composition and vegetation cover of the different parcels. Simó et al[.](#page-31-5) [\(2019](#page-31-5)) have shown that the variability at the hectometre scale can be very large in terms of the vertical gradient of temperature and moisture in the surface layer as well as of the upper soil water content. Furthermore they found that in dry conditions, the lateral advection of water vapour can be comparable to the evapotranspiration at one point, changing the characteristics of the atmosphere in that location compared to an homogeneous site and correspondingly evapotranspiration (Fig. [4\)](#page-14-0). Eichinger et al. [\(2006\)](#page-28-17) explored the estimated variability of evapotranspiration over agricultural fields with a Raman lidar and found large variability at the decametre and hectometre scales.

Finally, for estimating water needs for agricultural applications, the concept of a reference evaporation, E_0 , is often used. It is defined as the value of E_p for an ideal surface of well-watered (non-water stressed) grass. It is then multiplied by a non-dimensional so-called crop coefficient, commonly referred to as K_c , which represents the ratio of the true evapotranspiration to the reference value (Allen et al[.](#page-26-3) [1998](#page-26-3)). It takes into account the physiological plant properties and the effect of water stress. It is empirically adjusted and can range from zero to a value slightly above unity (to account for crops that are transpiring at values above the reference grass rate). It can also be split into two parts, the dual crop coefficient, which accounts separately for evaporation (using a water stress coefficient) and transpiration (using a basal crop coefficient that accounts for plant physiology and is multiplied by a plant stress coefficient). Such coefficients are used quite extensively at the field or plot scale, but satellite data can be used to adjust the seasonality of K_c for spatially-distributed estimates. Note that such methods are adapted for estimating daily evapotranspiration, and thus are not used directly for studying the link between the surface vapour flux and ABL dynamics, thus we will not develop this concept in the current study.

4.2 Alternative Approaches to Determining Evapotranspiration

There exist methods to deal with the evapotranspiration determination problem using approaches not following the Penman rationale and its implicit limitations. Here three of them are presented: (i) the advection–aridity model, which obtains evapotranspiration using E_p and the pan evaporation E_{pa} , without imposing either MOST or SEB closure, and implicitly incorporating advection; (ii) the maximum production entropy theory that, given R_n , estimates evapotranspiration using only the temperature and humidity of the surface, and (iii) the surface-flux equilibrium expression for daily evapotranspiration, which needs solely the daily-averaged screen values of air temperature and humidity.

Advection-aridity model. Also known as the 'complementary principle', it provides estimations of evapotranspiration without imposing the closure of the SEB and, in some applications, it can even bypass MOST. This concept was first given by Bouche[t](#page-27-11) [\(1963\)](#page-27-11), and developed further by Brutsaert and Stricke[r](#page-27-12) [\(1979](#page-27-12)), being formulated recently in a comprehensive theoretical manner by Brutsaer[t](#page-27-13) [\(2015](#page-27-13)).

The theory results from the relations between three types of evapotranspiration in the same environment, considered locally uniform: E , E_p and E_{pa} , the latter of which is called the 'apparent E_p ' which arises comes from a small surface of water that can be measured with an evaporation pan. When the surface has full availability of water, the three values are identical, otherwise they may be ordered as $E \leq E_p \leq E_{pa}$.

As the surface dries, $\lambda E_p - \lambda E = \Delta Q_e$, where ΔQ_e is the flux of energy not used as evapotranspiration. As Parlange and Katu[l](#page-30-16) [\(1992\)](#page-30-16) describe, the energy not employed to evaporate water in a hypothetically well-watered surface is used in a real non-saturated surface for other processes, including sensible heat flux, biological processes or lateral transport in heterogeneous environments. This idea allows the method to circumvent the need to impose the constraint of SEB closure, and this is the reason why the method is also called the "advection–aridity evaporation model".

This excess of energy can cause E_{pa} to become larger than E_p , because the environmental temperature may increase more for a non-saturated surface and therefore the evaporative demand would be larger. This increase above potential conditions ($E_{pa} - E_p$) was considered equal [t](#page-27-11)o ΔQ_e ΔQ_e ΔQ_e by Bouchet [\(1963](#page-27-11)) or proportional to it by Brutsaert and Parlange [\(1998\)](#page-27-14), without a clear justification in any of both cases.

Brutsaer[t](#page-27-13) [\(2015](#page-27-13)), inspired by Han et al[.](#page-29-22) [\(2012](#page-29-22)), proposed a polynomial function for which the coefficients are determined using realistic conditions for moist, dry and drying situations, applicable for arid environments, finding

$$
E = \left(\frac{E_p}{E_{pa}}\right)^2 (2E_{pa} - E_p) \tag{15}
$$

for which *Ep* can be found using a Penman-type expression and *Epa* using the value from an evaporation pan or Penman for a surface of water. Brutsaer[t](#page-27-13) [\(2015](#page-27-13)) used the Priestley– Taylor equation for E_p and Penman's formula over open water for E_{pa} , thereby providing a formula for the actual *E*. The temporal resolution of the formula is then just a matter of the corresponding resolution of the input data.

Maximum production of entropy. This approach is based on non-equilibrium thermodynamics (Wang and Bra[s](#page-32-11) [2009](#page-32-11), [2011\)](#page-32-12) and provides estimations for the energy fluxes in the surface layer for conditions varying from dry to saturated. A so-called "dissipation function", *D*, is built, which is proportional to the sum of the square of the heat fluxes, each of which is divided by its respective "thermal inertia" coefficient,

$$
D(\lambda E, H, G) \equiv \frac{2 G^2}{I_s} + \frac{2 H^2}{I_a} + \frac{2 (\lambda E)^2}{I_e}
$$
 (16)

where I_s is taken from a simple relation between the diurnal ranges of variation of landsurface temperature and G , I_a is derived for H making use of the Monin–Obukhov relations and I_e comes from $I_a = \sigma I_e$, assuming that both turbulent fluxes go through similar physical processes. The parameter σ is a postulated dimensionless parameter, which is formally similar to the inverse of the Bowen ratio: it varies between zero for a dry soil and *s*/γ for a saturated soil. Its general expression depends only on the temperature and moisture of the surface as

$$
\sigma = \frac{\lambda^2}{C_p R_v} \frac{q_s}{T_s^2} \tag{17}
$$

Minimizing *D* with the constraint that the SEB closes, then expressions of *H* and λE solely in terms of R_n and some physical parameters of the surface are obtained. The general expression for λ*E* is

$$
\lambda E = B(\sigma)H,\tag{18}
$$

$$
B(\sigma) = 6\left(\sqrt{1 + \frac{11}{36}\sigma} - 1\right). \tag{19}
$$

The extension for a fully vegetated surface assumes *G* as negligible providing modified expressions. This model provides a unique solution for λE , *H* and *G* given T_s , q_s and R_n , but not the other way around. It is applicable for the entire range of soil wetness, from dry to saturated conditions. The challenge remains in terms of the determination of q_s , which the authors suggest to take as the specific humidity of an infinitesimally-thin layer close to the evaporating surface. This theory, proposed for application in the field of hydrology, is formally not restricted to the daily scale, although its validation has been made with daily data.

A surface-flux equilibrium expression for daily evapotranspiration. Following the concept that the diurnal evolution of surface-layer temperature and humidity contains information on the magnitude of the surface heat fluxes if advection is limited (Bett[s](#page-26-4) [1992](#page-26-4)), it is hypothesized that the surface moistening and surface heating terms in the near-surface relative humidity budget approximately balance (Gentine et al[.](#page-28-22) [2016\)](#page-28-22). Assuming the conceptual framework of Raupac[h](#page-31-4) [\(2000](#page-31-4)) for a box, here limited to exchanges across its vertical top, evapotranspiration can be expressed as (McColl et al. [2019](#page-30-17); McColl and Ridgen [2020](#page-30-13))

$$
\lambda E = \frac{R_n - G}{1 + B},\tag{20a}
$$

$$
B \approx \frac{R_v C_p T_a^2}{\lambda^2 q_a}.
$$
 (20b)

In this expression, $(1 + B)^{-1}$ represents the evaporative fraction, and the Bowen ratio, *B*, is the result of the balance between the surface moistening and the surface heating in the budget. It is intended for locations without significant lateral transport of moisture, therefore it is best suited for inland continental areas. It depends only on *T* and *q* at the screen level, and implies that evapotranspiration increases with the relative humidity. This is only correct for time scales of days or longer, since greater evapotranspiration will reflect on more moisture in the atmosphere. McColl and Ridgen [\(2020](#page-30-13)) show that the relation provides good results for continental sites using climatological data at the daily scale. A schematic diagram of the methods described in the last two sections is given in Fig. [5.](#page-17-1)

Fig. 5 Schematics of the existing approaches to estimate evapotranspiration. The methods with an asterisk represent those based on daily values

5 Estimating Evapotranspiration Using Land-Surface Models

5.1 The Land-Surface Modelling Approach

Land-surface models were originally implemented in numerical weather prediction (NWP) models to provide interactive lower boundary conditions for atmospheric radiation and turbulence schemes. Their main task there was the computation of the fluxes of heat, mass and momentum between the land and the atmosphere on a time scale compatible with the aforementioned atmospheric processes (i.e. the diurnal cycle must be adequately resolved). The fluxes from the soil and the vegetation are computed through the solution of one or more SEB equations, and arguably evapotranspiration is the most important flux since it couples the energy and water budgets at the land surface.

In the past two decades, LSMs have evolved considerably to include more processes that are strongly linked with evapotranspiration in order to meet the growing demands of both the research and the user communities (van den Hurk et al[.](#page-31-20) [2011\)](#page-31-20), such as photosynthesis and the associated carbon fluxes, vegetation phenology (biomass evolution, net primary production), and both superficial and root zone soil moisture prediction (e.g., to estimate drought severity or crop irrigation needs).

The estimation of evapotranspiration from an LSM must be approached across scales, where processes are resolved in such models from the local (or the so-called agricultural 'parcel' scale, which is as small as on the order of tens of m: the scale at which evapotranspiration measurements are generally made using, for example, eddy-covariance techniques, see Sect. [2\)](#page-5-0), to the mesoscale (from the parcel up to several km), regional (up to tens of km) to global (areas up to hundreds of km). Of course, the aforementioned discrete scale definitions are somewhat artificial and result either from historical reasons and/or for convenience (adapted for a particular application). The LSM parametrization treats unresolved scale-dependent processes as a function of some grid-average state variable though a combination of conceptual models, empirical relationships, and theory. As such, they must account for scale change either statistically, through scaled input parameters, or a combination of both. Therefore, a combination of theory, modelling, analysis and observations (data from field campaigns, re-analysis datasets and satellite-based data) at multiple scales have been used to develop LSMs.

Generally speaking, the research community has a fundamental knowledge of how to model evapotranspiration using rather comprehensive approaches. However, progress in LSM development is made seemingly slowly at times in fully coupled or spatially distributed models since such numerical modeling must strike a sometimes delicate balance between computational efficiency, the ability to accurately define input parameters and their related uncertainties, and the complexity of the physical parametrization. Such factors weigh heavily for both operational applications (where tight schedules for getting products to end users must be respected) and climate research (where simulations can take months of computing time). And of course, certain applications require evapotranspiration estimates over large domains using dense computational grids (operational hydrological forecasting, e.g. Habets et al[.](#page-28-23) [2008](#page-28-23); Snow et al[.](#page-31-21) [2016\)](#page-31-21) for significantly long integration periods (e.g. high resolution land-surface reanalysis products: Carrera et al[.](#page-27-15) [2015](#page-27-15); Bonan et al[.](#page-27-16) [2020](#page-27-16)).

In order to strike a balance, researchers use the strategy of developing a parametrization that only considers what are deemed to be the main processes (or even only those for which we have reasonable estimates of input parameters). Such models are oftentimes developed and bench-marked based on more complex process-based schemes. As our understanding of processes, improved physiographic data (describing both soil and vegetation properties, and land use), computational resources and the availability of observational or satellite data sets all increase, more realistic and complete physically-based evapotranspiration representations can be developed.

5.2 Evapotranspiration in Land-Surface Models

Evapotranspiration is computed in LSMs from the SEB equation, and generally (neglecting cold-season processes such sublimation from snow or ice, and intercepted water) evapotranspiration from the land surface is parametrized as consisting of ground surface evaporation, E_g , and transpiration from vegetation, E_{tr}

$$
E = \frac{\rho_a}{r_{ae}} \left[q_c - q_a \right] = E_g \left(T_g \right) + E_{tr} \left(T_v \right) \tag{21}
$$

where T_g and T_v represent the ground surface and vegetation temperatures, respectively. The specific humidity of the canopy air space and overlying atmosphere at some reference level above the surface are represented by q_c and q_a , respectively. q_c is estimated by substituting the appropriate expressions for E_g and E_{tr} into Eq. [21](#page-18-1) (which will be presented in the following sub-sections). Finally, the aerodynamic resistance, *rae*, is parametrized using either MOST directly (Eq. [6,](#page-8-2) as described in Sect. [2.2\)](#page-7-1) or a bulk Richardson number approach empirically fitted to the aforementioned functions (Loui[s](#page-29-23) [1979](#page-29-23)).

Early simple LSMs used the composite soil–vegetation single SEB approach (e.g. Bhummralka[r](#page-26-5) [1975](#page-26-5); Noilhan and Planto[n](#page-30-11) [1989](#page-30-11)) for which a single energy budget was solved thus the surface temperature can be represented as a single temperature $(T_s = T_v = T_g)$ and r_{ae} defines the aerodynamic resistance between the composite surface and the overlying surface layer. There has been widespread use of such composite schemes to compute evapotranspiration fluxes in operational NWP models for years and they are still in use multiple operational centres for regional to global (e.g. Bélair et al[.](#page-26-6) [2003](#page-26-6); Ek et al[.](#page-28-24) [2003](#page-28-24)) and kilometric (e.g. Seity et al[.](#page-31-22) [2011](#page-31-22)) scale applications, owing in large part, to their relatively small number of required input (physiographic) parameters and easy implementation into operational data assimilation schemes.

In the late 1980s and early 1990s, the so-called big-leaf approach became more prevalent in which two surface energy budgets (also referred to as a two-source approach) are considered, one for the ground surface (often representing evaporation from a relatively thin surface soil layer) and the other for a bulk vegetation canopy. Sellers et al[.](#page-31-23) [\(1986\)](#page-31-23) proposed one of the first highly comprehensive schemes for use in a general circulation models (GCMs)

Fig. 6 The resistance pathways for the two-source energy budget model is shown on the left, with explicit resistances for explicit turbulent exchanges between the canopy air and the ground and the vegetation. The corresponding surface temperatures (for computing the evapotranspiration components) are shown. The single or composite energy budget scheme is shown on the right, for which both $E_{\ell v}$ and E_g are computed using the same aerodynamic resistance, *rae*, and surface temperature, *Ts*

which is still fairly representative of many LSMs in use today. If a two-source energy budget approach is used, then MOST is applied above a certain within-canopy displacement height to model the resistance between the so-called canopy air space and the overlying surface layer (*rae*). Furthermore, functions that account for the effects of vegetation density and height on the below canopy turbulence (eddy diffusivity) are used to compute the aerodynamic resistance between the ground and the vegetation and the canopy air space (Fig. [6\)](#page-19-0). Many LSMs use approaches inspired by Deardorf[f](#page-28-25) [\(1978\)](#page-28-25) with refinements (e.g. Choudhury and Monteit[h](#page-27-17) [1988](#page-27-17); Raupac[h](#page-30-18) [1994\)](#page-30-18). In recent years, some GCMs have begun adopting multi-layer vegetation canopy models to compute an integrated value of *Etr* using explicit within-canopy turbulent diffusivity computations as opposed to assumed profile functions (Naudts et al[.](#page-30-19) [2015](#page-30-19)) including more recent modifications to better represent the roughness sublayer (Bonan et al[.](#page-26-7) [2018\)](#page-26-7).

Note that one could also include evaporation terms from water intercepted by the vegetation canopy. Generally speaking, evaporation of canopy-intercepted water is a relatively small component of evapotranspiration, except for certain land-cover types such as dense tropical forests where it can be a significant part of the total evapotranspiration from vegetation. It is notoriously difficult to quantify, however some model-based estimates can be found in the literature. For example, Choudhury and DiGirolam[o](#page-27-18) [\(1998\)](#page-27-18) used a detailed physically-based model that used meteorological measurements as input to derive a global estimate of 20% of the total evapotranspiration. Since that time, multi-model based estimates have been made which give similar values (e[.](#page-28-26)g. 17% from Dirmeyer et al. [2006\)](#page-28-26). Finally, intercepted canopy water in irrigated fields can have a significant impact on evapotranspiration by covering leaf pores or by humidification of the canopy air space, but its estimation remains complex (Jasim et al[.](#page-29-24) [2015](#page-29-24)). Thus there remains considerable uncertainty in how to accurately model this process in LSMs so that most LSMs tend to use rather simple approaches (Wang et al[.](#page-32-13) [2007\)](#page-32-13).

Finally, some LSMs include evaporation of ponded water. But this process is either not represented or parametrized in very different ways among LSMs (perhaps using a different temperature or even methodology, or included in separate wetland or river storage modules). The evaporation from water surfaces such as lakes, marshes or rivers are therefore beyond the scope of the current discussion.

5.3 Ground Evaporation in Land-Surface Models

Ground evaporation is governed by molecular diffusion from the water surface in the soil pore space in some near surface soil layer to the reference level of the ground surface defined as the humidity roughness length, z_{0a} . As water is lost from this layer, additional moisture can be supplied from below via capillarity. Then, water vapour is exchanged with the overlying atmosphere through laminar and turbulent processes. The process in LSMs is generally represented using one of the three methods described below.

The so-called alpha approach expresses E_g as

$$
E_g = \frac{\rho_a}{r_{ae,g}} [\alpha q_{sat}(T_g) - q_c]
$$
 (22)

where $r_{ae,g}$ represents the resistance between the ground surface and the canopy air space (s m^{-1}), and q_{sat} represents the saturation specific humidity at the surface (at temperature T_g).

The relative humidity of the air is considered at the reference level (generally assumed to be at z_{0h} for moisture and heat) just above the surface. This quantity is usually unknown, and modelling it would require a significant amount of added complexity, therefore a proxy is used based on soil moisture in the surface soil layer. Generally, expressions are commonly used of the form

$$
\alpha = \min\left(1, \frac{a_{g\alpha}\theta_g}{b_{g\alpha}\theta_g + c_{g\alpha}}\right),\tag{23}
$$

$$
\alpha = \frac{1}{2} \left[1 - \cos \left(\frac{\theta_g}{\theta_{fc}} \frac{\pi}{2} \right) \right], \qquad (\alpha = 1 \text{ if } \theta_g \ge \theta_{fc}), \qquad (24)
$$

where θ_{g} represents the volumetric soil water content in the upper soil layer (m³ m⁻³) that has a depth (thickness) defined as z_{gs} (m). Note that the values of the parameters $a_{\varrho\alpha}$, $b_{\varrho\alpha}$ and *cg*^α vary among different studies and should likely depend on soil properties (such as texture, organic content...) or they could be calibrated based on more detailed soil models or observations. The so-called field-capacity volumetric water content, θ_{fc} , is generally based on soil texture properties in many LSMs, although for local scale applications it is generally best to define it based on soil moisture observations, if available. Note that it should be obvious that the two expressions for α generally have very different forms despite both depending on the same surface soil moisture. The various forms for α used among LSMs are known to be a source of potentially significant differences in simulated *Eg* (e.g. Mahfouf and Noilha[n](#page-29-25) [1991](#page-29-25)).

Note that the thickness of the surface layer, *zgs*, has yet to be defined: the basic idea is that a diurnal cycle of the surface soil moisture can be represented if this layer is thin enough to represent the dry down during the day and the capillary recharge of the soil moisture from below during periods of low radiative forcing (generally at night). Thus, the chosen value of the surface layer thickness (which is model dependent) can have a very large impact on the E_g via the selected α function since it is directly proportional to the surface water holding capacity. Finally, the application of the alpha equation to daytime conditions has been shown to work well, however, numerically speaking, certain modifications must be done at night to prevent excessive condensation mainly over very dry soils. In addition, there has been relatively little study of the ability to accurately represent condensation in the LSM community to date.

The so-called beta method is given as

$$
E_g = \frac{\rho_a}{r_{ae,g}} \beta_g \left[h_g q_{sat}(T_g) - q_c \right]. \tag{25}
$$

Compared to the alpha method, here the relative humidity of the upper soil h_g is included as

$$
h_g = \exp\left(\frac{g\,\psi}{R_v\,T_g}\right). \tag{26}
$$

where ψ represents the surface soil matric potential (m). The matric potential is related to volumetric soil water content in LSMs generally using the pedotransfer functions based upon Brooks and Core[y](#page-27-19) [\(1964](#page-27-19)) or van Genuchte[n](#page-32-14) [\(1980\)](#page-32-14). For this method, evaporation is assumed to come from a wet layer that becomes deeper in the soil as it dries. Theoretically speaking, this method requires relatively thin soil layers in order to properly model the strong vertical gradients of soil temperature and matric potential in the uppermost (near surface) layers. Some authors set this relative humidity factor h_g to unity and so β_g then simply depends on the soil moisture (e.g. Deardorf, 1978). Currently, LSMs generally model the beta function as

$$
\beta_g = \frac{r_{ae,g}}{r_{ae,g} + r_g}.\tag{27}
$$

Note that if a single composite energy budget is represented, then *rae*,*^g* is replaced by *rae* in Eq. [27,](#page-21-0) and q_c is replaced by q_a and T_g is replaced by T_s in Eq. [22.](#page-20-1) The resistance r_g represents a soil resistance term, that should depend on soil texture or other structural properties of the soil, but most currently used formulations are based on that of Sellers et al[.](#page-31-24) [\(1992\)](#page-31-24), which were calibrated for a single soil type and climate,

$$
r_g = \exp\left[b_{g\beta} - c_{g\beta} \left(\frac{\theta_g}{\theta_{sat}}\right)\right]
$$
 (28)

where *bg*^β and *cg*^β are calibrated empirical parameters. Merlin et al[.](#page-30-20) [\(2011\)](#page-30-20) suggest that the soil resistance parametrization has some conceptual problems that make its use in LSMs problematic: its use is more questionable when capillarity forces are strong or under conditions when gravitational drainage is dominating the drying of the near surface soil layers. They argue for an approach using Eq. [25](#page-21-1) with $h_g = 1$ and where β_g is represented by an analytical equation for evaporation efficiency that depends on both near-surface soil moisture and the potential evaporation. Despite very promising results for both energy and water driven regimes, use in an operational LSM would be more complex since estimating the potential evaporation at each time step within an LSM is not straightforward.

Finally, the so-called gamma method, which is based on the minimum of atmospheric demand, E_d , and soil moisture supply, reads

$$
E_g = \min\left\{ E_d, \frac{\rho_a}{r_{ae,g}} \left[q_{sat}(T_g) - q_c \right] \right\}
$$
 (29)

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In order to determine the supply limited value, an expression of the bare soil evaporation must be obtained and several formulations exist based on vertically integration of the expression for vertical water diffusive flux within the soil (Mahrt and Pa[n](#page-29-26) [1984;](#page-29-26) Wetzel and Chan[g](#page-32-15) [1987](#page-32-15)). One advantage of this method is that it does not require a relative humidity (or proxy) term, however it has been found to be highly sensitive to the method to compute the effective depth over which the diurnal cycle of moisture is damped, the parametrization of the rate of moisture diffusion within the soil is difficult to define, and it is highly sensitive to soil properties. This method is not commonly used among LSMs currently: it is assumed this is related to the aforementioned issues, but also for more pragmatic reasons: the α and β _{*o*} formulations are also more easily implemented numerically. It should be evident by now that all of the methods (Eq.s [23](#page-20-2)[-24](#page-20-3) and Eq. [29\)](#page-21-2) can be summarized as depending on surface soil moisture over some near-surface layer thickness, while having very different mathematical forms (thus potentially very different predicted E_g) and theoretical underpinnings.

As a final note, some LSMs have introduced parametrizations for litter, but the approach can be very different from one to another depending on their complexity. The simplest approach is to modify or add an additional ground resistance (Sakaguchi and Zen[g](#page-31-25) [2009\)](#page-31-25), while the alternative is to model the litter using an explicit single or multi-layer model (e.g., Wilson et al[.](#page-32-16) [2012;](#page-32-16) Napoly et al[.](#page-30-21) [2017](#page-30-21)). Including a litter layer implies that *Eg* would derive from the litter directly, with a possibly soil contribution (if litter covers a fractional surface or capillary rise from the soil into the litter is assumed, but this is generally thought to be small and is neglected in simpler models). The thermal properties of litter are also generally quite different from soil, thereby having an impact on T_g . And once again, the thickness of the source layer, the litter layer in this case, and the hydrological properties of the litter will have a large impact on the water storage capacity and therefore the simulated *Eg*.

5.4 Transpiration in Land-Surface Models

Transpiration refers to the loss of water from vegetation as water vapour. Land-surface models represent transpiration with varying degrees of complexity, usually used on the intended application. The basic processes that are represented can be summarized as follows: water (containing dissolved nutrients) is absorbed by roots and transported in liquid form via xylem into the plant cells for photosynthesis (for which the plant uses light energy and atmospheric CO2 to produce organic material). At the leaf surface, this water is transformed from liquid to water vapour where the associated latent heat release acts to keep the vegetation relatively cool. This vapour leaves the plant through the stomata. The subsequent increase in the matric potential gradient between the leaf and the soil then draws water into the plant from the soil. If there is insufficient soil moisture (or water stored in the plant), the stomata close and transpiration ceases.

Transpiration is generally represented using a beta formulation as

$$
E_{tr} = \frac{\rho_a}{r_{ae,v}} \beta_v \left[q_{sat}(T_v) - q_c \right] \tag{30}
$$

where

$$
\beta_v = \frac{r_{ae,v}}{r_{ae,v} + r_c},\tag{31}
$$

in which $r_{ae,v}$ represents the resistance between the canopy air and the vegetation. As mentioned in the previous subsection, most LSMs use parametrizations inspired by Deardorf[f](#page-28-25) [\(1978](#page-28-25)), Choudhury and Monteit[h](#page-27-17) [\(1988\)](#page-27-17) and Raupac[h](#page-30-18) [\(1994](#page-30-18)). If a single composite energy budget is represented, then $r_{ae,v}$ is replaced by r_{ae} in Eq. [31,](#page-22-0) and q_c is replaced by q_a and T_v is replaced by T_s in Eq. [30](#page-22-1) (Fig. [6\)](#page-19-0). Note that, in reality, the temperature of the transpiring surface is lower than that given by the energy balance, and this can be modelled by replacing T_v in qsat (T_v) in Eq. [30](#page-22-1) by an equivalent wet-bulb temperature, or a similar effect can be obtained b[y](#page-30-22) modification of the β_v (Milly [1992\)](#page-30-22) or by multiplying the q_{sat} (T_v) term by a reduction factor (akin to using an α type approach). The plant physical processes are encompassed in the *rc* term, which represents the stomatal resistance integrated over the entire vegetation canopy. Stomata close under sub-optimal conditions corresponding to insufficient solar radiation, a large humidity deficit between the atmosphere and the surface, as the air temperature falls outside of a species dependent specific optimal range (heat stress), and soil water stress. Through the 1990s, most LSMs used the relatively simple stomatal resistance model of Noilhan and Planto[n](#page-30-11) [\(1989\)](#page-30-11), which is based on Jarvi[s](#page-29-18) [\(1976\)](#page-29-18). It includes a representation of the aforementioned factors

$$
r_c = \left(\frac{R_{s,min}}{LAI}\right) \left[\frac{F_1(SW\downarrow)}{F_2(\theta_r) F_3(\delta e_a) F_4(T_a)}\right]
$$
(32)

where the inclusion of the leaf-area index (LAI) indicates an integration of the resistance over the entire canopy. $R_{s,min}$ is the minimum or unconstrained stomatal resistance (s m⁻¹), and many models use lookup tables (based on land cover type) to determine it. However, calibration is often required to obtain good results as r_c and thus E_{tr} are found to be highly sensitive to this parameter. F_1 models the effect of the photosynthetically active radiation (and is a function of the downwelling shortwave radiation, $SW\downarrow$). The remaining factors parametrize the dependence on root zone soil moisture, *F*2, the atmospheric vapour pressure deficit, *F*3, and temperature stress, *F*4.

In more recent years, *rc* formulations have been extended to represent photosynthesis. The stomatal conductance to water vapour can be expressed as

$$
g_c = \frac{1.6 A_n}{C_s - C_i} \tag{33}
$$

where $C_s - C_i$ (kg CO₂ m⁻³) corresponds to the gradient between the outside and the leaf intercellular $CO₂$ concentrations, respectively, and the factor 1.6 represents the proportionality factor of water vapour to CO_2 . The net assimilation rate, A_n , (kg CO_2 m⁻² s⁻¹), represents the net flow of $CO₂$ through the plant stomata and includes environmental factors (based on available radiation, air temperature, vapour pressure deficit, etc.). There are many models that have been proposed to represent A_n , and most methods used by LSMs are based on Farquhar et al[.](#page-28-18) [\(1980\)](#page-28-18), Collatz et al[.](#page-27-20) [\(1992\)](#page-27-20) and Jacobs et al[.](#page-29-19) [\(1996\)](#page-29-19). Once *An* is known, *gc* is then integrated from the leaf to the canopy level using as assumed canopy leaf vertical distribution and density via the leaf-area index(LAI), and this final value is then proportional to r_c^{-1} .

Such parametrizations permit the LSM to simulate the diurnal cycle of carbon and water vapour fluxes using CO2 responsive representations of photosynthesis (e.g. Calvet et al[.](#page-27-21) [1998](#page-27-21); Yang et al[.](#page-32-17) [2011;](#page-32-17) Boussetta et al., [2013;](#page-27-22) van Den Hoof et al[.](#page-31-26) [2013\)](#page-31-26). The relatively rapid impact of changes of net radiation and atmospheric conditions on *rc* and therefore evapotranspiration has been explored using fully coupled surface–atmosphere models in different studies which are mentioned in Section [3.2.](#page-11-1)

The photosynthesis schemes can also be coupled with models that simulate plant phenology, which thereby can impact *Etr* additionally by potentially changing surface characteristics such as *z*0, *LAI*, and surface albedo (e.g. Krinner et al[.](#page-29-27) [2005;](#page-29-27) Bonan et al[.](#page-26-8) [2011](#page-26-8)). The obvious advantage for climate applications or seasonal prediction is the ability to simulate feedbacks between the climate and the vegetation state (for example, better evapotranspiration owing to dynamically evolving vegetation characteristics as opposed to a pre-determined climatology), thus potentially significantly modifying the predicted evapotranspiration. In terms of computing past values of evapotranspiration in analysis mode, the ability to simulate a prognostic plant biomass or *LAI* has allowed the development of schemes to assimilate local or satellite-based measures of *LAI* (e.g. Kumar et al[.](#page-29-28) [2019](#page-29-28); Bonan et al[.](#page-27-16) [2020\)](#page-27-16), thus potentially improving evapotranspiration estimates.

These complex coupled models add a significant number of parameters to the LSM. However, the modeling of such processes is key to making projections of feedbacks between the plant and the atmosphere for different future greenhouse gas scenarios, among other applications. For either of the *rc* approaches (including photosynthesis or not), the parametrization of soil moisture stress is of critical importance for computing *Etr*. Some LSMs using the approaches above also now include advanced moisture stress parametrizations which depend upon different types of drought responses and are distinguished for different types of vegetation (e.g. Calvet et al[.](#page-27-23) [2004\)](#page-27-23). Verhoef and Ege[a](#page-32-10) [\(2014\)](#page-32-10) compare several approaches for modeling the effect of soil moisture availability on the transpiration. They note that current methods used in most LSMs, mainly based on volumetric water content, are dated and more realistic simulations can be obtained based on using soil matric potential, and eventually chemical signaling and plant hydraulics models (including more sophisticated representations of rooting systems) in the future (since such methods require additional input parameters and observational data for a myriad of climates, soils and plant types).

The extraction of soil water by rooting systems is obviously of critical importance to transpiration, notably when defining the overall amount of water available to plants over an extended period. In terms of land–atmosphere interactions, Desboroug[h](#page-28-27) [\(1997](#page-28-27)) found that the treatment of root distribution had a considerable impact on simulated E_{tr} and discussed implications for fully coupled LSM–GCM models. Land-surface models have adopted essentially two approaches: using a single bulk root-zone water content in the stress function or using a weighting based on the assumed vertical root-zone profile which generally remains fixed in time. But several key processes are neglected using such simplified models. For example, Meunier et al[.](#page-30-23) [\(2018\)](#page-30-23) showed that roots were responsible for the transfer of moisture from deeper soil layers upwards toward the surface during the night, and this was responsible for upwards of 20% of the transpiration the following day. Also, obviously rooting systems are dynamic, and Zhu et al[.](#page-32-18) [\(2018\)](#page-32-18) showed that by modelling the temporal evolution of the root density for a wheat crop substantially improved the model estimates of transpiration.

6 Perspectives

The study of evapotranspiration brings together basic and applied scientific disciplines, indicating the need to work in an interdisciplinary framework to help progress understanding and to improve applications (Cuxart et al[.](#page-27-24) [2019;](#page-27-24) Verhoef et al[.](#page-32-19) [2020\)](#page-32-19). Advances rely on the availability of comprehensive and trustable data, adequate understanding of the basics of the process for proper analysis of the data and consequently the development of new and improved parametrizations for modeling and applications.

Reference data are now provided by lysimeters and EC systems that compare relatively well for monthly averages, but show significant discrepancies at the sub-daily scale. The study of fast response lysimeter data at a scale which resolves the diurnal cycle could pave a way forward in ABL research, since they can provide information when EC systems are not reliable, especially at night or in the presence of rain and dew.

Indirect determinations of evapotranspiration make use of MOST, which is valid for homogeneous terrain and for a range of thermal stabilities in the surface layer. Research on similarity theory over heterogeneous terrain and for very stable and unstable cases is needed in order to increase the usability of these methods. In the case of using the surface energy budget, there is a debate on how to distribute the imbalance between *H* and λE , as some use the Bowen ratio and others propose to attribute it all to evapotranspiration. Lysimeter data may help elucidate this aspect.

The classical Penman–Monteith and Priestley–Taylor approaches are still the backbones of evapotranspiration parametrization for well-watered vegetated terrain. In the former, complex mechanisms in the atmosphere (entrainment) and in the soil and vegetation are all packed in one single parameter, the surface or canopy resistance. Priestley–Taylor even avoids the use of this part and substitutes it by a parameter which is determined experimentally and that is related to the entrainment rate and the canopy resistance. At the daily scale, the Makkink–de Bruin expression, which depends only on the incident solar radiation, is an alternative.

The aforementioned methods have a difficult time handling non-saturated surfaces, in which the prescription of a value for the moisture of the surface is a key research issue. As the canopy characteristics get more complicated, with varying vertical and horizontal vegetation cover, new challenges appear, which are now mostly addressed using LES coupled with detailed LSMs, in which the details of the canopy can be explicitly introduced, progressing towards firmly establishing the basis of new expressions for these complex environments.

The treatment of heterogeneity is one of the major challenges ahead for the ABL community (Bou-Zeid et al[.](#page-27-25) [2020\)](#page-27-25). In the last decades, the Raupach and the advection-aridity frameworks have provided ways to conceptually address the analysis of the problem. The issue can also be explored using LES modelling, estimating the impact of prescribed surface heterogeneity, eventually combining it with experimental data from dense networks (Mengelkamp et al[.](#page-30-24) [2006](#page-30-24)). The development of parametrizations for evapotranspiration in heterogeneous terrain is an expected research activity in the coming years.

Land-surface models have evolved considerably since the 1990s, and development has greatly benefited in the past three decades from international collaborative efforts, as those hosted by the Global Energy and Water Exchanges (GEWEX) project, which is supported by the World Climate Research Programme (WCRP) within the World Meteorological Organization (WMO). In terms of improvements, processes which modulate the transpiration component of evapotranspiration have been added and are the focus of current and future development, such as photosynthesis and plant phenology, the use of explicit single or multilayer vegetation canopy schemes (along with more advanced representations of with-in canopy turbulence and radiative transfer) along with explicit forest litter. In terms of soil evaporation, parametrizations that are the focus of current research include multi-layer soil schemes which consider organic material, more sophisticated representations of soil water uptake by roots, more complex infiltration parametrizations, and agricultural practices, to name a few. But despite this progress, there are still well known issues, for example LSMs generally produce very different evapotranspiration fluxes given the same input atmospheric forcing and basic physiographic information (e.g. Best et al[.](#page-26-9) [2015\)](#page-26-9).

With the continuing emphasis on representing more sophisticated processes arising from ever-increasing applications (drought monitoring, climate models which are able to model the full coupling of the carbon cycle with the atmosphere, operational hydrological forecast systems, surface reanalysis products, seasonal weather forecasting for which the land holds a significant amount of predictability, etc.), a myriad of additional feedback mechanisms and empirical parameters are also being introduced. In order to keep making advances in terms of model physics, LSMs will require more experimental data and over more contrasting regions of the globe. Satellite-based products can assist in this regard, but they can still not replace data from high quality field sites which are critical for process understanding. But statistical methods are being increasingly used to optimally combine the aforementioned data with LSMs to provided improved estimates of evapotranspiration, such as machine learning for improving the model input parameters (Chaney et al[.](#page-27-26) [2016](#page-27-26)) and data assimilation for providing improved flux estimates (Bonan et al[.](#page-27-16) [2020](#page-27-16)). Thus, the future improvement in LSM physics and parameter estimation that modulate evapotranspiration will likely continue to progress in tandem, and will continue to benefit from improved methods to monitor evapotranspiration using the observational techniques discussed herein.

Finally, there is a growing effort in the scientific community to promote efforts to evaluate LSM schemes in fully coupled mode (van den Hurk et al[.](#page-31-20) [2011](#page-31-20)), despite the additional complexity compared to offline testing. It is anticipated that such efforts will lead to further improved understanding and modelling of coupled LSM evapotranspiration processes. This is of significance since there is a need to improve future GCM projections of water resource evolution.

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References

- Allen RG, Pereira LS, Raes D, Smith M (1998) Crop evapotranspiration: guidelines for computing crop water requirements, Irrigation and Drainage Paper 56. United Nations FAO, Rome, 300 p
- Ball JT, Woodrow IE, Berry JA (1987) A model predicting stomatal conductance and its contribution to the control of photosynthesis under different environmental conditions. In: Biggins J (ed) Progress in photosynthesis research. Springer, Dordrecht, pp 221–224
- Bélair S, Crevier L-P, Mailhot J, Bilodeau B, Delage Y (2003) Operational implementation of the ISBA land surfacescheme in the Canadian regional weather forecast model. Part I: warm season results. J Hydrometeorol 4:352–370
- Belcher SE, Harman IN, Finnigan JJ (2012) The wind in the willows: flows in forest canopies in complex terrain. Annu Rev Fluid Mech 44:479–504
- Best MJ, Abramowitz G, Johnson H, Pitman AJ, Boone A, Cuntz M, Decharme B, Dirmeyer PA, Dong J, Ek M, Haverd V, van den Hurk BJJM, Nearing GS, Pak B, Peters-Lidard C, Santanello JA Jr, Stevens L, Vuichard N (2015) The plumbing of land surface models. J Hydrometeorol 16:1425–1442
- Betts AK (1992) FIFE atmospheric boundary layer budget methods. J Geophys Res 97(D17):18523–18531
- Bhummralkar CM (1975) Numerical experiments on the computation of ground surface temperature in an atmospheric general circulation model. J Appl Meteorol 14:67–100
- Bliss AK, Cuffey KM, Kavanaugh JL (2011) Sublimation and surface energy budget of Taylor Glacier. Antarct J Glaciol 57(204):684–696
- Bonan GB, Lawrence PJ, Oleson KW, Levis S, Jung M, Reichstein M, Lawrence DM, Swenson SC (2011) Improving canopy processes in the Community Land Model version 4 (CLM4) using global flux fields empirically inferred from FLUXNET data. J Geophys Res Biogeosci 116(G2):G02014
- Bonan GB, Patton EG, Harman IN, Oleson KW, Finnigan JJ, Lu Y, Burakowski EA (2018) Modeling canopyinduced turbulence in the Earth system: a unified parameterization of turbulent exchange within plant canopies and the roughness sublayer (CLM-ml v0). Geosci Model Dev 11(1467–1496):2018
- Bonan B, Albergel C, Zheng Y, Barbu AL, Fairbairn D, Munier S, Calvet J-C (2020) An ensemble square root filter for the joint assimilation of surface soil moisture and leaf area index within the Land Data Assimilation System LDAS-Monde: application over the Euro-Mediterranean region. Hydrol Earth Syst Sci 24:325–347
- Bosilovich MG, Robertson FR, Chen J (2011) Global energy and water budgets in MERRA. J Clim 24(22):5721–5739

Bouchet RJ (1963) Evapotranspiration réelle et potentielle, signification climatique. IAHS Publ 62:134–142

- Boussetta S, Balsamo G, Beljaars A, Panareda A-A, Calvet J-C, Jacobs C, van den Hurk B, Viterbo P, Lafont S, Dutra E, Jarlan L, Balzarolo M, Papale D, van der Werf G (2013) Natural land carbon dioxide exchangesin the ECMWF integrated forecasting system: implementation and offline validation. J Geophys Res Atmos 118(12):5923–5946
- Bou-Zeid E, Anderson W, Mahrt L (2020) The persistent challenge of surface heterogeneity in boundary-layer meteorology. Boundary-Layer Meteorol. <https://doi.org/10.1007/s10546-020-00551>
- Brooks RH, Corey AT (1964) Hydraulic properties of porous media, Hydrol. Pap. 3, Civ. Eng. Dep., Colo. State Univ., Fort Collins
- Brubaker KL, Entekhabi D (1996) Analysis of feedback mechanisms in land–atmosphere interaction. Water Resour Res 32(5):1343–1357
- Brutsaert W (2015) A generalized complementary principle with physical constraints for land-surface evaporation. Water Resour Res 51(10):8087–8093
- Brutsaert W, Parlange MB (1998) Hydrologic cycle explains the evaporation paradox. Nature 396(6706):30
- Brutsaert W, Stricker H (1979) An advection-aridity approach to estimate actual regional evapotranspiration. Water Resour Res 15(2):443–450
- Businger JA, Wyngaard JC, Izumi Y, Bradley EF (1971) Flux-profile relationships in the atmospheric surface layer. J Atmos Sci 28(2):181–189
- Calvet JC, Noilhan J, Roujean J-L, Bessemoulin P, Cabelguenne M, Olioso A, Wigneron J-P (1998) An interactive vegetation SVAT model tested against data from six contrasting sites. Agric For Meteorol 92:73–95
- Calvet JC, Rivalland V, Picon-Cochard C, Guehl JM (2004) Modelling forest transpiration and CO₂ fluxes -response to soil moisture stress. Agric For Meteorol 124(3–4):143–156
- CarreraML, Bélair S, Bilodeau B (2015) The Canadian Land Data Assimilation System (CaLDAS): description and synthetic evaluation study. J Hydrometeorol 16:1293–1314
- Chaney NW, Herman JD, Ek M, Wood E (2016) Deriving global parameter estimates for the Noah land surface model using FLUXNET and machine learning. J Geophys Res Atmos 121:13218–13235
- Choudhury BJ, DiGirolamo NE (1998) A biophysical process-based estimate of global land surface evaporation using satellite and ancillary data. I. Model description and comparison with observations. J Hydrol 205:164–185
- Choudhury BJ, Monteith JL (1988) A four-layer model for the heat budget of homogeneous land surfaces. Q J R Meteorol Soc 114(480):373–398
- Coll C, Caselles V, Galve JM, Valor E, Niclòs R, Sánchez JM, Rivas R (2005) Ground measurements for the validation of land surface temperatures derived from AATSR and MODIS data. Remote Sens Environ 97(3):288–300
- Collatz GJ, Ribas-Carbó M, Berry JA (1992) Coupled photosynthesis-stomatal conductance model for leaves of c4 plants. Funct Plant Biol 19(5):519–538
- Cristea NC, Kampf SK, Burges SJ (2013) Revised coefficients for Priestley–Taylor and Makkink–Hansen equations for estimating daily reference evapotranspiration. J Hydrol Eng 18(10):1289–1300
- Cuxart J, Conangla L, Jimenez MA (2015) Evaluation of the surface energy budget equation with experimental data and the ECMWF model in the Ebro Valley. J Geophys Res Atmos 120(3):1008–1022
- Cuxart J, Wrenger B, Martínez-Villagrasa D, Reuder J, Jonassen MO, Jiménez MA, Lothon M, Lohou F, Hartogensis O, Dünnermann J, Conangla L, Garai A (2016) Estimation of the advection effects induced by surface heterogeneities in the surface energy budget. Atmos Chem Phys 16:9489–9504
- Cuxart J, Verhoef A, Marthews TR, Evans J (2019) Current challenges in Evapotranspiration determination. Gewex News 29(1):5–8
- de Bruin HAR (1983) A model for the Priestley–Taylor parameter? J Appl Meteorol Clim 22(4):572–578
- de Bruin HAR (1987) From Penman to Makkink. In: Evaporation and weather: technical meeting 44, Ede, The Netherlands 25 March 1987. The Hague, Netherlands, pp 5–31. 1 fig, 4 tab, 34 ref
- de Bruin HAR, Holtslag AAM (1982) A simple parameterization of the surface fluxes of sensible and latent heat during daytime compared with the Penman–Monteith concept. J Appl Meteorol Clim 21(11):1610–1621
- de Bruin HAR, Lablans WN (1998) Reference crop evapotranspiration determined with a modified Makkink equation. Hydrol Process 12(7):1053–1062
- de Bruin HAR, Trigo IF, Bosveld FC, Meirink JF (2016) A thermodynamically based model for actual evapotranspiration of an extensive grass field close to FAO Reference, suitable for remote sensing application. J Hydrometeorol 17(5):1373–1382
- De Roo F, Mauder M (2018) The influence of idealized surface heterogeneity on virtual turbulent flux measurements. Atmos Chem Phys 18(7):5059–5074
- Deardorff JW (1978) Efficient prediction of ground surface temperature and moisture, with inclusion of a layer of vegetation. J Geophys Res 83:1889–1903
- Desborough CE (1997) The impact of root weighting on the response of transpiration to moisture stress in land surface schemes. Mon Wea Rev 125(8):1920–1930
- Diaz-Espejo A, Verhoef A, Knight R (2005) Illustration of micro-scale advection using grid-pattern minilysimeters. Agric For Meteorol 129(1–2):39–52
- Dirmeyer PA, Gao X, Zhao M, Guo Z, Oki T, Hanasaki N (2006) GSWP-2: multimodel analysis and implications for our perception of the land surface. Bull Am Meteorol Soc 87(10):1381–1398
- Dragoni D, Lakso AN, Piccioni RM (2005) Transpiration of apple trees in a humid climate using heat pulse sap flow gauges calibrated with whole-canopy gas exchange chambers. Agr For Meteorol 130(1–2):85–94
- Edwards JM (2009) Radiative processes in the stable boundary layer: Part I. Radiative aspects. Boundary-Layer Meteorol 131(2):105
- Eichinger WE, Cooper DI, Hipps LE, Kustas WP, Neale CMU, Prueger JH (2006) Spatial and temporal variation in evapotranspiration using Raman lidar. Adv Water Resour 29(2):369–381
- Ek MB, Holtslag AAM (2004) Influence of soil moisture on boundary layer cloud development. J Hydrometeorol 5(1):86–99
- Ek M, Mitchell KE, Lin Y, Rogers E, Grunmann P, Koren V, Gayno G, Tarpley JD (2003) Implementation of Noah land-surface model advances in the NCEP operational mesoscale Eta model. J Geophys Res 108(D22):8851
- Escalona JM, Fuentes S, Tomàs M, Martorell S, Flexas J, Medrano H (2013) Responses of leaf night transpiration to drought stress in *Vitis vinifera* L. Agric Water Manag 118:50–58
- Farquhar G, von Caemmerer S, Berry J (1980) A biochemical model of photosynthetic CO. Planta 149(1):78– 90. <https://doi.org/10.1007/BF00386231>
- Finnigan JJ, Shaw RH, Patton EG (2009) Turbulence structure above a vegetation canopy. J Fluid Mech 637:387–424
- Flint AL, Childs SW (1991) Use of the Priestley–Taylor evaporation equation for soil water limited conditions in a small forest clearcut. Agric For Meteorol 56(3–4):247–260
- Foken T (2006) 50 years of the Monin–Obukhov similarity theory. Boundary-Layer Meteorol 119(3):431–447 Foken T (2017) Micrometeorology, 2nd edn. Springer, Berlin
- Garcia-Carreras L, Parker DJ, Taylor CM, Reeves CE, Murphy JG (2010) Impact of mesoscale vegetation heterogeneities on the dynamical and thermodynamic properties of the planetary boundary layer. J Geophys Res Atmos 115(D3):D13301
- Garcia-Gonzalez R, Verhoef A, Luigi Vidale P, Braud I (2012) Incorporation of water vapor transfer in the JULES land surface model: implications for key soil variables and land surface fluxes. Water Resour Res 48(5):W05538
- Gebler S, Franssen HH, Pütz T, Post H, Schmidt M, Vereecken H (2015) Actual evapotranspiration and precipitation measured by lysimeters: a comparison with eddy covariance and tipping bucket. Hidrol Earth Syst Sci 19(5):2145
- Gentine P, Chhang A, Rigden A, Salvucci G (2016) Evaporation estimates using weather station data and boundary layer theory. Geophys Res Lett 43(22):11–661
- Girona J, Mata M, Ferreres E, Goldhamer DA, Cohen M (2002) Evapotranspiration and soil water dynamics of peach trees under water deficits. Agric Water Manag 54(2):107–122
- Goudriaan J (1986) A simple and fast numerical method for the computation of daily totals of crop photosynthesis. Agric For Meteorol 38:249–254
- Groh J, Vanderborght J, Pütz T, Vereecken H (2016) How to control the lysimeter bottom boundary to investigate the effect of climate change on soil processes? Vadose Zone J 15(7):1–15
- Groh J, Slawitsch V, Herndl M, Graf A, Vereecken H, Pütz T (2018) Determining dew and hoar frost formation for a low mountain range and alpine grassland site by weighable lysimeter. J Hydrol 563:372–381
- Groh J, Pütz T, Gerke HH, Vanderborght J, Vereecken H (2019) Quantification and prediction of nighttime evapotranspiration for two distinct grassland ecosystems. Water Resour Res 55(4):2961–2975
- Habets F, Boone A, Champeaux JL, Etchevers P, Leblois E, Ledoux E, Le Moigne P, Martin E, Morel S, Segui Q, Rousset-Regimbeau F, Viennot P (2008) The SAFRAN-ISBA-MODCOU hydrometeorological model applied over France. J Geophys Res 113:D06113
- Hagemann S, Machenhauer B, Jones R, Christensen OB, Déqué M, Jacob D, Vidale PL (2004) Evaluation of water and energy budgets in regional climate models applied over Europe. Clim Dyn 23(5):547–567
- Han S, Hu H, Tian F (2012) A nonlinear function approach for the normalized complementary relationship evaporation model. Hydrol Process 26(26):3973–3981
- Hargreaves GH, Allen RG (2003) History and evaluation of Hargreaves evapotranspiration equation. J Irrig Drain E ASCE 129(1):53–63
- Harman IN (2012) The role of roughness sublayer dynamics within surface exchange schemes. Boundary-Layer Meteorol 142(1):1–20
- Heusinkveld BG, Berkowicz SM, Jacobs AF, Holtslag AA, Hillen WC (2006) An automated microlysimeter to study dew formation and evaporation in arid and semiarid regions. J Hydrometeorol 7(4):825–832
- Hicks BB, Baldocchi D (2020) Measurements of fluxes over land-capabilities, origins, and remaining challenges. Boundary-Layer Meteorol
- Hirschi M, Michel D, Lehner I, Seneviratne SI (2017) A site-level comparison of lysimeter and eddy covariance flux measurements of evapotranspiration. Hydrol Earth Syst Sci 21(3):1809–1825
- Högström U (1988) Non-dimensional wind and temperature profiles in the atmospheric surface layer: a reevaluation. Boundary-Layer Meteorol 42:55–78
- Jacobs CMJ, van den Hurk BMM, de Bruin HAR (1996) Stomatal behaviour and photosynthetic rate of unstressed grapevines in semi-arid conditions. Agric For Meteorol 80(24):111–134
- Jacobs AF, Heusinkveld BG, Holtslag AA (2008) Towards closing the surface energy budget of a mid-latitude grassland. Boundary-Layer Meteorol 126(1):125–136
- Jarvis PG (1976) The interpretation of the variations in leaf water potential and stomatal conductance found in canopies in the field. Philos Trans R Soc Lond Ser B 273:593–610
- Jasim UJ, Foley R, Hancock Smith N (2015) A new approach to estimate canopy evaporation and canopy interception capacity from evapotranspiration and sap flow measurements during and following wetting. Hydrol Process 30(11):1757–1767
- Jia Z, Liu S, Xu Z, Chen Y, Zhu M (2012) Validation of remotely sensed evapotranspiration over the Hai River Basin, China. J Geophys Res Atmos 117(D13):D13113
- Jiang L, Islam S (2001) Estimation of surface evaporation map over southern Great Plains using remote sensing data. Water Resour Res 37(2):329–340
- Jones HG (2013) Plants and microclimate: a quantitative approach to environmental plant physiology. Cambridge University Press, Cambridge
- Katul GG, Oren R, Manzoni S, Higgins C, Parlange MB (2012) Evapotranspiration: a process driving mass transport and energy exchange in the soil-plant-atmosphere-climate system. Rev Geophys 50(3):185–201
- Kim CP, Entekhabi D (1998) Feedbacks in the land-surface and mixed-layer energy budgets. Boundary-Layer Meteorol 88(1):1–21
- Kivalov SN, Fitzjarrald DR (2019) Observing the whole-canopy short-term dynamic response to natural step changes in incident light: characteristics of tropical and temperate forests. Boundary-Layer Meteorol 173(1):1–52
- Kooijmans LM, Hartogensis OK (2016) Surface-layer similarity functions for dissipation rate and structure parameters of temperature and humidity based on eleven field experiments. Boundary-Layer Meteorol 160(3):501–527
- Krinner G, Viovy N, de Noblet-Ducoudre N, Ogee J, Polcher J, Friedlingstein P, Ciais P, Sitch S, Prentice IC (2005) A dynamic global vegetation model for studies of the coupled atmosphere–biosphere system. Global Biogeochem Cycles 19:GB1015
- Kumar S, Mocko DM, Wang S, Peters-Lidard CD, Borak J (2019) Assimilation of remotely sensed leaf area index into the Noah-MP land surface model: impacts on water and carbon fluxes and states over the continental United States. J Hydrometeorol 20(7):1359–1377
- Lee X, Massman W, Law B (eds) (2004) Handbook of micrometeorology: a guide for surface flux measurement and analysis, vol 29. Springer, Berlin
- Liu W, Wang L, Zhou J, Li Y, Sun F, Fu G, Li X, Sang YF (2016) A worldwide evaluation of basin-scale evapotranspiration estimates against the water balance method. J Hydrol 538:82–95
- Lohou F, Patton EG (2014) Surface energy balance and buoyancy response to shallow cumulus shading. J Atmos Sci 71(2):665–682
- López-Urrea R, de Santa Olalla FM, Fabeiro C, Moratalla A (2006) Testing evapotranspiration equations using lysimeter observations in a semiarid climate. Agric Water Manag 85(1–2):15–26
- Louis J-F (1979) A parametric model of vertical eddy fluxes in the atmosphere. Boundary-Layer Meteorol 17:187–202
- Mahfouf J-F, Noilhan J (1991) Comparative study of various formulations of evaporation from bare soil using in situ data. J Appl Meteorol 9:351–362
- Mahrt L (2014) Stably stratified atmospheric boundary layers. Annu Rev Fluid Mech 46:23–45
- Mahrt L, Pan HL (1984) A 2-layer model of soil hydrology. Boundary-Layer Meteorol 29:1–20
- Makkink GF (1957) Testing the Penman formula by means of lysimeters. J Inst Water Eng 11:277–288
- Mauder M, Foken T, Cuxart J (2020) Surface energy balance closure over land: a review. Boundary-Layer Meteorol 176(1):85–103
- McColl KA (2020) Practical and theoretical benefits of an alternative to the Penman–Monteith evapotranspiration equation. Water Resour Res e2020WR027106
- McColl KA, Rigden AJ (2020) Emergent simplicity of continental evapotranspiration. Geophys Res Lett 47(6):e2020GL087101
- McColl KA, Salvucci GD, Gentine P (2019) Surface flux equilibrium theory explains an empirical estimate of water-limited daily evapotranspiration. J Adv Mod Earth Syst 11(7):2036–2049
- Meijninger WML, Green AE, Hartogensis OK, Kohsiek W, Hoedjes JCB, Zuurbier RM, de Bruin HAR (2002) Determination of area-averaged water vapour fluxes with large aperture and radio wave scintillometers over a heterogeneous surface-Flevoland field experiment. Boundary-Layer Meteorol 105(1):63–83
- Mengelkamp HT, Beyrich F, Heinemann G, Ament F, Bange J, Berger F, Huneke S (2006) Evaporation over a heterogeneous land surface. Bull Am Meteorol Soc 87(6):775–786
- Merlin O, Bitar AA, Rivalland V, Baziat P, Ceschia E, Dedieu G (2011) An analytical model of evaporation efficiency for unsaturated soil surfaces with an arbitrary thickness. J Appl Meteorol 50:457–471
- Meunier F, Rothfuss Y, Bariac T, Biron P, Richard P, Durand J-L, Couvreur V, Vanderborght J, Javaux M (2018) Measuring and modeling hydraulic lift of *Lolium multiflorum* using stable water isotopes. Vadose Zone J 17:160134
- Milly PCD (1992) Potential evaporation and soil moisture in general circulation models. J Clim 5:209–226
- Miralles DG, De Jeu RA, Gash JH, Holmes TR, Dolman AJ (2011) Magnitude and variability of land evaporation and its components at the global scale. Hydrol Earth Syst Sci 15:453–469
- Moene AF, Van Dam JC (2014) Transport in the atmosphere–vegetation–soil continuum. Cambridge University Press, Cambridge
- Monin AS, Obukhov AM (1954) Basic laws of turbulent mixing in the surface layer of the atmosphere. Contrib Geophys Inst Acad Sci USSR 151(163):e187
- Monteith JL (1965) Evaporation and environment. In: Symposia of the society for experimental biology, vol 19. Cambridge University Press, Cambridge, pp 205–234
- Napoly A, Boone A, Samuelsson P, Gollvik S, Martin E, Seferian R, Carrer D, Decharme B, Jarlan L (2017) The interactions between soil–biosphere–atmosphere (ISBA) land surface model multi-energy balance (MEB) option in SURFEX—Part 2: model evaluation for local scale forest sites. Geosci Model Dev 10:1621–1644
- Naudts K, Ryder J, McGrath MJ, Otto J, Chen Y, Valade A, Bellasen V, Berhongaray G, Bonisch G, Campioli M, Ghattas J, De Groote T, Haverd V, Kattge J, MacBean N, Maignan F, Merila P, Peñuelas J, Peylin P, Pinty B, Pretzsch H, Schulze ED, Solyga D, Vuichard N, Yan Y, Luyssaert S (2015) A vertically discretised canopy description for ORCHIDEE (SVN r2290) and the modifications to the energy, water and carbon fluxes. Geosci Model Dev 8:2035–2065
- Noilhan J, Planton S (1989) A simple parameterization of land surface processes for meteorological models. Mon Wea Rev 117(3):536–549
- Or D, Lehmann P, Shahraeeni E, Shokri N (2013) Advances in soil evaporation physics—a review. Vadose Zone J 12(4):1–16
- Parlange MB, Katul GG (1992) An advection-aridity evaporation model. Water Resour Res 28(1):127–132
- Paulson CA (1970) The mathematical representation of wind speed and temperature profiles in the unstable atmospheric surface layer. J Appl Meteorol 9(6):857–861
- Pedruzo-Bagazgoitia X, Ouwersloot HG, Sikma M, Van Heerwaarden CC, Jacobs CMJ, Vila-Guerau de Arellano J (2017) Direct and diffuse radiation in the shallow cumulus–vegetation system: enhanced and decreased evapotranspiration regimes. J Hydrometeorol 18(6):1731–1748
- Penman HL (1948) Natural evaporation from open water, bare soil and grass. Proc R Soc Lond Ser A Math Phys Sci 193(1032):120–145
- Pereira LS, Allen RG, Smith M, Raes D (2015) Crop evapotranspiration estimation with FAO56: past and future. Agric Water Manag 147:4–20
- Pérez-Priego O, López-Ballesteros A, Sánchez-Cañete EP, Serrano-Ortiz P, Kutzbach L, Domingo F, Eugster W, Kowalski AS (2015) Analysing uncertainties in the calculation of fluxes using whole-plant chambers: random and systematic errors. Plant Soil 393(1–2):229–244
- Priestley CHB, Taylor RJ (1972) On the assessment of surface heat flux and evaporation using large-scale parameters. Mon Wea Rev 100(2):81–92
- Pütz T, Kiese R, Wollschläger U, Groh J, Rupp H, Zacharias S, Borg E (2016) TERENO-SOILCan: a lysimeternetwork in Germany observing soil processes and plant diversity influenced by climate change. Environ Earth Sci 75(18):1242
- Raupach MR (1994) Simplified expressions for vegetation roughness length and zero-plane displacement as functions of canopy height and area index. Boundary-Layer Meteorol 71:211–216
- Raupach MR (2000) Equilibrium evaporation and the convective boundary layer. Boundary-Layer Meteorol 96(1–2):107–142
- Rijtema PE (1965) An analysis of actual evapotranspiration. Doctoral dissertation, Pudoc
- Roerink GJ, Su Z, Menenti M (2000) S-SEBI: a simple remote sensing algorithm to estimate the surface energy balance. Phys Chem Earth Part B Hydrol Oceans Atmos 25(2):147–157
- Sakaguchi K, Zeng X (2009) Effects of soil wetness, plant litter,and under-canopy atmospheric stability on ground evaporation in the Community Land Model (CLM3.5). J Geophys Res 114:D01107
- Schrader F, Durner W, Fank J, Gebler S, Pütz T, Hannes M, Wollschläger U (2013) Estimating precipitation and actual evapotranspiration from precision lysimeter measurements. Procedia Environ Sci 19:543–552
- Seity Y, Brousseau P, Malardel S, Hello G, Bénard P, Bouttier F, Lac C, Masson V (2011) The AROME-France Convective-Scale operational model. Mon Wea Rev 139(3):976–991
- Sellers PJ, Mintz Y, Sud YC, Dalcher A (1986) The design of a Simple Biosphere model (SiB) for use within general circulation models. J Atmos Sci 43:505–531
- Sellers PJ, Heiser MD, Hall FG (1992) Relations between surface conductance and spectral vegetation indices at intermediate (100 m² to 15 km²) length scales. J Geophys Res 97:19033-19059
- Seneviratne SI, Lehner I, Gurtz J, Teuling AJ, Lang H, Moser U, Zappa M (2012) Swiss prealpine Rietholzbach research catchment and lysimeter: 32 year time series and 2003 drought event. Water Resour Res 48(6):W06526
- Shuttleworth WJ (2007) Putting the vap into evaporation. Hydrol Earth Syst Sci 11(1):210–244
- Shuttleworth WJ, Wallace JS (1985) Evaporation from sparse crops: an energy combination theory. Q J R Meteorol Soc 111(469):839–855
- Sikma M, Vilà-Guerau de Arellano J (2019) Substantial reductions in cloud cover and moisture transport by dynamic plant responses. Geophys Res Lett 46(3):1870–1878
- Sikma M, Vilà-Guerau de Arellano J, Pedruzo-Bagazgoitia X, Voskamp T, Heusinkveld BG, Anten NPR, Evers JB (2019) Impact of future warming and enhanced [CO2] on the vegetation? Cloud interaction. J Geophys Res Atmos 124(23):12444–12454
- Simó G, Martínez-Villagrasa D, Jiménez MA, Caselles V, Cuxart J (2018) Impact of the surface-atmosphere variables on the relation between air and Land Surface Temperatures. Pure Appl Geophys 175(11):3939– 3953
- Simó G, Cuxart J, Jiménez MA, Martínez-Villagrasa D, Picos R, López-Grifol A, Martí B (2019) Observed atmospheric and surface variability on heterogeneous terrain at the hectometre scale and related advective transports. J Geophys Res Atmos 124(16):9407–9422
- Sinclair TR, Murphy CE, Knoerr KR (1976) Development and evaluation of simplified models for simulating canopy photosynthesis and transpiration. J Appl Ecol 13:813–829
- Snow AD, Christensen SD, Swain NR, Nelson EJ, Ames DP, Jones NL, Ding D, Noman NS, David CH, Pappenberger F, Zsoter E (2016) A high-resolution national-scale hydrologic forecast system from a global ensemble land surface model. J Am Water Res Assoc (JAWRA) 52(4):950–964
- Stewart JB (1988) Modelling surface conductance of pine forest. Agric For Meteorol 43(1):19–35
- Thornthwaite CW (1948) An approach toward a rational classification of climate. Geograph Rev 38(1):55–94 Trenberth KE, Smith L, Qian T, Dai A, Fasullo J (2007) Estimates of the global water budget and its annual cycle using observational and model data. J Hydrometeorol 8(4):758–769
- Trenberth KE, Fasullo JT, Kiehl J (2009) Earth's global energy budget. Bull Am Meteorol Soc 90(3):311–324
- Trigo IF, de Bruin H, Beyrich F, Bosveld FC, Gavilán P, Groh J, López-Urrea R (2018) Validation of reference evapotranspiration from Meteosat Second Generation (MSG) observations. Agric For Meteorol 259:271– 285
- Trugman AT, Medvigy D, Mankin JS, Anderegg WRL (2018) Soil moisture stress as a major driver of carbon cycle uncertainty. Geophys Res Lett 45(13):6495–6503
- Vallis GK, Parker DJ, Tobias SM (2019) A simple system for moist convection: the rainy-Benard model. J Fluid Mech 862:162–199. <https://doi.org/10.1017/jfm.2018.954>
- Vila-Guerau de Arellano J, Ney P, Hartogensis O, de Boer H, van Diepen K, Emin D, de Groot G, Klosterhalfen A, Langensiepen M, Matveeva M, Miranda G, Moene A, Rascher U, Röckmann T, Adnew G, Graf A (2020) CloudRoots: integration of advanced instrumental techniques and process modelling of subhourly and sub-kilometre land-atmosphere interactions. Biogeosci Discus. [https://doi.org/10.5194/bg-](https://doi.org/10.5194/bg-2020-132)[2020-132](https://doi.org/10.5194/bg-2020-132)
- van Den Hoof C, Vidale PL, Verhoef A, Vincke C (2013) Improved evaporative flux partitioning and carbon flux in the land surface model JULES: impact on the simulation of land surface processes in temperate Europe. Agric For Meteorol 181:108–124
- van den Hurk B, Best M, Dirmeyer P, Pitman A, Polcher J, Santanello J (2011) Acceleration of land surface model development over a decade of glass. Bull Am Meteorol Soc 92:1593–1600
- van Dijk AI, Gash JH, van Gorsel E, Blanken PD, Cescatti A, Emmel C, Montagnani L (2015) Rainfall interception and the coupled surface water and energy balance. Agric For Meteorol 214:402–415
- van Genuchten MT (1980) A closed-form equation for prediction the hydraulic conductivity of unsaturated soils. Soil Sci Soc Am J 44:892–898
- van Heerwaarden CC, Vila-Guerau de Arellano J, Moene AF, Holtslag AA (2009) Interactions between dryair entrainment, surface evaporation and convective boundary-layer development. Q J R Meteorol Soc 135(642):1277–1291
- van Heerwaarden CC, Mellado JP, De Lozar A (2014) Scaling laws for the heterogeneously heated free convective boundary layer. J Atmos Sci 71(11):3975–4000
- Verhoef A, Egea G (2014) Modeling plant transpiration under limited soil water: comparison of different plant and soil hydraulic parameterizations and preliminary implications for their use in land surface models. Agric For Meteorol 191:22–32
- Verhoef A, Diaz-Espejo A, Knight JR, Villagarcia L, Fernandez JE (2006) Adsorption of water vapor by bare soil in an olive grove in southern Spain. J Hydrometeorol 7(5):1011–1027
- Verhoef A, Cuxart J, Marthews TR, Evans J, van Oevelen P (2020) Report on the first determining evapotranspiration workshop. GEWEX Q 30(1):p16
- Wang J, Bras RL (2009) A model of surface heat fluxes based on the theory of maximum entropy production. Water Resour Res 45(11):W11422
- Wang J, Bras RL (2011) A model of evapotranspiration based on the theory of maximum entropy production. Water Resour Res 47(3):W03521
- Wang YP, Leuning R (1998) A two-leaf model for canopy conductance, photosynthesis and partitioning of available energy I: model description and comparison with a multi-layered model. Agric For Meteorol 91(1–2):89–111
- Wang J, Salvucci GD, Bras RL (2004) An extremum principle of evaporation. Water Resour Res 40(9):W09303
- Wang D, Wang G, Anagnostou EN (2007) Evaluation of canopy interception schemes in land surface models. J Hydrol 347:308–318
- Ward HC, Evans JG, Hartogensis OK, Moene AF, de Bruin HAR, Grimmond CSB (2013) A critical revision of the estimation of the latent heat flux from two-wavelength scintillometry. Q J R Meteorol Soc 139(676):1912–1922
- Wetzel PJ, Chang JT (1987) Concerning the relationship between evapotranspiration and soil moisture. J Clim Appl Meteorol 26:18–27
- Wilson T, Meyers T, Kochendorfer J, Anderson M, Heuer M (2012) The effect of soil surface litter residue on energy and carbon fluxes in a deciduous forest. Agric For Meteorol 161:134–147
- Woods DB, Turner NC (1971) Stomatal response to changing light by four tree species of varying shade tolerance. New Phytol 70(1):77–84
- Wulfmeyer V, Pal S, Turner DD, Wagner E (2010) Can water vapour Raman lidar resolve profiles of turbulent variables in the convective boundary layer? Boundary-Layer Meteorol 136(2):253–284
- Yang Z-L, Niu G-Y, Mitchell KE, Chen F, Ek MB, Barlage M, Longuevergne L, Manning K, Niyogi D, Tewari M, Xia Y (2011) The community Noah land surface model with multi-parameterization options (Noah-MP): 2. Evaluation over global river basins. J Geophys Res 116:D12110
- Zhang K, Kimball JS, Running SW (2016) A review of remote sensing based actual evapotranspiration estimation. Wiley Interdiscip Rev Water 3(6):834–853
- Zhu Y, Ren L, Horton R, Lu H, Wang Z, Yuan F (2018) Estimating the contribution of groundwater to the root zone of winter wheat, using root density distribution functions. Vadose Zone J 17:170075

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