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Numerical modeling of the interaction of normal fault and shallow embedded foundation

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Abstract

The consequences to structures caused by permanent fault displacement have been investigated for dip-slip faulting, but not for the efect of the embedment depth on the interaction between a normal fault rupture and shallow embedded foundation. This study investigated the efect of the embedment depth on the interaction of normal fault rupture and shallow foundation using a numerical model validated with centrifuge experiments. It was found that a gapping interaction mechanism and foundation distress occurred at diferent foundation positions relative to the fault rupture outcrop for an embedded foundation in comparison with a surface foundation. The extent of this area depended on the combined infuences of the foundation position, foundation surcharge, embedment depth, and fault dip angle. The sidewalls of the shallow embedded foundation were observed to act as kinematic constraints and had considerable infuence on the rotation, displacement and stressing of the foundations. With regard to the level of rotation and displacement of the embedded foundation, the lateral earth pressure distribution on the footwall sidewall was similar to that of Rankine active earth pressure in a triangular distribution and on the hangingwall sidewall as a parabolic distribution of passive earth pressure. Foundations laid on loose soil exhibited less rotation than those on dense soil because the fault ruptures were absorbed or bifurcated around both sides of the foundation.

Keywords Normal fault rupture · Shallow foundation · Embedment depth · Numerical modeling

1 Introduction

The propagation of a fault rupture through the soil layer is a hazard associated with fault-induced dislocation. Most research on this occurrence was initiated after the 1999 earthquakes in Turkey and Taiwan (Ulusay et al. [2002](#page-27-0); Dong et al. [2003](#page-26-0)) and the 2008

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earthquake in Wenchuan, China (Lin and Ren [2009\)](#page-26-1). The destruction from these earthquakes clarifed the efect of a fault rupture on structures located near the fault trace at the ground surface. These studies focused on free-feld fault rupture propagation, the interaction of the structures and the fault, and mitigation strategies for decreasing the efects of fault-structure interaction by feld investigations (Faccioli et al. [2008;](#page-26-2) Lin et al. [2006](#page-27-1)), experimental studies (Bransby et al. [2008a](#page-26-3),[b;](#page-26-4) Rojhani et al. [2012](#page-27-2); Ashtiani et al. [2015;](#page-26-5) Ahmadi et al. [2018;](#page-26-6) Yao and Takemura [2019;](#page-27-3) Sadra et al. [2020;](#page-27-4) Fadaee et al. [2020;](#page-26-7) Yao et al. [2020a,](#page-27-5) [b](#page-27-6); Sabagh and Ghalandarzadeh [2020a, b](#page-27-7)), and numerical modeling (Bray et al. [1994a;](#page-26-8) Anastasopoulos et al. [2007](#page-26-9), [2008,](#page-26-10) [2009;](#page-26-11) Oettle and Bray [2016](#page-27-8); Baziar et al. [2019;](#page-26-12) Agalianos et al. [2020;](#page-26-13) Naeij and Soroush [2021;](#page-27-9) Rasouli and Fatahi [2020](#page-27-10); Azizkandi et al. [2021\)](#page-26-14).

Research on free-feld fault rupture propagation was performed to determine the pattern of rupture propagation through the overburden (Cole and Lade [1984;](#page-26-15) Bray et al. [1994a;](#page-26-8) Ng et al. [2012](#page-27-11); Yao et al. [2020a](#page-27-5)) and the height of fault rupture emergence at the ground surface (Bray et al. [1994b\)](#page-26-16). The studies showed that the pattern of rupture propagation of a dip-slip fault through the soil layer depended on the alluvium depth, soil characteristics, fault dip angle, and fault type. Many buildings have been destroyed by permanent ground displacement during an earthquake. However, the fault ruptures can be diverted in some cases or the level of damage to a building could be reduced (Faccioli et al. [2008](#page-26-2)). This has been observed in studies on fault rupture-structure interaction that have specifed the infuence of important parameters on the interaction (e.g., Bransby et al. [2008a,](#page-26-3) [b](#page-26-4); Gazetas et al. [2008;](#page-26-17) Anastasopoulos et al. [2009;](#page-26-11) Ashtiani et al. [2015;](#page-26-5) Oettle and Bray [2016;](#page-27-8) Naeij and Soroush [2021\)](#page-27-9). These parameters include the type of fault, fault dip angle, type and stifness of the soil, alluvium depth on bedrock, building weight, type and rigidity of the foundation, position of the foundation relative to fault rupture emergence at the ground surface, and the condition of the superstructure. Nevertheless, further investigation is required on the diferent aspects of structure-fault interaction and strategies for decreasing the hazards associated with the fault rupture on buildings.

Most of the research mentioned above has been performed on buildings with shallow foundations located at the ground surface (i.e., without embedment depth). In urban settings, a lack of space and the need for parking space require excavation of foundations for the construction of buildings with one or more basement stories. It is clear that ignoring to address the embedment depth of shallow foundations can afect these previously studied behaviors. Therefore, the infuence of foundation embedment depth on the buildingfault rupture interaction must be investigated. Ashtiani et al. ([2015\)](#page-26-5) investigated the efect of foundation embedment depth on the interaction of buildings and reverse fault rupture using centrifuge modeling. Ashtiani and Ghalandarzadeh [\(2020](#page-26-18)) and Naeij et al. [\(2019](#page-27-12)) carried out complementary studies on the interaction of embedded shallow foundations and reverse faulting. They concluded that the combined efect of the foundation embedment depth, surcharge, and position will cause a change in the interaction behavior. Loli et al. ([2011,](#page-27-13) [2012\)](#page-27-14) investigated the behavior of caisson foundations afected by dip-slip faults. Their results showed that the caisson foundation caused the deviation or difusion of the fault rupture. Also, with regard to the foundation rigidity and its constraints, fault-induced dislocation had relatively little infuence on the caisson foundation.

As the interaction of a shallow embedded foundation and a normal fault rupture has not yet been investigated, the current study focused on the efect of foundation embedment depth. Finite element software and a modifed Mohr–Coulomb constitutive model were used when considering the internal friction angle and dilation softening behavior and were implemented as a user subroutine into the program. The numerical model was validated

according to the centrifuge results. The efect of the parameters of foundation embedment depth, fault dip angle, position of the foundation relative to the fault rupture, and the foundation surcharge were considered in the model. In this study, the foundation rotation, profle of the ground surface, and the earth pressure distribution on the foundation sidewalls have been examined.

2 Problem defnition

Figure [1a](#page-2-0) shows the interaction of a shallow embedded foundation and normal faulting for the problem under study. This includes a uniform soil layer with thickness $H=25$ m and model length L , where the normal fault moves with dip angle α and creates downward displacement having vertical component *h*. After propagation of the fault rupture through the soil layer, the shear-band strikes a shallow foundation with breadth *B*, embedment depth *D*, and applied pressure *q*. The distance between the bottom left edge of the foundation and the fault rupture emergence at the ground surface specifes the position of the foundation. As a result of fault rupture propagation, the ground surface is displaced (δy) and the foundation experiences rotation θ and translational displacement Δ . Embedment depths of 0, 3,

Fig. 1 Problem defnition: **a** interaction between a normal fault rupture and shallow foundation with breadth *B*, embedment depth *D*, and surcharge *q*; **b** positions of shallow foundations relative to free-feld fault rupture

6, and 9 m were examined. A depth of zero relates to the foundation at the ground surface (i.e., surface foundation) and the other depths are for shallow embedded foundations.

It is important to note that, when a foundation is embedded, the position at which the free-feld fault rupture strikes the foundation base will change. In other words, for a specifed foundation position, the values of parameter *s* will not be the same at diferent embed-ment depths, as is shown in Fig. [1](#page-2-0)b. Because parameter s is a factor affecting the foundation-fault interaction, the horizontal position of the foundation will change with an increase in the embedment depth in order to maintain a constant value for *s*.

2.1 Finite element model

Two-dimensional plane strain numerical modeling was performed using ABAQUS fnite element software. To minimize the infuence of the boundaries on the results of modeling, the width of the models was set at $L=4H$ (Bray et al. [1994a](#page-26-8)). A 4-node rectangular plane strain element with a width of $d_{FF} = 0.5$ m was used to model the soil. The mesh size was selected using sensitivity analysis for models with elements of 1.0 and 0.5 m in width. It was found that models with element widths of 0.5 m were more consistent with the experimental results. The position of the fault outcropping and the foundation rotation were predicted with better accuracy in models with an element width of 0.5 m than of 1.0 m.

A foundation with breadth *B* and embedment depth *D* was modeled with beam elements and high elastic parameters to provide a rigid foundation. A beam element was used to model the surface foundation. For the embedded foundation, four beam elements were used to model the elements of the bottom, top, and sidewalls of the foundation such that the connection of these elements created a box with embedment depth *D*. The numerical analysis assumed that the bending rigidity of the foundation sidewalls was similar to that of the foundation basement.

The interface between the sidewalls and base of the embedded foundation and the soil was considered using a gap element (Anastasopoulos et al. [2008\)](#page-26-10). Gap elements are infnite in compression, but ofer no resistance in tension and their behavior for shearing follows Columbus's friction law. The coefficient of friction was based on the friction between the soil and the concrete to be 2/3φ, where φ is the internal friction angle of the soil. Displacement was applied to the right boundaries of the model (the hanging wall) in a pseudo-static manner in small increments to prevent the numerical model from becoming unstable during the solution.

2.2 Soil constitutive model

Studies have shown that the post-peak behavior of the soil is important to the accurate prediction of fault rupture propagation through the soil layer and the fault rupture-structure interaction (Anastasopoulos et al. [2007](#page-26-9), [2009](#page-26-11); Oettle and Bray [2016;](#page-27-8) Naeij and Soroush [2021\)](#page-27-9). Dense sand exhibits post-peak softening and reaches a critical state (residual) condition. In the present study, the modifed Mohr–Coulomb constitutive model with postpeak softening was incorporated into ABAQUS through a user subroutine (UMAT), which was similar to that of Anastasopoulos et al. (2007) (2007) . In this constitutive model, the postpeak behavior, as the peak friction angle and dilation angle (φ _{*P*} and ψ _{*P*}) linearly decreased to the residual values (φ_{res} and $\psi_{res} = 0$) with an increase in the plastic shear strain (γ^P).

$$
\varphi_{mob} = \begin{cases}\n\varphi_P - \frac{\varphi_P - \varphi_{res}}{\gamma_f^P} \gamma^P & \text{for } 0 \le \gamma^P < \gamma_f^P \\
\varphi_{res} & \text{for } \gamma^P \ge \gamma_f^P\n\end{cases}
$$
\n
$$
\psi_{mob} = \begin{cases}\n\psi_P \left(1 - \frac{\gamma^P}{\gamma_f^P}\right) & \text{for } 0 \le \gamma^P < \gamma_f^P \\
\psi_{res} = 0 & \text{for } \gamma^P \ge \gamma_f^P\n\end{cases}
$$
\n(2)

where γ_f^P is the plastic shear strain at failure in which softening is complete.

Anastasopoulos et al. ([2007\)](#page-26-9) proposed Eq. ([3\)](#page-4-0) to calculate γ_f^p by considering the mesh dependency (Gudehus and Nubel, [2004](#page-26-19)) and scale effects (Muir Wood, [2002](#page-27-15)) when comparing the results of numerical modeling with those of the centrifuge experiment.

$$
\gamma_f^p = \frac{\delta x_p - \delta x_y}{D} + \frac{\delta x_f - \delta x_p}{d_{FE}}N\tag{3}
$$

where *N* is the centrifugal acceleration, d_{FE} is the mesh size in the shear-band area of numerical modeling, *D* is the sample height in the direct shear test, and δx_v , δx_p , and δx_f were obtained from the results of the direct shear tests. When modeled as a real-scale problem, *N* must be equal to one.

In this study, dense and loose granular types of sand were used in the modeling. The strength and deformation parameters of the ideal granular soil types are shown in Table [1](#page-4-1). The soil modulus of elasticity was considered as a variable that is a function of the soil depth.

2.3 Parameters used in numerical modeling

The parameters used in the numerical analysis, the embedment depth of the foundation, its location relative to the fault rupture trace at the ground surface, foundation surcharge, and fault dip angle are summarized in Table [2.](#page-5-0) The numerical models were analyzed for a soil depth of 25 m and a foundation breadth of 10 m. Assuming the weight per unit of area of each story to be 10 kN/m², the foundation surcharges considered were equal to 40, 60, 80, 100, and 120 kPa. These pressures represent 4, 6, 8, 10, and 12 story buildings, respectively. The embedment depth to breadth ratios were *D/B*=0 (surface foundation) and $D/B = 0.3$, 0.6, and 0.9 (embedded foundations). The rigidity of the foundation of $EI = 10^8$ $kN.m²$ represents a rigid foundation. The dip angles of the normal fault used for numerical analysis were $\alpha = 45^{\circ}$, 60°, 75° and 90°.

Sand		Density γ Peak friction Residual (kg/m^3) angle φ_p (°) friction	angle, φ_{res} (°)	Dilation angle ψ_p (°) tic shear	Failureplas- strain γ_c^p	Modulus of elasticity, E (MPa)	Poisson ratio, ν
Dense 2000		45	30	18	0.05	$2.25Z*$	0.3
Loose	1600	32	30		0.08	0.75Z	0.35

Table 1 Soil parameters used in numerical analysis (Anastasopoulos et al. [2007\)](#page-26-9)

*Z is soil depth

The maximum ratio of fault vertical displacement to soil depth was $h/H = 5\%$, where $h=1.25$ m and $H=25$ m. This value of displacement for a normal fault is approximately proportional to an earthquake of magnitude 6.8 as presented in the correlation by Wells and Coppersmith ([1994\)](#page-27-16).

3 Validation

Normal fault rupture-shallow foundation interaction tests were conducted in a beam centrifuge at the University of Dundee (Bransby et al. [2008a](#page-26-3)). These tests were conducted at 115 g on *Dr*=60% Fontainebleau sand and simulated the free-feld normal fault rupture propagation and normal fault rupture-foundation interaction. They investigated the patterns of fault rupture propagation through a sandy soil deposit and the diferent mechanisms for the diferent foundation positions. The foundation was located on a 25 m sand deposit. The parameters for the centrifuge model tests for verifcation with numerical analysis are sum-marized in Table [3](#page-5-1) (Bransby et al. [2008a](#page-26-3)). The properties of the sand used in the centrifuge model tests are presented in Table [4](#page-6-0) (Anastasopoulos et al. [2007\)](#page-26-9).

Before the investigation of the fault rupture-foundation interaction, free-feld fault rupture propagation through the soil layer was modeled to provide a base condition. Figure [2](#page-7-0)a shows the deformed model for the free-field condition at $H=25$ m in dry sand at $D_r=60\%$ that has been subjected to a normal fault at $\alpha = 60^\circ$. In Fig. [2](#page-7-0)a and b, the fault rupture deviated towards the hanging wall as it propagated toward the ground surface. A comparison shows satisfactory consistency between the results of the centrifuge model tests and numerical analysis. Figure [2c](#page-7-0) shows good agreement for vertical displacement δy at the soil surface between the experimental and numerical results.

In Table [3](#page-5-1), tests 2 and 3 verify the numerical modeling of normal fault rupture-foundation interaction. All parameters were similar to those of the free-feld test, except that the foundation surcharges were diferent (37 and 90 kPa represent light and heavy foundations, respectively) and were approximately positioned at $s/B = 0.3$ $s/B = 0.3$. Figures 3 and [4](#page-9-0) show the

Test no.	Height, $H(m)$ Length, $L(m)$		Dip angle of Foundation fault, α (°)	breadth, $B(m)$ position, s/B	Foundation	Foundation surcharge, q (kPa)
	25	76	60			
\overline{c}	25	76	60	10	0.31	37
3	25	76	60	10	0.29	90

Table 3 Characteristics of models used to validate numerical analysis (Bransby et al. [2008a\)](#page-26-3)

Fig. 2 Free-feld normal faulting propagation at a dip angle of 60° through 2.16 m of Fontainebleau sand at $D_r = 60\%$: **a** deformed centrifuge model (Bransby et al. [2008a\)](#page-26-3); **b** deformed numerical model; **c** vertical displacement profle at soil surface

satisfactory comparison of the centrifuge results are compared to the numerical predictions in terms of the deformed model, the vertical displacement profle of ground surface, and the rotation of foundation. The numerical model was able to simulate the diversion of fault rupture towards the footwall for a foundation resting on a hanging wall as similar to the centrifuge experiment results. The vertical displacement profle at the ground surface and the foundation rotation were similar. It appears that the numerical model can appropriately simulate the fault rupture-foundation interaction.

4 Results and discussion

The interaction between the normal fault rupture and shallow embedded foundation was investigated. Initially, the free-feld model determined the position where the fault rupture would have outcropped in the absence of a shallow embedded foundation. Then, the foundation was placed at various distances relative to the location of the free-feld fault rupture outcrop and at diferent depths. In the normal fault rupture-shallow embedded foundation interaction, the location of the foundation, its embedment depth and surcharge, as well as the fault dip angle could have afected the behavior of the foundation. Therefore, a parametric study was conducted to derive an understanding of the normal fault rupture-shallow embedded foundation interaction. In the following sections, the results of the parametric analysis are presented and discussed.

Fig. 3 Foundation-normal fault rupture interaction mechanism for $B = 10$ m, $q = 37$ kPa, $S = 3.1$ m, and *h*=2.03 m: **a** deformed centrifuge model (Bransby et al. [2008a](#page-26-3)); **b** deformed numerical model; **c** vertical displacement profle at ground surface; **d** rotation of foundation

4.1 Free‑feld condition

The free feld models for dense and loose sand were analyzed for an alluvium depth of $H=25$ m and normal faults with dip angles of 45° , 60° , 75° , and 90° . Figure [5](#page-10-0) shows the diferent vertical displacement profles at the ground surface for diferent dip angles of a normal fault propagating through the soil layer. The location of the fault trace at the ground surface difered with changes in the dip angle of the fault. The fault zone at ground level was highest for a dip angle of 45° and lowest for a dip angle of 90°.

It should be considered that, with a decrease in the dip angle of the fault, a gravity graben was created in both the dense and loose soils in the faulting zone. This has been observed in previous studies (e.g., Lade et al. [1984;](#page-26-20) Hazeghian and Soroush [2017](#page-26-21)), which shows that this type of hazard occurs for low-angle dipping of a normal fault. As seen in Fig. [5,](#page-10-0) the width of zone afected by the graben in dense sand was less than in loose sand (1.0*H* versus 1.32*H*), but had a greater depth (0.021*H* versus 0.01*H*). The loose sand attracts and deviates the fault rupture deformation because of the lower stifness and more elastic deformations compared to dense sand.

4.2 Efect of embedment depth and location of foundation

To investigate the efect of the embedment depth of a shallow foundation and its location on the normal fault rupture-foundation interaction, foundations with a width of

Fig. 4 Foundation-normal fault rupture interaction mechanism for $B = 10$ m, $q = 90$ kPa, $S = 2.9$ m, and *h*=2.16 m: **a** deformed centrifuge model (Bransby et al. [2008a](#page-26-3)); **b** deformed numerical model; **c** vertical displacement profle at ground surface; **d** rotation of foundation

10 m, embedment depths of *D/B*=0, 0.3, 0.6, 0.9, and surcharges *q*=40 and 100 kPa were modeled at $s/B = -0.5$, 0, 0.25, 0.5, 0.75, and 1.0 for a normal fault at $\alpha = 60^{\circ}$. Figure [6](#page-11-0) shows the foundation rotation relative to the foundation location in dense and loose sand. The results show that the effect of the embedment depth on the fault-foundation interaction signifcantly depended on the location of the foundation relative to the fault rupture and the foundation surcharge. This can be attributed to a change in the mechanism of the fault rupture-foundation interaction.

The interaction mechanisms were hanging wall, gapping, and footwall types (discussed by Ahmed and Bransby 2009), which vary with a change in the embedment depth and the location of the foundation. As seen, for $s/B < 0.5$ at $q = 40$ and 100 kPa, an increase in the embedment depth increased the foundation rotation in dense and loose sand. This increase in the embedment increased the likelihood of the fault rupture striking the bottom of the embedded foundation relative to the surface foundation $(D=0)$. In most cases, the interaction mechanism for embedded foundations was the gapping type.

For $s/B \ge 0.5$ in $q = 40$ kPa and $s/B \ge 0.75$ in $q = 100$ kPa, the rotation of the surface foundation was greater than for the shallow embedded foundation, which could relate to the interaction mechanism of the foundations. When the foundation moved towards the hanging wall, the interaction mechanism of the surface foundation was gapping. The mechanism for the shallow embedded foundation gradually changed to a footwall, the fault rupture was diverted to the right side of the embedded foundation, and the foundation rotation decreased.

Fig. 5 Vertical displacement profle at ground surface for normal free-feld fault rupture with dip angles of 45°, 60°, 75°, 90°: **a** dense sand; **b** loose sand

A comparison of the foundation rotation caused by the embedment depth under nor-mal faulting (i.e., this study) and reverse faulting (Ashtiani et al. [2015](#page-26-5); Naeij et al. [2019](#page-27-12)) showed that embedment depth of the foundation changed the mechanism of the fault rupture-foundation interaction. At the same value of *h/H*, the embedded foundation experienced either less or greater rotation than the surface foundation under both normal and reverse faulting, depending on the fault rupture-foundation interaction mechanism.

Figures [7](#page-12-0) and [8](#page-13-0) summarize the efect of the embedment depth of the foundation and its position relative to the fault rupture outcrop on contact pressure *p* and bending moment *M* of foundation base in dense and loose sand, respectively. Contact pressure *p* was

Fig. 6 Rotation of foundation in terms of position vs. embedment depth: **a** dense sand; **b** loose sand

normalized with foundation surcharge *q* and *M* with *qB*² . Only the response of foundations with $q=100$ kPa subjected to normal faulting for $\alpha=60^{\circ}$ and $h/H=5%$ were investigated due to space limitation. For $s/B = 0$ (Fig. [7](#page-12-0)a), the rupture diverted toward the footwall (left edge) of the foundations. Despite diversion of the fault rupture, the embedded foundations experienced significant stressing. Initially, at $D/B = 0$ and 0.3, the foundations remained in almost full contact with the soil. The foundation surcharge *q* and fault-induced deformation bent the foundations downwards (sagging deformation). After increasing the embedment depth of the foundation to $D/B = 0.6$ and 0.9, these foundations lost the contact at their centers. This caused an increase in the bending moment of the foundation. In general, as the embedment depth increased, foundation surcharge *q* and faulting-induced deformation cause sagging deformation.

At $s/B = 0.5$, the plastic deformation diffused beneath the foundation. Figure [7](#page-12-0)b shows that the contact pressure profle of the surface foundation altered near its middle in comparison with the foundation at $s/B = 0$. The embedded foundations then detached from the soil near their ends and the value of p increased significantly near the middle. This means that an embedded foundation tended to behave as a cantilever beam at the two ends. The faulting-induced deformation caused downward bending of surface foundations (sagging deformation) and reversal of the stressing at the left edge of the embedded foundation with a decrease in the maximum bending moment compared to the foundation at $s/B = 0$. As the fault rupture diverted toward the hanging wall side of the foundation $(s/B = 1.0)$, as shown in Fig. [7c](#page-12-0), the static contact pressure distribution is remained fairly constant at $D/B = 0$ and 0.3 and *M* approximately took the form of sagging-type deformation. An increase in the embedment depth to $D/B = 0.6$ and 0.9, caused the contact pressure p to increase slightly and the foundation detached from the soil at both edges. As a result, this mechanism caused

Fig. 7 The efect of embedment depth of foundation and its position on the contact pressure distribution and bending moment of foundation supported on dense sand; for foundation with $q=100$ kPa subjected to a normal fault at $\alpha = 60^\circ$ and $h/H = 5\%$. **a** s/B = 0, **b** s/B = 0.5, **c** s/B = 1.0

complete reversal of stressing (hogging instead of sagging deformation). It should be noted that, while the interaction mechanism, contact pressure, and bending moment of the foundation changed as the fault rupture diverted toward the right edge (hanging wall side) of the foundation, the maximum bending moment decreased.

To illustrate the efect of soil stifness, Fig. [8](#page-13-0) shows the response of shallow foundations supported on loose sand. Figures [7](#page-12-0) and [8](#page-13-0) reveal differences between the two soil types in the p/q and M/qB^2 profiles. For example, for embedded foundations at $s/B=0$ on dense sand, the foundations experienced loss of contact in the middle and, on loose sand, contact was maintained along the entire width. As a result, faulting-induced stressing decreased with an increase in the soil compliance. Similar results have been reported by Anastasopoulos et al. ([2009\)](#page-26-11). Figure [6](#page-11-0)a and b show that the surface foundations located on dense sand experienced greater rotation than those located on loose sand. This could be attributed

Fig. 8 The efect of embedment depth of foundation and its position on the contact pressure distribution and bending moment of foundation supported on loose sand; for foundation with $q = 100$ kPa subjected to a normal fault at $\alpha = 60^\circ$ and $h/H = 5\%$. **a** s/B = 0, **b** s/B = 0.5, **c** s/B = 1.0

to the ability of the loose soil to absorb fault-induced displacement and difuse the rupture as it approached the foundation.

The normal fault rupture-foundation interaction mechanisms for dense and loose sand presented in Fig. [9](#page-14-0) to facilitate understanding of the behavior of a foundation subjected to normal faulting. The corresponding mechanisms for an increase in the foundation embedment depth and a change in location are presented in this fgure. The diferent mechanisms when occur for the soil and foundation embedment depth and positions investigated in the numerical models are described as follows:

1. Region $s/B < 0.25$: The hanging wall interaction mechanism was related to the surface foundation and the foundation experienced relatively low rotation. A gapping mechanism also occurred with an increase in the foundation embedment depth in addition

(a)

to the occurrence of a hanging wall mechanism. This caused the shallow embedded foundation to experience greater rotation than the surface foundation.

- 2. Region 0.25≤*s/B*≤0.75: The interaction mechanism was most closely of the gapping type. In this area, an increase in the foundation embedment depth increased the foundation rotation. This could be attributed both to the interaction mechanism and to the kinematic constraints from the sidewalls of the shallow embedded foundation. Because the shallow embedded foundation was located in the faulting zone, embedment of the foundation caused the structure to experience fault-induced deformation. A decrease in the surcharge load changed the interaction mechanism of the shallow embedded foundation to a hanging wall type, which fnally resulted in a relative decrease in the foundation rotation.
- 3. Region $s/B > 0.75$: An increase in the foundation embedment depth diverted the fault rupture towards the hanging wall and caused the foundation to remain on the footwall.

Because the foundation was a considerable distance from the faulting zone, the foundation behavior was similar to that of a caisson foundation and experienced little rotation. A gapping mechanism formed for the surface foundation in addition to a footwall mechanism and the foundation experienced greater rotation.

4.3 Efect of surcharge on foundation

To determine the efect of the foundation surcharge on the interaction of a normal fault rupture and a shallow embedded foundation, the responses of foundations resting on dense and loose sand with a width of 10 m and embedment depths of $D/B = 0$, 0.3, 0.6, 0.9 at $s/B = 0.25$, 0.75 were subjected to a normal fault with a dip angle of 60 $^{\circ}$. The foundation rotations at surcharges of $q=40, 60, 80, 100, 120$ kPa are shown in Fig. [10.](#page-15-0) The results indicated that the efect of the foundation surcharge depended on the location of the foundation relative to the fault rupture. At $s/B = 0.25$, the rotation of the foundation decreased in both dense and loose soil with an increase in the value of *q*. At $s/B = 0.75$, the foundation rotation increased with an increase in the surcharge of the foundation. Generally, an increase in the foundation surcharge did not always cause a decrease in the foundation rotation, but depended on the fault rupture-foundation interaction mechanism.

Figure [11](#page-16-0) shows the interaction mechanisms (i.e., plastic shear strain contours) for foundations at an embedment depth of $D/B = 0.6$ at $s/B = 0.25$ and 0.75. For the foundation at $s/B = 0.25$, the dominant mechanism was a hanging wall at a high surcharge, while both the hanging wall and gapping mechanisms depended on the foundation embedment depth and

Fig. 10 Efect of foundation surcharge on rotation of foundation by embedment depth: **a** dense sand; **b** loose sand

Fig. 11 Model deformation from fault-foundation interaction by foundation surcharge at *D/B*=0.6 and $\alpha = 60^\circ$: **a** $s/B = 0.25$; **b** $s/B = 0.75$

its surcharge at a low surcharge value (Fig. [11](#page-16-0)a). The footwall mechanism occurred for the foundation at $s/B = 0.75$ (see Fig. [11](#page-16-0)b). When the interaction mechanism was in the form of a hanging wall, an increase in the foundation weight decreased the foundation rotation and had a positive efect on reducing the building damage level. In this case, the foundation was placed in a faulting zone and tended to rotate, but an increase in the surcharge caused the foundation to return to its initial position. When the interaction mechanism was of the footwall type, an increase in the surcharge could cause an increase in the foundation rotation.

4.4 Efect of fault dip angle

The efect of the fault dip angle on the interaction of a normal fault rupture and shallow embedded foundation were analyzed for rigid foundations at $B=10$ m, surcharge $q = 100$ kPa, and $D/B = 0$, 0.3, 0.6 at $s/B = 0.5$ for both dense and loose sands.

4.4.1 Vertical displacement profle at ground surface

The vertical displacement profles at the ground surface, as a hazard caused by a normal fault rupture at dip angles of $\alpha = 45^{\circ}$, 60°, and 90° and a fault throw of $h/H = 5\%$ for dense and loose sand, are shown in Fig. [12.](#page-18-0) The existence of a graben is a hazard associated with normal faulting that forms between the main fault rupture and a secondary rupture. As the fault dip angle increases, the width and depth of the graben will decrease because of the to the declining formation of secondary ruptures in a high-angle dipping normal fault. For a normal $α=45°$ fault with a foundation having an embedment depth of $D/B=0.6$, a graben was created in both dense and loose sand at widths of 1.12 and 1.3 *H* and depths of 0.02 and 0.008 *H*, respectively.

With an increase in the fault dip angle to 60° , a graben developed in dense sand, but not in loose sand. With increases in the fault dip angle to 75° and 90°, no graben developed in any model. Based on the model proposed by Cole and Lade ([1984\)](#page-26-15), at a dilation of $\alpha \leq 45 + \psi/2$ of the soil under normal faulting, a secondary rupture developed in addition to the main rupture that resulted in the formation of a gravity block (graben) between the rupture surfaces. Hazeghian and Soroush [\(2017](#page-26-21)) reported that a graben developed for a normal fault at α = 60° in dense soil. The characteristics of the numerical models were not satisfied using the Cole and Lade ([1984\)](#page-26-15) model.

Similarly to the free-feld condition, the depth of the graben in dense sand was much greater than in loose sand. This indicates that loose sand was capable of absorbing and dissipating fault-induced dislocation at the ground surface. The width of the graben in loose sand was somewhat greater than in dense sand. This indicates that the fault rupture propagated through the loose sand and difused in the border zone around the foundation.

4.4.2 Active and passive failure zones

Other consequences of a normal fault rupture-shallow embedded foundation interaction include active and passive failure zones on the footwall and hanging wall sides of the foundation, respectively (left and right sides of the foundation, respectively). These ruptures resulted from the rotation and translational displacement of the foundation during the interaction with a normal fault rupture. Figure [12](#page-18-0) shows that a rupture zone of the active type was created on the left side of the foundation for all dip angles with widths of 0.28 and 0.3 *H* in dense and loose sand, respectively.

Figures [13](#page-19-0) and [14](#page-20-0) show the plastic shear strain contours for the interaction of foundations with embedment depths of $D/B = 0.3$ and 0.6 for normal faults having different dip angles. A graben is visible for the low-angle dipping fault and the greater the fault dip angle, the lower the probability of the formation of a secondary rupture and graben. Active ruptures fully mobilized in front of the left sidewall of the foundation, but a passive rupture plane did not fully form on the right side (i.e., hanging wall). This could be attributed to the degree of rotation and translation of the foundation sidewalls that mobilized the active and passive failure zones.

4.4.3 Rotation of foundation

The rotation of the embedded foundation resting on dense and loose sand at diferent dip angles for a normal fault rupture is shown in Fig. [15](#page-21-0). As shown, an increase in the

Fig. 12 Surface deformation due to fault-foundation interaction at diferent fault dip angles and embedment depths at $s/B = 0.5$ and $q = 100$ kPa: **a** dense sand; **b** loose sand

fault dip angle decreased the foundation rotation, especially for surface foundations. An increase in the foundation embedment depth increased the efect of larger dip angles and increased the foundation rotation relative to surface foundations.

zone A: Active failure zone

zone GP: Graben and passive failure zone zone P: Passive failure zone

The range of foundation positions at which the gapping mechanism occurred for embedded foundations was greater than for the surface foundations. This increased the probability of distress of a shallow embedded foundation, but it should be noted that this range was not valid at all fault dip angles, especially at $\alpha = 90^\circ$. For example, the rotation of the surface foundation at $\alpha = 90^{\circ}$ normal faulting was almost negligible for all positions and it was clear that the foundation-fault rupture interaction mechanism was not of the gapping type. An increase in the embedment depth increased the probability that the fault rupture would strike the foundation base and cause a large rotation of the foundation. At *s/B*>0.75 in dense sand, Fig. [15](#page-21-0)a showed that the degree of foundation rotation at diferent embedment depths was negligible and the interaction mechanism was of the footwall type.

zone A: Active failure zone

zone GP: Graben and passive failure zone zone P: Passive failure zone

Fig. 14 Model deformed by fault-foundation interaction vs. fault dip angle at $D/B = 0.6$, $s/B = 0.5$, *q*=100 kPa: **a** dense sand; **b** loose sand

4.4.4 Lateral earth pressure distribution

The design of the basement walls was based on lateral earth pressure theories for at-rest and/or active conditions. The wall deformations and relative displacement between the wall and soil were determined and the lateral earth pressure distribution on the wall was calculated. However, during faulting, the fault-induced displacement of the soil and the wall appeared to be very large and the earth pressure distribution on the basement walls difered. To examine the lateral earth pressure distribution on the basement walls during its interaction with a normal fault rupture, the pressure distribution at the left and right sidewalls of the foundation at an embedment depth of $D/B = 0.6$, a surcharge of

Fig. 15 Rotation of foundation vs. fault dip angle and embedment depth at $q = 100$ kPa: **a** dense sand; **b** loose sand

 $q=100$ kPa, and at $s/B=0.25$, 0.5, and 0.75 for dense and loose soil are presented in Figs. [16](#page-22-0) and [17](#page-23-0).

The analysis was carried out for normal fault dip angles of $\alpha = 45^{\circ}$, 60°, 75°, and 90° and a fault throw of $h/H = 5\%$. For the normal fault rupture-foundation interaction, it was clear that the condition of the left sidewall was active and the right sidewall was passive; therefore, the lateral earth pressure distribution on both sides of the wall was expected to adhere to these conditions. The lateral earth pressure distribution on the left sidewall shown in Figs. [16](#page-22-0)a and [17a](#page-23-0) was distributed in an approximate triangular pattern and the active earth pressure was zero in the upper parts of the wall due to the loss of contact between the soil and wall. The pressure values applied to the wall were less than the Rankine active earth pressure. This could be attributed to large displacement of the soil and a decrease in the height of a backfll subjected to the normal faulting and the post-peak state of the soil. At some fault dip angles, the pressure either increased or decreased at specific positions. In particular, at a dip angle of 45° , at $s/B = 0.25$, these

Fig. 16 Earth pressure acting on foundation walls vs. fault dip angle at *D/B*=0.6, *q*=100 kPa and dense sand: **a** left sidewall of foundation; **b** right sidewall of foundation

fuctuations were intense and were greater than the active earth pressure at some positions. In general, it would be conservative to assume an active or at-rest earth pressure for the design of the footwall sidewall of an embedded foundation.

The lateral earth pressure distribution on the right sidewall of the embedded foundation in Figs. [16](#page-22-0)b and [17](#page-23-0)b demonstrate that the applied pressure distribution was non-

Fig. 17 Earth pressure acting on foundation walls vs. fault dip angle at $D/B = 0.6$, $q = 100$ kPa in loose sand: **a** left sidewall of foundation; **b** right sidewall of foundation

Rankine theory. The pressure on the wall also was greater than the Rankine passive earth pressure for the upper parts of the wall and lower at depths near the toe wall.

The passive earth pressure distribution for the right sidewall of the shallow embedded foundation creates fundamental doubts. The schematic deformation of the shallow embedded foundation during its interaction with normal faults with diferent dip angles is shown

Fig. 18 Type of foundation rotation: **a** pattern of foundation rotation during normal fault interaction $(s/B = 0.5, q = 100 \text{ kPa}, D/B = 0.6, \text{ dense sand}), \mathbf{b}$ expected wall stress distribution for wall rotation about its toe in dense sand (James and Bransby [1971\)](#page-26-22)

translational displacement and rotation about the toes of the sidewalls. The pressure distribution on the wall that had rotated about its toe, as for James and Bransby ([1971\)](#page-26-22), was similar to the distribution shown in Fig. [18](#page-24-0)b. Comparison of this distribution with those obtained from numerical modeling indicated that the passive earth pressure distribution on the right sidewall was nonlinear and depended on the extent of the foundation wall rotation about its toe. In addition, the magnitude of foundation rotation was dependent on factors such as the fault dip angle, foundation embedment depth and its position, and the magnitude of applied surcharges. Thus, the change in the rotation of the foundation wall indicates that the state of the soil may have occurred for pre-peak, peak, and post-peak (i.e., residual) behavior, which would lead to a nonlinear pressure distribution on the wall.

5 Conclusion

The present study used numerical modeling to investigate the efects of the foundation embedment depth, foundation position relative to the fault rupture outcrop, foundation surcharge, and fault dip angle on the interaction between a normal fault rupture and a shallow embedded foundation. The numerical models were validated using the results of centrifuge experiments. The results obtained from numerical analyses are as follows:

- 1. In the free-feld case, a graben was observed to be a hazard of surface faulting. This type of hazard developed in both loose and dense sandy soil, especially at low dip angles (45° and 60° for dense soil; 45° for loose soil). Also, a change in the dip angle of the fault caused the faulting zone to vary at the ground surface. The width of the faulting zone was less in dense soil compared to loose soil, but its depth was greater. The results show reasonable agreement with previous research (Lade and Cole 1984; Anastasopoulos et al. [2007;](#page-26-9) Bransby et al. [2008b;](#page-26-4) Hazeghian and Soroush [2017](#page-26-21)).
- 2. The interaction between the shallow embedded foundation and a normal fault rupture was dependent on the efects of the foundation position, its embedment depth, and the surcharge applied to it. The diferent behavior of the foundations could be attributed to the type of interaction mechanism between the foundation and normal fault rupture and the kinematic constraints of the embedded foundation walls. In general, for the hanging wall and gapping interaction mechanisms, the shallow embedded foundation experienced more rotation than the surface foundation because the foundation walls acted as kinematic constraints and forced the foundation to follow the faulting-induced deformation. For the footwall interaction mechanism, the rotation was similar for all foundations and the shallow embedded foundation experienced relatively less rotation. It should be noted that the foundations located on loose soil experienced less rotation than those on dense soil, as the loose soil was able to absorb or divert the fault rupture.
- 3. Depending on the embedment depth of the foundation and its position relative to the fault rupture outcrop, detachment of the foundation base from the soil could take place either at its middle or at its two ends. This caused a change in the relative stressing of the embedded foundations compared to the surface foundations. Also, despite diversion of the fault rupture in the interaction between an embedded foundation and normal faulting, the embedded foundation experienced substantial distress.
- 4. An increase in the foundation surcharge did not always result in a decrease in the foundation rotation. The rotation increased or decreased depending on the foundation location relative to the fault rupture outcrop, as well as the type of interaction mechanism between the fault rupture and foundation. Generally, if the interaction mechanism was of the hanging wall type, the surcharge was greater and the foundation rotation was less. In contrast, if the interaction mechanism was of the footwall type, the surcharge was greater, but the foundation rotation was larger.
- 5. Graben was hazards observed with rupture propagation in the interaction of a normal fault rupture and a shallow embedded foundation. At low dip angles, a graben was observed for both dense and loose soil because of the formation of a secondary rupture in addition to the main fault rupture. Also, active and passive ruptures were observed in the front of sidewalls of the shallow embedded foundation and were the result of the rotation and displacement of the foundation when subjected to normal faulting. These hazards have destructive efects on adjacent structures. In general, the region afected by graben was larger for loose soil than for dense soil, but the depth of graben at the ground surface and the active rupture in the front of sidewall were less in loose soil than in dense soil.
- 6. It should be noted that the diferences in the rotation of a foundation subjected to a normal fault rupture at diferent dip angles were dependent on the foundation position relative to the fault rupture outcrop, its embedment depth, and the type of soil.
- 7. The triangular pressure distribution in accordance with Rankine theory can be used to design a good approximation of a left sidewall of embedded foundation (footwall side). However, the pressure distribution on the right sidewall of the embedded foundation (hanging wall side) was not similar to the triangular pressure distribution of the Rankine

theory. It had a parabolic distribution that related to the magnitude of foundation rotation and the state of the soil (peak or residual); thus, the patterns proposed by James and Bransby [\(1971](#page-26-22)) could be applied.

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