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Structural seismic damage and loss assessments using a multi‑conditioning ground motion selection approach based on an efficient sampling technique

Abdoul R. Ghotbi[1](http://orcid.org/0000-0001-9344-3502) · Ertugrul Taciroglu1

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Abstract

The application of Latin Hypercube and Monte Carlo (*MC*) sampling techniques for ground motion selection purposes is investigated. Latin Hypercube Sampling (*LHS*) works by frst stratifying a probability distribution domain into multiple equally spaced and nonoverlapping stripes and then by permutationally drawing samples from those stripes. To examine the efficiency of these two distinct sampling methods, a set of conditional multivariate distributions was ft to an intensity measure vector based on a single, two, or average of more-than-two (average) conditioning intensity measure. *LHS* was then utilized for sampling purposes from the conditional multivariate distributions, which in turn demonstrated superiority over *MC* given the same number of realization samples. Accordingly, it was utilized as an underlying peace of a broader ground motion selection framework to facilitite the selection of a number of ground motion suites based on diferent methods of conditioning. Using the selected suites, response history and subsequent damage/ loss analyses were conducted on a generic 4-story non-ductile reinforced concrete building. The outcomes of these latter studies demonstrated that the ground motion suite selected based on an average-intensity-measure conditioning criterion performed better than those selected through single- and two-intensity-measure conditioning criteria.

Keywords $LHS \cdot MC \cdot$ Conditioning criteria \cdot Damage analyses \cdot Loss assessments

1 Introduction

The generalized conditional intensity measure (*GCIM*) methodology originally developed by Bradley ([2011\)](#page-14-0) is arguably the most comprehensive method for ground motion selection. As such, ground motion suites selected using this method are known to meet the *sufficiency* and *efficiency* criteria with respect to capturing the true seismic behavior of structures across multiple modes of vibration. In this method, it is common to frst put together an intensity measure vector consisting of several intensity measures $(IM'_i s)$ and that is to

 \boxtimes Abdoul R. Ghotbi civil_ghotbi40@yahoo.com

¹ University of California, 5731E Boelter Hall, Los Angeles, CA 90025, USA

capture various characteristics of an earthquake during the record selection phase. Hence, each intensity measure in that vector represents a specifc content of an earthquake ground motion record. For instance, spectral acceleration at a given period *(SAT)* represents the amplitude and frequency content at that period, Arias Intensity (*AI*) or Cumulative Absolute Velocity (*CAV*) each represents the cumulative content, and Signifcant Duration (*Ds*575 or *Ds*595) represents the duration content. In *GCIM*, a multivariate distribution is fit to the IM_i vector. Subsequently, any number of target realization samples associated with each IM_i in the vector are drawn. Finally, a ground motion record database is searched to find matching records whose IM_i 's are identical to those of the target realization samples, and that is to fully enforce hazad consistency.

One of the primary issues in the *GCIM* approach is the utilization of a reliable sampling technique for drawing an adequate number of samples from a conditional multivariate distribution of various intensity measures. To this end, this work is organized to (1) devise two diferent sampling methods, namely the Latin Hypercube Sampling (*LHS*) and Monte Carlo (*MC*) for the purpose of drawing realization samples from a target conditional multivariate distribution of various IM_i^{\prime} , (2) compare the performance of each of these methods in a real ground motion selection exercise based on single, two and average of more-than-two (average) conditioning intensity measure criteria developed by Ghotbi and Taciroglu ([2020a](#page-15-0)), (3) utilize the selected ground motion suites to perform a series of damage/loss assessments on a generic 4-story moment frame non-ductile reinforced concrete building to examine the diferences in estimated damage and losses due to use of diferent methods of conditioning.

1.1 Background

The application of Latin Hypercube and Monte Carlo sampling techniques is explored herein for drawing realization samples from a conditional multivariate distribution of various *IM'_i*'s. Despite a broader use of *MC* in the field of ground motion selection (Bradley [2010,](#page-14-1) [2012;](#page-15-1) Tarbali and Bradley [2015,](#page-15-2) [2016;](#page-15-3) Tarbali et al. [2018\)](#page-15-4), *LHS* applications are scarce. As such, in this section it is aimed to review some of the prior works in which the applications of both of these methods are demonstrated.

Vorechovsky and Novák [\(2009](#page-16-0)) combined *MC* and *LHS* in order to draw a smaller number of samples from a multivariate distribution of various variables. The samples were drawn such that the empirical distributions of them closely match the theoretical target distributions aiming at preserving the correlation structure among all variables with respect to the theoretical covariance matrix. Dolsek [\(2009](#page-15-5)) utilized *LHS* to draw realization samples from the *PDF* of various structural modeling parameters to consider the epistemic variability in those parameters besides the variability in ground motions to perform a set of incremental dynamic analyses. Chouna and Elnashai ([2010\)](#page-15-6) utilized a simplifed method based on modifying the quantile arithmetic methodology and compared it with *MC*, in order to consider the epistemic variability associated with diferent parameters involved in seismic loss assessment of structures. Zhongxian et al. [\(2014](#page-16-1)) studied the efects of variability in ground motions and some of the structural modeling parameters on the probabilistic seismic responses of bridges. They used *LHS* to consider the efects of uncertainity in structural modeling parameters. Decò and Frangopol [\(2013](#page-15-7)) used *LHS* to generate random earthquakes for the purpose of life-cycle risk assessment of bridges. Celarec and Dolšek [\(2013](#page-15-8)) studied the effects of variability in structural modeling parameters on the

probabilistic seismic risk of reinforced concrete (*RC*) structures by using the frst-ordersecond-moment (*FOSM*) reliability method combined with *LHS.*

Decò et al. ([2013\)](#page-15-9) utilized *MC* and *LHS* to consider the efects of uncertainty associated with the expected damage, restoration process, and rehabilitation costs in resilience-based seismic assessment of bridges. Kosič et al. [\(2014](#page-15-10)) studied the probabilistic response of *RC* structures using a single-degree-of-freedom (*SDOF*) structural system instead of modeling the entire structure. They used *LHS* to consider the effects of structural modeling parameters and used a suite of ground motion records in order to incorporate the efects of recordto-record variability in ground motions. Vamvatsikos and Fragiadakis ([2010\)](#page-16-2) performed an incremental dynamic analysis (*IDA*) on a 9-story moment frame steel structure considering the efects of epistemic variability in structural modeling parameters and the variability in ground motion earthquake records. They used diferent methods such as *MC* mixed with *LHS* as well as the *FOSM* method to consider the efects of the aforementioned variability.

Bucher [\(2009](#page-15-11)) used *MC* mixed with *LHS* for the purpose of optimization and design of seismic isolation devices to be incorporated into various structural systems. Pan et al. ([2007\)](#page-15-12) utilized *LHS* and a restricted pinning approach with respect to considering the uncertainty in various modeling parameters of the steel bridges. They also considered the simultaneous efects of variability in ground motion earthquake records and studied the corresponding impacts of both sources of uncertainty on the seismic demand fragilities for various components of the bridges. Tubaldi et al. ([2012\)](#page-15-13) utilized *MC* mixed with *LHS* for the purpose of uncertainty propagation into the structural models in order to perform seismic damage assessment on multi-span continuous bridges with dissipative piers and a steel–concrete composite deck. Finally, Vamvatsikos [\(2014a](#page-16-3),[b\)](#page-16-4) adopted *MC* mixed with *LHS* to incorporate the efects of uncertainty in structural modeling parameters on the *IDA*, which was used to assess the seismic responses of various structures given multiple damage limit states.

As demonstrated with the review provided herein, the application of *LHS* in the feld of ground motion selection with the main objective of generating hazard-consistent target realizations sampled from a theoretical multivariate distribution, namely the *GCIM*, is quite scarce. As such, the present study aims at utilizing *LHS* to select a number of ground motion suites based on diferent methods of conditioning. It is also aimed to utilize these suites to perform a number of seismic damage/loss assessments on a generic 4-story moment frame non-ductile reinforced concrete building to explore the distinct efects due to diferent methods of conditioning. The underlying framework to develop *GCIM*-based target distributions using a variety of conditioning approaches is addressed in Ghotbi ([2018\)](#page-15-14) and Ghotbi and Taciroglu [\(2020a](#page-15-0)), and the datails of the *GCIM*-based approach are omitted here for brevity.

2 Monte Carlo sampling technique

Here it is aimed to develop an approach in which the *MC* sampling technique is utilized to draw realization samples from a conditional multivariate distribution fitting to an IM_i vector, given the methodologies developed in Ghotbi and Taciroglu [\(2020a](#page-15-0)). To this end and following Bradley [\(2012](#page-15-1)), a two-level approach will be adopted here to draw realization samples of each IM_i from the conditional multivariate distributions of various $IM_i's$, which was defned in Ghotbi and Taciroglu [\(2020a](#page-15-0)) based on single-, two-, and *Avg*−*IMj* (average of more-than-two *IMj* 's) conditioning criteria. This is carried out frst by obtaining a random rupture probability (Rup^{nsim}) from a disaggregation density function. Then, to draw samples from a multivariate distribution, an uncorrelated standard normal random vector is defined (u^{nsim}) whose elements are drawn from a standard normal distribution, independently. Using this vector, a correlated vector can be defned as

$$
v^{nsim} = Lu^{nsim} \tag{1}
$$

where *L* is the Cholesky decomposition of the correlation matrix, which is

$$
\rho_{lnIM|IM_{j,Rup}} = LL^T. \tag{2}
$$

Using this, the realization sample for each IM_i can be obtained via

$$
\ln M_i^{nsim} = \mu_{ln M_i|Rup, M_j} + \sigma_{ln M_i|Rup, M_j} v_i^{nsim}
$$
\n(3)

where $v_i^{nsim} = v^{nsim}(i)$ is the *i*-th element in the v^{nsim} vector, and $Rup = Rup^{nsim}$.

3 Latin hypercube sampling technique

The Latin hypercube sampling (*LHS*) can be applied through a stratifed sampling approach (see Fig. [1](#page-3-0)). In order to draw realization samples from the distribution of an IM_i , its domain is stratifed into *N* equally spaced and non-overlapping intervals. Next, samples are randomly drawn from each interval. By utilizing a random permutation approach, a set of random *LHS* samples can be obtained. The overall method to draw samples from a theoretical multivariate distribution of multiple IM_i 's can thus be carried out through the following steps:

- 1. Sample from the actual marginal distribution of each IM_i using LHS (Zhang and Pinder [2003\)](#page-16-5).
- 2. Derive the correlation matrix of the sampled realizations of various $IM_i's$.

- 3. Obtain the Cholesky decomposition of a Hermitian positive-defnite matrix (*L*) of the correlation coefficient matrix (see Eq. [2\)](#page-3-1). If *L* is not positive-definite, then a method to fnd the nearest *PD* matrix can be used (see, e.g., Higham [2002](#page-15-15)).
- 4. Add dependency between the independent samples, drawn using *LHS*, by transforming their governing normal distribution into a uniform distribution (this transformation preserves the dependency between the variables).
- 5. Map each of the IM_i 's uniform distribution onto the corresponding probability distribution of each, defned by a *GMPE*.
- 6. Obtain the correlation structure among the new realization samples in order to compare it with the original correlation structure of the theoretical multivariate distribution to ensure that they are identical. To enforce this, a stochastic optimization using the simulated annealing (Dolsek [2009](#page-15-5)) is incorporated in order to preserve the correlation structure among the realization samples.

4 Applications

Applications of the methodologies described in the preceding sections are presented here. First, a vector of IM_i 's needs to be populated. As suggested by Bradley [\(2012](#page-15-1)), various intensity measures—such as spectral acceleration at multiple periods (*SAT*), Arias Intensity (*AI*), Cumulative Absolute Velocity (*CAV*), 5–75% signifcant duration (*Ds575*) and 5–95% significant duration ($Ds595$)—will be picked to populate the IM_i vector. For *SAT*, 21 different periods, identical to those for which the hazard curves are available, have been adopted. The *GMPEs* to be used to defne the moments (i.e., the median and standard deviation) of the distribution of each IM_i in the IM_i vector are adopted from Boore and Atkinson [\(2008](#page-14-2)) for *SAT*, *PGA*, and *PGV*, from Campbell and Bozorgnia [\(2012](#page-15-16)) for *AI*, from Campbell and Bozorgnia [\(2010](#page-15-17)) for *CAV*, and from Bommer et al. ([2009\)](#page-14-3) for *Ds575*, and *Ds595*. For generating the multivariate distributions of IM_i 's in the IM_i vector, a matrix containing the cross-correlations between the IM'_i s should be defined in addition to the median and standard deviation of each IM*ⁱ* (for details, see Table 1 in Bradley [2012,](#page-15-1) and Table 2 in Tarbali and Bradley [2015](#page-15-2)).

Based on Ghotbi [\(2018](#page-15-14)), three diferent algorithms are utilized to generate hazardconsistent target *IM*′ *i s* based on a multi-conditioning (single-, two-, or *Avg*−*IMj*) approach leading to three distinct multivariate distributions of the adopted *IM*_{*i*} vector. The *MC* and *LHS* will then be employed to draw 30 realization samples from the marginal distribution of each IM_i . To this end, Fig. [2](#page-5-0) displays the realization samples (blue curves) for the response spectrum (*SAT*) conditioned on a set of diferent *IM*′ *j s*. It is also useful to add that L *HS* was utilized to draw samples from the theoretical distribution of the IM_i vector whose median (see the red solid curves) and $16th/84th$ percentiles (see the red dashed curves) are also shown in the sub-fgures.

Figure [3](#page-6-0) shows the comparison between the *SAT* (Fig. [3a](#page-6-0)) obtained using *MC* (shown in blue) and *LHS* (shown in black) based on a single conditioning approach. Figure [3](#page-6-0)b–d display the empirical distributions of *CAV*, *AI* and *Ds*595, respectively, which were obtained using *MC* (shown in blue) and *LHS* (shown in black), again for a single conditioning (single-*IMj*) intensity measure. As noticed from all the graphs, *LHS* performance is slightly better than *MC* given the same number of samples, which can be noticed from the extent to which the statistics (Fig. [3a](#page-6-0)) or the distributions (Fig. [3b](#page-6-0)–d) of the realization samples match those of the *GCIM* targets (shown in red). Of course,

Fig. 2 Theoretical distribution (red solid and dashed curves) as well as realization samples (blue curves) of *SAT* based on **a** single-; **b** two-; and **c** *Avg*−*IMj* criteria

the *MC* performance can be improved by increasing the number of samples or repeating the sampling process for a number of times to get better results, but clearly at a higher computational cost.

Figure [4](#page-7-0) is a repeat of Fig. [3,](#page-6-0) however given a two- IM_j conditioning approach for *SAT*, *CAV*, *Ds*575 and *Ds*595 as the adopted target *IM*[']_i's. It is clear, once again, that the *LHS* performance is more desirable compared to the *MC*.

The same set of comparisons are made for the case of *Avg*−*IMj* (see Fig. [5\)](#page-8-0), which affirms, once again, the superiority of *LHS* over *MC*, albeit slightly less so compared to the single- and two-*IMj* cases.

In some of the graphs showing the empirical distributions of the realization samples, it is observed that the blue curves (e.g., see Fig. [5](#page-8-0)c), obtained using *MC*, intercept the confdence bounds (dashed curves) meaning that those samples must be rejected. However, none of the cumulative distributions obtained using *LHS* (see the black curves) demonstrated such unacceptable behavior. Moreover, the main reason why *LHS* performed better in the majority of above cases can be attributed to the stratifcations strategy in *LHS*, which made it possible to draw samples from the entire distribution domain. Whereas in MC, since the samples are randomly drawn, as the number of designated

Fig. 3 Comparison between the statistics of **a** *SAT*; and the empirical distributions of **b** *CAV*; **c** *AI*; and **d** *Ds*595 obtained using *MC* and *LHS* with respect to the *GCIM* theoretical targets given a single-*IMj* conditioning approach

samples are quite low, there is no guarantee that those samples are drawn uniformly from the entire distribution domain. Again, increasing the number of samples or repeating the *MC* for a number of times should improve the outcomes, but this will result in higher computational costs.

5 Ground motion selection

In this section, ground motion records are selected to match the target realizations drawn using *LHS* through the procedure laid out in the previous section. In order to select the ground motion records, a hypothetical site in the City of Los Angeles, California (LONG−118.43; LAT−34.053) with a V_s =760 m/sec and a depth to a 2.5 km/s shearwave velocity horizon of $z_{2.5} = 1 \text{km}$ is chosen. Using the relationships developed in Ghotbi ([2018\)](#page-15-14) and Ghotbi and Taciroglu ([2020a](#page-15-0)), diferent *GM* suites are selected based on different conditioning criteria by specifcally putting major emphasis on the ground motion

Fig. 4 Comparison between the statistics of **a** *SAT*; and the empirical distributions of **b** *CAV*; **c** *Ds*575; and **d** *Ds*595 obtained using *MC* and *LHS* with respect to the *GCIM* theoretical targets given a two-*IMj* conditioning approach

spectral content—for example a 99% importance weigh is assigned to *SAT*-based content during the selection phase (see Ghotbi and Taciroglu [2020a](#page-15-0)). For the causal parameters, the magnitude range of $M = [5, 8.5]$, the closest source-to-site distance range of $R_{ib} = [0, 100]km$, and the shear wave velocity range of $V₃₀ = [600, 1200]m/sec$ corresponding to site class $B \& \text{upper-C}$, are adopted. The maximum scale factor is set to be 4.5, however an attempt was made to keep the scaling factor (on average) as close to 1.0 as possible in order to keep the original earthquake records unaltered (see, e.g., Baker [2015;](#page-14-4) Miano et al. [2018\)](#page-15-18). The hazard consistency is enforced by considering up to 2000 rupture scenarios and their relative contributions to diferent types of conditioning intensity measure.

As an example, a suite of ground motions consisting of 30 bi-directional records selected based on an *Avg*−*IMj* conditioning approach is provided here (see Fig. [6](#page-8-1)) and the rest along with the associated details are omitted for brevity, however can be found elsewhere (see Ghotbi and Taciroglu [2020a\)](#page-15-0). The PEER NGA-West2 database (Bozorgnia et al. [2014](#page-14-5)) is consulted to select the earthquake records matching the target realization samples. Once a

Fig. 5 Comparison between the statistics of **a** *SAT*; and the empirical distributions of **b** *AI*; **c** *Ds595*; and **d** *Ds*575 obtained using *MC* and *LHS* with respect to the *GCIM* theoretical targets given an *Avg*−*IMj* conditioning approach

Fig. 6 Summary of the selected records based on an *Avg*−*IMj* conditioning approach and given 99% *SAT* and 1% non-*SAT* weight factors: **a** response spectra of the selected records; and **b** cumulative probability distribution of the selected records for *AI*

record that is matching a target realization is selected, it is no longer utilized in the remainder of the selection process.

Fig. [6a](#page-8-1) shows that, given a larger weight assigned to *SAT* during the selection process, the statistics of the selected records (shown in green) match those of the target (shown in blue). However, as seen in Fig. [6](#page-8-1)b, the cumulative distribution of a non-*SAT* intensity measure (e.g., *AI*), which is shown in black, does not match the target (shown in blue). This rather signifcant mismatch can be attributed to the smaller weight, which was initially assigned to non-*SAT* intensity measures.

6 Structural seismic responses

A generic 4-story moment frame non-ductile reinforced concrete (*RC*) building is modeled and used in nonlinear response history analyses. The degree of non-ductility is defned through the ratio V_p/V_n , where V_p is the shear at probable moment strength, and V_n is the nominal shear strength per ASCE/SEI 41-06 for low ductility demand. Accordingly, V_p/V_n is set equal to 1.0. The building's fundamental period of vibration is $T1 = 1.30$ s. The structure is modeled as a two-dimensional moment frame in OpenSees (McKenna et al. [2000](#page-15-19)). More details regarding the structural properties can be found in Galanis [\(2014](#page-15-20)), and Ghotbi and Taciroglu ([2020b\)](#page-15-21).

Figure [7](#page-9-0) shows the key elements and material models that are used for simulating the non-ductile behavior (see Elwood [2004\)](#page-15-22); and Fig. [8](#page-10-0) displays the schematic of the building. More specifcally, Fig. [7a](#page-9-0) presents the backbone curve that defnes the plastic hinge (shown in purple in Fig. [8](#page-10-0)) behavior based on the work of Ibarra et al. [\(2005](#page-15-23)). Bar-slip is implicitly considered through an elastic rotational spring (Fig. [7](#page-9-0)b). While the axial-fexure interaction is incorporated, the shear-fexure interaction is neglected due to the slenderness of the structural members of this particular building. More useful information regarding the incorporation of axial-shear-fexure interaction in reinforced concrete structural elements can be found in Miano et al. ([2019\)](#page-15-24).

Details of the element properties—including the cross-sectional properties and defnitions and assigned values of plastic hinge parameters for simulating non-ductile behavior can be found in Galanis [\(2014](#page-15-20)). It is also worth noting here that, given a high computational

Fig. 7 a Backbone curve for the component model (adopted from Ibarra et al. [2005\)](#page-15-23); **b** zero-length elements assigned to plastic hinges to simulate non-ductile behavior (adopted from Galanis [2014\)](#page-15-20)

Fig. 8 Schematic of the 4-story moment frame non-ductile *RC* building used in the present study

cost associated with the nonlinear response history analyses that will be described later; a parallel computing approach was adopted (Ghotbi [2018](#page-15-14)). As such, all of the analyses were carried out on *STAMPEDE2*, which presently is the primary supercomputer of the Extreme Science and Engineering Discovery Environment (*XSEDE*).

6.1 Effects of conditioning intensity measures $\left(\textit{IM}_{j}^{\prime}\textit{s}\right)$ \mathbf{r}

The efects of ground motions selected based on diferent conditioning approaches on the structural seismic responses are presented in this section. A risk-based point-of-comparison (*POC*) approach (Kwong [2015](#page-15-25)) is adopted to develop reference demands, which are then used as the basis for comparison purposes to examine the relative efficiency of different *GM* suites selected based on various conditioning approaches. Details of this procedure are omitted here for brevity, however can be found in the study by Ghotbi and Taciroglu [\(2020b](#page-15-21)). Two engineering demand parameters (*EDPs*), namely the inter-story drift ratio (*IDR*) and the peak foor acceleration (*PFA*) are selected to be used in comparison studies.

Figure [9](#page-11-0) shows the statistics (i.e., median and percentiles) of the responses obtained from nonlinear response history analyses. On each plot, the damage thresholds associated with the immediate occupancy (*IO*), life safety (*LS*), and collapse prevention (*CP*) limit states (see FEMA 356) are also shown.

Here, the statistics of the *EDP*s obtained using the *GM* suites selected based on single-, two-, and *Avg*−*IM_j* criteria, are compared against the risk-based *POC* reference demands. In order to compensate for defciency of the single conditioning intensity measure approach to capture the structural responses associated with higher modes of vibration, three distinct *GM* suites, instead of just one, were selected for the single-*IM*_j case—namely, for

Fig. 9 Median (solid curves) and 16th and 84th percentiles (dashed curves) of **a** *IDR*(%); and **b** *PFA*(*g*); for a generic 4-story moment frame non-ductile *RC* structure

upper- (2.0*T*1) and lower-bound (0.20*T*1) conditioning periods (see Kohrangi et al. [2017](#page-15-26)) in addition to 1.0*T*1—, and maximum responses obtained by using all of these suites are plotted (shown in cyan color) in addition to the other cases.

Figure [9](#page-11-0)a,b display the *IDR* and *PFA* values. It is evident from these fgures that the *Avg*−*IMj* case (red curves) is superior, albeit a bit less so for the case of *PFA*, when the median responses are compared against the *POC* reference demands (pink curves). The single- (blue curves), and two- IM_j (black curves) and maximum of the set of three single- IM'_j s (cyan curves) have all underestimated the drift demand when compared to the *POC* demand, but performed better when it came to predicting the *PFA*. The reason for such better performance can be traced back to the higher spectral content of selected *GMs* at shorter periods. It is also worth adding that the superiority of the *Avg*−*IM_j* case with respect to capturing the drift demands is likely due to the richer spectral content across multiple modes of vibration — of earthquake records in that suite.

It is critical to note that the selected records—especially for the case of two-*IMj* in terms of spectral matching over the period range of interest—are afected by several restrictions set forth initially with respect to the casual parameters, scaling factors and the availability of the ground motion records. As such, the inherently lower likelihood of fnding records for the two-*IMj* (whose spectra are pinched at the lower- and upper-bound conditioning periods) may have afected some of the results. Nevertheless, this potential shortcoming is avoided with the *Avg*−*IMj* approach, which has smoother spectra (Ghotbi and Taciroglu [2020a](#page-15-0)).

6.2 Seismic loss analyses

In order to examine the efects of various ground motion selection strategies based on diferent methods of conditioning, a simplifed loss assessment on the 4-story moment frame non-ductile *RC* building is conducted. Figure [10](#page-12-0) shows the process of obtaining the cumulative distribution function $G(dv|dm)$ of seismic losses (e.g., repair cost, and time). This task is fully automated and available through a web-based application called the Performance Assessment Calculation Tool (*PACT*), which is based on the methodologies described in FEMA P-58. Thus, *PACT* was utilized in this study. To

Fig. 10 Probabilistic procedure for seismic loss assessments (adopted from Yang et al. [2009\)](#page-16-6)

this end, the subsequent loss assessment workfow was organized to (1) populate vectors of various engineering demand parameters (*EDPs*)- *IDR* and *PFA* here- through seismic response history analyses on the building given diferent suites of earthquake records (see Sect. [6.1\)](#page-10-1), (2) defne various Performance Groups (*PGs*) and their quantities (Yang et al. [2009;](#page-16-6) Baradaran Shoraka et al. [2013](#page-14-6)) each of which is controlled by a certain *EDP*, (3) define fragilities based on a range of damage limit states (e.g., minor, moderate and major damage) for each performance group and determine the repair cost and time associated with each damage state, (4) use *PACT* to generate the loss fragilities.

There is a variety of component fragilities available in the *PACT* library. Accordingly, relative to their applications to non-ductile reinforced concrete buildings, some of those fragilities were used here for grouping the structural components into diferent *PGs*. A certain *EDP* governs each *PG*. For instance, the non-code-conforming beams, columns and joints in each foor comprise a *PG*, which is governed by *IDR*; or wall partitions form another *PG*, which are also governed by *IDR*. Some other components, however, are governed by *PFA-* e.g., chiller, air hanging unit, etc. An example of fragilities based on diferent damage limit states for a *PG* (i.e., the beams or joints) is provided in Fig. [11.](#page-13-0)

In order to increase the accuracy of the seismic loss assessments conducted here, and since the number of *EDPs* in each *EDP* vector is bounded by the limited number of response history analyses, the statistical approach described in Yang et al. [\(2009\)](#page-16-6) is utilized to generate 200 realizations per each *EDP* vector. To keep the study brief, the collapse state was excluded from the analyses, which would trigger subsequent losses associated with the building's demolition and replacement.

Using the information provided above, a seismic loss assessment was conducted using *PACT* by utilizing three suites of ground motion records selected based on single-*IMj*, two-*IMj*, and *Avg*−*IMj* conditioning approaches. Figure [12](#page-13-1) presents the outcomes where it can be seen that, for both the repair cost (see Fig. [12a](#page-13-1)) and repair time (a.k.a., downtime) (see Fig. [12](#page-13-1)b), the ground motion suite based on the *Avg*−*IMj* conditioning approach was able to estimate the losses more accurately. The two other ground motions sets (based on single- IM_j and two- IM_j) appear to have underestimated the losses. The main reason for this can be traced back to the response history analy-ses (see Sect. [6.1](#page-10-1)), where it was concluded the *Avg*−*IM_j* suite was able to more accurately predict the responses when comparisons were made with respect to a baseline risk-based approach, namely the point-of-comparison (*POC*). As such, the diference in the responses obtained by using diferent ground motion suites can be the root cause of the diference observed in the associated seismic loss curves (see Fig. [12](#page-13-1)). To this

Fig. 11 Fragility of non-code conforming beam and joint components for minor (green curve), moderate (yellow curve) and major (red curve) damage states (Adopted from the *PACT* library)

end, the median repair costs associated with the single-*IMj*, two-*IMj*, and *Avg*−*IMj* cases are \$9.40 M, \$10.32 M and \$14.40 M, and the median repair times are 318, 340 and 454 days, respectively. This demonstrates a roughly %40+diference between the

Fig. 12 Seismic loss assessments of a generic 4-story moment frame non-ductile *RC* building using *GM* suites selected based on single-*IM_j*, two-*IM_j*, and *Avg*−*IM_j* conditioning approaches, **a** repair cost based on the total replacement cost of \$30 M; and **b** repair time based on the total replacement time of 800 days

median repair costs and times obtained using the *Avg*−*IM_j* suite compared to the rest. It is also necessary to add that the conclusions made herein are bounded by various

limitations set forth in this study (e.g., building type and modeling, ground motion characteristics, etc.) so more studies would have to be conducted for more comprehensive conclusions.

7 Concluding remarks

The performances of the Latin Hypercube versus Monte Carlo (*MC*) sampling technique were examined in a process to draw realization samples from a conditional multivariate distribution of various intensity measures based on a generalized conditional intensity measure (*GCIM*) approach. To facilitate this, three diferent methods of conditioning were employed to generate a set of conditional multivariate distributions to be ftted to an intensity measure vector consisting of several intensity measures. *LHS* has exhibited superiority over *MC* for the same number of realization samples associated with any given intensity measure in the intensity measure vector. As such, it was utilized as a baseline for sampling purposes, which was ultimately used in a subsequent ground motion selection efort. To this end, various suites of ground motion records were selected by searching a ground motion database to fnd matching records whose characteristics are identical to those of the realization samples drawn by *LHS*. The ground motion selection process was repeated for three different methods of conditioning, namely single-*IM_j*, two-*IM_j*, and *Avg*−*IM_j*. Using the selected suites, a series of nonlinear response history analyses was conducted on a generic 4-story moment frame non-ductile reinforced concrete structure.

The analyses outcomes revealed the superiority of the ground motion suite selected based on the *Avg*−*IM_j* over the single-*IM_j* and two-*IM_j*, relative to a risk-based *POC* reference demand. The three ground motion suites were also used in a subsequent loss assessment, where various performance groups and *EDP* responses were designated to compute the repair cost and time for the building. Based on that, it was observed that the ground motion suites selected based on single-*IMj* , and two-*IMj* conditioning approaches appeared to have underestimated the seismic losses by over 40% compared to the suite selected based on *Avg*−*IMj* .

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