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Multi-level nonlinear modeling verification scheme of RC high-rise wall buildings

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Abstract Earthquake-resistant reinforced concrete (RC) high-rise wall buildings are designed and detailed to respond well beyond the elastic range under the expected earthquake ground motions. However, despite their considerable section depth, in terms of analysis, RC walls are still often treated as linear elements, ignoring the effect of deformation compatibility. Due to the limited number of available comprehensive experimental studies on RC structural wall systems subjected to cycling loading, few in-depth analytical verification studies have been conducted. Motivated by the increasing need for more accurate seismic risk assessment of high-rise buildings in multi-scenario seismic regions, a multi-level nonlinear modeling verification scheme is presented in this paper to investigate two different nonlinear modeling techniques for shear walls (2- and 4-noded fiber-based elements). The investigated modeling approaches and their key parameters are verified against the results of Phase I of uniaxial shaking table specimen tests (performed at the University of California, San Diego) on a seven-story full-scale RC shear wall structure under base excitations representing four earthquake records of increasing intensities. Three numerical models are created using two different tools (ZEUS-NL and PERFORM-3D). The results obtained from the numerical models are compared with the experimental results both on global and local response levels (top displacement, interstory drift, story shear force, story bending moment, period elongation and rebar tensile strain). The study reveals the superior performance of 4-noded fiber-based wall/shell element modeling approach in accounting for the 3D effects of deformation compatibility between lateral and gravity-force-resisting systems. The study also highlights the sensitivity of attained results to the stiffnesses assigned to the rigid links and 3D joints required to connect the shear walls to neighboring elements when a 2-noded element is used.

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1 Introduction

With increasing concern for the seismic performance of multi-story RC buildings following extensive damages caused by recent strong earthquakes (Kobe 1995; Kocaeli 1999; Chi-Chi 1999; Tohoku 2011), the effectiveness of RC shear walls in medium- to high-rise buildings in earthquake-prone regions needs to be assessed. Shear walls can be found either as single elements coupled with moment-resisting frames or in the form of L, T, U-shaped or tubular cross-sections. Based on modern seismic codes, earthquake-resistant buildings are designed and detailed to respond inelastically under the design and maximum considered earthquakes. In RC high-rise buildings, well designed and proportioned RC slender shear walls can provide the needed strength, stiffness, and deformation ductility to ensure the adequate performance of the structure in the ''service'', ''damage'' and ''ultimate'' limit states. Nonetheless, for simplicity, RC shear walls are often modeled as linear elements during the analysis, despite their considerably large depth (ATC [2010;](#page-17-0) PEER [2010](#page-18-0)). This can lead to considerable underestimation of the deformed shape and compatibility issues between shear and flexural lateral resisting mechanisms, as well as, of the local high deformation demand. Furthermore, due to high costs and lack of availability of large-scale testing facilities, there are few reliable and comprehensive studies on the cyclic behavior of RC wall buildings that can be used for verification purposes (Beyer et al. [2008](#page-17-0); Ji et al. [2007;](#page-17-0) Wallace [2007;](#page-18-0) Wallace and Moehle [2012](#page-18-0)). Hence, there is still a need for a reliable nonlinear modeling methodology of building response which is essential for assessing the seismic vulnerability and estimating the seismic risk of such structures (ATC [2010](#page-17-0); Ji et al. [2007;](#page-17-0) Martinelli and Filippou [2009\)](#page-17-0).

Nonlinear Response History Analysis (NRHA) is the most reliable tool currently available for predicting building response at different levels of ground motion intensity. In NRHA, the accuracy of the nonlinear model is measured by its sufficiency in capturing significant modes of deformation and deterioration in the analyzed structure from the onset of damage to collapse. Various aspects of nonlinear modeling, such as element discretization, material force–deformation relationships, and assumptions on modeling of viscous damping are essential in defining the level of model accuracy in predicting the global and local seismic response of a structure. Very sophisticated wall microscopic models (i.e. continuum FE models) have the ability to provide a refined and detailed definition of the local response with a high level of flexibility and accuracy. However, the time requirement for computer run, post-processing, and interpretation of the numerical results render these models forbiddingly expensive for the seismic vulnerability assessment of high-rise structures especially when Multi-Record Incremental Dynamic Analysis (MRIDA) techniques are adopted. Alternatively, the macroscopic fiber-based element modeling approach is commonly used for RC shear walls (e.g. Wallace [2007](#page-18-0), [2012](#page-18-0)). Using this approach provides a proper description of wall geometry, detailing of steel reinforcing bars and material behavior. It accounts for key response features such as relocation (shifting) of the neutral axis along the cross-section of the wall during loading and unloading phases, interacting with the other components in the structure connecting the walls such as gravity frames and coupling beams (both in and out of the plane of the wall).

It also considers the impact of variation of axial load on wall flexural strength and stiffness. Given that experimental data of RC structural wall systems subjected to cycling load are very limited as most tests were conducted on isolated wall elements, few in-depth analytical verification attempts have been conducted for such systems. Therefore, it is essential to verify the nonlinear modeling techniques and parameters to be used with RC wall buildings against full-scale, shake-table tested RC wall structures.

The aim of the present study is to arrive at a verifiable nonlinear modeling approach and key modeling parameters that can be adopted in assessing the seismic performance of RC high-rise wall buildings. This is achieved by simulating the nonlinear dynamic response of a shake table full-scale seven-story RC wall building slice within a Multi-Level Nonlinear Modeling Verification Scheme (MLNMVS). This building was tested under base excitations representing four earthquake records of increasing intensities on the Large High-Performance Outdoor Shake Table (LHPOST) at University of California, San Diego (UCSD) [\(Panagiotou et al. 2007a,](#page-17-0) [b,](#page-17-0) [2011\)](#page-18-0). To model the shear walls in the tested structure, two fiber-based modeling approaches are investigated: (i) 2-noded beam-column line element (also termed wide-column element), where an equivalent column at the wall centroidal axis with wide cross section is used to model the property of the wall; and (ii) 4-noded wall element, a modeling approach conceptually similar to the Multiple-Vertical-Line-Element model (Wallace [2007,](#page-18-0) [2010\)](#page-18-0). ZEUS-NL analysis tool (Elnashai et al. [2012](#page-17-0)) is utilized to implement the first modeling approach, while PERFORM-3D (CSI [2011](#page-17-0)) is chosen to investigate the second.

A brief description of the USCD shake table test program and the test structure are given in Sect. 2 of this paper. In Sect. [3,](#page-3-0) the four input ground motions used in the tests are discussed. The numerical models created in the current study along with the comparison of their results to the experimental data are detailed in Sect. [4.](#page-4-0) The paper concludes with a summary of the work, findings, and modeling recommendations (Sect. [5](#page-16-0)).

2 Description of the test structure

The test program was performed on the LHPOST at UCSD as part of the George E. Brown Jr. Network for Earthquake Engineering Simulation (NEES) program. The tests were conducted in two phases: Phase I: Rectangular Wall ([Panagiotou et al. 2007a,](#page-17-0) [2011](#page-18-0)); and Phase II: T-Wall [\(Panagiotou et al. 2007b](#page-17-0)). In the current work, selected test results from Phase I (interstory drifts, story displacements, story shears, story moments, period elongation and local strains) are used to verify the numerical results obtained from the conducted MLNMVS.

The test structure is a representative slice of a 7-story prototype residential load bearing wall building located in Los Angeles, California. It consisted of a 3.66 m long load bearing RC rectangular wall directed East–West (loading direction), hereafter referred to as ''web wall'', a 4.88 m long load bearing RC rectangular wall directed North–South, hereafter referred to as ''flange wall'', an auxiliary C-shaped precast segmental pier with unbonded post-tensioning, hereafter referred to as ''precast pier'', and four auxiliary pin-ended gravity columns at the north and south ends of the test structure. The web wall alongside the gravity columns provide support to seven, 200 mm thick, 3.65 m \times 8.13 m simply supported RC slabs spaced at 2.74 m (story height). The precast pier was designed to have pin–pin connections with the floor slab. This was accomplished by using horizontal steel truss (angles) bolted to the floor slab at one end and to the precast pier at the other. The

bolted connections combined with the limited moment capacity of the steel angles prevented the transfer of moment from the floor slab to the precast pier.

During Phase I of the test program, web and flange walls were linked with a 610 mm wide slab. The link slab had two, 140 mm deep by 51 mm wide, slots on both ends. The near-pinned link was designed to guarantee diaphragm action in the longitudinal and transverse directions but a reduced capacity for moment transfer and coupling between the flange and web walls. In this area, overlapping transverse reinforcing bars from the web and flange walls were provided to account for the future establishment of monolithic connection during Phase II. Furthermore, a vertical gap of 635 mm width between the web and the flange walls was left to avoid shear transfer between the two walls. This arrangement allowed the flange wall to provide stability only in the longitudinal direction (North–South), while the web wall primarily provided lateral force resistance in the earthquake loading direction. During Phase II of the test, the 635 mm vertical gap was cast to ensure a T-section wall monolithic behavior. The web and flange walls were fixed at the base, while the precast pier connection to the shake table was designed to allow rocking the loading direction (pin connection) while providing large moment resistance in the orthogonal direction (fixed connection). The precast pier with its foundation, the horizontal steel truss, and the link slab, as a system, provided the torsional stability for the entire test structure, including the flange wall. Therefore, rotational strains at the flange wall ends were not needed. It is worth emphasizing that during both test phases, the earthquake excitations (loading) were applied only in the web wall direction (East–West).

The four pin-ended gravity columns were made of high-strength, prestressed steel threaded Dywidag bars, 44.5 mm in diameter for the first story and 25.4 mm in diameter for the above stories. The Dywidag bars were grouted inside high-strength, 102 mm diameter, 8.6 mm thick steel pipes to prevent them from buckling. These bars formed the columns' end pin-connections with the RC slabs and the foundation, enabling the columns to carry axial tension and compression only and not to contribute to lateral force resistance. The test structure height, starting from the top of the foundation, was 19.20 m with total mass (excluding the foundation) of around 210 tons.

Concrete with a target 27.6 MPa specified compressive strength and Grade 60 steel reinforcement were used in the test structure. The measured average concrete compressive strength at the day of the final test was 37.9 MPa, while the average measured reinforcing steel yield strength was 455 MPa. The footings under web and flange walls were longitudinally prestressed and designed to remain elastic during testing. Figure [1](#page-4-0) shows floor plans of the prototype building with a perspective view of the test structure, while the geometry of the test structure and the reinforcement details for the web wall, flange wall, and slabs are given in Figs. [2](#page-5-0) and [3](#page-6-0), respectively. More details about the test structure can be found in Panagiotou et al. [\(2007a](#page-17-0), [2011\)](#page-18-0).

3 Input ground motions

Phase I of the test program investigated the response of the cantilever web wall to four levels of excitations with increased intensities (EQ1–EQ4) representing four historical earthquakes recorded in Southern California. Prior to and between the earthquake tests, the structure was subjected to long-duration ambient vibration tests and long-duration lowamplitude white noise tests for system damage identification (Moaveni et al. [2010\)](#page-17-0). The low-intensity input motion EQ1 was the VNUY longitudinal component from the 1971 M_w

Fig. 1 Prototype building and test structure used in modeling verification: a Residential floor plan; b parking floor plan; c perspective view of the test structure (Panagiotou et al. [2007a\)](#page-17-0)

6.6 San Fernando earthquake. The two medium intensity input motions EQ2 and EQ3 were the VNUY transverse component record from the 1971 M_w 6.6 San Fernando earthquake and the WHOX longitudinal component from the 1994 M_w 6.7 Northridge earthquake, respectively. The large intensity input motion EQ4 was the Sylmar Olive View Med 360 component record from the 199[4](#page-7-0) M_w 6.7 Northridge earthquake. Figure 4 shows the acceleration time histories alongside the acceleration and displacement response spectra of the four input motions while Table [1](#page-7-0) lists the peak recorded values of selected response parameters for the test structure (Panagiotou et al. [2011\)](#page-18-0).

4 Multi-level modeling verification scheme

Three numerical models are developed for the present study. ZEUS-NL (Elnashai et al. [2012\)](#page-17-0) is utilized to develop the first two: ''Z-Model''; a two-dimensional (2D) nonlinear model using 2-noded fiber-based frame element modeling approach in modeling the RC walls, and ''IZ-Model''; an improved 2D nonlinear model using the same aforementioned approach. PERFORM-3D (CSI [2011\)](#page-17-0) is utilized to develop the third model ''P-Model''; a three-dimensional (3D) nonlinear model using 4-noded fiber-based wall modeling approach. Modeling key features and the multi-level verification results for each of the three developed numerical models are given in the following sub-sections. Figure [5](#page-8-0) shows schematic diagrams of the three models.

4.1 Modeling and verification using 2D, 2-noded fiber-based frame element modeling approach: Z-Model

The 2D (in the plane of excitations) model for the test structure is developed using ZEUS-NL (Fig. [5a](#page-8-0)). The centerline model included the web wall, flange wall, gravity columns, prestressed segmental pier, link slab and the braces connecting the segmental pier to the structure. 2-noded fiber-based cubic elasto-plastic elements are used to model the response of web and flange walls as well as the slotted slab connecting them. Elastic frame elements are used to model the prestressed segmental pier, the gravity columns, and the braces.

Fig. 2 Test structure used in modeling verification: a Elevation; b floor plan view; c foundation plan view

Fig. 3 Reinforcement details for the test structure: a Web and flange walls at first level; b web and flange walls at levels 2–6; c floor and link slabs at all levels

Rigid links are utilized to connect the web wall centerline to the gravity column elements at both wall ends. A 3D joint element characterized by linear elastic behavior is used to simulate the pin–pin connection of gravity columns, braces and the East–West hinge connection between the segmental prestressed pier and its footing. The 3D joint element can be used in 2D and 3D modeling to model pin joints, inclined supports, structural gaps, soil-structure interaction and elasto-plastic joint behavior. To define a 3D joint element, four nodes are required. Nodes 1 and 2 are the end nodes of the element and must be initially coincident; node 3 defines the x-axis of the joint, while the fourth node defines the x–y plane (Fig. [5d](#page-8-0)). Each of nodes 1 and 2 has 6-degrees of freedom where for each; three different types of force–deformation relationships (linear elastic, bilinear/trilinear symmetric elasto-plastic and bilinear/trilinear asymmetric elasto-plastic) can be assigned to represent axial, shear and bending cyclic behavior. Any degree of freedom in nodes 1 and 2 can be restrained by assigning a linear force–deformation relation with a very high stiffness value to it. The seismic mass of the test structure is lumped at floor levels to simplify the

Fig. 4 Most intense 30 s time histories and response spectra of recorded table ground motions for the test structure used in modeling verification

Response parameter	Before Equation 1	After Equation 1	After	After Equation 2 Equation 3	After Equation 4
Fundamental period (s)	0.51	0.65	0.82	0.88	1.16
Roof relative lateral displacement (m)	$\overline{}$	0.05	0.14	0.16	0.38
Roof drift ratio $(\%)$		0.28	0.75	0.83	2.06
Inter-story drift ratio*		0.35	0.89	1.03	2.36
Peak table acceleration (g)		0.15	0.27	0.35	0.91
System base shear $(kN)^8$		425	628	704	1185
System base moment $(kNm)^{8}$		5606	8093	8490	11839

Table 1 Peak recorded values of selected response parameters for the test structure (Panagiotou et al. [2011\)](#page-18-0)

* Overall stories

§ Calculated as the product of story mass with measured horizontal floor acceleration

numerical model. The weight of the structure is also applied as nodal loads to account for gravity and $P-\Delta$ effects during NRHA.

The uniaxial nonlinear constant confinement constitutive model of Mander et al. ([1988](#page-17-0)) with improved cyclic rules proposed by Martínez-Rueda and Elnashai (1997) (1997) is used to calculate the properties of confined concrete which are assigned to the corresponding fibers in the web and flange walls cross-sections at the first story (Fig. [6](#page-8-0)a). The concrete in the upper stories had no confinement reinforcement and thus modeled using unconfined concrete fibers. In both cases, the tensile strength of concrete is neglected. The force– deformation behavior of the steel reinforcing bars in the test structure (Fig. [6](#page-8-0)b) is idealized using the uniaxial steel model of Menegotto and Pinto ([1973\)](#page-17-0) coupled with the isotropic

Fig. 5 Schematic diagrams of developed models for the test structure: a Z-Model; b IZ-Model; c P-Model; d 3D joint element

Fig. 6 Constitutive material models: a concrete in Z-Model and IZ-Model; b steel rebars in Z-Model and IZ-Model; c general four-linear-segment F–D relation for concrete and steel rebars in P-Model

hardening rules proposed by Filippou et al. (1983) (1983) . In Fig. [6](#page-8-0)b, E_0 is the initial elastic modulus of steel, E_1 is the strain-hardening modulus, R_0 is a parameter defining the initial loading curvature, and a_1 to a_4 are experimental-based parameters that control the curvature and isotropic strain hardening in subsequent load cycles, taken as 20, 18.5, 0.15, 0.01 and 7, respectively (Elnashai et al. [2012](#page-17-0)).

Previous studies indicated that shear deformation may have a significant contribution to the lateral displacement of walls especially at lower stories, even in walls that are categorized as flexure-dominated (Thomsen and Wallace [1995](#page-18-0)). In ZEUS-NL, the fibers in the cubic elasto-plastic element used to model the web wall have zero resistance to transverse forces, and hence shear deformation cannot be determined at the section level. It can be, however, explicitly modeled by introducing shear springs to the wall element. Justified by the fact that the experimental results for the test structure evidenced almost exclusively flexural cracking at the web wall base (Martinelli and Filippou [2009;](#page-17-0) Panagiotou et al. [2007a\)](#page-17-0), shear deformation is not considered in this numerical model.

ZEUS-NL includes Rayleigh damping as the only option to account for the effects of the viscous damping during dynamic analysis. The mathematical model of Rayleigh damping in this package is based on initial stiffness in calculating the damping matrix. When the use of tangent stiffness-proportional damping is not an available option, previous studies recommended lowering the first mode initial stiffness-proportional damping value (e.g. Hall [2006;](#page-17-0) Smyrou et al. [2011\)](#page-18-0). The use of the mass-proportional damping term in the damping matrix is discouraged by several researchers. For an instant, Priestley and Grant ([2005\)](#page-18-0) showed that including the mass-proportional term in the damping equation can heavily weight the mass matrix, leading to a nearly constant damping matrix during the post-elastic response of the structure regardless of stiffness degradation. Hall ([2006](#page-17-0)) suggested that the presence of mass-proportional damping will generate extraneous damping forces due to the rigid body motion component involved in the formulation of earthquake analysis that is based on total motion. It is worth noting that rigid body motion phenomena become more significant in the analysis of tall buildings.

For the test structure, previous studies have adopted different approaches and values to model viscous damping. For instance, Panagiotou and Restrepo [\(2006](#page-17-0)) used a damping ratio of 0.3% for the first longitudinal mode to accurately simulate the response to earthquake input motions; Martinelli and Filippou ([2009\)](#page-17-0) used Rayleigh damping with mass and initial stiffness-proportional damping matrix and a 1.0% damping ratio for the first two flexural modes; while Waugh and Sritharan [\(2010](#page-18-0)) used tangent stiffness-proportional viscous damping corresponded to 0.5 and 0.8% damping ratios for the first and third uncracked mode periods, respectively. The use of such a low damping ratio in modeling the test structure can be attributed to the absence of non-structural elements and also to the fact that flexural cracking was largely limited to the lower part of the structure as a consequence of the low ratio of longitudinal reinforcements in which the design approach of the building led to (i.e. displacement-based design). Based on the above discussion, a stiffness-proportional viscous damping corresponding to 0.5% damping ratio in the first longitudinal mode is used in the Z-Model, while the mass-proportional damping term is set to zero.

The input motions shown in Fig. [4](#page-7-0) are applied to the base of the Z-Model in the East– West direction parallel to the web wall. Using the Newmark integration scheme, NRHA is conducted at a time step of 1/60 s. The four input motions, EQ1 to EQ4, are concatenated to account for the accumulated structural damage on the response of the test structure. Six seconds of zero base acceleration is added in between the earthquake records to allow the

structure to come to rest prior to being subjected to the next record. The applied concatenated base motion record is 523 s long in total.

The capability of the Z-Model in predicting the global response of the test structure during the most intense 30 s of each of the four earthquake input motions is assessed by comparing the numerical results with measured data for top-floor relative displacement time histories (Fig. 7), response envelopes of story displacement, interstory drift (ISD), story shear force and story overturning moment (Fig. [8\)](#page-11-0). Figure 7 shows that the model captures well all the significant peak relative displacements recorded during EQ1, EQ2, and EQ4, while the peak displacements on EQ3 are under predicted by as much as 25%. The discrepancies of the computed response for EQ3 have also been reported in other studies (Kelly [2007](#page-17-0); Waugh and Sritharan [2010](#page-18-0)). This is mainly attributed to the similarity in earthquake intensity between EQ2 and EQ3 input motions. As a consequence of these two records having comparable intensities, the unloading and reloading paths of the material models rather than their envelopes have a big influence on the numerical response of EQ3. Accurate representation of the unloading and reloading behavior of material models becomes more important when the structure does not move into virgin territory, as for example during aftershocks. Figure [8a](#page-11-0) shows very good agreement between predicted and measured displacement envelopes at floor-levels (story displacement). As expected, the displacements of EQ3 are under predicted. The maximum calculated roof drift ratios are found to be 0.30% for EQ1, 0.75% for EQ2 and 2.05% for EQ4, compared to their corresponding measured values of 0.28, 0.75, and 2.06%, respectively. For EQ3, the obtained and measured maximum roof drifts are 0.78 and 0.83%, respectively. ISD is typically considered as a key parameter in defining performance limit states for seismic vulnerability assessment of buildings and hence it is essential to have this parameter accurately predicted. As shown in Fig. [8](#page-11-0)b, the ISD envelopes are well predicted by the

Fig. 7 Z-Model: measured versus computed top relative displacement under the four input motions

Fig. 8 Z-Model: measured versus computed envelopes: a Relative displacement; b interstory drift; c story shear; **d** story overturning moment

analysis for EQ1, EQ2, and EQ4, while for EQ3 the envelope is within 30% of the experimental values for the reasons given above.

Despite the very good agreement between predicted and measured response values (top displacement time histories, story displacement, and ISD envelopes), the Z-Model underestimates the story shear and consequently story moment envelopes of the test structure, especially when the structure behaves inelastically (Fig. 8c, d). The discrepancies between reported and numerical story shear and moment values can be attributed to the influence of the 3D interaction between gravity columns, floor slabs and the web wall on the overall lateral capacity of the test structure. The significant contribution of this interaction to the lateral force resistance of the test building was also confirmed by Panagiotou and Restrepo ([2006\)](#page-17-0) using pushover analysis. The main reason for this influence is that, due to their interaction with the floor slab, the gravity columns developed significant axial strains during testing. Consequently, the columns near the tension side of the web wall experienced tensile forces whilst those closer to the compression side were subjected to compression forces. Given the 3.05 m span between the columns, the tension and compression forces enabled a large moment to be developed and effectively increased the lateral force resistance of the test structure.

4.2 Modeling and verification using 2D, 2-noded fiber-based frame element modeling approach: IZ-Model

To address the shortcomings of the Z-Model, an improved 2-noded fiber-based model (IZ-Model) is developed to introduce the 3D slab-columns-web wall interaction effect. In this model, 3D joint element is introduced at both ends of the rigid link that connect the web

wall centerline to the gravity columns at each floor level (Fig. [5b](#page-8-0)). A bilinear asymmetric moment–curvature relation is assigned to those elements in the 2D plane of the model to simulate the out-of-plane flexural rigidity of the slab. The asymmetric relation is due to the different reinforcement mats in the top and bottom of the slabs in the test structure. The remaining five degrees of freedom in nodes 1 and 2 of the 3D joint were restrained by assigning them high stiffness values. Figure 9 shows the story shear and moment envelopes predicted using the IZ-Model for EQ1 to EQ4, where significant improvements can be seen. This exercise highlights the importance of taking into account the 3D interaction effect of all structural members in the building to accurately predict the seismic response.

To assess the capability of the IZ-Model to capture the damage evolution of the test structure during the four input motions, the frequency spectra of the top relative displacement time histories using the Fast Fourier Transform (FFT) method and the structure periods of the first two modes are plotted for EQ1 to EQ4 in Fig. [10](#page-13-0). It is worth noting that the measured fundamental frequency of the test structure changed from 1.96 Hz before testing to 0.86 Hz at the end of EQ4, with corresponding fundamental periods of 0.51 and 1.16 s, respectively. Despite the significant lengthening of the fundamental period of the test structure by more than 200%, the IZ-Model was able to track this damage progression with good accuracy. At the end of EQ4, the observed difference between measured and predicted first mode frequency is 20%, which can be attributed to the high flexural stiffnesses of the rigid links and 3D joints in the model.

Another measure of the capability of the numerical model is the determination of local damage. Figure [11](#page-13-0) depicts the tensile strain envelope of an outer reinforcing bar located in the web wall, marked as ST2 in the tests, along the height of the first level for EQ4 input motion. It should be noted that computed strains can be mesh-sensitive, especially at zones of concentrated plasticity. To investigate the influence of mesh size on the computed stains, the web wall member in the first level of the building is modeled using four different meshes: One Element-mesh (1E); Two Element-mesh (2E); Three Element-mesh (3E); and Six Element-mesh (6E). The results presented in Fig. [11](#page-13-0) indicate that the IZ-Model (2E) predicted the tensile strain envelopes of the ST2 reinforcing bar with good accuracy. It is worth mentioning that the 2E needed an element length of 1321 mm, which is close to the expected plastic hinge length at the web wall base (0.5 times the flexural depth of the wall =1830 mm) as proposed by ASCE/SEI 41-06 ([2007\)](#page-17-0). Hence, mesh sizes not exceeding the expected plastic zone length are confirmed as being suitable for fiber-based modeling of RC shear walls.

Fig. 9 IZ-Model: measured versus computed envelopes: a Story shear; b story moment

Fig. 10 IZ-Model: evolution of modal characteristics under the four input motions: a Frequency spectra; b structure periods

Fig. 11 IZ-Model: tensile strain of ST2 reinforcing bar over the height of the first level under EQ4

4.3 Modeling and verification using 3D, 4-noded fiber-based wall modeling approach: P-Model

To evaluate the capability of the 4-noded element modeling approach in predicting the response of the test structure, the P-Model is developed using PERFORM-3D (CSI [2011](#page-17-0)). To model the web and flange walls, a 4-noded fiber-based shear wall element is used with nonlinear vertical fibers to represent the behavior of concrete and reinforcing steel. Based on the outcome of the element mesh sensitivity study conducted on the IZ-Model in Sect. [4.2](#page-11-0), the web wall in the first level is represented by two vertical elements. The link slab is modeled using 2-noded fiber-based frame element. An elastic frame element with specified cross-section properties is used to model the prestressed segmental pier, while elastic bar element is utilized to model the pin–pin end braces and gravity columns. Finally, an elastic 4-noded shell element is used to represent the floor slabs. For the sake of comparison, the same principles used in the Z-Model and IZ-Model for modeling the seismic mass of the test structure are followed.

A four-linear-segment Force–Deformation (F–D) relation is used to approximate the concrete stress–strain relationship based on the modified Mander model (Fig. [6](#page-8-0)c). For the reinforcing steel material model, a similar relation is used with the post-yield stiffness and cyclic degradation parameters defined following the adjustments described by Orakcal and Wallace [\(2006](#page-17-0)). A linear stress–strain relation is used to model the materials of the prestressed segmental pier, floor slabs, braces and gravity columns. In PERFORM-3D, viscous damping can be modeled using modal damping, a more preferred viscous damping modeling approach (CSI [2011](#page-17-0)). However, for consistency, the same assumptions and procedures used in the ZEUS-NL models for the viscous damping, applying of input motions and numerical strategy are adopted in this model.

Shear deformation in the web wall is accounted for in the P-Model by assigning a trilinear relation to the wall element similar to the one given in ASCE/SEI 41-06 ([2007\)](#page-17-0) to represent the nonlinear shear behavior of the wall. Test results by Thomsen and Wallace (2004) (2004) and the follow-up calibration studies by Gogus (2010) are used to define the shear F–D relation. In the used trilinear relation, the uncracked shear modulus is taken as $0.4 E_c$ and diagonal (shear) cracking is assumed to start at $0.25\sqrt{f\overline{c'}} \le 0.5v_n$, where v_n is the wall nominal shear strength from ACI code [\(2014](#page-17-0)). The post-cracking slope is reduced to 0.01 E_c to account for the nonlinear shear deformations due to shear-flexure interaction (Massone [2006\)](#page-17-0).

Following the same sequence used in the previous section, Figs. 12, [13](#page-15-0), [14](#page-15-0) and [15](#page-16-0) show predicted versus measured top-floor relative displacement time histories, response envelopes, evolution of modal characteristics and ST2 steel rebar tensile strain, respectively. Very good agreement can be seen for all predicted responses except for EQ3, for the same reasons discussed earlier.

While the data measured from the shake table test confirmed the accuracy of the investigated modeling approaches and key parameters in predicting global response and local damage induced by seismic demands on slender wall structures, some limitations became apparent in the 2-noded fiber-based modeling approach (e.g. accounting for 3D

Fig. 12 P-Model: measured versus computed top relative displacement under the four input motions

Fig. 13 P-Model: measured versus computed envelopes: a Relative displacement; **b** interstory drift; c story shear; d story overturning moment

Fig. 14 P-Model: evolution of modal characteristics under the four input motions: a Frequency spectra; b structure periods

compatibility effects). The study reveals the superior ability of 4-noded fiber-based wall/ shell element to account for 3D effects of deformation compatibility between lateral and gravity-force-resisting systems. The study also addresses the sensitivity of attained results to the stiffnesses assigned to the rigid links and 3D joints required to connect the shear walls to neighboring elements when the 2-noded fiber-based element modeling approach is used.

Fig. 15 P-Model: tensile strain of ST2 reinforcing bar over the height of the first level under EQ4

5 Summary and conclusions

In this paper, the results from Phase I of the shake table tests undertaken at UCSD of a fullscale slice of a seven-story RC wall building are employed to conduct a Multi-Level Nonlinear Modeling Verification Scheme (MLNMVS). The scheme verifies different approaches and key parameters in modeling RC slender shear walls forming the lateralforce-resisting system in RC high-rise wall buildings. Three numerical models are created to simulate the nonlinear response of the test structure to four consecutive table excitations representing real earthquake motions with increasing maximum acceleration from 0.15 to 0.91 g. 2-noded fiber-based beam-column element approach is adopted to model the web and flange walls in the 2D ''Z-Model'' and 'IZ-Model'' centerline models using ZUES-NL tool. PERFORM-3D package is utilized to create the third, 3D, model ''P-Model'' using 4-noded fiber-based wall/shell element. The main conclusions drawn from this study are:

- With appropriate care in the modeling of the geometry, both investigated nonlinear modeling approaches (2- and 4-noded fiber-based elements) are sufficient to predict global deformation response (story lateral displacement and interstory drift) of RC wall buildings with relatively good accuracy.
- The study reveals the supremacy of 4-noded fiber-based wall/shell element in accounting for the 3D effects of deformation compatibility between lateral and gravityforce-resisting systems. The 3D interaction between gravity columns, floor slabs, and the web wall significantly contributed to the overall lateral capacity of the test structure.
- When initial stiffness is used in constructing the damping matrix for RC wall buildings with no or well-isolated non-structural elements, low viscous damping ratio (0.5% for the test structure) is suitable for assessing their seismic performance.
- The observed difference between predicted and measured responses of the test structure under the two consecutive input motions with comparable intensities (EQ2 and EQ3) highlights the importance of accurate representation of the unloading/reloading paths of the material models. This is particularly true when assessing the performance of buildings under earthquake motions that do not move the structure into virgin territory (i.e. past previous deformations).
- No noticeable change is observed in the numerical response of the test structure when shear deformation is accounted for in the P-Model compared to the results obtained

from the IZ-Model. This is justified by the test results that demonstrated almost exclusively flexural cracking at the web wall base. However, shear deformation may still make a significant contribution to the lateral displacement of walls in tall buildings, even in walls categorized as slender and/or flexure-dominated. Hence, considering the shear deformation either implicitly (coupled model) or explicitly (uncoupled model) is recommended.

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