



A general purpose, low power, analog integrated image edge detector, based on a current-mode Gaussian function circuit

Georgios Gennis¹ · Vassilis Alimisis¹ · Christos Dimas¹ · Paul Peter Sotiriadis¹

Received: 30 March 2022 / Revised: 17 June 2022 / Accepted: 13 August 2022 / Published online: 23 August 2022
© The Author(s), under exclusive licence to Springer Science+Business Media, LLC, part of Springer Nature 2022

Abstract

A low power analog integrated image edge detector is proposed consisting of Gaussian function and threshold circuits. The operating principle of this architecture is based on a hardware-friendly approximation of the Robert's Cross operator. The system level implementation can be easily modified to account for various image resolutions. Therefore, the proposed architecture can be used as a building block in larger smart sensor systems. The edge detector was evaluated using 3 medium resolution images, achieving average Peak Signal-to-Noise-Ratio of 27.7 dB and Structural Similarity Index Metric of 0.81, while consuming only 33 nW per pixel. To demonstrate the performance and accuracy of the proposed architecture, Monte-carlo simulation results are provided. Both schematic and post-layout simulations are carried out in 90 nm CMOS process, using the Cadence IC suite.

Keywords Analog integrated implementation · Bump circuits · Edge detector · Low-power design · Robert's Cross operator

1 Introduction

Internet-of-things (IoT) is a combination of sensor-based devices and systems which have the ability to collect and transfer data over a network without the need of manual control [1]. There are many cases in which power hungry devices are used in order to connect the node of a system's data with data centers [2]. In order to reduce the unnecessary data transferring and the high power consumption new computing paradigms are applied. Edge computing is a solution which brings computation and data storage closer to data sources. In the case of remote sensor systems, where online recharging capabilities are unavailable, power consumption

is a vital factor. As a result edge computing should utilize power efficient devices.

A potential approach to minimize such systems' power consumption involves analog integrated architectures, especially with transistors that operate in the sub-threshold region [3]. A particular field which can benefit from the advantages of analog computing and hardware parallelization is image processing, since it is usually computationally expensive. A popular image processing method is edge detection, which can be used in various applications, including medical diagnosis [4], real-time object recognition [5], navigation systems [6] and more [7, 8].

In the literature only a few works that involve analog integrated-based image edge detection exist. In particular, [9] demonstrates a two-stage network, in which the first stage detects the edges by applying a series of filters and thresholding circuits. Then, the second stage reconstructs the original image based on the edges that are previously detected. [10] presents a morphological edge-detector which estimates the images' erosion and dilation. In addition, [11] and [12] propose an analog implementation of the Sobel operator [13], achieving high quality results at the cost of chip area and power consumption. Another existing approach is to combine current [14] or voltage mode [15, 16] mixed-signal circuitries that employ convolution filters.

✉ Vassilis Alimisis
alimisisv@gmail.com

Georgios Gennis
giorgosyennis@gmail.com

Christos Dimas
chdim@central.ntua.gr

Paul Peter Sotiriadis
pps@ieee.org

¹ Department of Electrical and Computer Engineering,
National Technical University of Athens, 15780 Zografou,
Athens, Greece

Despite the fact that the aforementioned works are characterized by lower power consumption compared to their digital counterparts, the growing need in higher image resolutions requires even greater power management, especially for battery-dependent IoT devices. In this direction, the work presented in [17] utilizes a compact Gaussian function circuit, reducing the circuit's power dissipation to 0.9 μW per pixel. Nonetheless, this reduction was achieved, using a custom edge-detection algorithm, at the cost of performance in accuracy.

In this work, motivated by the challenges related to the trade-off between power efficiency and performance, we propose a high-performance compact analog integrated edge-detector that takes advantage of an ultra-low power current-mode Gaussian function circuit. Its architecture is directly integrated on a photodiode sensor array and produces a digital output without the need of any data converters. The proposed design can be used in various different applications without any significant modifications. This article extends the authors' previous work [18] which shares a low-power, low area and fast analog Bayesian classifier for thyroid disease detection, based on a low-power current-mode Gaussian function circuit. In particular, we present a hardware-friendly implementation of the Robert's Cross operator (RCO) to structure an analog edge-detector, using the same building blocks as in [18]. The implemented architecture achieves a low power dissipation of 33 nW per pixel, Peak Signal-to-Noise-Ratio (PSNR) value of 27.7 dB and Structural Similarity Index Metric (SSIM) of 0.81.

The remainder of this paper is organized as follows. Section 2 explains the mathematical foundations of the RCO. The proposed implementation and its basic building blocks are analyzed in Sect. 3. Section 4 presents the experimental results of the proposed edge detector and compares them with a software-based model. A comparison and discussion are provided in Sect. 5. Section 6 concludes the article.

2 Mathematical background

The RCO is one of the first and simplest edge detectors in the literature [19, 20]. It is a computationally efficient differential operator that, despite the approximations considered, achieves impressive results. The RCO detects regions with high spatial frequency in the diagonal direction and therefore produces results that mimic to the human perception's ones.

We assume an image with a $N \times M$ resolution, x_{ij} denotes the light intensity of a pixel (i, j) , for each $i < N$, $j < M$. First, consider y_{ij} as the root square of x_{ij} :

$$y_{ij} = \sqrt{x_{ij}}, \quad (1)$$

then, the approximation of the image's gradient z_{ij} is calculated as:

$$z_{ij} = \sqrt{(y_{ij} - y_{i+1,j+1})^2 + (y_{i+1,j} - y_{i,j+1})^2}. \quad (2)$$

This gradient is in fact a grayscale image in which the detected edges are characterized by a high intensity value, whereas flat areas by a low one.

In practice, the RCO is calculated by convolving the given image with two 2×2 diagonal matrices \mathbf{M}_x and \mathbf{M}_y , given by:

$$\mathbf{M}_x = \begin{bmatrix} +1 & 0 \\ 0 & -1 \end{bmatrix} \text{ and } \mathbf{M}_y = \begin{bmatrix} +1 & 0 \\ 0 & -1 \end{bmatrix}. \quad (3)$$

Through the convolution of \mathbf{M}_x and \mathbf{M}_y with the image considered, the two components \mathbf{G}_x and \mathbf{G}_y are calculated as:

$$\mathbf{G}_x = \mathbf{Image} * \mathbf{M}_x, \quad (4)$$

$$\mathbf{G}_y = \mathbf{Image} * \mathbf{M}_y. \quad (5)$$

where $*$ denotes the convolution operator. The calculation process for both \mathbf{G}_x and \mathbf{G}_y can be simplified as:

$$G_x(i, j) = y_{ij} - y_{i+1,j+1}, \quad (6)$$

$$G_y(i, j) = y_{i+1,j} - y_{i,j+1}. \quad (7)$$

In this case, the approximation of the image's gradient $\nabla I(i, j)$ is calculated as:

$$\nabla I(i, j) = \sqrt{G_x(i, j)^2 + G_y(i, j)^2}, \quad (8)$$

for each pixel (i, j) for $i < N$, $j < M$. Finally, one could optionally use a threshold on the the gradient $\nabla I(i, j)$ to produce a binary image $bin(i, j)$ that indicates the edges:

$$I_{bin}(i, j) = \begin{cases} 0 & \text{if } \nabla I(i, j) < I_{th} \\ 1 & \text{if } \nabla I(i, j) \geq I_{th} \end{cases}, \quad (9)$$

where, I_{th} is a parameter threshold value.

3 Proposed analog edge detector

A hardware-friendly modification of the RCO as well as the proposed analog edge detector's building blocks and operation are explained in this section. We note that, all transistors in the following design operate in the sub-threshold domain with power supply rails set to $V_{DD} = -V_{SS} = 0.3\text{V}$ in order to reduce the power consumption of the entire circuitry.

3.1 Hardware-friendly Robert’s cross operator

In the literature, Bump circuits are used to implement Bell-like curves, that greatly resemble the Gaussian curve [21]. Despite being less accurate than the other Gaussian function circuit implementations, their low power consumption and compactness makes them preferable in various applications that require simultaneous operation of multiple Gaussian function circuits [21]. Their vast range of applications includes RBF-based classifiers [22], neuromorphic circuits [23], fuzzy and neuro-fuzzy controllers [24] and smart sensor systems like anomaly [25] and edge detection [17] circuits. In this work, we propose a hardware-friendly modification of the RCO (see Sect. 2) which facilitates a simple implementation of the analog edge detector by using Bump circuits as basic computational blocks. This is preferable to implementing the original RCO using squaring and root square circuits that, typically, are more challenging and power expensive than Bump circuits [21].

We assume the aforementioned image with a $N \times M$ resolution. In our hardware-friendly implementation we make use of the following mapping $\hat{z}_{i,j}$ of the RCO $z_{i,j}$ using a Gaussian Kernel transformation:

$$\begin{aligned} \hat{z}_{i,j} &\triangleq e^{-\frac{1}{2\sigma^2}(z_{i,j})^2} \\ &= e^{-\frac{1}{2\sigma^2}(\sqrt{(y_{i,j}-y_{i+1,j+1})^2+(y_{i+1,j}-y_{i,j+1})^2})^2} \\ &= e^{-\frac{1}{2}\frac{(y_{i,j}-y_{i+1,j+1})^2}{\sigma^2}} e^{-\frac{1}{2}\frac{(y_{i+1,j}-y_{i,j+1})^2}{\sigma^2}}, \end{aligned} \tag{10}$$

where the variance σ acts a parameter that controls the sensitivity of the edge detection operator. This equation can be expressed as follows:

$$\hat{z}_{i,j} = 2\pi\sigma^2 \mathcal{N}(y_{i,j}||y_{i+1,j+1}, \sigma^2) \mathcal{N}(y_{i+1,j}||y_{i,j+1}, \sigma^2), \tag{11}$$

where $\mathcal{N}(x||\mu, \sigma^2)$ is the univariate Gaussian function and is given by:

$$\mathcal{N}(x||\mu, \sigma^2) = \frac{1}{\sqrt{(2\pi)\sigma^2}} e^{-\frac{1}{2}\frac{(x-\mu)^2}{\sigma^2}}. \tag{12}$$

Here, μ denotes the mean value of the Gaussian function. In practice, for the hardware implementation of (11), $2\pi\sigma^2$, for a given σ , is a scalar constant and can be ignored. Also, unlike the original RCO, here, the edges are characterized by a low intensity value and the non-edges by a high one.

3.2 Edge detector architecture

In this paper, the basic building block is the Bump circuit introduced in our previous work [18], depicted in Fig. 1. It is composed of two neuron cells and a symmetrical current

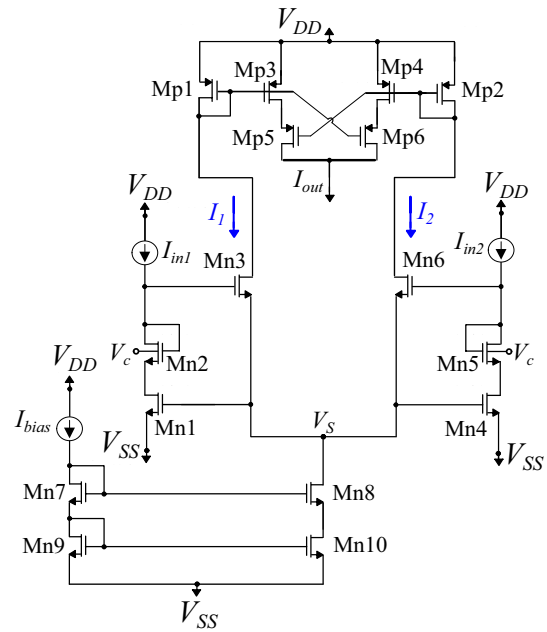


Fig. 1 The proposed analog architecture implementing a Bump circuit. I_{in1} , I_{in2} , V_c and I_{bias} are the 2 input currents, the voltage controlling the variance and the bias current controlling the height of the Gaussian curve, respectively. [18]

correlator biased by a cascode current mirror. The two neuron cells operate as a differential pair, where the differential voltage input is replaced by two input currents. Unlike a typical Bump circuit [21, 26, 27], where one of the differential pair’s voltage inputs acts as a constant parameter, here, based on (11) both I_{in1} and I_{in2} are in fact inputs to the circuit. The two neurons produce two drain currents I_1 and I_2 , which consist of two complementary sigmoidal curves. Given these sigmoidal currents, the correlator’s output current resembles a Gaussian curve. The voltage parameter V_c and the bias current I_{bias} control the variance and the height of the Gaussian curve, respectively. In particular, as shown in Fig. 2 by increasing the absolute value of V_c , the Gaussian curve’s width also increases. Furthermore, the output current’s maximum value $I_{out,max}$ is approximately equal to the bias current value I_{bias} . All transistors’ dimensions are summarized in Table 1.

Bump circuits can efficiently perform multiplication without the use of additional components. In particular, let us consider two Bump circuits. If we bias the second Bump circuit (I_{bias2}) with the first Bump circuit’s output current (I_{out1}), the output current of the second Bump equals the product of their respective Gaussian curves [27]. In this configuration, only the first Bump circuit is biased with a specified external bias current (I_{bias}). This topology constitutes the analog implementation of the RCO, depicted in Fig. 3 and its output current approximates a 2×2 image’s gradient.

Fig. 2 Left: Parametric analysis over I_{bias} , for $I_{in1} \in [0, 10]$ nA, $I_{in2} = 5$ nA, $V_c = 0$ V. Right: Parametric analysis over V_c , for $I_{bias} = 12$ nA, $I_{in1} \in [0, 10]$ nA and $I_{in2} = 5$ nA. [18]

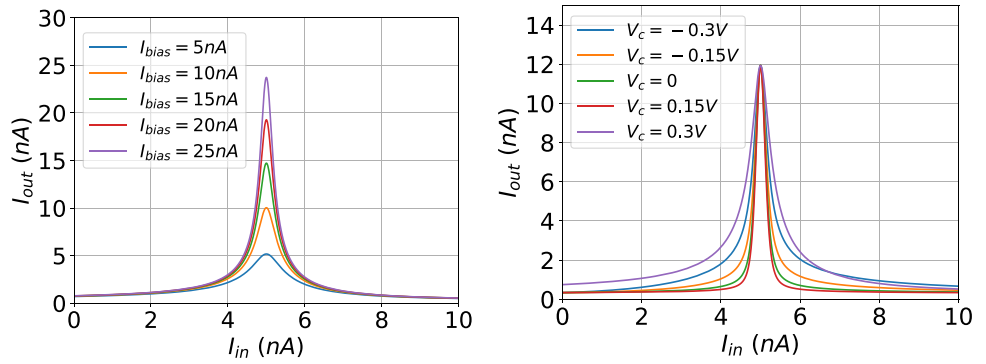


Table 1 MOS transistors’ dimensions (Fig. 1)

Differential block	W/L ($\mu\text{m}/\mu\text{m}$)	Current correlator	W/L ($\mu\text{m}/\mu\text{m}$)
M_{n1} – M_{n6}	0.4/1.6	M_{p1} – M_{p6}	0.4/1.6
M_{n7} – M_{n8}	0.4/1.6	–	–
M_{n9} – M_{n10}	0.8/1.6	–	–

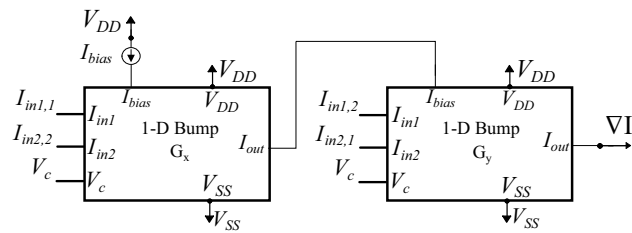


Fig. 3 A 2-D Bump circuit that implements the analog Robert’s Cross operator

In the literature, Winner-Take-All (WTA) circuits are used to implement the argmax operator [28]. In particular, a N -input N -output WTA circuit, is composed of N neurons, each one associated with one input and one output. If a given input I_{inj} , $j \leq N$, is larger than the rest, then the respective output I_{outj} has a high value, whereas the rest are zero. A 2-neurons Lazzaro WTA circuit example, shown in Fig. 4 can also be used as a simple threshold circuit, where its second input is the threshold value I_{th} . To counter the fact that in the analog implementation, edges have a low intensity value, whereas in the software implementation they have a high one, the overall output of the circuit is the output of the neuron with the I_{th} as its input. Therefore, this topology operates complementary to a threshold circuit. The analog implementation of the RCO with the threshold circuit is depicted in Fig. 5.

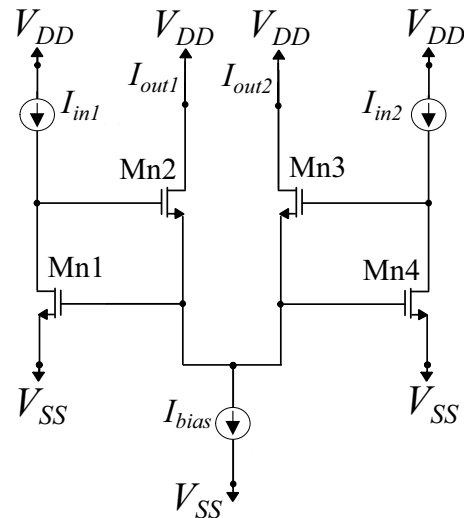


Fig. 4 A two neurons NMOS Lazzaro WTA circuit

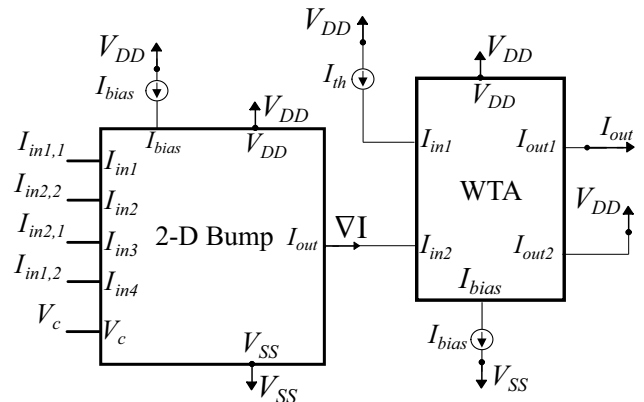
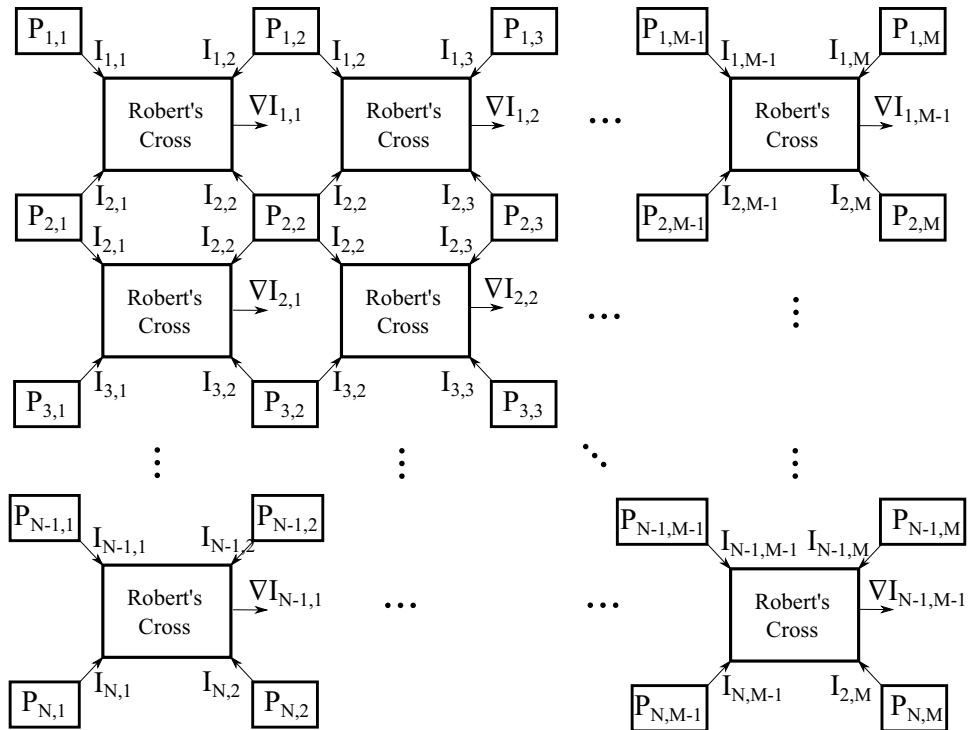


Fig. 5 The 2-D Bump circuit that implements the analog Robert’s Cross operator paired with a Winner-Take-All circuit that operates as a threshold circuit. I_{th} is the threshold current

Fig. 6 Conceptual system-level architecture, where multiple analog edge detector cells directly integrated on the photodiodes

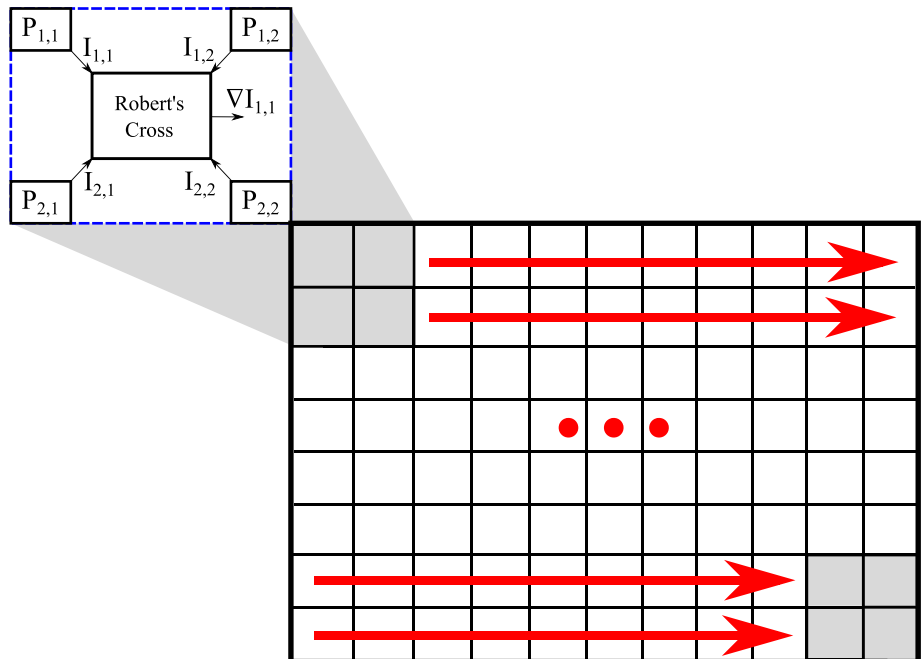


3.3 System-level architecture

The proposed circuitry can be used on multiple high-level architectures in order to regulate the trade-off between the area, power consumption and operation speed. The straightforward solution, also proposed in [11] and shown in Fig. 6, is to construct a $N \times M$ grid which is directly integrated on

the photodiodes. This approach is suitable for accelerator circuits since it offers very high operation speeds at the cost of increased chip area and power consumption. On the other hand, a more area and power efficient configuration (shown in Fig. 7), consists of a single RCO cell, which is sequentially shifted throughout to the entire image. This approach, requires significantly more computation time (proportionally

Fig. 7 Conceptual system-level architecture, where a single analog edge detector cell is shifted towards the entire image



to the size of the image) in comparison to the previous one, as well as memories and digital circuitry to synchronize the whole procedure.

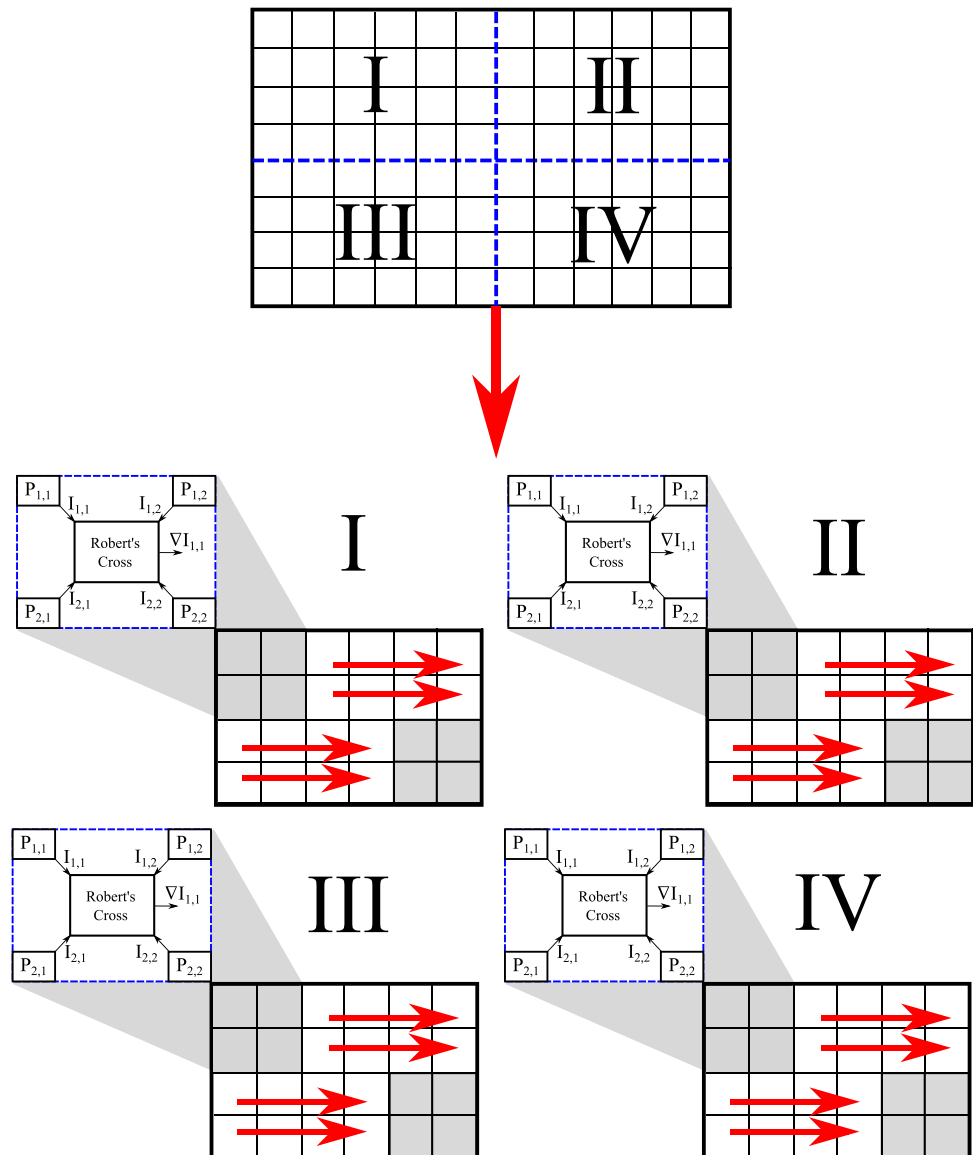
Unfortunately, both of the aforementioned approaches are inefficient for large images. Therefore, a middle ground, subsequently called the analog hardware-friendly implementation, that combines elements from both of them and can be adjusted in respect to the image's size, is adopted in this work. In particular, an image can be segmented into smaller parts in which a single RCO cell is used as explained in Fig. 7. Then the processed segments are connected to reform the original image. In this topology, the size of each segment acts as a hyper-parameter controlling the trade-off between efficiency and operation speed. However, a drawback of this approach is that additional digital circuitry for reconstructing

the original image is also required. An explanatory demonstration of this approach is depicted in Fig. 8.

4 Simulation results

In this section, a comparison between the analog hardware-friendly and software implementations of an RCO approximation in various different images is provided. The analog edge detector has been designed using the Cadence IC suite in a TSMC 90 nm CMOS process whereas the software implementation was evaluated using Python 3.7. All simulations presented are conducted on the layout, which is depicted in Fig. 9 (post-layout simulations). To avoid mismatches and manufacturing considerations, based on the common-centroid

Fig. 8 Proposed system-level architecture, where multiple analog edge detector cells are shifted along the entire image



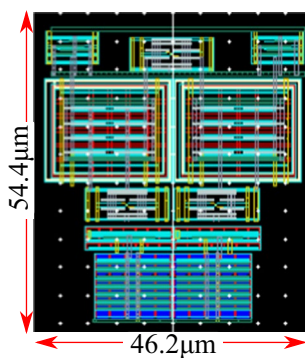


Fig. 9 Layout of the implemented RCO cell along with the WTA circuit

technique extra dummy transistors are used in the implementation of the layout [29].

In order to import the images in Cadence, the pixel values were normalized in the range [2, 6] nA. These currents are the inputs of the Bump circuit and therefore values lower than 2 nA may lead to misleading results. The bias currents for the multivariate Bump circuits and the WTA circuit were set as $I_{bias,b} = 4$ nA and $I_{bias,wta} = 6$ nA, respectively. These are the minimum recommended current values for the proper operation of the edge detector. The hyperparameters V_c and I_{th} directly affect the results of the edge detector. For the simulations in this section their values are set to $V_c = 0.3$ V and $I_{th} = 3$ nA.

In order to quantitatively evaluate the edge detector’s performance, three figures of merit, that are widely used in image assessment [30], have been applied. Assuming for a reference image \mathbf{X} and the produced image \mathbf{Y} . The SSIM is a perceptual metric which is calculated according to the following formula [31]:

$$SSIM(\mathbf{X}, \mathbf{Y}) = \frac{(2\mu_X\mu_Y + C_1)(2\sigma_{XY} + C_2)}{(\mu_X^2 + \mu_Y^2 + C_1)(\sigma_X^2 + \sigma_Y^2 + C_2)}, \quad (13)$$

where μ_X the average of \mathbf{X} (similarly for \mathbf{Y}), σ_X^2 the variance of \mathbf{X} (similarly for \mathbf{Y}) and σ_{XY} the covariance of \mathbf{X} and \mathbf{Y} . Furthermore, for the coefficients C_1 and C_2 we select $C_1 = (0.01L)^2$ and $C_2 = (0.03L)^2$, where L is the specified dynamic range value of the images ($L = 1$ in our case).

The PSNR is given by [32, 33]:

$$PSNR(\mathbf{X}, \mathbf{Y}) = 20 \log_{10} \left(\frac{\max\{\mathbf{X}\}}{\sqrt{MSE(\mathbf{X}, \mathbf{Y})}} \right), \quad (14)$$

where MSE is the mean squared error between the images \mathbf{X} and \mathbf{Y} and is given by [34]:

$$MSE(\mathbf{X}, \mathbf{Y}) = \frac{1}{NM} \sum_{i,j=1}^{N,M} |\mathbf{X}(i,j) - \mathbf{Y}(i,j)|^2, \quad (15)$$

for each pixel (i, j) of the denoted images. The Mean Absolute Percentage Error (MAPE), for each of the denoted images, is given as:

$$MAPE(\mathbf{X}, \mathbf{Y}) = \left(\frac{\sum_{i,j=1}^{N,M} |\mathbf{X}(i,j) - \mathbf{Y}(i,j)|}{\sum_{i,j=1}^{N,M} X_{ij}} \right) 100\%, \quad (16)$$

note that in (16) the mean value terms $\frac{1}{NM}$ cancel each other out.

To test the proposed edge detector a typical 512×512 image (see Fig. 10a) is used and the results are presented in Fig. 10b, c. The quality of the analog generated images can be assessed by a visual inspection in area with high edge concentration. Two representative examples are the face and the feather; in the former the analog implementation adequately captures the basic features of a human face but in the latter presents a generic depiction with lesser details. This is true for both the images with and without the threshold in Fig. 10b, c, respectively.

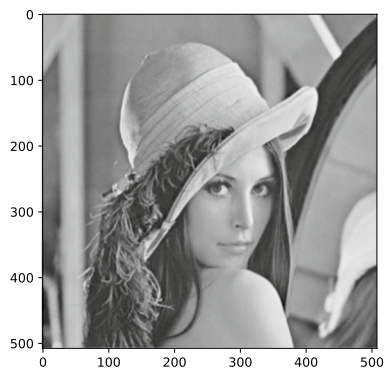
These results are also verified by observing the aforementioned metrics. In particular, the PSNR and the SSIM between the software and the analog generated images are equal to 28.4 dB and 0.85 (values over 0.9 indicate that the differences are not detectable by the human eye), respectively. It should be noted that the PSNR is calculated on the image without applying any threshold (see Fig. 10b), whereas the SSIM is computed on between the binary images (see Fig. 10c). To further (qualitatively) verify the performance of the proposed edge detector, the produced images for 2 additional reference images are provided. The results are presented in Fig. 11a, b and the PSNR and SSIM metrics for all images are summarized in Table 2.

The proposed edge detector is also tested in terms of circuit’s sensitivity behavior in PVT variations. Specifically, a Monte-Carlo analysis for $N = 200$ points is conducted on 4 random pixels that indicate an edge and on 4 random pixels that indicate a flat area. Both Monte-Carlo analysis histograms are shown in Fig. 12. Their mean values are $\mu_{edges} = 0.55$ nA, $\mu_{flat} = 2.66$ nA with standard deviation of $\sigma_{edges} = 0.28$ nA and $\sigma_{flat} = 0.20$ nA, respectively.

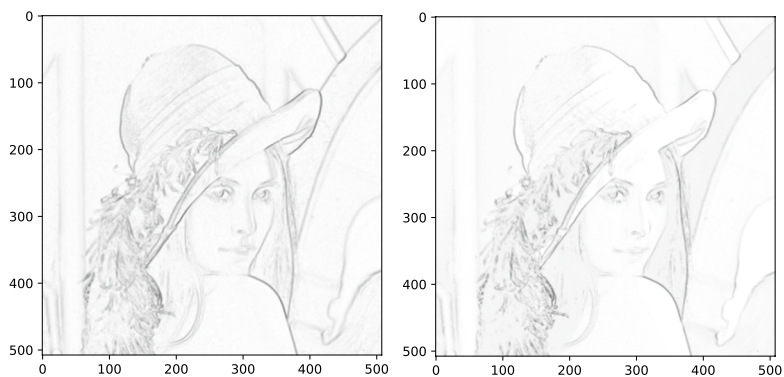
5 Performance summary and discussion

A performance summary in terms of circuit’s specifications for existing analog edge detectors is presented in Table 3. The aim of this work was to lower the detector’s power consumption. By observing Table 3 it is evident that the proposed work significantly outperforms the rest in terms

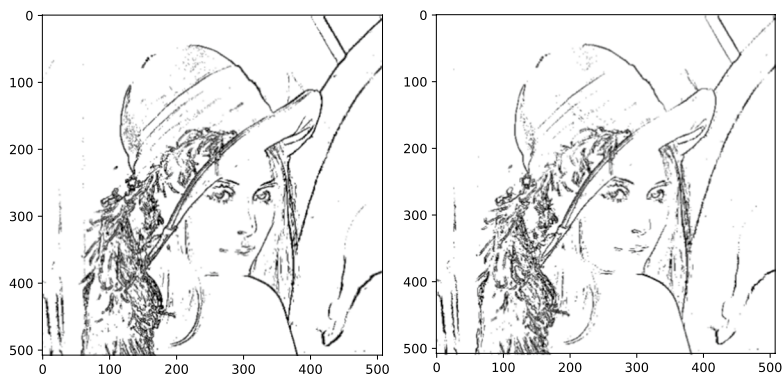
Fig. 10 Edge detection on an image of Lenna



(a) The original image.



(b) Left: Image provided by the software-based edge detector. Right: Image provided by the analog circuit-based edge detector.

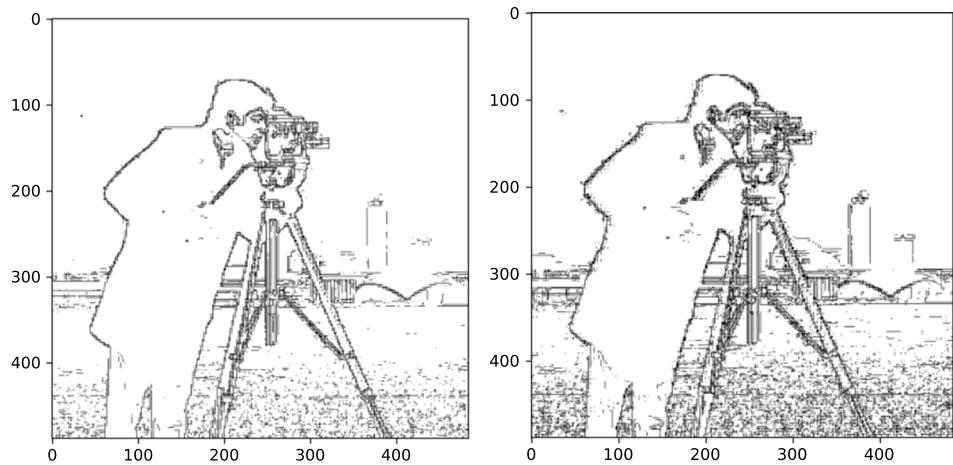


(c) Left: The binary edge detection image created by the software implementation. The threshold value is chosen arbitrarily as 0.13. Right: The binary edge detection image created by the analog circuit, for $I_{th} = 2$ nA.

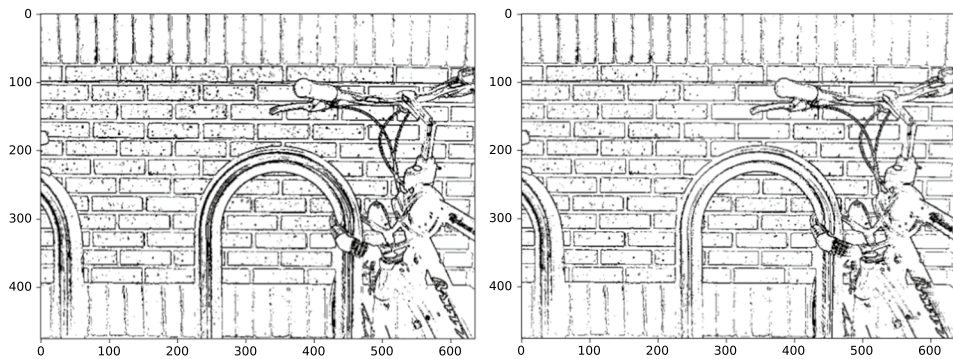
of power consumption per pixel. Additionally, the proposed circuit achieves the high computation speed, measured in frames per second (FPS), compared to the existing works. Nonetheless, this increased performance is area-expensive, since the proposed detector requires $2392\mu\text{m}^2$ per pixel, which is among the highest area per pixel values in Table 1.

The proposed analog edge detector targets smart sensor IoT devices that involve photodiodes. Its low power consumption and high quality results that match those of digital and software-based systems, make it suitable for high performance systems. For the incorporation of the analog edge detector in smart sensor system, except from the digital circuitry that synchronizes the shift of the RCO cells along

Fig. 11 Up: Edge detection on an image of a cameraman. Down: Edge detection on an image of a bike



(a) Left: The binary edge detection image created by the software implementation. The threshold value is chosen arbitrarily as 0.13. Right: The binary edge detection image created by the analog circuit, for $I_{th} = 2 \text{ nA}$.



(b) Left: The binary edge detection image created by the software implementation. The threshold value is chosen arbitrarily as 0.13. Right: The binary edge detection image created by the analog circuit, for $I_{th} = 2 \text{ nA}$.

Table 2 Performance summary for analog edge detectors

Image	Resolution	PSNR dB	SSIM	MAPE (%)
Lenna	512 × 512	28.4	0.85	2.65
Cameraman	480 × 640	26.3	0.78	3.86
Bike	490 × 484	28.4	0.82	2.51

the photodiode array, (see Fig. 8), additional components are also required. In particular, since the RCO suffers from noise distortion [19], a filtering circuit should be added between the photodiodes and the proposed edge detector. Furthermore, since the output of the circuit is in a binary format,

no analog-to-digital converters are needed. Nonetheless, a digital memory is necessary for the reconstruction of the image that indicates the edges after the RCO cells are shifted along the entire photodiode array.

6 Conclusion

An analog edge detector based on a hardware-friendly modification of the RCO was presented with the scope of increasing the performance of the detector, while maintaining a low power consumption. This is achieved by utilizing a low power, current mode Bump and a Lazzaro

Fig. 12 Left: Post-layout Monte-Carlo sensitivity analysis histogram for 4 random pixels that indicate an edge. Right: Post-layout Monte-Carlo sensitivity analysis histogram for 4 random pixels that indicate a flat area

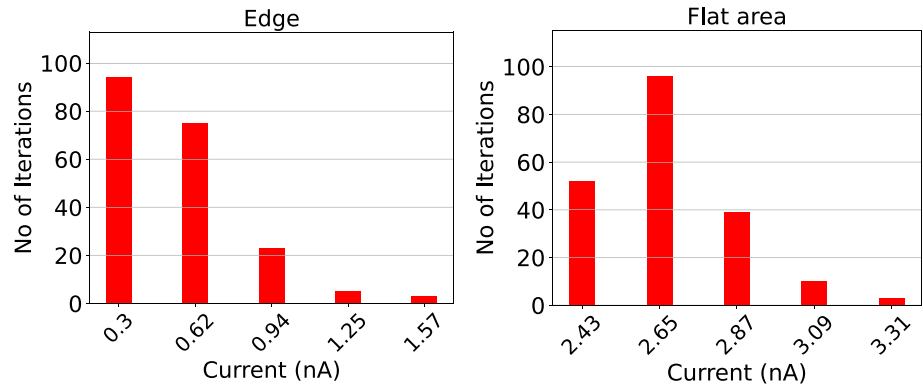


Table 3 Performance summary for analog edge detectors

Ref.	Technology	Supply voltage (V)	Power consumption per pixel	Area per pixel (μm^2)	FPS
This work	90 nm	0.6	33 nW	2392	100 K
[10]	0.5 μm	1.8	0.368 mW	8600	N/A
[11]	150 nm	1.8	790 μW	140	75
[14]	0.6 μm	1.8	3.6 μW	100	50
[12]	0.35 μm	3.3	26.8 μW	1125	2000
[15]	0.35 μm	3.3	5.8 μW	1125	N/A
[16]	250 nm	N/A	1.2 μW	633	N/A
[17]	180 nm	1.8	0.9 μW	225	1300

WTA circuit. A single RCO cell, composed of these building blocks, can receive 100 K inputs per second consuming only 33 nW. To evaluate the proposed architecture 3 medium resolution images were used. Post-layout simulation results suggest that the produced images achieve an average PSNR value of 27.7 db and an average SSIM of 0.81, indicating an excellent result.

Availability of data and materials Availability of data and materials: Data used in the experiments has been generated through publicly available simulators. Related simulation files have been shared through the links given in the paper in order to fully reproduce the presented results.

References

- Ishtiaq, A., Khan, MU., Ali, S., Habib, K., Samer, S., & Hafeez, E. (2021). A review of system on chip (soc) applications in internet of things (iot) and medical. In *ICAME21, international conference on advances in mechanical engineering*, Pakistan, pp. 1–10
- Miettinen, A. P., & Nurminen, J. K. (2010). Energy efficiency of mobile clients in cloud computing. In *2nd USENIX workshop on hot topics in cloud computing (HotCloud 10)*.
- Wang, A., Calhoun, B. H., & Chandrakasan, A. P. (2006). Sub-threshold design for ultra low-power systems, vol. 95. Springer.
- Nikolic, M., Tuba, E., & Tuba, M. (2016). Edge detection in medical ultrasound images using adjusted canny edge detection algorithm. In *2016 24th Telecommunications Forum (TELFOR)*, pp. 1–4. *IEEE*.
- Shin, M. C., Goldgof, D., & Bowyer, K. W. (1999). Comparison of edge detectors using an object recognition task. In *Proceedings. 1999 IEEE Computer Society Conference on Computer Vision and Pattern Recognition (Cat. No PR00149)*, vol. 1, pp. 360–365. *IEEE*.
- Zecca, R., Marks, D. L., & Smith, D. R. (2019). Symphotic design of an edge detector for autonomous navigation. *IEEE Access*, 7, 144836–144844.
- Zhai, L., Dong, S., & Ma, H. (2008). Recent methods and applications on image edge detection. In *2008 International workshop on education technology and training & 2008 international workshop on geoscience and remote sensing, vol. 1*, pp. 332–335. *IEEE*.
- Lakshmi, S., & Sankaranarayanan, D. V., et al. (2010). A study of edge detection techniques for segmentation computing approaches. *IJCA Special Issue on “Computer Aided Soft Computing Techniques for Imaging and Biomedical Applications” CASCT*, pp. 35–40.
- Dron, L. (1993). The multiscale veto model: A two-stage analog network for edge detection and image reconstruction. *International Journal of Computer Vision*, 11(1), 45–61.
- Gaspariano, L. A. S., Sánchez, A. D. Analog cmos morphological edge detector for gray-scale images.
- Soell, C., Shi, L., Roeber, J., Reichenbach, M., Weigel, R., & Hagelauer, A. (2016). Low-power analog smart camera sensor for edge detection. In *2016 IEEE international conference on image processing (ICIP)*, pp. 4408–4412. *IEEE*.
- Dubois, J., Ginjac, D., Paindavoine, M., & Heyrman, B. (2008). A 10,000 fps CMOS sensor with massively parallel image processing. *IEEE Journal of Solid-State Circuits*, 43(3), 706–717.
- Vincent, O. R., & Folorunso, O., et al. (2009) A descriptive algorithm for sobel image edge detection. In *Proceedings of informing science and IT Education Conference (InSITE)*, vol. 40, pp. 97–107.
- Njuguna, R., & Gruev, V. (2011). Low power programmable current mode computational imaging sensor. *IEEE Sensors Journal*, 12(4), 727–736.
- Massari, N., Gottardi, M., Gonzo, L., Stoppa, D., & Simoni, A. (2005). A CMOS image sensor with programmable pixel-level analog processing. *IEEE Transactions on Neural Networks*, 16(6), 1673–1684.
- Kim, J.-H., Kong, J.-S., Suh, S.-H., Lee, M., Shin, J.-K., Park, H. B., & Choi, C. A. (2005). A low power analog CMOS vision chip for edge detection using electronic switches. *ETRI Journal*, 27(5), 539–544.
- Nam, M., & Cho, K. (2018). Implementation of real-time image edge detector based on a bump circuit and active pixels in a CMOS image sensor. *Integration*, 60, 56–62.

18. Alimisis, V., Gennis, G., Dimas, C., & Sotiriadis, P. P. (2021). An analog Bayesian classifier implementation, for thyroid disease detection, based on a low-power, current-mode gaussian function circuit. In *2021 International conference on microelectronics (ICM)*, pp. 153–156 .IEEE.
19. Roberts, L. (1965). *Machine perception of 3-D solids, optical and electro-optical information processing*. MIT Press Cambridge, MA.
20. Davis, L. S. (1975). A survey of edge detection techniques. *Computer Graphics and Image Processing*, 4(3), 248–270.
21. Alimisis, V., Gourdouparis, M., Gennis, G., Dimas, C., & Sotiriadis, P. P. (2021). Analog gaussian function circuit: Architectures, operating principles and applications. *Electronics*, 10(20), 2530.
22. Lee, K., Park, J., & Yoo, H.-J. (2019). A low-power, mixed-mode neural network classifier for robust scene classification. *Journal of Semiconductor Technology and Science*, 19(1), 129–136.
23. Payvand, M., & Indiveri, G. (2019). Spike-based plasticity circuits for always-on on-line learning in neuromorphic systems. In *2019 IEEE international symposium on circuits and systems (ISCAS)*, pp. 1–5 .IEEE.
24. Ota, Y., & Wilamowski, B. M. (1995). Current-mode CMOS implementation of a fuzzy min-max network. In *World Congress of Neural Networks*, vol. 2, pp. 480–483.
25. Shylendra, A., Shukla, P., Mukhopadhyay, S., Bhunia, S., & Trivedi, A. R. (2020). Low power unsupervised anomaly detection by nonparametric modeling of sensor statistics. *IEEE Transactions on Very Large Scale Integration (VLSI) Systems* 28(8), 1833–1843.
26. Gourdouparis, M., Alimisis, V., Dimas, C., & Sotiriadis, P. P. (2021). An ultra-low power, ± 0.3 v supply, fully-tunable gaussian function circuit architecture for radial-basis functions analog hardware implementation. *AEU-International Journal of Electronics and Communications* 136, 153755.
27. Alimisis, V., Gourdouparis, M., Dimas, C., Sotiriadis, P.P. (2021). A 0.6 v, 3.3 nw, adjustable gaussian circuit for tunable kernel functions. In *2021 34th SBC/SBMicro/IEEE/ACM symposium on integrated circuits and systems design (SBCCI)*, pp. 1–6 . IEEE.
28. Lazzaro, J., Ryckebusch, S., Mahowald, M. A., & Mead, C. A. (1988). Winner-take-all networks of o (n) complexity. *Advances in neural information processing systems*, 1.
29. Sharma, A. K., Madhusudan, M., Burns, S. M., Mukherjee, P., Yaldiz, S., Harjani, R., & Sapatnekar, S. S. (2021). Common-centroid layouts for analog circuits: Advantages and limitations. In *2021 Design, automation & test in Europe Conference & Exhibition (DATE)*, pp. 1224–1229 . IEEE.
30. Sara, U., Akter, M., & Uddin, M. S. (2019). Image quality assessment through FSIM, SSIM, MSE and PSNR: A comparative study. *Journal of Computer and Communications*, 7(3), 8–18.
31. Rehman, A., & Wang, Z. (2012). Reduced-reference image quality assessment by structural similarity estimation. *IEEE Transactions on Image Processing*, 21(8), 3378–3389.
32. Huynh-Thu, Q., & Ghanbari, M. (2008). Scope of validity of PSNR in image/video quality assessment. *Electronics Letters*, 44(13), 800–801.
33. Poobathy, D., & Chezian, R. M. (2014). Edge detection operators: Peak signal to noise ratio based comparison. *IJ Image, Graphics and Signal Processing*, 10, 55–61.
34. Allen, D. M. (1971). Mean square error of prediction as a criterion for selecting variables. *Technometrics*, 13(3), 469–475.

Publisher's Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Springer Nature or its licensor holds exclusive rights to this article under a publishing agreement with the author(s) or other rightsholder(s);

author self-archiving of the accepted manuscript version of this article is solely governed by the terms of such publishing agreement and applicable law.



artificial intelligence and machine learning. He is an IEEE Student member. He has received the Best Paper Award in the IEEE Int. Conf. on Microelectronics 2021.



His main research interests include analog microelectronic circuits, low power electronics, analog computing and integrated circuit architectures with applications in artificial intelligence and machine learning. He has received the Best Paper Award in the IEEE Int. Conf. on Microelectronics 2020, the Best Paper Award in the IEEE Int. Conf. on Microelectronics 2021 and the Best Paper Award in IEEE Symposium on Integrated Circuits and Systems Design (SBCCI) 2021. He is a regular reviewer for many journals and conferences and an IEEE student member.



Georgios Gennis is a Senior Graduate Student in Electrical and Computer Engineering Department at the National Technical University of Athens, Greece. Currently, he is pursuing his Diploma Thesis, under the supervision of Prof. Paul P. Sotiriadis. He has authored and co-authored several conference papers and a journal article. His main research interests include analog microelectronic circuits, low power electronics, analog computing and integrated circuit architectures with applications in

Vassilis Alimisis received the B.Sc. in Physics (top 1%) and the M.Sc. degree in Electronics and Communications from the University of Patras, Greece, in 2017 and 2019 respectively. Currently, he is pursuing Ph.D. degree at the National Technical University of Athens, Greece, under the supervision of Professor Paul P. Sotiriadis. He is a Teaching Assistant in undergraduate and graduate courses and supervises diploma theses. He has authored and co-authored several conference papers and journal articles.

Christos Dimas received the diploma degree in Electrical and Computer Engineering from the National Technical University of Athens, Greece, in 2016, his Ph.D. degree from the National Technical University of Athens, Greece, in 2022, and is currently a post-doc researcher at the same department, under the supervision of Prof. Paul P. Sotiriadis. His PhD thesis research subject is “Image Reconstruction Approaches and Circuit Modeling in Electrical Impedance

Tomography". He is a Teaching Assistant in undergraduate and graduate courses and supervises diploma theses. His main research includes electrical impedance tomography, bio-impedance measurement, modeling and instrumentation. He has authored and co-authored several conference papers and journal articles. He has received the Best Paper Award in the IEEE Int. Conf. on Microelectronics 2020, the Best Paper Award in the IEEE Int. Conf. on Microelectronics 2021 and the Best Paper Award in IEEE Symposium on Integrated Circuits and Systems Design (SBCCI) 2021. He is a regular reviewer for many journals and conferences and an IEEE student member.



Paul Peter Sotiriadis (SM'18) is a Professor of Electrical and Computer Engineering of the National Technical University of Athens, Greece, the Director of the Electronics Laboratory of the University and a governing board member of the Hellenic Space Center, the National space center of Greece. He runs a team of 30 researchers. He received the Diploma degree in Electrical and Computer Engineering from same University, the M.S. degree in Electrical Engineering from Stanford University, USA and

the Ph.D. degree in Electrical Engineering and Computer Science from the Massachusetts Institute of Technology, USA, in 2002. In 2002, he joined the faculty of the Johns Hopkins University Electrical and Computer Engineering Department and in 2012 he joined the faculty of the Electrical and Computer Engineering Department of the National Technical University of Athens. He has authored and coauthored more than 160 research publications, holds one patent, and has contributed several chapters to technical books. His research interests include the design, optimization, and mathematical modeling of analog, mixed-signal, RF and microwave integrated and discrete circuits, sensors and instrumentation architectures, biomedical instrumentation, interconnect networks and advanced frequency synthesis. He has led several projects in these fields funded by U.S. organizations and has collaborations with industry and national labs. He has received several awards, including the 2012 Guillemin-Cauer Award from the IEEE Circuits and Systems Society, a Best Paper Award in the IEEE International Symposium on Circuits and Systems 2007, a Best Paper Award in the IEEE Int. Frequency Control Symposium 2012, a Best Paper Award in the IEEE Int. Conf. on Modern Circuits and Systems Tech. 2019, a Best Paper Award in the IEEE Int. Conf. on Microelectronics 2020, a Best Paper Award in the IEEE Int. Conf. on Microelectronics 2021 and a Best Paper Award in IEEE Symposium on Integrated Circuits and Systems Design (SBCCI) 2021. Dr. Sotiriadis is an Associate Editor of the IEEE Sensors Journal, has served as an Associate Editor of the IEEE Trans. on Circuits and Systems - I (2016-2020) and the IEEE Trans. on Circuits and Systems - II (2005-2010) and has been a member of technical committees of many conferences. He regularly reviews for many journals and conferences and serves on proposal review panels.