

Missing value imputation: a review and analysis of the literature (2006–2017)

Wei‑Chao Lin1,2,3 · Chih‑Fong Tsai4

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Abstract

Missing value imputation (MVI) has been studied for several decades being the basic solution method for incomplete dataset problems, specifcally those where some data samples contain one or more missing attribute values. This paper aims at reviewing and analyzing related studies carried out in recent decades, from the experimental design perspective. Altogether, 111 journal papers published from 2006 to 2017 are reviewed and analyzed. In addition, several technical issues encountered during the MVI process are addressed, such as the choice of datasets, missing rates and missingness mechanisms, and the MVI techniques and evaluation metrics employed, are discussed. The results of analysis of these issues allow limitations in the existing body of literature to be identifed based upon which some directions for future research can be gleaned.

Keywords Missing values · Imputation · Supervised learning · Incomplete dataset · Data mining

1 Introduction

Data mining or big data analysis has been recognized as an important and challenging task for many problems in daily life. To perform big data analysis or data mining, a specifc dataset for a chosen target problem is collected. However, in practice, the collected dataset usually contains some proportion of incomplete data that have one or more missing attribute values. There are many reasons for incompleteness in datasets, arising from a variety of sources, the database system per se, the network, improper, mistaken data entries, and so on.

According to Strike et al. ([2001\)](#page-21-0) and Raymond and Roberts [\(1987](#page-20-0)), when the dataset contains a very small amount of missing data, e.g. the missing rate is less than 10% or 15%

 \boxtimes Chih-Fong Tsai cftsai@mgt.ncu.edu.tw

¹ Department of Information Management, Chang Gung University, Taoyuan, Taiwan

² Healthy Aging Research Center, Chang Gung University, Taoyuan, Taiwan

³ Department of Thoracic Surgery, Chang Gung Memorial Hospital, Linkou, Taiwan

⁴ Department of Information Management, National Central University, Zhongli, Taoyuan, Taiwan

for the whole dataset, the missing data can simply be removed from the dataset without having a significant effect on the final mining or analysis result. However, when the missing rate exceeds 15%, careful consideration needs to be given to dealing with these missing data (Acuna and Rodriguez [2004](#page-17-0)). It should be noted that this does not mean that every domain problem dataset follows this kind of rule. Often small amounts of missing data may contain important information that cannot be ignored, such as the records containing very high amount of money spent by some consumers but some of their personal information is missing, e.g. age, income, education, etc.

Unlike the case deletion strategy, missing value imputation (MVI) is the solution method most commonly used to deal with the incomplete dataset problem. In general, MVI is a process in which some statistical or machine learning techniques are used to replace the missing data with substituted values. Statistical techniques, such as mean/mode and regression, have been applied for this purpose, for several decades (Little and Rubin [1987](#page-20-1)), with machine learning techniques, such as the k nearest neighbor, artifcial neural network, and support vector machine techniques being employed in the last 10 years (Garcia-Lae– ncina et al. [2010](#page-19-0)).

There is variety of MVI techniques suitable for application to different domain problems. A large number of surveys of MVI from diferent perspectives have already appeared in the literature, such as for operation management (Tsikriktsis [2005\)](#page-21-1), medical problems (Aittokallio [2009](#page-18-0); Donders et al. [2006;](#page-18-1) Harel and Zhou [2007;](#page-19-1) Liew et al. [2011](#page-20-2)), pattern classifcation (Garcia-Laencina et al. [2010](#page-19-0)), and questionnaires and surveys (Baraldi and Enders [2010;](#page-18-2) De Leeuw [2001](#page-18-3)).

Most of these surveys have mainly focused on describing the basic concepts of the rel evant MVI techniques. However, from the experimental design procedure viewpoint, there are many technical issues that have not been adequately reviewed and analyzed. For example, it is not known which technique(s) are the most widely used, what kinds of domain problem datasets have been studied, how many dataset missing rates are considered in the simulations, and so on.

Therefore, unlike previous surveys, this survey provides statistical analyses of technical questions related the experimental design procedure. Specifcally, 111 journal papers published over the past decade, from 2006 to 2017, are reviewed and analyzed. In addition, some limitations of related works are also discussed for indication of possible future research directions.

The rest of this paper is organized as follows. Section [2](#page-1-0) describes the commonly used experimental design procedure for MVI. The related literature for each of the major components of the procedure is analyzed, with Sects. [3](#page-2-0), [4](#page-5-0), and [5](#page-11-0) focused on the datasets used, as well as the related information including missing rates and missingness mechanisms, MVI techniques, and evaluation metrics, respectively. Section [6](#page-15-0) discusses the limitations of related work and Sect. [7](#page-17-1) offers some conclusions.

2 The experimental design procedure for missing value imputation

There are three technical issues that need to be considered in the experimental design pro-cedure for MVI outlined in Fig. [1](#page-2-1). The first one is the chosen datasets for related experiments. The experimental dataset may contain a number of missing data or it may be a complete dataset. For complete datasets, a missing value simulation is performed. That is, the chosen dataset is simulated with different missing rates (e.g., 10% or 20%) using three

Fig. 1 The experimental design procedure for MVI

diferent missingness mechanisms: missing completely at random (MCAR), missing at random (MAN), and missing not at random (MNAR). This results in different incomplete datasets having diferent proportions of missing data.

The second technical issue is the techniques used for missing value imputation. Dur– ing the imputation process, each incomplete dataset can be divided into a set of complete data and a set of missing data. The former is used for the 'estimation' of suitable values by diferent imputation methods to replace the missing values in the set of missing data. Consequently, this produces a 'pseudo' complete dataset for later data mining or analysis tasks, if any.

The third technical issue is performance evaluation of imputation results. The most straightforward method to evaluate the performance of the imputation method is to assess the diferences between the real values in the original dataset and the estimated values in the 'pseudo' dataset. Another method involves using the 'pseudo' dataset to perform some data mining task, such as classifcation or clustering, then observing the fnal mining performance.

According to the three technical issues, related literatures are reviewed and analyzed by their experimental datasets collected, MVI techniques used, and performance evaluation methods considered, which are discussed in Sects. [3,](#page-2-0) [4](#page-5-0), and [5,](#page-11-0) respectively.

3 Analysis of experimental datasets

3.1 Dataset domains

Table [1](#page-3-0) shows the number of works using each type of dataset from the 111 related studies. As can be seen, most researchers use the UCI (University of California at Irvine) data-sets^{[1](#page-2-2)} for their experiments. Often, several UCI datasets are used in each study, which can include a variety of domain problems. In contrast, medical related datasets, such as micro array or gene datasets, are the most widely considered domain problem in MVI. Other domain problems considered less often include image data, software measurement and project, fnancial data, questionnaire based data.

The results indicate that in most MVI studies, more than one specifc domain problem is considered. The advantage of doing this is to prove the domain scalability of the MVI

¹ <http://archive.ics.uci.edu/ml/>.

	UCI	Medical	Images	Software	Financial	Questionnaire	KDD ^a	Other
2017	5	3	0					
2016	3							
2015								
2014	3							
2013	5							
2012	5							
2011	6							
2010	3							
2009	3		0					
2008	3	4						
2007	4		0					
2006	\overline{c}							
Total	48	34						12

Table 1 The numbers of works using diferent domain datasets

a <http://www.kdd.org/kdd-cup>

method used. However, further analysis of the dataset characteristics, including the number of features (i.e., attributes) and data samples, allows some limitations of past work to be identifed. One major limitation is the problem of dataset size. That is, most studies use small scale UCI datasets that contain small numbers of features and/or data samples, with the number of features ranging from 4 to 89 and the usual number of data samples rang– ing from several hundred to thousands. Some exceptions are Folino and Pisani ([2016\)](#page-18-4) and Farhangfar et al. ([2007\)](#page-18-5), who used very large scale datasets containing a very high number of feature dimensions, i.e., 216, and a very large amount of data samples, i.e., 581,012 and 256,000, respectively.

Another limitation of past studies is that although there are three different types of fea– tures, categorical, numerical, and mixed types, very few have analyzed differences in performance of MVI methods between different feature types. There are, however, two exceptions to this, namely, Tsai and Chang ([2016\)](#page-21-2) and Stekhoven and Buhlmann ([2012\)](#page-21-3).

3.2 Missing rates

In general, most studies have examined imputation performance by performing diferent missing value simulations over a chosen dataset using diferent missing rates. Some have considered very small missing rates, e.g., less than 30%, while others have focused on large ranges of missing rates, such as from 5 to 80%. Figure [2](#page-4-0) shows the number of works that consider missing rates that are less than 30%, between 30 and 50%, and greater than 50%.

As we can see from the fgure, most studies discuss missing rates that are less than 30% with only twelve works considering missing rates that are larger than 50%. Of the studies using very large missing rates, seven of them used the UCI datasets (Eirola et al. [2013](#page-18-6); Kapelner and Bleich [2015;](#page-19-2) Kiasari et al. [2017](#page-19-3); Mesquite et al. [2017](#page-20-3); Purwar and Singh [2015;](#page-20-4) Qin et al. [2009](#page-20-5); Zhu et al. [2011](#page-22-0)), one the Digital Bibliographic Library Browser

Fig. 2 Number of works using missing rates that are less than 30%, between 30 and 50%, and greater than 50%

(DBLP) dataset² (Li et al. [2014](#page-20-6)), one the wireless sensor network dataset (Li and Parker 2014), one the medical dataset (Janssen et al. 2010), one the traffic flow dataset (Chen et al. [2017\)](#page-18-7), and one a synthetic dataset (Graham et al. [2007\)](#page-19-5).

In short, most of the datasets which have been used are relatively small, containing several hundreds to thousands of data samples, in contrast to the DBLP and wireless sensor networks datasets which contain 10,000 and 12,000 data samples, respectively.

3.3 Missingness mechanisms

According to Little and Rubin ([1987\)](#page-20-1), there are three types of missingness mechanisms that can cause an incomplete dataset. They are missing completely at random (MCAR), missing at random (MAR), and not missing at random (NMAR). MCAR occurs when the probability of an instance (case) having a missing value for an attribute does not depend on either the known values or the missing data.

On the other hand, MAR occurs when the probability of an instance having a missing value for an attribute may depend on the value of that attribute. In other words, when the distribution of an instance having missing values for an attribute depends on the observed data, but does not depend on the missing data. NMAR occurs when the probability of an instance having a missing value for an attribute may depend on the value of that attribute.

Therefore, there are three diferent ways to artifcially simulate a collected dataset as an incomplete dataset containing a controlled missing rate. Figure [3](#page-5-1) shows the number of works detailing simulations of the three types of missingness mechanisms.

The results show that most researchers have only used the MCAR mechanism for their experiments. Very few (i.e., 15 works) have considered all three mechanisms for each chosen dataset. Specifcally, seven have used the UCI datasets (Garciarena and Santana [2017](#page-19-6); Kapelner and Bleich [2015;](#page-19-2) Pan et al. [2015;](#page-20-8) Tian et al. [2014;](#page-21-4) Twala [2009](#page-21-5); Twala et al. [2008;](#page-21-6) Valdiviezo and Van Aelst [2015;](#page-21-7) Xia et al. [2017](#page-21-8); Zhu et al. [2012\)](#page-22-1), three the software meas‑ urement/project datasets (Khoshgoftaar and Van Hulse [2008;](#page-19-7) Song et al. [2008](#page-21-9); Van Hulse

² <http://dblp.uni-trier.de/db/index.html>.

Fig. 3 Number of works discussing the diferent missingness mechanisms

and Khoshgoftaar [2014\)](#page-21-10), one for the medical dataset (Armitage et al. 2015), and two syn-thetic datasets (Ding and Simonoff [2010](#page-18-9); Hapfelmeier and Ulm [2014\)](#page-19-8).

4 Missing value imputation techniques

In general, missing value imputation techniques can be classifed into two types, namely, statistical and machine learning based techniques (Aittokallio [2009;](#page-18-0) Garcia-Laencina et al. [2010\)](#page-19-0). Related studies have considered some of these techniques as the basis for relevant experiments regardless of whether the work focuses on proposing a novel imputation technique or on comparing some chosen imputation techniques for specifc domain problems.

The following subsections describe the analysis related to the questions as to what kinds of baseline techniques have been used for MVI and which is the most popular. Note that describing the concepts of these statistical and machine learning based techniques is not the main focus of this paper.

4.1 Statistical techniques

Table [2](#page-6-0) lists the statistical techniques that have been used in studies published from 2006 to 2017. As we can see, expectation management (EM), linear regression (LR), least squares (LS), and mean/mode are the top four most widely used statistical techniques, having been applied in 23, 15, 33, and 28 works respectively.

Among these top four statistical techniques, the mean and mode methods are the sim plest imputation methods for imputing numerical and categorical attribute values, respectively. In the mean approach, missing attributes are flled in by the average value of that attribute in all the observed data. On the other hand, the mode approach uses the attribute value in all the observed data that appears most often to fll in the missing attribute values.

In the EM algorithm, it consists of two steps where the E-step calculates the expectation of the complete data sufficient statistics given the observed data and current parameter estimates, and the M-step updates the parameter estimates through the maximum likelihood approach based on the current values of the complete sufficient statistics. The EM

Table 2 (continued)

algorithm then proceeds in an iterative manner until the diference between the last two consecutive parameter estimates converges to a specifed criterion. According to the fnal parameter estimates and the observed data, the expectation of each missing value can be calculated, which will be used as the imputation value.

For regression based imputation methods, the relationships among attributes are estimated, and then the regression coefficients are used to estimate the missing attribute values.

Fig. 4 The year-wise distribution of the number of works using the EM, LR, LS, and mean/mode techniques

Particularly, linear regression and logistic regression are used for the prediction of numeri– cal and categorical attribute values, respectively. In general, the method of least squares (LS) (or ordinary least squares) is used in linear regression to produce the fnal estimation by minimizing the measured and predicted values of the attributes.

More specifcally, for the category of least squares (LS), various estimation techniques can be used to replace ordinary least squares (OLS) to produce the fnal prediction result, such as ILLS, LTS, LSA, LLS, NIPALS, OLS, PLS, and SLLS.

Figure [4](#page-8-0) shows the year-wise distribution of works applying the top four statistical techniques. Although LS is the most widely used MVI technique, there has had been no related work considering this technique within the last 3 years, except for Pati and Das ([2017\)](#page-20-17). Instead, researchers have tended to prefer the EM, LR, and mean/mode techniques. Of these, the mean/mode technique is the second mostly widely used, having been used in publications appearing each year from 2006 and 2017. This survey indicates that the mean/ mode technique should be regarded as one of the representative baseline statistical MVI techniques.

Regarding the researches using one of the top four statistical MVI techniques, we can further analyze the relationships between these techniques and their experimental datasets, which are shown in Table [3](#page-9-0).

As we can see that the major statistical MVI technique for medical domain datasets is LS. This indicates that most medical domain datasets contain the numerical data type of missing values. Moreover, these medical domain datasets are usually simulated with the missing rates that are smaller than 30%, and related studies using the LS techniques only consider the MCAR and MAR missingness mechanism. On other hand, EM, LR, and mean/mode are the widely used statistical MVI techniques for UCI datasets where the simulated missing rates mostly range from 30 to 50%.

4.2 Machine learning based techniques

Table [4](#page-10-0) lists the machine learning based techniques that have been applied in the literature from 2006 to 2017. The top four techniques are clustering, DT, KNN and RF, which have been used in 14, 17, 52, and 9 related works, respectively.

Among the top four machine learning based techniques, cluster analysis is only the unsupervised learning technique whose task is to group a set of similar objects into the

the relationships between the top four statistical MVI techniques

same clusters. Specifcally, each cluster center (or centroid) is the mean of the objects in the same cluster. To impute the missing values, the distance between incomplete data and the identifed cluster centroids is calculated where the closest centroid's values are used to fll in missing values.

On the other hand, KNN is one representative supervised learning (classifcation) technique where missing values are imputed using the values calculated from the *k* near‑ est observed data. In particular, the nearest neighbors can be identified by some specifc distance function, usually the Euclidean distance. For missing value imputation, the missing data is used as the testing case, in which the complete and missing attributes represent the input features and output class label (or prediction), respectively. Next, its *k* nearest observed data using the complete attributes can be identifed whose class label is used to impute the missing attribute.

In DT, it is a tree-like model that each internal node denotes a test of an attribute and each branch represents an outcome of the test. The leaf nodes represent classes or class distributions. The upper-most node in a tree is the root node with the highest entropy. In the tree-growing process, the attribute having the highest information gain is chosen to split the node into child nodes. In related literatures, C4.5/5.0 and CART are used for imputing categorical and numerical attribute values, respectively.

About RF, multiple decision trees are constructed based on the bootstrapping pro– cedure and the fnal predictions are given by averaged values or majority votes of each tree's prediction. The imputation process by DT and RF is similar to KNN where the internal and leaf nodes represent the input features and output class label, respectively.

Figure [5](#page-11-1) shows the year-wise distribution for the number of works that have used the top four machine learning based techniques. KNN is no doubt the most popular MVI technique in this category, and can be regarded as the most representative base– line machine learning based MVI technique. On the other hand, the clustering and RF

Techniques	Works			
Artificial neural networks (ANN)	Aydilek and Arslan (2012), Gautam and Ravi (2015), Nishanth and Ravi (2016) and Shao et al. (2017)			
Association rule (AR)	Li et al. (2014)			
Collateral missing value estimation (CMVE)	Sehgal et al. (2008, 2009)			
Clustering	<i>Fuzzy c-means (FCM)</i> : Aydilek and Arslan (2013), Di Nuovo (2011), Li et al. (2010), Somasundaram and Nedunchezhian (2011), Tian et al. (2014) and Zhang et al. (2015)			
	<i>Fuzzy k-means (FKM)</i> : Luengo et al. (2012) and Pan et al. (2015)			
	<i>Hierarchical clustering (HC)</i> : Celton et al. (2010)			
	<i>K-means (KM)</i> : Eirola et al. (2013) , Kang (2013) , Luengo et al. (2012) and Somasundaram and Nedunchezhian (2011)			
	Self-organizing map (SOM): Garcia-Laencina et al. (2013), Jerez et al. (2010), Merlin et al. (2010) and Somasundaram and Nedunchezhian (2011)			
Decision tree (DT)	Classification and regression tree (CART): Burgette and Reiter (2014) , Ding and Simonoff (2010) , Doove et al. (2014) , Ghanad- Rezaie et al. (2010), Hapfelmeier et al. (2012), Iacus and Porro (2007) and Purwar and Singh (2015)			
	$C4.5$: Ding and Simonoff (2010), Fortes et al. (2006), Hruschka et al. (2007), Nishanth and Ravi (2016), Saar-Tsechansky and Provost (2007), Twala (2009) and Twala et al. (2008)			
Extreme learning machine	Shao et al. (2017)			
Genetic algorithm (GA)	Garcia et al. (2011)			
K-nearest neighbor (KNN)	KNN: Armitage et al. (2015) , Bras and Menezes (2007) , Brock et al. (2008) , Celton et al. (2010) , Chiu et al. (2013) , De Souto et al. (2015) , Ding and Ross (2012) , Doquire and Verleysen (2012) , Farhangfar et al. (2008), Eirola et al. (2014), Gan et al. (2006), Garcia-Laencina et al. (2009, 2013), Hron et al. (2010), Hu et al. (2006) , Huang et al. $(2016, 2017)$, Iacus and Porro (2007) , Jerez et al. (2010) , Kang (2013) , Khoshgoftaar, and Van Hulse (2008) , Li and Parker (2014) , Liu et al. (2010) , Luengo et al. (2012) , Nishanth and Ravi (2016), Oh et al. (2011), Pan et al. (2015), Pati and Das (2017), Paul et al. (2017), Rao et al. (2013), Sehgal et al. (2008, 2009), Stekhoven and Buhlmann (2012), Song et al. (2008), Sun et al. (2009), Tian et al. (2014), Tsai and Chang (2016), Tuikkala et al. (2008), Valdiviezo and Van Aelst (2015), Van Hulse and Kho- shgoftaar (2014), Wang et al. (2006), Xia et al. (2017), Yu et al. (2011), Zhang (2008, 2011, 2012), Zhang et al. (2008, 2011, 2015) and Zhu et al. (2011)			
	Grey based KNN: Zhang (2012) and Zhu et al. (2012)			
	<i>Iterative KNN</i> : Bras and Menezes (2007), Chiu et al. (2013), Hu et al. (2006) and Pati and Das (2017)			
	Sequential KNN: Bras and Menezes (2007), Chiu et al. (2013) and Pati and Das (2017)			
	Weighted KNN: Luengo et al. (2012) and Shao et al. (2017)			
Kernel-based imputation	Zhu et al. (2011)			
Multilayer perceptron (MLP)	Garcia-Laencina et al. (2013), Gautam and Ravi (2015), Jerez et al. (2010) , Nishanth et al. (2012) and Silva-Ramirez et al. (2011) , 2015)			

Table 4 The machine learning based techniques used in the literature

Techniques	Works
Random forest (RF)	Doove et al. (2014), Hapfelmeier and Ulm (2014), Hapfelmeier et al. (2012) , Iacus and Porro (2007) , Kapelner and Bleich (2015) , Nishanth and Ravi (2016), Purwar and Singh (2015), Shah et al. (2014) , Valdiviezo and Van Aelst (2015) and Xia et al. (2017)
Rough set theory (RST)	Clark et al. (2014)
Support vector machine/regression (SVM/SVR)	Aydilek and Arslan (2013) , Iacus and Porro (2007) , Luengo et al. (2012) , Tuikkala et al. (2008) and Wang et al. (2006)

Table 4 (continued)

Fig. 5 The year-wise distribution for the number of works that have used the DT, clustering, KNN, and RF techniques

techniques have recently been utilized in a number of studies, whereas DT has been consistently used each year from 2006 and 2016.

According to the researches using one of the top four machine learning based MVI techniques, Table [5](#page-12-0) shows the relationships between these techniques and their experimental datasets.

Regarding Table [5](#page-12-0), KNN is the most widely used machine learning based MVI technique, especially for UCI and medical datasets. However, for the questionnaire datasets, related studies have never considered machine learning based MVI techniques before. On other hand, for the missing rates, if we count the number of works by DT and RF (an ensemble of DTs) together, very few studies simulated with the missing rates that are smaller than 30% (i.e. 3 out of 22) whereas 13 and 6 works consider the 30–50% and larger than 50% missing rates, respectively. This is diferent from clustering and KNN that most studies simulated with the missing rates that are smaller than 30% (i.e. 10 out of 16 and 34 out of 60, respectively).

5 Evaluation methods

5.1 Direct evaluation

The fnal step after imputation of the missing values is to evaluate the imputation results. The most commonly used method is to directly assess the diference between the original

values in the collected dataset and the estimated or predicted values in the simulated incomplete dataset. There are two types of attribute values, namely, discrete and continuous. For evaluation of results of the imputation of discrete values, the percentage of values that have been predicted correctly (or incorrectly) for the missing values is usually used, e.g. Nishanth and Ravi [\(2016](#page-20-14)) and Valdiviezo and Van Aelst [\(2015](#page-21-7)). The percentage of correct predictions (PCP) can be obtained by

$$
PCP = 100 \times \frac{number\ of\ correct\ predictions}{total\ number\ of\ predictions}
$$
 (1)

On the other hand, for the imputation of continuous values, the mean absolute percent– age error (MAPE) and/or root-mean-square error (RMSE) related measures are used. Gau tam and Ravi ([2015\)](#page-19-23) and Silva-Ramirez et al. [\(2015](#page-21-13)). MAPE and RMSE can be computed by Eqs. (2) (2) (2) and (3) , respectively.

$$
MAPE = \frac{100}{n} \sum_{i=1}^{n} \left| \frac{x_i - \hat{x}_i}{x_i} \right| \tag{2}
$$

$$
RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_i - \hat{x}_i)^2}
$$
 (3)

where x_i is the actual value, \hat{x}_i is the predicted value and *n* is the total number of missing value.

5.2 Classifcation accuracy

Another strategy for assessing the imputation quality is to examine the classifcation per‑ formance of some chosen classifers trained by the imputed datasets. Diferent from the direct evaluation strategy, after the imputation process is completed, the imputed dataset

Fig. 6 The number of works using the diferent evaluation methods

without missing values is used to train some specific classifier(s), and another testing set is chosen to test their classifcation performance. Since using diferent imputation methods for the same incomplete datasets is likely to produce different imputation results, the classifer with higher classifcation accuracy is indicated by the better imputation quality of its training and datasets. Consequently, the better imputation methods can be identifed.

The proportion of related works that utilize this type of evaluation strategy is much smaller than the number utilizing the direct evaluation strategy. Moreover, studies which consider both evaluation strategies at the same time are even rarer. Figure [6](#page-13-0) shows the number of works using these evaluation methods and Table [6](#page-13-1) lists the related works that consider the classifcation accuracy of classifers and two evaluation methods at the same time. As we can see that very few studies consider both evaluation methods at the same time.

Ten diferent classifcation techniques have been employed in related works for analysis of the classifcation accuracy of the classifers, as shown in Fig. [7.](#page-14-0) As can be seen, KNN,

Fig. 7 The number of works using the ten diferent classifers

DT, NB, SVM, and MLP are the top five classifiers constructed for evaluating the imputation results.

5.3 Computational time

In addition to the two afore-mentioned evaluation strategies, it is also important to take into consideration the computational time for each MVI method. This issue is especially critical for machine learning based MVI techniques which require some time for the model train– ing step. Moreover, when the size of the dataset as well as the missing rate is very large, the imputation process is likely to take a lot of time. Among the articles reviewed, only 16 examined the computation time, these are Huang et al. ([2017\)](#page-19-3), Kiasari et al. (2017), Saha et al. (2017) (2017) , Valdiviezo and Van Aelst (2015) (2015) , Li and Parker (2014) (2014) , Shah et al. (2014) (2014) , Tian et al. ([2014\)](#page-21-4), Aydilek and Arslan [\(2013](#page-18-23)), Liu et al. [\(2013](#page-20-22)), Rahman and Islam [\(2013](#page-20-18)), Stekhoven and Buhlmann [\(2012](#page-22-1)), Zhu et al. (2012), Zhang et al. [\(2011](#page-22-9)), Tuikkala et al. ([2008\)](#page-21-15), Farhangfar et al. [\(2007](#page-18-5)), and Lin et al. ([2006\)](#page-20-9).

5.4 Missing data simulation strategies for missing value imputation

The simulation of an incomplete dataset with a specifc missing rate is usually performed several times in order to avoid producing biased imputation results. This is because the missing data in the incomplete dataset can be diferent for each simulation even with the same missing rate. In general, there are two strategies used to perform a missing data simulation. The frst one is to directly use the whole of the chosen dataset, making it become an incomplete dataset based on a specifed missing rate.

The second strategy is to first divide the chosen dataset into training and testing subsets by some method such as *n*-fold cross validation (CV) (Kohavi [1995](#page-19-27)), or by adopting fixed proportions for the training and testing subsets, e.g. 70% and 30%, respectively. Then, either the training or testing subset is used to perform the missing data simulation for a specifc missing rate.

Figure [8](#page-15-1) shows the number of works that have used the diferent strategies, including the whole dataset (denoted as whole), training set obtained by cross validation (CV-training),

Fig. 8 The number of works using the whole, CV-training, and CV-testing simulation strategies

and the testing set obtained by cross validation (CV-testing). Note that studies that do not clearly describe their simulation strategies are not counted here.

This result shows that most studies use the whole dataset strategy, with the imputation results usually evaluated by the direction evaluation method. Only a small proportion of related studies use the cross validation method for missing data simulation. It should be noted that there is no study which has considered both training and testing subsets when performing missing data simulation for a specifc missing rate. This simulation method is much closer to real world problems based on historical data where the collected data contain some missing values and the new unknown testing data may also contain some missing values.

6 Discussion

The above results of analysis of the related literature show the existence of some limita tions related to technical issues in the experimental procedure, which can be regarded as future research directions for MVI. They are discussed in greater detail below.

6.1 The chosen datasets

The domain problem datasets for MVI can be broadly classifed into two categories. The frst type is based on a number of UCI datasets that cover various domain problems. The second is based on specifc (real world) domain datasets. Although a survey of related works in the frst category study show variety of diferent domain datasets, they are not as large in scale as real world datasets, which often contain a very large number of feature dimensions (e.g. over 100) and/or data samples (e.g. over 100,000).

In addition, in terms of attribute values, the chosen dataset can contain categorical, numerical, or both categorical and numerical types of data. Using diferent types of data may afect the imputation performances of diferent MVI methods.

We now discuss the missing rate used for the simulation for a chosen dataset. It is very hard to defne the missing rates as practical, say less than 30%. To deal with real world problems, however, it would be better to be able to perform simulations with larger missing

rates (e.g. 70%) or a wide range of missing rates (e.g. from 10 to 90%). The fndings from this kind of simulation would be more practical.

About the missing mechanisms, diferent domain problem datasets with missing data may be occurred based on the MCAR, MAR, and NMAR scenarios. Consideration of only one type of scenario in the incomplete dataset simulation is not enough to fully understand the imputation performance of the MVI methods.

Another issue that could afect the imputation results is whether to perform feature and/ or instance selection before or after MVI. Feature and instance selection are aimed at flter‑ ing out unrepresentative features and data samples from a given dataset, respectively. Performing one or both of these tasks before MVI could make the complete dataset 'cleaner', which might lead to produce better imputation results.

Alternatively, performing feature and/or instance selection over an imputed dataset after MVI could make the classifier perform better than one based on the imputed dataset with– out feature and/or instance selection. There have been very few studies which have considered the efect of feature/instance selection on MVI (Aussem and de Morais [2010;](#page-18-10) Doquire and Verleysen [2012;](#page-18-14) Hapfelmeier and Ulm [2014](#page-19-8); Huang et al. [2016](#page-19-26); Sun et al. [2009](#page-21-14); Tsai and Chang [2016](#page-21-2)).

6.2 The MVI techniques

The various baseline MVI techniques discussed in related works can be classifed into two types, statistical or machine learning based techniques. The analytical results detailed in Sect. [4](#page-5-0) clearly identify the most popular MVI techniques. However, there has been no comprehensive study comparing these well-known MVI techniques in terms of diferent domain datasets containing a wide range of missing rates based on diferent missing mechanisms. The fndings of this study allow us to understand which technique(s) are more suitable for which kind of incomplete dataset. The results can be regarded as guidelines for the choice of the most representative MVI technique(s) in future work.

Several novel approaches have been proposed that do not require performing the MVI process to tackle the incomplete datasets; see for example, Conroy et al. ([2016](#page-18-29)), Polikar et al. (2010) (2010) (2010) , and Yan et al. (2017) (2017) . It would very useful to examine the final classification accuracy of these constructed classifers based on these approaches as well as the imputed datasets by the representative baseline MVI technique(s). This study can answer the question: When should we perform missing value imputation?

Furthermore, most of the proposed novel (hybrid) approaches are either statistical techniques (such as the studies on dynamic Fisher's linear discrimination by Leung and Leung [2013](#page-19-22); iterative bi-cluster based least squares by Cheng et al. [2012](#page-18-17); interval imputuation by PCA by Zuccolotto [2012,](#page-22-4) etc.), or machine learning based techniques (such as the studies by Folino and Pisani [\(2016](#page-18-4)) who combined genetic programming and ensemble learning models; Zhang et al. ([2015](#page-22-5)) who combined particle swarm optimization and fuzzy c-means; Silva-Ramirez et al. ([2015](#page-21-13)) who combined MLP and KNN, and so on). The results show that there have been very few studies where a combination of both types of MVI techniques is considered.

6.3 The evaluation methods

Evaluation is very critical for validation of the performance of the MVI technique and reach– ing the fnal conclusions. As noted in Sect. [5](#page-11-0), the direct evaluation method, the classifcation accuracy of the classifers, and consideration of the computational time are the three main ways to evaluate the MVI technique. Using all three of these evaluation metrics would allow us to fully understand the performance as well as provide suggestions for the development of better technique(s). However, this has not been the case, all three evaluation metrics are not used together in most related studies, which is one of the main limitations of current work in the literature and should be considered in future research.

It is suggested that when the chosen dataset is divided into training and testing subsets for missing data simulation, it would be more practical to make both subsets become incomplete rather than focus on only one of them. For instance, start with a collected historical dataset which is incomplete. After performing the MVI process the imputed dataset is used to train a classifer, after which a new testing dataset can be collected, ready for the classifcation task. However, it could happen that this testing dataset is also incomplete, so MVI is required. After performing MVI over the incomplete testing dataset, it can then be fed into the constructed classifer.

It this case, the missing rates of the training and testing datasets can signifcantly afect the final classification accuracy of the classifiers and what is the best combination of MVI techniques and classifers should be answered.

7 Conclusion

Missing value imputation (MVI) for incomplete datasets is a very important problem in data mining and big data analysis. If the incomplete datasets are not well imputed, the fnal mining or analysis result could be affected. This paper discusses a literature review and analysis of 111 related journal articles published from 2006 to 2017.

The review and analysis focus on the issues encountered during the MVI process. They include (1) the chosen datasets as well as their domain problems, missing rates, and missingness mechanisms in the simulation, (2) the MVI techniques employed, and (3) the eval– uation methods considered.

The analysis results show the existence of many limitations encountered in the current literature, which can be improved upon in future. In summary, these include the scalability of datasets, the wide range of missing rates with the MCAR, MAR, and NMAR missing– ness mechanisms, the representative MVI baseline techniques, the development of novel hybrid approaches by combining statistical and machine learning based techniques, the consideration of three evaluation metrics together, and missing data simulation for both training and testing datasets.

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