REVIEW

A comprehensive review on liquid–liquid two‑phase fow in microchannel: fow pattern and mass transfer

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Abstract

Liquid–liquid two-phase fow in microchannel is very common in micro-chemical and micro-biological system, etc. Deep understanding of the liquid–liquid two-phase fow mechanisms and mass transfer in microchannel can promote industrial applications signifcantly. To summarize the recent research progress on the liquid–liquid two-phase fow in microchannel, this paper collects research work about this topic, especially focusing on fow pattern and mass transfer. To begin with, fow patterns observed in various conditions are identifed and factors which infuence the fow patterns are analyzed. Then, mass transfer in liquid–liquid two-phase fow is discussed, especially the mass transfer during droplet fow, with both experiments and simulations. Furthermore, energy dissipation involved in liquid–liquid two-phase fow in microchannel is also briefy discussed. Finally, future needs are proposed for extending the researches on liquid–liquid two-phase fow and enlarging its application felds.

Keywords Flow pattern · Mass transfer efficiency · Energy dissipation · Liquid–liquid two-phase flow · Microchannel

List of symbols

- *C* Concentration of solute
- Arbitrary node concentration of the scalar
- $\frac{C_i}{C_{\sigma}}$ C_{σ} Standard deviation
 \overline{C} Concentration which
- *C̄* Concentration which the mixing is achieving at ideal condition
- ⟨*C*⟩ Statistical average value of the normalized concentration in the analyzed droplet
- *C** Equilibrium concentration of solute
- *Ca* Capillary number
- Constant, $i = 1, 2, 3, ...$
- c_i
 d_h **Hydraulic diameter**
- *h* Channel depth or flm thickness
- *IOS* Intensity of segregation
- $k_1 a$ Overall volumetric mass transfer coefficient

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*l*_d Droplet length *l*_U Droplet unit length
MI Mixing index *MI* Mixing index *N* Number of the nodes in the analyzed droplet Q_d Flow rate of the dispersed phase Q_c Flow rate of the continuous phase R Radius of droplet cap *R* Radius of droplet cap *Re* Reynolds number u_c Velocity of the continuous phase u_{d} Velocity of the dispersed phase *v* Droplet velocity w_c Continuous phase channel width w_d Dispersed phase channel width *We* Weber number Weber number

Greek symbols

- *α* Dispersed phase length fraction
- *δ* Dimensionless surface roughness
- *ε*d Dispersed phase fraction
- *λ* Viscosity ratio of the dispersed phase to the continuous phase
- *μ* Viscosity
- *θ* Contact angle
- *ρ* Density
- *σ* Interfacial tension
- *τ* Residence time
- *Φ* Flow rate ratio of the dispersed phase to the continuous phase
- *Γ* Ratio of channel depth to the continuous phase channel width
- *Λ* Ratio of the dispersed phase channel width to the continuous channel width
- *Ω* Dimensionless interfacial tension

Subscripts

1 Introduction

In recent decades, ever-growing attention has been paid to microfuidic systems due to their outstanding features such as smaller volume, higher security, easier controlling and superior heat and mass transfer performance. The most common two-phase fows in microfuidic systems are gas–liquid fow and liquid–liquid fow. There are widely used in chemical synthesis (Zhao et al. [2015a;](#page-29-0) Oelgemöller and Shvydkiv [2011;](#page-27-0) Yue [2018](#page-28-0)), biomedicine (Zheng et al. [2013](#page-29-1); Lee et al. [2014;](#page-27-1) Cao et al. [2013;](#page-26-0) Murphy et al. [2017\)](#page-27-2) and solvent extraction (Yun et al. [2011;](#page-28-1) Wang and Luo [2017](#page-28-2)). In micro-scale, surface tension is more dominating compared to inertia force and gravity. Depending on operating conditions, different flow regimes are observed such as bubbly flow, Taylor flow, slug–bubbly flow, slug–annular flow, churn flow and annular flow in gas-liquid two-phase flow system and droplet flow, slug flow, slug-drop flow, deformed interface fow, annular fow and parallel fow in liquid–liquid two-phase flow system (Kashid et al. [2011a](#page-27-3)). For precise control, many researches have been conducted to determine the optimal parameters of the microfuidic systems. These parameters can be mainly classifed into two aspects: parameter optimization of microfuidic device which includes structure optimization and dimension optimization; parameter optimization of fuid fow which includes two-phase property optimization and two-phase velocity optimization.

For better guidance on future work of two-phase fow in micro-scale, many reviews are presented. Gu et al. [\(2011](#page-26-1)), Karadimitriou and Hassanizadeh ([2012](#page-27-4)), Seemann et al. (2012) (2012) and Cate et al. (2015) (2015) (2015) gave detailed reviews on fabrication of micro-devices and presented the most common materials used in micro-devices. Seemann et al. [\(2012](#page-28-3)), Vladisavljevic et al. [\(2012](#page-28-4)), Lee et al. [\(2016\)](#page-27-5) and Cai et al. ([2017\)](#page-26-3) summarized the most common structures of microdevices. Christopher and Anna ([2007](#page-26-4)) reviewed microfuidic methods for generating continuous drop streams. Shui et al. [\(2007\)](#page-28-5) discussed the methods of controlling multiphase flow to generate drop (or bubble) or stratified interfaces between fuidic phases. Cristini and Tan [\(2004](#page-26-5)), Antony et al. [\(2014](#page-26-6)), Mao and Yang ([2017](#page-27-6)) and Chen et al. ([2018\)](#page-26-7) gave comprehensive introductions of numerical methods and experimental methods which have been used to carry out two-phase fow in micro-scale. Kashid et al. ([2011\)](#page-27-3) and Sattari-Najafabadi et al. ([2018](#page-28-6)) reviewed studies on both gas–liquid and liquid–liquid mass transfer in micro-scale. Operating conditions and geometry efects on mass transfer were discussed. Antony et al. ([2014\)](#page-26-6) also reviewed mass transfer in micro-scale, especially mass transfer in slug fow. Yao et al. [\(2018\)](#page-28-7) presented a detailed review which aimed at ionic liquid systems in microchannels. The hydrodynamics, mass transfer and application are summarized in detail. Antony et al. ([2014](#page-26-6)), Chinnov et al. ([2015\)](#page-26-8) and Zhu and Wang [\(2017](#page-29-2)) classified the two-phase flow patterns and pointed out the factors afecting the fow patterns. Moreover, Song et al. [\(2006](#page-28-8)) reviewed reactions that occur within seg-mented flows in microfluidic systems. Teh et al. [\(2008](#page-28-9)) presented methods for drop mixing and sorting. Ward and Fan ([2015\)](#page-28-10) summarized the enhancement methods of mixing in micro-scale. Applications of two-phase fow in micro-scale are summarized by Oelgemöller and Shvydkiv ([2011\)](#page-27-0), Cao et al. [\(2013](#page-26-0)), Murphy et al. ([2017\)](#page-27-2), Yun et al. [\(2011\)](#page-28-1), Wang and Luo [\(2017](#page-28-2)), Yao et al. [\(2015\)](#page-28-11) and Šalić et al. [\(2012\)](#page-28-12).

Liquid–liquid two-phase fow holds an important status in microfuidic systems. This paper mainly focuses on the mechanism of liquid–liquid two-phase fow in microchannel and mass transfer in liquid–liquid two-phase fow in microchannel. First, fow patterns observed in various conditions are identifed and factors which infuenced the fow patterns are analyzed. Then, mass transfer in liquid–liquid two-phase flow is discussed, especially mass transfer in droplet flow. Both experiments and simulations are presented. In addition, energy dissipation involved in liquid–liquid two-phase fow in microchannels is only briefy concluded since there are less studies published. Finally, future needs are proposed for extending the research on liquid–liquid two-phase fow and enlarging its application felds.

Table 1 Dimensionless numbers used in liquid–liquid two-phase fow

2 Fundamentals of liquid–liquid two‑phase fow in microchannels

2.1 Dimensionless numbers

The characteristics of liquid–liquid two-phase flow are afected by the following dimensional and physical parameters: continuous phase channel width w_c and dispersed phase channel width w_d , channel depth h , hydraulic diameter d_h , velocity of the continuous phase u_c and dispersed phase u_d (or flow rate of the continuous phase Q_c and dispersed phase Q_d), viscosity of the continuous phase μ_c and dispersed phase μ_d , density of the continuous phase ρ_c and dispersed phase ρ_d and interfacial tension σ . The subscripts c and d represent the continuous phase and dispersed phase, respectively. Dimensionless parameters, deduced from the aforementioned parameters, are commonly used for describing the liquid–liquid two-phase fow (Table [1](#page-2-0)).

2.2 Flow patterns and fow patterns map

Flow patterns are determined by the interaction of various forces including inertia force, gravity, viscosity force and surface tension. In micro-scale, continuous phase and dispersed phase interact with each other in microchannels. Surface tension is more dominating and it makes liquid–liquid two-phase fow in microchannel more controllable. Two-phase interface varies with operating conditions and fuid properties; thus, various fow patterns are presented accordingly. Garstecki et al. [\(2006](#page-26-9); De Menech et al. [2008\)](#page-26-10) described forces which involved the droplet formation process in detail and identifed three distinct regimes, namely squeezing, dripping and jetting to describe the droplet formation process. Xu et al. [\(2008](#page-28-13)) also distinguished the droplet formation mechanisms into three regimes as squeezing, transition and dripping. Later, the squeezing regime and dripping regime are often used by many researchers (Gupta and Kumar [2010a;](#page-26-11) He et al. [2010](#page-27-7); Wehking et al. [2014](#page-28-14); Van Loo et al. [2016](#page-28-15)). In the squeezing regime, the droplet formation process is mainly dominated by the buildup of pressure upstream of an emerging droplet. Droplet length is larger than the microchannel width. In this regime, fow pattern is slug flow dominated. In dripping regime, droplet formation process is mainly dominated by the shear stress which is exerted on the droplet tips. Generally, the droplet length in the dripping regime is smaller than microchannel width. In this regime, flow pattern is droplet flow. Both slug flow and droplet flow are more stable flow patterns than other flow patterns. Flow patterns which have been observed so far are summarized and presented in Table [2](#page-3-0) and Fig. [1.](#page-5-0)

2.2.1 Flow patterns in diferent conditions

Flow patterns depend on the microchannel geometries, property of two phases and flow rate of two phases. Many researches have been conducted for identifying the fow patterns under diferent conditions. Recent progress is summarized as follows.

1. Efect of microchannel features on fow patterns

For a given two-phase system, microchannel features including microchannel material, microchannel geometry both have great influence on flow patterns.

The most common materials for fabricating a microchannel are PTFE, PDMS, PMMA, glass and quartz. Efect of materials on fow patterns is mainly caused by the differences of wetting properties of the phases to the walls, namely the contact angle between phases and walls. The value of the contact angle is determined by phase properties and microchannel material. Salim et al. ([2008](#page-28-16)) measured contact angles of oil droplets on quartz and glass of 12° and 3°, respectively. However, contact angles of water droplets were 42° and 38°, respectively. Table [3](#page-5-1) shows the

Table 2 A summary of flow patterns in published literature

Fig. 1 Representative flow patterns in published literature. **a** slug flow (Zhao et al. [2006\)](#page-28-17); **b** droplet flow (Zhao et al. [2006](#page-28-17)); c thread flow (Cubaud and Mason [2008\)](#page-26-12); **d** jet flow (Cubaud and Mason [2008](#page-26-12)); **e** deformed interface fow (Kashid and Kiwiminsker [2011\)](#page-27-8); **f** annular/parallel fow (Kashid and Kiwiminsker [2011\)](#page-27-8); **g** intermittent fow (Tsaoulidis et al. [2013\)](#page-28-20); **h** throat annular fow (Tsaoulidis et al. [2013\)](#page-28-20); **i** irregular flow (Liu et al. [2018](#page-27-12)); **j** string of sausages (Liu et al. [2018](#page-27-12)); **k** annular–dispersed fow (Zhang et al. [2019](#page-28-22)); **l** droplet–dispersed fow (Zhang et al. [2019\)](#page-28-22); **m** slug–dispersed fow (Zhang et al. [2019](#page-28-22)); **n** annular–dispersed fow (Zhang et al. [2019\)](#page-28-22)

Table 3 Contact angles on borosilicate glass and Tefon plates by Tsaoulidis et al. ([2013\)](#page-28-20)

contact angles on borosilicate glass and Teflon plates which were measured by Tsaoulidis et al. ([2013\)](#page-28-20). Results showed that the main patterns observed in glass microchannels were plug, plug and drop train and dispersed flow; while in the Tefon microchannel, annular, plug and droplet fow prevailed. More important, the authors found that in glass microchannel, the continuous phase and dispersed phase were determined by the fuid which initially flled the microchannel. With water initially saturated in a glass microchannel, it became the continuous phase. However, in a Tefon microchannel, whether the water was initially saturated or

an ionic liquid was initially saturated, the ionic liquid was always the continuous phase.

Xu et al. ([2006](#page-28-18)) studied fow patterns in n-octane–water system; contact angle of oil phase was changed by adding diferent amount of sodium dodecyl sulfate (SDS) in water. Results showed that the contact angle increased with the addition of SDS. The contact angle increased up to more than 90° when the SDS concentration exceeded a critical micellar concentration (0.05% w/w). When the contact angle was more than 90 $^{\circ}$, ordered flow of drops can be formed. To investigate the effect of contact angle on flow patterns, Zhao et al. ([2010](#page-29-3)) made surface modifcation on a PMMA microchannel and a stainless steel mcirochannel. The changes of contact angle before and after modifcation are presented in Table [4](#page-6-0). Flow patterns before surface modifcation were presented as slug, monodispersed drop and parallel fow. However, after the surface modification, only parallel flow was observed.

Compared with experiments, numerical simulation provides an alternative way to study the effect of contact angle on flow patterns. Sang et al. (2009) (2009) varied the contact angle from 130° to 180°, and measured the droplet length for different contact angles. Results showed that the increase of the contact angle led to a decrease of the droplet length. This efect became lower when the contact angle was larger than 165°. Further, Raj et al. ([2010](#page-27-13)) observed flow patterns for diferent contact angles including 60°, 90°, 120°, 140°, 160°, 180° by the VOF (volume of fuid) method. With increasing contact angle, parallel flow, slug flow and droplet flow were observed in turn. More importantly, when the contact angle was increased form 160° to 180°, the droplet length changed marginally. The same results were also presented by Bashir et al. ([2011](#page-26-18)). They studied the efect of contact angle on droplet length by the level set method. Droplet lengths for various contact angles and capillary numbers were measured. Results indicated that with the contact angle greater than 165°, the droplet length remained nearly constant for all capillary numbers considered. It can be seen that when the contact angle is larger than a certain value, approximately 165°, the efect on droplet length becomes marginal.

The most common inlet structures of microchannel are T-junction, Y-junction and Cross-shaped junction. Raj et al. ([2010\)](#page-27-13) conducted simulations for determining the efect of inlet structure on the slug formation process. The slug size was measured in cross-shaped T-junction, T-junction and Y-junction and results indicated that the inlet structures only had minor infuence on slug size. Qian et al. [\(2019](#page-27-14)) investigated the effect of microchannel geometry on the slug formation process. Both the dispersed phase channel width and channel depth were considered, and quantitative analyses were presented based on the dimensionless numbers. The results gave a constructive reference for determining the microchannel geometry. Dessimoz et al. ([2008](#page-26-19)) carried out experiments in water–toluene systems to investigate the fow patterns in microchannel with Y-junction and T-junction. Results presented that for all volumetric fow rates used in the experiments, Y-junction always led to a parallel flow, while slug flow was formed in T-junction. Kashid and Kiwiminsker [\(2011](#page-27-8)) carried out experiments to identify the fow patterns in microchannels with diferent cross sections and contacting geometries. Four diferent microchannels which named T-square, T-trapezoidal, Y-rectangular and concentric as shown in Fig. [2](#page-7-0) were used. Flow patterns including slug, slug–drop, deformed interface and parallel/annular were observed in all tested microchannels. Wu et al. [\(2017\)](#page-28-21) developed an unsteady model of droplet formation to investigate the role of microchannel geometry on droplet formation. Axisymmetric microchannels called co-fow and fow-focusing as shown in Fig. [3](#page-7-1) were designed and used for simulation. Drop flow, transition flow and jet flow were observed in both microchannels. Results also indicated that the co-fow microchannel had great superiority for producing monodispersed droplet, while the flow-focusing microchannel performed well in producing droplets with higher frequency. For improving the droplet formation frequency, Wang et al. ([2011\)](#page-28-24) made a slight modifcation of an ordinary T-junction microchannel—the continuous phase channel was designed with an equicrural trapezoid block to form a venturi-shaped neck and called venturi-shaped microchannels. Results indicated that the venturi-shaped microchannels could produce smaller **Fig. 2** Diferent microchannels used by Kashid and Kiwiminsker. ([2011\)](#page-27-8). **a** T-square; **b** T-trapezoidal; **c** Y-rectangular; **d** concentric

droplets with a higher frequency compared with T-junction microchannels at the same fow conditions. The authors further studied the efect of venturi-shaped neck position on droplet formation. Results showed that with a suitable position, the venturi-shaped microchannels could save more than 90% of the continuous phase when producing a droplet with same diameter in T-junction microchannels. Further, Derzsi et al. [\(2013](#page-26-14)) compared fow patterns which were observed in microchannels with three diferent confgurations as shown in Fig. [4.](#page-8-0) In all three microchannels, the same sequence of flow pattern transitions was observed which included drop without satellites, drop with single satellite, multiple satellites and jet fow. Detailed study showed that by comparing FF-2 and FF-3, the dimension of the outlet had no infuence on the droplet size in droplet fow. However, in jet fow, the FF-3 with a wider outlet could produce droplets with larger diameter. In addition, fow patterns in microchannels with more complex structures were investigated by Ploufe et al.

Fig. 4 Microchannels with three diferent confgurations used by Derzsi et al. ([2013\)](#page-26-14). FF-1: ordinary cross-shaped micorchannel; FF-2: crossshaped microchannel with contraction; FF-3: cross-shaped microchannel with contraction and a wider outlet

Fig. 5 Diferent microchannels used by Ploufe et al. ([2016\)](#page-27-9). **a** SZ; **b** TG; **c** Venturi; **d** Sickle; **e** Spade

[\(2016\)](#page-27-9). Microchannels named SZ, TG, Venturi, Sickle and Spade as shown in Fig. [5](#page-8-1) were used in the experiments. With an increase of fow rates, slug, parallel, drop and dispersed flows were captured in sequence in microchannels of SZ, TG and Spade. In the microchannels of Venturi and Sickle, there was no parallel flow observed.

2. Efect of physical properties on fow patterns

Properties of two phases include densities of two phases, viscosities of two phases and interfacial tension. In microscale, inertia force and gravity are less important which means that the efect of density can be negligible. Many researches have been conducted to confrm the efects of viscosities of two phases and interfacial tension on fow patterns. For Newtonian system, Liu and Zhang ([2009\)](#page-27-15) investigated the role of viscosity ratio on fow patterns. Results showed that for a critical capillary number $(Ca_c=0.018)$, viscosity ratio may influence the drop size only when $Ca > Ca_c$ and the drop size is decreased with an increase of viscosity ratio. Gupta and Kumar [\(2010](#page-26-20)) analyzed the continuous phase viscosity on fow patterns. Results showed that at large flow rate ratio (Φ = 1/5), an increase of the continuous phase viscosity made the fow patterns to transform from parallel flow to droplet flow. Higher continuous phase viscosity was more beneficial for droplet flow. Feigl et al. (2014) (2014) investigated the effect of the continuous phase viscosity and dispersed phase viscosity on fow patterns, respectively. The constant viscosity ratio of $\lambda = 6$ was achieved by increasing the dispersed phase viscosity or decreasing the continuous phase viscosity. The dispersed phase velocity was kept as 0.011 m/s in both cases. It was shown that when increasing the dispersed phase viscosity, the flow patterns changed from droplet flow to jet flow. To maintain the droplet flow, the dispersed phase velocity should be decreased to 0.0011 m/s. However, when decreasing the continuous phase viscosity, the droplet fow was prevailed. Wehking et al. [\(2014](#page-28-14)) also investigated the efect of viscosity ratio on flow patterns. The flow pattern transition from droplet flow to parallel fow was easily happened at low viscosity ratio.

Viscosity of Newtonian fuids and non-Newtonian fu-ids has different effects on flow patterns. Sang et al. ([2009\)](#page-28-23) investigated the efects of continuous phase viscosity on drop size. Both Newtonian and non-Newtonian fuids were considered. Results indicated that the increase of viscosity in Newtonian fuids and power-law fuids reduced the drop size. However, in Bingham fuids, the increase of viscosity had less effect on drop size. The 960% variation of viscosity only made a 4% variation of drop size. Experiments were carried out by Derzsi et al. (2013) (2013) to illustrate the dynamics of Newtonian droplet formation in non-Newtonian/Newtonian systems. Comparatively, Newtonian droplet formation in Newtonian/Newtonian systems was presented as well. In Newtonian/Newtonian systems, the continuous phase of Newtonian fuid shared the same shear viscosity with the non-Newtonian counterpart. Figure [6](#page-9-0) displays the comparisons of flow pattern in Newtonian/Newtonian (N) and non-Newtonian/Newtonian (nN) systems.

In Fig. [6,](#page-9-0) the columns and rows illustrated the drop formation in various fow rate ratios and the dispersed phase viscosities. It can be seen that the droplet shape was more deformed when the continuous phase is the non-Newtonian fuid. It can be seen that the droplet in Newtonian/Newtonian system was nearly spherical and the shapes kept constant when the droplet moved downstream. While in

Fig. 6 Examples of fow patterns in Newtonian/Newtonian (N) and non-Newtonian/Newtonian (nN). systems observed by Derzsi et al. [\(2013](#page-26-14))

non-Newtonian/Newtonian system, the droplet transformed from elliptical shapes to bulleted shapes. The deformation rate of droplet was increased with an increase of the continuous phase fow rate. In addition, elasticity of the non-Newtonian fluid made a more stable jet flow compared with the Newtonian fuid. Other remarkable results indicated that viscoelastic liquids had superiority to produce droplet with higher frequency at low flow rates. Fu et al. ([2015\)](#page-26-15) conducted experiments to investigate the fow patterns of Newtonian (dispersed phase)/non-Newtonian fuids (continuous phase) two-phase flow. Four flow patterns were mainly observed which included slug flow, drop flow, jet flow and parallel flow. The non-Newtonian fluids were carboxyl methyl cellulose (CMC) in demineralized water with diferent concentrations. The increases of concentration of CMC led to an increase of viscosity. Thus, it was made possible to form droplet fow even at a low dispersed phase velocity. Liu et al. ([2018](#page-27-12)) investigated dynamics of water–ionic liquid ([BMIM] [PF6]) two-phase flow in a flow-focusing microchannel. The ionic liquid had a high viscosity of 251.76 mPa s. By changing the fow rates of the two phases, fow patterns which included dripping, jetting, irregular and string of sausages were observed. In addition, the droplet formation mechanisms in Newtonian and non-Newtonian fluids were also compared with Cubaud and Mason [\(2008](#page-26-12)), Qiu et al. ([2010](#page-27-16)) and Chiarello et al. [\(2015\)](#page-26-22).

Interfacial tension is related to properties of two phases. Dessimoz et al. [\(2008](#page-26-19)) studied effect of interfacial tension on fow patterns in water–toluene system. Solutes were added in water and toluene for changing the interfacial tension of the systems. Results showed that at lower interfacial tension, flow patterns were parallel flow dominated. With an increase of interfacial tension, slug fow was observed. Timung et al. (2015) (2015) (2015) studied the effect of viscosity and interfacial tension on flow patterns. With reduction of interfacial tension, fow patterns including slug, plug, drop, core-annular and stratifed were presented in sequence. Darekar et al. ([2017\)](#page-26-16) investigated the effect of interfacial tension on flow patterns. The variation of interfacial tension was achieved using different two-phase systems which included water/n-butanol, water/n-butyl acetate and water/toluene. The interfacial tension was 1.75 mN/m, 14.1 mN/m and 36 mN/m, respectively. Results showed that in water/toluene system with the highest interfacial tension, slug flow was dominating among all fow patterns. With the decrease of interfacial tension, parallel flow was more pronounced. Wehking et al. ([2014](#page-28-14)) investigated the effect of interfacial tension on flow patterns and the transition lines of droplet fow to parallel fow were compared. Raj et al. (2010) (2010) also investigated the effect of viscosity and interfacial tension on slug size.

3. Efect of fow rate on fow patterns

Flow rate is an important parameter affecting the flow patterns. It can be easily changed to achieve various fow patterns. Generally, slug flow is more observed at a low flow rate of both phases. When the continuous phase fow rate increases while the dispersed phase flow rate is kept constant, droplet fow is presented. In contrast, when the dispersed phase fow rate increases while the continuous phase flow rate is kept constant, parallel flow is emerged (Kashid and Kiwiminsker [2011](#page-27-8); Darekar et al. [2017\)](#page-26-16).

Up to now, nearly all researches have been operated at room temperature. However, in actual conditions, temperature is also a non-negligible factor on liquid–liquid twophase fow patterns. Zhang et al. ([2019\)](#page-28-22) conducted experiments at diferent temperatures to investigate the efect of temperature on liquid–liquid two-phase fow hydrodynamics. Three temperatures, namely 0.5, 10 and 25 °C, were selected for experiments. Physical properties of each fuid were measured at diferent temperatures as shown in Table [5.](#page-10-0) The viscosities of water and 92% H₂SO₄ presented highly **Table 5** Physical properties of the fuids at diferent temperatures by Zhang et al. ([2019\)](#page-28-22)

sensitivity to temperature. In all experiments, the oil phase was the continuous one, while the aqueous phase was the dispersed one. Thus, an increase of temperature directly led to a decrease of dispersed phase viscosity. According to the authors, the dispersed phase viscosity played an important role in the fow pattern transition from slug to annular fow. Thus, the increase of temperature made the slug flow to dominate the fow pattern map.

2.2.2 Flow pattern maps

Flow pattern maps are plotted for identifying the fow pattern transitions distinctly. Parameters such as velocity of two phases (Salim et al. [2008;](#page-28-16) Kashid and Kiwiminsker [2011;](#page-27-8) Fu et al. [2015](#page-26-15); Mahdi et al. [2017](#page-27-11); Cao et al. [2018\)](#page-26-17), fow rates of two phases (Zhao et al. [2006](#page-28-17); Sarkar et al. [2012;](#page-28-19) Darekar et al. [2017;](#page-26-16) Mahdi et al. [2017\)](#page-27-11), Capillary numbers (Cubaud and Mason [2008](#page-26-12); Darekar et al. [2017\)](#page-26-16), Weber numbers (Fu et al. [2012](#page-26-13); Darekar et al. [2017](#page-26-16)) and so on (Wu et al. [2017](#page-28-21); Zhang et al. [2019](#page-28-22)) are mainly used as coordinates for plotting flow pattern maps.

Zhao et al. (2006) (2006) (2006) plotted flow pattern maps as shown in Fig. [7\(](#page-12-0)a) based on Weber number of two phases. The flow pattern maps were divided into three regions and corresponding criteria were proposed as:

I: the interfacial tension-dominated region, including slug flow, monodispersed flow parallel flow with smooth interface, for (We_{KS} <1) ∩ (We_{WS} <1); II: region where the inertia and interfacial tension were comparable, including parallel fow with wavy interface and droplet populations, for $[(We_{KS}$ <10)∩(We_{WS} <10)] ∩[(We_{WS} >1)∪ (We_{KS} >1)]; III: the inertia-dominated region, including droplet populations and chaotic thin striations flow, for (*We*_{KS}>10)∪ $(We_{\rm WS} > 10).$

Kashid and Kiwiminsker ([2011](#page-27-8)) observed flow patterns in diferent microchannel structures and fow pattern maps were plotted based on velocities of the two phases as shown in Fig. [7](#page-12-0)b–d. By comparing the three fow pattern maps, fow pattern transitions with increasing velocity of the two phases could be distinguished obviously. Furthermore, a criterion for identifying flow patterns in a given microchannel was proposed as: surface tensiondominated region: $Re_d d_h / \varepsilon_d < 0.1$ m; Transition region: 0.1 m $\lt R e_d d_h / \varepsilon_d \lt 0.35$ m; Inertia-dominated region: $Re_{d}d_{h}/\varepsilon_{d}$ > 0.35 m.

Wehking et al. ([2014\)](#page-28-14) carried out nearly one hundred experiments for identifying hydrodynamics of liquid–liquid two-phase flow. Critical capillary numbers were proposed to predict fow pattern transitions from droplet to parallel.

$$
Ca = c_0 \Gamma^{c_1} \Omega^{c_2} \lambda^{c_3} \Phi^{c_4},\tag{1}
$$

where $c_0 \sim c_4$ are constants and have different values in slug/ parallel transition and drop/parallel transition. *Ω* represents the dimensionless interfacial tension.

Fu et al. ([2015\)](#page-26-15) investigated flow patterns of non-Newtonian systems and plotted the fow pattern maps based on velocity of the two phases as shown in Fig. [7e](#page-12-0). Based on Weber number, microchannel dimension and viscosity of the two phases, a general model was proposed for predicting fow pattern transitions including slug/drop transition line, drop/jet transition line, slug/jet transition line and parallel/ jet transition line.

$$
c_0 W e_c^{c_1} (h/w)^{c_2} \delta^{c_3} (\mu_c / \mu_d)^{c_4} = W e_d^{c_5} (h/w)^{c_6} \delta^{c_7} (\mu_c / \mu_d)^{c_8}, \tag{2}
$$

where $c_0 \sim c_8$ are constants and have different values for each transition. δ represents the dimensionless surface roughness. The viscosity of non-Newtonian fuid was calculated based on Carreau model. The experimental conditions were: 2.18 5 × 10⁻³ < *Ca*_c < 9.27 × 10⁻², 3.643 × 10⁻³ < *Re*_c < 17.1528, $7.9605 \times 10^{-6} < We_c < 0.9770, \quad 5.5181 \times 10^{-6} <$ $Ca_d < 4.258 \times 10^{-3}$, 9.63 × 10⁻³ < Re_d < 80.2537, 5.3142×10^{-7} < We_d < 0.3417.

Cao et al. [\(2018\)](#page-26-17) also plotted fow pattern maps based on velocity of the two phases as shown in Fig. [7](#page-12-0)f. A general empirical correlation was proposed for identifying fow pattern transitions including annular/slug transition and slug/ drop transition.

$$
c_0 R e_c^{c_1} W e_c^{c_2} = R e_d^{c_3} W e_d^{c_4}, \tag{3}
$$

where $c_0 \sim c_4$ are constants and have different values for each transition.

Zhang et al. ([2019\)](#page-28-22) carried out comprehensive experiments to study efects of temperature, properties of fuids and microchannel dimensions on fow patterns. Figure [7](#page-12-0)g and h present the fow pattern maps in diferent two-phase systems based on capillary number of the continuous phase and Reynolds number of the dispersed phase. Flow patterns which include droplet flow, slug flow, irregular slug

Fig. 7 Typical fow pattern maps reported in literature. **a** Flow pattern ◂maps and transition lines plotted by Zhao et al. ([2006\)](#page-28-17) **b** Flow pattern maps in T-square and T-trapezoidal microchannels plotted by Kashid and Kiwiminsker ([2011\)](#page-27-8) **c** Flow pattern maps in Y-rectangular microchannel plotted by Kashid and Kiwiminsker [\(2011](#page-27-8)) **d** Flow pattern maps in concentric microchannel plotted by Kashid and Kiwiminsker [\(2011](#page-27-8)) **e** Flow pattern maps and transition lines for fow patterns plotted by Fu et al. ([2015\)](#page-26-15) **f** Flow pattern maps plotted by Cao et al. ([2018\)](#page-26-17) **g** Flow pattern maps in toluene/water system plotted by Zhang et al. ([2019\)](#page-28-22) **h** Flow pattern maps in ethyl acetate/water system plotted by Zhang et al. (Zhang et al. [2019\)](#page-28-22)

flow, slug–dispersed flow, slug–annular flow, annular flow, annular–dispersed fow and droplet–dispersed fow were observed. These flow patterns were divided into three regions according to the forces involved as shown in Fig. [7](#page-12-0)g and h. A general correlation was proposed as Eq. ([4\)](#page-12-1), to predict the slug/parallel transition and slug/drop transition.

$$
Ca_{d}^{0.7}Re_{d}^{0.5} = c_{1}(Ca_{c}Re_{c}^{0.5})^{c_{2}},
$$
\n(4)

where c_1 and c_2 are constants and have different values for each transition. The authors verifed the universality of the proposed correlation by comparing experimental results in published literature which involved a large viscosity range from 0.85 to 1200 mPa s.

3 Mass transfer in liquid–liquid two‑phase fow in microchannels

The overall volumetric mass transfer coefficient calculated in microchannels was more than two or three orders of magnitude higher than those in conventional reactors and the energy consumption in microchannels was far less than in conventional reactors (Zhao et al. [2007](#page-29-4); Kashid and Agar [2007\)](#page-27-17). Due to the great superiority of liquid–liquid twophase fow in microchannels, many researches have been carried out for studying mass transfer in liquid–liquid twophase fow in microchannels. Table [6](#page-13-0) gives a detailed summary of volumetric mass transfer coefficients in liquid–liquid two-phase fow in microchannels tested so far.

3.1 Enhancement of mass transfer performance

Among all the fow patterns mentioned in Sect. [2,](#page-2-1) droplet flow and slug flow present great superiority in mass transfer performance due to the existing inner circulation in the droplet/slug and the large specifc interfacial area. These two aspects are illustrated in this part in detail. In the following descriptions, the droplet is used to represent both droplet and slug.

3.1.1 Inner circulation in droplets

When the droplet moves along the microchannel, due to the shear stress exerted by the wall, radial velocity gradient exists when fuids are fowing through the microchannel. The velocity reduces from the axial direction of the microchannel to the walls. However, when droplet is moving through the microchannel, not only a velocity gradient exists in the radial direction due to the shear stress exerted by the wall, but also a velocity gradients exist both in the radial direction and the axial direction. The former is induced by the interaction with the wall and the latter is caused due to the interaction with the continuous phase. Therefore, inner circulations are induced due to the velocity gradient. The inner circulation promotes the surface renewal and reduces the thickness of the boundary layer at the phase interface, so the mass transfer performance is enhanced accordingly. One of the earliest experiments for elaborating mass transfer performance enhanced by inner circulation in droplet was performed by Burns and Ramshaw [\(2001](#page-26-23)). Later, experiments and simulations were carried out by Kashid [\(2005](#page-27-18)), Kashid et al. ([2007,](#page-27-19) [2008](#page-27-20)) and Kinoshita et al. ([2007\)](#page-27-21) to further clarify the inner circulation in the droplet and the stagnant region where the liquid velocity is zero in droplet. Particle image velocimetry (PIV) and CFD particle tracing algorithm were used for visualizing the inner circulation in a droplet.

Figure [8](#page-15-0) presents the schematic representation of inner circulation and velocity distribution in droplets (Li and Angeli [2017](#page-27-22)). It can be seen from Fig. [8a](#page-15-0) that three pairs of inner circulation existed in the droplet. The main circulation is induced by the interaction with the wall which marked as 1. The minor circulation is induced by the interaction with the continuous phase which marked as 2.

3.1.2 Specifc interfacial area

The droplet flow pattern provides a uniform interfacial area which signifcantly promote the mass transfer process. Moreover, the uniform interfacial area makes the prediction of the overall volumetric mass transfer coefficient possible. In liquid–liquid droplet fow, the specifc interfacial area is defned as the ratio of droplet surface to unit cell volume. Methods for determining the specifc interfacial area can be classifed into physical method and chemical method (Ghaini et al. [2010](#page-26-24)). For physical measurement, the most common method is light induced fuorescence combined with photography. By taking high-resolution images, the droplet surface area and droplet unit volume can be calculated and the specifc interfacial area is obtained as well. However, the main difficulties lie in the simplification of the droplet shape and the measurement of the flm thickness. Figure [9](#page-15-1) shows the schematic diagram of droplet flow in microchannels with and without film. In Fig. [9](#page-15-1), L_d , L_U , R, w and h represent the

(a) Velocity distribution and inner circulation in a droplet

(b) Non-dimensional horizontal component of total velocity at different locations along a droplet

Fig. 8 Velocity distribution and inner circulation in a droplet (Li and Angeli [2017\)](#page-27-22). **a** Velocity distribution and inner circulation in a droplet. **b** Non-dimensional horizontal component of total velocity at diferent locations along a droplet

droplet length, droplet unit length, radius of droplet cap, microchannel width and flm thickness, respectively.

Generally, for a droplet with regular shape as shown in Fig. [9](#page-15-1), the droplet can be considered as a cubic combined with hemispheric shape (Raimondi et al. [2014](#page-27-23); Sattari-Najafabadi et al. [2017a](#page-28-28)). The most used method for the prediction of the flm thickness is proposed by Brethertons (Kashid and Agar [2007;](#page-27-17) Ghaini et al. [2010;](#page-26-24) Xu et al. [2013](#page-28-26)). The Brethertons law (Bretherton [1961\)](#page-26-26) considers the capillary number as the signifcant factor for determining the flm thickness. In addition, correlations for calculating the flm thickness based on other parameters such as Weber number, Reynolds number or the combinations (Tsaoulidis and Angeli [2016;](#page-28-29) Dore et al. [2012\)](#page-26-27) are proposed and theses correlations are summarized by Li and Angeli [\(2017](#page-27-22)) in detail.

3.2 Methods of mass transfer performance studies

Table [7](#page-16-0) summarizes the general methods used for conducting mass transfer performance studies in liquid–liquid twophase fow in microchannels. Experiments and simulations are included.

When conducting experiments involving reactions, neutralization of an acid with alkali is widely used in studying the mass transfer efficiency. Alkali and acid are added into the aqueous phase and organic phase, respectively. With droplets moving, the acid is transferred from the organic phase into the aqueous phase and reaction happens (Dessimoz et al. [2008;](#page-26-19) Kashid [2005](#page-27-18); Sattari-Najafabadi et al. [2017b](#page-28-30)). One important thing is that the transferred acid should be reacted with the alkali instantaneously in order to avoid the accumulation of the acid in the organic phase and further eliminate the efect of reactions on the mass transfer performance. Indicators such as bromothymol-blue, phenol red and Sudan III are added in the aqueous phase or organic phase. The reaction process is visualized by color change of the phases including indicators. Figure [10](#page-17-0)a shows the neutralization of $CH₃COOH$ with NaOH recorded by Dessimoz et al. [\(2008\)](#page-26-19). The color change of the aqueous phase from blue to yellow was clearly observed as droplet was moving along the microchannel. In addition, saponifcation and alkaline hydrolysis are also used for analyzing mass transfer efficiency (Zhang et al. 2019). The concentration of alkali in the aqueous phase was subsequently measured by

to uniform in droplets

Table 7 (continued)

Table 7 (continued)

Fig. 10 Visualization of mass transfer in droplet. **a** neutralization of CH 3COOH with NaOH recorded by Dessimoz et al. ([2008\)](#page-26-19). The color change of aqueous phase from blue to yellow with droplet mov ing along the microchannel. **b** Dstribution of tracers in moving drop lets recorded by Zhao et al. ([2015\)](#page-29-6) using LBM coupled with passive tracer model

acid–base titration. When conducting experiments without reaction, extraction is more often used for analyzing mass transfer efficiency (Raimondi et al. [2014;](#page-27-23) Woitalka et al. [2014](#page-28-27); Kashid et al. [2007;](#page-27-19) Aoki et al. [2011;](#page-26-28) Matsuoka et al. [2016](#page-27-24); Darekar et al. [2014](#page-26-29)). UV-spectrophotometry measure ments are adopted for measuring the concentration of the extraction phase.

When conducting simulations involving reactions, 2D CFD is adopted. The aqueous phase and organic phase are represented by two adjacent units and the moving walls are set to replace the flow of the phases (Harries et al. [2003](#page-27-25); Zhang et al. [2016](#page-28-31); Sahu et al. [2016\)](#page-27-26). However, most researches are conducted without reaction and the mass transfer efficiency is represented by the uniformity of species/scalars/tracers in droplets. Coupled methods including the level set coupled with species transport model, VOF cou pled with user defned scalar and LBM coupled with passive tracer model are mostly used (Zhao et al. [2012](#page-29-5); Özkan and Erdem [2015;](#page-27-27) Yang et al. [2018](#page-28-32)). Figure [10b](#page-17-0) presents distribution of tracers in droplets. It can be seen that with droplets moving along the microchannel, the distribution of tracers in droplets tends to be uniform.

For comparing mass transfer efficiency in different conditions, the overall volumetric mass transfer coefficient k_La ,

Fig. 11 The overall volumetric mass transfer coefficient in microchannels with diferent dimensions

mixing index MI and intensity of segregation IOS are calculated and used for quantitative analysis.

$$
k_{\text{L}}a = \frac{1}{\tau} \ln \left(\frac{C_{\text{aqu,in}}^* - C_{\text{aqu,in}}}{C_{\text{aqu,out}}^* - C_{\text{aqu,out}}} \right),\tag{5}
$$

where τ is the residence time, C^* and C are the equilibrium concentration of solute and concentration of solute, respectively. The subscripts in and out represent the inlet and outlet, respectively. The subscript aqu represents the aqueous phase. The solute is transformed from organic phase to aqueous phase.

$$
MI = \left(1 - \frac{\sqrt{\frac{1}{N} \sum_{i=1}^{N} (C_i - \overline{C})^2}}{\overline{C}}\right) \times 100\%,\tag{6}
$$

where C_i is the arbitrary node concentration of the scalar, *C* is the concentration for which the mixing is achieved at ideal condition, *N* is the number of nodes in the analyzed droplet. MI is the abbreviation of mixing index, which is defned based on the standard deviation from the ideal condition. The value of MI represents the uniformity of scalar distribution in the droplet.

$$
IOS = \left(\frac{C_{\sigma}^2}{\langle C \rangle - \langle 1 - \langle C \rangle \rangle}\right),\tag{7}
$$

where C , $\langle C \rangle$ and C_{σ} represent the normalized concentrations of fuids at each individual lattice, the statistical average value of *C* in droplets and standard deviation, respectively.

IOS is the abbreviation of intensity of segregation. The value of IOS represents the uniformity of the concentration distribution in droplets (Zhao et al. [2012](#page-29-5)).

3.3 Mass transfer efficiency in different conditions

3.3.1 Efect of microchannel features on mass transfer efficiency

For a specifc two-phase system, microchannel features play an important role for mass transfer performance.

Generally, the microchannel with small dimensions performs better for enhancement of mass transfer efficiency (Ghaini et al. [2010](#page-26-24); Xu et al. [2013;](#page-28-26) Raimondi et al. [2014](#page-27-23); Matsuoka et al. [2016;](#page-27-24) Özkan and Erdem [2015\)](#page-27-27). Figure [11](#page-18-0) summarizes the overall volumetric mass transfer coefficient in microchannels with diferent dimensions. Although different liquid–liquid systems used, the infuence of the microchannel dimension on the overall volumetric mass transfer coefficient is more remarkable.

The reduced microchannel dimension facilitates the droplet formed with a larger specifc interfacial area and shortens the mass transfer length. Ghaini et al. [\(2010](#page-26-24)) studied efects of internal capillary diameter on mass transfer coefficient using both physical and chemical methods. Results indicated that decreasing the capillary diameter gave higher enhancement of the mass transfer coefficient. For example, $k_{\text{I}}a$ was obtained for capillary diameters 1000 μ m, 750 μm and 500 μm and the values were 1 s^{-1} , 1.28 s^{-1} and 1.58 s⁻¹, respectively, at a constant aqueous phase flow rate of 70 ml/h. Xu et al. [\(2013](#page-28-26)) compared volumetric extraction rate in microchannels for a capillary diameters of 600 μm and 800 μm. The volumetric extraction rate in capillary diameter of 600 μm was always higher than for 800 μm. This was caused by the diferences in specifc interfacial areas between the phases. The mean interfacial area measured for the capillary diameter 600 μ m was 4000 m²/m³, while for the capillary diameter 800 μ m the value was only 3000 m²/m³. Raimondi et al. [\(2014](#page-27-23)) investigated mass transfer mechanism in microchannels with square cross section. The concentration profle of solute in dispersed phase along the microchannel was measured. Results showed that a smaller microchannel size provided a larger interfacial area, and accordingly a larger mass transfer coefficient. Matsuoka et al. (2016) (2016) studied efects of the hydraulic diameter on mass transfer efficiency. Circular and semicircular microchannels with a hydraulic equivalent diameter range of 600 μm to 2000 μm were designed to perform liquid–liquid extraction of phenol from dodecane to water. At the same Reynolds number, volumetric mass transfer coefficient increased with the decrease of hydraulic equivalent diameter both in circular and semicircular microchannels.

Fig. 12 Confgurations of inlet junction designed by Zhao et al. ([2012\)](#page-29-5). **a** T-junction; **b** crossshape microchannel; **c** coaxial micro-capillary; **d** modifed T-junction with venturi-shape; **e** micro-capillary insertion microchannel

Microchannel structures including confgurations of inlet junction and confgurations of the main channel are most important for enhancement of mass transfer efficiency.

Confgurations of inlet junction mainly afect the mass transfer efficiency in the droplet formation process. Kashid et al. ([2011](#page-27-32)) conducted experiments to identify the mass transfer efficiency in different microchannels including T-square, T-trapezoidal, Y-rectangular, concentric and caterpillar as shown in Fig. [2.](#page-7-0) It is worth noting that the caterpillar microchannel was a microchannel with internal bas-relief structure and the other four microchannels had no internal structures. By changing the water flow rate, the mass transfer coefficient in each microchannel was obtained and plotted. Results showed that the caterpillar microchannel had best performance due to its internal bas-relief structure. The existence of the internal bas-relief structure created a considerably fne dispersion and provided a higher interfacial area compared with other microchannels. Compared with non-structured microchannels, the mass transfer coefficient in caterpillar microchannel was almost 1 order of magnitude higher than the concentric microchannel and 2–3 times higher than that of on the other microchannels. Zhao et al. (2012) compared mass transfer efficiency in different confgurations of the inlet junction including T-junction, cross-shaped junction and coaxial micro-capillary as shown in Fig. [12](#page-19-0)a–c. The LBM method was adopted in the simulations. Results showed that in cross-shaped junction microchannel and micro-capillary microchannel, the velocity feld and concentration distribution were both kept symmetric in the droplet formation process. This made the tracers difficult to distribute uniformly and caused lower mass transfer efficiency. For breaking up the bilateral symmetry, modifed T-junction with venturi-shape and micro-capillary insertion microchannel were proposed as shown in Fig. [12d](#page-19-0)–e. The modifed structures performed well for enhancement of mass transfer efficiency. When droplet moves through the microchannel, distribution of the tracers was reorientated due to the asymmetric inner circulation which was disturbed by the venturi-shape structure and micro-capillary insertion structure. Sattari-Najafabadi et al. ([2017\)](#page-28-28) compared efects of two aspect ratios (ratio of the width to the depth of microchannel) and three confgurations of the inlet junction which includes cross-shaped junction, crossed-shaped T-junction and opposed T-junction on mass transfer efficiency in liquid–liquid droplet fow. Results showed that a longer droplet length, which was formed in microchannel with an aspect ratio two, induced a growth of the stagnant zone and a decline of the wall renewal. Thus, mass transfer efficiency in the microchannel with aspect ratio two was lower than in microchannel with an aspect ratio one. Also, comparing confgurations of the inlet junction revealed that cross-shaped junction had better performance than crossshaped T-junction and opposed T-junction. This is because in cross-shaped junction, continuous phase was in contact with the dispersed phase from both sides; while in other confgurations, the continuous phase touched the dispersed phase only from one side. In addition, the authors extended the experiments to study the efect of hydraulic diameters on mass transfer efficiency (Sattari-Najafabadi et al. [2017b](#page-28-30)). The microchannels were designed with hydraulic diameters of 200 μm, 400 μm and 600 μm. The calculated mass transfer coefficients in three microchnnels revealed that with decreasing hydraulic diameter, the mass transfer efficiency was remarkably increased. On average, the overall mass transfer coefficients were promoted by 112.2% and 124.4% the hydraulic diameter was reduced from 600 μm to 400 μm and 400 μm to 200 μm, respectively.

Confgurations of the main channel have a dominating efect when the droplet is moving along the microchannel. Curvature-based microchannel and obstacle-based microchannel are the two main types used for enhancement of mass transfer efficiency when a droplet is moving along the microchannel (Plouffe et al. [2016a,](#page-27-9) [b;](#page-27-10) Woitalka et al. [2014](#page-28-27); Aoki et al. [2011;](#page-26-28) Darekar et al. [2014](#page-26-29); Özkan and Erdem [2015;](#page-27-27) Yang et al. [2018;](#page-28-32) Zhao et al. [2015b;](#page-29-6) Malsch et al. [2008](#page-27-33)). When a droplet is moving along the microchannel, the changing microchannel structure disturbed the fluid flow and broke up the symmetrical inner circulation in the droplets. Thus, the mass transfer efficiency was greatly enhanced.

Fig. 13 Variations of mass transfer efficiency before and after the droplet across the serpentine section (Qian et al. [2019b\)](#page-27-30)

Figure [13](#page-20-0) presents the variations of the mass transfer efficiency before and after the droplet across the serpentine section (Qian et al. [2019a\)](#page-27-14). It can be seen that before the droplet across the serpentine section, the mass transfer efficiency is about $7\% \sim 8\%$. However, the mixing efficiency reaches 36% when the droplet moves out of the turn. The results quantifed the efect of the main channel structure on the mixing process.

The serpentine section promotes the mass transfer efficiency signifcantly due to the deformed inner circulation in droplet. Figure [14](#page-21-0) presents the inner circulation in droplets observed in straight microchannel and curvature-based microchannel (Malsch et al. [2008](#page-27-33)). It can be seen obviously that droplets moving along the straight microchannel have an axially symmetric inner circulation. The symmetric inner circulation obstructs the concentration redistribution in the radial direction. In contrast, in the curvature-based microchannel, the inner circulation is asymmetric and enables the concentration gradient to be more uniform.

Nonino et al. [\(2009\)](#page-27-34) designed zig-zag, curvilinear and square-wave microchannels with square cross section. Simulations were conducted to determine the mass transfer efficiency in each microchannel and comparisons were made with straight microchannels. The mass transfer efficiency was plotted as a function of Reynolds number. In all microchannels, curvilinear and square-wave microchannels presented better mass transfer efficiency than zig-zag microchannels. Aoki et al. [\(2011\)](#page-26-28) examined extraction rate in microchannels with expansion and contraction structure as shown in Fig. [15.](#page-21-1) Results showed that at a constant total fow rate, 10 ml/min and 20 ml/min, the extraction rate in the microchannel with expansion structure was higher than the one with contraction structure. The authors further studied the relationship between location of the expansion structure

 $d = 1.59$ mm

 L_{2}

 $1/16$ " union tee

 $d = 1.00$ mm

 L_1

 (a)

 (b)

 $d = 1.00$ mm

 L_2

 $1/8$ " union tee

 L_1

 $d = 1.59$ mm

and the extraction rate. The maximum efficiency was achieved in the specifc location of the expansion near the outlet. The results also indicated that with a sudden change of the microchannel dimension near the outlet can re-activate the inner circulation in droplets which may contribute to the improved mass transfer efficiency. Darekar et al. (2014) (2014) carried out extraction experiments to quantify the overall mass transfer coefficient for various conditions. A T-junction serpentine microchannel and a split and recombine microchannel were used in the experiments as shown in Fig. [16.](#page-22-0) The overall mass transfer coefficient in the two microchannels was compared at the same residence time, the same Reynolds number and the same average velocity. Results showed that only at the same residence time, the mass transfer coefficient in the T-junction serpentine microchannel was higher than in the split and recombine microchannels. At the same Reynolds number and the same average velocity, the split and recombine microchannels had better performance. The authors suggested that comparison of mass transfer efficiency based on average velocity was more reasonable. This was argued as the average velocity is directly linked to the energy dissipation which is another important index for evaluation of the systems. Özkan and Erdem ([2015](#page-27-27)) conducted simulations to identify the mass transfer efficiency in sinusoidal microchannels as shown in Fig. [17.](#page-22-1) Mass transfer efficiency in six different microchannels including various channel curvature and cross section area was calculated. Results showed that microchannels with smaller radius and smaller cross section area provided higher mass transfer efficiency. The decreased microchannel size provided wider dispersion length diference, more frequent velocity change and vertical trajectory variation of particles. All of these were greatly enhancing the mass transfer efficiency. Plouffe et al. $(2016a, b)$ $(2016a, b)$ $(2016a, b)$ $(2016a, b)$ conducted experiments to study mass transfer efficiency in various microchannels which were named SZ, TG, Venturi, Sickle and Spade as shown in Fig. [5](#page-8-1). It is worth noting that not the overall mass transfer coefficients were compared in diferent microchannels but the Damköhler numbers were compared. Based on diferent Damköhler numbers, the best and the worst mass transfer rates were achieved by the Sickle microchannel and TG microchannels, respectively.

In addition, microchannel structures which promote the mass transfer efficiency both in the droplet formation process and droplet movement along the microchannel have been proposed. Bai et al. ([2018\)](#page-26-30) performed experiments for analyzing the mass transfer efficiency in cross-shaped microchannel. However, due to the high viscosity and small diffusion coefficient of the ionic liquid, which was used in their experiment, the cross-shaped microchannel presented poor mass transfer efficiency. To enhance the mass transfer efficiency, two methods were adopted by the author. One method was to change the way of droplet formation, and accordingly the cross-shaped junction microchannel was

Fig. 17 Microchannels designed by Özkan and Erdem ([2015\)](#page-27-27)

replaced by T-junction and Y-junction. The other method was to change the way of droplet movement along the microchannel, and then the straight microchannel was replaced by meandering microchannel and deforming microchannel. Finally, the authors combined the two methods and proposed the Y-deforming microchannel for achieving excellent mass transfer performance. The combined structure also was adopted by Yang et al. ([2018](#page-28-32)). The authors studied the mass transfer efficiency in T-junction microchannel and sinusoidal microchannel, respectively. Based on the results, an optimized microchannel structure was proposed which combined a T-junction inlet with a sinusoidal microchannel. This optimized structure combined twirling efect, dean

Fig. 18 The overall volumetric mass transfer coefficient in function of the total flow rate $(Q_d = Q_c)$

vortices and droplet deformation efect together. Thus, the mass transfer efficiency was significantly promoted.

3.3.2 Efect of fow rate

The increase of the total flow rate leads to an increase of the droplet velocity. With higher droplet velocity, the intensifcation of the inner circulation is more pronounced and the mass transfer efficiency is significantly improved. Figure 18 summarizes the over volumetric mass transfer coefficient as a function of the total fow rate in published literatures which all have the same hydraulic diameter of 400 μm. It can be seen that with an increase of the total flow rate, the overall volumetric mass transfer coefficient increases accordingly whether in the droplet regime or the parallel regime. However, it should be emphasized that in the droplet fow regime, the overall volumetric mass transfer coefficient increases with a high rate. When transiting to the parallel regime, the rate of increase reduces. This highlights the superiority of the droplet in mass transfer performance due to the specifc interfacial area and intense inner circulation.

In addition, it can be seen from Fig. [18](#page-23-0) that the overall volumetric mass transfer coefficient measured by Dessimoz et al. ([2008](#page-26-19)) is much higher than that measured by Sattari-Najafabadi et al. ([2017\)](#page-28-28), although the same liquid (hexane)–liquid (water) system is used in their experiment. Two possible reasons may be the amount of the acid contained in the oil phase and the deviation induced by the specifc interfacial area. In experiment conducted by Sattari-Najafabadi et al. ([2017\)](#page-28-28), the organic phase was n-hexane with 0.5 M acetic acid. While in experiment conducted by Dessimoz et al. ([2008](#page-26-19)), the organic phase was n-hexane containing 0.6 M trichloroacetic acid. The increase of the acid concentration led to the decrease of the interfacial tension. The increased interfacial movement promoted the mass transfer process. Moreover, according to Sattari-Najafabadi et al. ([2017\)](#page-28-28), the droplet cap was considered as two hemispheres with the radius equal to the microchannel width. However, the radius of droplet cap in Dessimoz et al. ([2008](#page-26-19)) was calculated by the Brethertons law (Bretherton [1961\)](#page-26-26). The diferences induced the relative error for calculating the specifc interfacial area which directly led to the deviation on the overall volumetric mass transfer coefficient.

Moreover, at constant total flow rate, the dispersed phase fraction ε_d (0 < ε_d < 1), which is defined as Eq. [\(8](#page-23-1)), has an effect on mass transfer efficiency.

$$
\varepsilon_{\rm d} = \frac{u_{\rm d}}{u_{\rm total}},\tag{8}
$$

where u_d and u_{total} represent the dispersed phase velocity and total velocity, respectively. It should be noted that the noslip velocity between phases is assumed when using Eq. [\(8](#page-23-1)). Generally, the actual droplet velocity is higher than the total velocity (Salim et al. [2008](#page-28-16); Darekar et al. [2014](#page-26-29); Yagodnitsyna et al. [2016](#page-28-34)).The increase of the dispersed phase fraction leads to an increase of the droplet length. The maximum mass transfer efficiency only achieved at a suitable droplet length. Tice et al. ([2003](#page-28-35)) studied the relationship between droplet length and mass transfer efficiency experimentally. The droplet was set to move along the microchannel with a constant velocity of 50 mm/s. Diferent droplet length was achieved by adjusting the dispersed phase fraction. For analysis of the mass transfer efficiency, marker was added in dispersed phase and the uniformity of the marker concentration in droplets was measured. Results showed that the maximum mass transfer efficiency was achieved at the dispersed phase fraction 0.3. In addition, Wang et al. ([2015](#page-28-33)) carried out simulations to study the relationship between droplet length and mass transfer efficiency. Results showed that only for the dimensionless droplet length less than 2, fast mixing could be achieved. The best mass transfer efficiency was obtained when the droplet length was comparable with the microchannel width. In the research conducted by Qian et al. ([2019](#page-27-31)), the dimensionless droplet lengths were all higher than two, while the fast mixing was also achieved. This was mainly caused due to the selection of the cross-shaped junction and the initial distribution of the dispersed phase and the continuous phase. For most researches using the cross-shaped junction, the dispersed phase and the continuous phase are injected in the microchannel through the horizontal channel and the vertical channel, respectively (Cao et al. [2018;](#page-26-17) Sattari-Najafabadi et al. [2017a](#page-28-28); Bai et al. [2018](#page-26-30)). However, the initial distribution of the dispersed phase and continuous phase presented in Ref. (Qian et al. [2019c\)](#page-27-31) was totally opposite. The dispersed phase was injected through the vertical inlet and the continuous phase was injected into the microchannel through the horizontal one. This approach **Table 8** Relative error between the data obtained in experiments and data predicted by Eqs. ([9](#page-24-0)) to ([12](#page-24-2)) (Eain et al. [2015](#page-26-32))

made the best use of the inner circulation when the droplet moving through the microchannel. Therefore, the best mass transfer performance can be achieved without restriction the droplet length.

3.4 Energy dissipation

An ideal condition for enhancement of mass transfer performance should consider not only the mass transfer efficiency but also the energy dissipation. Thus, the balance between mass transfer efficiency and energy dissipation should be considered seriously. Pressure drop is adopted as an indicator for the assessment of energy dissipation (Nonino et al. [2009](#page-27-34); Lemenand et al. [2013](#page-27-35)). The higher velocity, the more complex structure of microchannels and the smaller microchannel dimensions all lead to a higher pressure drop. Salim et al. (Salim et al. [2008\)](#page-28-16) investigated water–oil two-phase fows in microchannels with two diferent hydraulic diameters. Pressure drops at various flow rates were measured using the homogeneous and Lockhart–Martinelli models. Results indicated that pressure drops depend closely on the fow rates, the phase which was the frst injected and microchannel material. When oil was saturated initially in microchannels, the pressure drop increased at low water superficial velocities and then decreased sharply. After the water superfcial velocities exceeded 10 cm/s, the pressure drop increased almost linearly with water superfcial velocities. However, with water initially saturated in microchannels, the pressure drop always increased with oil superficial velocity. Similar results were also found by Tsaoulidis et al. [\(2013](#page-28-20)). Kashid and Agar [\(2007](#page-27-17)) carried out experiments to study the hydrodynamics of water–cyclohexane two-phase flow. Pressure transducers were placed at the inlet and downstream of the microchannel to record the pressure variation for the two-phase flow. Pressure behaviors observed at different droplet velocities and capillary dimensions were plotted. Results indicated that the pressure drop increased with increasing droplet velocity and decreasing capillary dimensions. Furthermore, correlations were proposed for pressure drop predictions along the microchannel as shown in Eqs. (9) and (10).

$$
\Delta P_{\text{WOF}} = \frac{L}{L_{\text{U}}} \left(\left[\frac{8u_{\text{d}} \nu \alpha L_{\text{U}}}{R^2} \right] + \left\{ \frac{8u_{\text{c}} \nu (1 - \alpha) L_{\text{U}}}{R^2} \right\} \right) + \frac{2L - L_{\text{U}}}{L_{\text{U}}} \left\langle \frac{2\sigma}{R} \cos \theta \right\rangle, \tag{9}
$$

$$
\left(\frac{\Delta P}{L}\right)_{\text{WF}} = \left(\frac{\alpha}{1 - \left((R - h)/R\right)^4}\right) \left(\frac{\Delta P}{L}\right)_{\text{c}},\tag{10}
$$

where L, L_{U} , R and h represent the capillary length, droplet unit length, radius of capillary and flm thickness, respectively. μ and σ represent the fluid viscosity and interfacial tension. ν and α represent the droplet velocity and dispersed phase length fraction, respectively. *θ* represents the contact angle. ΔP_{WOF} and ΔP_{WF} represent the pressure drop without flm and pressure drop with flm, respectively. Comparing with data collected in the experiment, the correlation with a flm showed a better agreement. Jovanovic et al. [\(2011](#page-27-36)) studied the pressure drop in water–toluene and ethylene glycol/water–toluene systems. Two models, which were called stagnant flm model and moving flm model, were proposed for predicting the pressure drop.

$$
\Delta P_{\rm SF} = \left[\frac{8u_{\rm d}v\alpha L}{\left(R - h\right)^2}\right] + \left\{\frac{8u_{\rm c}v(1 - \alpha)L}{R^2}\right\} + \left\langle\frac{L}{L_{\rm U}}7.16(3Ca)^{2/3}\frac{\sigma}{d}\right\rangle,\tag{11}
$$

$$
\Delta P_{\text{MF}} = \left[\frac{4v\alpha L}{(R^2 - (R - h)^2)/u_c + 0.5(R - h)^2/u_d} \right] + \left\{ \frac{8u_c v(1 - \alpha)L}{R^2} \right\} + \left\{ \frac{L}{L_U} 7.16(3Ca)^{2/3} \frac{\sigma}{d} \right\},
$$
\n(12)

where L, L_{U} , R, d and h represent the capillary length, droplet unit length, radius of capillary, diameter of capillary and film thickness, respectively. μ and σ represent the fluid viscosity and interfacial tension. ν and α represent the droplet velocity and dispersed phase length fraction, respectively. *θ* represents the contact angle. ΔP_{SE} and ΔP_{MF} represent the pressure drop with stagnant flm and pressure drop with moving flm, respectively. The models were compared with the liquid–liquid pressure drop studies found in literature. Finally, the stagnant film model was found to be more adequate to predict pressure drop. The proposed models in Kashid and Agar ([2007\)](#page-27-17) and Jovanovic et al. ([2011\)](#page-27-36) both considered that the pressure drop across the length of the capillary comprised three parts: pressure drop caused by the dispersed phase expressed in Eqs. (9) (9) , (11) (11) and (12) (12) by the frst term, the pressure drop caused by the continuous

Fig. 19 Overall volumetric mass transfer coefficients in different microchannels in n-butanol/aqueous NaOH system plotted by Ploufe et al. [\(2016](#page-27-9))

phase expressed in Eqs. (9) (9) , (11) (11) and (12) (12) (12) by the second term and pressure drop caused by the interface expressed in Eqs. (9) (9) , (11) (11) and (12) by the third term.

To validate the accuracy of the pressure drop models proposed by Kashid and Agar [\(2007\)](#page-27-17) and Jovanovic et al. ([2011](#page-27-36)), Eain et al. ([2015](#page-26-32)) conducted comprehensive experiments in diferent liquid–liquid two-phase systems which included a wide range of Reynolds number, $1.45 < Re < 97.48$, and Capillary number, $4.49 \times 10^{-5} < Ca < 0.0098$. Table [8](#page-24-4) presents the summary of the relative error between the experimental data obtained in diferent systems and data predicted by Eqs. (9) (9) to (12) .

It can be seen that the data predicted by the model without flm, Eq. ([9](#page-24-0)), greatly deviate the experimental data due to the assumption of without flm. In this assumption, the contact angle is considered to be constant when the droplet across the microchannel. Moreover, data predicted by two models, Eqs. (11) (11) and (12) (12) , show a highly similarity. This is attributed to the assumption that the pressure drop caused by the continuous phase and the interface account for over 90% of the total pressure drop. While the two terms in Eqs. ([11\)](#page-24-1) and [\(12](#page-24-2)) keep the same. Finally, Eain et al. ([2015\)](#page-26-32) pointed out that none of the proposed models gave a relatively accurate prediction within $\pm 15\%$ of the relative error. The main problem lies in the methods used to predicted the interface pressure drop.

Based on pressure drop, the energy dissipation rate can be quantified as shown in Eq. (13) (13) (13) .

$$
\varepsilon_{\Delta P} = \frac{u\Delta P}{\rho L}.\tag{13}
$$

Ploufe et al. ([2016](#page-27-9)) plotted the overall mass transfer coefficients versus the energy dissipation rate as shown in Fig. [19.](#page-25-1) It is obvious that higher mass transfer efficiency is always accompanied by a higher energy dissipation.

4 Conclusion

Extensive efforts have been made for exploring the hydrodynamics of liquid–liquid two-phase fow in microchannels and promoting its industrial applications. However, there are still many aspects deserve to be considered in further research.

Liquids involved in experiments and simulations are mainly Newtonian liquids. Thus, researches focused on non-Newtonian liquids should be performed for a comprehensive understanding of liquid–liquid two-phase fow; Experiments and simulations are carried out mostly at room temperature. However, some liquid properties are highly sensitive to temperature. Thus, variation of temperature should be considered; Researches on liquid–liquid two-phase fow are widely studied; while, the uniform criteria such as for distinguishing the fow pattern transition and predicting the droplet characteristic are still inadequate. Thus, data at diferent conditions should be collected and databases should be set up. Scaling laws and general correlations need to be proposed.

The inner circulations existed in a droplet can be divided into two parts: the main circulation which is induced by the interaction with the wall and the minor circulation which is induced by the interaction with the continuous phase. Whether the correlations are existed between two-circulation path and the droplet length may deserve to further consider. In addition, the flm thickness plays a signifcant role to calculate the specifc interfacial area. Although the widely use of the Brethertons law, methods for determining the flm thickness need to be further developed.

Simulations performed for studying the mass transfer performance in liquid–liquid two-phase fow mainly adopt non-reaction systems and the mass transfer efficiency is represented by the distribution uniformity of tracers/species/ scalars in droplets. No better guidance is provided when reactions are involved. Thus, more effective simulation methods should be developed to better adopt actual working conditions; Mass transfer performance is widely studied in stable flow patterns such as droplet flow and parallel flow. However, in actual working conditions, flexible flow conditions may increase the instability of fuid fow and cause diferent fow patterns. Thus, mass transfer performance in transition fow patterns should be studied.

Energy dissipation is an important parameter for evaluating the overall efficiency of a microfluidic system and it has been widely studied in turbulent fow. However, in laminar fow, there are less reports. Researches should be extended further to determine the balance between energy dissipation and mass transfer efficiency. In addition, when droplets moving through the microchannel, it can be analogous to an electric circuit and the droplet can be considered as the resistance. In a particular microchannel length, the pressure drop may be infuenced by not only the droplet length and droplet unit length, but also the numbers of droplet. This question needs to be further clarifed.

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