**ORIGINAL PAPER**



# **Auxiliary power through marine waste heat recovery using**  a CO<sub>2</sub>-organic cascading cycle

**Subha Mondal1 · Soumitra Datta2 · Sudipta De2**

Received: 25 June 2019 / Accepted: 28 February 2020 / Published online: 12 March 2020 © Springer-Verlag GmbH Germany, part of Springer Nature 2020

### **Abstract**

An appreciable part of primary energy input to a marine diesel engine is rejected as waste heat. Thus, through marine diesel engine waste heat recovery signifcant amount of secondary energy can be produced to satisfy the auxiliary power requirement of the marine ship. In present study, a  $CO<sub>2</sub>$ -organic fluid cascading cycle is considered for the utilization of the waste heat released by the marine diesel engine. R290, R600 and R1233zd (E) are considered as the working fuids of the bottoming cycle for their lower global warming potentials. The analysis revealed that power output of the cascading cycle is comparable to that of the baseline transcritical  $CO<sub>2</sub>$  power cycle. However, for similar power output, operating pressure in the flue gas- $CO<sub>2</sub>$  heat recovery unit of the transcritical  $CO<sub>2</sub>$  power cycle is significantly higher compared to that of the cascading cycle. Thus, possible leakage due to very high operating pressure of a conventional  $CO<sub>2</sub>$  power cycle can be addressed by using the cascading system. Bare module costs per unit power output of cascading cycles are also signifcantly smaller. It is also apparent from the study that the marine diesel engine waste heat recovery through the  $CO<sub>2</sub>$ -organic cascading cycle would lead to 8–9.5% annual fuel saving. Reduced fuel consumption will also result in lesser  $CO_2$  emission from the marine ship.

#### **Graphic abstract**



Extended author information available on the last page of the article

#### Keywords Marine diesel engine · Waste heat · CO<sub>2</sub> power cycle · CO<sub>2</sub>-organic cascading · Bare module cost

#### **List of symbols**



#### **Greek symbols**



#### **Subscripts**





TRC Transcritical Rankine cycle

# **Introduction**

About three hundred million metric tons of fossil fuel is consumed by ocean-going ships in a year (Corbett and Koehler [2003](#page-12-0)). Thus, consumption of fossil fuels and emission from these ships are issues of great concern. The cost associated with marine transport is also increasing steadily due to escalating fuel prices. Recently, it was reported by Mondal and De ([2020](#page-13-0)) that conversion of readily available low and medium grade heat into power and other energy utilities would reduce fossil fuel consumption and greenhouse gas emission simultaneously. Appreciable amount of thermal energy is carried away by exhaust fue gas, scavenging air cooling water and jacket cooling water of any marine diesel engine. This waste heat may be utilized to produce some secondary energy. Thus, there is a great scope in a marine diesel engine to reduce both fuel consumption and associated emission by cutting down fuel consumption by adopting an efficient waste heat recovery scheme.

Recent studies indicated that organic Rankine cycle is one of the emerging technologies to generate power from low and medium grade heat. Braimakis and Karellas ([2018](#page-12-1)) analyzed the performance of regenerative organic Rankine cycles using hot pressurized water as the heat source. Baik et al. ([2013](#page-12-2)) reported that while utilizing low-temperature geothermal heat, the transcritical ORC with R125 yielded higher power output compared to the power outputs of subcritical ORCs using R134a, R245fa and R152a as working fuids. Saleh et al. ([2007](#page-13-1)) pointed out that in an ORC a supercritical working fuid should be used to maximize the heat transfer from the low-temperature heat carrier.

Organic fash cycle (OFC) is also emerging as a possible technology for low-grade waste heat utilization due to the absence of pinch limitation in the heat recovery unit. The study conducted by Ho et al. [\(2012\)](#page-12-3) revealed that the utilization efficiency of an organic flash cycle (OFC) was comparable to that of a basic ORC. Mondal and De [\(2017a\)](#page-13-2) reported that an OFC would be economically preferred over a  $T-CO<sub>2</sub>$  power cycle for producing power from low-grade waste heat of the flue gas, free from  $SO_2$ . To reduce irreversibility of the OFC, Mondal and De [\(2017b](#page-13-3)) proposed to replace the low-pressure throttle valve of the OFC by an ejector that entrained the working fuid exiting the evaporator of a refrigeration cycle. Mondal et al. ([2018\)](#page-13-4) also incorporated an ejector in an OFC to increase the turbine power output. Mondal and De ([2019](#page-13-5)) showed that the possibility of accidental fame propagation with R600 could be reduced appreciably by using a mixture of R245fa and R600 as the working fuid of an OFC. The GWP of the mixture was also smaller than the GWP of pure R245fa.

 $CO<sub>2</sub>$  is a nonflammable, non-toxic and environment friendly working fluid. Thus,  $CO<sub>2</sub>$ -based power cycle would be preferred for low-grade heat recovery. Guo et al. ([2010\)](#page-12-4) showed that power output of a low-grade heat-driven  $T-CO<sub>2</sub>$ power cycle had been 3–7% higher compared to an organic Rankine cycle using R245fa as the working fuid. Mondal and De  $(2015a)$  proposed a regenerative T-CO<sub>2</sub> power cycle that utilized the heat of the turbine bleed gas to preheat the CO<sub>2</sub> stream entering the heat recovery unit. Mondal and De  $(2015b)$  $(2015b)$  revealed that specific power output and 2nd law efficiency of a low-grade heat-driven supercritical  $CO<sub>2</sub>$  power cycle could be enhanced by increasing the number of compression stages along with intercooling.

In recent time, substantial research is going on marine diesel engine waste heat recovery. Song et al. ([2015\)](#page-13-6) showed that an ORC can be driven economically by the waste heat released by a marine diesel engine. Yang and Yeh [\(2015\)](#page-13-7) demonstrated that while recovering waste heat from a large marine diesel engine, the ORC with R1234yf would exhibit superior thermo-economic performance compared to those of the ORCs using R1234ze, R152a, R600a and R245fa as working fuids. Yang [\(2016](#page-13-8)) conducted the optimization of a marine diesel engine waste heat recovery system to select the best possible working fuids for the transcritical ORC. According to his analysis, R236fa appeared as the best performing working fuids out of six considered working fuids. Yang ([2018](#page-13-9)) also evaluated the payback period for ORC-based marine engine waste heat recovery system that utilized mixtures of diferent working fuids instead of a pure working fuid. Yang and Yeh [\(2017\)](#page-13-10) proposed a

new parameter, namely "net power output index" to evaluate the economic performance of the marine diesel engine exhaust-driven transcritical organic Rankine cycle (TORC). In many of the recent studies,  $CO<sub>2</sub>$ -based power cycles were considered for engine waste heat recovery mainly due to nonfammable, non-toxic and environment friendly nature of  $CO<sub>2</sub>$ .  $CO<sub>2</sub>$  is also readily available at a lower cost. It is also preferred for engine waste heat recovery as it is chemically stable even at higher temperature (Song et al. [2018](#page-13-11)). Shi et al. ([2017](#page-13-12)) experimentally evaluated the performance of an engine waste heat-driven  $T-CO<sub>2</sub>$  power cycle. Chen et al. ([2005](#page-12-7)) reported that the engine waste heat could be used as the input to a  $CO_2$ -based power cycle to reduce the fuel consumption of a vehicle.

Most of the previous studies presented marine diesel engine waste heat recovery by using either organic Rankine cycle or  $CO_2$ -based power cycles. It should be noted that operating pressure in the heat recovery unit of the  $CO<sub>2</sub>$ -based power cycle should be signifcantly high to ensure an acceptable thermal efficiency. Most of the low GWP organic fluids are either fammable or commercially unavailable. Thus, the selection of suitable working fuid for waste heat recovery is a challenging task. By using a  $CO<sub>2</sub>$ -organic cascading cycle, the high operating pressure in the heat recovery unit of the  $CO<sub>2</sub>$ -based power cycle can be decreased. The risk of flame propagation with the cascading cycle will also be less as the requisite mass of organic working fuid is signifcantly smaller for the cascading system. Thus, in the present study, cascading between a  $CO<sub>2</sub>$  power cycle and a transcritical ORC is considered for the marine diesel engine waste heat recovery to address the above issues. The cycle is designated as  $CO_2$ -organic cascading cycle, with  $CO_2$  cycle as the topping one. R600, R290 and R1233zd (E) are considered as the diferent alternative working fuid of the bottoming cycle of the cascading due to their lower GWP. The proposed system is analyzed thermodynamically considering a regenerative  $T-CO<sub>2</sub>$  power cycle as the baseline system.

In the proposed waste heat recovery scheme, to maximize the thermal efficiency,  $CO<sub>2</sub>$  is heated to a temperature  $(-270 \degree C)$  which is closest to the inlet temperature  $(-290 \degree C)$  of the engine exhaust gas. The mass flow rate of  $CO<sub>2</sub>$  is estimated from the energy balance of the flue gas- $CO<sub>2</sub>$  heat recovery unit (FGCHRU). It should be noted that the entire mass of jacket cooling water is utilized to preheat the  $CO<sub>2</sub>$  before entering the FGCHRU. At a lower operating pressure of the FGCHRU (i.e.,  $<$  13 MPa), heat available with the mass of jacket cooling water is not sufficient to preheat  $CO<sub>2</sub>$  from pump exit condition to the inlet condition of the FGCHRU. Thus, for lower pressures of the FGCHRU, a small mass of scavenging air cooling water is directed through another heater to preheat the  $CO<sub>2</sub>$  stream from pump exit condition to the inlet condition of the heater recovering the heat of the jacket cooling water. Some mass

<span id="page-3-0"></span>**Table 1** Waste heat from a large marine diesel engine (Yang [2016](#page-13-8))

Waste heat source	Mass flow rate $(kg/s)$	Inlet tem- perature $(^{\circ}C)$	Minimal exit temperature °C)
Exhaust gas	148.51	290	138
Cylinder jacket cooling water	158	90	74
Scavenge air cooling water	162.5	76	36

of scavenging air cooling water is also utilized to preheat the organic fluid before entering into the  $CO<sub>2</sub>$ -organic fluid heat recovery unit (COFHRU). Even after these distributions, heat carried with a certain mass fraction of the scavenging air cooling water remains unutilized. In short, in the present study, fowing mass of cylinder jacket cooling water as well as scavenging air coiling water are split into diferent streams and directed through three diferent preheaters to maximize the heat recovery from these sources.

## **System description**

In the present work, exhaust gas, cylinder jacket cooling water and scavenge air cooling water of a large marine diesel engine are considered as waste heat sources. Heat content along with the inlet and outlet temperature of the above mentioned streams are summarized in Table [1](#page-3-0) (Yang [2016\)](#page-13-8).

Layout of proposed  $CO_2$ -organic fluid cascading cycle, utilizing waste heat from a marine engine is presented in Fig. [1.](#page-3-1) Figure [2a](#page-4-0), b is T-S diagrams for the topping transcritical  $CO<sub>2</sub>$  cycle and bottoming transcritical ORC, respectively. The sequence of waste heat recovery by the  $CO<sub>2</sub>$  is according to the available temperature.  $CO<sub>2</sub>$  stream exiting the pump at state-1 recovers heat from scavenging air cooling water, jacket cooling water and exhaust fue gas of a large marine diesel engine in Heater-A (i.e., process 1–2), Heater-B (i.e., process 2–3) and flue gas- $CO<sub>2</sub>$ heat recovery unit (FGCHRU) (i.e., process 3-4), respectively. The intention of the present study is to heat the  $CO<sub>2</sub>$ stream close to the fue gas inlet temperature to ensure the higher thermal efficiency. Thus the  $CO<sub>2</sub>$  stream is heated to 270 °C by the heat of exhaust fue gas stream. Mass fow rate of  $CO<sub>2</sub>$  stream is estimated from the energy balance of the FGCHRU. The  $CO<sub>2</sub>$  mass at state-4 enters the expander (i.e., the turbine) to produce the power output. The temperature of  $CO<sub>2</sub>$  stream at the exit of the turbine (i.e., state-5) is appreciably high. Thus, this  $CO<sub>2</sub>$  is cooled (process 5–6) in a  $CO<sub>2</sub>$ -organic fluid heat recovery unit (COFHRU) by exchanging heat to any one of the three selected organic fuids. The organic fuid exiting the COFHRU (at state-13) also expands (i.e., process 13–14) in a turbine to produce some power output. The organic fuid also recovers heat



<span id="page-3-1"></span>**Fig. 1** Layout of the  $CO_2$ -organic cascading cycle

from the scavenging air cooling water in heaters C (i.e., process 11–12) before entering the COFHRU. Organic fuid mass fow rate is estimated from the energy balance of the COFHRU.

It should be noted that at higher operating pressures (i.e., above 13 MPa) of the FGCHRU  $CO<sub>2</sub>$ , mass flow rate reduces appreciably and available mass of jacket cooling water is slightly higher than the mass required to preheat the  $CO<sub>2</sub>$ from pump exit condition (i.e., state 1) to the inlet condition of the FGCHRU (i.e., state 3). Thus, Heater-A is to be removed from the system layout if the pressure in the FGCHRU is above 13 MPa. Otherwise, both heaters (i.e., Heater-A and Heater-B) are required.

Selection of suitable working fuid for the bottoming organic cycle is critical as use of the chlorofuorocarbon (CFCS) and most of the hydro-chlorofuorocarbons (HCFCs) are restricted due to either ozone-depleting nature or higher values of GWP. HFCs are to be phased out soon according to Kigali amendment to the Montreal protocol. In present study, two hydrocarbons (R290, R600) and one HFO (R1233zd (E)) refrigerant are considered as the working fuid of the bottoming cycle due to lower values of GWP as listed in Table [2](#page-4-1). As turbine exit temperature of topping  $CO<sub>2</sub>$ cycle varies between 190 and 235 °C, the bottoming organic cycle can be heated in transcritical mode.



<span id="page-4-0"></span>**Fig. 2** T-S diagram for **a** topping  $CO_2$  cycle of the cascading. **b** Bottoming transcritical ORC of the cascading

Layout of the engine waste heat-driven baseline  $T-CO<sub>2</sub>$ power cycle is presented in Fig. [3](#page-5-0). In the baseline  $T-CO<sub>2</sub>$ power cycle,  $CO<sub>2</sub>$  stream exiting the jacket cooling water is heated in the regenerator (i.e., process 13–14) by the heat of the  $CO_2$  stream exiting the turbine.  $CO_2$  mass flow rate for the baseline  $T-CO<sub>2</sub>$  power cycle is also estimated from the energy balance of the FGCHRU. For better representation of operating conditions, terminal temperature diferences in diferent heat recovery units are presented in Table [3](#page-5-1).

## **Mathematical modeling**

In initial part of the mathematical modeling, from the mass and energy balance of each of the equipment, equations are developed to represent the energetic performances of the waste heat recovery scheme. Thermodynamic and transport properties of various working fuids are evaluated using REFPROP-9.1 (Lemmon et al. [2013](#page-12-8)). During the modeling, following assumptions are considered to simplify the analysis:

- 1. All the equipments are steady fow devices.
- 2. Turbine isentropic efficiency is 90%.
- 3. Isentropic efficiencies of the pump as well as the compressor are assumed to be 85% each.
- 4. Ambient condition is specified by 100 kPa and 20 °C.
- 5. Maximum permissible fue gas velocity is 15 m/s.
- 6. All heat exchangers are assumed to have shell-and-tube confguration with multi pass arrangement.
- 7. During heat exchanger design fue gas thermo-physical properties are assumed to be same as air.

#### **Thermodynamic modeling**

Mass flow rate  $CO<sub>2</sub>$  through the topping cycle can be evaluated from the energy balance of the FGCHRU as follows:

$$
m_{\text{CO2}} = \frac{m_{\text{g}}c_{\text{Pg}}(T_{\text{g,i}} - T_{\text{g,o}})}{(h_4 - h_3)}
$$
(1)

Mass flow rate organic working fluid through the bottoming cycle can be evaluated from the energy balance of the COFHRU as presented in Eq. [2:](#page-4-2)

<span id="page-4-2"></span>
$$
m_{\rm r} = \frac{m_{\rm CO2}(h_5 - h_6)}{(h_{13} - h_{12})}
$$
 (2)

Power outputs from topping cycle turbine and bottoming cycle turbine are estimated in Eqs. [3](#page-5-2) and [4,](#page-5-3) respectively.

<span id="page-4-1"></span>





<span id="page-5-0"></span>**Fig. 3** Layout of baseline Regenerative  $T-CO<sub>2</sub>$  power cycle

<span id="page-5-1"></span>**Table 3** Terminal temperature diferences in HRUs

<b>FGCHRU</b>	48	20	
Heater-A	10	Variable	
Heater-B	Variable	10	
$Heater-C$	30	10	
<b>COFHRU</b>	10	20	
<b>FGCHRU</b>	10	20	
Heater-C	10	Variable	
Heater-D	Variable	10	
Regenerator	Variable	Variable	
		Heat recovery unit $\Delta t_{\text{LTE}}$ (°C) $\Delta t_{\text{HTE}}$ (°C)	

$$
W_{\text{t,tur}} = m_{\text{CO2}}(h_4 - h_5) \tag{3}
$$

$$
W_{b, \text{tur}} = m_{\text{r}} \left( h_{13} - h_{14} \right) \tag{4}
$$

Equations [5](#page-5-4) and [6](#page-5-5) are representing pump power inputs of the topping cycle and the bottoming cycle, respectively.

$$
W_{t, pump} = m_{CO2}(h_1 - h_7)
$$
 (5)

 $W_{\text{b,pump}} = m_{\text{r}} (h_{11} - h_{15})$  (6)

Now, net power outputs of the topping cycle as well as the bottoming cycle are evaluated as follows:

$$
W_{t, \text{NET}} = |W_{t, \text{tur}}| - |W_{t, \text{pump}}| \tag{7}
$$

$$
W_{\rm b,\,NET} = \left| W_{\rm b, tur} \right| - \left| W_{\rm b,pump} \right| \tag{8}
$$

Now, power output of the cascading cycle

$$
W_{\text{Cascade}} = W_{\text{t, NET}} + W_{\text{b, NET}} \tag{9}
$$

#### **Heat exchanger area estimation**

Heat exchangers are divided in "*N*" number of subsections for taking care of varying transport property of working fuids with varying temperature. Enthalpy drops across each of the subsections are assumed to be equal. Now area of any one of the subsections can be evaluated as follows:

<span id="page-5-6"></span>
$$
A_{\text{exh,j}} = \frac{Q_{\text{exh,j}}}{U_{\text{exh,j}} F \Delta T_{\text{mean}, \text{exh,j}}}
$$
(10)

In Eq. [10,](#page-5-6) Δ $T_{\text{mean,exh,j}}$  is LMTD (logarithmic mean temperature diference) for the counter fow arrangement and *F* is correction factor to take care of multi passes. Elemental heat duty of Eq. [10](#page-5-6) can be estimated by Eq. [11.](#page-5-7)

<span id="page-5-7"></span>
$$
Q_{\text{exh,j}} = \frac{m_{\text{WF}} \left| (h_{\text{i}} - h_{\text{o}}) \right|}{N} \tag{11}
$$

In Eq. [11,](#page-5-7)  $h_i$  and  $h_o$  are enthalpies of working fluid in inlet and exit of the heat exchanger, respectively.

Overall, heat transfer coefficient of each of the heat exchanger element can be expressed as

$$
U_{\text{exh,j}} = \frac{1}{1/\alpha_{\text{tube}} + 1/\alpha_{\text{shell}}}
$$
\n(12)

<span id="page-5-2"></span> $\alpha_{\text{tube}}$  and  $\alpha_{\text{shell}}$  are tube side and shell side convective heat transfer coefficients, respectively. Various correlations considered for convective heat transfer coefficients are summarized in Table [4](#page-6-0).

#### <span id="page-5-3"></span>**Bare module cost estimation**

<span id="page-5-4"></span>In order to estimate the cost of the equipment for preliminary design, the cost equations proposed by Turton et al. ([2013\)](#page-13-14) are employed. Equation used for the purchased cost of individual equipment  $(C_p^0)$  at ambient operating pressure and using carbon steel (CS) construction is as follows:

<span id="page-5-5"></span>
$$
\log_{10} C_p^0 = K_1 + K_2 \log_{10} Z + K_3 (\log_{10} Z)^2
$$
 (13)

Equation of heat transfer coefficient	Fluid	Phase	Heat exchanger
$\text{Nu} = \Bigg\lvert \frac{\binom{\ell_{\rm b}}{8}\text{Re}_{\rm r}~\text{Pr}_{\rm r}}{\binom{\ell_{\rm b}/80.5\left(\text{Pr}_{\rm r}^{\frac{2}{3}}-1\right)+1.07}\Bigg\rvert\binom{C_{\rm pav}}{C_{\rm pv}}\bigg)\binom{\frac{k_{\rm b}}{k_{\rm wall}}}{\binom{\frac{\ell_{\rm w}}{k_{\rm wall}}}\Bigg\rvert}$	Working fluid	Supercritical	<b>FGCHRU</b> <b>COFHRU</b> Heaters A-D
$0.5 \le Pr \le 2000$ $3 \times 10^3 \leq Re \leq 5 \times 10^6$			
$Nu = \left[\frac{\left(\frac{f_b}{8}\right)Re_r Pr_r}{(f_b/8)^{0.5}\left(Pr_r^{\frac{2}{3}} - 1\right) + 1.07}\right]$		$CO2$ vapor	<b>COFHRU</b> $CO2$ cooler
Nu = $0.05Re_{eq}^{0.8}$ Pr sating		Two-phase $CO2$	CO <sub>2</sub> condenser
$R_{\text{eq}} = \text{Re}_{\text{vap}} \frac{\mu_{\text{satvap}}}{\mu_{\text{cation}}} \left( \frac{\rho_{\text{satliq}}}{\rho_{\text{cation}}} \right)^{0.5} + \text{Re}_{\text{liq}}$			
$\text{Re}_{\text{liq}} = G(1-x) \frac{d_i}{\mu_{\text{satliq}}}$			
$\text{Re}_{\text{vap}} = Gx \frac{d_i}{\mu_{\text{satvap}}}$			
$Nu = 0.0131Re0.883Pr0.36$		Organic fluid vapor	Condenser
$4.5 \times 10^5 \le \text{Re} \le 7 \times 10^6$			
$Nu = 0.729 \left( \frac{g \rho_{f(\rho_f - \rho_g)} D_o^3 i'_{fg}}{\mu_f K_r (T_{sat} - T_{wall})} \right)^{1/4}$		Two phase organic fluid	Condenser
Nu = 0.71Re <sup>0.5</sup> Pr <sup>0.36</sup> $\left(\frac{Pr}{Pr_{run}}\right)^{0.25}$	<b>Exhaust Gas</b>	Gas	<b>FGCHRU</b>
$1000 \le Re \le 2 \times 10^5$			
$Nu = 0.023Re0.8Pr0.3$	Jacket cooling water, scavenging air	Liquid	Heaters A.
$Re > 10^4$	cooling water, cooling water		B, C, D, condenser
$0.7 \leq Pr < 160$			

<span id="page-6-0"></span>Table 4 Correlations for estimation of convective heat transfer coefficient (Pioro et al. [2004](#page-13-15); Incropera and Dewitt [2002;](#page-12-10) Kreith and Bohn [1993;](#page-12-11) Cengel and Boles [2006\)](#page-12-12)

<span id="page-6-1"></span>**Table 5** Equipment cost parameters (Turton et al. [2013](#page-13-14))

Equipments	Performance parameters $(Z)$	$K_1$	$K_2$	$K_3$	$B_1$	B <sub>2</sub>	$F_{\rm M}$	$C_1$	$\mathcal{C}_{2}$	$C_3$
<b>FGCHRU</b>	$A_{\text{exh}}$ (m <sup>2</sup> )	4.3247	$-0.303$	0.1634	1.63	1.66	1.4	0.0388	$-0.11272$	0.08183
Heaters A, B, C, D	$A_{\rm sca}, A_{\rm cyl}$ (m <sup>2</sup> )									
Condenser	$A_{\rm con}$ (m <sup>2</sup> )									
<b>COFHRU</b>	$A_{\text{reg}}$ (m <sup>2</sup> )	4.3247	$-0.303$	0.1634	1.63	1.66	1.4	$-0.395$	0.3957	$-0.00226$
Pump	$W_{\text{pump}}$ (kW)	3.3892	0.0536	0.1538	1.89	1.35	$-0.3935$	$-0.395$	0.3957	$-0.00226$
Turbine	$W_{\text{Tur}}$ (kW)	2.7051	1.4398	$-0.1776$	$\theta$		3.4	$\overline{0}$	$\theta$	$\mathbf{0}$

where *Z* is the parameter for capacity and size of the equip-ment as provided in Table [5](#page-6-1).  $K_1$ ,  $K_2$   $K_3$  are the constants, as shown in Table [5](#page-6-1). Since the equipments rarely operate at ambient pressure, pressure factor  $F_p$  is used to take care of elevated operating pressure. The bare module cost for shelland-tube heat exchangers and pump is given by

$$
C_{BM} = C_P^0 (B_1 + B_2 F_P F_M) = C_P^0 F_{BM}
$$
\n(14)

Bare module cost of turbine is expressed as

$$
C_{BM} = C_p^0 F_p F_{BM} \tag{15}
$$

In these equations,  $F_P$ ;  $F_M$  and  $F_{BM}$  are pressure factor, material factor and bare module factor, respectively, constants.  $B_1$  and  $B_2$  are constants as presented Table [5](#page-6-1) (Turton et al. [2013](#page-13-14)).  $F_p$  can be estimate from following equation

$$
\log_{10} F_{\rm p} = C_1 + C_2 \log_{10} (10P - 1) + C_3 (\log_{10} (10P - 1)^2)
$$
\n(16)

 $C_1$ ,  $C_2$  and  $C_3$  are constants whose values are also provided in Table [5.](#page-6-1) In Eq. [16](#page-7-0), *P* is the operating pressure in MPa. Subsequently the total cost of the equipments is obtained by adding the cost of individual equipments used in the system as shown below

$$
C_{\text{Tot}} = \sum \left( C_{\text{BM,eq}} \right) * \frac{\text{CEPCI}_{\text{current year}}}{\text{CEPCI}_{2001}} \tag{17}
$$

In Eq. [17,](#page-7-1) CEPCI is the chemical engineering plant cost index, taking the effect of time on purchased equipment cost into account.

## **Results and discussion**

In the present study, a cascading between  $T-CO<sub>2</sub>$  power cycle and Organic Rankine cycle is considered for the recovery of waste heat rejected by a large marine diesel engine. Results are presented by considering a regenerative  $T-CO<sub>2</sub>$  power cycle as the baseline one.

The mass flow of  $CO<sub>2</sub>$  for the cascading cycle is determined from the energy balance between  $CO<sub>2</sub>$  and exhaust gas in the flue gas- $CO<sub>2</sub>$  HRU (FGCHRU). It can be seen from Fig. [4a](#page-7-2) that the mass flow rate of  $CO<sub>2</sub>$  decreases with an increase in FGCHRU pressure. This can be easily explained from Fig. [4b](#page-7-2). It is observed in Fig. [4b](#page-7-2) that with an increase in pressure of the FGCHRU, both  $h_3$  and  $h_4$  decreases (refer to Fig. [2](#page-4-0)a). However, difference between  $h_4$  and  $h_3$  increases with an increase in pressure of the FGCHRU. Thus, heated mass of  $CO<sub>2</sub>$  reduces as heat released by flue gas is constant.

Power output of the topping cycle of the cascading increases with an increase in FGCHRU pressure as shown in Fig. [5](#page-8-0). The total power is directly proportional to product of mass and the specifc work output. Although the mass flow rate decreases, it is overcompensated by specific work output and thereby increasing the power.

With an increase in topping cycle turbine inlet pressure,  $CO<sub>2</sub>$  mass flow rate decreases as already presented in Fig. [4](#page-7-2)a. Temperature of  $CO<sub>2</sub>$  exiting the turbine of the topping cycle also reduces with an increase in FGCHRU pressure as shown in Fig. [6](#page-8-1). Lower turbine exit temperature of the topping cycle also results in lower turbine inlet temperature for the bottoming ORC. Thus, total heat available for heating the organic fluid of bottoming cycle as well as efficiency of the bottoming cycle reduces. Due to reduction in heat input as well

<span id="page-7-1"></span><span id="page-7-0"></span>

<span id="page-7-2"></span>**Fig. 4**  $\alpha$  CO<sub>2</sub> mass flow rate of the topping CO<sub>2</sub> power cycle versus FGCHRU pressure. **b** State point enthalpy variation with varying pressure in FGCHRU

as thermal efficiency, power output of the bottoming cycle decreases with an increase in FGCHRU pressure as shown in Fig. [7.](#page-8-2)

The total power output of the cascading cycle ultimately increases with an increase in FGCHRU pressure as shown in Fig. [8.](#page-8-3) It is important to note that improvement achieved in total power output of  $CO<sub>2</sub>$ -organic cascading cycle becomes negligible above a certain value of FGCHRU pressure. It is also observed in Fig. [8](#page-8-3) that for a specifed working fuid and FGCHRU pressure, total power output of the cascading cycle increases with an increase in bottoming cycle turbine inlet pressure. However, above a certain value of bottoming cycle turbine inlet pressure, this improvement is almost negligible. Thus, for a specifed pressure of FGCHRU, there exists a turbine inlet pressure of the bottoming cycle above which no appreciable improvement in power output of the cascading cycle occurs.



<span id="page-8-0"></span>**Fig. 5** Power output of the topping CO<sub>2</sub> power cycle versus FGCHRU pressure



<span id="page-8-1"></span>**Fig. 6**  $CO_2$  turbine exit temperature  $(T_5)$  versus FGCHRU pressure

In Fig. [9,](#page-9-0) power outputs of the cascading cycle are compared with the power outputs of the baseline cycle (i.e., the regenerative  $T-CO<sub>2</sub>$  power cycle) for varying FGCHRU pressure. R290, R600 and R1233zd (E) are working fuids considered for the bottoming cycle of the  $CO<sub>2</sub>-Organic$ cascading cycle. For all cascading systems, power outputs are considered at the bottoming cycle turbine inlet pressure above which power output of a cascading cycle becomes almost insensitive to the varying bottoming cycle turbine inlet pressure. The total power output of the cascading cycle increases with an increase in pressure of the FGCHRU and reaches to a peak if R1233zd (E) or R600 is used as the working fuid of the bottoming cycle. For R290, above a certain value of the FGCHRU pressure, the



<span id="page-8-2"></span>**Fig. 7** Power output of the bottoming ORC with R290 versus FGCHRU pressure



<span id="page-8-3"></span>**Fig. 8** Power output of the  $CO_2$ -R290 cascading cycle versus FGCHRU pressure

variation of cascading cycle power output is negligible. It is also observed that for lower values of FGCHRU pressure (<15 MPa), the cascading cycle can yield appreciably higher power output compared to that of the baseline regenerative  $T-CO<sub>2</sub>$  power cycle with all three selected working fuids of the bottoming cycle. The cascading cycle yields the highest power output if R1233zd (E) is used as the working fuid of the bottoming cycle of cascading. As pressure in the FGCHRU is increased, the power output of the baseline cycle increases sharply and becomes comparable to that of the cascading cycles as the pressure in the FGCHRU reaches close to 16 MPa.



<span id="page-9-0"></span>**Fig. 9** Comparison of power output of cascading cycle with that of the baseline  $T-CO<sub>2</sub>$  cycle



<span id="page-9-1"></span>**Fig. 10** Comparison of BMC of cascading cycle with that of the baseline  $T-CO<sub>2</sub>$  cycle

Efects of varying FGCHRU pressure on bare module cost per unit power output is presented in Fig. [10](#page-9-1). It is observed in Fig. [10](#page-9-1) that at a lower FGCHRU pressure BMC per unit power is appreciably higher for the baseline  $T-CO<sub>2</sub>$  power cycle. However, BMC per unit power output reduces sharply as elevated pressure is ensured in the FGCHRU. It should be noted that though the total BMC of the base line cycle increases with an increasing FGCHRU pressure, BMC per unit power sharply reduces with the increasing pressure of FGCHRU due to steady rise in cycle power output. Beyond a certain value of the FGCHRU pressure, reduction achieved in BMC per unit power output of the baseline cycle is negligible.

It is further observed in Fig. [10](#page-9-1) that BMC per unit power output of all the cascading cycles are appreciably smaller compared to the baseline cycle, especially at lower pressures of the FGCHRU. This is due to higher power outputs of cascading cycles at lower operating pressures of FGCHRUs. However, BMC per unit power of the cascading cycle increases slowly with increasing pressure of the FGCHRU.

For similar heat carriers, the power output of the present waste heat recovery scheme is appreciably higher compared to that was produced by the waste heat recovery system proposed by Yang ([2016\)](#page-13-8). This is occurring because in the present study the thermal efficiency is maximized by heating CO<sub>2</sub> closer to the engine exhaust gas and the heat recovery from jacket cooling water and scavenging air cooling water also maximized by distributing their mass fow to three different heaters. On the other hand, Yang [\(2016](#page-13-8)) tried to minimize the costing parameters while designing the waste heat recovery system.

In Fig.  $11$ , 1st law efficiency of the proposed waste heatdriven cascade system is compared with that of a regenerative  $T-CO<sub>2</sub>$  power cycle without heat recovery. While estimating 1st law efficiency of the regenerative  $T-CO<sub>2</sub>$  power cycle, regenerator heat duty is maximized by maintaining 10 °C terminal temperature diference in the low temperature end of the  $CO<sub>2</sub>$  regenerator. It is observed in Fig. [11,](#page-9-2) that for close to 10 MPa  $CO<sub>2</sub>$  turbine inlet pressure, 1st law efficiencies of both cycles are almost equal. However, for higher turbine inlet pressure, 1st law efficiency of the regenerative  $T-CO<sub>2</sub>$  power cycle without heat recovery is appreciably higher compared to that of the proposed waste heatdriven cascade system. It is important to note that though 1st law efficiency of the regenerative  $T-CO<sub>2</sub>$  power cycle without heat recovery is appreciably high; it is not suitable for marine diesel engine waste heat recovery. This is because the temperature of  $CO<sub>2</sub>$  exiting the regenerator is so high that heat available with jacket cooling water and scavenging air cooling water cannot be recovered. Thus, due to smaller heat input power output of the regenerative  $T-CO<sub>2</sub>$  power



<span id="page-9-2"></span>Fig. 11 Comparison between 1st law efficiency of the waste heatdriven cascade cycle and that of the regenerative  $T-CO<sub>2</sub>$  cycle without heat recovery

cycle will be appreciably small if regenerator heat duty is maximized.

It should be noted that the auxiliary power requirement of a ship may be assumed to be 5% of the total power output of a marine diesel engine (Malley et al. [2015\)](#page-12-13). Thus, the additional power produced from waste heat recovery can be utilized to supply the auxiliary power. The power produced by the waste heat recovery scheme may be higher to some extent compared to the auxiliary power requirement of the ship. In this situation, after catering the auxiliary power, the remaining power of the waste heat recovery system may be utilized to reduce propeller engine power requirement. However, this would affect output of the waste heat recovery unit as available waste heat would also reduce. Thus, if power output of the waste heat recovery unit is higher compared to the power requirement of the auxiliary unit, fuel savings due to the incorporation of waste heat recovery scheme can be estimated through an iterative calculation as shown in Fig. [12.](#page-10-0) During this calculation, fuel consumption is assumed to be 0.167 kg/kW-h and annual operation

<span id="page-10-0"></span>

hour is assumed to be 7200 h. Waste heat released by the engine supplying the propeller power is only considered for the waste heat recovery.

The annual fuel savings is closely related with the additional power produced by the proposed waste heat recovery scheme. The more the power produced, the greater is the fuel saving. The percentage of oil saved is plotted for  $CO_2$ -organic fluid cascade system and regenerative  $T-CO<sub>2</sub>$  cycle operating at FGCHRU pressures of 10 MPa (Fig. [13](#page-11-0)a) and 16 MPa (Fig. [13b](#page-11-0)), respectively. It is observed that at lower operating pressure of 10 MPa, the  $CO<sub>2</sub>-R1233zd$  (E) cascading cycle can save 9.53% of fuel annually while the same is signifcantly lower in regenerative  $T-CO<sub>2</sub>$  at 4.62%. The annual fuel saving percentage improves significantly for regenerative  $T-CO<sub>2</sub>$ cycle when the FGCHRU pressure is increased. The annual fuel savings for regenerative T-CO<sub>2</sub> cycle at 16 MPa is  $8.25\%$ which is marginally lower than the  $CO_2$ -organic cascade cycle. It is interesting to note from Fig. [14](#page-11-1) that the annual fuel savings of  $CO<sub>2</sub>$ -organic cascade cycle does not vary significantly with FGCHRU pressures but that of regenerative  $T-CO<sub>2</sub>$ cycle improves signifcantly, owing to higher power output at higher pressure. However, operating at lower pressure is



<span id="page-11-0"></span>**Fig. 13** Annual fuel saving due to waste heat recovery at **a** 10 MPa, **b** 16 MPa pressure in the FGCHRU



<span id="page-11-1"></span>**Fig. 14** Annual fuel saving versus FGCHRU pressure

always better from capital investment as well as operational simplicity. Hence, cascaded cycle will provide better overall performance than  $T-CO<sub>2</sub>$  cycle with better oil saving operating at lower pressure.

It is also necessary to compare the power output of the cascading cycle with that of a regenerative transcritical organic Rankine cycle to select the best possible waste heat recovery scheme for a marine diesel engine. In Fig. [15a](#page-12-14), the power output of the regenerative ORC with R290 is compared with that of the  $CO<sub>2</sub>-R290$  cascading cycle. Initially, the power output of the regenerative ORC increases with increasing operating pressure in the organic fuid HRU. Then the power output decreases due to the reduced heat duty of the regenerator. A slightly increasing trend is observed further as specific turbine power output increases with the elevated pressure in organic fuid HRU. It is observed in Fig. [15a](#page-12-14) that the power output of a regenerative ORC with R290 is higher compared to the power produced by a  $CO<sub>2</sub>-R290$  cascading cycle. For the cascading cycle, pressure in the FGCHRU is taken to be 12 MPa or less to avoid the leakage of  $CO<sub>2</sub>$  from the piping joint.

It is clear from Fig. [15](#page-12-14)b that the mass fow rate of the R290 for each MW power output of the regenerative ORC is appreciably higher compared to that of the  $CO<sub>2</sub>-R290$ cascading cycle yielding the same power output. Thus, the chance of the accidental and uncontrolled fame propagation would be reduced appreciably by using a  $CO<sub>2</sub>$ -organic cascading cycle for the marine diesel engine waste heat recovery as mass of fammable working fuid to be handled reduces appreciably.

## **Conclusions**

In the present study, a cascading between a  $T-CO<sub>2</sub>$  power cycle and an organic Rankine cycle is considered for the marine diesel engine waste heat recovery. R290, R600 and





<span id="page-12-14"></span>**Fig. 15 a** Comparison between of power output of regenerative ORC with R290 and that of CO<sub>2</sub>-R290 cascading. **b** Comparison of mass flow rate of R290 in regenerative ORC to that of in  $CO<sub>2</sub>-R290$  cascading cycle

R1233zd (E) are selected as the working fuids of the bottoming cycle considering their lower GWPs. The outcome of the study can be summarized as follows:

- By using the marine diesel engine waste heat, a  $CO<sub>2</sub>$ -organic cascading cycle yields good power output even at 10 MPa pressure in the flue gas- $CO<sub>2</sub>$  heat recovery unit (FGCHRU). For producing a comparable power output, the pressure in the FGCHRU of the baseline regenerative  $T-CO<sub>2</sub>$  power cycle should be close to 16 MPa.
- The bare module cost for producing each kW power output appears to be smaller for the cascading cycle com-

pared to that of the baseline regenerative transcritical  $CO<sub>2</sub>$  power cycle.

• In present study, R1233zd (E) appears as the best performing working fuid, as the cascading cycle that is using R1233zd (E) as bottoming cycle fuid yields highest power and lowest BMC per kW. Waste heat recovery through  $CO<sub>2</sub>$ - R1233zd (E) cascading cycle would reduce annual fuel consumption by 9.53%.

In summary, marine diesel engine waste heat recovery through the  $CO<sub>2</sub>$ -organic cascading cycle would produce a less adverse efect on the environment as it would reduce marine  $CO<sub>2</sub>$  emission by cutting down the fuel consumption.

## **References**

- <span id="page-12-2"></span>Baik Y-J, Kim M, Chang K-C, Lee Y-S, Yoon H-K (2013) A comparative study of power optimization in low-temperature geothermal heat source driven R125 transcritical cycle and HFC organic Rankine cycles. Renew Energy 54:78–84
- <span id="page-12-1"></span>Braimakis K, Karellas S (2018) Energetic optimization of regenerative Organic Rankine Cycle (ORC) confgurations. Energy Convers Manag 159:353–370
- <span id="page-12-9"></span>Calm JM, Hourahan GC (2011) Physical, safety, and environmental data for current and alternative refrigerants. In: Conference physical, safety, and environmental data for current and alternative refrigerants, Prague, Czech Republic, pp 21–26
- <span id="page-12-12"></span>Cengel YA, Boles MA (2006) Thermodynamics: an engineering approach, 5th edn. McGraweHill, New York
- <span id="page-12-7"></span>Chen Y, Lundqvist P, Platell P (2005) Theoretical research of carbon dioxide power cycle application in automobile industry to reduce vehicle's fuel consumption. Appl Therm Eng 25:2041–2053
- <span id="page-12-0"></span>Corbett JJ, Koehler HW (2003) Updated emissions from ocean shipping. J Geophys Res 108(D20):4650. [https://doi.](https://doi.org/10.1029/2003JD003751) [org/10.1029/2003JD003751](https://doi.org/10.1029/2003JD003751)
- <span id="page-12-4"></span>Guo T, Wang HX, Zhang SJ (2010) Comparative analysis of  $CO<sub>2</sub>$ -based transcritical Rankine cycle and HFC245fa-based subcritical organic Rankine cycle using low temperature geothermal source. Sci China 53:1638–1646
- <span id="page-12-3"></span>Ho T, Samuel SM, Greif R (2012) Comparison of the Organic Flash Cycle (OFC) to other advanced vapor cycles for intermediate and high temperature waste heat reclamation and solar thermal energy. Energy 42:213–223
- <span id="page-12-10"></span>Incropera FP, Dewitt DP (2002) Fundamentals of heat and mass transfer, 5th edn. Wiley, New York
- <span id="page-12-11"></span>Kreith F, Bohn MS (1993) Principles of heat transfer, 5th edn. West Publishing Company, New York
- <span id="page-12-8"></span>Lemmon EW, Huber ML, McLinden MO (2013) NIST standard reference database 23: reference fuid thermodynamic and transport properties—REFPROP, version 9.1. National Institute of Standards and Technology, Standard Reference Data Program, Gaithersburg
- <span id="page-12-13"></span>Malley S, Walsh K, Hasen A, Bratvold D, Ratafa-Brown J (2015) Marine fuel choice for ocean going vessels within emission control areas. Energy Information Administration
- <span id="page-12-5"></span>Mondal S, De S (2015a) Transcritical  $CO<sub>2</sub>$  power cycle—effects of regenerative heating using turbine bleed gas at intermediate pressure. Energy 87:95–103
- <span id="page-12-6"></span>Mondal S, De S (2015b)  $CO<sub>2</sub>$  based power cycle with multi-stage compression and intercooling for low temperature waste heat recovery. Energy 90:1132–1143
- <span id="page-13-2"></span>Mondal S, De S (2017a) Power by waste heat recovery from low temperature industrial fue gas by Organic Flash Cycle (OFC) and transcritical- $CO<sub>2</sub>$  power cycle: a comparative study through combined thermodynamic and economic analysis. Energy 121:832–840
- <span id="page-13-3"></span>Mondal S, De S (2017b) Ejector based organic fash combined power and refrigeration cycle (OFCP&RC)—a scheme for low grade waste heat recovery. Energy 134:638–648
- <span id="page-13-5"></span>Mondal S, De S (2019) Waste heat recovery through organic fash cycle (OFC) using R245fa–R600 mixture as the working fuid. Clean Technol Environ Policy 21:1575–1586
- <span id="page-13-0"></span>Mondal S, De S (2020) Power and other energy utilities from low grade waste heat—novel technologies to reduce carbon footprint. Encycl Renew Sustain Mater 3:667–677
- <span id="page-13-4"></span>Mondal S, Alam S, De S (2018) Performance assessment of a low grade waste heat driven organic fash cycle (OFC) with ejector. Energy 163:849–862
- <span id="page-13-15"></span>Pioro IL, Khartabil HF, Duffey RB (2004) Heat transfer to supercritical fuids fowing in channels—empirical correlations (survey). Nucl Eng Des 230:69–91
- <span id="page-13-1"></span>Saleh B, Koglbauer G, Wendland M, Fischer J (2007) Working fluids for low-temperature organic Rankine cycles. Energy 32:1210–1221
- <span id="page-13-12"></span>Shi L, Shu G, Tian H, Chang L, Huang G, Chen T (2017) Experimental investigations on a  $CO<sub>2</sub>$ -based Transcritical Power Cycle (CTPC) for waste heat recovery of diesel engine. Energy Procedia 129:95
- <span id="page-13-6"></span>Song J, Song Y, Gu C (2015) Thermodynamic analysis and performance optimization of an Organic Rankine Cycle (ORC) waste heat recovery system for marine diesel engines. Energy 82:976–985

# **Afliations**

## **Subha Mondal1 · Soumitra Datta2 · Sudipta De2**

- $\boxtimes$  Sudipta De de\_sudipta@redifmail.com
- <sup>1</sup> Department of Mechanical Engineering, Aliah University, Kolkata 700160, India
- <span id="page-13-11"></span>Song J, Li X, Ren X, Gu C (2018) Performance improvement of a preheating supercritical  $CO<sub>2</sub>$  (S-CO2) cycle based system for engine waste heat recovery. Energy Convers Manag 161:225–233
- <span id="page-13-14"></span>Turton R, Bailie RC, Whiting WB (2013) Analysis, synthesis and design of chemical processes, 4th edn. Prentice Hall PTR, New Jersey
- <span id="page-13-8"></span>Yang M (2016) Optimizations of the waste heat recovery system for a large marine diesel engine based on transcritical Rankine cycle. Energy 113:1109–1124
- <span id="page-13-9"></span>Yang M (2018) Payback period investigation of the organic Rankine cycle with mixed working fuids to recover waste heat from the exhaust gas of a large marine diesel engine. Energy Convers Manag 162:189–202
- <span id="page-13-7"></span>Yang M, Yeh R (2015) Thermo-economic optimization of an organic Rankine cycle system for large marine diesel engine waste heat recovery. Energy 82:256–268
- <span id="page-13-10"></span>Yang M, Yeh R (2017) Economic research of the transcritical Rankine cycle systems to recover waste heat from the marine mediumspeed diesel engine. Appl Therm Eng 114:1343–1354
- <span id="page-13-13"></span>Yang J, Sun Z, Yu B, Chen J (2018) Experimental comparison and optimization guidance of R1233zd (E) as a drop-in replacement to R245fa for organic Rankine cycle application. Appl Therm Eng 141:10–19

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

<sup>2</sup> Department of Mechanical Engineering, Jadavpur University, Kolkata 700032, India