# **Evaluation of shear strength of clayey soils by using their liquidity index**

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**Abstract** It is well known that overconsolidated clays have higher shear strength than unconsolidated clays. The liquidity index makes possible an evaluation of the consolidation degree of clays. However, there is no empirical information about this relation. In this study, clayey soil samples have been collected from various locations and tested. The tests include the determination of liquidity index and shear strength. Obtained parameters were correlated and regression equations were established among liquidity index and undrained shear strength, presenting high coefficients of correlation  $(R=-0.93)$ . So, an equation  $[c_u = e^{(0.026-1.21 I_L)}]$  that makes possible a rough evaluation of the shear strength of clayey soils by using their liquidity index value is an improvement.

**Résumé** Il est bien connu que la résistance au cisaillement des argiles sur-consolidées est plus grande que celle des argiles sous-consolidées. L'indice de liquidité rend possible une évaluation du degré de consolidation des argiles. Mais il n'y a aucune donnée au sujet de cette relation. Dans cette étude, des échantillons de sols argileux ont été prélevés en divers endroits et testés. Les tests concernent la détermination de l'indice de liquidité et de la résistance au cisaillement. Les paramètres obtenus ont été corrélés et l'analyse de régression entre l'indice de liquidité et la résistance au cisaillement a donné des coefficients de corrélation élevés  $(R = -0.93)$ . Aussi une équation  $[Cu = e^{(0.026-1.21 I_L)}]$  a été établie, permettant d'obtenir une estimation grossière de la résistance au cisaillement de sols argileux en utilisant la valeur d'indice de liquidité.

**Keywords** Liquidity index  $\cdot$  Shear strength  $\cdot$  Clay

Mots clés Indice de liquidité · Résistance au cisaillement  $\cdot$  Argile

## **Introduction**

This study considers the possibility of expressing the relationship between the undrained shear strength  $(c<sub>u</sub>)$  and liquidity index  $(I_L)$  of clays by an empirical equation, such that it would be possible to estimate the shear strength of a clay by using its liquidity index. It is considered that Atterberg limit tests are not only convenient but may also provide a cheaper method of assessing the quick undrained shear strength of clays.

It is well known that overconsolidated clays have a higher shear strength than unconsolidated deposits and this is also reflected in the liquidity index by the difference in moisture content. To date, the empirical relationship between the shear strength and the liquidity index has not been established.

In this study, block samples of clayey soil were collected from various locations in Turkey and liquidity index  $(I_L)$ and shear strength  $(c<sub>u</sub>)$  by triaxial compression tests determined. The parameters obtained were correlated and regression analysis was performed to express the best fit relationship between the  $c<sub>u</sub>$  and  $I<sub>L</sub>$ . It is considered that this work provides a rough indication of the shear strength of clayey soils by using their liquidity index value.

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## **Material and methods**

The materials used in this study were mostly fine-grained alluvial soils from various locations in Turkey (e.g. Sivas,

Tokat, Bursa, Zonguldak). Block samples of undisturbed soils were collected from depths of 2 to 4 m. Of the 41 samples collected, 30 were chosen to obtain, as far as possible, similar characteristics. On these, undrained shear strength  $(c<sub>u</sub>)$ , natural water content, plastic limit and liquid limit values were determined by laboratory tests.

The relative consistency of a cohesive soil in the natural state can be defined by a ratio (Eq. 1) called the liquidity index  $(I_L)$ :

$$
I_{L} = (w_{n} - w_{p})/I_{p} \tag{1}
$$

In this equation, if  $I_L = 1.0$ , the soil is at its liquid limit; if  $I_L = 0$ , the soil is at its plastic limit. The liquidity index is believed by many authors to more usefully reflect the properties of plastic soil than the generally used plastic and liquid limits ( $w_p$  and  $w_L$ ). The Atterberg tests are carried out on remoulded soil in the laboratory, but the same soil, in its in-situ state, may exhibit a different consistency at the same moisture content due to sensitivity effects. For this reason, it does not necessarily imply that a soil found to have a liquid limit of 50% will be in liquid state if its in-situ water content is also 50%.

If  $w_n$  is greater than the test value of  $w_L$  then  $I_L$  is  $>1.0$  and it is obvious that if the soil was remoulded it would become a slurry. Such a soil would probably be an unconsolidated sediment with a  $c<sub>u</sub>$  value in the order of 15–50 kPa. Most cohesive soil deposits have  $I_L$  values within the range 1.0–0.0. The lower the value of  $w_n$ , the greater the amount of compression that must have taken place and the nearer  $I_L$  will be to zero. If  $w_n$  is less than the test value of the plastic limit, then  $I_L < 0.0$  and the soil cannot be remoulded (as it is outside the plastic range). In this case the soil is most likely to be a compressed sediment. Soil in this state will have a  $c<sub>u</sub>$  value varying from 50 to 250 kPa (Smith 1990).

Rominger and Rutledge (1952) and Means and Parcher (1963) consider that the liquidity index provides a reliable indication of the degree of consolidation of clayey soils. Means and Parcher (1963) reported that  $I_L=0$  for overconsolidated clays and the value of the liquidity index is negative for highly overconsolidated clays.

deposits, and a statistical relationship (Eq.2) for the (After-Means-and-Parcher-1963) The undrained shear strength increases with the effective overburden pressure in normally consolidated clay

#### **Table 1**

Consistency of fine-grained soils. (After British Standards Institution 1975)



undrained shear strength, the effective overburden pressure and the plasticity index of the soils is possible (Skempton 1957). Equation (2) is an extremely useful relationship. If the plasticity index of a normally consolidated clay deposit is known, then the variation of undrained shear strength with depth can be estimated (Das 1994).

$$
(c_{\rm u}/\sigma') = 0.11 + 0.0037 \, \rm I_p \tag{2}
$$

The property that enables a material to remain in equilibrium when its surface is not horizontal is known as its shear strength. Soils in liquid form have virtually no shear strength and even when solid have shear strengths of relatively small magnitudes compared to those exhibited by steel or concrete. Cohesion is a major contributory factor to the shear forces in cohesive soils. The physical state of cohesive soils is expressed by the term consistency; a consistency classification for clays is given in Table 1 (Anon 1979). As shown in Fig. 1 (Means and Parcher 1963), the state of consolidation is indicated by the liquidity index.

In the first stage of the laboratory experiments, grain size distribution, liquid limit, plastic limit and natural water content were determined in accordance with BS 1377 (British Standards Institution 1975). Sieving and hydrometer methods were used to obtain the grain size; the results

**Fig. 1**

Relationship between degree of consolidation and liquidity index.







**Table 2** Results of regression analyses



indicated the materials to be generally silty clays. In view of its effect on the engineering behaviour of soil, the organic material content was also determined using the Walkey-Black method (Nelson and Sommers 1982). For the fine-grained soils it was found to vary from 0.45 to 0.64%, with an average value of 0.48%. Such a low value would not influence the engineering characteristics of the soils to any significant extent. The plasticity index first increased slightly then decreased with increasing organic content up to 10%.

## **Results and discussion**

Regression analysis of the results comparing the undrained shear strength and liquidity index is shown in Fig. 2. As seen in Table 2, a good correlation is indicated  $(R = -0.93)$ . The relationship between the two parameters is

$$
c_{u} = e^{(0.026 - 1.21 \, I_{L})}
$$
\n(3)

While Fig. 2 indicates a general trend which clearly will be useful for some workers where the Atterberg limits are available, as pointed out by Bell and Culshaw (1998) and Bell and Maud (1995), the liquidity index is a physical property while the shear strength is a mechanical property of the soils and hence empirical methods to obtain the shear strength should always be treated with caution.

### **References**

- Anon (1979) Classification of rocks and soils for engineering geological mapping. Part I: rock and soil materials. Bull IAEG 19 : 364–371
- BELL FG, CULSHAW MG (1998) Some geohazards caused by soil mineralogy, chemistry and microfabric: a review. In: Maund JG, Eddleston M (eds) Geohazards in engineering geology. Geological Society, London, Engineering Geology Spec Publ 15, pp 427–441
- BELL FG, MAUD RR (1995) Expansive clays and construction, especially of low-rise structures: a viewpoint from Natal, South Africa. Environ Eng Geosci I(1) : 41–59
- British Standards Institution (1975) Methods of test for soils for civil engineering purposes. BS 1377. BSI, London
- Das BM (1994) Principles of geotechnical engineering. PWS, Boston, 672 pp
- Means WE, Parcher JV (1963) Physical properties of soils. Charles E. Merril, Columbus, Ohio, 476 pp
- Nelson DW, Sommers LE (1982) Total carbon, organic carbon and organic matter. Methods of soil analysis – Part 2 : chemical and microbiological properties. Agronomy Monogr no 9, 2nd edn. American Society of Agronomy–Soil Science Society of America, Madison, Wisconsin, pp 539–578
- ROMINGER JF, RUTLEDGE PC (1952) Use of soil mechanics data in correlation and interpretation of Lake Agassiz sediments. J Geol 60(2) : 160–180
- SMITH GN (1990) Elements of soil mechanics. Blackwell Scientific Publications, Oxford, 509 pp