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# **Shear wave implications in wetting‑induced collapse of sand–clay mixtures**

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### **Abstract**

Collapsible soils pose signifcant challenges to engineering projects due to their instability and sudden changes in volume upon variations in water content. In this study, the collapse potentials of specimens with sand–clay mixtures are experimentally investigated by considering factors, such as initial water content and clay fraction. The specimens are subjected to vertical stress up to  $\sigma'$ <sub>*v*</sub>=440 kPa in an instrumented oedometer cell, including the wetting process at  $\sigma'$ <sub>*v*</sub>=220 kPa. The settlement and shear wave velocity  $(V<sub>s</sub>)$  are continuously measured during loading and wetting to propose a geophysical approach based on shear wave velocity measurements for better understanding of collapse mechanisms. The results show that the collapse potential of sand–clay mixtures increases with increasing clay fraction at a specifc water content. However, the variation in the collapse potential can be the sole function of the clay water content (=water content/clay fraction). As the suction pressure decreases upon wetting, the  $V_s$  shows a time-dependent decrease during wetting, and the decreasing is proportional to the collapse potential, indicating the loss of small-strain stifness. However, when the settlement ceases, a portion of  $V_s$  can be recovered over time because of the formation of a stable soil structure, leading to the ratio of  $V_s$  after collapse to *V<sub>s</sub>* before collapse ranges from 0.85 to 1.05. Additionally, this study reveals that a relatively higher initial degree of saturation  $(>50\%)$  is necessary to recover stiffness/strength after soil collapse, emphasizing the importance of proper compaction in engineering projects involving collapsible soils.

**Keywords** Collapse potential · Sand–clay mixture · Clay water content · Shear wave velocity · Suction pressure

# **Introduction**

Collapsible soils are a considerable concern in geotechnical engineering, posing risks to infrastructure and challenges for construction projects. These soils are widely distributed worldwide, covering 15–20% of Europe, China, and the United States, particularly in arid and semi-arid regions (Das [1995](#page-11-0); Rogers [1995;](#page-12-0) Gao [1996](#page-11-1); Gaaver [2012;](#page-11-2) Assadi-Langroudi et al. [2018\)](#page-10-0). The collapse potential of sand-clay mixtures, which are common in natural deposits, has not been thoroughly investigated, despite its critical implications

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for engineering applications. This study aims to bridge this knowledge gap by investigating the efects of initial water content, dry density, and clay content on the collapse potential of sand-clay mixtures, and by examining the relationship between collapse potential and shear wave velocity changes before and after the collapse.

Collapsible soils are characterized by their low density, low water content, and high sensitivity to changes in moisture content (Mitchell and Soga [2005;](#page-11-3) Roger [1995](#page-12-0)). Their unique structure, often described as a loose honeycomb-type arrangement, makes them susceptible to sudden volume changes (i.e., collapse) upon wetting, leading to catastrophic consequences such as landslides, diferential settlement of structures, and instability of earthworks (Clemence and Finbarr [1981;](#page-11-4) Rollins and Rogers [1994](#page-12-1)). This instability typically arises from the breakdown of capillary suction pressure and cementation effects between particles when water content increases (Feda [1966;](#page-11-5) Lawton et al. [1989;](#page-11-6) Houston et al. [2001;](#page-11-7) Rao and Revanasiddappa [2002](#page-12-2); Pereira et al. [2005\)](#page-12-3). The collapse potential  $(C_p)$  is defined as the ratio

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between the change in height upon wetting  $(\Delta H_w)$  and the initial specimen height  $(H_i)$ , providing a quantitative measure of the volumetric change potential (ASTM D5333-03— ASTM [2003](#page-11-8)).

Natural soils can be highly complex in their composition; thus, natural coarse-grained sediments generally contain varying amounts of fines (particle size  $< 0.075$  mm per Unified Soil Classifcation System, USCS) that can be categorized into silt or clay in geotechnical engineering (Monkul and Ozden [2007](#page-11-9); Karakan and Demir [2018](#page-11-10)). Previous research has primarily focused on the impact of fne fractions on the behavior of coarse grains, examining aspects such as compressional and compaction behavior, undrained shear strength, and physical properties (e.g., Monkul and Ozden [2007](#page-11-9); Cabalar and Hasan [2013;](#page-11-11) Cabalar and Mustafa [2017](#page-11-12); Karakan and Demir [2018;](#page-11-10) Cabalar et al. [2020;](#page-11-13) Karakan et al. [2020](#page-11-14); Kim et al. [2021](#page-11-15); Shimobe et al. [2021\)](#page-12-4). However, the efect of clay content on the collapse potential of sand or coarse-grained soils remains unclear. Furthermore, while previous studies have explored the volume changes associated with collapse (Mahmood and Abrahim [2021](#page-11-16)), the variations in mechanical properties, such as shear wave velocity, during this process have not been thoroughly investigated. Because the shear wave velocity is determined by interparticle contacts (determined by the applied stress) and interparticle coordination (determined by the packing state), shear wave velocity measurements for collapsible soils would be benefcial in terms of monitoring the decrease in capillary suction pressure during the collapse and the formation of a stable soil structure after the collapse.

Traditionally, the study of collapsible soils has been categorized into three approaches: (1) traditional (soil properties) approach, (2) microstructure (soil fabric) approach, and (3) soil mechanics-based approach (Li et al. [2016\)](#page-11-17). Firstly, previous traditional approach has emphasized the soil property factors that infuence collapse mechanisms, such as the dry density, Atterberg limits, initial water content, and clay content, and a large number of empirical equations have been proposed (Clevenger [1958;](#page-11-18) Gibbs and Bara [1962](#page-11-19); Feda [1966;](#page-11-5) Li et al. [2016](#page-11-17); Khodabandeh et al. [2023](#page-11-20)). Secondly, the microstructure approach has interpreted the efects of particle fabric, pore formation and distribution, and the form of bonding materials between particles on the collapse behavior (Assallay et al. [1997](#page-10-1); Derbyshire and Mellors [1988;](#page-11-21) Romero and Simms [2008\)](#page-12-5). Many researchers have tried to understand the soil pore patterns and stability of bonding materials, but there is a certain limitation to clearly evaluate those microstructures for fne-grained, such as silt and clay (Gu et al. [2011](#page-11-22)). Additionally, soil collapse is caused by multiple combinations of factors rather than one single reason because the soil properties primarily govern the microstructure of soils. Lastly, the soil mechanics-based approach has focused on the reduction of suction pressure among particles due to wetting, resulting in the signifcant volume change of collapsible soils (El-Ehwany and Houston [1990;](#page-11-23) Jotisankasa [2005](#page-11-24); Pereira and Fredlund [2000](#page-11-25)). As mentioned above, the soil collapse is consequence of the complicated response among particles, which can be simultaneously afected by soil properties (approach 1), soil fabric (approach 2), and suction pressure (approach 3). Therefore, the main objective of this study is to evaluate the collapse potential of sand-clay mixture with various composition, and also to estimate the evolution of shear wave velocity (smallstrain stifness) before and after the collapse.

In this study, the effects of the initial water content, dry density, and clay content on the collapse potential of sand are investigated. To this end, silica sand specimens mixed with various clay fractions and water contents are consolidated in an oedometer cell and immersed in water to trigger collapse. The collapse potential is determined from the volume changes during the wetting process to estimate the signifcance of these factors. Additionally, the shear wave velocities before and after wetting are measured to correlate the changes in the small-strain stifness and collapse potential. The correlations between collapse potential and small-strain stifness can provide a better understanding of the geophysical manner of soil collapse, including the fabric alteration and stifness recovery processes after the collapse. Furthermore, this study provides a new category for the study of collapse mechanism, which is geophysical approach, in additional to previous traditional, microstructure, and soil mechanics-based approaches.

# **Experimental study**

## **Experimental device**

In Fig. [1](#page-2-0)a, an instrumented oedometer cell is designed to measure the vertical displacement and shear wave velocity during the consolidation and wetting processes. The oedometer cell is made of stainless steel and has an inner diameter of 100 mm and a wall thickness of 10 mm to ensure  $K_0$ consolidation conditions (i.e., negligible horizontal strain  $(< 10^{-5})$ ) during vertical loading. The top and bottom caps are equipped with a pair of bender elements (BE) to measure the shear wave velocities at various stress conditions, including wetting-induced soil collapse. The step input signal is generated from a function generator (Keysight 33210A) with a voltage of 10 V and a frequency of 20 Hz. Note, a step signal includes all frequencies; thus, a clear signal can be obtained regardless of soil stifness (Lee and Santamarina [2005\)](#page-11-26). The generated waves from the bottom bender element travel the specimen upwardly and are then captured at the top bender element. The captured signatures are averaged by stacking 1024 signals and displayed on an oscilloscope



<span id="page-2-0"></span>**Fig. 1** (**a**) Schematic drawing of an instrumented oedometer cell and (**b**) typical shear wave signatures captured during the vertical loading and following wetting processes of S40-C60 specimen with water content  $(w) = 11\%$ . Note the circles in figure (**b**) indicate the first arrival time

(Keysight DSOX 2014A) (Fig. [1b](#page-2-0)). The frst arrival time (travel time) of the shear wave is determined according to recommendation of Lee and Santamarina [\(2005](#page-11-26)). The vertical displacement during loading and wetting is monitored using a linear variable diferential transformer (LVDT), and updated specimen height is used to calculate the travel length of shear wave signatures.

# **Tested materials**

The specimens are reconstituted using a mixture of silica sand and kaolin clay to imitate collapse-susceptible soils in the laboratory. Note silica sand is the most abundant type of sand found worldwide and kaolin clay is a very common clay type due to the abundance of kaolinite, which makes up the majority of its composition. The grain size distribution curves for the two unmixed soils are shown in Fig. [2.](#page-2-1) The soil index properties of the silica sand (K-5 sand, manufactured by Kyung In Material, South Korea) are as follows: coefficient of uniformity  $C_u = 1.47$ , median grain size  $D_{50}$ =800  $\mu$ m, specific surface  $S_s$ =0.03 m<sup>2</sup>/g, and specific gravity  $G_s = 2.65$ . Kaolin clay is manufactured by the Lakwoo Company, South Korea and has  $D_{50}$  = 3.96 µm, liquid limit *LL* = 38.4%, plastic limit *PL* = 23.6%,  $S_s$  = 10.92 m<sup>2</sup>/g, and  $G_s = 2.53$ . Thus, according to the USCS, the tested sand and clay are classifed as poorly graded sand (SP) and lowplasticity clay (CL), respectively. Sand–clay mixtures are prepared using predetermined sand/clay mass fractions, that



<span id="page-2-1"></span>**Fig. 2** Grain size distribution of the tested unmixed soils

is, S80-C20 (80% sand+20% clay), S60-C40, S40-C60, and S20-C80.

## **Specimen preparation and experimental procedures**

Modified proctor compaction tests are first performed to determine the variation in the dry unit weight according to the initial water content, as shown in Fig. [3](#page-3-0) (ASTM D1557-12; ASTM [2012\)](#page-11-27). The specimens are prepared with predetermined sand/clay mass fractions (i.e., S80-C20, S60-C40, S40-C60, and S20-C80) to evaluate the effects



<span id="page-3-0"></span>**Fig. 3** Comparison of the compaction curve (empty markers with dotted line) and test conditions of the specimens (flled markers): (**a**) S80-C20 (i.e., specimens with sand fraction=80% and clay fraction=20%); (**b**) S60-C40; (**c**) S40-C60; (**d**) S20-C80 (note: *S*=degree of saturation)

of the clay fraction on the maximum dry unit weight and the corresponding optimum water content. The maximum dry unit weight and optimum water content of the mixtures varies with the sand/clay fraction: the S60-C40 specimens attain the highest maximum dry density at a water content of 12% (Fig. [3b](#page-3-0)), whereas the S20-C80 specimens exhibit the lowest maximum dry density at a water content of 18% (Fig. [3d](#page-3-0)). An increased optimum water content corresponds to an increased clay fraction. The results reveal that a larger amount of water is required to obtain the maximum dry unit weight with a higher clay fraction (Shimobe et al. [2021](#page-12-4)).

For the wetting tests, the sand–clay mixtures with predetermined initial water contents are premixed and stored in a plastic bag and placed in three layers in an oedometer cell. Tamping is performed to achieve the target dry unit weight. The initial water contents and dry unit weights of the tested specimens are shown in Fig. [3](#page-3-0). The dry unit weight of the tested specimens is targeted to 80% of the maximum dry unit weight of each sand/clay fraction to represent the collapse-susceptible soil (i.e., non-compacted near-surface soil or insufficiently compacted soil with relatively lower relative compaction). Note that the soil collapse tends to be more pronounced in loose-packing soils. The specimens are prepared using various initial water contents to estimate the efects of the initial water content on the collapse potential. Furthermore, complementary specimens (S20-C80) are tested at diferent dry unit weights at the optimum water content to evaluate the role of the packing density during the collapse.

The prepared specimens are subjected to stepwise vertical stress up to  $\sigma'_{v}$ =220 kPa under  $K_0$  consolidation conditions, after which they are inundated with distilled water for 24 h (ASTM D5333-03; ASTM [2003\)](#page-11-8). An additional vertical stress of  $\sigma'_{v}$ =440 kPa is then applied to the wet specimens to compare the compressibility before and after the collapse. Note that collapse index is generally measured at  $\sigma'_{v}$ =200 kPa (per ASTM D5333). During these procedures, the vertical displacement is continuously monitored to assess the collapse potential triggered by wetting. Furthermore, shear wave signatures are continuously captured during the loading and wetting processes.

# **Results and discussion**

#### **Efect of inundation stress on collapse potential**

This study measures the collapse potential at a vertical efective stress (inundation stress) of 220 kPa because of the predetermined oedometer cell size and set of weights (note: the test protocol defnes the collapse index as the collapse potential at inundation stress of 200 kPa [ASTM D5333]). Because the collapse potential varies with the magnitude of inundation stress (Howayek et al. [2011;](#page-11-28) Silveira and Rodrigues [2020](#page-12-6)), the collapse potentials of the S20-C80 samples (20% sand with 80% clay) with relative compaction of 80% and initial water content of 14% are measured at three inundation stress values (Fig. [4](#page-4-0)a). Figure [4b](#page-4-0) illustrates the effect of inundation stress on collapse potential  $(C_p)$ , showing a slight increase in  $C_p$  with increasing vertical effective stress  $(\sigma'_v)$ . The estimated  $C_p$ at  $\sigma'_{v}$ = 200 kPa, which is the collapse index, is approximately 8% based on interpolation, while the measured  $C_p$ at  $\sigma'$ <sub>v</sub>=220 kPa is 8.2% (Fig. [4](#page-4-0)b). This suggests that considering the measured collapse potential in this study as the collapse index would be practically acceptable.



<span id="page-4-0"></span>**Fig. 4** Efect of inundation stress on collapse potential. (**a**) evolution of vertical strain of S20-C80 specimens with initial water content  $w = 14\%$  during the  $K_0$ -consolidation and wetting at vertical stress of 55, 110, and 220 kPa; (**b**) variation of collapse potential according to inundation stress

#### **Efect of initial water content on collapse potential**

Figure [5](#page-5-0) presents the relationship between the vertical (or volumetric) strain and the applied vertical stress  $(\sigma'_v)$  for the S40-C60 specimens (sand fraction = 40%) and clay fraction= $60\%$ ) during the static loading history up to  $\sigma'_{v}$ =440 kPa, where the wetting process occurs at  $\sigma'_{v}$ =220 kPa. The vertical strain gradually increases until  $\sigma'_{v}$ =220 kPa because of the compression of the voids (i.e., a decrease in the void ratio), followed by an abrupt change in the vertical strain during wetting at  $\sigma'_{v}$ =220 kPa. This sharp volume reduction is mainly attributed to the wetting process, which disrupts the stability of the initial particle bonding at a specifc initial water content. Soil stifness under partially saturated conditions is primarily infuenced by capillary pressure, which is a function of the water content and features of grain gradation (Wu et al. [1984](#page-12-7); Cho and Santamarina [2001;](#page-11-29) Ng et al. [2020](#page-11-30)). Noticeably, S40-C60 specimens with higher initial water contents exhibit less signifcant volumetric changes when subjected to wetting under constant vertical stress.

Figure [6](#page-5-1) shows the calculated collapse potentials of the tested specimens with various sand/clay fractions and a broad range of initial water contents. The results show that an increase in the initial water content decreases the collapse potential. Numerous previous studies have reported similar efects of water content on the collapse potential of soils because of the lower suction pressure at a higher water content (Li et al. [2016;](#page-11-17) Khodabandeh et al. [2023](#page-11-20)). Specifcally, when the initial water content is lower than 2–4% below the optimum water content  $(w_{opt})$ , the effect of the water content on the variation in collapse potential is insignifcant, although the measured collapse potential is large. In contrast, when the initial water content exceeds the values that are 2–4% lower than  $w_{opt}$  (dry of  $w_{opt}$ ), the collapse potential rapidly decreases with increasing water content, and further reduction is expected in the wet of  $w_{opt}$  (i.e., higher water content than  $w_{opt}$ ). The results indicate that the initial water content should be higher than 2–4% below the optimum water content  $(w_{opt})$  to minimize the soil collapse potential (see similar observations in Howayek et al. [2011](#page-11-28)).

#### **Efect of clay content on collapse potential**

Figure [7](#page-6-0) shows the evolution of the vertical strain in response to the vertical stress for the four specimens containing various sand/clay fractions at a fxed water content of 12%. Clearly, the collapse potential  $(C_p)$  at an identical initial water content of 12% tends to increase with increasing clay fraction. High capillary pressure builds up in clayey-dominant pores under unsaturated conditions, leading to enhanced soil stifness (Agus et al. [2010\)](#page-10-2); however, the suction-induced efective stress diminishes during the



<span id="page-5-0"></span>**Fig. 5** Evolution of vertical strain of S40-C60 specimens during the  $K_0$ -consolidation and wetting. The wetting occurred at a vertical stress of 220 kPa, followed by an additional loading to 440 kPa. (a) Initial water content  $w=9\%$ ; (b)  $w=11\%$ ; (c)  $w=13\%$ ; (d)  $w=15\%$ 



<span id="page-5-1"></span>**Fig. 6** Relationships between collapsible potential and initial water content

wetting process. Therefore, soil mixtures with higher clay fractions exhibit a more significant  $C_p$  during the wetting process. After wetting, the specimens with a higher clay fraction exhibit high volume compression during further static loading from  $\sigma'_v$  = 220 to  $\sigma'_v$  = 440 kPa, indicating the residual potential of soil deformation because of the higher clay fraction (Choo et al. [2017\)](#page-11-31). Note that the specimens with lower clay fractions (i.e., S80-C20 and S60-C40) show negligible changes in the compression index  $(C_c = \text{change})$ in void ratio/change in log  $\sigma'$ <sub>v</sub>) before and after wetting, whereas the  $C_c$  values of specimens with higher clay fractions increases more than fvefold after collapse (Fig. [7](#page-6-0)), demonstrating that the specimens with higher clay fractions experience a more signifcant decrease in suction pressure than specimens with lower clay fractions.

Because the specifc surface of kaolin particles is signifcantly larger than that of sand particles, it can be assumed that most of the water molecules are adsorbed by clay particles rather than sand particles at low water contents (Agus et al. [2010\)](#page-10-2). Based on this assumption, the clay water content  $w_c$  (%) in Eq. [\(1](#page-5-2)) can capture the variation in suction pressure in sand–clay mixtures with varying water contents and clay fractions  $(f_c)$  (Agus et al. [2010](#page-10-2)).

<span id="page-5-2"></span>
$$
w_c = \frac{w}{f_c} \tag{1}
$$

where  $w$  = water content (weight ratio between water and solid, including sand and clay in this study);  $w_c$ ,  $w_r$ , and  $f_c$  are in percentage. Figure [8](#page-6-1) shows the collapse potential as a function of  $w_c$  and demonstrates that the collapse



<span id="page-6-0"></span>**Fig.** 7 Evolution of vertical strain during the  $K_0$ -consolidation and wetting under the identical initial water content  $w = 12\%$ : (a) S80-C20; (**b**) S60-C40; (**c**) S40-C60; (**d**) S20-C80



<span id="page-6-1"></span>**Fig. 8** Relationships between collapse potential and clay water content of the tested specimens with varying clay fractions. Note clay water content  $w_c =$ Eq. ([1\)](#page-5-2)

potential follows the power function of  $w_c$ . Surprisingly, the four curves of the collapse potential versus the initial water content space in Fig. [6](#page-5-1) appear to merge into a single trend (Fig. [8](#page-6-1)). In other words, the variation in the collapse potentials of the tested materials with varying clay fractions could be the sole function of  $w_c$ . Because  $w_c$  determines the suction pressure of sand–clay mixtures, Fig. [8](#page-6-1) indicates that a decrease in soil suction is the most important reason for the collapse behavior of soils (Mahmood and Abrahim [2021](#page-11-16)).

#### **Efect of dry unit weight on collapse potential**

The tested specimens containing various sand/clay fractions have different ranges of dry unit weights, as shown in Fig. [3](#page-3-0). Complementary tests are conducted on the S20-C80 specimens (i.e., sand fraction  $= 20\%$  and clay fraction =  $80\%$ ) at an initial water content of  $18\%$  (= optimum water content for the S20-C80 specimen) to clearly explore the effects of packing density on the collapse potential (Fig. [3](#page-3-0)d). Figure [9a](#page-7-0) shows that a higher dry unit weight constrains the collapse potential compared to a relatively lower dry unit weight because densely packed specimens tend to exhibit a greater frictional resistance. Additionally, a change in the dry unit weight at a constant water content results in a change in the degree of saturation. Because the degree of saturation is one of the most critical parameters that influence the collapse



<span id="page-7-0"></span>**Fig. 9** Efects of (**a**) initial dry unit weight and (**b**) degree of saturation on the collapsible potential of S20-C80 specimens

potential (Basma and Tuncer [1992](#page-11-32); Li et al. [2016](#page-11-17); Hou et al. [2021](#page-11-33); Khodabandeh et al. [2023\)](#page-11-20), the collapse potential of the S20-C80 specimens is plotted as a function of the degree of saturation in Fig. [9](#page-7-0)b. For comparison, the results of the S20-C80 specimens with varying initial water contents in Fig. [6](#page-5-1) also overlap in Fig. [9](#page-7-0)b. Because an increase in the dry unit weight results in a decrease in the degree of saturation and the consequent less contribution of the metastable forces supporting the soil particles prior to wetting, the collapse potential decreases with increasing dry unit weight. However, the changes in the collapse potential caused by the dry unit weight are less significant than those caused by the water content (Fig. [9](#page-7-0)b). This implies that the dry unit weight has a secondary effect on the collapse potential, particularly in specimens with a high collapse potential (i.e., S20- C80). In this context, it is notable that the total suction of sand–clay mixtures is mainly determined by the initial water content, whereas the influence of the initial dry density on the magnitude of the suction pressure is insignificant (Agus et al. [2010\)](#page-10-2).

#### **Shear wave velocity reduction during wetting**

The shear wave velocity  $(V<sub>s</sub>)$  is measured during the consolidation and wetting processes. Figure  $10$  shows the  $V<sub>s</sub>$ evolution for the S40-C60 specimens with diferent initial water contents. Because the applied stress determines the interparticle contact stiffness, the  $V<sub>s</sub>$  of dry and saturated soils can be expressed as a power function of the mean efective stress  $(\sigma'_m)$ :

<span id="page-7-1"></span>
$$
V_s = \alpha \bullet \left(\frac{\sigma_m \prime}{P_r}\right)^{\beta} \tag{2}
$$

where  $\alpha$  and  $\beta$  are experimentally determined fitting parameters and  $P_r$  is the reference pressure  $(= 1 \text{ kPa})$  in unit matching  $\sigma'_{m}$ . The  $\alpha$ -factor corresponds to the  $V_s$  value at  $\sigma'_m = P_r = 1$  kPa and significantly reflects the packing state (i.e., interparticle coordination), and the *β*-exponent corresponds to the  $V<sub>s</sub>$  sensitivity of tested materials to the changes in  $\sigma'_m$ . In the case of unsaturated soils, the matric suction  $(u_a - u_w)$ , where  $u_a$  is the pore air pressure, and  $u_w$  is the pore water pressure) gives an additional increase in interparticle contact stifness (Kim et al. [2023;](#page-11-34) Shwan [2023\)](#page-12-8). Note the osmotic suction is negligible in the case where the pore water is tap water or deionized water (Alramahi et al. [2010](#page-10-3); Mahmood and Abrahim [2021](#page-11-16))**.** Thus, Eq. [\(2](#page-7-1)) can be modifed as follows (Clariá and Rinaldi [2007\)](#page-11-35):

<span id="page-7-2"></span>
$$
V_s = \alpha \bullet \left(\frac{\sigma_m \prime}{P_r}\right)^{\beta} + \lambda \bullet (u_a - u_w)
$$
 (3)

where  $\lambda$  is the fitting parameter, which reflects the packing state and soil type.

During vertical loading (i.e., consolidation), an increasing trend in  $V<sub>s</sub>$  is observed because of the improved soil stiffness at a higher vertical effective stress  $\sigma'_{v}$  (Eqs. [\(2](#page-7-1)) and [\(3](#page-7-2)), and Fig. [10](#page-8-0)). However, a sharp decrease in *V<sub>s</sub>* occurs during wetting, mainly owing to the loss of soil stifness at higher water contents. Additional loading of  $\sigma'_{v}$ =440 kPa after wetting results in an increase in  $V<sub>s</sub>$  (Eq. ([2\)](#page-7-1) and Fig. [10\)](#page-8-0). As already implied in the comparison between Eqs.  $(2)$  $(2)$  and  $(3)$  $(3)$ , this observation indicates that wetting-induced collapse prevails when a reduction in small-strain stifness results from the breakage of the metastable soil fabric due to decreased soil suction. Similar to the results presented in Fig. [5](#page-5-0), Fig. [10](#page-8-0) also shows a significant decrease in the  $V<sub>s</sub>$  values of the specimens with lower initial water contents, indicating that the specimens with higher volume compression (i.e., greater collapse potential) during the wetting process exhibit a greater reduction in *Vs*.

Figure [11](#page-8-1) presents the relationship between the collapse potential and shear wave velocity reduction  $\Delta V_s$  during wetting. The collapse of the specimens is triggered by





<span id="page-8-0"></span>**Fig. 10** Shear wave velocity values during the  $K_0$ -consolidation and wetting of S40-C60 specimens with diferent initial water content: (**a**) initial water content  $w=9\%$ ; (**b**)  $w=11\%$ ; (**c**)  $w=13\%$ ; (**d**)  $w=15\%$ .



<span id="page-8-1"></span>**Fig. 11** Relationships between collapse potential and shear wave velocity reduction during wetting

a reduction in stifness, resulting in a greater reduction in *Vs*. This increases the collapse potential, leading to a positive relationship between  $\Delta V_s$  and the collapse potential. Figure [11](#page-8-1) also shows that  $\Delta V_s$  increase with decreasing clay fraction at a given collapse potential. This implies that

The wetting occurred at a vertical stress of 220 kPa. The captured typical shear wave signatures are presented in Fig. [1](#page-2-0)

the infuence of decreased suction pressure on the collapse potential and  $\Delta V_s$  differs according to the soil type. At the later part of the wetting, the measured  $V<sub>s</sub>$  show an increased trend (recovery) with time, following the  $V<sub>s</sub>$  reduction upon wetting (Fig. [10](#page-8-0)). More details of  $V<sub>s</sub>$  recovery will be discussed in the next Section.

#### **Sher wave velocity recovery during wetting**

Soils often involve time-varying load–deformation responses; in fact, some portion of shear wave velocity  $(V<sub>s</sub>)$ can be recovered during wetting (Fig. [10](#page-8-0)). Thus, Fig. [12a](#page-9-0) shows the time-dependent variations in the volumetric strain and  $V<sub>s</sub>$  for the S60-C40 specimen at an initial water content of *w*=9%. Rearrangement of soil particles (or volume compression of soil) occurs when the induced stress in the soil exceeds the frictional resistance between the soil particles (Won et al. [2023](#page-12-9)). As the wetting process induces a decrease in suction pressure and a consequent decrease in efective stress as a function of time, the frictional resistance between the soil particles decreases during wetting processes. Thus, under a constant applied stress level (i.e., an inundation stress of 220 kPa), the tested specimens settle over time and



<span id="page-9-0"></span>**Fig. 12** Shear wave velocity response during soil collapse: (a) timedependent collapsible soil behavior, including the variations of vertical strain and shear wave velocity of S20-C80 specimen with initial water content  $w=14\%$ ; (b) relationships between collapse potential and shear wave velocity ratio. Note shear wave velocity ratio=shear wave velocity after collapse / shear wave velocity before collapse

reach a stable volumetric state and asymptotic strain. Similarly, a progressive decrease in  $V<sub>s</sub>$  with time is observed upon wetting, as shown in Fig.  $12a$ . However,  $V_s$  slightly increase after~200 min when settlement ceases, refecting the emergence of a new stable soil structure.

The second term in Eq.  $(3)$  $(3)$  $(3)$  decreases upon wetting, resulting in a time-dependent decrease in  $V<sub>s</sub>$  during wetting. However, the collapse of soils (i.e., a large volume decrease in soils) results in the rearrangement of soil particles to achieve a dense packing condition (i.e., increased interparticle coordination). Thus, the  $\alpha$ -factor in Eq. [\(2](#page-7-1)) after collapse is greater than that in Eq. [\(3](#page-7-2)) before collapse, resulting in some recovery of  $V<sub>s</sub>$ . Many previous studies reported that stiff materials exhibit greater  $\alpha$ , and the  $\alpha$  value for a given soil increases with decreasing void ratio (Santamarina et al. [2001](#page-12-10); Choo and Burns [2015;](#page-11-36) Won et al. [2023](#page-12-9)). This *V*<sub>s</sub> recovery during wetting can also be attributed to the increase in mean effective stress  $(Eq. 2)$  $(Eq. 2)$  because the horizontal stress under the constant  $\sigma'$ <sub>v</sub> increases upon wetting (Fattah and Dawood [2020](#page-11-37); Mahmood and Abrahim [2021](#page-11-16)**)**.

The shear wave velocity ratio ( $V<sub>s</sub>$  ratio =  $V<sub>s</sub>$  after collapse  $/V<sub>s</sub>$  before collapse) is defined, and a relationship of the collapse potential against the  $V<sub>s</sub>$  ratio is plotted to quantify the degree of shear wave velocity recovery (Fig. [12](#page-9-0)b). The *V<sub>s</sub>* ratio increases with decreasing collapse potential. This observation indicates that  $V<sub>s</sub>$  with higher initial water contents in the soil exhibited lower dependency on suction stress; therefore, the decreased  $V<sub>s</sub>$  induced by the loss of soil suction could be recovered by forming a new stable soil structure. In addition, soils with a moderate degree of collapse, according to ASTM D5333, can exhibit a *V<sub>s</sub>* ratio of 0.85, indicating that moderately collapsible soils can exhibit a 15% decrease in  $V<sub>s</sub>$  upon wetting (Fig. [12b](#page-9-0)). Note that a 15% decrease in  $V<sub>s</sub>$  indicates a decrease of 28% in the small-strain stifness. Thus, the collapse of soils afects both the serviceability and stability of geostructures. Although the settlement ceases after the wetting-induced collapse and a higher dry density is expected, the initial stifness (or mechanical properties) could not be recovered (Fig. [10\)](#page-8-0).

The  $V<sub>s</sub>$  ratio of the tested materials is plotted as a function of the initial degree of saturation (*S*) to determine the condition where  $V<sub>s</sub>$  could be fully recovered after the collapse because the tested materials showed diferent optimum water contents and maximum dry unit weights according to the clay fractions (Fig. [13\)](#page-10-4). Most notably, it can be observed that the  $V<sub>s</sub>$  ratios of all tested materials with varying clay fractions and initial water contents are equal to or greater than 1.0 when the nominal *S* is greater than approximately 50%. Thus, being apart from the settlement of collapsible soils, the sand–clay mixtures used in the compaction fll should be compacted to have an initial degree of saturation exceeding 50% to prevent permanent stifness/strength loss upon wetting.

# **Conclusions**

In this study, the collapse potentials of specimens with various sand–clay fractions are experimentally investigated by considering factors, such as the initial water and clay content. The specimens are subjected to a static vertical stress up to  $\sigma'_{v}$  = 440 kPa in an instrumented oedometer cell, where they experience wetting at a constant  $\sigma'_{v}$ =220 kPa. The shear wave velocity  $(V<sub>s</sub>)$  is continuously measured during the loading and wetting processes. The main fndings are summarized as follows.

• The calculated collapse potentials of the tested specimens containing various sand/clay fractions decrease with increasing initial water content and dry unit weight because of the less signifcant contribution of the metastable forces supporting the soil particles before wetting.



<span id="page-10-4"></span>**Fig. 13** Relationship between initial degree of saturation and shear wave velocity ratio

- The collapse potential of the tested sand–clay mixtures increases with increasing clay fraction at a specifc water content. However, the variation in the collapse potential of the tested materials with varying clay fractions and water contents is the sole function of the clay water content regardless of the clay fraction because most of the water molecules are adsorbed by clay particles.
- Because the suction pressure fades away during the wetting process, the shear wave velocity  $(V<sub>s</sub>)$  of the tested materials shows a time-dependent decrease during wetting. However, when the settlement ceases, a portion of the shear wave velocity could be recovered over time because of forming a new stable soil structure with a denser packing state and greater lateral effective stress. This results in that the ratio of  $V<sub>s</sub>$  before collapse to  $V<sub>s</sub>$ after collapse ranges from 0.85 to 1.05.
- Shear wave velocity measurements successfully capture the loss of capillary suction pressure (i.e., small-strain stifness) during the wetting. More pronounced collapse potential and shear wave velocity reduction are observed with the decrease in the initial water content.
- Similar time-dependent variations of shear wave velocity and settlement during wetting, and the positive relationship between shear wave velocity reduction and collapse potential imply that the geophysical approach, newly suggested in this study based on shear wave velocity measurements, can be benefcially employed as a tool for the study of collapse mechanism.

• The decrease in the shear wave velocity upon wetting could be fully recovered when the initial degree of saturation of the tested materials is greater than approximately 50%. Therefore, it is suggested that the initial degree of saturation should be higher than 50% in the compaction fll to expect the recovery of stifness/strength after the soil collapse behavior.

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**Data availability** The datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

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