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Compositional verification of real-time systems using ECDAR

Alexandre David • Kim. G. Larsen • Axel Legay • Mikael H. Møller • Ulrik Nyman • Anders P. Ravn • Arne Skou • Andrzej Wąsowski

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Abstract We present a specification theory for timed systems implemented in the ECDAR tool. We illustrate the operations of the specification theory on a running example, showing the models and verification checks. To demonstrate the power of the compositional verification, we perform an in depth case study of a leader election protocol; Modeling it in ECDAR as Timed input/output automata Specifications and performing both monolithic and compositional verification of two interesting properties on it. We compare the execution

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A. David · K. G. Larsen · M. H. Møller · U. Nyman (⊠) ·
A. P. Ravn · A. Skou
Department of Computer Science, Aalborg University,
Aalborg, Denmark
e-mail: ulrik@cs.aau.dk

A. David e-mail: adavid@cs.aau.dk

K. G. Larsen e-mail: kgl@cs.aau.dk

M. H. Møller e-mail: mikaelhm@cs.aau.dk

A. P. Ravn e-mail: apr@cs.aau.dk

A. Skou e-mail: ask@cs.aau.dk

A. Legay INRIA/IRISA, Rennes Cedex, France e-mail: axel.legay@irisa.fr

A. Wąsowski

IT University of Copenhagen, Copenhagen, Denmark e-mail: wasowski@itu.dk

time of the compositional to the classical verification showing a huge difference in favor of compositional verification.

Keywords Timed input/output automata · Compositional verification · Real-time systems · Leader election protocol

1 Introduction

Programs are intrinsically component based, they are built from simple commands, and when we reason about their correctness, we intuitively think in terms of what we can assume about the program state before the command is performed and what it guarantees about the state afterwards. This simple fact was formalized early on in terms of Floyd assertions [19] and led to Floyd–Hoare logic [21] and is really the foundation of program verification, which led to much fruitful research in the following years. In particular, the challenge of compositional analysis of concurrent programs was pursued first by Owicki and Gries [32], who extended Floyd–Hoare logic to parallel programs with shared variables, and later by Jones [24], who introduced the rely-guarantee method, allowing for a compositional version of the Owicki-Gries method. Yet, there are larger components in software applications: subroutines from libraries, classes in object-oriented languages, service modules in service-oriented architectures, control modules in embedded systems, etc.

Common for such larger scale components are the characteristics made explicit by Szyperski [36]:

a unit of composition with contractually specified interfaces and fully explicit context dependencies that can be deployed independently and is a subject to third party composition. We shall not consider deployment or component implementation. These are interesting questions, but we get to grips with *composition* at the level of *interfaces*, because this is essential for getting a useful product out of gluing components together and deploying them. Interfaces are essentially specifications of what we assume about the environment of the component and what the implementation guarantees to deliver. To have a good theory for reasoning about component interface specification, we expect that for a given specification, we can determine:

Consistency When a specification is satisfied by at least one implementation it is consistent. Consistency is needed to verify that specifications are well formed and do not contain contradictory statements. Without consistency, we can specify miraculous components which no one can deliver.

Conjunction Specifications are essentially logics, and when composing them using conjunction this should give exactly the intersection of feasible implementations of the constituents. Should the intersection be empty, that is, the conjunction is not consistent, it is useless to put those components together.

Composition When actual components are deployed together, they form a new composite component. A similar parallel composition operation is needed for their specifications to build systems in a stepwise manner.

Refinement There is a natural partial order on components defined by replacement of one by another, while maintaining the functionality of the system as a whole. When such substitutions are possible, the more detailed and constraining specification *refines* the one for the component that is replaced.

Specification theories with refinement were pioneered by Jones [25] in a setting of sequential program components and it has lead to further development of such theories, most recently in the area of object-oriented programming with design by contract and for instance the Java Modeling Language (JML) [29].

However, since we wish to deal with a context of distributed, communicating components, a specification theory with the state given by program variables is not well suited. Specifications for such systems are better built on process algebras [5] and their underlying transition system semantics. Transition systems are also intimately linked to automata models. Since transition systems generate traces of events or actions, specification logics describe properties of traces, and here a very liberal use of assumptions and guarantees may lead to unsound reasoning. Essentially, a guarantee can specify that the past is changed to fit an assumption, or an assumption can speak about a future that the guarantee contradicts. This was investigated by Abadi and Lamport [1]. However, since the specification formalism employed here is automata based, it does not suffer from these anomalies.

An interesting question with (parallel) composition of components is whether one can find a strongest specification for an unknown component that composes with a given one to give a desired result. It is the question of finding a *quotient* or a weakest prespecification. This can be done for the current theory, a result that originates in [4,27,28]. Similar results in a logic-based refinement theory are found in [22], although this solution is more a proof of existence than an actual construction.

1.1 Related work

In a series of recent work, it has been advocated that specifications can be represented by interface automata that are automata whose transitions are typed with input and output. The semantics of such an automaton is given by a two-player game: the *input* player represents the environment, and the output player represents the component itself. Contrary to the input/output model proposed by Lynch [31], this semantic offers an optimistic treatment of composition: two interfaces can be composed if there exists at least one environment in which they can interact together in a safe way. In [16], a timed extension of the theory of interface automata has been introduced, motivated by the fact that time can be a crucial parameter in practice, e.g., in embedded systems. In this paper, we represent specifications by timed input/output automata (TIOAs) [26], i.e., timed automata whose sets of discrete transitions are split into input and output transitions. Contrary to [16] and [26], we distinguish between implementations and specifications by adding conditions on the models. This is done by assuming that implementations have fixed timing behavior and they can always advance either by producing an output or delaying. Also, we provide a gamebased methodology to decide whether a specification is consistent, i.e. whether it has at least one implementation. An implementation exists when there is a strategy that despite the behavior of the environment will avoid states that cannot possibly satisfy the implementation requirements.

Our theory is rich in the sense that it captures all the good operations for a compositional design theory discussed above. Also, all the algorithms have been implemented in the ECDAR tool set. This implementation (available at http://ecdar.cs.aau.dk/) is build on top of the UPPAAL-TIGA tool-set[7]. UPPAAL-TIGA is a tool that implements a series of algorithms for solving timed games [10] as well as checking timed temporal logic properties. ECDAR uses UPPAAL-TIGA to solve various games that arise in computing the composition operations and refinements.

The first part of the paper presents an overview of the theory implemented in the ECDAR tool set. The second, and

maybe most interesting part of the paper, applies ECDAR theory to a leader election protocol. More precisely, we show how compositional design can be used to check two important properties of the protocol in an incremental manner, outperforming classical model checking techniques for timed automata that are working on the entire system directly. The incremental approach used is based on the concept of independent implementability [15], in which a specification can be refined into a more detailed specification independently of what it is composed with. This method is correct because our refinement operator is a precongruence with respect to parallel composition [13].

Another tool supporting refinement is PAT [34,35]. Unlike ECDAR, it builds on CSP with a failures, divergences and refusal semantics which makes a direct comparison difficult. However, the CSP theory does not support quotienting or simple conjunction of specifications. And thus in contrast to ECDAR, PAT does not support assume/guarantee reasoning about systems.

1.2 Structure

The rest of the paper falls in three parts: Theory, Case-study and Conclusion. The theory is presented in Sect. 2 on page 705. The theory with its definitions is included to make the paper self-contained. Theorems and proofs can be found in [13]. The case-study, a leader election protocol, is presented in Sect. 3 on page 711. While conclusion and future work is given in Sect. 4 on page 717.

2 Timed input/output automata specifications

Before we proceed to discuss our case study, let us present the main concepts and constructions of the specification theory for real-time systems supported by the ECDAR tool. We only focus on the designer-facing aspects of the framework. A reader interested in the theoretical discussions is referred to [13].

The main concept in our modeling framework is that of a specification—an abstract, usually under-specified, description of an implementation of a system. Each specification normally admits multiple implementations that can be derived by different resolutions of detailed design choices.

We use the syntax of TIOAs to represent specifications. We will now recall their definition and only then proceed to define specifications themselves along with a notion of satisfaction of a specification by an implementation, notion of refinement between specifications, and the compositional design operators that allow manipulating and combining specifications.

TIOAs are essentially the usual timed automata [2] extended with two types of edges: inputs and outputs. Input



Fig. 1 University specification UniSpec

edges are drawn as solid arrows labeled by actions followed by a question mark. Output edges are dashed and their actions are suffixed with an exclamation point. Figure 1 shows an example of a TIOA describing the main research process at a hypothetical university, that, given grants as inputs produces patents as outputs.

The kind of communication an automaton can engage in is limited by its *sort*—a signature of available input and output actions. In Fig. 1, the sort is depicted as incoming arrows (inputs) and outgoing arrows (outputs) incident with the border surrounding the automaton. The initial location is indicated by a doubly circled outline. In this initial location, after the university receives the grant input, it will output a patent.

The colors used in the figures do not carry semantic meaning but are used consistently to increase the readability of the models. These colors—guards (green), resets (navy blue), invariants (violet), and actions (turquoise)—are the same as used in the editor of ECDAR and in related tools such as UPPAAL.

Additional labels on edges denote timing constraints over *clocks* (known as guards) and clock *resets*. For example, the grant must be received before the clock u exceeds two time units $(u \le 2)$. This clock is reset immediately upon reception of the grant (u = 0). Then, the patent is issued within 20 time units, as the automaton can only reside in the target location for twenty time units as indicated by the *location invariant* $u \le 20$. Any further grants received within this time interval are ignored through the grant input loop that has no guard and no resets. When the patent is issued the clock u is again reset.

If the first grant arrives after more than two time units, or if any subsequent grant arrives later than two time units after a patent has been filed, then the behavior of the university automaton becomes *unpredictable*. This is captured by the leftmost location in the figure, a so-called *universal* location, in which any communication can appear at any time; the location has outgoing edges for any available action and imposes no timing constraints. Strictly speaking, the behavior of the automaton is still completely specified, but since it provides

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no guarantees about its output in a *universal* location we also call this unpredictable.

Let us now recall a formal definition of a TIOA:

Definition 1 A timed I/O automaton (TIOA) is a tuple A =(Loc, q_0 , Clk, E, Act, Inv) where Loc is a finite set of locations, $q_0 \in$ Loc is the initial location, Clkis a finite set of clocks, $E \subseteq$ Loc × Act × $\mathcal{B}(Clk) \times \mathcal{P}(Clk) \times$ Loc is a set of edges with $\mathcal{B}(Clk)$ being a set of clock constraints, $\mathcal{P}(Clk)$ is the set of clocks to reset, Act = Act_i \uplus Act_o is a finite set of actions, partitioned into inputs and outputs, respectively, and Inv : Loc $\mapsto \mathcal{B}(Clk)$ is a set of location invariants.

As we have intuitively sketched above, TIOA syntax has a semantic interpretation as a timed execution of a branching process. This is formally captured by a Timed I/O transition system (TIOTS), which is like a usual discrete automaton but infinitely branching and over an infinite state space. In a TIOTS, time delays are modeled as continuously many 'discrete' actions.

Definition 2 (*TIOTS*) A TIOTS is a quadruple $S = (St^S, s_0, \Sigma^S, \rightarrow^S)$, where St^S is an infinite set of states, $s_0 \in St$ is the initial state, $\Sigma^S = \Sigma_i^S \oplus \Sigma_o^S$ is a finite set of actions partitioned into inputs (Σ_i^S) and outputs (Σ_o^S) and $\rightarrow^S : St^S \times (\Sigma^S \cup \mathbb{R}_{\geq 0}) \times St^S$ is a transition relation. We write $s \stackrel{a}{\rightarrow} s'$ instead of $(s, a, s') \in \rightarrow^S$ and use i?, o! and d to range over inputs, outputs and $\mathbb{R}_{\geq 0}$, respectively. We sometimes omit the transition system name $(s \stackrel{a}{\rightarrow} s')$ if obvious from the context and we omit the target location $(s \stackrel{a}{\rightarrow} s)$ if we only need to know the existence but not the identity of the target location. In addition any TIOTS satisfies the following:

[time determinism] whenever $s \xrightarrow{d} S'$ and $s \xrightarrow{d} S''$ then s' = s''[time reflexivity] $s \xrightarrow{0} S'$ for all $s \in St^S$

[time additivity] for all $s, s'' \in St^S$ and all $d_1, d_2 \in \mathbb{R}_{\geq 0}$ we have $s \stackrel{d_1+d_2}{\longrightarrow} s''$ iff $s \stackrel{d_1}{\longrightarrow} s'$ and $s' \stackrel{d_2}{\longrightarrow} s''$ for an $s' \in St^S$

A *state* of the TIOTS derived from a TIOA *A* is a pair (q, V) where *q* is a location and *V* : Clk $\mapsto \mathbb{R}_{\geq 0}$ is a *valuation function* that assigns a non-negative value to each clock in Clk. We use *u*, *u'* to range over clock valuations. We write u + d, where $d \in \mathbb{R}_{\geq 0}$ is a delay, to denote a valuation such that for any clock *r* we have (u+d)(r) = x + d iff u(r) = x. Given $c \subseteq$ Clk, we write $u[r \mapsto 0]_{r \in c}$ for a valuation which agrees with *u* on all values for clocks not in *c*, and returns 0 for all clocks in *c*. We use **0** to denote the constant function mapping all clocks to zero. The *initial state* of *A* is the pair $(q_0, \mathbf{0})$.

The semantics of a TIOA $A = (\text{Loc}, q_0, \text{Clk}, E, \text{Act}, \text{Inv})$ is a TIOTS $\llbracket A \rrbracket_{\text{sem}} = (\text{Loc} \times (\text{Clk} \mapsto \mathbb{R}_{\geq 0}), (q_0, \mathbf{0}), \text{Act}, \rightarrow)$, where \rightarrow is the transition relation defined by the following rules:

- Each $(q, a, \varphi, c, q') \in E$ gives rise to $(q, u) \xrightarrow{a} (q', u')$ for each clock valuation $u \in [\text{Clk} \mapsto \mathbb{R}_{\geq 0}]$ such that $u \models \varphi$ and $u' = u[r \mapsto 0]_{r \in c}$ and $u' \models \text{Inv}(q')$.
- Each location q ∈ Loc with a valuation u ∈ [Clk → ℝ_{≥0}] gives rise to a transition (q, u) → (q, u + d) for each delay d ∈ ℝ_{≥0} such that u + d ⊨ Inv(q).

We only consider deterministic TIOAs, so TIOAs whose semantics results in a deterministic TIOTS: for each action– state pair at most one action is enabled.

2.1 Specifications

We now define specifications in terms of TIOAs.

Definition 3 A specification automaton is a TIOA that is input-enabled, i.e., in each state all the inputs should be available at all times.

The assumption of input-enabledness, also seen in many interface theories [17,20,30,33,37], reflects our belief that an input cannot be prevented from being sent to a system, but it might be unpredictable how the system behaves after receiving it. The idea is actually quite old, and can be traced to the notion of a CHAOS process in CSP [23].

Input-enabledness encourages explicit modelling of unpredictability, and compositional reasoning about it; e.g., deciding if an unpredictable behavior of one component induces unpredictability of the entire system. Observe that, it is easy to check whether a TIOA is input-enabled. In practice, tools can interpret absent input transitions in at least two reasonable ways. First, they can be interpreted as ignored inputs, corresponding to location loops in the automaton. Second, they may be seen as unavailable ('blocking') inputs, which can be achieved by assuming implicit transitions to a designated error state.

We note that our example of Fig. 1 can always accept grant? from any location. It is also deterministic. Thus, UniSpec TIOA is a well-formed specification.

2.2 Implementations

The role of specifications in a specification theory is to abstract, or under-specify, sets of possible implementations. *Implementations* are concrete executable realizations of systems. We will assume that implementations of timed systems have fixed timing behavior (outputs occur at predictable times) and systems can always advance either by producing an output or delaying. An implementation that cannot voluntarily output or delay would have to block passage of time, which is not realistic.

Definition 4 An implementation *P* is a specification whose underlying TIOTS satisfies the following conditions:



Fig. 2 a Specification of a coffee/tea Machine, b an implementation, and (c-h) more specifications of a coffee/tea machine

1. Independent progress: in each state, either an output is possible or one can delay until an output is enabled.

either $(\forall d \ge 0, p \xrightarrow{d}^{P})$ or $\exists d \in \mathbb{R}_{\ge 0}, \exists o! \in \Sigma_{0}^{P}, p \xrightarrow{d} p' \text{ and } p' \xrightarrow{o!}^{P}.$

- 2. Output urgency: an available output cannot be delayed:
 - $\forall p', p'' \in St^P \text{ if } p \xrightarrow{o!} p' \text{ and } p \xrightarrow{d} p'' \text{ then } d = 0 \text{ (and consequently, due to determinism and time reflexivity we have <math>p = p''$)

Example Figure 2a specifies a vending machine that can serve tea or coffee. We will use this as a component in our example. A possible implementation of this machine can be found in Fig. 2b. The implementation *refines* the specification, which is defined in the next section. Both automata are deterministic. Note that the output transitions of the implementation Impl arrive at a fixed moment in time and cannot be delayed, which guarantees output urgency (the invariant guarantees progress and the guard constrains the transition). Each time, the output tea! from Idle to Idle is taken, the clock y is reset. Without this reset, independent progress would not be guaranteed for valuations of the clock y that are greater than 6.

2.3 Satisfaction and refinement

Refinement is always a pivotal element of a specification theory. Akin to entailment for logical specifications, refinement allows to start with very abstract models, and elaborate them towards more specific ones. An early *abstract* specification would typically allow a large set of diverse implementations. This set is monotonically reduced in a stepwise refinement process towards a detailed, more fine grained and *concrete* specification that can be implemented directly.

Any refinement should satisfy the following *substitutability* condition: If A_S refines A_T , it should be possible to replace A_T with A_S in every context and obtain a safe system. It is well known from the literature [8, 14, 15] that to give these kind of guarantees a refinement should have the flavor of *alternating (timed) simulation* [3].

In our theory, we define the refinement between specifications, by requiring a suitable refinement relation in their semantic expansion (TIOTS).

Definition 5 (*Refinement relation*) Let A_S and A_T be two specification automata and $S = (St^S, s_0, \Sigma, \rightarrow^S)$ and $T = (St^T, t_0, \Sigma, \rightarrow^T)$ be their corresponding timed transition systems. We say that A_S refines A_T , written $A_S \leq A_T$, iff there exists a binary relation $R \subseteq St^S \times St^T$ containing (s_0, t_0) and for all states sRt implies:

- 1. Whenever $t \xrightarrow{i?} t'$ for some $t' \in St^T$ then $s \xrightarrow{i?} s'$ and s'Rt' for some $s' \in St^S$
- 2. Whenever $s \xrightarrow{o! S} s'$ for some $s' \in St^S$ then $t \xrightarrow{o! T} t'$ and s'Rt' for some $t' \in St^T$
- 3. Whenever $s \xrightarrow{dS} s'$ for $d \in \mathbb{R}_{\geq 0}$ then $t \xrightarrow{dT} t'$ and s'Rt' for some $t' \in St^T$.

Intuitively, if A_S refines A_T then it can delay at most as much as A_T can, and it can only produce outputs that A_T produces—not others. It, however, may admit more inputs than A_T , as long as all A_T 's inputs are handled. This construction ensures substitutability, because then, if placed in the same context, A_S will engage in less computations than A_T , while



Fig. 3 Specification of a the Researcher, and the Administration as a conjunction of two components, b HalfAdm1 and c HalfAdm2

maintaining ability to always receive the same inputs. This means that safety properties will be preserved.

In the example of Fig. 2, Machine2 (Fig. 2c), Machine3 (Fig. 2d), and Machine4 (Fig. 2e) refine Machine (Fig. 2a). Machine6 (Fig. 2f) refines both Machine3 (Fig. 2d) and Machine4 (Fig. 2e). Machine7 (Fig. 2h) refines Machine4 (Fig. 2e).

Definition 5 is non-constructive in the sense that it cannot be directly used to decide refinement between two automata. Discussion of a proper efficient refinement checking algorithm is out of scope for this work. See [8, 13] for details.

We relate specifications to implementations using a notion of *satisfaction*. A proper implementation of a specification is said to satisfy it. Technically, in our framework, the satisfaction is a special case of the refinement, when the left hand side is an implementation (it satisfies independent progress and output urgency—see Definition 4).

The set of all implementations of A is denoted $[\![A]\!]_{mod}$. In [13], we have shown that the refinement relation is complete for our implementation model, i.e., A_S refines A_T if and only if the set of implementations that satisfy A_S is included in the set of implementations that satisfy A_T . This is an important usability criterion for tools. It means that if you indeed elaborated A_T into A_S such that any implementation of the latter implements the former, the tool will never report a false positive when checking $A_S \leq A_T$.

Consistency It can happen that a specification cannot be implemented, e.g., because it enforces reachability of a stuck state, which violates independent progress. As all implementations satisfy independent progress, they can never satisfy such a specification. We say that a specification which admits at least one implementation is (globally) *consistent*. For example, coffee machine of Fig. 2, the implementation Fig. 2b refines Fig. 2a. Since Fig. 2a admits at least one implementation.

In the example of Fig. 2, Machine5 (Fig. 2g) is in fact inconsistent since, in the state Serving no output is

available and time cannot diverge, thus violating independent progress.

Inconsistency of a specification in a stepwise design process is normally unintended—an error on behalf of the specifier. Thus, it is important for tools to provide feedback on consistency. In [13], we have shown that this question can be answered automatically using an algorithm that decides if there exists a strategy for the system (output) to avoid reaching stuck states in the specification. Furthermore, we added a facility called *pruning* that removes from the TIOA all behaviors that are not covered by such a maximal strategy. Pruning thus reduces the size of the TIOA specification by removing inconsistent parts, while maintaining the same set of implementations (Theorem 5 in [13]).

2.4 Step-wise refinement

We decompose and refine our University specification of Fig. 1 in a top-down manner. The refinement is based on a knowledge of how the system under design is supposed to meet the overall requirements. We decompose our specification into three components in parallel: a Coffee/Tea machine, a Researcher, and an Administration. The Machine (Fig. 2a) needs coins to function and provides the Researcher with coffee and tea. In addition, it may offer tea for free. The Researcher (Fig. 3a) produces publications with some guaranteed timing constraints when provided with coffee and tea regularly, otherwise the publication output is not guaranteed any more. The Administration is in charge of turning grants into coins to enable the use of the Machine and also to file patents when publications are produced by the Researcher. We could make one TIOA to specify this behavior, but it is naturally expressed as a conjunction and making this TIOA manually is error prone. Instead, we specify our Administration as a conjunction of HalfAdm1 and HalfAdm2, each in charge of one of the tasks. Figure 3b shows the alternation between coin! and grant? while Fig. 3c shows the alternation between patent! and pub? We note that since both automata are parts of the administration, HalfAdm1 always allows patent! and HalfAdm2 always allows coin!. Both sub-specifications are also input-enabled and can always accept grant? and pub?

Verification of this refinement is carried out step-wise using *pruning* at every step. In this example, the components are checked for consistency individually and pruned to valid behaviors. Then, they are combined step-wise, first with the conjunction operator (explained later), the result being pruned, and then with the composition operator, and then pruned. The resulting state graphs for both specifications are finally checked for refinement.

The result here is that the refinement does not hold, which may seem surprising. It turns out that the original specification of Fig. 1 does not allow for "free" patents: grants must be received before a patent is produced. However, given that the Machine can produce free tea, free publications may appear and, therefore, free patents as well, which was not specified. It is possible to correct this by either allowing for free patents or removing free tea in the Machine.

In the following sections, we will elaborate how the specifications are composed in the framework.

2.5 Combining specifications

In our example, we used parallel composition and conjunction intuitively. Now, we give more details on all available operators, namely parallel composition, conjunction, and quotient. In the rest of the section, we will consider two specification automata $A_S = (\text{Loc}_1, q_0^1, \text{Clk}_1, E_1, \text{Act}^1, \text{Inv}_1)$ and $A_T = (\text{Loc}_2, q_0^2, \text{Clk}_2, E_2, \text{Act}^2, \text{Inv}_2)$. For technical reasons, we also assume that $\text{Clk}_1 \cap \text{Clk}_2 = \emptyset$.

There are two main ways of composing specifications in our framework: conjunction and parallel composition. The latter is the well-known structural combination of components—parallel composition is meant to combine specifications of *two separate* interacting components into a single box. In our example, the Researcher specification is composed with the beverage dispensing Machine specification in this manner.

The other operator, conjunction, is meant to combine two different specifications for the *same* component. The two specifications can typically represent requirements from a different viewpoint. In our example HalfAdm1 represented requirements with respect to providing funding (coins); HalfAdm2 represented requirements on producing patents.

Conjunction In our framework, conjunction can only be defined if $\operatorname{Act}_i^S = \operatorname{Act}_i^T$ and $\operatorname{Act}_o^S = \operatorname{Act}_o^T$ (the extension to dissimilar alphabets is straightforward). The operation reduces to check whether the two specifications can progress in the same way. Formally, the conjunction of A_S and A_T , denoted $A_S \wedge A_T$, is the TIOA $A = (\operatorname{Loc}, q_0, \operatorname{Clk}, E, \operatorname{Act}^S, \operatorname{Inv})$ given by: $\operatorname{Loc} = \operatorname{Loc}_S \times \operatorname{Loc}_T$,

 $q_0 = (q_0^S, q_0^T)$, Clk = Clk_S \oplus Clk_T, Inv((q_S, q_T)) = Inv(q_S) \wedge Inv(q_T). The set of edges *E* is generated by the following rule:

$$\frac{(q_S, a, \varphi_S, c_S, q'_S) \in E_S}{((q_S, q_T), a, \varphi_S \land \varphi_T, c_S \cup c_T, (q'_S, q'_T)) \in E_T}$$

The conjunction operator may introduce locally inconsistent states. For example, assume that A_S reaches a state from *s* where the only available action is the output *a* and A_T reaches a state *t* from where the only available action is the output *b*. Assume also that A_S and A_T cannot delay in *s* and *t*. In (*s*, *t*), the conjunction will not issue any output and will not be able to delay, which violates the *independent progress* property. As stated above, the locally inconsistent states are removed by ECDAR using the pruning facility.

In the example of Fig. 2, Machine5 (Fig. 2g) is a conjunction of Machine2 (Fig. 2c) and Machine4 (Fig. 2e) (though it is an inconsistent conjunction). Furthermore, Machine6 (Fig. 2f) is a conjunction of Machine3 (Fig. 2d) and Machine4 (Fig. 2e).

Parallel composition This operation computes the classical product between timed specifications [26], where components synchronize on common inputs/outputs. Two components are *composable* iff the intersection between their output alphabets is empty.

Formally, the *parallel composition* of A_S with A_T , denoted $A_S || A_T$, is the TIOA $A = (\text{Loc}, q_0, \text{Clk}, E, \text{Act}, \text{Inv})$ given by: Loc = Loc_S × Loc_T, $q_0 = (q_0^S, q_0^T)$, Clk = Clk_S \uplus Clk_T, Inv $((q_S, q_T))$ = Inv $(q_S) \land$ Inv (q_T) and the set of actions Act = Act_i \uplus Act_o is given by Act_i = Act_i^S \Act_o^T \cup Act_i^T \Act_o^S and Act_o = Act_o^S \cup Act_o^T. The set of edges E is generated by the following rules:

- Whenever (q_S, a, φ_S, c_S, q'_S) ∈ E_S with a ∈ Act_S \Act_T then for each q_T ∈ Loc_T also ((q_S, q_T), a, φ_S, c_S, (q'_S, q_T)) ∈ E
 Whenever (q_T, a, φ_T, c_T, q'_T) ∈ E_T
 - with $a \in \operatorname{Act}_T \setminus \operatorname{Act}_S$ then for each $q_S \in \operatorname{Loc}_S$ also $((q_S, q_T), a, \varphi_S, c_S, (q_S, q'_T)) \in E$
- 3. Whenever $(q_S, a, \varphi_S, c_S, q'_S) \in E_S$ and $(q_T, a, \varphi_T, c_T, q'_T) \in E_T$ with $a \in \operatorname{Act}_S \cap \operatorname{Act}_T$ then also $((q_S, q_T), a, \varphi_S \land \varphi_T, c_S \cup c_T, (q'_S, q'_T)) \in E$.

The first rule represents all the cases where A_S makes an individual move, be it input or output, because *a* is not in the signature of A_T . Similarly, the second rule handles all individual moves by the second component A_T . The third rule handles all synchronizations between the two components. The possibilities are input/input which again gives an input or input/output which gives an output.



Fig. 4 Specification of a the ButtonSpec, b the assumption ButtonA, c the guarantee ButtonG

Quotient The operation of *quotienting* is radically different from the other composition operators. It is a differencing operator [18] that can be used to synthesize requirements for missing components in a project. Two fix attention, let us assume that we have an abstract specification A_T for the entire system, and a specification A_S of an existing available component. The quotient synthesizes a specification $A_T \setminus A_S$ for the missing component—the component that when composed with A_S would implement A_T .

The use of quotient simplifies independent design of components. Assume that X is the missing component that needs to be designed by another person, or even another vendor than the rest of the system. The correctness requirement for X is $A_S || X \leq A_T$. In general, this requirement might be a rather complicated verification expression. Fortunately, it is sufficient to separate the concerns using quotienting. The new designer does not need to have access to the entire system, nor does he need to perform the verification of the entire system each time he checks his current design for X. It suffices to synthesize the quotient $A_T \setminus A_S$ and he can simply check whether $X \leq A_T \setminus A_S$. This latter specification effectively captures all contextual requirements for X.

Summarizing, quotienting allows for factoring out behavior from a larger component. If one has a large component specification A_T and a small one A_S then $A_T \setminus A_S$ is the specification of exactly those components that when composed with A_S refine A_T .

Quotienting for specifications is defined in the following way. Consider two specifications $A_T = (\text{Loc}_T, q_0^T, \text{Clk}_T, E_T, \text{Act}_T, \text{Inv}_T)$ and $A_S = (\text{Loc}_S, q_0^S, \text{Clk}_S, E_S, \text{Act}_S, \text{Inv}_S)$ with $\text{Act}_i^S \subseteq \text{Act}_i^T \cup \text{Act}_o^T$ and $\text{Act}_o^S \subseteq \text{Act}_o^T$. The quotient, which is denoted $A_T \setminus A_S$ is the TIOA given by: $\text{Loc} = \text{Loc}_T \times \text{Loc}_S \cup \{l_u, l_\emptyset\}, q_0 = (q_0^T, q_0^S), \text{Clk} = \text{Clk}_T \uplus \text{Clk}_S \uplus \{x_{\text{new}}\}, \text{Inv}((q_T, q_S)) = \text{Inv}(l_u) = \text{tt}$ and $\text{Inv}(l_\emptyset) = \{x_{\text{new}} \le 0\}$. The two new locations l_u and l_\emptyset are, respectively, universal and inconsistent. The set of actions $\text{Act} = \text{Act}_i \uplus \text{Act}_o$ is given by $\text{Act}_i = \text{Act}_i^T \cup \text{Act}_o^S \cup \{i_{\text{new}}\}$ and $\text{Act}_o = \text{Act}_o^T \setminus \text{Act}_o^S$. The set of edges *E* is generated by the following rules:

- Whenever $q_T \in \text{Loc}_T, q_S \in \text{Loc}_S$ and $a \in \text{Act}$ then also $((q_T, q_S), a, \neg \text{Inv}_S(q_S), \{x_{\text{new}}\}, l_u) \in E$.
- Whenever $q_T \in \text{Loc}_T$, $q_S \in \text{Loc}_S$ then also $((q_T, q_S), i_{\text{new}}, \neg \text{Inv}_T(q_T) \land \text{Inv}_S(q_S), \{x_{\text{new}}\}, l_{\emptyset}) \in E.$
- Whenever $(q_T, a, \varphi_T, c_T, q'_T) \in E_T$ and $(q_S, a, \varphi_S, c_S, q'_S) \in E_S$ then $((q_T, q_S), a, \varphi_T \land \varphi_S, c_T \cup c_S, (q'_T, q'_S)) \in E$
- Each $(q_S, a, \varphi_S, c_S, q'_S) \in E_S$ with $a \in \operatorname{Act}_o^S$ gives rise to $((q_T, q_S), a, \varphi_S \land \neg G_T, \{x_{\text{new}}\}, l_\emptyset)$ where $G_T = \bigvee \{\varphi_T \mid (q_T, a, \varphi_T, c_T, q'_T)\}$
- Each $(q_T, a, \varphi_T, c_T, q'_T) \in E_T$ and $a \notin \operatorname{Act}_S$ gives $((q_T, q_S), a, \varphi_T, c_T, (q'_T, q_S)) \in E$
- Each $(q_T, a, \varphi_T, c_T, q'_T) \in E_T$ with $a \in \operatorname{Act}_o^S$ gives rise to $((q_T, q_S), a, \neg G_S, \{\}, l_u)$ where $G_S = \bigvee$ $\{\varphi_S \mid (q_S, a, \varphi_S, c_S, q'_S)\}$
- Each $a \in Act_i$ gives rise to $(l_{\emptyset}, a, x_{new} = 0, \{\}, l_{\emptyset})$
- For each $a \in Act$ gives rise to $(l_u, a, tt, \{\}, l_u)$.

Just like conjunction, the quotient operation may produce (locally) inconsistent specifications. Hence, each quotient operation is followed by pruning.

In the following, we will illustrate the quotienting through a very simple example. The example consists of three TIOAs Specifications as shown in Fig. 4. We start with a simple specification, shown in Fig. 4a of a system with two buttons. The specification states that as long as only button1 is pressed then only good output will be produced. If at some point, button2 is pressed then the system could start to produce bad output.

The following definition defines an operator known as weaken or weakening that is used for easier specification of assume guarantee specifications.

Definition 6 Weaken >>:

For any two TIOAs specifications A and G we define G >> A as follows:

$$G >> A \equiv (A||G) \backslash A$$

In our simple example, we would like to express the assumptions and guarantees that we have to the system separately. In Fig. 4b, we specify the assumption that button2 is never pressed, while in Fig. 4c we specify the guarantee that the system never produces bad output. Even though, in this example, our ButtonSpec is quite simple the assumption ButtonA and guarantee ButtonG are even simpler and extremely easy to understand.

For this example, we can use ECDAR to prove the following two refinements:

refinement: (ButtonG >> ButtonA) <= ButtonSpec
refinement: ButtonSpec <= (ButtonG >> ButtonA)

Thus effectively being able to substitute ButtonG >> ButtonA for ButtonSpec in any context.

The possibility of splitting assumptions from guarantees becomes even more appealing when having multiple assumptions and guarantees that are conjoined.

2.6 Syntactic extensions

The ECDAR tool offers a range of syntactic extensions build over the core language described above. These extensions do not affect the theoretical expressiveness of the language, but instead they enable more natural description of systems using primitives such as finite domain types, variables, constants, channels, committed locations, and arrays. These are the same extensions as known from UPPAAL, but adapted to the two player semantics.

Types, variables and constants ECDAR allows to introduce finite domain variables ranging over restricted integer types. The variables are more concise descriptions of counters and value placeholders than finite state machines. Named constants allow easy parameterization of models, e.g., with allowed delays.

Channels and arrays Actions are defined using the syntax: "broadcast chan a" which gives both the input label a? and the output label a!. Actions are, as defined in the theory, broadcast and thus outputs are never blocked.

Channels can be organized in arrays. This is very convenient to encode local communication—e.g., a two -dimensional $n \times n$ array of channels can model individual two-ended channels between n processes.

Select statements The modeling language of ECDAR also allows for using select statements of the form e:id_t on a transition. This translates into a set of transitions with e having each of the possible values that the type id_t can assume. This is only syntactic sugar which allows for much more compact models.

Templates Templates are specifications parameterized with named but unresolved constants. Templates can be instantiated by providing values for constants, and the semantics is given by macro expansion. Templates are useful for instantiating many similar processes, perhaps with different initial conditions. They interplay well with constants and channel array.

Instantiating templates allows not only to change timing properties, but also to configure various communication topologies. For example, parameterize the template with the name (index in an array) of a channel to be used for communication. Then instantiate the parameters so that the instances create trees, rings, and other layouts. We will use this technique to model rings in the case study in the following section.

3 The leader election protocol

We analyze a variant of the leader election protocol that operates on a ring topology. The protocol can be instantiated for an arbitrary number of nodes. Each node in the ring has both a place in the ring represented by its *id* and, apart from this, also a unique *priority*. The protocol performs one round of leader election selecting the node with the highest *priority* as the leader. When the protocol is initiated all nodes know that the election has started and can thus start to send their own *priority* to the next node in the ring topology. Figure 5 illustrates an instantiation of the protocol for six nodes, with their initial priorities and the communication channels used between the nodes. If a node receives a *priority* that is lower



Fig. 5 Overview of the ring topology and communication channels in a ring with 6 nodes. Each node has both an *id* given by its name (e.g. N0) and a priority (e.g. pr5). Between each set of nodes in the ring there is a set of communication channels used to mimic value passing



Fig. 6 Illustration of one scenario of how the information could be passed around the ring using the protocol. For the sake of illustration, every node happens to send the information to the next node at exactly

the same time thus giving us six distinct steps. Notice that the maximum *priority* will travel exactly once around the ring. In this case giving a total of 30 messages

than its own *priority* it will just discard the received *priority*. If it receives a *priority* that is higher than its own *priority*, it will keep a copy of the new *priority* and then send it on at the same time stopping to send its own *priority*. If at some point, a node receives its own *priority*, it will know that it is the leader, since this *priority* has traveled one full round on the ring topology without being discarded and thus is greater than all other priorities.

The execution of the protocol is illustrated in Fig. 6 which shows how the information flows in a ring of 6 nodes, in the case where all nodes just happen to send the information at exactly the same time (synchronously).

We proceed to specify the protocol using TIOAs in the ECDAR tool. Let N be a constant that determines the number of nodes in the ring.

```
const int N = 6;
```

We also declare a constant for the maximum delay before a node sends the maximal *priority* that it has seen to the next node in the ring.

Finally, we declare a data type id_t which is used for all the variables containing *ids* and *priorities*.

typedef int[0,N-1] id_t;

Using the constant N, we declare two global arrays of channels that are used to communicate the information in the model.

```
broadcast chan send[N][N];
broadcast chan leader[N];
```

The send channel is actually an array of N by N channels. In the channel expression send [4] [3]!, the first index (in this case node number 4) represents the *id* of the node that is the receiver of the message. The second index (in this case 3) represents the priority *pr* that is being send as the message. This is the standard way of modeling value passing in time (i/o) automata.

3.1 Specification model for the nodes

Figure 7 shows the template for specifying the nodes. Each node is instantiated with an identifier id and a priority pr. Each node uses a local variable cur of type id_t to store the current priority value, initialized with the value of the pr constant:

The node consists of three locations. The top location which is also the initial location represents the normal operation of the protocol. This state has an invariant $x \le MaxD$ ensuring



Fig. 7 Node template used for each of the nodes in the ring topology

eader

leader[0]!



that the node will send the maximal *priority* that it has seen so far, stored in the local variable cur to the next node in the ring with intervals of no more that MaxD time units.

Each node receives on the set of channels send[id][e]? where *e* can be any priority. Similarly, it sends on a set of channels send[(id+1) N][e] to the next node in the ring (the % is the modulus operator). On a given edge in the template, say the top leftmost one in Fig. 7, the select statement $e:id_t$ semantically translates into the instantiated template being able to receive any priority which is then bound to the variable e.

The node template has three input transitions in its initial location. The one leading to the second location is taken exactly in the case where the priority received matches the priority of the node itself. If this transition is taken, the node will declare itself leader. The other two represents the two cases where the local variable cur should be updated or not.

Both the second and third location are input enabled but does nothing with the input. The second location, marked with a u meaning that it is urgent, will immediately send out the leader[id]! output.

3.2 Verification

The correctness of a ring of **N** nodes we are interested in has both a functional part—i.e. the correct leader is elected—as well as a non-function part—i.e. the leader is elected within an acceptable upper time bound. For this, we formulate and verify the two general properties elaborated below.



Fig. 9 A property \mathcal{T} stating that a leader is elected within the specified time-bound

The first property S, shown in Fig. 8, states that only the correct node, the one with the lowest priority, can declare itself leader.

The second property T, shown in Fig. 9, states that a leader will be elected within x<= (N+1) *MaxD time units, being equal to the maximal priority traveling exactly one round as slowly as possible.

These overall properties of the ring of nodes can be verified with the following refinement checks:

refinement:											
(NO		N1		N2		N3		N4		N5)	<= S
refinement:											
(NO		N1		N2		N3		N4		N5)	<= T

We call this type of verification monolithic, since it constructs and explores the specification representing the entire systems to settle the suggested refinements. In the present case with 6 nodes, ECDAR quickly proves the refinements and provides a witnessing strategy which can be exercised interactively. However, it is clear that the monolithic approach will suffer from the exponential growth of the states in the number of nodes in the ring.

3.3 Compositional verification

To combat the state-space explosion problem and enable verification of the correctness of the protocol for larger numbers of nodes, we will apply *compositional verification* for both the functional correctness property S and the non-functional correctness property T. The idea is to create N sub-specifications S_i (and T_i) that may be shown to capture the behavior of the sub-ring $N_N || \ldots || N_i$ inductively, by demonstrating the following sequence of refinements:

$$N_N \le \mathcal{S}_N \tag{1}$$

$$\mathcal{S}_{i+1}||N_i \le \mathcal{S}_i \text{ for } i = (N-1)\dots 1$$
(2)

$$S_1||N_0 \le \mathcal{S} \tag{3}$$

As mentioned in the introduction this compositional verification is sound because our refinement operator is a precongruence with regard to parallel composition [13].

Using that the refinement relation \leq is a precongruence with respect to parallel composition and transitive, it may be concluded that the ring is a refinement of S. Given six nodes



Fig. 10 Overview of how the induction hypothesis $\varphi 1$ is used to prove the property for a larger and larger set of nodes

(1), (2) and (3) amounts to performing the following series of refinement checks:

refinement:	N!	5 <=	S	5			
refinement:	(S5		N4)	<=	S4
refinement:	(S4		N3)	<=	S3
refinement:	(S3		N2)	<=	S2
refinement:	(S2		N1)	<=	S1
refinement:	(S1		N0)	<=	S

The series of refinement checks is illustrated in Fig. 10. Though greater in number than the *single* monolithic verification each of the six refinement checks only involve three small components, thus making the overall verification effort linear rather than exponential in the number of nodes in the ring.

To obtain the sub-specifications S_i and T_i as instances of general templates, we define the following set of Boolean arrays which are simply used as a reverse look up of which *ids* are included in the set of nodes that a given instantiation of the induction hypothesis covers.

const	poot	S5[N]	=	ł	Ο,	Ο,	Ο,	1,	Ο,	0};
const	bool	S4[N]	=	{	0,	Ο,	1,	1,	0,	0};
const	bool	S3[N]	=	{	0,	Ο,	1,	1,	1,	0};
const	bool	S2[N]	=	{	0,	1,	1,	1,	1,	0};
const	bool	S1[N]	=	{	1,	1,	1,	1,	1,	0};

These Boolean arrays are then used as input parameters to the corresponding instantiations of the induction hypotheses. The sub-specifications S_i used to inductively prove the functional property S is shown in Fig. 11, and may be informally described as follows:

S_i first and final version:

Whenever the sub-ring $N_N || \dots || N_i$ receives priorities



Fig. 11 The sub-specification S_i . The nodes covered by the sub-specification (N_N, \ldots, N_i) can only declare themselves leader after having received a priority also covered by the sub-specification

outside those belonging to one of its nodes, no leader is declared. If a priority belonging to one of the nodes of the sub-ring is received, it is allowed for any of the nodes to declare leader-ship.

The sub-specification does not restrict that it has to be the same node that declares itself leader as the one that receives its own *id*. It is worth noting that the sub-specification is this way captures the part of the behavior that is important to prove exactly this property, while ignoring other aspects. In particular, nothing is said about timing of events.

3.3.1 Timing property

Now let us apply the compositional approach to establish the non-functional property \mathcal{T} , i.e. that a leader will be elected within (N+1) *MaxD time units. Thus, we are searching a (timed) sub-specification \mathcal{T}_i , for $i = N \dots 1$ satisfying the following set of refinements:

$$N_N \le \mathcal{T}_N \tag{4}$$

 $\mathcal{T}_{i+1}||N_i \le \mathcal{T}_i \text{ for } i = (N-1)\dots 1$ (5)

$$\mathcal{T}_1||N_0 \le \mathcal{T} \tag{6}$$

The first attempt at defining the timed sub-specification is shown in Fig. 12 and may informally be read as follows:

T_i first attempt:

Whenever the sub-ring $N_N||...||N_i$ receives a priority larger than any one belonging to one of its nodes, this priority will be delivered to N_0 before (N-i+1) *MaxD time-units.

Note the use of the local variable g for ensuring that the priority delivered is the one received. However, this proposal for a sub-specification T_i turned out to be too erroneous (too strong) as it is too strong to be used as the induction hypothesis as it is possible to prove the final step but neither the iterative step nor the base case.





In particular, the base case does not hold as there is no guarantee that a "large" priority received will eventually be delivered to N_0 as an even "priority" may be received by the sub-ring in the mean-time. An attempt of correcting this is given in Fig. 13, and may be read informally as follows:

T_i second attempt:

Whenever the sub-ring $N_N||...||N_i$ receives a priority larger than any one belonging to one of its nodes, this priority will be delivered to N_0 before (N-i+1) * MaxD time-units, unless another priority is received before.

As desired, the modified sub-specification validates the refinements required in the base case and the final case. Unfortunately, though seemingly a true property, it turns out that it is too weak for the refinement of the iterative step to hold.

Figure 14 is an attempt of finding a sub-specification for which the refinements of the iterative steps are valid. Here, the behavior after having received a priority and storing it in g is made dependent on whether the priority received is equal to the one stored in g. Unfortunately, this renders all the refinement checks incorrect. After three (and in fact several) more failing attempts, we finally obtain the satisfactory sub-specification in Fig. 15, which radically differs from the previous in that it only keeps track of what happens to the messages that contains the maximum priority. Informally, the sub-specification reads as follows:

\mathcal{T}_i final version:

Whenever the sub-ring $N_N||...|N_i$ receives the maximum priority before i *MaxD time-units - and unless one of the nodes of the sub-ring declares itself leader - the maximum priority will be delivered to N_0 before (N-i+1) *MaxD time-units.

Fortunately, this make the sub-specification strong enough to prove the final property \mathcal{T} as well as the iterative refinement steps, yet weak enough to be able to prove the base case and pass the consistency check.

3.4 Assume/guarantee specifications

To make the hunt for the correct sub-specifications easier, we will specify S and T in the form of a pair of an assumption and a guarantee part. The assumption and guarantee equivalents of S are shown in Figs. 16 and 17, respectively.





Fig. 16 The simple assumption SA_i that no input will be sent with priorities that belong to the set of nodes represented by the sub-specification

Fig. 17 The simple guarantee SG_i that no leader output will be generated





SA_i first and final version:

We will never send any priority to the sub-ring $N_N || \dots ||N_i$ with priorities belonging to one of its nodes.

SG_i first and final version:

The sub-ring $N_N || \dots || N_i$ will never generate any leader output.

These two very simple TIOAs can be combined into a contract using the weakening operator >>.

The following two refinements hold (for each *i*):

refinement: S1 <= (SG1 >> SA1)
refinement: (SG1 >> SA1) <= S1</pre>

Thus, we have shown that the *S* that we have come up with is identical to the more easily understandable assumption and guarantee.

The assumption and guarantee equivalents of T are shown in Figs. 18 and 19, respectively.

\mathcal{TA}_i first and final version:

The maximum priority will be delivered to the sub-ring $N_N || \dots || N_i$ before i * Max D time units.

\mathcal{TG}_i first and final version:

The sub-ring $N_N || \dots || N_i$ deliver a message with the maximum priority to the node 0 before (N+1)*MaxD time units.



Fig. 18 The assumption \mathcal{TA}_i that a message with the maximum priority will be delivered to the sub-specification before i * MaxD time units



Fig. 19 The guarantee TG_i the sub-specification will deliver a message with the maximum priority within (N + 1) * MaxD time units

Similarly as for the other case we can now combine these two specifications into a contract. For this case only one way of the refinements hold (for each *i*):

refinement: (TG1 >> TA1) <= T1

This means that in this case we can conclude that the composed sub-specification \mathcal{T} that we have come up with refines the contract composed from the assumption and guarantee and thus we can use \mathcal{T} when performing the verification and still rely on the fact the guarantee will hold.

3.5 Performance comparison of analysis methods

To compare the efficiency of regular monolithic and compositional verification we timed the verification of the two properties S and T for several different values of N. All the verification was performed on the same machine and all verification instances where allowed a maximum of 5 min to terminate. The choice of exactly 5 min as the upper bound is arbitrary and will not effect the shape of the graphs that we obtain, but only determine the point at which the graphs stop. The upper bound is needed to be able to run a large amount of experiments efficiently. The results are listed in Fig. 20. For both the properties in the monolithic cases, they took more than 5 min to verify for rings with 7 nodes.

As can be seen from the graph, the compositional verification method is capable of handling much larger instances within a reasonable time bound. Besides this, the compositional method also has a much larger theoretical upper bound. It will only verify one step at a time and thus will not suffer from lack of available memory as long as a single step can be handled with the available memory.

4 Conclusion and further work

Conclusion In this paper, we have presented the complete specification theory for timed systems underlying the ECDAR



Fig. 20 Timing results of verification of S and T for the compositional and monolithic cases

tool. Being powered by the game solving engine of the branch UPPAAL-TIGA, the ECDAR tool provides support for refinement and consistency checking between specifications as well as allow for the logical and structural composition. In particular, as demonstrated in our treatment of the leader election protocol example, the theory and tool allow for efficient compositional verification of systems by the exploitation of engineer-provided sub-specifications. As such, the compositional usage of the tool is not *fully* automated, and the design of appropriate sub-specifications-strong enough to entail an overall specification and sufficiently weak to be entailed themselves-is a major challenge. We believe that engineers will always be unfamiliar with any new specification formalism. However, we believe that engineer-provided sub-specifications are not only necessary in the development of realistic systems, but also extremely useful for raising the overall understanding of the systems. In order for the method to be applicable in large-scale projects it needs to be supported by a mature tool that is as intuitive as possible to use. As demonstrated in the leader election protocol, tool support is vital in establishing a coherent set of subspecifications. The need for programmer generated specifications is in no way unique to our approach and is also needed in frameworks such as SPEC# [6] in which assertions (invariants) written by the programmer about a C# program are checked by a range of different analysis techniques.

An important feature of our theory is the existence of a quotient construct (i.e. weakest property transformer with respect to parallel composition), which, in particular, allows for sub-specifications to be obtained from pairs of assumptions and guarantees. As demonstrated, this often allow for substantially simpler specifications of sub-systems.

Performance analysis The specification theory presented and the tool ECDAR provide support for establishing hard realtime guaranteed properties from TIOA models. However, as we will sketch in the following, it is possible to also derive soft real-time properties in terms of expected behavior from the same TIOA models. E.g. in the extensive treatment of the leader election protocol of Sect. 3, we have firmly established that the correct leader is guaranteed to be declared within (N+1) *MaxD time-units, given a ring of N nodes each implementing the TIOA specification of Fig. 7, i.e. 14 time-units for a ring with 6 nodes. The specification theory presented in this paper, assumes that implementations are concrete executable realizations of specifications. In particular, implementations are assumed to have fixed timing behavior, meaning that outputs occur at predictable and exact time moments. However, in a richer setting, the timing behavior of implementations could be stochastic, with timing delays of components being chosen by distributions.



Fig. 21 Performance Analysis of the leader election protocol, giving the probability that the leader will be declared \mathbf{a} within T time-units and \mathbf{b} within M messages being send, estimated by UPPAAL-SMC

In a line of recent work [9, 11, 12], such a stochastic semantics has been put forward for networks of TIOA, giving a probability measure on sets of runs. This allows for refined probabilistic performance properties to be defined and analyzed, such as the property "the probability of the set of runs where a leader is declared within 4 time-units is greater than 0.3", which could be highly interesting for the leader election protocol. The new UPPAAL-SMC branch offers a simulation engine allowing to settle such probabilistic properties within desired levels of confidence based on a number of random runs of the system. Assuming that the delay of each node is given by uniform distribution on the interval [0, MaxD] Fig. 21a gives the estimated probability, that the leader (node N_2) is declared within T time-units, with T ranging from 0 to 14. Knowing from our previous verification effort that 14 is the guaranteed upper bound, it is interesting to see that the average time before election is significantly lower, namely 4.42624 time-units. Using UPPAAL-SMC, we obtain [0.38241, 0.402412] as a 95% confidence interval for the probability of that the leader is elected within 4 time-units using 18,445 random runs. On the other hand, directly testing whether this probability is greater than 0.3 with significance level 0.05 is confirmed with only 266 runs, using the sequential testing method implemented in UPPAAL-SMC.

Extending the model slightly, we may also estimate the "probability that a leader is declared within a given number M of messages being send". Figure 21b gives an estimation of this probability for M ranging from 0 to 50. We note that on average transmission of some 25 messages is needed.

Following the sketch above for the leader election protocol, we believe that a semantically well-founded extension of the presented TIOA-based specification theory to allow for stochastic implementation would be extremely interesting. In particular, it would enable the refinement of hard realtime guarantees with soft performance statistics in a consistent manner, and allow for the analysis and development of mixed-criticality systems.

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