



Aqueous degradation of 6-APA by hydroxyl radical: a theoretical study

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Abstract

Context Degradation reactions of micropollutants such as antibiotics with OH radicals are very important in terms of environmental pollution. Therefore, in this study, the degradation kinetic mechanism of 6-aminopenicillanic acid (6-APA) with OH radical was investigated by density functional theory (DFT) methods.

Methods For the calculations, different functionals such as B3LYP, MPW1PW91, and M06-2X were used with a 6-31 g(d,p) basis set. The aquatic effect on the reaction mechanism was investigated by conductor-like polarizable continuum model (CPCM). For the degradation kinetics in aqueous media, the addition of explicit water molecules was also calculated. Subsequent reaction mechanism for the most probable reaction product was briefly discussed.

Results Among the functionals used, B3LYP results were consistent with the experimental results. Calculated kinetic parameters indicated that the OH-addition path was more dominant than the H-abstraction paths. With the increase of explicit water molecules in the models, the energy required for the formation of transition state complexes decreased. The overall rate constant is calculated as $2.28 \times 10^{11} \text{ M}^{-1} \text{ s}^{-1}$ at 298 K for the titled reaction.

Keywords 6-Aminopenicillanic acid · Density functional theory · Hydroxyl radical · Kinetics

Introduction

Approximately 210,000 tons of antibiotics are produced all over the world every year, and beta-lactam antibiotics are the most consumed ones [1, 2]. 6-Aminopenicillanic acid (6-APA) is a beta-lactam-type antibiotic. These kinds of antibiotics are widely used because they are inexpensive and easily accessible [3]. As a consequence of excessive consumption of 6-APA, it is frequently detected in the aquatic environment. This is an important problem due to its potential toxicity for human health and all living organisms [4]. Degradation reactions are very important for their removal from water. Their degradation products may lead to harmful results. The theoretical study of the oxidation mechanism of Dibutyl phthalate in gas and aqueous phase by hydroxyl and sulfate radicals can be given as an example to such reactions [5]. In some cases, the decomposition products can also be toxic or more toxic than the parent drug [6].

Therefore, antibiotics in water sources, especially drinking water sources, must be adequately treated due to their adverse effects on the ecosystem and human health. Special methods can be applied to remove pharmaceutical wastes, such as antibiotics, from water treatment plants. Advanced oxidation processes (AOPs) have been frequently used in recent years to remove environmental pollutants from water sources. The main mechanism of AOPs is the generation of highly reactive free radicals. The most reactive of the radicals formed are OH radicals. In the AOP technique, pollutants are decomposed through reactions with hydroxyl radicals [5, 7–10]. Thus, wastes such as antibiotics and micropollutants in the water are removed by OH radicals. There are some studies on antibiotic degradation with the AOP technique in the literature, but unfortunately, these are mostly for increasing the degradation rates [6, 11–17]. However, it is sometimes insufficient to fully explain the mechanism. Experimental methods involve long processes, are expensive, and also require equipment. Due to these difficulties in the experimental investigation of such reactions, quantum chemical computation methods are an important advantage [18, 19].

Quantum chemical computation methods are very useful for explaining the kinetic mechanism of reactions. In recent years, density functional theory (DFT) has been

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used especially to investigate the kinetics of reactions at the molecular level due to its reliability and low cost [18]. The mechanisms, thermochemical properties, kinetic parameters of the reactions, and each possible reaction path can be determined by quantum chemical modeling methods [20]. In the literature, there are some studies about the degradation kinetics of antibiotics [21–24], but as far as we know, there is no quantum chemical computational kinetic study of the degradation reaction of 6-APA with the OH radical.

This study aims to examine in detail the kinetic mechanism of the degradation reaction of 6-APA with the OH radical. For this purpose, the rate constants and branching ratios of the reaction of 6-APA with the OH radical were calculated quantum chemically. Calculations were performed using different functionals of the DFT method. All kinetic and thermodynamic parameters were calculated in aqueous media using the conductor-like polarizable continuum model (CPCM) solvent model. Besides, the degradation reaction kinetics for the most probable reaction path were also investigated using explicit solvent models. The subsequent reaction mechanism for the most probable degradation product was proposed using Fukui functions.

Computational details

All calculations were performed using the DFT method in the Gaussian16 package program [25]. Different DFT functionals such as B3LYP, M06-2X, and MPW1PW91 were used to find reliable kinetic results for the degradation kinetics of 6-APA. These functionals were developed to study organic reactions with a computational demand similar to the HF method [26]. It has been shown in some previous studies that B3LYP and MPW1PW91 functionals gave reliable results for oxidation reactions of organic compounds [4, 27]. Also, the M06-2X function was found suitable for kinetic and thermodynamic calculations and was proposed for such reactions [28]. In previous studies, B3LYP/6-31G(d,p) is the most suitable level of theory to predict the energy barriers of radical addition reactions [29, 30]. Based on these results, all the geometry optimizations were performed at 6-31G(d,p) level, followed by single point energy calculations at B3LYP/6-311+G(d,p) level. Molecular electrostatic potential (MEP), frontier molecular orbital (FMO) analysis, and natural bond orbital (NBO) analysis were performed. All the molecular structure visualizations were prepared with the Gauss View 5.0 program [31].

All the reactants, pre-reactive complexes (PR), transition state complexes (TS), and products (P) were verified by frequency analyses. Transition state complexes were characterized by having one imaginary frequency. The intrinsic reaction coordinate (IRC) calculations were performed to understand the correlations of TS geometries with products and reactants along the

reaction coordinate [32]. Zero-point vibrational energies (ZPEs) were calculated at the same level as the theory.

The thermodynamic parameters were calculated with standard statistical thermodynamic at 298.15 K and 1 atm. The reaction paths rate constants were calculated by using transition state theory with Wigner correction with the following equation:

$$k = \kappa \frac{k_B T}{h} e^{-\Delta G^\ddagger / RT} \quad (1)$$

$$\kappa = 1 + \frac{1}{24} \left[\frac{hI}{k_B T} \right]^2 \quad (2)$$

$$\delta = \frac{k_i}{k_{tot}} \times 100 \quad (3)$$

in which: κ is transmission coefficient, k_B is Boltzmann constant, h is Plank constant, T is the temperature, ΔG^\ddagger is activation Gibbs free energy, I is the imaginary frequency of a transition state complex, k_{tot} is the total rate constant value, k_i is the rate constant value of each path, and δ is branching ratio [33, 34]. All the parameters were calculated manually.

Fukui functions are widely used for predicting reaction sites of the molecules. The larger the value of the Fukui functions, the higher the reactivity. There are three Fukui functions for nucleophilic attack f_i^+ , electrophilic attack, f_i^- , and radical attack f_i^o . Fukui functions were calculated as defined in the equations below.

$$f_i^+ = q_i(N+1) - q_i(N) \quad (4)$$

$$f_i^- = q_i(N) - q_i(N-1) \quad (5)$$

$$f_i^o = \frac{f_i^+ - f_i^-}{2} \quad (6)$$

where $q_i(N)$, $q_i(N+1)$, and $q_i(N-1)$ are the electron densities of the i atom in the neutral, anionic, and cationic molecules, respectively [35, 36].

The aquatic effect on the reaction mechanism was investigated with explicit water molecules and an implicit solvent model (to describe bulk water behavior) CPCM with the dielectric constant value of water, $\epsilon = 78.355$ [37]. It is known that in implicit solvent models, long-range interactions between solvent and solute are considered, but some important electronic interactions cannot be considered. The explicit solvent model with implicit solvents as the mixed model is a reasonable strategy for solvent–solute interactions [38]. Therefore, in this study, we have also explicitly investigated the increased 1 and 2 numbers of water molecules effect on the reaction kinetics. The addition of water molecules to the calculations was done one by one.

Results and discussion

Analysis of reaction paths

The degradation reaction of 6-APA with the hydroxyl radical can take place in two ways: (i) hydrogen abstraction of OH radicals from saturated bonds and (ii) OH radical addition to unsaturated bonds [28]. The calculated MEP, FMO, and NBO results are given in the Supplementary Materials. Concerning the MEP, FMO, and NBO results,

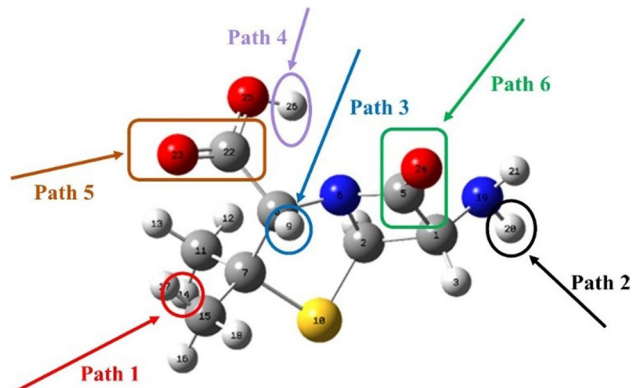
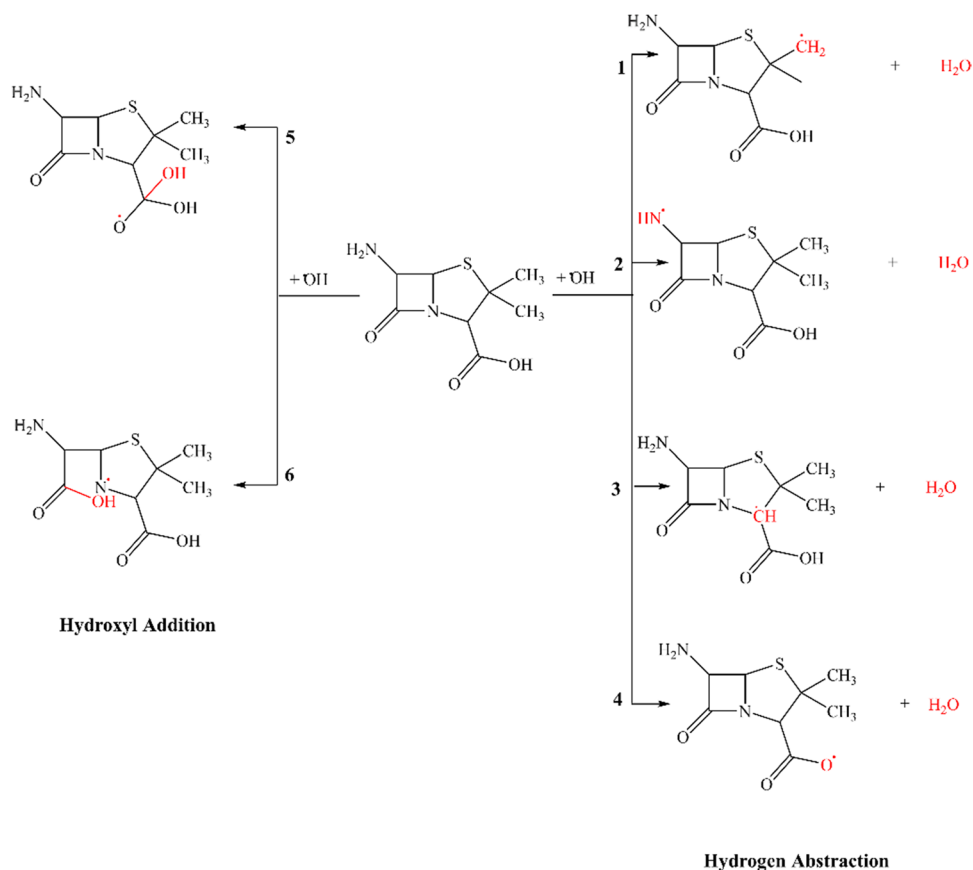


Fig. 1 Possible reaction paths for 6-APA

Scheme 1. Initial degradation paths for 6-APA



the possible reaction paths of 6-APA with the OH radical are determined. These reaction paths include four possible hydrogen abstractions and two hydroxyl radical additions. As understood from the NBO results, the abstraction of hydrogens from the beta-lactam ring (the hydrogen atoms of C1 and C2) is sterically difficult because these atoms are not as electrophilic as the other hydrogen atoms. All possible initial degradation paths are shown in Fig. 1 and Scheme 1. Paths 1, 2, 3, and 4 are the hydrogen abstraction paths, and paths 5 and 6 are the hydroxyl radical addition paths.

Degradation reaction mechanism

Abstraction paths

Optimized geometries of pre-reactive complexes, transition state complexes, and products for hydrogen abstraction reaction paths are given in Fig. 2 for B3LYP/6-31G(d,p). The potential energy graph for these reaction paths is given in Fig. 3. Optimized geometries of structures and potential energy graphs for other functionals are also given in the Supplementary Material.

The pre-reactive complexes are important for the reaction paths because they lower the activation energies.

These complexes have lower energies than reactants due to hydrogen bonds or Van der Waals attraction [39]. According to the preliminary calculation results, four different pre-reactive complexes are formed in the 6-APA reaction with OH radicals, as shown in Scheme 1. The major changes in the geometries of the optimized pre-reactive complexes are observed in the bonds between the oxygen atom of OH and the C or N atom, to which the hydrogen atom is to be abstracted in 6-APA. In the PR1 complex, there is a 2.29 Å Van der Waals interaction between the oxygen atom of the OH radical and the hydrogen of C11, and the angle between the hydroxyl radical and C11 is 98.52°. In PR2, a hydrogen bond of 1.67 Å length is formed between the oxygen atom of the OH radical and the hydrogen atom of N19. The angle between the OH radical and the N19 atom is 106.34° in PR2. As seen in Fig. 2, there are two interactions in the PR3 complex. They are 1.92 Å and 2.37 Å long bond lengths between the OH radical and the O24 and hydrogen of C8 atoms, respectively.

The angle between the OH radical and the C8 atom in PR3 is 80.36°. In the PR4 complex, there are also two hydrogen bond interactions with the OH radical. They have 1.93 Å and 1.82 Å bond lengths with the hydrogen of O23 and the N19 atom, respectively. The angle between the OH radical and hydrogen atom of O23 is 112.62°. As seen in Fig. 3, PR4 has the lowest energy. This may be the result of the two hydrogen bond interactions in PR4, and these bond lengths are shorter than the others. As seen in the potential energy graph, the energies of the pre-reactive complexes are 0.63, 5.02, 4.39, and 12.99 kcal·mol⁻¹ lower than those of the reactants, respectively. The energetically most stable complex is PR4.

For each of the possible reaction paths, four transition state complexes are identified. In the formation of transition state complexes, the main geometric changes are observed around the atom from which the hydrogen is abstracted. While the C-X or N-X bonds to which the hydrogen is abstracted are lengthening, the lengths of the subsequent

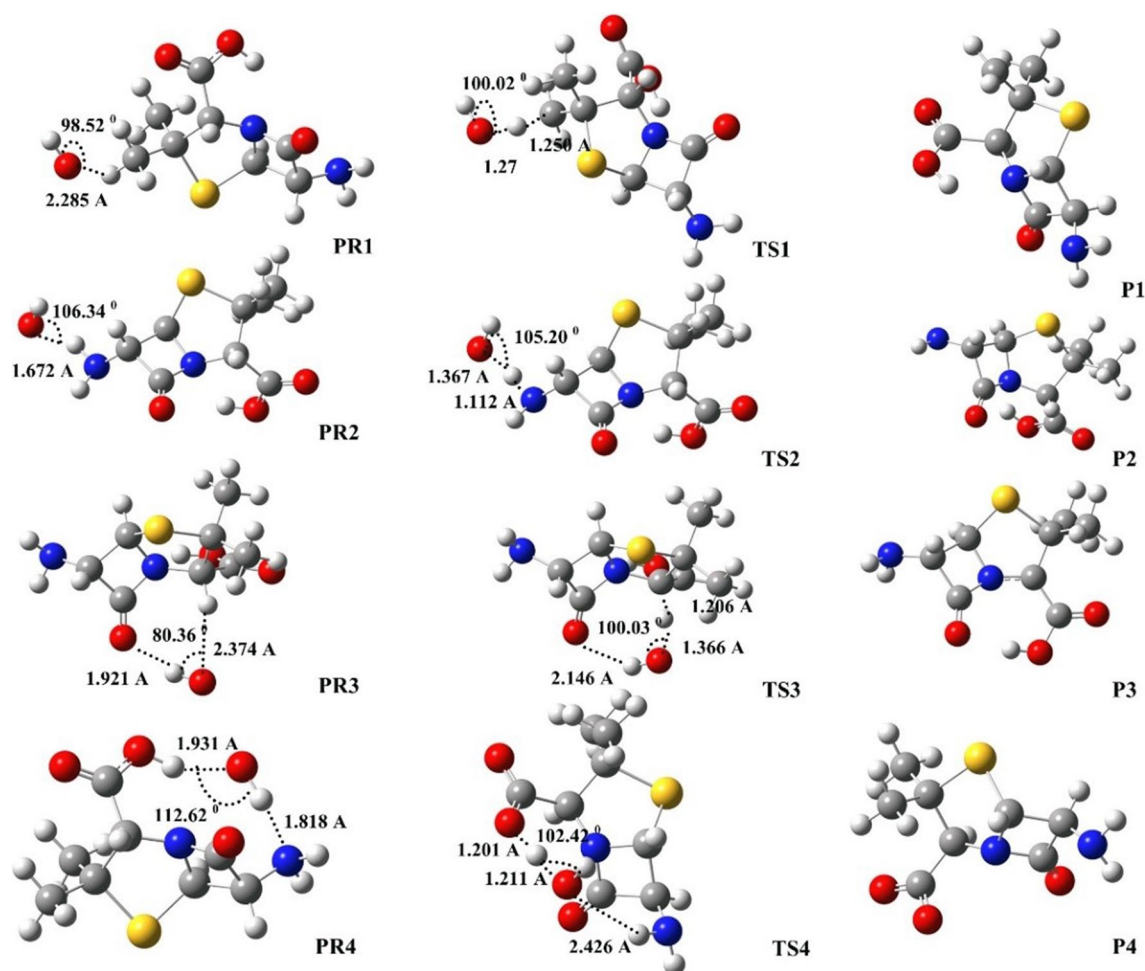
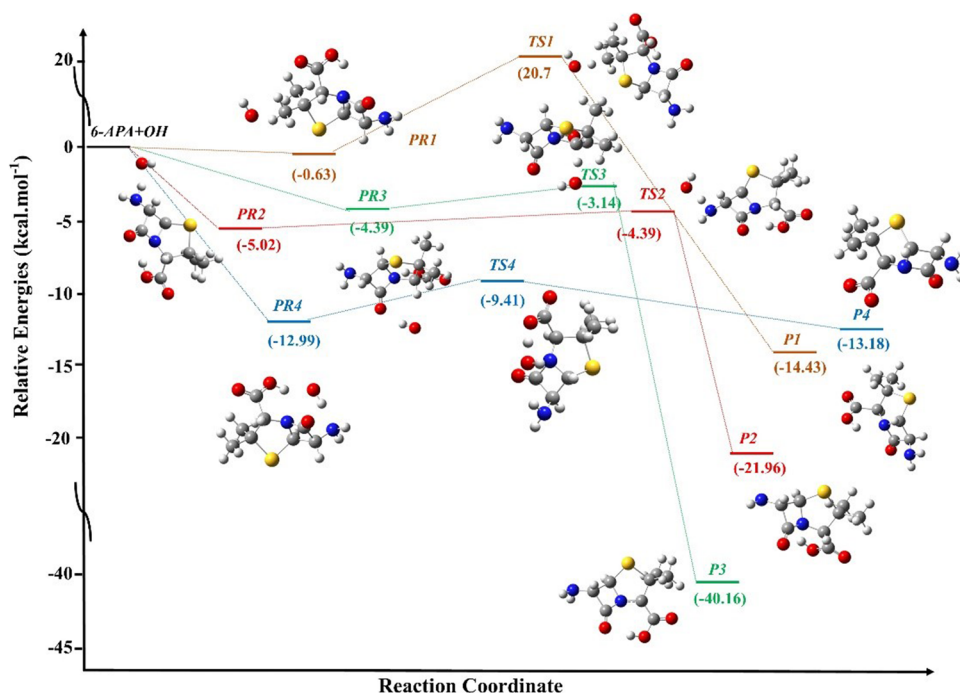


Fig. 2 Optimized geometries of pre-reactive complexes, transition state complexes, and products for hydrogen abstraction reaction paths for B3LYP/6-31G(d,p)

Fig. 3 Potential energy diagram for hydrogen abstraction paths for B3LYP/6-31G(d,p)



bonds remain the same. In the transition state complexes, the breaking bond lengths C-H and N-H of 6-APA are 1.25 Å, 1.11 Å, 1.21 Å, and 1.20 Å. The elongation in broken bonds is 0.16, 0.09, 0.11, and 0.22 Å for TS1, TS2, TS3, and TS4, respectively. The length of the O-H bond formed is also important in the formation of TS complexes along the reaction coordinate. The occurring O-H bond lengths are 1.27 Å, 1.37 Å, 1.37 Å, and 1.21 Å for TS1, TS2, TS3, and TS4, respectively. So these structures are early transition states that resemble reactants, as stated in Hammond's postulate [40]. In transition state structures, the angles between the approaching OH radical and the abstracted hydrogen atoms average 101.92°. As seen in the potential energy diagram (Fig. 3), all transition state complexes have higher energy than pre-reactive complexes. The TS energies except TS1 are below the energies of the reactants, and we can order their stability TS4 > TS2 > TS3 > TS1. The energies of the transition state complexes are 21.34, 0.63, 1.25, and 3.58 kcal/mol higher than those of the pre-reactive complexes, respectively.

Addition paths

The optimized geometries of the pre-reactive complexes, transition state complexes, and products formed in hydroxyl radical addition paths and the potential energy graphs are given in the Supplementary Material.

In the pre-reactive complexes PR5 and PR6, the C-O bond lengths of the OH radical and the C5 and C22 atoms are 3.40 Å and 3.50 Å, respectively. In the pre-reactive complex structures, the bond angle with the OH radical is

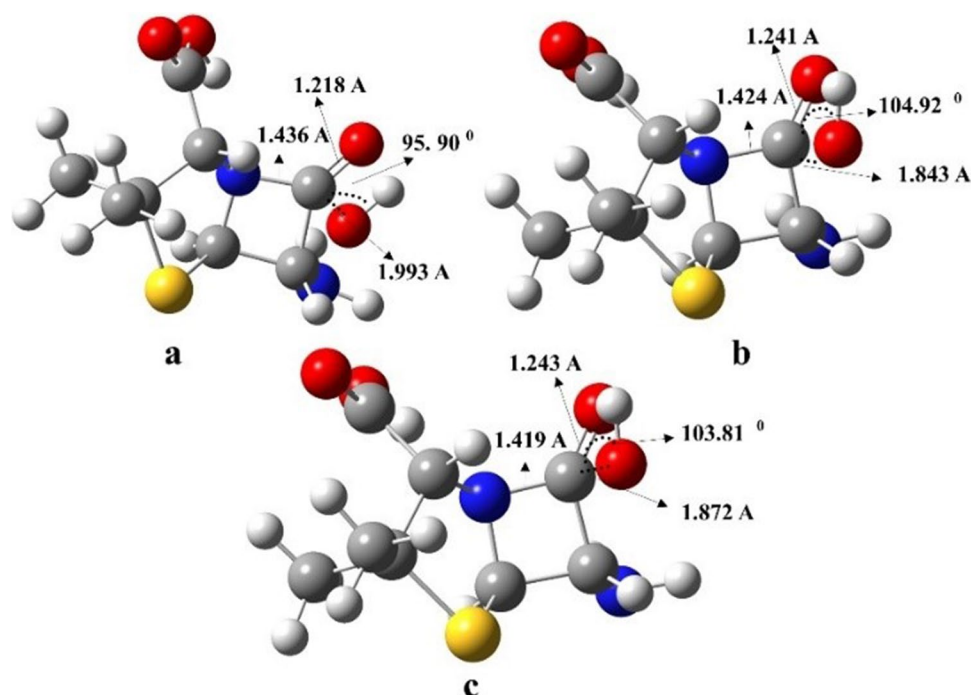
approx. 91.61°. For TS structures, the length of the C-O bonds formed by the interaction of the hydroxyl radical and carbonyl groups is 1.88 (C5) Å and 1.99 (C22) Å for TS5 and TS6, respectively. The angle between carbonyl groups and the OH radical in TS5 and TS6 is approximately 101.92°. As seen in the potential energy diagram in the supplementary file, the energy of TS5 is higher than that of the reactants and TS6.

In this study, functional effects on molecular geometry are also tried to understand. The obtained transition state complex structures for path 6 are given together for different functionals. Interestingly, it is seen that functional differences have no important effect on the molecular geometries of the transition state complex structures. It is understood from Fig. 4 that no matter what functionals are used, similar structures are found. In Domingo's study [26], the same results were also found for the structure of transition state complexes.

Energetic and kinetic parameters

The calculated thermodynamic parameters for hydrogen abstraction and OH-addition reaction paths are given in Table 1. As can be seen from Table 1, the Gibbs free energy of path 5 is positive for all three functionals. Therefore, it can be concluded that path 5 is a thermodynamically non-spontaneous process. The most negative enthalpy and Gibbs free energies belong to path 6, with values of -47.24 kcal/mol and -38.57 kcal/mol (B3LYP). So, with the addition of OH radical to the carbonyl group of the beta-lactam unit,

Fig. 4 Optimized geometries of transition state complexes' structures for path 6 **a** B3LYP, **b** M06-2X, **c** MPW1PW91



path 6 spontaneously occurs with its exergonic nature. This result is also compatible with some experimental degradation studies [41–43]. The order in the calculated Gibbs free energies is path 6 < path 3 < path2 < path1 < path 4 < path 5. This order is the same for the reactions enthalpies. All DFT functionals used have the same energy order as seen in Table 1.

The calculated kinetic parameters of the 6-APA with the OH radical are listed in Table 2. As seen in Table 2, the lowest activation Gibbs free energy belongs to path 6, and the highest one belongs to path 1. This result is also the same for rate constants and branching ratios. Among the reaction paths, the OH-addition reaction from the beta-lactam ring of 6-APA, path 6, is the one that will most likely occur. Among the hydrogen abstraction paths, the smallest activation Gibbs free energy belongs to path 4, hydrogen abstraction from the carboxylic acid end. This

path is the second possible reaction path, as seen from its branching ratio. Among the all hydrogen abstraction paths for hydrogen abstraction from the methyl group, path 1 has a minor effect on the reaction kinetics. The total rate constant value calculated according to B3LYP is closer to the experimentally obtained value than the total rate constant results of other functionals [44]. We can conclude that B3LYP gives better results for the 6-APA degradation reaction. Similar results were found in the Rajakumar et al. study for the OH radical degradation reaction with bromine oxide [45].

In order to show the effectiveness of a higher base set on the results, a single point energy calculation was done with the B3LYP/6–311 + G(d,p) basis set [30]. All the results are given in the Supplementary Materials. As seen in Table S3, the rate constant is more consistent with the experimental value when calculating with a higher basis set.

Table 1 Enthalpies (ΔH , kcal/mol) and Gibbs free energies (ΔG , kcal/mol) for different functionals

	B3LYP		M06-2X		MPW1PW91	
	ΔH	ΔG	ΔH	ΔG	ΔH	ΔG
1	-12.89	-14.79	-14.95	-16.71	-10.68	-11.96
2	-19.40	-20.33	-17.20	-18.40	-14.02	-15.05
3	-36.25	-37.51	-32.47	-34.13	-30.61	-32.36
4	-10.58	-13.21	-2.79	-4.59	-3.37	-5.23
5	-5.09	5.71	-8.63	2.42	-6.62	4.48
6	-47.24	-38.57	-48.50	-40.73	-46.08	-36.66

Table 2 Calculated kinetic parameters, I (cm⁻¹), ΔG^\ddagger (kcal/mol), k (M⁻¹ s⁻¹)

	B3LYP				M06-2X				MPW1PW91			
	I	ΔG^\ddagger	k_{calc}	δ	I	ΔG^\ddagger	k_{calc}	δ	I	ΔG^\ddagger	k_{calc}	δ
1	-1338.24	8.22	5.82×10^6	2.55×10^{-3}	-1583.48	4.65	2.42×10^9	0.10	-1448.66	9.03	1.49×10^6	3.96×10^{-4}
2	-791.29	3.92	8.27×10^9	3.63	-814.08	1.69	3.60×10^{11}	15.45	-959.46	5.68	4.28×10^8	0.11
3	-837.03	3.64	1.33×10^{10}	5.83	-1518.74	2.86	4.98×10^{10}	2.13	-946.18	3.67	1.27×10^{10}	3.37
4	-1281.93	2.96	4.15×10^{10}	18.20	-353.46	2.74	6.09×10^{10}	2.61	-685.20	2.46	9.76×10^{10}	25.96
5	-432.25	5.25	8.80×10^8	0.39	-612.15	3.41	1.96×10^{10}	0.84	-1363.31	3.67	1.28×10^{10}	3.40
6	-641.10	2.15	1.64×10^{11}	71.93	-203.93	0.72	1.84×10^{12}	78.86	-493.26	1.90	2.53×10^{11}	67.29
k_{tot}			2.28×10^{11}				2.33×10^{12}				3.76×10^{11}	
$\log k_{\text{tot}}$			11.36				12.37				11.58	
$\log k_{\text{exp}}$ [44]			9.38				9.38				9.38	

Effect of explicit water molecules on the reaction kinetic

Adding some discrete water molecules to the implicit computation is an important strategy to explain the effect of water on the reaction. This is less costly and simpler for getting good, comparable results with experimental ones [46].

The effects of discrete solvent water molecules on the reaction kinetics are also investigated. Because of the high computational time demands of this type of calculation, explicit solvent model calculations are only performed for the most probable reaction path, path 6. Thus, 1 and 2 open water molecules are added to the reaction coordinate to test the water environment effect (0 water model is the pure implicit model). For the selected reaction path, the addition of water for the pre-reactive and transition state complexes, and products is done one at a time in the reaction center. After the addition of water molecules to each structure, re-optimizations are performed by allowing all added water molecules to interact with the 6-APA molecule. The optimized structures by adding the explicit water molecules for path 6 are given in Fig. 5. IRC calculations were performed to confirm the transition state that connected the true reactants and products for path 6, and these plots are given in Fig. 6. The potential energy diagrams for the explicit solvent models are given in the Supplementary Material.

In one water model, the stabilization of the pre-reactive complex occurs by forming hydrogen bonding between the oxygen of the water molecule and the hydrogen atom of O25 with a distance of 1.71 Å. In this pre-reactive structure, the approaching distance of the OH radical to C5 is 3.01 Å which is 0.01 Å smaller than the same bond in the 0 water model. In the transition state complex structure, the distance between the OH radical and the C5 atom is 2.09 Å. In this complex, two hydrogen bonds occurred by hydrogen of O25 and oxygen of water is 1.71 Å and hydrogen of water and O24 is 1.87 Å. The obtained product structure in 1 water model contains two different extra hydrogen bondings with oxygen of water and hydrogen of O23 and oxygen of water

and hydrogen of C8 bond lengths of 1.93 Å and 2.42 Å, respectively. It is seen from Fig. 5 the pre-reactive complex of 2 waters model, explicitly added water molecules interacts with O25, oxygen of hydroxyl radical, and hydrogen of C8 atom with bond lengths of 2.19 Å, 2.18 Å, and 1.71 Å, respectively. In the transition state complex structure for the 2 waters model, the bond distance between the oxygen atom of OH radical and the C5 atom of the 6-APA molecule is 1.74 Å. The transition state structure is stabilized by hydrogen bondings between hydrogen atoms of water molecules and 6-APAs' of O24 atom with distances of 1.90 Å and 1.79 Å, respectively. In product structure, three hydrogen bonds occurred with water molecules, hydrogen of C8 and O24, and hydrogen of N19, with bond lengths of 2.44 Å, 1.93 Å, and 2.00 Å, respectively.

Hydrogen bonds are important attractions for occurring pre-reactive complexes, transition state complexes, and products. As a result of these attractions, the energy of the molecules decreased and their stabilization increased. As seen in Fig. 5, for the 1 water model, the addition of water molecules results in molecular attraction, and the hydroxyl radical distance to the C5 atom is 0.098 Å higher than for the 0 water model. This distance is 0.251 Å smaller than the transition state complex found for the 2 waters model. In the explicit 2 waters model, the OH radical can approach the carbonyl group in the beta-lactam ring more easily than in the implicit model. That, in turn, affects the reaction properties.

The calculated thermodynamic and kinetic parameters for 0 water, 1 water, and 2 water models are given in Table 3. It is seen from Table 3, one and two water models are the exergonic paths, and their enthalpy and Gibbs free energy values are all negative. The activation Gibbs free energy value in the pure implicit model is 2.15 kcal/mol. As the number of explicit water molecules increases, the Gibbs free energy also increases. Accordingly, as can be seen from Table 3, the reaction rate also decreases. In the reaction mechanism, hydrogen bonds formed between 6-APA and the oxygen atom of the water molecule cause the

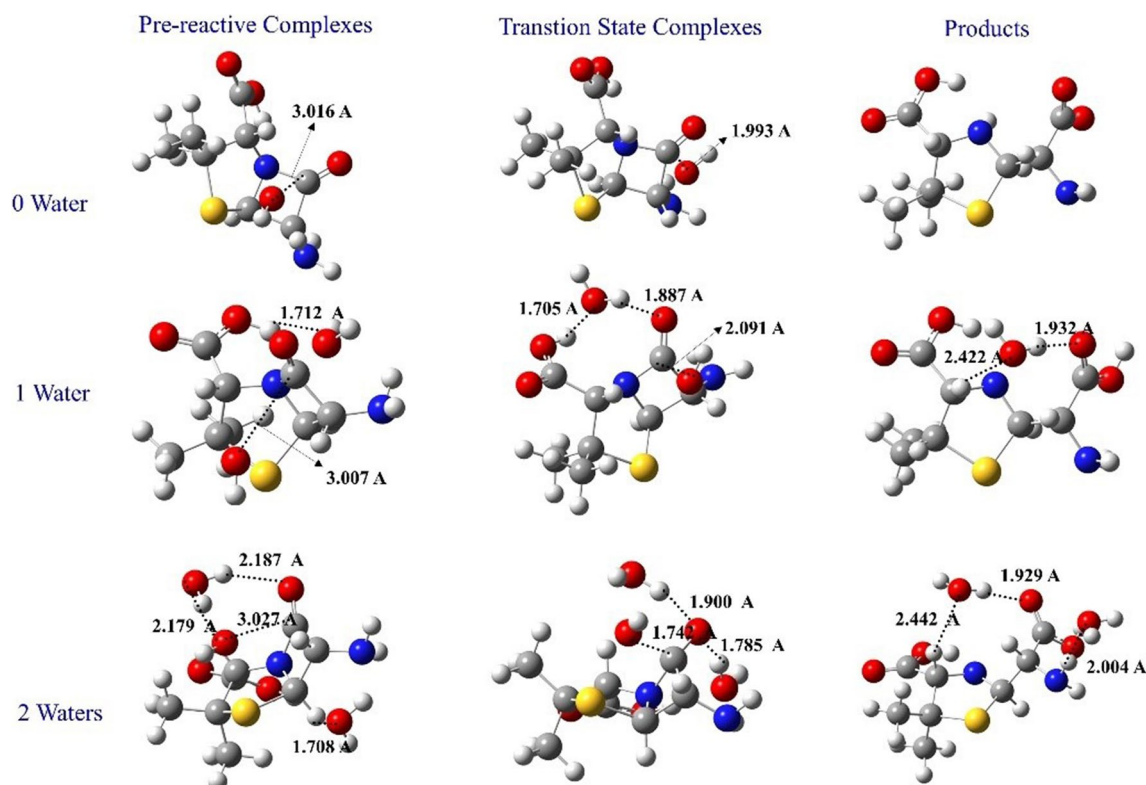


Fig. 5 Optimized geometries of pre-reactive complexes, transition state complexes, and products for varying number of water molecules

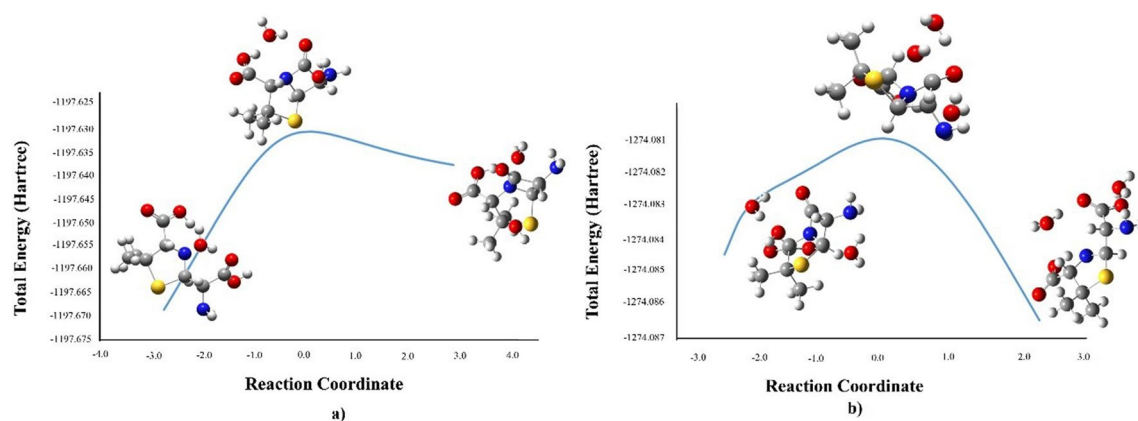


Fig. 6 IRC plots for path 6 **a** 1 water model and **b** 2 waters model

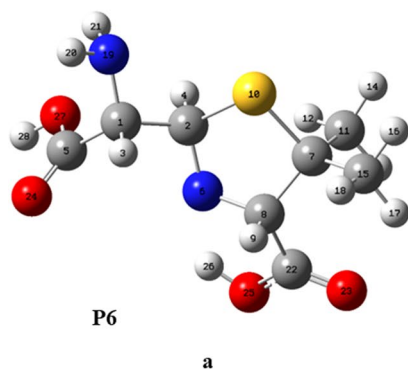
reaction to be suppressed. Thus, as the number of explicitly added water molecules increases, the relative energies of the structures increase, and the molecular system becomes unstable. Because, during the investigation of the reaction with explicit water molecules, the water molecules can form hydrogen bonds with each other and with 6-APA. Adding more water molecules makes the theoretical degradation kinetic model results more compatible with the experimental ones. The addition of explicit water molecules causes the relative energies of the structures to increase, as seen in

Table 3. Thus, instability occurs in the molecular system, and thus the Gibbs activation free energy increases. In addition, as can be seen from the entropy values, as the number of water molecules increases, the entropy increases due to the disorder. As a result, instability occurs in the molecular system, resulting in an increase in Gibbs activation free energy. Therefore, it can be concluded that 2 waters model can be used for the degradation kinetics of other penicillin derivatives. Ideally, working with explicit water molecules yields results closer to the experimental results, although

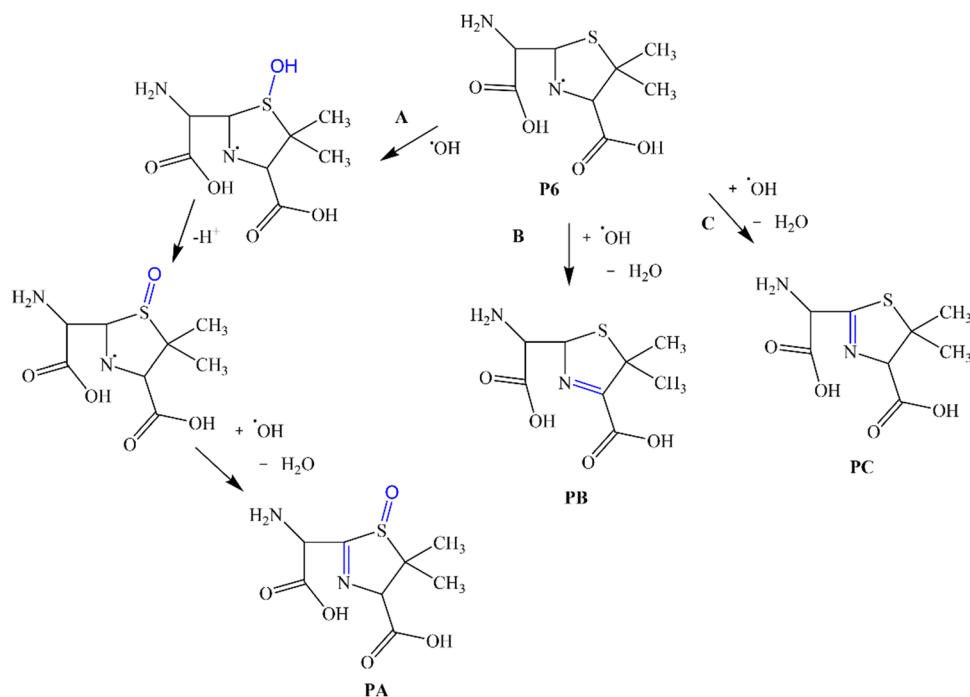
Table 3 Calculated thermodynamic and kinetic parameters for path 6

	Explicit models		
	0 Water	1 Water	2 Waters
ΔH (kcal/mol)	-47.24	-37.41	-37.41
ΔS (cal/mol/K)	-29.08	0.67	2.08
ΔG (kcal/mol)	-38.57	-37.61	-38.03
I (cm ⁻¹)	-641.10	-479.79	-258.26
ΔG^\ddagger (kcal/mol)	2.15	2.94	5.95
k_{calc} (M ⁻¹ s ⁻¹)	1.64×10^{11}	4.31×10^{10}	2.67×10^8
$\log k_{\text{calc}}$ (M ⁻¹ s ⁻¹)	11.21	10.63	8.43

the computational difficulties and numerous configurations make it very unwieldy. Therefore, it can be concluded that 2 waters model can be used for the degradation kinetics of other beta-lactam derivative antibiotics.

Fig. 7 **a** Optimized geometry for P6 and **b** Mulliken charge populations and Fukui functions of P6

P6	q(N)	q(N+1)	q(N-1)	f_i^+	f_i^-	f_i^0
C1	6.006	5.984	6.036	-0.022	-0.030	-0.026
C2	6.087	6.008	6.147	-0.080	-0.059	-0.070
C5	5.410	5.422	5.377	0.012	0.032	0.022
N6	7.383	7.728	7.275	0.345	0.109	0.227
C7	6.130	6.097	6.172	-0.033	-0.042	-0.037
C8	6.018	5.941	6.045	-0.078	-0.026	-0.052
S10	15.935	16.083	15.664	0.149	0.271	0.210
C11	6.311	6.302	6.324	-0.009	-0.013	-0.011
C15	6.318	6.314	6.322	-0.004	-0.004	-0.004
N19	7.606	7.623	7.541	0.017	0.065	0.041
C22	5.383	5.425	5.344	0.042	0.039	0.040
O23	8.486	8.528	8.429	0.041	0.057	0.049
O24	8.490	8.513	8.443	0.023	0.047	0.035
O25	8.498	8.522	8.470	0.024	0.028	0.026
O27	8.492	8.498	8.480	0.006	0.012	0.009

Scheme 2. Possible subsequent reaction mechanism of P6

Subsequent processes of the P6

The Fukui functions of atoms in P6 were calculated to examine the plausible subsequent processes of the most probable product, P6. The optimized geometric structure and Fukui functions of P6 are given in Fig. 7, and the predicted degradation mechanism is given in Scheme 2.

The atoms with a larger Fukui functions value are the possible reaction sites. As demonstrated in Fig. 7b, N6 and S10 are suitable sites for electrophilic hydroxyl radical attack. In path A, hydroxyl radical attack to S10 atom in the thiazolidine ring leads to the production of an oxidation product. Then PA is obtained by hydrogen abstraction of the hydroxyl radical from the carbon atom near the nitrogen atom (N6) of the oxidation product. Serna-Galvis et al. obtained a similar product in the degradation study of oxacillin, a beta-lactam type antibiotic [47]. In path B and path C,

products of hydrogen atoms abstracted from C atoms bound to reactive N6 are proposed. In these paths, PB and PC are formed as a result of hydrogen abstraction from the unsaturated thiazolidine ring. Similar reactions and products were obtained in experimental studies [22, 47–49].

Conclusions

In this study, the degradation kinetics of 6-APA with hydroxyl radicals are investigated by the DFT method with different functionals. The comparison between the three functions shows that the B3LYP results are more consistent with the experimental results than the M06-2X and MPW1PW91. The calculated kinetic and thermodynamic parameters, reaction enthalpies, and Gibbs free energies demonstrate that the OH-addition path is more favorable than the H-abstraction path. It was found that OH radical addition to the carbonyl group of the beta-lactam ring (path 6) is the most favorable path. Water molecules affect the degradation reaction mechanism. As the number of solvent water increases, the results of the explicit model are in agreement with those obtained experimentally. The energy of the molecular system increases with the addition of explicit water molecules, and accordingly, the reaction rate constant decreases. With the addition of two water molecules, the rate constant is more in agreement with the experimental results. It can be concluded that the results of the explicit water model play an important role in estimating the experimental degradation kinetic rate constant. Finally, possible subsequent reactions of P6 were also examined. The proposed end products are compatible with the literature. Therefore, such theoretical studies will be informative in terms of understanding the degradation kinetics of other beta-lactam-derived antibiotics.

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Data availability It will be given if it is necessary.

Code availability It will be given if it is necessary.

Declarations

Conflict of interest The authors declare no competing interests.

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