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Comparison and selection criterion of missing imputation methods and quality assessment of monthly rainfall in the Central Rift Valley Lakes Basin of Ethiopia

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Abstract

Missing data is a common problem in all scientifc research, and the availability of gap-free data is rare in most developing countries. Statistical and empirical methods are the most often used for the approximation of missing data. The performance of eight missing estimation methods was evaluated using PBIAS, RMSE, and NSE for stations located in the rift-bounded lakes system of Katar and Meki subbasins in Ethiopia. The multicriteria decision method of compromise programming was used to identify the best imputation method. Four homogeneity test methods were used to evaluate the homogeneity of the time series data. The Mann–Kendall trend test and Son's slope were used to locate the change and calculate the magnitude of the trend. Multiple linear regression and multiple imputation by chained equations were well performed at most stations. Alternatively, the modified version of IDWM based on spatial distance and elevation difference (IDWM_{E&D3} for $k=3$) was ranked third at many stations. The inclusion of elevation diferences between stations has improved the capability of the inverse distance weight method. However, the performance of all the missing estimation methods decreased as the percentage of missing data increased. Radius infuences have no signifcant impact on the performance of missing imputation methods. Only Butajera station exhibited nonhomogeneity. Dagaga, Iteya, Bui, and Butajera stations all exhibited decreasing trends. Kulumsa and Ejerese-Lele stations presented an increasing trend in monthly rainfall. However, the rest station has shown no signifcant increasing or decreasing trends in monthly rainfall.

1 Introduction

Missing data is a common problem in all scientifc research, project planning, and the development of water resource infrastructure. It (i) reduces the power and precision of

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statistical analysis results (Piazza [2011](#page-19-0); Houari et al. [2014](#page-18-0); Schmitt et al. [2015;](#page-19-1) Gao et al. [2018](#page-18-1)); (ii) leads to a biased estimate and draws the wrong conclusion about the relationship between two or more variables (Pigott [2001;](#page-19-2) Gao et al. [2018;](#page-18-1) Ekeu-wei et al. [2018](#page-18-2); Gao et al. [2018;](#page-18-1) Teegavarapu et al. [2019](#page-19-3)). It is very common in hydrology and other related felds to estimate the missed values of a target station from the values of neighboring stations. There are various methods available to approximate the missing value of the target station, and they are grouped as empirical, statistical, and function-ftting methods (Xia et al. [1999;](#page-19-4) Sattari et al. [2016\)](#page-19-5). Unusually, deleting or substituting missing values by the arithmetic mean or median is used as an alternative method (Peugh and Enders [2004\)](#page-19-6). Modern approaches, including spatial interpolation techniques such as inverse distance weighting average (IDWA), normal ratio (NR), simple arithmetic average (AA), kriging, and co-kriging, are the most widely used techniques in diferent geographic locations (Hartkamp et al. [1999;](#page-18-3) Ferrari and Ozak [2014](#page-18-4); El Kasri et al. [2018](#page-18-5); Barrios et al. [2018](#page-17-0)). The statistical methods, including correlation coefficient weighting (CCW) and

multiple linear regression (MLR), are used alternatively to compute the missing values for the target station (Xia et al. [1999](#page-19-4); Barrios et al. [2018\)](#page-17-0). Recently, the advance of big data analysis and the computing power of the computer have created an opportunity for the development of multiple imputation by chained equation (MICE) (Peugh and Enders [2004](#page-19-6); Schmitt et al. [2015;](#page-19-1) Gao et al. [2018\)](#page-18-1).

More than 21 missing estimation methods are available in the scientifc literature (Armanuos et al. [2020](#page-17-1)), and it is very difficult to identify which method is the best for specific geographic locations. Choosing any of the methods among the alternatives depends on the characteristics of the observed variables (Gao et al. [2018\)](#page-18-1), the geographic location and spatial distance between the stations (Barrios et al. [2018\)](#page-17-0), the percentage of missing data (Radi et al. [2015\)](#page-19-7), and the characteristics of the missing mechanism (Rubin [1976;](#page-19-8) El Kasri et al. [2018](#page-18-5)). It is very common to use any of the imputation methods based on an individual's preferences, knowledge, or experience (Hasanpour Kashani and Dinpashoh [2012](#page-18-6)). But the random use of any missing estimation method without evaluating its performance will increase the error value and reduce the reliability of the statistical results (Ismail and Ibrahim [2017;](#page-18-7) Barrios et al. [2018;](#page-17-0) El Kasri et al. [2018](#page-18-5)).

Recently, research has started to evaluate the ability of missing imputation techniques using statistical metrics. For instance, Barrios et al. ([2018](#page-17-0)) assessed the capability of the five missing estimation techniques and the effect of the radius of infuence on the complex topography of central South Chile and discovered that the ANN, MLR, and IDW had produced the lowest errors and were the best technique for bridging the gap of missed monthly rainfall. El Kasri et al. (2018) have evaluated the performance of five imputation methods in the southern Atlas of Morocco and have recommended the Theisen polygon, normal ratio, inverse distance weighted, and multiple imputation methods as the best methods for flling the gap of missed rainfall. Similarly, Ismail and Ibrahim ([2017](#page-18-7)) have recommended the inverse distance-weighted and correlation coefficient methods to fill the data gap. The normal ratio (NR) and multiple imputation (MI) methods are considered the most appropriate methods by Radi et al. [\(2015](#page-19-7)) at 5%, 10%, and 20% to represent various cases of missing data percentages. A similar study to this was conducted by Addi et al. [\(2022](#page-17-2)) in the river basin in Ghana. The authors evaluated the statistical imputation techniques of mean, regression, multiple imputation by chain equation, *k*-nearest neighbor, missForest, linear interpolation, hot deck, expectation maximization, Gaussian copula, inverse distance weighting, and kriging methods by artifcially adding missing record percentages (5%, 10%, 20%, and 30%) to the entire datasets. The performance of the imputation methods was assessed using the root mean square error, mean absolute error, bias, coefficient of determination, similarity index, and Kolmogorov–Smirnov performance statistics (Addi et al. [2022\)](#page-17-2). They have reported that, based on the performance criteria chosen, the fndings were variable. However, regression, PPCA, and missForest imputation methods were the top contenders.

It is very difficult to decide which infilling technique is best suited depending on two to more performance statistics without referring to the criteria on the decision-making process (Armanuos et al. [2020\)](#page-17-1). When many criteria (or objectives) must be taken into account at once, multi-criteria decision-making (MCDM) is one of the most exact ways to make decision (Aruldoss [2013\)](#page-17-3). Multi-criteria decision method was developed by Benjamin Franklin when he published his research on the moral algebra concept (Taherdoost and Madanchian [2023\)](#page-19-9). Since then, the method has been widely used in the felds of engineering (Raju and Nagesh [2014\)](#page-19-10), urban transport (Hajduk [2022\)](#page-18-8), computer science (Pramanik et al. [2021](#page-19-11)), social science (Pomerol and Barba-Romero [2000](#page-19-12)), agriculture (Romero and Rehman [2003](#page-19-13)), healthcare and bioengineering (Ozsahin et al. [2021](#page-19-14)), hydrology and water resources engineering (Yilmaz and Harmancioglu [2010](#page-20-0); Osinowo and Arowoogun [2020](#page-18-9); Gebre et al. [2021](#page-18-10); Vassoney et al. [2021;](#page-19-15) Abdullah et al. [2021](#page-17-4)) to solve complex problems by setting diferent criteria (Taherdoost and Madanchian [2023](#page-19-9)). The method allows researchers to consider multiple factors simultaneously and analyze efectively, weigh their importance, and make informed decisions based on a comprehensive evaluation of the problem at hand (Beula and Prasad [2012\)](#page-18-11). For example, Raju and Kumar [\(2014\)](#page-19-16) used multicriteria decision method (MCDM) to rank the global climate model after evaluating their performances to simulate the climate condition in India. Similarly, the authors of this research (Balcha et al. [2023](#page-17-5)) applied MCDM of compromise programming to select the best regional climate model (RCM) for the same study area.

All the above-mentioned studies have evaluated the ability of diferent missing imputation methods, and there are no signifcant studies reported to consider the problem from a multi-objective perspective or provide a clear approach or criteria to select the best method from a wide range of alternatives for missing data management. Furthermore, the choice of inflling technique may also depend on the intended application of the flled data, and the researchers may need to consider any potential biases or limitations associated with each inflling method before making a fnal decision. This is more of a series in an area of complex topography, sparsely and unevenly located measuring stations, and specifc climate conditions like the Central Rift Valley Lakes subbasin of Ethiopia. For example, stations found at high altitudes have received the highest amounts of rainfall compared to stations at lower altitudes in the study region. Even so, stations located at similar altitudes but in opposite directions, such as Leeward or Windward, have exhibited diferent agroecology and rainfall amounts.

Therefore, to overcome with research gaps the present study seeks to (i) identify performance metrics and assess the performance of eight missing imputation methods; (ii) use a compromise programing method to rank and choose the best imputation method; and (iii) evaluate the homogeneity and trend of the monthly precipitation dataset for selected stations in the study region.

2 Materials and methods

2.1 Description of study area

The Great Rift of the Earth runs from Jordan southward through East Africa to Mozambique (Meshesha et al. [2012](#page-18-12)). The Ethiopian rift extends from the Kenya border up to the Red Sea and is divided into three subsystems: Chew Bahir (Lake Stephanie), the Central Rift Valley Lakes subbasin, "hereafter referred to as the CRV Lakes subbasin," and the Afar triangle. The CRV is subdivided into four hydrologically interconnected lakes, namely, Ziway, Langano, Shalla, and Abijata. Ziway Lake is the only freshwater lake among the rest of the lakes and fows into Abijata Lake through the Bulbula River. Two river systems fow into Ziway, namely, the Katar and Meki rivers. The Katar and Meki watersheds are located in the CRV Lakes subbasin of Ethiopia's Rift Valley Lakes Basin. Geographically, the Katar watershed extends between 38.88° and 39.41° E longitudes and 7.36° and 8.18° N latitudes eastward of Lake Ziway. The Meki watershed is extended between 38.22° and 39.00° E longitude and 7.83° and 8.46° N latitude westward of Lake Ziway. The altitude ranges from 1600 m above mean sea level (a.m.s.l.) on the rift foor near Ziway Lake to 4118 a.m.s.l. in the Katar and Meki subbasins (eastern and western highlands, respectively). The subbasins are subdivided into three topographic zones: the eastern highlands (Arsi Mountains, Wonji fault belt) form the eastern escarpment of the rift system; the western highlands (Guraghe Mountains, Silte-Bishoftu fault zone) form the western escarpment; and the rift foor (Ayenew [2001](#page-17-6)). The average annual precipitation ranges from 749 to 1276 mm and 712 to 1150 mm, respectively, for the Katar and Meki subbasins (Fig. [1](#page-2-0)). Average monthly minimum and maximum temperatures in the subbasins range between 13.4 and 14.2 °C and 27.5 and 28.7 °C, respectively, and 24 to 27 °C and 27.5 to 30 °C in the high land areas. According to Hulluka et al. [\(2023](#page-18-13)),

Fig. 1 Location of the study area, target station (red star) and neighboring stations (black star). The elevation data extracted from a 30 m resolution of Shuttle Radar Topographic Mission

rainfed agriculture accounts for 76.8% of the area, while irrigated agriculture accounts for less than 3%. Approximately 44% of the existing irrigated area is dependent on surface water from streams, 31% on Lake Ziway directly, and 25% on groundwater wells.

2.2 Data accusation

2.2.1 Observed data

Monthly observed rainfall data for 22 meteorological stations was collected from the National Meteorology Agency of Ethiopia (ENMA) for the time intervals of January 1997 to December 2017. Exploratory data analysis includes the prescreening of negative values of precipitation, multiple dots between values, and computing the missing percentage and the outlier for each station. Additionally, the spatial distances between stations were calculated to determine the maximum radius of infuence. Stations that were more than 40 km away from any other station and had more than 25% missing values been excluded from the analysis. Sixteen meteorological stations were selected in this study for further analysis [1](#page-3-0)).

2.2.2 Reanalysis data

In Ethiopia, most stations are unevenly located on the main roads of cities and do not provide timely or sufficient data free of missing value. This is causing inhomogeneity, abrupt change, and trends in climate datasets. The reanalysis data has been extensively used as an alternative source of information for the study of climate variability (Dile and Srinivasan [2014;](#page-18-14) Fuka et al. [2014](#page-18-15); Funk et al. [2015](#page-18-16); Alhamshry et al. [2020](#page-17-7)) and to evaluate the ability of regional climate model (RCM) output (Bichet et al. [2020](#page-18-17)). In this study, the Climate Hazards Group Infrared Precipitation with Station (CHIRPS) was downloaded from [http://clima](http://climateserv.servirglobal.net/site) [teserv.servirglobal.net/site](http://climateserv.servirglobal.net/site) for the time span of 1983–2005 to assess the ability of missing imputation methods. CHIRPS is a quasi-global dataset (covering the area between 50° N and 50° S) available from 1981 to present day at 0.05° spatial resolution (5.3 km), and it is produced using multiple data sources developed to support the US Agency for International Development Famine Early Warning Systems Network (FEWS NET) (Funk et al. [2015\)](#page-18-16).

2.3 Over view of missing data

The distribution of missing values in the percentage varies from station to station. The ratio of missing values in percentage for the years considered is displayed in Fig. [2](#page-4-0)**.** The percentage of missing observations in the selected stations varies from 0.36 in Kulumsa to 22.1% in Katar G. stations. The study considers diferent techniques of inflling daily rainfall and compares them to identify the best method for each of the selected stations.

2.4 Approaches of the evaluation

Four steps are followed to assess the performance of missing imputation methods. Monthly CHIRPS datasets of each grid point were extracted using a python script and interpolated

Table 1 Geographic location of selected stations, average rainfall, and percentage of missed precipitation (1983– 2005)

µRF is mean annual rainfall, σRF is the standard deviation of rainfall, % MD is the percent of missed data, Ele is the elevation in meters, lat. is latitude, and Lon is longitude

Fig. 2 Percentage of missing values (ratio of number of missing observations to total number of observations) of daily rainfall data from 1997 to 2017 for selected station in Katar and Meki subbasins

into each meteorological station using four grid points around each observed station using IDWM (Table [1\)](#page-3-0). Then, they deliberately and randomly assigned NA (not available) complete datasets of CHIRPS using R-program to represent diferent levels of missing percentage of 5%, 10%, 15%, 20%, and 25% of Table [1](#page-3-0) using R software. Second, stations within a 20-and 40-km radius of infuence from the target station were considered neighboring stations and recalculated the missed values of target stations using eight imputation methods. Third, the ability of the imputation method was evaluated using RMSE, PBIAS, and NSE. Fourth, multicriteria decision methods of compromise programing was applied to identify the best imputation method for each station, and fnally, the quality of the data was studied for homogeneity and trend using the selected methods.

2.5 Methods of missing imputation techniques

More than 21 missing estimation methods are available in the scientific literature (Armanuos et al. [2020\)](#page-17-1), and it is very difficult to identify which method is the best for specific locations. Several authors employed diferent methods, which are already discussed in Sect. 1. There is no clear guideline or criteria to select the best imputation techniques in Ethiopia. Researchers or practitioners used any of the methods, mostly the Invers distance-weighted method, kriging, normal ratio method, or MICE based on personal experience, to fll in missing data, unaware of the impacts of missing data on rainfallrunoff modeling and the quality of the result. Different studies showed the necessity of evaluating the missing imputation techniques while using them for hydrological simulation. For example, Lee and Kang [\(2015](#page-18-18)) evaluated five kernel functions for predicting missing values for hydrological simulation using the SWAT model in the Imha watershed. The simulation results showed that the knn-regression exhibits lower SWAT simulation performance for streamfow estimation than other methods. The accuracy of rainfall data is critical for some complex models, like soil–plant-atmosphere models, which are sensitive to variations in precipitation and possibly other environmental inputs (Heinemann et al. [2002\)](#page-18-19). The variability of the simulated outputs is directly correlated to the accuracy of the model inputs. According to Zhang et al. ([2023\)](#page-20-1), the annual runoff increases by approximately 10% if the annual precipitation increases by 100 mm. In general, the strength of the selected methods are dependent on the type of the missing data mechanism, the state of neighboring stations, intrinsic features, and consecutive occurrences of rainfall, among other factors (Jahan et al. [2019](#page-18-20)). Therefore, the present study employed eight methods of missing imputation techniques in Ethiopia by artifcially introducing missing data for the complete dataset of monthly CHIRPS rainfall to represent the missing percentage of observed data in Table [1](#page-3-0).

2.5.1 Spatial imputation method

A deterministic spatial interpolation technique such as the inverse distance weighting method is modifed based on elevation difference, correlation coefficient (CC) , and a combination of correlation coefficient and Euclidian distance as weighting factors to estimate missing values for the target station (Vieux [2004;](#page-19-17) Barrios et al. [2018](#page-17-0)). According to Hartkamp et al. ([1999](#page-18-3)), the assumption is that values closer to the target station are more representative of the value to be estimated than values further away. Weights change according to the linear distance between target and neighboring stations; in other words, nearby stations have a heavier weight. In this spatial imputation method, missing values of target station were estimated based on the distance, elevation difference, and correlation coefficient between the target station and surrounding stations. The efficiency of this method depends on the strength of the correlation, the close distance, and the lesser elevation diference between the target stations and the surrounding stations (Teegavarapu and Chandramouli [2005;](#page-19-18) Armanuos et al. [2020\)](#page-17-1). The details of each method are given below.

a. Invers distance weighted average (IDWA)

The inverse distance weighting method is commonly used for approximately calculating missing data (Teegavarapu and Chandramouli [2005](#page-19-18)). The missing value of the target station is determined from the observed values of neighboring stations using Eq. [\(1](#page-4-1)) (Vieux [2004;](#page-19-17) Barrios et al. [2018\)](#page-17-0).

$$
P_{mi} = \frac{\sum_{i=1}^{n} d_{mi}^{-k} * q_{j(i)}}{\sum_{i=1}^{n} d_{mi}^{-k}}
$$
(1)

where P_{mi} is the calculated missing value of the target station, *n* is the number of neighboring stations, d_{mi} is the Euclidian distance between the target and neighboring station *i*, and $q_{j(i)}$ is the observed value at station *i*. *k* is a coefficient, and its value varies between 1 and 6, but the most commonly suggested value is 2 (Teegavarapu and Chandramouli [2005\)](#page-19-18). The negative sign of *k* implies that stations closer to the target stations are more important than those farther away (Vieux [2004\)](#page-19-17). The Euclidian distance between the target and neighboring stations is calculated using Eq. ([2\)](#page-5-0) (Barrios et al. [2018\)](#page-17-0).

$$
d_{m(i)} = \frac{\sqrt{(X_i - X_m)^2 + (Y_i - Y_m)^2}}{1000}
$$
 (2)

where X_i and Y_i are the projected coordinates of the neighboring stations, and X_m and Y_m are the projected coordinates of the target station.

b. Modified inverse distance weighting (MIDWE $_{\&D}$) based on elevation

Several researchers proposed the needs to modify the IDW (Vasiliev [1996](#page-19-19); Teegavarapu and Chandramouli [2005](#page-19-18), O'Sullivan and Unwin [2013](#page-18-21)). According to Vasiliev [\(1996](#page-19-19)), the IDW strongly depends on the existence of the strong positive autocorrelation. The normal inverse distance weighted method is mainly modifed by taking into account the spatial relationship between the target and neighboring stations, considering both their correlation coefficient weight (CCW) and elevation diferences. Elevation is one of the topographic factors that signifcantly afects the spatiotemporal distribution of precipitation and other climate variables (Golkhatmi et al. [2012\)](#page-18-22). As long as the elevation diference has an effect, the conventional inverse distance-weighted method is modifed by the inclusion of the elevation diference between the target and neighboring stations and the correlation coefficient. The values of k ranged from 1 to 3, and the IDWM_{E&D} was modified by varying the k values and missing values of the target station calculated using Eq. ([3\)](#page-5-1) (Barrios et al. [2018](#page-17-0)).

$$
P_{mi} = \frac{\sum_{i=1}^{n} h_{mi}^{-a} * d_{mi}^{-k} * q_{j(i)}}{\sum_{i=1}^{n} h_{mi}^{-a} * d_{mi}^{-k}}
$$
(3)

where h_{mi} is the elevation difference between the target and the neighboring station, and the exponent "*a*" is a power parameter and whose value ranges from 1 to 3, with the most commonly used value being 1 (Barrios et al. [2018](#page-17-0)).

c. Modified inverse distance weighted (MIDWMD $_{\&C}$) based on correlation coefficient

For orographic and complex climate regions, the normal inverse distance weighted method is modifed based on the spatial distance and correlation coefficient between the target and the neighboring station (R. Romero et al. [1998](#page-19-20)).

The missed value of the target station is estimated from the neighboring station by Eq. ([4](#page-5-2)):

$$
P_{mi} = \frac{\sum_{i=1}^{n} \alpha_{j(i)} * q_{j(i)}}{\sum_{i=1}^{n} \alpha_{j(i)}}
$$
(4)

 $\alpha_{j(i)}$ is the weighting factor between the target station and the neighboring stations. The weighting factor is calculated by using the Euclidian distance and Pearson correlation target and neighboring stations by Eq. (5) (5) :

$$
\alpha_{j(i)} = \frac{R_{j(i)}^2}{d_{j(i)}^2} \tag{5}
$$

where $R_{j(i)}^2$ is the correlation coefficient between the target station and the neighboring stations.

d. Coefficient of correlation weighting method (CCWM)

In this version of the inverse distance weighting method, the weighting factors are substituted by the correlation coef-ficient (Teegavarapu and Chandramouli [2005](#page-19-18); Teegavarapu [2009\)](#page-19-21), and the missing value of the target station is given by Eq. (6) (6) (6) :

$$
P_{mi} = \frac{\sum_{i=1}^{n} R_{j(i)} * q_{j(i)}}{\sum_{i=1}^{n} R_{j(i)}}
$$
(6)

where $R_{j(i)}$ is the coefficient of correlation, which is the ratio of covariance between the target and neighboring stations to the product of the standard deviation of the datasets. Its values are derived from available historical data.

2.5.2 Multiple linear regression (MLR)

Multiple linear regressions (MLR) are a statistical method used to estimate the relationship between one dependent variable and two or more independent variables. It is used to identify the best weighted combination of independent variables to predict the dependent variable (Sattari et al. [2017](#page-19-22)). Eisched et al. [\(1995](#page-18-23)) emphasized the benefts of the multiple linear regression method for interpolating missed data using Eq. [\(7](#page-5-5)):

$$
P_{mi} = a_{j(o)} + \sum_{i=1}^{n} a_{j(i)} q_{j(i)}
$$
\n(7)

where $a_{j(i)}$ is the regression coefficient and $a_{j(0)}$ is the intercept.

2.5.3 Multivariate imputation by chained equation (MICE)

Multivariate imputation by chained equations is known as sequential regression imputation, which estimates several missing values systematically and generates distinct sets of complete datasets. In this method, the incomplete dataset can be copied several times, and the missing values are imputed to each copied dataset diferently. The imputed missed values are randomly estimated for each copied dataset and combined into the average value of the dataset (Ibrahim et al. [2005](#page-18-24)). The R package of Bayesian-based MICE functions is available to compute missing values for the target station from the values of neighboring stations. The default setting was used in the MICE function to generate diferent imputed datasets using the predictive mean matching method (pmm) and five $(m=5)$ imputations. Finally, the imputed values were averaged to represent the missed value of the target station.

2.6 Accuracy assessment methods

There are several model accuracy assessment metrics described in the literature (Moriasi et al. [2007\)](#page-18-25). Root mean square error (RMSE), Nash-Sutcliff (NS_F) , and percent of bias (PBIAS) are commonly used to assess the performance and predictive capability of missing estimation methods (Moriasi et al. [2007;](#page-18-25) Barrios et al. [2018](#page-17-0)). RMSE can measure the error between the observed and predictive values and give greater weight to any extreme outliers present in the prediction results (Plouffe et al. [2015\)](#page-19-23). The optimal value varies between zeros, which means no residual variation and perfect model simulation, and a greater positive value (Moriasi et al. 2007) and calculated by Eq. (8) (8) :

$$
RMSE = \left(\frac{\left(\sum_{i=1}^{n} (Y_{oi} - Y_{si})^2\right)}{\left(\sum_{i=1}^{n} (Y_{oi} - Y_{mi})^2\right)}\right)^{1/2}
$$
(8)

According to Moriasi et al., ([2007\)](#page-18-25) and Barrios et al., (2018) , "Nash-Sutcliffe efficiency is a normalized statistic that determines the relative magnitude of the residual variance (noise) compared to the measured data variance (information)". It shows the degree of observed versus simulated aligned on the plot of the 1:1 line (Nash and Sutclife [1970\)](#page-18-26) and calculated by Eq. [9](#page-6-1):

$$
NS_E = 1 - \left(\frac{\left(\sum_{i=1}^{n} (Y_o - Y_s)^2\right)}{\left(\sum_{i=1}^{n} (Y_o - Y_m)^2\right)}\right)
$$
(9)

where Y_{oi} is the *i*th observed value, Y_{si} is the *i*th simulated value for Y_m is the mean of observed data, and *n* is the total number of observations. The NSE ranges between−∞ and 1.0, with $NS_E=1$ being the ideal value and values between 0 and 1 being the range for acceptable levels of performance, while values < 0.0 indicate unsatisfactory performance and the observed value is better predictor than the simulated (Moriasi et al. [2007\)](#page-18-25).

Percent of bias (PBIAS) measures the average diference between the simulated and observed counterparts (Moriasi et al. [2007;](#page-18-25) Barrios et al. [2018](#page-17-0)) and is calculated by Eq. [\(10](#page-6-2)):

$$
PBIAS = 100 * \left(\sum_{i=1}^{n} (Y_{oi} - Y_{si}) / \sum_{i=1}^{n} (Y_{oi})\right)
$$
 (10)

The optimal values of PBIAS vary between zero for perfect model simulation and a positive or negative value that shows model underestimation or over estimation of bias, respectively (Moriasi et al. [2007\)](#page-18-25).

2.7 Multicriteria decision method (MCDM) of compromise programing

There are several decision-making methods for diferent problems (Sabaei et al. [2015](#page-19-24); Mardani et al. [2015](#page-18-27); Majmder [2015;](#page-18-28) Raju and Kumar [2018\)](#page-19-25). In most multi-criteria decision-making (MCDM) models, assigning weights to criteria is an important step that needs to be reexamined. Though, determining the weights of criteria is one of the key problems that arise in multi-criteria decision making. Over the past few decades, various weighting methods that have been developed for solving diferent MCDM problems such as goal programming, analytic hierarchy process (AHP), weighted score method, VIKOR, TOPSIS, Elimination EtChoix Traduisant la REalite (ELECTRE), PROMETHEE, and gray theory, compromise programing (CP) (Aruldoss [2013;](#page-17-3) Odu [2019\)](#page-18-29). The primary distinctions between each weighting methods are the complexity level of the algorithms, weighting method of the criteria, the manner in that preferences are evaluated, the possibility of uncertain data, and, ultimately, the type of data aggregation. For example, analytic hierarchy process (AHP) is easy to use and faces issues due to the interdependence between criteria and alternatives. On the other hand, in fuzzy set theory (FST) using imprecise input is possible; however, this method is not easy to develop (Hajduk [2022;](#page-18-8) Taherdoost and Madanchian [2023\)](#page-19-9). The advantage and disadvantage of each method were summarized in Aruldoss ([2013](#page-17-3)). The multicriterion decision method of compromise programing (CP) weighting method is used to measure the minimum distance between the ideal value and performance indicators to identify and rank the missed imputation by Eq. ([11\)](#page-6-3) (Raju et al. [2016\)](#page-19-26):

$$
L_{p(a)} = \left[\sum_{j=1}^{J} w_j^p \left(f_j^* - f_{j(a)}\right)^p\right]^{\frac{1}{p}}
$$
\n(11)

where indicators $j = 1,2...$ *J*, $L_{p(a)} = L_p$ metric for imputation method a for the chosen value of parameter p , $f_{j(a)}$ = normalized value of indicator *j*, w_i = weight of performance indicator *j* got from the entropy method, $p =$ parameter (1 for linear,

2 for Euclidean distance measure), and for this study we adopted the *p* value of 2. Based on the minimum value of the L_p metrics, the imputation methods were ranked accordingly and the best method was proposed for each station. To decide independently of the views of the decision maker, normalizing and weighting of the performance indicators are required. The entropy method is used to normalize and estimate the weight of various criteria from the given payoff matrix (Pomerol and Barba-Romero [2000,](#page-19-12) Raju and Kumar [2014;](#page-19-16) Zhu et al. [2020](#page-20-2)). First, the performance indexes are standardized and the payof matrix (P_{ii}) is calculated using Eq. (12) (Zhu et al. [2020](#page-20-2)):

$$
P_{ij} = \frac{P_{ij}}{\sum P_{ij}}\tag{12}
$$

For a given normalized payoff matrix p_{ij} , an entropy E_i is calculated using Eq. ([13\)](#page-7-1) for a set of alternative criterion (*j*):

$$
E_j = \frac{1}{\ln(N)} \sum_{i=1}^{N} p_{ij} \ln(p_{ij}) \text{for } j = 1, \dots J \tag{13}
$$

where *N* is the number of imputation techniques and *j* is the number of indicators. Degree of diversifcation of the information provided by the outcomes of criterion *j* was calculated by Eq. ([14\)](#page-7-2):

$$
D_j = 1 - E_j \text{for } j = 1, ..., J \tag{14}
$$

Then fnally, the normalized weights of indicators calculated by Eq. (15) (15) (15) :

$$
w_j = \frac{D_j}{\sum_{i=1}^J D_j} \tag{15}
$$

2.8 Data quality check

2.8.1 Homogeneity test

In order to conduct reliable studies on climate variability, good quality and long-term datasets are required. Actually, many studies have confrmed that climate change analyses are not possible without a clear understanding of the homogeneity of data. There is an assumption that the climate record is considered homogeneous when its variations are caused only by changes in weather and climate (Caloiero et al. [2020](#page-18-30); Kocsis et al. [2020](#page-18-31); Patakamuri et al. [2020\)](#page-19-27). However, there are non-climatic factors that make the magnitude of climate signals larger than the actual (Caloiero et al. [2020\)](#page-18-30).

The following are the four test techniques that were chosen to assess the time series departure from homogeneity: the standard normal homogeneity test (SNHT), which is sensitive to detecting the breaks near the beginning and end of the data (Alexandersson [1986](#page-17-8)), Buishand's range test (BRT) (Buishand [1982](#page-18-32)), and the Pettit test (Pettitt [1979\)](#page-19-28), are sensitive to locating the breaks in the middle of the series, and the Von Neumann range test (VNRT) do not located the break (Von Neumann [1941\)](#page-19-29). But, if there is a break in the data, the test statistics is less than two, and if not, the test statistics is equal to two. Generally, the frst three tests can locate the year of break that is likely to occur. The Pettitt test, unlike the SNHT and the Buishand's range test, does not assume that Xi values are regularly distributed. Since the Pettitt test is based on the rankings of the elements of a series rather than on the values themselves, such an assumption is not required. All tests are executed under the null hypothesis that annual values *Xi* of the testing variable *X* are independent and identically distributed. The alternative (Ha) hypothesis for NSHT, BRT, and PTT is a step-wise shift in the mean of the data. However, the alternative hypothesis for VNRT assumes that the time series data is not randomly distributed. All these tests were conducted using XLSTAT 2020. Then fnally, the test results have been summarized by Wijngaard et al. [\(2003](#page-19-30)) as useful (when the test has rejected none or one null hypothesis out of four tests), doubtful (when the test has rejected two null hypotheses out of four tests), and suspect (when the test has rejected three or all null hypotheses out of four tests).

2.8.2 Trend analysis of future climate conditions

The Mann–Kendall trend (MK) test is a non-parametric test which is used to determine the presence or absence of mnotonic trends in time series data of a candidate station (Kocsis et al. [2020](#page-18-31); Shahfahad et al. [2022](#page-19-31)). The null hypothesis (Ho) of MK is that there is no trend, and the alternative hypothesis (Ha) is that the time series of a candidate station follows a monotonic trend over time. The Mann–Kendall test statistic is calculated by Eq. (16) (16) :

$$
S = \sum_{i=1}^{n-1} * \sum_{j=i+1}^{n} sign(X_j - X_i)
$$
 (16)

where X_i and X_j are the sequential data in the series and *n* is the size of the data series.

j>I and *i* = 1, 2, 3,..., *n*⁻¹ k = 2, 3, 4,..., *n*, and *n* is the number of data sign $(X_j - X_i)$ is calculated by Eq. [\(17\)](#page-7-5):

$$
sign(X_j - X_i) = \begin{cases} +1if(X_j - X_i) > 0\\ 0if(X_j - X_i) = 0\\ -1if(X_j - X_i) < 0 \end{cases}
$$
(17)

The variance *S* is calculated by Eq. [\(18](#page-7-6)):

$$
var(S) = \frac{S(n-1)(2n+5) - \sum_{p=1}^{q} t_p(t_p - 1)(2t_p + 5)}{18}
$$
 (18)

where

- t_p is the number of data in the *p*th tied group,
- *n* is the total number of data in the time series.

A positive value of *S* indicates that an increasing and negative value of *S* is decreasing trend of time series data of the candidate station.

The standardized Mann–Kendall test statistics is calcu lated by Eq. (19) (19) (19) :

$$
Z = \begin{cases} \frac{S-1}{\sqrt{var(S)}} \, \text{if } S > 0\\ 0 \, \text{if } S = 0\\ \frac{S+1}{\sqrt{var(S)}} \, \text{if } S < 0 \end{cases} \tag{19}
$$

3 Results

3.1 Performance of missing estimation methods

In the previous part, various strategies and their comparative methodologies were already covered in order to choose the best imputation technique. Approaches to missing estima tions, methods of evaluating their performance, and tech niques to identify the best method were discussed in Sect. 2. In this section, the fndings of comparative techniques for identifying station-wise suitable methods are discussed. The ability of each missing estimation technique was evaluated using the statistical metrics of RMSE, NSE, and PBIAS. Tables [1](#page-3-0) and [2](#page-8-1) show the performances of each missing method at a 20- and 40-km radius of infuence and at dif ferent levels of missing percentage. The MLR and MICE methods gave the best results for all statistical performance measures across all stations. Alternatively, the modifed inverse distance method (IDW $M_{E\&D}$) presented lower values of RMSE and PBIAS and a higher value of NSE. On the contrary, for all target stations and missing percentage combinations, the CCWM approach performed the worst in terms of percent bias. Stations within a 20-km radius of infuence produce less RMSE and PBIAS and a higher NSE than stations within a 40-km radius of infuence. However, the radius infuences have no signifcant impact on the per formance of missing imputation methods. The CCWM, normal IDWM, and modifed versions of IDWM such as IDWM_{C&D}, IDWM_{E&D at $k = 1$, and IDWM_{E&D2 at $k = 2$ pre-}} sented higher biases in RMSE and PBIAS and lower NSE (Fig. [3a](#page-9-0)–c). The estimation approaches showed an increase in RMSE and PBIAS, as well as a decrease in NSE, when **E** $\int_{\sqrt{\text{mrt}(S)}}^{\sqrt{\text{sin}(S)}} f/S > 0$ (19) $0/f/S = 0$ (19) $\frac{0}{\sqrt{\text{mrt}(S)}} f/S < 0$
 3.1 Performance of missing estimation methods

In the previous part, various strategies and their comparative

methodologies were already c

all stations considered in this study. Considering the spatial missing estimation techniques such as $IDWM_{C&D}$, IDWM_{E&D at $k = 1$, and IDWM_{E&D2 at $k = 2$, modified based}} on correlation coefficient, spatial distance and elevation difference are better performed than the normal IDWM and CCWM in terms of RMSR, PBIAS, and NSE with respect to missing value percentages. The inclusion of the correlation coefficient into normal IDWM and modified IDWM $_{C\&D}$ signifcantly decreased the error PBAS increase; however, do not apply for RMSE (Fig. [3b](#page-9-0)). Comparing the eight methods, the MLR, MICE, and IDWM_{E&D3} performed best over most stations at all levels of missing percentages.

3.2 Impacts of elevation diference, radius of infuence and exponent value "k"

The normal inverse distance weighted method (IDWM) is modified by the inclusion of the elevation difference between the target and neighboring stations and the exponent value of "*k*," for distances that range from 1 to 3. As shown in Table [3,](#page-10-0) the inclusion of an elevation difference and gradually increasing the exponent values for distance signifcantly lowered the error in terms of RMSE and PBIAS and increased the NSE of the inverse distance weighted method. The inclusion of an elevation diference between the stations signifcantly increased the performance of normal IDWM. For example, the comparison between IDWM and the modified version IDWM_{E&D for $k = 1$ has} shown that the RMSE is reduced from 1.52 (IDWM) to 0.74 (IDWM_{E&D for $k = 1$), the PBIAS is reduced from 43.6} (IDWM) to 20.19 (IDWM_{E&D for $k = 1$), and the NSE is} increased from−1.31 (IDWM) to 0.45 (IDWME&D for *k* = 1) at 5% of the missing percentage and a 20-km radius of infuence for Arata station.

The other value added for IDWM is the value of the exponent for the Euclidian distance between the target and neighboring stations. Gradually increasing the exponent value from 1 to 3 increases the performance of IDWM. For exponent values of $k=1$ and $k=3$, the performance of the models was signifcantly improved (see Table [3](#page-10-0) as an example for the Arata station and the Appendix B for all stations). For example, at 10% of missing value the RMSE and PBIAS were reduced from 1.79 for (IDWM) to 0.5 (for IDWM_{E&D for $k = 3$) and 68.53 (IDWM) to 11.62 (for} IDWM_{E&D for $k = 3$), respectively. Even at the maximum} missing percentage (25%), the RMSE and PBIAS range from 3.75 to 42.92 and 234.74 to 239.20 for IDWM at 20 and 40-km radius of infuence. These errors were reduced for the same condition (25% missing value and radius of infuence) from 0.75 and 29.89 to 30.40, respectively, for IDWM_{E&D for $k = 3$. The modification of IDWM by inclusion} elevation difference and $k=3$ significantly reduced the errors

Fig. 3 Results of performance measures for the missing value estimation techniques applied to estimate 5, 10, 15, 20, and 25% missing values. RMSE (a), PBAS (b), and NSE (c) for Arata station in Katar subbasin

and increase the goodness of ft. Generally, accounting for the elevation diference and increasing the exponent value "*^k*=3" can increase the performance of the inverse distance weighted method by lowering the error of RSR and PBIAS and increasing the precision (NSE). However, as the assess ment results have been shown in Table [3](#page-10-0) and Appendix, both radiuses of infuence have no signifcant diference between the IDWM and its version. Therefore, similar results were obtained for other stations that are considered in this study (the results summarized in Appendix B).

3.3 Impact of missing percentage

As shown in Tables [2](#page-8-1) and [4](#page-11-0) for the Arata station and in Appendix A for the rest of the stations, the performance of the missing estimation method has decreased as the missing percentage has increased over all stations. The MLR, MICE, and IDWM_{E&D3} at $k=3$ performed very well for most stations at all levels of missing percentages compared to other miss ing estimation techniques. For example, the IDWM method presented the poorest performance for Arata station, which resulted in 16.68 RMSE , 239 PBIAS, and 13 NS_{E} . Similarly, for the rest stations, as long as the missing percentages are increasing, the model performance tends to decrease to accurately estimate the missed values of the target station (Appendix A).

3.4 Identifying of the best method

To identify the best inflling technique, the multicriteria decision with compromise programming (CP) method was used. Here, the result for Arata station has been shown for demonstration. Among the three performance indicators, PBIAS (0.498) has a signifcant weight in the ranking of the missing estimation methods, followed by RMSE (0.421) and NS_E (0.08). Equations ([11\)](#page-6-3)–([15](#page-7-0)) were coded in Excel 2016, and the entropy, degree of diversifcation, normalized weight, payoff matrix (Pij) , and L_p metrics were calculated subsequently. Then, based on the minimum values of L_p metrics, each missing estimation method was ranked. As the results in Tables [5](#page-11-1) and [6](#page-12-0) showed for Arata station, the MLR, MICE, and IDWM_{E&D3 at $k=3$ were ranked as the 1st,} 2nd, and 3rd best methods, respectively. The normal IDWM and CCWM are ranked 7th and 8th, respectively. Similarly, for the rest stations, the results of the best of three methods are summarized in Appendix A.

3.5 Quality assessment for precipitation data

3.5.1 Statistical characteristics of precipitation

The long-term mean and maximum monthly observed rainfall in the Katar subbasin varied from 58.24 to 87 mm **Table 4** Impact of the exponent value of "*k*" on the spatial distance of the inverse distance weighted method for Arata station

Performance evaluation based on root mean square error (RMSE)								
Missing percentage	IDWM		IDWM _{E&D} ^{k} for $k = 1$		IDWM _{E&D} ^k for $k=2$		IDW $M_{E&D}^k$ for $k=3$	
	Radius of influence							
	$20 \mathrm{km}$	40 km	$20 \mathrm{km}$	40 km	$20 \mathrm{km}$	40 km	$20 \mathrm{km}$	$40 \mathrm{km}$
5	1.52	1.55	0.74	0.77	0.37	0.38	0.30	0.30
10	1.79	1.83	0.92	0.96	0.55	0.56	0.49	0.50
15	3.08	3.14	1.56	1.62	0.86	0.88	0.74	0.74
20	3.28	3.34	1.51	1.59	0.64	0.67	0.48	0.48
25	3.75	42.92	1.76	1.84	0.87	0.90	0.75	0.75
Nash Sutcliffe efficiency (NSE)								
5	-1.31	-1.39	0.45	0.40		0.85	0.91	0.91
10	-2.22	-2.33	0.15	0.09	0.70	0.69	0.76	0.75
15	-8.51	-8.83	-1.44	-1.64	0.26	0.22	0.46	0.45
20	-9.75	-10.17	-1.28	-1.51	0.59	0.55	0.77	0.77
25	-13.09	-13.61	-2.09	-2.38	0.24	0.20	0.44	0.44
Percent of bias (PBIAS)								
5	43.60	44.42	20.19	21.18	8.07	8.44	5.24	5.34
10	68.53	69.91	33.59	35.18	15.63	16.23	11.46	11.62
15	161.68	164.64	79.27	82.81	36.77	38.10	26.89	27.23
20	186.67	190.46	84.01	88.51	30.92	32.61	18.53	18.97
25	234.74	239.20	109.59	114.92	44.95	46.95	29.89	30.40

and 230.6 to 581 mm, and for the Meki subbasin, they varied from 60 to 85.63 mm and 292.3 to 489.3 mm, respectively. The standard deviation (SD) varied from 57 to 94.33, and the coefficient of variation (CV) varied from 84.69 to 108.42% for the Katar subbasin. Similarly, for the Meki subbasin, SD and CV varied from 62 to 86.23 and 97.32 to 119.01%, respectively. This demonstrated that there was signifcant temporal variability in monthly rainfall from 1997 to 2017 in both subbasins. The greatest variability was observed at the Adami, Tulu, and Iteya stations (Table [7](#page-12-1)).

3.5.2 Homogeneity tests

An absolute homogeneity test was applied using SNHT, Buishand's, Pettitt, and Von Neumann tests to check whether the long-term climatological data belongs to the same population with no temporal variation. If any change in the time series was only attributed to a natural occurrence. Based on the hypothesis test for homogeneity, the empirically calculated *p*-value is at 95% of the significant level summarized in Tables [8](#page-12-2) and [9](#page-12-2) for the Katar and Meki subbasins, respectively. Based on the test results, seven stations were homogeneous in the Katar watershed based on the above four tests. However, one station, Iteya, was nonhomogeneous based only on Buishand's test. Similarly, for stations in the Meki watershed, homogeneity tests were conducted (Table [8\)](#page-12-2). Except for Butajera station, all stations were homogeneous based on the test results of the SNHT, Buishand's, Pettit, and Von Neumann tests at 95% of the significant level (Table [9](#page-13-0)). An extensive examination was carried out on the metadata and archive information concerning the history of the

Table 6 Multi-criteria decision method for Arata Station compromise programming within a 20-km radius of infuence

Table 7 Monthly rainfall statistics for 16 stations from 1983 to 2017 after missing data have been flled

SD is standard deviation and CV is coefficient of variation

Table 8 Calculated *P*-values for homogeneity testes at alpha (α) =0.05 for Ketar sub basin and decision made based on Wijngaard et al. ([2003\)](#page-19-30)

measurements for both stations. No apparent explanation could be found for the causes of the changes. Based on Wijngaard et al. ([2003](#page-19-30)) classification for homogeneity, 15 stations were classified as useful, and only Butajera stations were suspected.

3.6 Trend analysis

Each chosen station has 17 series (12 months, four seasons, and an annual series), for a total of 255 time series data from 15 meteorological stations. Monthly, seasonal, and annual monotonic upward or downward trends in rainfall were assessed for each station independently using the Mann–Kendall trend test, and the magnitude of the trend was estimated using the Sone's slope for the time series data of 1997–2017.

3.6.1 Monthly trend analysis

As shown in Table [10,](#page-14-0) the rainfall had a combination of increasing and decreasing trends at all stations. There was a statistically significant decreasing trend for Dagaga station for the month of January, with a magnitude of 1.52 mm/month. For Iteya station, the rainfall amount shows a decreasing trend for the months of June, August, and October with a magnitude of 2.15, 5.05, and 3.06 mm, respectively. At Kulumsa station, there was a significant increasing trend in rainfall for the months of May and September, with a magnitude of 4.38 and 3.13 mm, respectively. Similarly, Bui station showed a statistically significant decreasing trend with a magnitude of 0.83 mm. At Butajera station for the months of March, April, August, and October, there was a significant decreasing trend with a magnitude of 6.82, 4.54, 5.7, and 4.07 mm, respectively. For Ejerese-lele station, there was a significant increase in monthly rainfall during September, with a magnitude of 2.63 mm. However, the rest station has shown no statistically significant increasing or decreasing trends in monthly rainfall.

3.6.2 Seasonal and annual trend analysis

Seasonal trend analysis was performed and considered the sum of three consecutive months, such as spring (March, April, and May), summer (June, July, and August), autumn (September, October, and November), and winter (December, January, and February). An annual trend analysis was performed for a time series of rainfall data from 1997 to 2017. As a trend, the results of the analysis are stated in Table [11,](#page-15-0) both increasing (positive) and decreasing (negative) in seasonal and annual rainfall. A decreasing trend in seasonal rainfall was observed for Iteya station during summer (10.65 mm) and autumn (11.48 mm). The Dagaga station had a statistically signifcant decrease in seasonal rainfall during the autumn (6.41 mm). Similarly, Butajera showed a signifcant decreasing trend during spring (14.75 mm) and autumn (9.9 mm). The annual trend analysis resulted in increasing and decreasing trends in the annual rainfall series. Iteya and Butajera stations have shown statistically signifcant decreasing trends with a magnitude of 34.84 mm/year and 40.36 mm/year, respectively. The homogeneity test station at Butajera exhibited suspected result. The non-homogenies of the results may be afecting the trend result and it needs further analysis by considering long data series.

4 Discussion

Accurate and reliable precipitation data helps in assessing the availability and distribution of water resources, which is crucial for managing irrigation systems and ensuring sustainable agricultural practices. It also aids in predicting and preparing for extreme weather events such as droughts or heavy rainfall, allowing for timely emergency response measures to be implemented. Missing data is a problem for all. The most common reasons for missing data are equipment malfunctions, human error, or data transmission issues. The main effects of missing data are to reduce the power and precision of statistical analysis results, lead to a biased estimate, and draw the wrong conclusion about the relationship

Table 9 Calculated *P*-values for homogeneity tested methods at alpha (α) = 0.05 for Meki sub basin and decision made based on Wijngaard et al. ([2003\)](#page-19-30)

* represents signifcant at 95% confdence level with the corresponding critical value of 1.96

between two or more variables. Therefore, it is crucial to address and properly handle missing data in order to ensure the accuracy and reliability of hydrometeorological analyses and predictions. To bridge this gap, missing data can be flled using diferent techniques depending on the characteristics of a particular geographic location, and the missing data mechanism and, fnally, the quality of the data should be checked before being used for the intended purposes.

In this study, the outcomes of eight missing estimation methods, such as normal IDWM and its modified versions of IDWM_{C&D}, IDWM_{E&D for $k = 1$, IDWM_{E&D for $k = 2$,}} IDWM_{E&D for $k = 3$, CCWM, MLR, and MICE, were assessed} for inflling missing monthly rainfall records in the Katar and Meki subbasins. Their performances were evaluated using three widely used error metrics, such as RMSE, PBAIS, and goodness of ft tests (NSE) at two radiuses of infuence and diferent levels of missing percentage. The outcome of the study has presented here based on level of missing percentage, radius of infuence, and elevation diference between target and neighboring stations.

The percentage of missing values signifcantly increases the error metrics of RMSE and PBIAS and decreases the ft test at all stations considered in this study. The performance of the missing estimation method has decreased as the missing percentage has increased over all stations. The MLR, MICE, and IDWME_{&D for $k = 3$ performed very well} for most stations at all levels of missing percentages compared to other missing estimation techniques. The computed values of error for the IDWM method presented the poorest performance for Arata station, which resulted in 16.68% RMSE, 239% PBIAS, and -ve13.61 NSE Table [4.](#page-11-0) These values indicate that the normal IDWM method was not able

Table 11 Seasonal and annual rainfall trend analysis for the Katar and Meki watersheds

* represents signifcant at 95% confdence level with the corresponding critical value of 1.96

to accurately estimate missing data for target (Arata) station compared to the modifed IDWM based on the distance and elevation diference between the target and neighboring stations.

The rest station in Appendix A yielded similar fndings, indicating consistency in the results. The performance of each missing estimation technique was reduced as the missing percentage increased. These studies also found similar results, indicating a consensus among researchers (Schnei-der, [2001;](#page-19-32) El Kasri et al. [2018\)](#page-18-5). This suggests that the missing estimation methods are not robust enough to handle a high percentage of missing values. It is crucial to develop more advanced techniques that can efectively handle missing data in order to improve the performance of these estimation methods. This is because missing data can introduce bias and reduce the representativeness of the sample. Additionally, the larger the percentage of missing data, the greater the potential for imprecise estimates and decreased statistical power, making it more challenging to draw accurate conclusions from the analysis (Pigott 201; Piazza [2011](#page-19-0); Houari et al. [2014](#page-18-0); Schmitt et al. [2015;](#page-19-1) Sanusi et al. [2017](#page-19-33); Gao et al. [2018](#page-18-1)). This may result in uncertain flood estimates and imperfect food management decisions and intervention mechanisms (Ekeu-Wei et al. [2018\)](#page-18-2).

The inverse distance-weighted method was modifed by including the elevation diference between the target and neighboring stations and gradually increasing the *k* exponent for distance. As the studies indicated, topography is one of the factors that afect the characteristics of rainfall (Duckstein et al. [1973](#page-18-33)). In the study region, topography and direction of the rainfall play a signifcant role in the rainfall amount and characteristics. Additionally, the direction of rainfall (windward and leeward) and microclimate in the study region signifcantly afect the rainfall amount and characteristics. For example, Asella and Bui stations are found at altitudes of 2400 and 2000 m in the opposite direction of rainfall (Asella is on the leeward side and Bui station is on the windward side), and the rainfall characteristics are almost similar (Table [1\)](#page-3-0). Therefore, the inclusion of an elevation diference between target and neighboring stations signifcantly reduces error in terms of RMSE and PBIAS compared to the normal IDWM and modifed version of IDWM (IDWME&D for $k = 1$, IDWME&D for $k = 2$, and IDWME&D for $k=3$). Figure [4](#page-15-1) shows that the RMSE reduced as the elevation diference was considered and the

Fig. 4 Performance evaluation based on RMSR and distance and elevation diference between the target and neighboring stations. MD is missing data percentage

exponent (*k*) for distance gradually increased from 1 to 3. Similarly, Fig. [5](#page-16-0) displays that the error term of PBIAS is decreasing, as is the inclusion of elevation diference and the gradual increase in exponent values for distance for the inverse distance-weighted method at all levels of missing percentages.

The CP method allows for the consideration of multiple criteria simultaneously, enabling a comprehensive evaluation of diferent inflling techniques. By using this method, the study aimed to determine the best inflling technique that would provide the most optimal results of missing value of the target station. Here, the result for Arata station has been shown for demonstration. Among the three performance indicators, PBIAS (0.498) has a signifcant weight in the ranking of the missing estimation methods, followed by RMSE (0.421) and NSE (0.08) . Equations (11) (11) (11) – (15) (15) were coded in Excel 2016, and the entropy, degree of diversifcation, normalized weight, payoff matrix (Pij), and LP metrics were calculated subsequently. Then, based on the minimum values of LP metrics, each missing estimation method was ranked, and MLR, MICE, and IDWM_{E&D for $k = 3$ are ranked} as 1st to 3rd, respectively, over most stations. The normal IDWM and CCWM are ranked 7th and 8th, respectively; Table [5](#page-11-1) for 40-km and Table [6](#page-12-0) for 20-k radius of infuences, respectively. Similarly, for the rest stations, the results of the best of the three methods are summarized in Appendix B. A similar study has been conducted by Radi et al. [\(2015](#page-19-7)) on the performance of missing estimation methods and utilized ANOVA to determine the most efective approach. Similarly, Raju et al. ([2016](#page-19-26)) employed the compromise programing method to assess and choose the optimal global climate models specifcally for India's climate conditions.

Then, after evaluating the missing estimation method and identifying the best for each station, the missing value is flled for each station using their best method. The absolute

Fig. 5 Performance evaluation based on PBIAS and distance and elevation diference between the target and neighboring stations. MD is missing data percentage

homogeneity (SNHT), Buishand's, Pettit's, and Von Neumann's tests were used in the quality assessment for rainfall to determine whether the long-term climatological data belong to the same population with no temporal variation. Only one station (Iteya) passed Buishand's test as being nonhomogeneous, leaving out the other two stations. At the 95% level of signifcance, the results of the SNHT, Buishand's, Pettit's, and Von Neumann's tests revealed that all stations at one station (Butajera) were homogeneous. The quality assessment for rainfall was applied using absolute homogeneity (SNHT), Buishand's, Pettit's, and Von Neumann's tests to check whether the longterm climatological data belong to the same population with no temporal variation. Except for two stations, Iteya and Butajera stations, all stations were homogeneous based on the test results of SNHT, Buishand's, Pettit's, and Von Neumann's tests at 95% of the signifcant level (Tables [8](#page-12-2) and [9](#page-13-0)). The meta-data and archive information pertaining to the history of measurements for both stations were thoroughly examined, and no apparent explanation could be found for the causes of the changes. Based on Wijngaard et al.'s ([2003](#page-19-30)) classifcation for homogeneity, 15 stations were classifed as useful, and only one (Butajera) station was classifed as suspected. Similar studies were conducted by Schönwiese and Rapp ([1997](#page-19-34)) and Patakamuri et al. [\(2020](#page-19-27)) and classifed the station using the Winjngaard procedure.

Then, after the homogeneity test, trend analysis was employed for each selected station. The Mann–Kendall trend (MK) test, a popular non-parametric test, was applied to determine the presence or absence of monotonic trends in the time series data of each candidate station (Machiwal and Jha [2012](#page-18-34); Kocsis et al. [2020](#page-18-31); Shahfahad et al. [2022\)](#page-19-31) and the magnitude of the change is estimated using Son's slope. The trend analysis results are summarized in Tables [10](#page-14-0) and [11](#page-15-0) for monthly, seasonal, and annual time series from 1997 to 2017. The trend analysis results show statistically signifcant decreasing and increasing trends in the monthly rainfall over some stations. The annual trend analysis of Iteya station in Katar subbasin and Butajera station in Meki subbasin shows signifcant decreasing by 34.84 and 40.4 mm, respectively. The trends in these two stations also refect seasonality. These two locations are highly productive rainfed agricultural areas on which the Ethiopian economy is primarily dependent (Welteji [2018](#page-19-35)) and high potential areas for runoff generation and water yield in the subbasins (Balcha et al. [2022\)](#page-17-9). The study agrees with past studies conducted in the subbasin (Kassie et al. [2014](#page-18-35)) and elsewhere in Ethiopia (Bedane et al. [2022](#page-17-10); Ware et al. [2023\)](#page-19-36).

5 Conclusion and recommendation

The missing values can lead to inaccurate calculations and interpretations, as well as hinder the ability to identify patterns or trends in rainfall patterns. This can be overcome

through the use of imputation techniques. However, the efectiveness of any imputation technique depends largely on the climatology of the area, the density of the rain gauge network, and the geographical location, among other factors. Thus, it is imperative to assess the performance of various imputation methods to determine the best ones to use for a specifc area of interest. By evaluating the performance of diferent imputation methods, researchers can determine techniques most suitable for a study area. This assessment ensures that the chosen imputation methods effectively compensate for missing rainfall data without distorting patterns or trends, enabling accurate analysis and prediction of rainfall patterns in the area of interest. Instead of applying one ft for all strategy for estimating the missed value of rainfall, we evaluated the performance of 8 missing estimation techniques using RMSE, PBIAS, and NSE and apply a MCDM of compromise programing methods to select the best missing estimation technique. In general, the error statistics (RMSE and PBIAS) were relatively high, with poor goodness of ft (NSE) for IDWM and CCWM. However, MLR, MICE, and IDWME&D for *k*=3 performed better for all the percentages of missingness examined. We therefore recommend using MLR, MICE, and IDWME&D for $k=3$ to treat missing historical rainfall data in the Katar and Meki subbasins and probably the whole of the Rift Valley Lakes Basin. The methodology we applied in this study may help the researchers working in similar type of study. Nowadays, it is very common to evaluate the performance of missing estimation techniques using diferent statistical metrics. However, it is not common to use MCDM to select the best methods in climatology. By utilizing the multi-criteria decision method in our study, we have provided a novel approach to selecting the best missing imputation techniques. This methodology can potentially enhance the accuracy and reliability of future research in this feld, benefting other researchers seeking to explore similar areas of study. More than 21 missing estimation techniques are available in the literature. The study's limitation is that it does not account for all missing estimation techniques, and the evaluation metrics are also not limited to those used in this study. Future studies should also explore the impact of diferent missing estimation techniques and apply other MCDM to select the best imputation techniques.

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Data availability All datasets, raw or preprocessed, are available upon request from the corresponding author. However, permission is required for observed data collected from National Meteorology Agency of Ethiopia.

Declarations

Consent to participate Not applicable.

Consent for publication Not applicable**.**

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