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Controlling Borehole Geometry as a Feasible Strategy for Optimization of Heat Extraction in Geothermal Systems

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Abstract

Optimizing the heat extraction performance of geothermal systems is a long-standing issue in the study of geothermal energy. Besides the heat extraction in fractured hot rock, minimizing the heat loss during water fowback through boreholes is also critical for the system performance. Here, we conducted a series of experimental and numerical studies to understand the controlling factors of heat extraction rate and efficiency and to explore practical approaches for the optimization of heat extraction performance in a geothermal borehole. We performed water fow experiments to observe the heat extraction from neighboring hot granite and reproduced the heat extraction process using a three-dimensional water fow model. Our results show that the heat extraction rate frst increases with a higher fow rate to the maximum value and then decreases with a further rise in flow rate. The heat extraction efficiency decreases constantly with a higher flow rate. To improve the heat extraction performance with both the heat extraction rate and efficiency approaching the maximum values, we scaled up the laboratory-scale borehole and found that the heat extraction performance is enhanced with a triangular zone of heat extraction and a reduced zone of low-temperature water along a feld-scale borehole. We fnally discovered that a proper control of borehole geometry, such as section diameters along a multi-section borehole and bending angle of borehole trajectory, is a feasible strategy to modulate the heat extraction performance in a geothermal borehole and to replenish the heat loss during water flowback.

Highlights

- Experimental and numerical studies are conducted to understand the controlling factors of heat extraction rate and efficiency.
- Heat extraction performance is enhanced with a triangular zone of heat extraction and a reduced zone of low-temperature water.
- Multi-section borehole is a feasible strategy to modulate the heat extraction performance in a geothermal borehole.
- Proper bending angle of borehole trajectory is another feasible strategy to optimize the heat extraction performance.

Keywords Geothermal energy · Heat extraction · Flow rate · Multi-section borehole · Borehole trajectory

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1 Introduction

Geothermal energy is the almost inexhaustible heat from the earth's interior and has substantial potential as a clean energy to reduce global carbon emissions (Barbier [2002](#page-10-0); Li et al. [2022](#page-11-0)). The heat extraction performance of geothermal systems relies primarily on the thermal properties of host rock (e.g., heat-producing granite) and the physical characteristics and operational parameters of working fuid (e.g., water and carbon dioxide). Extensive eforts have been

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made to improve the heat extraction performance, such as enhanced geothermal systems to create hydraulically fractured reservoirs (Li et al. [2021;](#page-11-1) Rathnaweera et al. [2020](#page-11-2)), advanced drilling technologies to access deeper and hotter geothermal sources (Ji et al. [2021;](#page-11-3) Rossi et al. [2020\)](#page-11-4), and novel exchanger designs to enable better heat transfer and energy conversion (Hu et al. [2022](#page-11-5); Liu et al. [2022](#page-11-6)). These eforts aim essentially to improve the amount of heat energy transferred to working fuid and to reduce the loss of heat energy due to the frictional, gravitational, and Joule–Thom-son effects (Phuoc et al. [2019](#page-11-7); Zhang et al. [2022](#page-11-8)), which are commonly known as heat extraction rate and efficiency, respectively.

Maximizing the heat extraction rate and efficiency is an ideal scenario to optimize the heat extraction performance of geothermal systems. Numerous studies have demonstrated dissimilar variations of heat extraction rate and efficiency under geological (e.g., heat distribution and conduction) and operational (e.g., fow rate and injection pressure) conditions. The heat extraction rate can be improved by appropriate coupling of thermo–hydro–mechanical processes (Pandey and Vishal 2017 ; Sun et al. 2021), efficient fluid flow and heat fow in fracture networks (Chen and Zhao [2020](#page-10-1); Xu et al. [2023\)](#page-11-11), and low-salinity working fuid (Borgia et al. [2012\)](#page-10-2), but cannot be increased constantly with a higher flow rate (Zhao et al. [2022\)](#page-11-12). The heat extraction efficiency has diferent quantitative indicators, showing diverse relationships with the geological and operational conditions. For instance, the energy efficiency defined as the ratio of produced thermal energy to consumed internal energy is correlated positively with fracture permeability and rock thermal conductivity and negatively with fow rate (Zeng et al. 2013). The heat extraction efficiency defined as the ratio of average outlet temperature to heat recovery factor increases with a higher injection pressure until reaching a specified limit (Sun et al. [2020](#page-11-14)). The heat extraction efficiency is also defned as the ratio of pump energy consumption rate to energy extraction rate and inversely proportional to in-situ stress (Shu et al. [2022](#page-11-15)). Hence, the heat extraction rate and efficiency assessed by various geological and operational factors can be complex and may vary in diferent manners. In engineering practice, the heat extraction rate and efficiency are critical for the thermal power output and the heat recovery effectiveness of geothermal systems, respectively (Li et al. [2023\)](#page-11-16). However, how to optimize the heat extraction performance remains a topic of debate, and what factors controlling the variations of heat extraction rate and efficiency are still unclear.

The objectives of this study include understanding the controlling factors of heat extraction rate and efficiency according to the experimental and numerical studies and exploring practical approaches to improve the feld-scale heat extraction performance based on the laboratory-scale fundamental studies. The study sheds light on the heat extraction while water fowing through the borehole. Meanwhile, the loss of geothermal heat extracted from fractured hot rock can be minimized and replenished during water flowback. We first conducted three suits of water flow experiments to observe the variation of water temperature in a laboratory-scale borehole under diferent combinations of surrounding temperature and fow rate. We then built a three-dimensional (3D) water fow model using COMSOL Multiphysics software to reproduce the experimental process and to evaluate the heat extraction rate and efficiency. We adopted simple and common defnitions of heat extraction rate and efficiency, which are the heat energy extracted by water per unit time and in relative to the heat energy removed from rock, respectively. We fnally extended the numerical model from laboratory scale to feld scale and discussed a feasible strategy by changing borehole geometry to improve the heat extraction performance of a geothermal borehole.

2 Methods

2.1 Experimental Method

We performed a series of water flow experiments through a drilled borehole to extract heat from surrounding hot rocks. Bukit Timah granite sourced from central Singapore was used as the rock medium. The medium-grained granite was composed of 62% feldspar, 32% quartz, 5% black mica, and 1% hornblende. The bulk density, porosity, Young's modulus, and intrinsic permeability of the granite were 2660 kg/ $m³$, 0.26%, 74 GPa, and 1.3 μ D, respectively. The thermal conductivity, specifc heat capacity, and thermal expansion coefficient of the granite were 3.5 W/(m K), 800 J/(kg K), and 7×10^{-6} K⁻¹, respectively. A granite core with a diameter of 50 mm was cut into two cylindrical specimens with a length of 100 mm using a diamond saw, and the specimen ends were ground within 0.02 mm fatness using sandpaper. A small borehole with a diameter of 6 mm was drilled along the specimen axis to facilitate water fow and heat extraction.

In the experimental setup, the drilled specimen was placed between two iron coreholders with internal waterpipes. Two fiberglass sheets were inserted between the specimen and the coreholders to minimize heat loss from the specimen ends. The specimen was sealed using a shrinkable plastic tube and fxed on the coreholders using a steel wire. The side wall of the sealed specimen was covered by a mica heater, which is capable of heating up to 250 °C and controlled by a closed-loop temperature controller with temperature fuctuation less than 1 °C. A Vindum pump was utilized to provide a continuous fow of distilled water and to monitor fow rate and water pressure. Five thermocouples

were used to measure water and granite temperatures: three thermocouples (A, B, and S) attached on the upper end of the specimen, the wall of the borehole, and the side wall of the specimen to monitor the temperature distribution over the cross-sectional area of the specimen, and two thermocouples (C and D) placed near the borehole ends to record the inflow and outflow temperatures of distilled water (Fig. [1](#page-2-0)). The thermocouples with a measurement accuracy of ± 1.5 °C were connected to a LabVIEW data acquisition system at a sampling rate of 10 Hz. An axial load of 1 kN was applied to fix the setup, and the room temperature was 22° C.

We conducted three suites of water flow experiments to investigate the heat extraction performance using distilled water at three flow rates $(5, 10, \text{ and } 15 \text{ ml/min})$ through the heated specimen at three surrounding temperatures of 80, 100, and 120 °C (Fig. [2\)](#page-2-1). The infow and outfow water pressures were 0.6 MPa and atmospheric, respectively. The experimental procedure included three sequential and three reverse-sequential steps. For the three sequential steps, the specimen was frst heated to a desired temperature, and distilled water was pumped into the borehole at a constant fow rate of 5 ml/min. The flow rate was kept for about 30 min to ensure the inflow and outflow temperatures stable. The flow rate was subsequently increased to 10 and 15 ml/min and kept for similar durations. After a 30-min break, the specimen temperature was recovered to the desired temperature. In the three reverse-sequential steps, distilled water was frst pumped into the borehole at a constant fow rate of 15 ml/ min for about 30 min, followed by pumping with fow rates of 10 and 5 ml/min and maintained for similar durations. The axial load, surrounding temperature, and flow rate were fxed during the experiments, and the infow and outfow temperatures were recorded by the data acquisition system.

Fig. 1 Schematic diagram of water flow experimental setup. Red dots indicate the locations of thermocouples

Fig. 2 Experimental procedure of water fow experiment. The surrounding temperatures used are 80, 100, and 120 ºC. The infow and outflow temperatures (not to scale) vary depending on the surrounding temperature and fow rate

2.2 Numerical Method

We built a 3D water flow model using COMSOL Multiphysics software to reproduce the heat extraction process. We assumed that the granite matrix was homogeneous, incompressible, and impermeable. Water fow was laminar within the borehole. The temperature distribution in water and granite was solved under a steady-state condition. The water flow model, as shown in Fig. [3a](#page-2-2), has the same dimension as the granite specimen used in the water fow experiment. The

Fig. 3 Laboratory-scale water fow model, including **a** model geometry and **b** model mesh

model was meshed with tetrahedral and hexahedral elements and with fner elements in and around the borehole (Fig. [3](#page-2-2)b).

In the model setup, the equations of energy conservation for water and rock were expressed according to the heat transfer equation (Jäckel et al. [2019\)](#page-11-17):

$$
\rho_w C_{pw} \frac{\partial T}{\partial t} + \rho_w C_{pw} \mathbf{u} \cdot \nabla T = -\nabla \cdot \left(k_w \nabla T \right) + Q \tag{1}
$$

$$
\rho_r C_{pr} \frac{\partial T}{\partial t} = -\nabla \cdot \left(k_r \nabla T \right) + Q \tag{2}
$$

where ρ_w and ρ_r [kg/m³] are the densities of water and rock, respectively, C_{pw} and C_{pr} [J/(kg·K)] are the specific heat capacities of water and rock, respectively, *T* [K] is the timedependent temperature field, t [s] is the elapsed time, \mathbf{u} [m/s] is the flow velocity vector of water, k_w and k_r [W/(m K)] are the thermal conductivities of water and rock, respectively, and *Q* [J] is the other forms of energy in the domain, including the viscous dissipation heating, the Joule heating, and the pressure work.

The momentum conservation is written according to the Navier–Stokes equation (Tritton [1977](#page-11-18)):

$$
\rho_w \frac{\partial \mathbf{u}}{\partial t} + \rho_w (\mathbf{u} \cdot \nabla \mathbf{u}) = -\nabla p + \mu \nabla^2 \mathbf{u} + \mathbf{F}
$$
(3)

where p [Pa] is the water pressure, μ [kg/(m s)] is the kinematic viscosity of water, and \mathbf{F} [N/m³] is the body force vector due to the gravity of water.

The continuity equation of mass conservation is (Tritton [1977](#page-11-18)):

$$
\frac{\partial \rho_w}{\partial t} + \nabla \cdot (\rho_w \mathbf{u}) = 0 \tag{4}
$$

For the boundary conditions, the upper and lower ends of the granite specimen were thermally insulated, and the temperature on the side wall was fxed between 60 and 200 °C.

The water infow velocity was associated with the fow rate in a range of 1–20 ml/min. The infow temperature was set as the room temperature (22 °C) to eliminate the infuence of uncontrollable infow temperature in the experimental study and to focus on the heat exchange at the rock–water interface. Following the experimental procedure, the infow and outfow pressures of water were 0.6 MPa and atmospheric, respectively.

3 Results

3.1 Experimental Results

The experimental results demonstrate changes in water and granite temperatures during the heat extraction process. As shown in Fig. [4](#page-3-0)a, taking 100 °C surrounding temperature as an example, the temperatures measured by the thermocouples A and S show that the granite temperature on the upper end of the specimen keeps roughly constant during the experiment, while the granite temperature on the inner wall of the borehole measured by the thermocouple B is reduced during the sequential and reverse-sequential steps and recovered between these steps. The sequential and reverse-sequential steps thus start on the same thermal condition, allowing us to compare the diferences between the infow and outflow temperatures in these steps. The granite temperatures obtained by averaging the data points in the sequential and reverse-sequential steps indicate the temperature reduction from the inner wall of the borehole to the side wall of the specimen (Fig. [4](#page-3-0)b). At diferent surrounding temperatures (i.e., 80, 100, and 120 °C), the temperature reductions of neighboring granite around the borehole are similar (e.g., between the thermocouples A and B). A higher surrounding temperature exhibits a larger temperature reduction near the side wall of the specimen (e.g., between the thermocouples A and S), implying that more heat is extracted by fowing

Fig. 4 a Temperature recovery between sequential and reversesequential steps at 100 °C surrounding temperature; the inset shows the specimen end with the locations of three thermocouples, and **b** temperature reductions from thermocouple S at 80, 100, and 120 °C surrounding temperatures to thermocouples A and B

water. In addition, the water temperatures measured by the thermocouple B are below 100 \degree C in these cases, indicating that water remains in the liquid phase.

The water temperatures at the lower and upper ends of the borehole are described as infow and outfow temperatures, respectively. Figure [5](#page-4-0) shows that the outfow temperature higher than the infow temperature demonstrates successful heat extraction from the heated granite. In the three suites of water fow experiments, both the infow and outfow temperatures increase with a higher surrounding temperature and decrease with a higher fow rate. Both the infow and outflow temperatures are relatively stable at a low surrounding temperature and become fuctuating at a high surrounding temperature. A high flow rate enhances the temperature fuctuation owing to a large variation of water temperature along the borehole. The infow and outfow temperatures are slightly diferent in the sequential and reverse-sequential steps likely due to diferent amounts of available heat after previous steps.

3.2 Numerical Results

Figure [6](#page-5-0) presents the validation of the numerical model by comparing the temperature diferences obtained from the experimental and numerical studies. The experimental temperature diference is calculated based on the average infow and outfow temperatures in the sequential and reverse-sequential steps. The error bar is plotted based on the standard error. The numerical temperature diference is obtained based on the fxed infow temperature and the

Fig. 5 Infow and outfow temperatures during water fow experiments with 5, 10, and 15 ml/min fow rates at **a** 80, **b** 100, and **c** 120 °C surrounding temperatures

Fig. 6 Temperature diference of infow and outfow temperatures between experimental (non-shadowed) and numerical (shadowed) results of water fow experiments with 5, 10, and 15 ml/min fow rates at 80, 100, and 120 °C surrounding temperatures

average outfow temperature. For the three surrounding temperatures, the temperature diferences at diferent fow rates from the numerical study are close to the experimental results and fall in the range of error bar. However, measuring the temperature differences is insufficient to evaluate the heat extraction performance from the heated granite.

The heat extraction process is associated with heat conduction in rock, heat advection in water, and heat convection at the rock–water interface (Pandey et al. [2018\)](#page-11-19). To quantify these characteristics involved in this process, we used the specifc enthalpy change of water Δ*h* [kJ/kg], the temperature loss of rock *D*, as well as the heat extraction rate *P* [W] and efficiency γ of rock–water interface, as follows:

$$
\Delta h = C_{pw}(T_{\text{out}} - T_{\text{in}}) \tag{5}
$$

$$
D = \frac{T_{r0} - T_{rt}}{T_{r0}} \times 100\%
$$
 (6)

$$
P = C_{pw} \rho_w q (T_{\text{out}} - T_{\text{in}}) \tag{7}
$$

$$
\gamma = \frac{T_{\text{out}} - T_{\text{in}}}{T_{r0} - T_{\text{in}}} \times 100\%
$$
\n(8)

where T_{out} [K] and T_{in} [K] are the outflow and inflow temperatures, respectively, T_{r0} and T_{rt} [K] are the initial temperature of rock and the fnal temperature at equilibrium, respectively, Δt is the unit time, and *q* [m³/s] is the volumetric flow rate of water.

As shown in Fig. [7,](#page-6-0) a change in specifc enthalpy of water refects the variations of internal energy and fow work (Wang et al. [2017\)](#page-11-20) and increases with a higher surrounding temperature and a lower flow rate. A larger difference of infow and outfow temperatures amplifes the specifc enthalpy change. A temperature loss of rock is resulted from the heat exchange at the rock–water interface and should not exceed 10% for sustainable heat extraction (Lei et al. [2020](#page-11-21)). A higher surrounding temperature and a larger flow rate lead to a greater rock temperature loss. A higher surrounding temperature causes increases in heat extraction rate and efficiency, which is consistent with the numerical results of full-scale geothermal systems (Sun et al. [2020](#page-11-14); Huang et al. [2023\)](#page-11-22). A larger flow rate induces a decrease in heat extraction efficiency. However, the heat extraction rate frst increases to the maximum value and then decreases with a further rise in flow rate. The reduction of heat extraction rate at a very high fow rate is unexpected, and similar results can be observed based on the net power of Davis and Michaelides ([2009](#page-10-3)) and the Carnot cycle power of Harris et al. [\(2021](#page-11-23)). The physical mechanism behind the reduction of heat extraction rate is likely associated with multiple geological and operational factors involved in the heat extraction process but remains largely unconstrained.

4 Discussion

Our results highlight diferent variations of heat extraction rate and efficiency as functions of surrounding temperature and flow rate. To optimize the heat extraction performance of geothermal systems, it is essential to understand the controlling factors for the variations of heat extraction rate and efficiency. Toward this end, a laboratory-scale borehole is insufficient to accommodate the fully heat extraction process, given the long heat exchange duration (Fig. [5\)](#page-4-0) and a desired high fow rate (Gan and Elsworth [2016\)](#page-10-4). Hence, we scaled up the numerical model by increasing specimen diameter, specimen length, and borehole diameter proportionally to 2.5, 5, and 0.3 m, respectively. We then piled up the amplifed models to form a feld-scale borehole with a length of 100 m (Fig. [8](#page-7-0)a). We considered a surrounding temperature of 150 \degree C and investigated the effect of flow rate (0.02–10 l/s) on the heat extraction process. The infow temperature and pressure of water remained 22 °C and 0.6 MPa, respectively, and the outflow pressure was atmospheric. Note that the feld-scale borehole represents a section of geothermal borehole with efective heat extraction, not a full-length borehole in geothermal systems.

The results of feld-scale water fow modeling, as shown in Fig. [9,](#page-8-0) exhibit the temperature distribution in water and rock below and above the dashed line, respectively, covering the zoom-in region in Fig. [8](#page-7-0)b. The distance from the

Fig. 7 Heat extraction characteristics, including water-specific enthalpy change, rock temperature loss, as well as heat extraction rate and efficiency, as a function of fow rate at surrounding temperatures of **a** 60, **b** 90, **c** 150, and **d** 200 °C

borehole axis is normalized by the model radius (1.25 m). After reaching temperature equilibrium in the model, both the temperatures of water and rock increase nonlinearly with a higher flow rate. The water temperature near the infow port rises slightly, indicating an unfavorable scenario for heat exchange (Mohammed [2009](#page-11-24)). The water temperature beyond the infow port distributes uniformly in the radial direction of the borehole, a favorable scenario for heat exchange, and increases notably in the longitudinal direction. The reduction of rock temperature initiates near the infow port and expands parallel and perpendicular to the borehole axis to form a heat exchange zone. With increasing fow rate, the shape of heat exchange zone changes from a triangle to a trapezoid. The triangular zone was also observed in previous studies (Gao and Shi [2021](#page-11-25); Kang et al. [2022](#page-11-26)). Our results reveal that the size and shape of heat exchange zone are related to the fow rate. At a low flow rate, a small size of triangular zone indicates that the effective heat exchange is limited near the infow port and the available heat around the 100 m borehole is largely unextracted (Fig. [9](#page-8-0)a and b). At a high flow rate, the heat exchange zone is extended into a trapezoidal shape, resulting in an insufficient heating of flowing water (Fig. [9](#page-8-0)e and f). Therefore, the heat extraction rate can be optimized at an intermediate fow rate when the maximum size of triangular zone is achieved (Fig. [9c](#page-8-0) and d). Meanwhile, the heat extraction efficiency decreases with a higher flow rate as indicated by an increasing size of low-temperature area (as indicated by the blue color) in the borehole, showing that the variation of heat extraction

Fig. 8 Field-scale water fow model, including **a** building up this model using laboratory-scale models and **b** highlighting temperature distribution in water and granite using color section

efficiency with increasing flow rate is different from that of heat extraction rate.

The maximum values of heat extraction rate and efficiency appear at diferent fow rates (Fig. [9a](#page-8-0) and d), indicating that the heat energy extracted by water per unit time and in relative to the total energy from rock cannot achieve the maximum values at the same time. A compromise solution for the improvement of heat extraction performance is to make the heat extraction rate approach the maximum value and to keep the heat extraction efficiency as high as possible at the corresponding flow rate. However, for a large diference of fow rates related to the maximum values of heat extraction rate and efficiency (e.g., 50 times in Fig. $9a$ and d), controlling fow rate may not lead to a satisfactory compromise solution in a geothermal borehole.

To address this challenge, we were inspired by section drilling, which means borehole drilling with multiple sections in a stepping-down mode (Hosein et al. [2019;](#page-11-27) Talalay and Hong [2021](#page-11-28)). Controlling the diameters of borehole sections can be an efective strategy to improve the heat extraction performance. For a single-section borehole with a diameter of 0.3 m and a length of 100 m, fowing water at a fxed rate of 1 l/s causes a trapezoidal zone (Fig. [10](#page-9-0)a), indicating insufficient water heating. We modified the borehole with five sections each with a length of 20 m and a diameter changing from 0.5 on the top to 0.3 m on the bottom with an interval of 0.05 m. Under the same geological and operational conditions (Fig. [9\)](#page-8-0), the heat exchange zone over the multi-section borehole becomes a triangular zone (Fig. [10b](#page-9-0)), meaning the improvement of heat extraction rate. The size of low-temperature area in the multi-section borehole representing inefective heat extraction is much smaller than that in the single-section borehole, showing the improvement of heat extraction efficiency. Controlling the diameters of borehole sections is thus proved as an efective strategy. Although the borehole diameters are determined by drill bits, the lengths of multiple sections can be controlled in the borehole design.

Another strategy of controlling borehole geometry to improve the heat extraction performance is changing the borehole trajectory, which was inspired by the heat transfer in ground heat exchangers using inclined boreholes (Cui et al. [2006;](#page-10-5) Marcotte and Pasquier [2009](#page-11-29)). We considered a single-section borehole with a diameter of 0.3 m and a length of 100 m containing fowing water at a fxed rate of 1 l/s. As shown in Fig. [11](#page-10-6), we locked the upper half of the borehole vertically and bent the lower half from a sub-vertical angle (15°) to a horizontal angle (90°) . The two halves were connected by a short arc section with a radius of 1.5 m, which was insignificant to affect the heat extraction performance. The results show that the heat exchange zone along the borehole expands in a triangle zone when the lower half deviates from 15° to 30° and becomes a trapezoidal zone at 45°. The heat exchange zone reduces to a triangle zone at 60° and shrinks until 90°. The variation of heat exchange zone indicates that a bending angle in a range of 30–60° is suitable to promote the heat extraction performance along the borehole. For a bending angle close to 45°, the formation of triangle zone can be obtained by reducing flow rate (Fig. [9\)](#page-8-0) and by changing borehole diameter (Fig. [10\)](#page-9-0). Our study suggests that borehole geometry, including borehole trajectory and cross-section area, can be controlled to enhance the heat extraction in a geothermal borehole.

5 Conclusions

This study reports a series of experimental and numerical studies to understand the controlling factors of heat extraction rate and efficiency and to explore practical approaches for the improvement of heat extraction performance in a geothermal borehole. Our results show dissimilar variations of heat extraction rate and efficiency as a function of flow rate. In this case, a simple compromise solution with

Fig. 9 At a surrounding temperature of 150 °C, temperature distribution of water and rock (below and above the dashed line) as a function of fow rate. The vertical axis is normalized by the model radius

Fig. 10 Temperature distribution in water and rock over **a** a single-section borehole and **b** a multi-section borehole. The number on the left side indicates the borehole diameter

the heat extraction rate approaching the maximum value and the heat extraction efficiency kept as high as possible at the corresponding fow rate may not be feasible, particularly for the case with a large diference of fow rates related to the maximum values of heat extraction rate and efficiency. The study proposes and verifies the modification of borehole geometry to modulate the heat extraction performance in a geothermal borehole. Proper controls of section diameters along a multi-section borehole and bending angle of borehole trajectory can produce a triangular

zone of heat extraction and a reduced zone of low-temperature water along the borehole, which are key fndings to ensure the optimization of heat extraction performance. These fndings can be considered in the design of geothermal systems to minimize the heat loss during water fowback. The study also inspires us to jointly consider other geological and operational factors (e.g., fracture network and fuid viscosity) to further improve the heat extraction performance of geothermal systems.

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Data availability Data is available upon request.

Declarations

e 90°

Conflict of interest The authors declare no confict of interest.

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