



Analyze of entropy generation for NEPCM melting process inside a heat storage system

M. Sheikholeslami^{1,2} · M. Jafaryar^{2,3} · Ahmad Shafee^{4,5} · Zhixiong Li^{6,7}

Received: 27 September 2018 / Accepted: 7 January 2019 / Published online: 14 January 2019
© Springer-Verlag GmbH Germany, part of Springer Nature 2019

Abstract

The purpose of current article is to simulate melting of NEPCM inside a cylinder with V shaped fins. Two dimensional transient formulations were modeled via finite volume method. Copper oxide nanoparticles were dispersed into paraffin. Second law treatments during melting are reported. Outputs illustrate that thermal entropy generation detracts with augment of temperature. Temperature rises as time progress due to stronger buoyancy forces.

List of symbols

g	Gravity
NEPCM	Nano-enhanced PCM
T_m	Fusion temperature
C	Mushy zone constant
k	Thermal conductivity
L_f	Latent heat coefficient

Subscripts

p	Particle
s	Solidus
nf	NEPCM
l	Liquidus
nf	Nanofluid

Greek symbols

ϕ	Nanoparticle volume fraction
ρ	Fluid density
α	Thermal diffusivity (m^2/s)

1 Introduction

Several scientist selected phase change materials for saving energy in heat storage units. Also, they added metallic Nano sized particles to overcome the low thermal conductivity. Selimefendigil and Oztop (2019) scrutinized CNT nanoparticles transportation due to MHD inside a corrugated cavity. Sheikholeslami et al. (2018) illustrated the unsteady solidification of NEPCM. They employed Galerkin approach to show the phase change process. Nanofluid mass transfer over step with elastic wall was scrutinized by Selimefendigil and Oztop (2018). Khan et al. (2017) demonstrated nanomaterial treatment due to radiative heating. They utilized non-Newtonian model in presence of MHD. Sheikholeslami et al. (2019) employed nanoparticles and V shaped fins to reach higher rate of solidification. They presented FEM simulation for solving unsteady problem. Heatline approach has been applied by Bondareva et al. (2016) for natural convection of nanoparticles inside a wavy enclosure with local heater. Sheremet et al. (2015) presented second law behavior of nanomaterial thorough a cavity with hot obstacle. They utilized hemogenous model (Tiwari model) for thermal conductivity. Mahian et al. (2013) scrutinized irreversibility analysis of nnaoparticles in existence of MHD impact.

✉ M. Sheikholeslami
mohsen.sheikholeslami@yahoo.com

- ¹ Department of Mechanical Engineering, Babol Noshirvani University of Technology, Babol, Islamic Republic of Iran
- ² Renewable Energy Systems and Nanofluid Applications in Heat Transfer Laboratory, Babol Noshirvani University of Technology, Babol, Iran
- ³ MR CFD LLC, No 49, Gakhokidze Street, Isani-Samgori District, Tbilisi, Georgia
- ⁴ FAST, University Tun Hussein Onn Malaysia, Batu Pahat, 86400 Parit Raja, Johor State, Malaysia
- ⁵ Applied Science Department, College of Technological Studies, Public Authority of Applied Education and Training, Shuwaikh, Kuwait
- ⁶ School of Engineering, Ocean University of China, Qingdao 266110, China
- ⁷ School of Mechanical, Materials, Mechatronic and Biomedical Engineering, University of Wollongong, Wollongong, NSW 2522, Australia

Tahir et al. (2017) studied the Maxwell nanofluid radiation along a sheet. They supposed uniform magnetic field to control the flow. Copper oxide migration due to MHD impact in a duct was scrutinized by Selimefendigil and Oztop (2018). They examined optimization procedure via ANFIS. Nguyen et al. (2016) demonstrated the transient nanofluid flow in an enclosure with various heaters. Moatimid et al. (2017) scrutinized nanofluid transient double diffusion flow. Characteristics of nanofluid inside a heat exchanger were examined by Qi et al. (2018). They reported stability behavior of nanofluid and its characteristics. Finding better working fluid in view of heat transfer is hot topic in recent decade (Rehman et al. 2018; Sun et al. 2017; Sheikholeslami et al. 2019; Sheikholeslami and Oztop 2016, 2017; Sheikholeslami 2018, 2019a, b; Khan et al. 2018a, b; Eldabe et al. 2018; Hayat et al. 2018; Darzi et al. 2016; Ahmed et al. 2017).

In present report, V shaped fins and NEPCM are considered as two effective methods to improve the melting rate. Simulation is done via FEM. Entropy and exergy contours at various stages are demonstrated.

2 Geometry and formulations

2.1 Enclosure with fins

The aim of current article is to carry out numerical investigation of transient, two-dimensional melting process inside the cavity with V shaped fins. The cavity is filled with PCM based copper oxide nanoparticle. This geometry can be fins in Fig. 1. In this paper, we consider $L = 0.04$ m, $D = 0.02$ m, $l = 0.01$ m, $t = 0.5$ mm. The concentration of copper oxide is 0.05.

2.2 Problem formulations

Let us consider transient laminar 2D melting process considering Boussinesq estimation as follows:

$$\nabla \cdot \vec{V} = 0, \tag{1}$$

$$C \frac{(1 - \lambda)^2}{\lambda^3 + \varepsilon} u + \frac{1}{\rho_{nf}} (\mu_{nf} \nabla^2 u - \nabla P) = \frac{\partial u}{\partial t} + \vec{V} \cdot \nabla u, \tag{2}$$

$$v \frac{(1 - \lambda)^2}{\lambda^3 + \varepsilon} C + \frac{1}{\rho_{nf}} (\mu_{nf} \nabla^2 v - \nabla P + g(\rho\beta)_{nf}(T - T_{ref})) = \frac{\partial v}{\partial t} + \vec{V} \cdot \nabla v$$

$$(\rho C_p)_{nf} = \phi(\rho C_p)_s + (1 - \phi)(\rho C_p)_f, \tag{3}$$

$$-\frac{\partial(\rho L \lambda)_{nf}}{\partial t} + \frac{k_{nf}}{(\rho C_p)_{nf}} \nabla^2 T = \frac{\partial T}{\partial t} + \vec{V} \cdot \nabla T. \tag{4}$$

Here we considered $\varepsilon = 10^{-3}$, $C = 10^5$.

$(\rho\beta)_{nf}$, ρ_{nf} , $(\rho L)_{nf}$ and $(\rho C_p)_{nf}$ are:

$$(\rho\beta)_{nf} / (\rho\beta)_f = (1 - \phi) + \phi \frac{(\rho\beta)_s}{(\rho\beta)_f}, \tag{5}$$

$$\rho_{nf} = \rho_f(1 - \phi) + \rho_s\phi, \tag{6}$$

$$\frac{(\rho L)_{nf}}{(1 - \phi)} = (\rho L)_f, \tag{7}$$

$$(\rho C_p)_f(1 - \phi) + (\rho C_p)_s\phi = (\rho C_p)_{nf}, \tag{8}$$

k_{nf} , μ_{nf} are obtained as:

$$k_{nf} = \frac{2k_f + k_p + 2\phi(k_s - k_f)}{k_p - \phi(k_s - k_f) + 2k_f} k_f, \tag{9}$$

$$\mu_{nf} = (1 - \phi)^{-2.5} \mu_f. \tag{10}$$

Fig. 1 Enclosure with V shaped fins

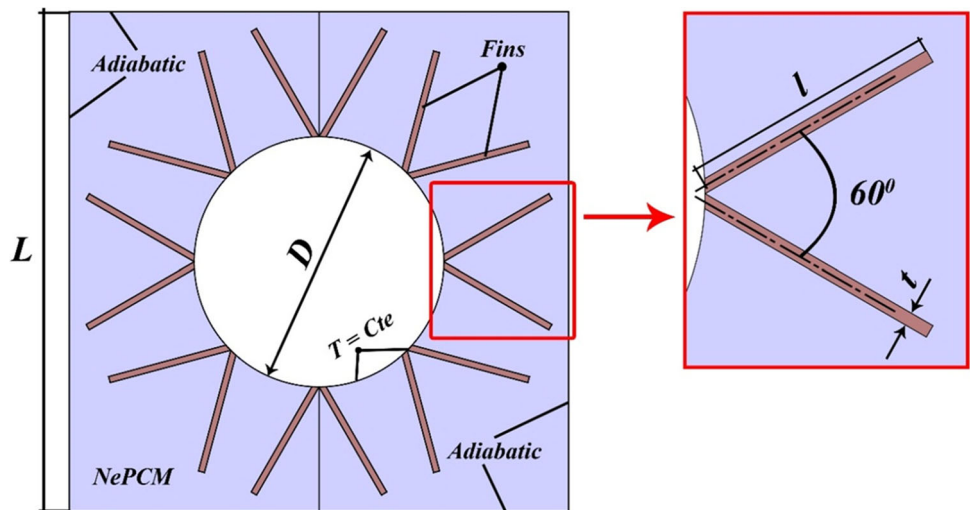


Table 1 Characteristics of CuO and (n-octadecane paraffin)

Property	Nanoparticles	N-octadecane
ρ (kg/m ³)	6500	770
C_p (j/kg K)	540	2196
k (w/mK)	18	0.148
$\mu \times 10^3$ (Pa s)	–	3.85
$\beta \times 10^5$ (K ⁻¹)	29	91
L (j/kg)	–	243,500
Fusion point (°C)	28	–

To see the properties, Table 1 has been presented.

Equation (11) and (12) can be employed to find the enthalpy:

$$H_e = h + \lambda L, \tag{11}$$

$$h = h_{ref} + \int_{T_{ref}}^T (C_p)_{nf} dT, \tag{12}$$

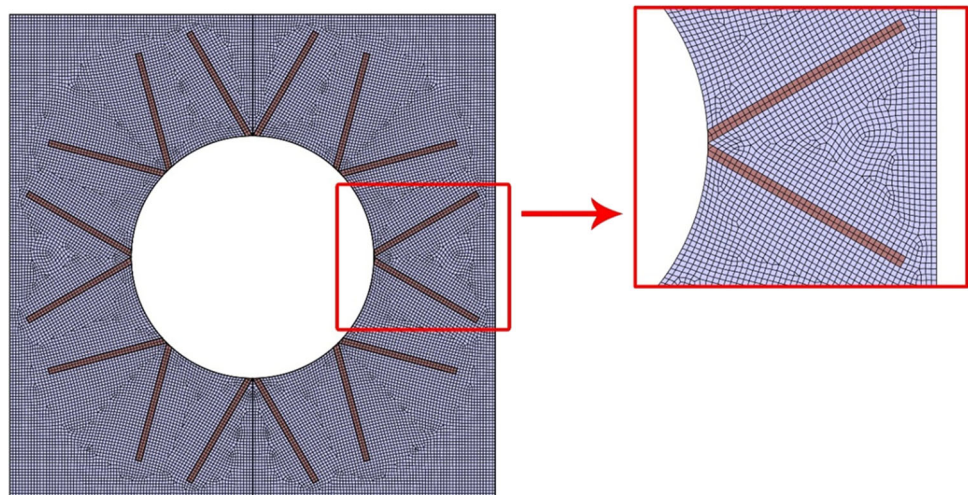
$$\lambda = \begin{cases} 0 & T < T_s \\ \frac{T - T_s}{T_l - T_s} & T_s < T < T_l \\ 1 & T > T_l \end{cases} \tag{13}$$

In above equation, we considered h_{ref} as enthalpy at 273 K.

In the present work, the definitions of $S_{gen,total}$, $S_{gen,th}$, $S_{gen,f}$ are:

$$\begin{aligned} S_{gen,total} &= S_{gen,th} + S_{gen,f} \\ &= \frac{k_{nf}}{T^2} \left[\left(\frac{\partial T}{\partial x} \right)^2 + \left(\frac{\partial T}{\partial y} \right)^2 \right] \\ &\quad + \frac{\mu_{nf}}{T} \left\{ 2 \left[\left(\frac{\partial u_x}{\partial x} \right)^2 + \left(\frac{\partial u_y}{\partial y} \right)^2 \right] \right. \\ &\quad \left. + \left(\frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x} \right)^2 \right\} \end{aligned} \tag{14}$$

Fig. 2 Example for Grid



2.3 Detail of modeling

Governing equations with the boundary conditions have solution which is obtained via FVM utilizing ANSYS Fluent 18.1. The space domain is modeled using Enthalpy-porosity method (Brent et al. 1988). PRESTO model is selected for pressure correction. Velocity under-relaxation is considered 0.2 and SIMPLE algorithm has been utilized. Figures 2 and 3 demonstrate sample grid and verification (Tan et al. 2009).

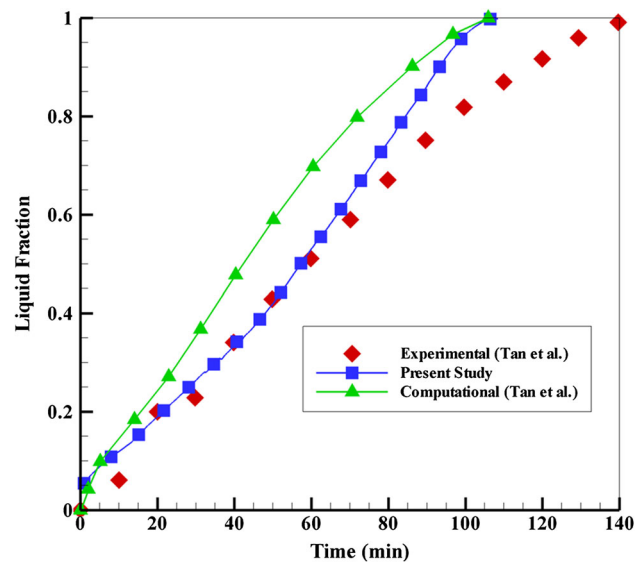


Fig. 3 Validation of code with Tan et al. (2009)

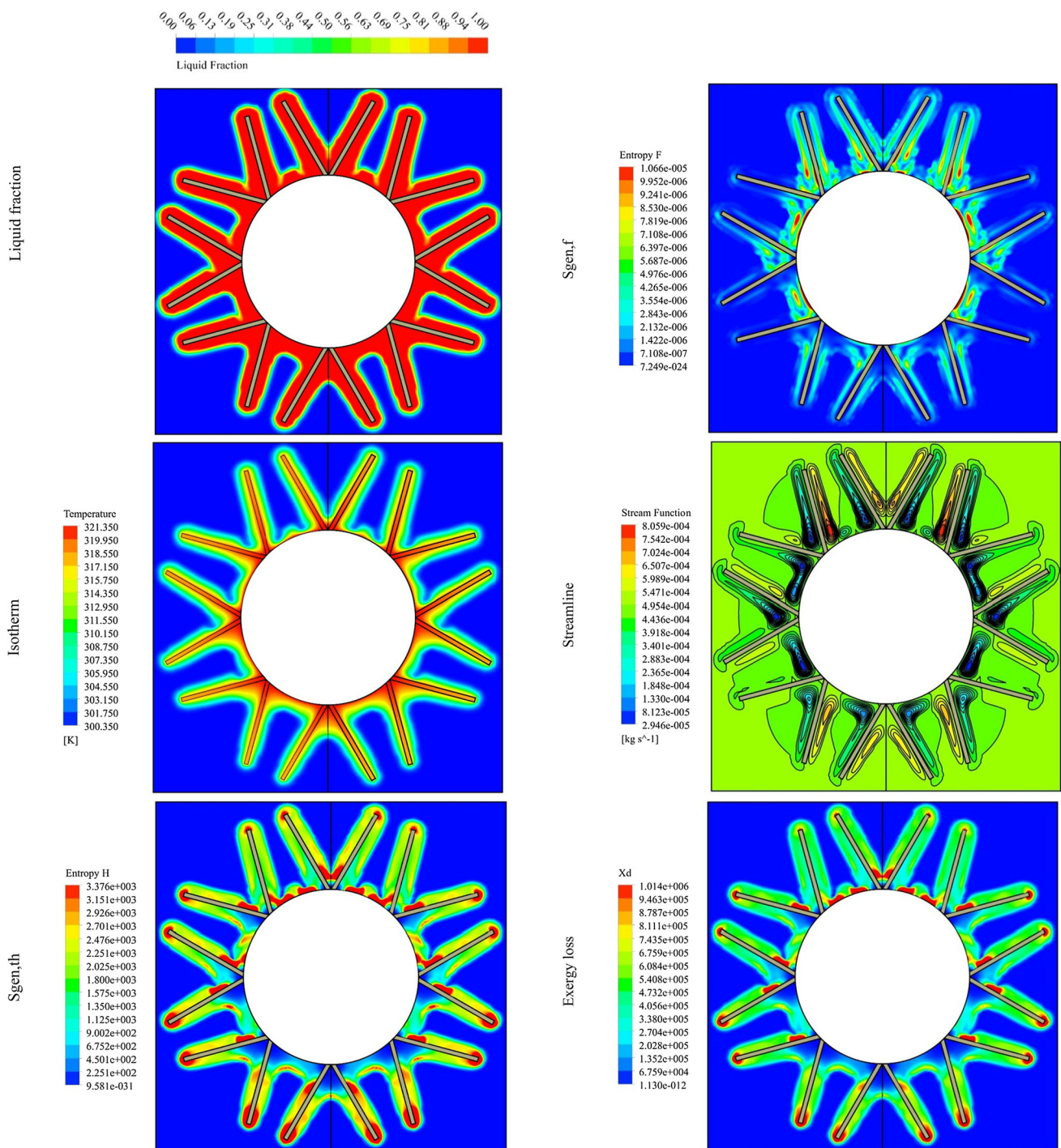


Fig. 4 Contours plots of $t = 60$ s

3 Results and discussion

Current section has been devoted to the analysis of melting process in an enclosure with V shaped fins. Not only melt fraction and temperature but also entropy generation and exergy have been analyzed. The system is filled with n-octadecane paraffin in which CuO has been dispersed.

The solution of equations was calculated using Finite Volume Method.

Both first and second law analysis during process was illustrated in Figs. 4, 5, 6 and 7. In lower time, the buoyancy is not enough strong to affect the melting. In greater time, convective mechanism affects the melting front and its shape become more complex. Vortex becomes stronger

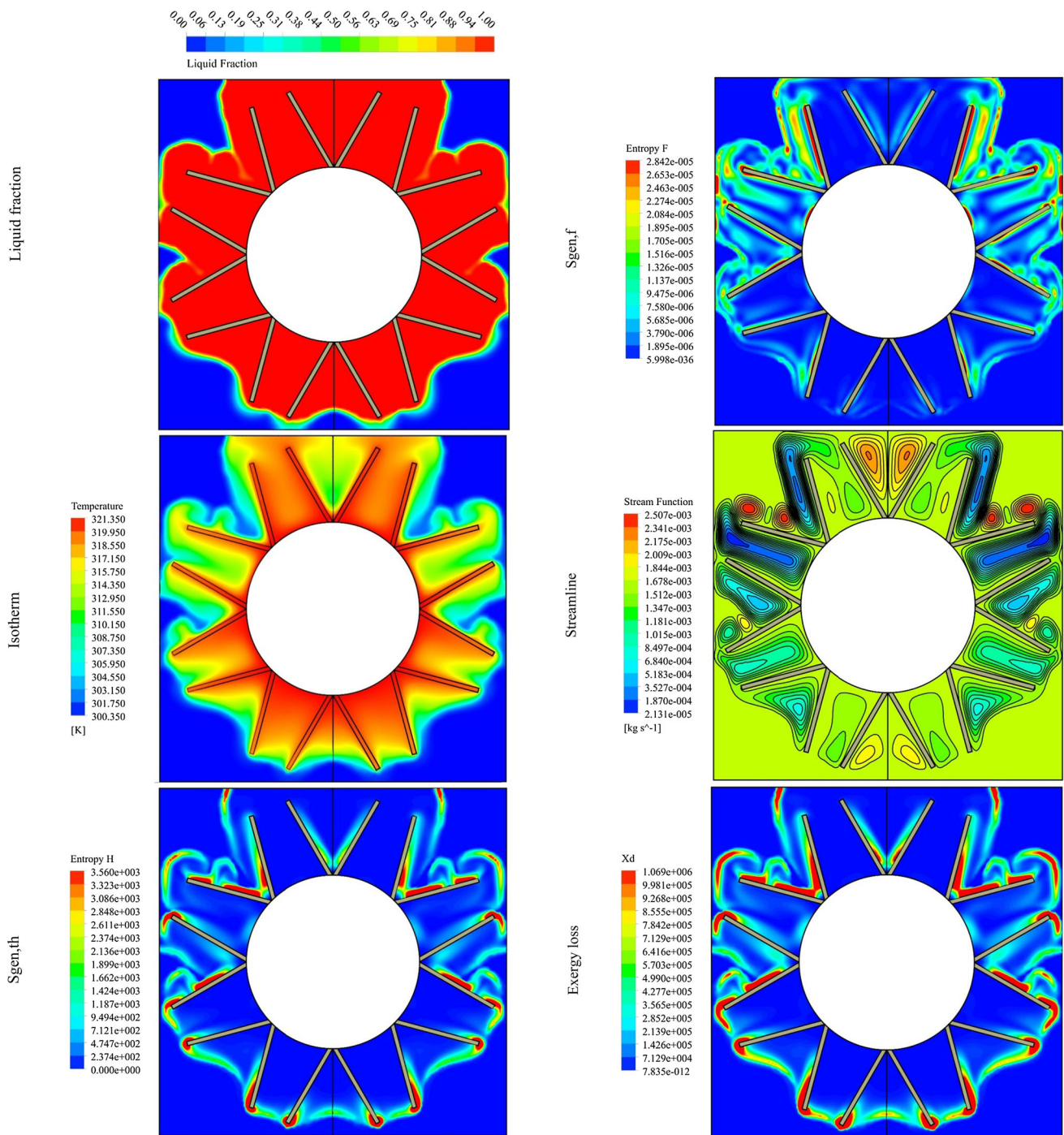


Fig. 5 Contours plots of $t = 180$ s

as the melting front reach to outer surface. The middle up of the enclosure converts to liquid phase sooner than the middle down. The region near the down wall is the final space in which the remained solid convert to liquid. This phenomena is due to absence of rotating eddies in that region. As temperature enhances, thermal entropy generation detracts as depicted in contours. Exergy loss has same

treatment, too. Liquid fraction, $S_{gen,f}$ and $S_{gen,th}$ are shown in Fig. 8. As time progress, average temperature enhances and melts fraction increases until it reaches to its maximum value. Thermal entropy generation detracts with rise of melt fraction. Frictional component has on maximum point in beginning times.

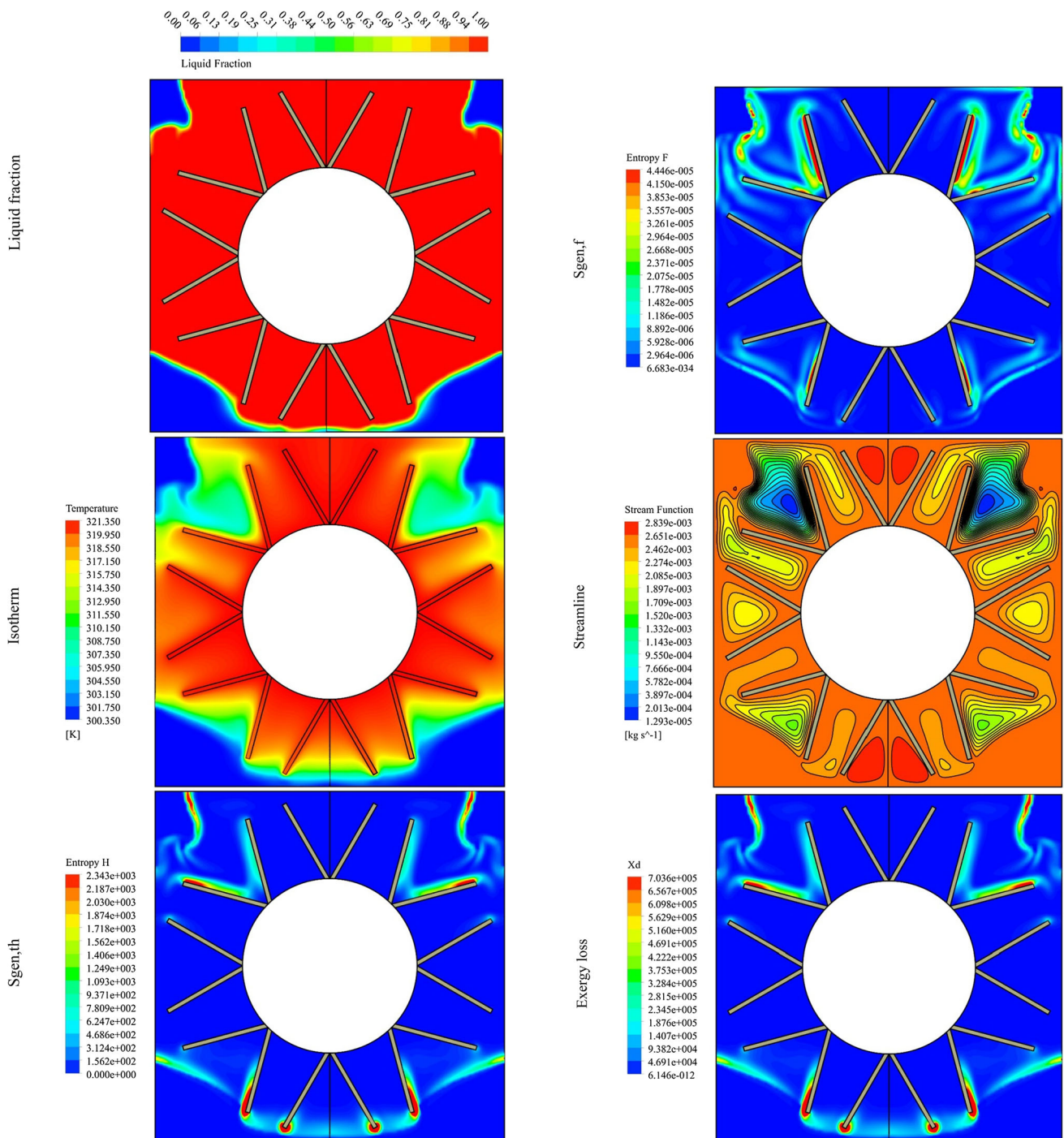


Fig. 6 Contours plots of $t = 300$ s

4 Conclusion

The NEPCM melting heat transfer inside a cylinder with V shaped fins are demonstrated. The unsteady problem has been modeled as governing PDEs which were solved via Finite Volume Method. Contours for melt fraction,

entropy, isotherm and exergy are reported in various times. Melt fraction enhances as time progress which means greater convection mode and higher temperature. So, $S_{\text{gen,th}}$ reduces with augment of time. At start of process, conduction has main role, thus $S_{\text{gen,f}}$ has one maximum point in its profile.

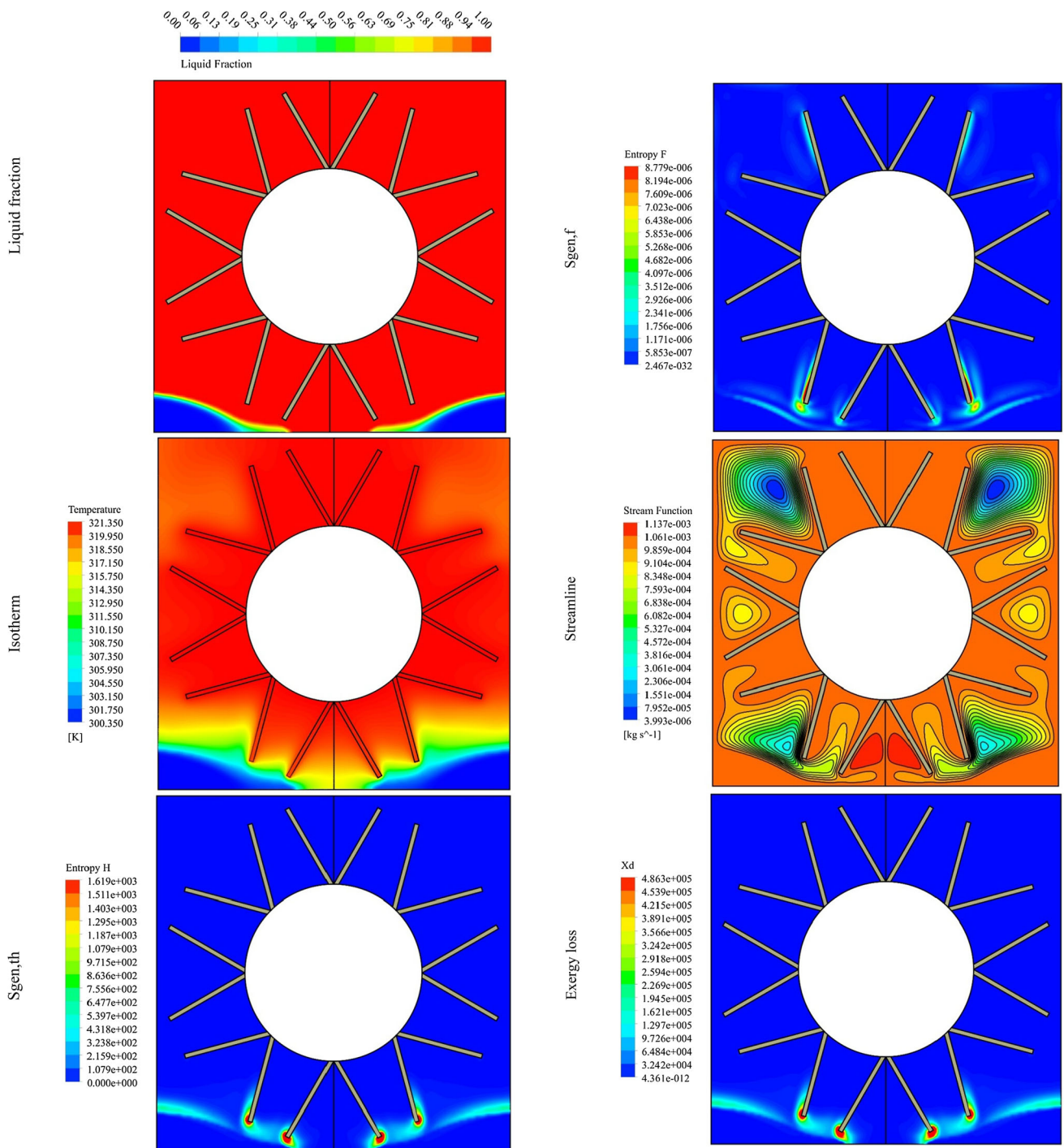


Fig. 7 Contours plots of $t = 540$ s

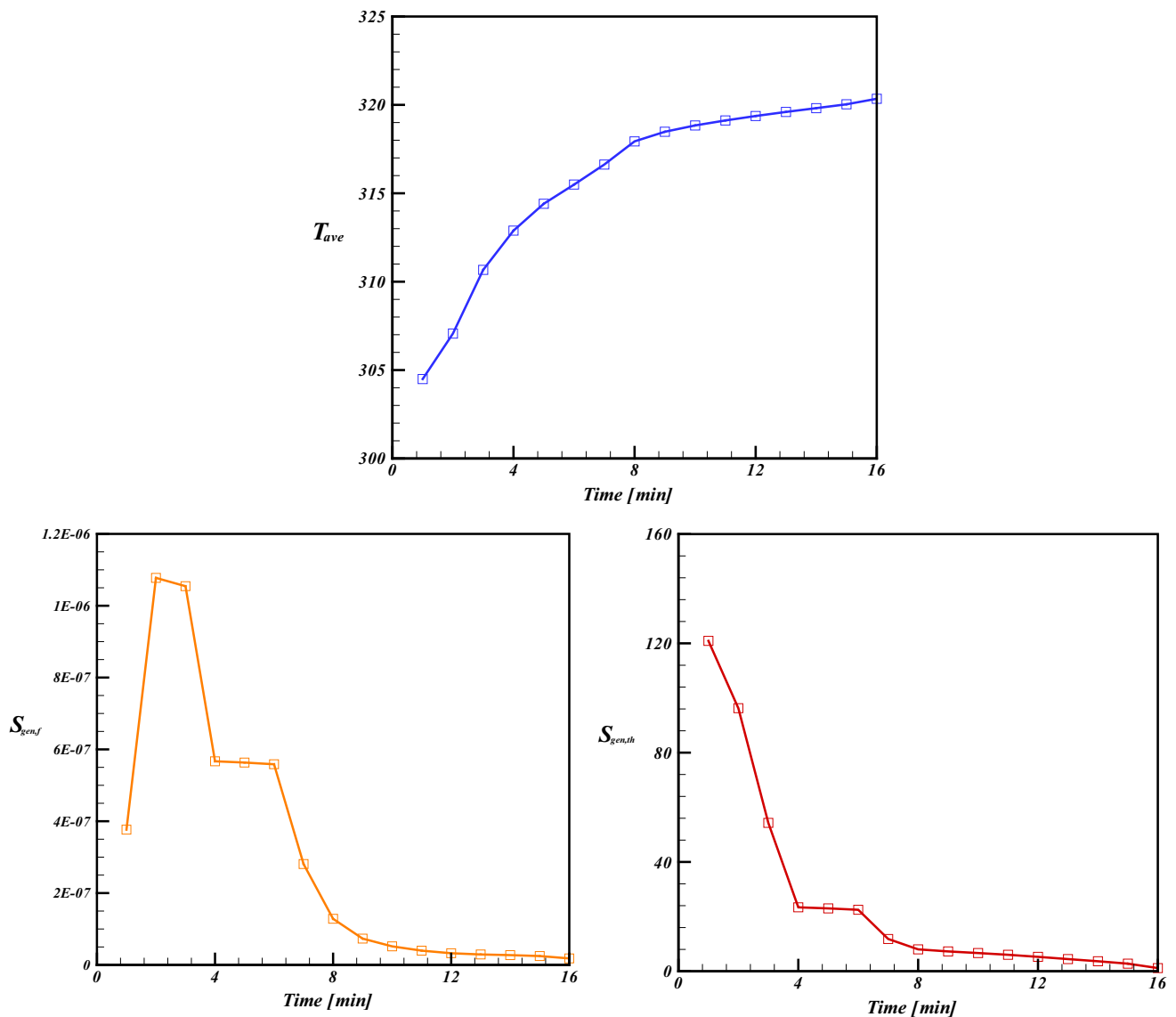


Fig. 8 Variation of temperature, entropy generation during melting process

Acknowledgements This paper was supported by the National Sciences Foundation of China (NSFC) (No. U1610109), Australia ARC DECRA (No. DE190100931) and Taishan Scholar of Shandong. Besides, the authors acknowledge the funding support of Babol Noshirvani University of Technology through Grant program No. BNUT/390051/97.

References

- Ahmed N, Khan AU, Mohyud-Din ST (2017) Unsteady radiative flow of chemically reacting fluid over a convectively heated stretchable surface with cross-diffusion gradients. *Int J Therm Sci* 121:182–191
- Bondareva NS, Sheremet MA, Oztop HF, Abu-Hamdeh N (2016) Heatline visualization of MHD natural convection in an inclined wavy open porous cavity filled with a nanofluid with a local heater. *Int J Heat Mass Transf* 99:872–881
- Brent AD, Voller VR, Reid KJ (1988) Enthalpy-porosity technique for modeling convection-diffusion phase change: application to the melting of a pure metal. *Numer Heat Transf* 13:297–318
- Darzi AAR, Jourabian M, Farhadi M (2016) Melting and solidification of PCM enhanced by radial conductive fins and nanoparticles in cylindrical annulus. *Energy Convers Manag* 118:253–263
- Eldabe NT, Gabr ME, Zaher SA (2018) Two dimensional boundary layer flow with heat and mass transfer of magneto hydrodynamic non-Newtonian nanofluid through porous medium over a semi-infinite moving plate. *Microsyst Technol* 24:2919–2928
- Hayat T, Aziz A, Muhammad T, Alsaedi A (2018) Three-dimensional flow of Prandtl fluid with Cattaneo–Christov double diffusion. *Results Phys* 9:290–296
- Khan M, Irfan M, Khan WA, Ahmad L (2017) Modeling and simulation for 3D magneto Eyring–Powell nanomaterial subject to nonlinear thermal radiation and convective heating. *Results Phys* 7:1899–1906

- Khan HM, Alshomrani AS, Haq RU (2018a) Investigation of dual solutions in flow of a non-Newtonian fluid with homogeneous-heterogeneous reactions: critical points. *J Eur J Mech B Fluids* 68:30–38
- Khan MI, Dong H, Shabbir F, Shoukat R (2018b) Embedded passive components in advanced 3D chips and micro/nano electronic systems. *Microsyst Technol* 24:869–877
- Mahian O, Pop I, Sahin AZ, Oztop HF, Wongwises S (2013) Irreversibility analysis of a vertical annulus using TiO₂/water nanofluid with MHD flow effects. *Int J Heat Mass Transf* 64:671–679
- Moatimid GM, Mohamed MAA, Hassan MA, El-Dakdoky EMM (2017) Unsteady Cattaneo–Christov double diffusion of conducting nanofluid. *Sci Eng Appl* 2(3):164–176
- Nguyen MT, Aly AM, Lee SW (2016) Unsteady natural convection heat transfer in a nanofluid-filled square cavity with various heat source conditions. *Adv Mech Eng* 8(5):1–18
- Qi C, Liu M, Wang G, Pan Y, Liang L (2018) Experimental research on stabilities, thermophysical properties and heat transfer enhancement of nanofluids in heat exchanger systems. *Chin J Chem Eng*. <https://doi.org/10.1016/j.cjche.2018.03.021>
- Rehman FU, Nadeem S, Rehman HU, Haq RU (2018) Thermophysical analysis for three-dimensional MHD stagnation-point flow of nano-material influenced by an exponential stretching surface. *Results Phys* 8:316–323
- Selimefendigil F, Öztıp HF (2016) Conjugate natural convection in a cavity with a conductive partition and filled with different nanofluids on different sides of the partition. *J Mol Liq* 216:67–77
- Selimefendigil F, Öztıp HF (2018a) Laminar convective nanofluid flow over a backward-facing step with an elastic bottom wall. *J Therm Sci Eng Appl* 10(4):041003
- Selimefendigil F, Öztıp HF (2018b) Magnetic field effects on the forced convection of CuO-water nanofluid flow in a channel with circular cylinders and thermal predictions using ANFIS. *Int J Mech Sci* 146:9–24
- Selimefendigil F, Öztıp HF (2019) Corrugated conductive partition effects on MHD free convection of CNT-water nanofluid in a cavity. *Int J Heat Mass Transf* 129:265–277
- Sheikholeslami M (2018) Finite element method for PCM solidification in existence of CuO nanoparticles. *J Mol Liq* 265:347–355
- Sheikholeslami M (2019a) Numerical approach for MHD Al₂O₃-water nanofluid transportation inside a permeable medium using innovative computer method. *Comput Methods Appl Mech Eng* 344:306–318
- Sheikholeslami M (2019b) New computational approach for exergy and entropy analysis of nanofluid under the impact of Lorentz force through a porous media. *Comput Methods Appl Mech Eng* 344:319–333
- Sheikholeslami M, Oztop H (2017) MHD free convection of nanofluid in a cavity with sinusoidal walls by using CVFEM. *Chin J Phys* 55(6):2291–2304
- Sheikholeslami M, Shehzad SA, Li Z, Shafee A, Abbasi FM (2018) Time dependent conduction heat transfer during solidification in a storage system using nanoparticles. *Microsyst Technol* 15:16. <https://doi.org/10.1007/s00542-018-4050-8>
- Sheikholeslami M, Haq R, Shafee A, Li Z (2019a) Heat transfer behavior of Nanoparticle enhanced PCM solidification through an enclosure with V shaped fins. *Int J Heat Mass Transf* 130:1322–1342
- Sheikholeslami M, Gerdroodbary MB, Moradi R, Shafee A, Li Z (2019b) Application of Neural Network for estimation of heat transfer treatment of Al₂O₃-H₂O nanofluid through a channel. *Comput Methods Appl Mech Eng* 344:1–12
- Sheremet MA, Oztop HF, Pop I, Abu-Hamdeh N (2015) Analysis of entropy generation in natural convection of nanofluid inside a square cavity having hot solid block: Tiwari and Das' model. *Entropy* 18(1):9
- Sun F, Yao Y, Li X, Zhao L, Ding G, Zhang X (2017) The mass and heat transfer characteristics of superheated steam coupled with non-condensing gases in perforated horizontal wellbores. *J Petrol Sci Eng* 156:460–467
- Tahir F, Gul T, Islam S, Shah Z, Khan A, Khan W, Ali L (2017) Flow of a nano-liquid film of maxwell fluid with thermal radiation and magneto hydrodynamic properties on an unstable stretching sheet. *J Nanofluids* 6:1–10
- Tan FL, Hosseinizadeh SF, Khodadadi JM, Fan L (2009) Experimental and computational study of constrained melting of phase change materials (PCM) inside a spherical capsule. *Int J Heat Mass Transf* 52:3464–3472

Publisher's Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.