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Prediction of the occurrence of slope instability phenomena through GIS-based hazard zonation

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Abstract Slope instability hazard assessment is based on the analysis of the terrain conditions at sites where slope failures occurred in the past. For the analysis of the causative factors the application of geographic information systems (GIS) is an essential tool in the data analysis and subsequent hazard assessment. Three scale levels of hazard mapping are defined. A direct experience-driven mapping at reconnaissance level, a statistical approach to determine the causative factors in a quantitative susceptibility mapping and a methodology at large-scale making using of deterministic models.

Key words Landslides · Hazard mapping · Geographic information system · Data analysis

Introduction

The occurrence of natural hazards is a serious constraint on economic development, particularly in developing countries, where the economic loss due to the impact of natural hazards often makes the difference between economic growth and stagnation (Fourier d'Albe 1976; Swiss Reinsurance Company 1990). On the other hand, practice has shown that adequate hazard mitigation is possible. The successful earthquake mitigation in the western United States in comparison with the earthquake in Armenia (1988), which had a comparable magnitude, is a striking example. Also successful examples of mitigation exist for other types of natural hazards (Hurricane Andrew, Pinatubo Volcano, etc.).

The present article presents the outlines of a methodology for landslide hazard zonation at small scales for regional assessments, medium scales for feasibility studies and large scales for local, more detailed studies. The results, based on research in the Andean Cordillera in Colombia, clarify some of the methodological concepts.

Slope instability hazard zonation

Slope instability hazard zonation is defined as the mapping of areas with an equal probability of occurrence of landslides within a specified period of time (Varnes 1984). A landslide hazard zonation consists of two different aspects:

- 1. The assessment of the susceptibility of the terrain for a slope failure, in which the susceptibility of the terrain for a hazardous process expresses the likelihood that such a phenomenon occurs under the given terrain conditions or parameters.
- 2. The determination of the probability that a triggering event occurs. The probability for the occurrence of a landslide is mostly evaluated by calculating the probability of triggering events such as major rainfall events or earthquakes. It is important to mention here that the calculation of landslide probability is more difficult than for other natural disasters (such as floods or earthquakes), since there is no simple relation between the magnitude of a landslide event and a return period. Another complicating factor is that mostly there are no reliable historic records of landslides that allow making a relation between landslide dates and rainfall or earthquakes.

An area is declared to be susceptible to landslides when the terrain conditions at that site are comparable to those in an area where a slide has occurred. The instability of a slope is governed by a complex of normality interrelated terrain parameters such as lithology and the structural conditions of the rocks, the weathering and the contact with overlying soils, the properties of these soils, slope gradient and form,

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hydrological conditions, vegetation, land use and landuse practice and, finally, human activities acting on the slope conditions.

The joint analysis of all these terrain variables in relation to the spatial distribution of landslides has gained enormously by the introduction of Geographic Information Systems (GIS), the ideal tool for the analysis of parameters with a high degree of spatial variability.

Considering that for slope instability hazard assessment the assumption is made that conditions which led in the past to slope failures will also result in potential unstable conditions in the present, the essential steps to be followed in landslide susceptibility zoning are defined automatically:

- 1. A landslide distribution mapping, differentiated according to type, activity, dimensions, etc., and based on information covering, when possible, a time span as large as possible
- 2. A mapping of the most relevant terrain parameters related to the occurrence of landslides
- 3. The analysis of the terrain conditions which can be considered responsible for the occurrence of the different types of landslides
- 4. The assignment of weights to the individual causative factors, the formulation of decision rules and the designation of susceptibility classes.

GIS-supported slope instability hazard methods

When making use of GIS techniques, the following methodological approaches can be differentiated:

- 1. Heuristic qualitative approach, particularly suited for small-scale regional surveys. The scale of such surveys is of the order of 1:100 000 to 1:250 000. They are used mostly by regional planning agencies.
- 2. Statistical quantitative approaches for mediumscale surveys. These are in the range of 1:25000– 1:500000 and are used by consulting firms or planning agencies for the preliminary planning of infrastructural works such as the definition of road corridors. The methods at this scale can be subdifferentiated as follows:
 - Data-driven multivariate statistical analysis
 - Experience-driven bivariate statistical analysis
 - Predictive modelling through the application of probability and favourability functions.
- 4. Deterministic approach for detailed studies at large scale (1:2000–1:10000), without entering that level of the engineering geological site investigation. Such small-scale studies are used by consulting firms or local planning agencies for the detailed planning of infrastructural works.

As observed before, all three methodologies require a good idea of the spatial distribution of landslides as the essential element for the analysis, although the landslide inventory mapping has to be minimized at the small scale in regional surveys to maintain an acceptable cost/benefit ratio. Therefore, the heuristic qualitative approach particularly suits reconnaissance phases, when an assessment has to be made without the time-consuming inventories of landslides and all possible terrain parameters. In such cases the role of professional expertise, leading to a classification, is essential.

A landslide inventory is executed with the objective to obtain good insight into the whole slope instability record of the area. The inventory should give an as good as possible characterization of the landslides, such as type and subtypes, as well as degree of activity or size. Historic databases are most useful for this work. However, most of the landslide distribution mapping will be obtained by aerial photo interpretation. The scale of the photos should not be smaller than 1:25000; otherwise, an important part of the slope failures will be overlooked. The use of infrared (false) colour photography is advocated, as these are more sensitive for variations in drainage and vegetational conditions, two parameters strongly related to the occurrence of landslides. To obtain a full idea of the occurrence of landslides, the study of sequential coverages is almost indispensable, as erosion and overgrowing by vegetation will wipe out the evidence for slope movements in a few years. This is particularly needed for large-scale surveys, but can also be applied to medium scales. The analysis of sequential aerial photograph coverages will offer further information on the degree of activity of the different types of processes, as well as the possible influence of changes of land use and other human activity on the stability of the slopes.

Image interpretation is sustained by fieldwork, normally accompanied by systematical data collection of terrain parameters associated with the slope failures. A detailed description of the differentiation of landslide types and degree of activity from stereoscopic photo interpretation procedures is given by Soeters and van Westen (1996).

The heuristic qualitative approach is a direct or semi-direct mapping methodology, which implies that during the landslide inventory a direct relationship is made between the occurrence of slope failures and the causative terrain parameters. An a priori knowledge on the causes of landslides is essential in decision making, and therefore the method relies heavily on the professional experience of the expert. During the photo interpretation of representative areas and in the fieldwork, the terrain conditions are evaluated at all places where landslides are encountered and preliminary conclusions are made on the causative factors. The analysis in GIS of the systematically collected data can support the expert opinion and is used to establish weight factors for the variables. Subjective decision rules, mainly based on experience, are formulated and geomorphological units are reclassified according to

their degree of susceptibility. For very large areas, socalled terrain mapping units (TMUs) are defined on the basis of air photo and satellite image interpretation. These TMUs are considered homogeneous at a scale of 1:100 000. They are subdivided into smaller units. Each unit is characterized by several factors such as lithology, internal relief and drainage density, which can be derived partly from overlaying the TMU map with a digital elevation model in a GIS. A schematic overview of the various factors which describe a TMU is given in Fig. 1.

The methodology for assigning hazard classes is essentially the same as the conventional techniques used in the assessment of the stability of slopes, with the advantage that GIS offers the possibility for a weighting of parameters and an easy display of slight modifications in the decision rules and the comparison of the results with the conception of the expert. The main criticism on the methodology is the subjectivity in the decision making. However, it should be realised that subjectivity is not necessarily bad, considering that it is based on the opinion of an expert. The reproductibility of subjective classifications is normally low, which can have legal consequences, which caused practical applications to be limited.

In the statistical approach an indirect mapping methodology is followed. All possible causative terrain parameters are entered into a GIS and crossed for their analysis with a landslide distribution map. When using multivariate statistical methods all parameters at sites of instability can be analysed by multiple regression techniques, or parameter maps are crossed with landslide distribution maps and the correlation is established for stable and unstable areas with discriminant analysis. A schematic overview of the method is given in Fig. 2.

Recent examples of multivariate statistical analysis in landslide studies using GISs have been presented mainly by Carrara (1988) and Carrara et al. (1992). In their work grid cells, morphometric units or uniquecondition polygons are reclassified into hazard classes according to the terrain parameters belonging to these grid cells or mapping units. The methodology is typically data driven and therefore highly objective. A difficulty in the application of multivariate statistics lies in the extremely voluminous matrices that are necessary for the calculations if reasonably small grid cells are used. On the other hand, when the grid cells are increased in size (Carrara used cells of 100×100 m) they become less homogeneous and consequently it is more difficult to assign a specific parameter class or the presence or absence of a landslide to a grid cell, when they affect only a small part of it. This results in the introduction of errors in the evaluation of the relation between landslide and parameter class (see Fig. 3). The homogeneity of the units, to which the statistical calculations are applied increases considerably when geomorphological terrain units are used. However, the

interpretation of these units at the necessary detail is a very time-consuming job, asking also for extensive professional knowledge. Therefore, the choice of small first-order catchments and morphological terrain units is an acceptable compromise. The units can be differentiated automatically by the use of a detailed digital terrain model, and these natural units are more homogeneous than grid cells.

By the use of bivariate statistical methods, the role of individual or combinations of parameters with regard to slope failures is statistically evaluated. Many statistical methods exist to determine the contribution of a certain parameter class to the occurrence of a landslide. Van Westen et al. (1993) used simple density functions to determine weights for the parameter classes (see Fig. 4).

A differentiation can be made between the normalisation of the number of landslides occurring per parameter class and the number of pixels with landslides over the total number of pixels in a parameter class. The overall density of landslides in the area can be used as standard in the calculation of the weights, by comparing the class density with the overall density. Yin and Yan (1988) define an information value to calculate the susceptibility for the occurrence of a slide, which is logarithm of the ratio between the density of landslides in a class over the density of landslides for the whole area.

Other authors (e.g. Bonham-Carter 1994) are using the fuzzy logic or the Bayesian approach to the problem of combining data sets. Chung and Fabbri (1993) developed statistical procedures under the name of predictive modelling, applying favourability functions on individual parameters. Using these statistical and probabilistic methods, terrain units or grid cells are transformed to new values representing the degree of probability, certainty, belief or plausibility that the respective terrain units or grid cells may contain or be subject to a particular landslide.

The bivariate statistical methods give a satisfactory combination of the (subjective) professionally geared direct mapping and the (objective) data-driven analysis capabilities of a GIS. The main advantage of bivariate statistical procedures is that the determination of parameters or parameter combinations used in the assessment is determined by the professional, who executes the analysis. This enables the introduction of expert opinion into the process.

Bivariate statistical methods have a serious drawback: they use the assumption of conditional independence. This means that the different parameter maps are independent with respect to the probability for the occurrence of a landslide. This assumption is mostly not valid, however, leading to probability values which are not realistic. The problem can be avoided when the user evaluates the data and makes a new parameter map by combining the dependence ones.

Terrain Mapping Unit approach







Counting circle



Valley density = length of streams/area

TMU - attribute table

TMU (TMU code linked with map) = 1
OR (Origin, geomorphology, physiography) = Denudational hills, straight slopes, incision
LC (Lithological complexity) = Two interbedded rocks, covering 100 % of TMU
LT (Lithological type) = Sandstone and marls
AL (Altitude: min/max) = 650 - 800 m.
RL (Relief length ratio in m/m) = 230/1600 m/m
IR (Internal relief in m) = 110 m
VD (Valley density in km/km2) = 6.9 km/km2
SU (Number of subunits) = 2
LD (Landslide density) = High
Hazard = High





Fig. 1 Representation of terrain mapping units and the various factors used to describe them

Multivariate statistical analysis

Landslide occurrence map



For tother types the process is repeated Only 1 landslide type is analyzed Selection of relevant factors for the prediction of landslides should be made first. Only some are shown.



Fig. 2 Representation for application of GIS in multivariate statistical landslide hazard analysis

Sampling units

Either pixels, slope units, or unique

Example 1: negative relation between parameter and landslides



Example 2: positive relation between parameter and landslides



no	relat	lon	
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Unit	Landslide	Parameter
1	0	1
2	0	1
3	1	1
4	1	1
5	0	1
6	1	1
7	1	1
8	0	1
9	0	1
10	1	1

Fig. 3 Problems related to sampling of variables in terrain units for statistical analysis. On the left side a negative relation exists, although the result of the sampling shows a positive relation, whereas on the other side a positive relation is not shown by the sampling

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Both the bivariate- as well as the multivariate statistical methods generally have some other drawbacks. To test the accuracy of the prediction the final hazard maps is compared with the landslides in the area, and through an iterative process of analysis and classification an optimalization of the model is established. This is, however, a kind of circular reasoning, which should be avoided. To avoid this, use should be made of multitemporal landslide maps. The models are constructed using a landslide map of a previous period (e.g. one decade ago), and the resulting map is checked with the present landslides.

The most serious drawback of the use of statistical methods is the collection of data over a large area regarding landslide distribution and factor maps. To realize this data gathering at an acceptable cost can be a serious problem. Therefore, the use of training areas and prediction (target) areas have been tested (Naranjo et al. 1994). A training area is defined as a small area within the overall study area, representative of the variability in the whole area. The occurrence of landslide in relation to the terrain conditions is analysed in detail in this sample area and the decision rules determined are extrapolated over the whole study zone, the prediction area. The results of the research show that the direct application of this methodology has serious limitations. The methodology asks for a careful confrontation of the hazard prediction with the "real world" and adaptation of decision rules where differences are observed, which is mostly on experiencedriven criteria.

The advantage of the application of deterministic models in landslide hazard studies is that use is made of sound physical models. Stability models, as used in geotechnical engineering, calculate the stability of a slope, using parameters such as normal stress, angle of internal friction, pore water pressure, etc. They result in a safety factor which can be used directly by engineers in the design of infrastructural or remedial works. Deterministic slope stability models have been used since the beginning of this century to calculate the stability of individual slopes (Nash 1987). Only recently have several researchers started to use the same models for the calculation of slope stability maps for larger areas such as catchments (Ward et al. 1981, 1982; Okimura and Kawatani 1987; Brass et al. 1989; Benda and Zhang 1990; Van Asch et al. 1992, 1993; Van Westen et al. 1993; Terlien et al. 1995; Terlien 1996) or road corridors (Hammond et al. 1992).

Bivariate statistical analysis



Fig. 4 Representation for application of GIS in bivariate statistical landslide hazard analysis

Hydrological models are frequently used to give an estimation of the maximum pore water pressures to be expected on the potential slip surfaces. In tectonically active regions the spatial distribution of ground accelerations as a consequence of earthquakes has to be incorporated in the final stability calculations as well (Brass et al. 1989; Van Westen et al. 1993). Several researchers also included the uncertainty in the input data in their calculations (e.g. Hammond et al. 1992; Van Westen et al. 1993). However, the use of deterministic hydrological models in combination with stability models has been successfully applied (Terlien et al. 1995; Terlien 1996).

Due to the high spatial variability of the geotechnical parameters and the labourious methods in acquiring these data, an acceptable approximation of the values is almost only attainable at the level of site investigation, which implies a serious limitation of these models in slope stability hazard zoning at a reasonable cost/benefit ratio.

In hydrological modelling and in slope stability calculations GIS can play an important role because of its computation power, and the elaboration of digital terrain models (DTMs) and derived maps such as slope maps, aspect maps and slope length maps (Wadge 1988). These maps are required for two-dimensional (2D) and three-dimensional (3D) hydrological modelling and slope stability calculations.

Deterministic landslide hazard zonation can only be successful when the failure- and trigger mechanisms of different landslide types are correctly identified and modelled. In Fig. 5 an example is shown of such an evaluation from an area in the Colombian Central Cordillera (Terlien 1996).

On the basis of a statistical evaluation of the relation between rainfall and landslide events, the monitoring of



Fig. 5 Antecedent rainfall of 25 days and landslide events in 1993 as a function of time for a research area in the Colombian Central Cordillera (Terlien 1996)

pore water pressure fluctuations in soils on landslideprone slopes and the back analysis of failed slopes, a number of hydrological failure mechanisms could be recognised:

- 1. Landslides triggered directly by rainfall, caused by the saturation of the topsoil during intense rainstorms. Especially in tropical soils this mechanism is thought to be a very important landslide trigger (Anderson and Kemp 1991).
- 2. Landslides triggered by a perched water table in more permeable materials, which occur between more impermeable materials. Rulon and Freeze (1985) give a review of this process.
- 3. Landslides triggered by ground water. Landslides may be triggered by a combination of shear strength reduction due to saturation in the upper part of the soil profile and buildup of positive pore water pressures in the lower part of the soil profile, or by convergence of saturated subsurface flow and ground-water flow in terrain concavities and hollows (e.g. Okimura and Kawatani 1987; Terlien 1996).

Hydrological and slope stability calculations can be performed within or outside the GIS environment. If the calculations are performed outside GIS with existing hydrological and slope stability models, GIS is used as a spatial database for storage, display and updating of the input data. Data has to be exported from the GIS to the external software and the results from the models are imported again in order to display them.

When one-dimensional models (e.g. infiltration models for vertical water flow) or 2D models (e.g. hillslope hydrological models for vertical and downslope water flow) are used, the model outcome which has to be used in distributed slope stability calculations has to be converted into a map. This is generally achieved by linking the model outcome to mapping units or slope configurations (Terlien 1996; Van Westen et al. 1993).

One-dimensional slope stability calculations can easily be performed in a raster GIS. In fact, the onedimensional infinite slope model (Graham 1984) which calculates the stability of each individual pixel, and ignores the influence of its neighbouring pixels, is most frequently used. More complex slope stability models generally operate on cross sections. The construction of a safety factor map from a large series of cross section in GIS is complicated.

To overcome the problems related to the use of external models, deterministic model calculations can be performed entirely within the GIS. The disadvantage of this approach is that in most GIS packages only simple operations, such as map overlaying and classification, can be performed. The facilities to use complex algorithms, iteration procedures, the use of neighbourhood operations, the third dimension and the time dimension are poorly developed in most 2D GIS packages (Coppock 1995). A schematic overview of the use of deterministic slope stability methods in a GIS is presented in Fig. 6.

Deterministic landslide hazard analysis



Fig. 6 Representation for application of GIS in deterministic slope stability analysis

The final stage in deterministic landslide hazard zonation consists of the calculation of failure probability maps. To convert safety factor maps into failure probability maps use is made of the probabilities of the triggering event (time probability), as well as the variance of the input data (variable probability: the probability that the safety factor, based on the distributions of the input data, will be ≤ 1). For the latter either Monte Carlo simulations (Hammond et al. 1992) or mathematical error propagation methods (Burrough 1986) can be used.

As a general conclusion, it can be stated that hydrological models and slope stability models can be applied successfully when the triggering mechanisms are well understood and properly modelled. The poor quality of input data and the lack of verification are the principal limitations for the use of hydrological models and slope stability models in GIS-based landslide hazard zonation. It should be understood that the results obtained with these methods cannot be used for slope stability design purposes, but they are suited for the determination of slope segments with a higher failure probability and to run scenarios when the effect of slope modifications, e.g. for road cuts, has to be evaluated.

Conclusion

Geographic information systems has proved to be an excellent tool in the spatial analysis of the terrain parameters for landslide hazard zonation. Good results are obtained in regional reconnaissance maps, when experienced based conclusions on hazard susceptibility are qualitatively extrapolated over large areas. The development of expert systems are promising for smallscale landslide hazard surveys. The maximum benefit of GIS is obtained at larger scales, when the causative factors are determined by a statistical analysis of terrain parameters in relation to the occurrence of landslides. Bivariate statistical methods are preferred over multivariate statistics, as the professional can use his experience in the determination of the parameters or parameter combinations chosen for the analysis. In an iterative process the optimization of the hazard zonation are positive as long as the quality of the input data is good and sufficient knowledge exists on the relation of the occurrence of the triggering mechanisms in relation to the occurrence of landslides.

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