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An assessment of total RMR classification system using unified simulation model based on artificial neural networks

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Abstract Engineering design has great importance in the cost and safety of engineering structures. Rock mass rating (RMR) system has become a reliable and widespread predesign system for its ease of use and variety in engineering applications such as tunnels, foundations, and slopes. In RMR system, six parameters are employed in classifying a rock mass: uniaxial compressive strength of intact rock material (UCS), rock quality designation (RQD), spacing of discontinuities (SD), condition of discontinuities (CD), condition of groundwater (CG), and orientation of discontinuities (OD). The ratings of the first three parameters UCS, ROD, and SD are determined via graphic readings where the last three parameters CD, CG, and OD are estimated by the tables that are composed of interval valued linguistic expressions. Because of these linguistic expressions, the estimated rating values of the last three become fuzzy especially when the related conditions are close to border of any two classes. In such cases, these fuzzy situations could lead up incorrect rock class estimations. In this study, an empirical database based on the linguistic expressions for CD, CG, and OD is developed for

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Electronics and Computer Education Department, Technical Education Faculty, Kocaeli University, Umuttepe Campus, 41380 Kocaeli, Turkey training Artificial Neural Network (ANN) classifiers. The results obtained from graphical readings and ANN classifiers are unified in a simulation model (USM). The data obtained from five different tunnels, which were excavated for derivation purpose, are used to evaluate classification results of conventional method and proposed model. Finally, it is noted that more accurate and realistic ratings are reached by means of proposed model.

1 Introduction

Rock masses are complex materials, which exhibit different properties so that they are divided into structural regions which show uniform features rather than the others in classifications. Quantitative rock mass classifications are based on the experiences of engineers and designers and provide communications between them [1].

For this reason, some classification systems were proposed in design of engineering applications. Like many other classification systems in use in engineering geological practice, rock mass classifications often involve criteria on which values are assigned in linguistic terms [2].

As being one of the classification systems, RMR is used more abundantly. The system, also known as geomechanics classification, was proposed in 1973 and modified according to the experiences of new cases (tunnel projects) and to adapt with the standards. Despite the changes made over years, the system remains the same in principle [3]. The RMR system has been used in many tunnel projects as one of the indicators to define the support or excavation classes [4]. In this study, the latest version (1989) of the system which utilizes six parameters for total RMR sum is used. In estimation of total RMR, an additional sixth parameter adjusts the basic RMR sum (Table 1) due to the engineering application. This parameter is used for estimating the effect of strike and dip orientations (OD) of discontinuities as linguistic terms (Table 4). Numerical values are assigned to estimate the quantitative value of the effect of the orientation of discontinuity.

There is a need to account for fuzzy variation of rock parameters approximately after taking uncertainty into account. Thus, it is better to assign a range of ratings for each parameter [1]. According to Hoek and Brown, a classification must be a non-linear process [5]. ANNs have the potential to map complex and non-linear relations between input and output variables of a system and so they are commonly used in non-linear engineering problems. In design of engineering projects, neural network systems can be used to confirm and refine design solutions [6].

Integration of the conventional and intelligent system modeling methods can be used in comparison of the different methods. For example, a model or a method could be embedded in another model or a method and could provide to enhance the other's capability [7].

2 Method

In this study, conventional method and ANN-based USM are compared and evaluated. Tunnels that have rock mass parameter values close to borderlines are selected to evaluate.

2.1 Evaluation of total RMR in conventional method

In RMR classification, also known as geomechanics classification, the rock mass in a given site is divided into structural regions of certain similar features. The following six parameters are determined for each structural region to classify a rock mass:

- 1. Uniaxial compressive strenght of rock material (UCS).
- 2. Rock quality designation (RQD).
- 3. Spacing of discontinuities (SD).
- 4. Condition of discontinuities (CD).
- 5. Condition of groundwater (CG).
- 6. Orientation of discontinuities (OD).
- In classification, the sum of the first five parameters is divided into five ranges of values that give the basic

| | | Deint land strength | > 10 | 4 10 | 2.4 | 1.2 | Easthis law areas anisaisl | |
|----|------------------------------|-----------------------|---------------------|--------------------|------------------|-----------------------|------------------------------|--|
| | Steen ath a f | index (MDe) | > 10 | 4-10 | 2-4 | 1-2 | For this low range, unlaxian | |
| | Strength of | muex (MFa) | | | | | compressive test is | |
| 1 | | | | 100 440 | #0 100 | | preferred | |
| | material | Uniaxial compressive | > 250 | 100-250 | 50-100 | 25-50 | 5-25 1-5 <1 | |
| - | _ | strength (MPa) | | | _ | | | |
| | Rating | | 15 | 12 | 7 | 4 | 2 1 0 | |
| 2 | Drill core Qual | ity RQD (%) | 90–100 | 75–90 | 50-75 | 25–50 | <25 | |
| | Rating | | 20 | 17 | 13 | 8 | 3 | |
| 3 | Spacing of disc | continuities | >2 m | 0.6-2m | 200-600 mm | 60–200 mm | <60 mm | |
| 5. | Rating | | 20 | 15 | 10 | 8 | 5 | |
| | | | Very rough surfaces | Slightly rough | Very rough | Slickensided surfaces | Soft gouge > 5mm thick | |
| | Condition of discontinuities | | Not continuous | surfaces surfaces | | or | or | |
| 4 | | | No. continuous | Separation < 1mm | Separation < 1mm | Rouge < 5 mm | Separation > 5mm | |
| | | | INO separation | Slightly weathered | Highly weathered | or | continuous | |
| | | | onweathered wan | | walls | Separation 1-5 mm | | |
| | | | TOCK | | | Continuous | | |
| - | Rating | | 30 | 25 | 20 | 10 | 0 | |
| | | Inflow per 10 m | | | | | | |
| | | tunnel length (L/min) | None | 10 | <25 | 25-125 | >125 | |
| | | | | | | | | |
| | | Joint water pressure | Or | Or | Or | Or | Or | |
| _ | Groundwater | Ratio | | | | | | |
| 5 | | Major principle | 0 | 0-0,1 | 0.1-0,2 | 0.2–0,5 | > 0.5 | |
| | | Stress | 0 | 0 | 0 | | | |
| | | | Or | Or | Or | Or | Or | |
| | | General conditions | Completely dry | Damp | Wet | Dripping | Flowing | |
| - | Rating | | 15 | 10 | 7 | 4 | 0 | |

Table 1 Rock mass rating system (geomechanics classification of rock masses)

RMR rating. Higher rating values indicate that the rock mass is in a better condition;

- (a) In evaluation of the first three parameters ratings, the charts (Fig. 1) proposed by International Standards of Rock Mechanics (ISRM) are used, which remove abrupt changes in borderline cases and also that ratings occur between categories as shown in Table 1 [8].
- (b) The 4th parameter CD is evaluated from Tables 2 and 3. General roughness and weathering situations of a rock mass are rated using the guidelines in Tables 2 and 3.
- (c) The 5th parameter CG is evaluated from the fifth row of the Table 1.



Fig. 1 Ratings of uniaxial compressive strength discontinuity length and a rock quality designation [3]

- The 6th parameter is the adjustment of basic RMR that regards the influence of dip orientation and strike (OD). Evaluation of the sixth parameter depends on engineering structures such as tunnel, mine, slope, or foundation. In tunneling, OD is determined by linguistic terms such as 'fair' (Table 4). Finally, rating of OD is scored as shown in Table 5."
- For total RMR rating, each tunnel is evaluated using basic RMR ratings and adjusting them by means of adding the OD ratings.

2.2 Evaluation with unified simulation model (USM)

USM shown in Fig. 2 is composed of three parts;

- Ratings of UCS, RQD, and SD are estimated assigning functions to the graphics in the first part of Fig. 1 whose charts are redrawn by means of curve fitting and obtained functions are used in USM.
- In the USM, CD and CG ratings are estimated by means of an ANN which determines conditions of both discontinuities and groundwater (ANN-CD&CG).
- In the third part, OD ratings are estimated by evaluating the effect of strike and dips parameters by a second ANN, called ANN-OD.

Structural properties of these two ANN models will be given as follows.

2.2.1 ANN classifiers

Contrary to the traditional method, ANN learns the solution from a set of training data as an alternative calculation method. Especially from human brain, this opinion is stemmed from biological neural system [9]. ANN is composed of neurons which generally are fully connected to each others by means of layers. A Multi Layer Perceptron (MLP) ANN structure shown in Fig. 3 consists of one input layer (X_i), one or more hidden layer(s), and one output layer (y_k). All the layers of the MLP are fully connected to each others [10]. An effective training algorithm based on back propagation of the error has made MLP ANN widely used [11].

To perform a rapid convergence in training phase, inputs of ANNs are (not compulsory but in general) normalized by a factor due to amplitude of the related possible maximum input values. But if such a way is applied in, we need to pay attention to redivide an input with the same factor also in the testing phase. In the training and testing phase of the ANNs, relatively great input ranges are normalized by 100, while relative smallers are normalized by 10.

| Parameter | R | Rating | | | | | | |
|----------------------|-------------|-----------|-----------|----------------------|------------------|--------------|--|--|
| Discontinuity length | | (1 m | 1–3 m | 3–10 m | 10–20 m | >20 m | | |
| | | 5) | (4) | (2) | (1) | (0) | | |
| Separation | | lone | <0.1 mm | 0.1–1 mm | 1–5 mm | >5 mm | | |
| | (6 | (6) | | (4) | (1) | (0) | | |
| Roughness | V | ery rough | Rough | Slightly rough | Smooth | Slickensided | | |
| | (6 | 5) | (5) | (3) | (1) | (0) | | |
| Infilling | | Hard fill | ing | | Soft filling | | | |
| | None | <5 mm | | >5 mm | <5 mm | >5 mm | | |
| | (6) | (4) | | (2) | (2) | (0) | | |
| Weathering | Unweathered | Slightly | weathered | Moderately weathered | Highly weathered | Decomposed | | |
| | (6) | (5) | | (3) | (1) | (0) | | |
| | | | | | | | | |

 Table 2 Guidelines for classification of CD

 Table 3
 Data combination which is used to synthesize inputs-output database of ANN-CD&CG for the training and testing phases

| Discontinuity length (m) | Separation (mm) | Infilling (mm) | Groundwater (lt/min) | Rating | | |
|-----------------------------|-----------------|-------------------|-------------------------|--------|--|--|
| 0.5 | 0 | 0 | 0 | 0 ~ 33 | | |
| 2 | 0.05 | 2.5 | 5 | | | |
| 6.5 | 0.55 | 6 | 17.5 | | | |
| 15 | 3 | -2.5 | 75 | | | |
| 21 | 6 | -6 | 126 | | | |

 Table 4 Effect of discontinuity strike and dip orientations (OD) in tunneling

| Strike perpendicular to tunnel axis | | | | | | | | |
|-------------------------------------|------------------|-----------------|-------------|--|--|--|--|--|
| Drive with dip Drive against dip | | | | | | | | |
| Dip 45–90 | Dip 20-45 | Dip 45–90 | Dip 20-45 | | | | | |
| Very favorable | Favorable | Fair | Unfavorable | | | | | |
| Strike parallel to the | unnel axis | Irrespective of | strike | | | | | |
| Dip 20-45 | Dip 45–90 | Dip 0–20 | | | | | | |
| Fair | Very unfavorable | Fair | | | | | | |

ANN designed for condition of discontinuities and condition of groundwater (ANN-CD&CG) A database for CD and CG is built by means of parameter ratings which are given by the tables. Six hundred and twenty five possible situations of ratings are selected, and related scores are derived from Tables 1 and 2, item 5. This database is used in training and testing of the ANN-CD&CG; in this way, 313 and 312 out of 625 data of ANN inputs–output pairs are used in training and testing phases, respectively. The ranges of training and testing data used in the ANN-CD&CG classifier are given in Table 3. The parameters are trained in a MLP. The Levenberg–Marquard Backpropagation learning algorithm is used in training Feed-Forward MLP [13].

Structural and operational properties of the ANN-CD& CG can be summarized as follow:

- 1. Discontinuity, separation, infilling, and groundwater are the four inputs of the MLP.
- 2. There is one output as discontinuity length and groundwater condition are calculated as ratings. Output layer of the neuron's activation function is chosen linearly.
- 3. The activation functions of neurons in the hidden layer(s) are chosen hyperbolic tangent. In addition to the hybrid structures of ANNs network optimization proposed by Lagaros et al. [12], architectures of ANNs are generally determined empirically. In this study, optimum hidden layer(s) and number of neurons in each layer are experimentally determined.
- 4. All the initial weights of the network are determined using Nguyen-Widrow algorithm [14].
- 5. Discontinuity, separation, and infilling parameters are divided by 10, and groundwater is divided by 100 to obtain training and testing data of the network. To normalize, discontinuity length and groundwater condition are also divided by 100 to increase the sensibility of the network to the minor changes.
- 6. 313 and 312 out of 625 data which were built for the parameters represent inputs and output of the network are used in training and testing, respectively.

Table 5 Rating adjustment for OD

| Strike and dip orienta | tions of discontinuities | Very favorable | Favorable | Fair | Unfavorable | Very unfavorable |
|------------------------|--------------------------|----------------|-----------|------|-------------|------------------|
| Ratings | Tunnels and mines | 0 | -2 | -5 | -10 | -12 |



Fig. 2 Unified simulation model for total RMR rating



Fig. 3 ANNs structure

ANN designed for orientation of discontinuities (ANN-OD) A database for OD conditions is built by means of parameter ratings. This database is used in training and testing of ANN-OD classifier. The training and testing database, which is relatively shorter for depicting than that of ANN-CD&CG, is given in Table 6. The parameters given in Table 6 are trained in a MLP. The Levenberg– Marquard Backpropagation learning algorithm is used in training Feed-Forward MLP [13].

Structural and operational properties of ANN-OD classifier can be summarized as follow:

Table 6 The training-testing data for ANN-CD&CG classifier

| Strike | Dip | Rating | Strike | Dip | Rating |
|--------|--------|--------|--------|--------|--------|
| 0 | -90 | -7.44 | 45 | 45 | -3.24 |
| 0 | -45 | -3.90 | 45 | 90 | -5.46 |
| 0 | -33.50 | -3.48 | 90 | -90 | -3.48 |
| 0 | -10 | -3.48 | 90 | -45 | -7.44 |
| 0 | 0 | -3.48 | 90 | -33.50 | -7.44 |
| 0 | 10.60 | 3.54 | 90 | -10 | -3.48 |
| 0 | 20.50 | -4.05 | 90 | 0 | -3.48 |
| 0 | 32 | -3.48 | 90 | 10.60 | -3.54 |
| 0 | 45 | -3.90 | 90 | 20.50 | -4.08 |
| 0 | 90 | -7.44 | 90 | 32 | -2.04 |
| 0 | 38 | -5 | 90 | 45 | -1.92 |
| 0 | 66 | -12 | 90 | 90 | -0.48 |
| 45 | -90 | -6 | 90 | 82 | -5 |
| 45 | -45 | -6 | 90 | 40 | -10 |
| 45 | -33.5 | -6 | 90 | 65 | -2 |
| 45 | -10 | -4.08 | | | |
| 45 | 0 | -4.08 | | | |
| 45 | 10.60 | -4.08 | | | |
| 45 | 20.50 | -3.24 | | | |
| 45 | 32 | -3.24 | | | |

- 1. MLP has two inputs: strike and dip.
- 2. There is one output which is rating of strike and dip conditions (OD). Output layer of the neuron's activation function is chosen linearly.



Fig. 4 MSE values of the ANN-OD





Table 7 OD rating adjustments of the tunnels

- 3. The activation functions of 16 neurons in the hidden layer are chosen hyperbolic tangent.
- 4. All the initial weights of the network are determined using Nguyen-Widrow algorithm [14].
- 5. Strike and dip parameters are divided by 10 to obtain training data of the network.

3 Results and discussion

Two neural network classifiers are analyzed in Sect. 2 to constitute the total RMR rating in USM.

To a given problem, the number and structure of operation units of input and output layers differ in any ANN applications. In order to determine an optimum architecture, every training data were investigated for different number of hidden layer(s) and neurons.

Considering both training and testing, the architecture of the ANN-CD&CG for one hidden layer with sixteen neurons gives the best solution.

Also, the same architecture was used for the second classifier, which is named as ANN-OD. The iteration steps and the corresponding MSEs of the ANN-OD are given in Fig. 4 as an example.

Absolute error values (AEV) are also given in Fig. 5, which is built by the network for training data due to target vectors. The couples of min and max AEV for training data are 3.5548×10^{-5} to 7.2907×10^{-2} . Percentage of mean AEV are determined as 0.0199 for the training data.

After the training, the MSE—percentage MSE values of ANN-CD&CG and ANN-OD classifiers are evaluated as 8.9469×10^{-6} to 1.4315×10^{-6} and 2.8756×10^{-4} to 8.2161×10^{-4} , respectively. Trained networks were used

| Tunnels | 1 | 2 | 3 | 4 | 5 |
|--------------------------------|---|---|--|---|---|
| Strike and dips | Strike is perpendicular to tunnel axis (90°) and drive is against dip (82°) | Strike is perpendicular to tunnel axis (90°) and drive is against dip (40°) | Strike is perpendicular to tunnel axis (90°) and drive is with dip (65°) | Strike is parallel to tunnel axis (0°) and dip is (38°) | Strike is parallel to tunnel axis (0°) and dip is (66°) |
| Rating adjustment for OD | Ratings of tunnels (convent) -5/-5.001 | ional/USM) —10/—9.998 | -2/-2 | -5/-4.989 | -12/-12 |

Table 8 Total RMR ratings

| Fotal RMR ratings (conventional—USM) | | | | | | | | | | |
|--------------------------------------|-------|----------|----------|-----------|-----------|-------|----------|-------|----------|--|
| Tunnel 1 | | Tunnel 2 | Tunnel 2 | | Tunnel 3 | | Tunnel 4 | | Tunnel 5 | |
| 73.00 | 65.77 | 60.90 | 58.92 | 90.00 | 89.93 | 53.70 | 52.44 | 40.90 | 39.58 | |
| Good | Good | Good | Fair | Very Good | Very Good | Fair | Fair | Fair | Poor | |
| Rock | Rock | Rock | Rock | Rock | Rock | Rock | Rock | Rock | Rock | |

in USM model design as ANN classifiers to determine total RMR rating.

In the assessment of the tunneling cases, five data sets of different rock masses were used as classification parameters in this study. In Table 7, the comparison of OD rating

 Table 9 Rock mass classes determined from total ratings

| | | | | | * |
|-------------|-------------------|--------------|--------------|--------------|-------------------|
| Class no | Ι | II | III | IV | V |
| Description | Very good rock | Good rock | Fair rock | Poor rock | Very poor rock |
| Rating | 100 ← 81 | 80 ← 61 | 60 ← 41 | 40 ← 21 | <20 |

Table 10 Input values of the cases for the CD and CG parameters

| Parameter | Tunnels | | | | | | | |
|--------------------------|---------|-----|------|-----|-------|--|--|--|
| | 1 | 2 | 3 | 4 | 5 | | | |
| CD | | | | | | | | |
| Discontinuity length (m) | 6.5 | 8 | 10 | 2.5 | 5 | | | |
| Separation (mm) | 0.05 | 0.4 | 0.01 | 1 | 0.05 | | | |
| Infilling (mm) | 0.04 | 0.3 | 0.01 | 1 | -0.05 | | | |
| Roughness (rating) | 3 | 3 | 5 | 3 | 3 | | | |
| Weathering (rating) | 6 | 5 | 6 | 3 | 3 | | | |
| CG | | | | | | | | |
| Groundwater (lt/min) | 4 | 1 | 0 | 10 | 20 | | | |

Table 11 Parameters of tunnels for basic RMR

adjustments of conventional method and ANN-OD model is given.

The total rating results obtained from the conventional and USM methods compared in Table 8. Then, rock mass classes are determined by means of Table 9.

The values obtained from conventional and USM belong to 5 different derivation tunnels parameters. Parameters of CD are given in the first 5 rows, and the CG is given in the sixth row in Table 10. Also, the numerical values correspond to linguistic terms are given in the same table.

In USM, infilling is divided into two parts depending on hard or soft filling. For instance, when the separation is 0.05 mm and infilling is hard then its value is taken as +0.005 and is taken -0.005 when infilling is soft with the 0.05-mm separation. These values are used as inputs of ANN-CD&CG in the USM.

The change of inflow of groundwater to the tunnel (CG) is represented between 0 and 126 lt/min in USM.

The difference of ratings between two methods reaches up to 7.43. This change is because of having the same value for a wide range in conventional method.

Regarding to the total RMR sum, rock masses of the 2nd and 5th cases fall into good and fair rock classes in conventional method whereas good and fair rock classes in USM as shown in Table 8, respectively.

Using the guides given in Tables 1, 2, and 3, descriptions and measurements of SD for the cases are carried out (Table 10).

| Parameter | Input of | lata | | | | | | | | | |
|---|------------------------|---------------|--|-------|------------------------|-------|------------------------|--------|--|-------------|--|
| Tunnels | 1 | 1 | | 2 | | 3 | | | 5 | | |
| 1. Uniaxial compressive strength, UCS (MPa) | 150 | | 125 | | 245 | 245 | | | 60 | | |
| Drill core quality RQD (%) | 85 | | 85 | | 92 | 92 | | 73 | | 60 | |
| 3. Spacing of discontinuity, SD (mm) | 285 | | 190 | 190 | | 1800 | | | 120 | | |
| 4. Discontinuity, CD, and groundwater, CG | Very rough surfaces | | Slightly rough surfaces | | Very rough surfaces | | Very rough surfaces | | Slightly rough surfaces | | |
| | Separation < 1 mm | | Separation < 1 mm Slightly weathered walls | | Separation < 1 mm | | Separation < | < 1 mm | Separation < 1 Slightly weat walls | mm hered | |
| Parameter I | Ratings | (Conventional | l – USM) | | | | | | | | |
| Tunnels | l | | 2 | | 3 | | 4 | | 5 | | |
| 1. UCS (MPa) | 12.30 | 12.43 | 11.20 | 11.13 | 14.90 | 15.06 | 9.00 | 9.2 | 5 6.70 | 6.60 | |
| 2. RQD (%) | 17.00 | 17.15 | 17.00 | 17.15 | 18.10 | 18.72 | 14.20 | 14.6 | 0 11.90 | 12.03 | |
| 3. SD (mm) | 8.70 | 8.31 | 7.70 | 7.33 | 19.00 | 19.12 | 7.50 | 6.9 | 6 7.30 | 6.58 | |
| 4. CD and CG | 40.00 | 32.88 | 35.00 | 33.30 | 40.00 | 39.04 | 28.00 | 26.6 | 2 27.00 | 26.36 | |
| Basic RMR rating | 78.00 | 70.77 | 70.90 | 68.92 | 92.00 | 91.93 | 58.70 | 57.4 | 3 52.90 | 51.58 | |

Basic RMR rating is calculated by means of Table 11. For total RMR rating, the sixth parameter, the effect of OD, is evaluated in Table 7. Rock mass classes of the tunnels are determined by means of Table 9 due to their total RMR ratings.

4 Conclusion

Bieniawski reported the deficiency stems from the abrupt changes in borderline cases [3]. Since ANN in USM take whole effects into consideration, in details, more sensitive and exact results are obtained.

The rock masses discussed in 2nd and 5th tunnels therefore fall in a more realistic class, that is, fair and poor rock classes, whereas good and fair rock classes in conventional method which makes a rougher evaluation as indicated. This rough evaluation possibly will cause misevaluation of support of rock tunnels and contractual problems. It could be concluded that RMR overestimates the rock classes considering these five cases (tunnels).

Taking into consideration the values of % 1.4315×10^{-6} and 2.8756×10^{-4} of MSEs for ANN-CD&CG and ANN-OD, ANN classifiers used in USM estimate more effective total RMR. Developing a single ANN classifier consisting of all parameters as inputs is proposed for future works.

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