<span id="page-0-0"></span>ORIGINAL ARTICLE

# Neural computing models for prediction of permeability coefficient of coarse-grained soils

Is¸ık Yilmaz • Marian Marschalko • Martin Bednarik • Oğuz Kaynar · Lucie Fojtova

Received: 17 June 2010 / Accepted: 27 January 2011 / Published online: 17 February 2011 - Springer-Verlag London Limited 2011

Abstract Correlations are very significant from the earliest days; in some cases, it is essential as it is difficult to measure the amount directly, and in other cases it is desirable to ascertain the results with other tests through correlations. Soft computing techniques are now being used as alternate statistical tool, and new techniques such as artificial neural networks, fuzzy inference systems, genetic algorithms, and their hybrids were employed for developing the predictive models to estimate the needed parameters, in the recent years. Determination of permeability coefficient  $(k)$  of soils is very important for the definition of hydraulic conductivity and is difficult, expensive, time-consuming, and involves destructive tests. In this paper, use of some soft computing techniques such as ANNs (MLP, RBF, etc.) and ANFIS (adaptive neurofuzzy inference system) for prediction of permeability of coarse-grained soils was described and compared. As a result of this paper, it was obtained that the all constructed soft computing models exhibited high performance for

I. Yilmaz  $(\boxtimes)$ 

Faculty of Engineering, Department of Geological Engineering, Cumhuriyet University, 58140 Sivas, Turkey e-mail: iyilmaz@cumhuriyet.edu.tr

M. Marschalko - L. Fojtova

Faculty of Mining and Geology, Institute of Geological Engineering, VŠB-Technical University of Ostrava, 17. listopadu 15, 708 33 Ostrava, Czech Republic

#### M. Bednarik

Faculty of Natural Sciences, Department of Engineering Geology, Comenius University, Mlynská dolina, 842 15 Bratislava, Slovak Republic

O. Kaynar

Department of Management Information System, Cumhuriyet University, 58140 Sivas, Turkey

predicting k. In order to predict the permeability coefficient, ANN models having three inputs, one output were applied successfully and exhibited reliable predictions. However, all four different algorithms of ANN have almost the same prediction capability, and accuracy of MLP was relatively higher than RBF models. The ANFIS model for prediction of permeability coefficient revealed the most reliable prediction when compared with the ANN models, and the use of soft computing techniques will provide new approaches and methodologies in prediction of some parameters in soil mechanics.

Keywords ANN · MLP · RBF · ANFIS · Soft computing - Soils - Grain size - Permeability

# 1 Introduction

It generally has been recognized that grain size is a fundamental independent variable controlling permeability in unconsolidated sediments. Previous theoretical and empirical investigations into the relationship between particle size and inter-granular permeability have resulted in the well-known formula (Eq. 1) for intrinsic permeability. In Eq. 1,  $d$  is particle diameter and  $c$  is dimensionless constant [\[1](#page-10-0)].

$$
k = cd^2 \tag{1}
$$

Since permeability is the measure of the ease with which water moves through aquifer material, certain relationships must exist between permeability and the statistical parameters that describe the grain-size distribution of the porous mediums.

Soft computing techniques—such as fuzzy logic, artificial neural networks, genetic algorithms, and neuro-fuzzy

<span id="page-1-0"></span>systems, which were first used in design of higher technology products—are now being used in many branches of sciences and technologies, and their popularities gradually increase.

Earth sciences aim to describe very complex processes and are in need of new technologies for data analyses. The number of researches in evolutionary algorithms and genetic programming, neural science and neural net systems, fuzzy set theory and fuzzy systems, fractal and chaos theory, and chaotic systems aiming the solution of problems in earth sciences (estimation of parameters; susceptibility, risk, vulnerability and hazard mapping; interpretation of geophysical measurement results; many kinds of mining applications; etc.) was especially increased in the last 5–10 years.

Correlations have been a significant part of scientific researches from earliest days. In some cases, it is essential as it is difficult to measure the amount directly, and in other cases it is desirable to ascertain the results with other tests through correlations. The correlations are generally semiempirical based on some mechanics or purely empirical based on statistical analysis [[2\]](#page-10-0).

However, determination of permeability coefficient  $(k)$  of a soil is time-consuming, expensive, and involves destructive tests. If reliable predictive models could be obtained between  $k$  with quick, cheap, and nondestructive test results such as grain-size distribution parameters, it would be very valuable for the estimation of  $k$ .

The study presented herein aims to predict the permeability coefficient  $(k)$  of the coarse-grained soils due to grain-size distribution curves using a few soft computing techniques (artificial neural networks—ANN and adaptive neuro-fuzzy inference system—ANFIS) and to compare the models in prediction capability point of view. Soil samples have been collected from various locations of Ostrava (Czech Republic) and tested. The tests included grain-size distribution and permeability coefficient; and  $d_{10}$ ,  $d_{30}$ , and  $d_{60}$  were first correlated with k; and statistically significant models were selected. In order to establish predictive models, soft computing techniques such as artificial neural networks and neuro-fuzzy models were used, and prediction performances were then analyzed.

#### 2 Perspective and purpose

Especially in water-bearing soils, permeability is one of the most important characteristics that significantly affect groundwater flow. Permeability represents the ability of a porous medium to transmit water through its interconnected voids. Accurate estimation of permeability is considered crucial for successful groundwater development and management practices. Grain-size distribution mainly controls the intrinsic permeability of medium, and increase in grain size increases the permeability due to the large pore openings. Moreover, sorting and uniformity of the grain size are also very important for permeability. Permeability decreases in poorly sorted soils because of the fine grains in pore spaces, while uniform soils have greater permeability coefficient than non-uniform soils.

Statistical grain-size distribution analyses are cheaper and lesser dependent on the geometry and hydraulic boundaries of the aquifer but reflect almost all the transmitting properties of the media [\[3](#page-10-0)]. That is why numerous attempts have been made to define the relationship between permeability and grain-size distribution of soil. Some wellknown examples of these researches are as follows.

Hazen [[4\]](#page-10-0) first proposed a relationship (Eq. [1](#page-0-0)) between k and effective grain size  $(d_{10})$ . Shepherd [[1\]](#page-10-0) extended Hazen's work by performing power regression analysis on 19 sets of published data for unconsolidated sediments. The data sets ranged in size from 8 to 66 data pairs. He found that the exponent in Eq. [1](#page-0-0) varies from 1.11 to 2.05 with an average value of 1.72 and that the value of the constant  $c$  is most often between 0.05 and 1.18 but can reach a value of 9.85. Values for both  $c$  and the exponent are typically higher for well-sorted samples with uniformly sized particles and highly spherical grains. Uma et al. [[5\]](#page-10-0) suggested an equation to estimate the Ks and transmissivity of sandy aquifers of the same form as Eq. [1,](#page-0-0) with  $c$  values that depend on the nature of the geologic environment. Krumbein and Monk [\[6](#page-10-0)] proposed an equation based on experiments performed with sieved glacial outwash sands that were recombined to obtain various grain-size distributions. Kozeny [[7\]](#page-10-0) proposed an equation based on porosity and specific surface. Rawls and Brakensiek [[8\]](#page-10-0) used field data from 1,323 soils across the United States to develop a regression equation that relates porosity  $n$ , percentages of sand- and clay-sized particles in the sample. Jabro [[9\]](#page-10-0) estimated permeability from grain-size and bulk density data. Sperry and Peirce [[10\]](#page-10-0) developed a linear model to estimate permeability based on grain size, shape, and porosity. Lebron et al. [\[11](#page-10-0)] sought to improve upon permeability prediction methods by quantifying the characteristics of the pore spaces at a microscopic scale [[12\]](#page-10-0).

However, many attempts were done for the estimation of k; correlation coefficients  $(R^2)$  of the models were generally lower than  $\sim 0.80$ ; and whole grain-size distribution curves were not included in the assessments.

Alyamani and Sen [[3\]](#page-10-0) included more information about the entire grain-size distribution curve by relating  $k$  to the initial slope and intercept of the curve for 32 sandy soil samples obtained in Saudi Arabia and Australia, and proposed the following equation:

$$
k = 1.505 * [Io + 0.025 * (d50 - d10)]2
$$
 (2)

in Eq. [2](#page-1-0), k is expressed in cm/s,  $I_0$  is x-intercept of the straight line formed by joining  $d_{50}$  and  $d_{10}$  of the grain-size distribution curve (mm). Alyamani and Sen [[3\]](#page-10-0) found that a log–log plot of k versus  $[I_0 + 0.025 * (d_{50} - d_{10}]$  for their data set yielded a straight line having an  $R^2 = 0.94$ .

In the useful suggested method of Alyamani and Sen [\[3](#page-10-0)], an extra graph, which is plotted by calculated percentiles corresponding to increments of 5% starting from 5% ( $d_5$ ,  $d_{10}$ ,  $d_{15}$ ,  $d_{20}$ ,..., $d_{95}$ ), is needed.  $I_0$  is then calculated from intercept of the straight-line drawn by joining  $d_{50}$  and  $d_{10}$  of this graph.

In order to predict the permeability coefficient from grain-size distribution curves directly, some neural computing models were constructed in this paper, and more information about the entire grain-size distribution curve relating to uniformity and sorting degree was included in the assessment of  $k$ . For grain-size distribution analyses and determination of permeability coefficient, selected 243 soil sample sets were first tested according to American Society for Testing and Materials (ASTM) guidelines [\[13](#page-10-0), [14\]](#page-10-0). These analyses were performed on the samples collected from the various locations of Ostrava (Czech Republic). After drawing the grain-size distribution curves, as the parameters of uniformity and sorting degree,  $d_{10}$ (grain-size diameter at which  $10\%$  by weight),  $d_{30}$  (grainsize diameter at which 30% by weight), and  $d_{60}$  (grain-size diameter at which 60% by weight) were then determined from the grain-size distribution curves. The results obtained from the experiments and their basic test statistics are tabulated in Table 1.

#### 3 Data sets used in the models

In order to establish relationships among the parameters obtained in this study, simple regression analyses were first performed, and relations between k with  $d_{10}$  (grain-size diameter at which 10% by weight),  $d_{30}$  (grain-size diameter at which 30% by weight), and  $d_{60}$  (grain-size diameter at which 60% by weight) were analyzed employing linear, power, logarithmic, and exponential functions (Table 2). Regression equations were established among  $k$  with grainsize distribution analyses results (Table 3), and it was found that the relationships were not statistically enough

Table 1 Basic statistics of the results obtained from analyses

	$k$ (*10 <sup>-6</sup> )	$d_{10}$	$d_{30}$	$d_{60}$
Minimum	0.0001	0.0017	0.011	0.0285
Maximum	0.005	0.65	17	43
Average	0.00051187	0.199	2.569	12.631
Std. dev.	0.00071	0.119	3.318	9.586

Unit of  $d$  is mm

Table 2 Correlation coefficients  $(R^2)$  obtained from the simple regressions between k with  $d_{10}$ ,  $d_{30}$ ,  $d_{60}$ 

Model	$d_{10}$	$D_{30}$	$D_{60}$
Linear	0.505	0.599	0.516
Logarithmic	0.162	0.351	0.164
Exponential	0.557	0.616	0.526
Power	0.179	0.387	0.192

Bold values show the highest correlation coefficients  $(R^2)$ 

strong to establish significant models by traditional statis-tical methods. Figure [1](#page-3-0) shows the plot of the k versus  $d_{10}$ ,  $d_{30}$ , and  $d_{60}$ . However, exponential regression models are relatively stronger than other models (Table 2). That is why some soft computing techniques were used for prediction of permeability coefficient from  $d_{10}$ ,  $d_{30}$ , and  $d_{60}$ .

Multiple regression analysis was also carried out to correlate the measured permeability to three grain-size parameters, namely,  $d_{10}$ ,  $d_{30}$ , and  $d_{60}$  (Table [4\)](#page-3-0). Multiple regression model to predict permeability is given below.

$$
k = (0.004)d_{10} + (3.4 \times 10^{-5})d_{30} + (8.6 \times 10^{-6})d_{60}
$$
 (3)

In fact, the coefficient of correlation between the measured and predicted values is a good indicator to check the prediction performance of the model. Figure [2](#page-4-0) shows the relationships between measured and predicted values obtained from the MR model for S%, with a poor correlation coefficient ( $R^2 = 0.587$ ).

## 4 An overview of Artificial Neural Network (ANN) models

When the materials are natural materials, there will be faced many uncertainty and material will never be known with certainty. That is why some methodologies in artificial neural networks, fuzzy systems, and evolutionary computation have been successfully combined, and new techniques called soft computing or computational intelligence have been developed in recent years. These techniques are attracting more and more attention in several research fields because they tolerate a wide range of uncertainty [\[15](#page-10-0)].

Artificial neural networks are data processing systems devised via imitating brain activity and have performance characteristics like biological neural networks. ANN has a

**Table 3** Predictive models for the assessment of  $k$ 

	Predictive model	$R^2$
$k - d_{10}$	$k$ (*10 <sup>-6</sup> ) = 0.0001 e <sup>5.6231(d</sup> ) <sub>10</sub>	0.557
$k - d_{30}$	$k$ (*10 <sup>-6</sup> ) = 0.0002 e <sup>0.2133(d</sup> <sub>30</sub> )	0.616
$k - d_{60}$	$k$ (*10 <sup>-6</sup> ) = 0.0001 e <sup>0.0682(d)</sup> 60	0.526

<span id="page-3-0"></span>Fig. 1 k versus  $d_{10}$ ,  $d_{30}$ ,  $d_{60}$ graphics



**Table 4** Model summaries of multiple regressions for prediction of  $k$ 



lot of important capabilities such as learning from data, generalization, working with unlimited number of variable [\[16](#page-10-0)]. Neural networks may be used as a direct substitute for auto correlation, multivariable regression, linear regression, trigonometric, and other statistical analysis and techniques [\[17](#page-10-0)]. Neural networks, with their remarkable ability to derive meaning from complicated or imprecise data, can be used to extract patterns and detect trends that are too complex to be noticed by either humans or other computer techniques [\[18](#page-10-0), [19](#page-10-0)]. Rumelhart and McClelland [\[20](#page-10-0)] reported that the main characteristics of ANN include large-scale parallel distributed processing, continuous nonlinear dynamics, collective computation, high fault tolerance, self-organization, self-learning, and real-time treatment. A trained neural network can be thought of as an "expert" in the category of information it has been given to

<span id="page-4-0"></span>Fig. 2 Cross-correlation of predicted and observed values of k obtained from multiple regression analysis



analyze. This expert can then be used to provide projections given new situations of interest and answer ''what if'' questions [\[21](#page-10-0)].

The most commonly used algorithms are multilayer feed-forward artificial neural network (multiple layer perceptron-MLP) and radial basis function network (RBFN). The radial basis function network (RBFN) is traditionally used for strict interpolation problem in multi-dimensional space and has similar capabilities with MLP neural network which solves any function approximation problem [\[22](#page-10-0)]. RBFs were first used in design of neural network by Broomhead and Lowe [[23\]](#page-10-0), who showed how a nonlinear relationship could be modeled by RBF neural network, and interpolation problems could be implemented [[23\]](#page-10-0). The main two advantages of RBFN are

- (a) Training of networks in a short time than MLP [[24\]](#page-11-0),
- (b) Approximation of the best solution without dealing with local minimums [\[25](#page-11-0)].

Moreover, RBFN are local networks compared to the feed-forward networks which perform global mapping. Otherwise, RBFN uses a single set of processing units, and each of these units is most receptive to a local region of the input space [[26\]](#page-11-0). That is why, RBFN are used as an alternative neural network model in applications of function approximation, time series forecasting as well as classifying task in recent years [[27–35\]](#page-11-0).

The structure of RBFN is composed of three layers (Fig. 3), and the main distinction between MLP and RBFN is the number of the hidden layer. RBFN has only one hidden layer, which contains nodes called RBF units, and radially symmetric basis function is used as activation functions of hidden nodes.

The input layer serves as an input distributor to the hidden layer. Different from MLP, the values in input layer are forwarded to hidden layer directly without being multiplied by weight values. The hidden layer unit measures the distance between an input vector with the center of its radial function and produces an output value depending on the distance. The center of radial basis function is called



Fig. 3 Architecture of radial basis function network (RBF)

reference vector. The closer input vector is to the reference vector, the more the value is produced at the output of hidden node. However, a lot of radial basis functions are suggested for using in hidden layer (Gaussian, Multi-Quadric, Generalized Multi-Quadric, Thin Plate Spline), Gaussian function is the most widely used in applications. Chen et al. [[27\]](#page-11-0) indicate that the choice of radial basis function used in network does not significantly affect performance of network. The activation function of the individual hidden nodes defined by the Gaussian function is expressed as follows:

$$
\phi_j = e^{\left[\frac{\left|\left|x-c_j\right|\right|^2}{\sigma_j^2}\right]} \quad j = 1, 2 \dots, L \tag{4}
$$

where  $\phi_i$  denotes the output of the *j*th node in hidden layer,  $\Vert \cdot \Vert$  is Euclidian distance function which is generally used in applications, X is the input vector,  $C_i$  is center of the jth Gaussian function,  $\sigma_i$  is radius which shows the width of the Gaussian function of the jth node, and  $L$  denotes the number of hidden layer nodes.

In the next step, the neurons of the output layer perform a weighted sum using the hidden layer outputs and the weights which connect hidden layer to output layer. Output of network can be presented as a linear combination of the basis functions:

$$
y_k = \sum_{j=1}^{L} \phi_j w_{kj} + w_{k0}
$$
 (5)

where  $w_{ki}$  is the weight that connects hidden neuron j and output neuron  $k, w_{k0}$  is bias for the output neuron.

#### 5 Artificial neural network models for prediction of  $k$

All data were first normalized and divided into three data sets, such as, training (1/2 of all data), test (1/4 of all data), and verification (1/4 of all data). In this study, Matlab 7.1 [\[36](#page-11-0)] software was used in neural network analyses having a three-layer feed-forward network, and models were constructed by MLP and RBF architectures.

#### 5.1 MLP models for prediction of  $k$

In this study, permeability coefficients of soils were first predicted indirectly by using the MLP algorithm. They consist of an input layer (3 neurons), one hidden layer (10 neurons), and one output layer (Fig. 4). In the analyses network parameters of learning parameters, momentum parameters, networks training function, and activation (transfer) function for all layer were respectively adjusted to 0.01, 0.9, trainLm, and tansig. As in many other network training methods, models and parameters were used to be



Fig. 4 MLP model used in this study<br>listed below.

Fig. 5 Cross-correlation of predicted and observed values of k for MLP model

able to reach minimum RMS values, and network goal was reached at the end of 437 iterations.

In fact, the coefficient of determination between the measured and predicted values is a good indicator to check the prediction performance of the model. Figure 5 shows the relationships between measured and predicted values obtained from the models for  $k$ , with good coefficient of determinations. In this study, variance account for (VAF) (Eq. 6) and root mean square error (RMSE) (Eq. 7) indices were also calculated to control the performance of the prediction capacity of predictive models developed in the study as employed by Alvarez and Babuska [[37,](#page-11-0) Finol et al. [[38\]](#page-11-0), Yilmaz and Yüksek [\[39](#page-11-0), [40](#page-11-0)]:

$$
VAF = \left[1 - \frac{var(y - y')}{var(y)}\right] \times 100\tag{6}
$$

RMSE = 
$$
\sqrt{\frac{1}{N} \sum_{i=1}^{N} (y - y')^{2}}
$$
 (7)

where y and  $y'$  are the measured and predicted values, respectively. If the VAF is 100 and RMSE is 0, then the model will be excellent. The obtained values of VAF and RMSE given in Table [5](#page-6-0) indicated a high prediction performance.

## 5.2 RBF models for prediction of  $k$

Training of RBF networks contains process of determination of center vector  $(C_i)$ , radius value  $(\sigma_i)$ , and linear weight values  $(w_{ki})$ . Two-stage hybrid learning algorithm is used to train RBF networks in general. In the first stage of hybrid learning algorithm, center and width of RBFs in hidden layer are determined by using unsupervised clustering algorithms or randomly selected from given input data set. Output weight is calculated in the second stage. A lot of methods are proposed in literature to determine the center and width of reference vector, and some of them are



<span id="page-6-0"></span>**Table 5** Performance indices (RMSE, VAF, and  $R^2$ ) for models used

Model	<b>RMSE</b>	VAF $(\%)$	$(R^2)$
ANN-MLP	0.00015	93.234	0.933
ANN-RBF (exact)	0.00016	91.481	0.915
ANN—RBF (k means)	0.00018	88.947	0.891
ANN-RBF (SOM based)	0.00017	90.896	0.912
<b>ANFIS</b>	0.00006	96.711	0.973

RMSE Root mean square error, VAF Value account for

Number of hidden neurons is set to the number of training examples, and all input vectors are also used as centers of RBFs. In other words, for each point in input space, one radial basis function is determined. This case is named as "*Exact RBF*". There are two disadvantages of Exact RBF such as size problem and overtraining problem. Size problem causes calculation complexity when data set is too large. Network is over trained with these noisy data, so the performance of the system for test data will not as good as performance of training data. To reduce calculating complexity and to deal with overtraining problem, the number of neurons in hidden layer is reduced as smaller than the number of sample in input data set, and central vectors are chosen from input vectors randomly.

Pruning or growing methods start with a number of prespecified hidden neuron and iteratively, and continues by adding/removing hidden neurons to/from RBFN. The network structure that has minimum testing and training error is selected as a final model of RBFN. In this iterative process, parameters of hidden nodes are randomly selected from input vectors or determined by using clustering methods. In order to determine central vectors with clustering methods, input vectors are devoted to certain number of clusters by using clustering algorithms, such as, k means, Self-Organization Map (SOM), and cluster centers are then used as RBF centers.

In the analyses, three different algorithms of RBF such as Exact RBF, RBF trained with  $k$  means, and RBF trained

with SOM were used in prediction of  $k$ . However, three models consist of 3 neurons in input layer and one output layer; the neuron numbers in the hidden layer of Exact RBF, RBF trained with  $k$  means, and RBF trained with SOM were, respectively, 26, 41, 37.

Cross-correlations between predicted and observed values (Figs. 6, [7](#page-7-0), [8](#page-7-0)), RMSE, and VAF values indicated that the three models of RBF constructed are highly acceptable for prediction of k. RMSE, VAF, and  $R^2$  values are also tabulated in Table 5.

## 6 Adaptive Neuro-Fuzzy Inference System model for prediction of  $k$

In ANFIS, both of the learning capabilities of a neural network and reasoning capabilities of fuzzy logic were combined in order to give enhanced prediction capabilities, when compared to using a single methodology alone. The goal of ANFIS is to find a model or mapping that will correctly associate the inputs (initial values) with the target (predicted values). The fuzzy inference system (FIS) is a knowledge representation where each fuzzy rule describes a local behavior of the system. The network structure that implements FIS and employs hybrid learning rules to train is called ANFIS.

Let  $X$  be a space of objects and  $x$  be a generic element of X. A classical set  $A \subseteq X$  is defined as a collection of elements or objects  $x \in X$  such that each x can either belong or not belong to the set A. By defining a characteristic function for each element  $x$  in  $X$ , we can represent a classical set A by a set of ordered pairs  $(x, 0)$  or  $(x, 1)$ , which indicates  $x \neq A$  or  $x \in A$ , respectively. On the other hand, a fuzzy set expresses the degree to which an element belongs to a set. Hence, the characteristic function of a fuzzy set is allowed to have values between 0 and 1, which denotes the degree of membership of an element in a given set. So a fuzzy set A in X is defined as a set of ordered pairs:





Fig. 7 Cross-correlation of predicted and observed values of  $k$  for RBF ( $k$  means) model

<span id="page-7-0"></span>



Fig. 8 Cross-correlation of predicted and observed values of k for RBF (SOM) model

$$
A = \{(x, \mu A(x)) | x \in X\}
$$
\n
$$
(8)
$$

where  $\mu A(x)$  is called the *membership function* (MF) for the fuzzy set A.

The MF maps each element of  $X$  to a membership grade (or a value) between  $0$  and  $1$ . Usually,  $X$  is referred to as the universe of discourse or simply the universe. The most widely used MF is the generalized bell MF (or the bell MF), which is specified by three parameters  $\{a, b, c\}$  and defined as [[41\]](#page-11-0)

bell 
$$
(x; a, b, c) = 1/(1 + |x - (c/a)|^{2b})
$$
 (9)

Parameter  $b$  is usually positive. A desired bell MF can be obtained by a proper selection of the parameter set  ${a, b, c}$ . During the learning phase of ANFIS, these parameters are changing continuously in order to minimize the error function between the target output values and the calculated ones [\[42](#page-11-0), [43\]](#page-11-0).

The proposed neuro-fuzzy model of ANFIS is a multilayer neural network-based fuzzy system. Its topology is shown in Fig. [9,](#page-8-0) and the system has a total of five layers. In this connected structure, the input and output nodes represent the training values and the predicted values, respectively, and in the hidden layers, there are nodes functioning as membership functions (MFs) and rules. This architecture has the benefit that it eliminates the disadvantage of a normal feed-forward multilayer network, where it is difficult for an observer to understand or modify the network.

For simplicity, we assume that the examined fuzzy inference system has two inputs  $x$  and  $y$  and one output. For a first-order Sugeno fuzzy model, a common rule set with two fuzzy if–then rules are defined as

Rule 1: If 
$$
x
$$
 is  $A_1$  and  $y$  is  $B_1$ , then  
\n $f_1 = p_1 x + q_1 y + r_1,$ \n(10)

Rule 2 : If 
$$
x
$$
 is  $A_2$  and  $y$  is  $B_2$ , then  $f_2 = p_2 x + q_2 y + r_2$ . (11)

As seen from Fig. [9b](#page-8-0), different layers of ANFIS have different nodes. Each node in a layer is either fixed or adaptive [[44\]](#page-11-0). Different layers with their associated nodes are described below:

Layer 1 Every node  $I$  in this layer is an adaptive node. Parameters in this layer are called premise parameters.

Layer 2 Every node in this layer is a fixed node labeled  $\Pi$ , whose output is the product of all the incoming signals. Each node output represents the firing strength of a rule.

Layer 3 Every node in this layer is a fixed node labeled N. The ith node calculates the ratio of the ith rules' firing strength. Thus, the outputs of this layer are called normalized firing strengths.

<span id="page-8-0"></span>

Layer 4 Every node  $i$  in this layer is an adaptive node. Parameters in this layer are referred to as consequent parameters.

Layer 5 The single node in this layer is a fixed node labeled  $\Sigma$ , which computes the overall output as the summation of all incoming signals.

The learning algorithm for ANFIS is a hybrid algorithm, which is a combination of gradient descent and the leastsquares method. More specifically, in the forward pass of the hybrid learning algorithm, node outputs go forward until layer 4 and the consequent parameters are identified by the least-squares method [[44\]](#page-11-0). In the backward pass, the error signals propagate backwards and the premise parameters are updated by gradient descent. Table 6 summarizes the activities in each pass.

The consequent parameters are optimized under the condition that the premise parameters are fixed. The main

Table 6 Forward and backward pass for ANFIS

	Forward pass	Backward pass
Premise parameters	Fixed	Gradient descent
Consequent parameters	Least-squares estimator	Fixed
Signals	Node outputs	Error signals

benefit of the hybrid approach is that it converges much faster since it reduces the search space dimensions of the original pure back propagation method used in neural networks. The overall output can be expressed as a linear combination of the consequent parameters. The error measure to train the above-mentioned ANFIS is defined as [\[45](#page-11-0)]:

$$
E = \sum_{k=1}^{n} (f_k - f'_k)^2
$$
 (12)

where  $f_k$  and  $f'_{k}$  are the kth desired and estimated output, respectively, and  $n$  is the total number of pairs (inputs– outputs) of data in the training set.

In this study, a hybrid intelligent system called ANFIS (the adaptive neuro-fuzzy inference system) (Table [7\)](#page-9-0) for predicting k was also applied. ANFIS was trained with the help of Matlab version 7.1 [\[36](#page-11-0)], SPSS 10.0 [\[46](#page-11-0)] package was used for RMSE and statistical calculations. Different parameter types and their values used for training ANFIS can be seen in Table [7.](#page-9-0)

According to the RMSE, VAF,  $R^2$  values (Table [5](#page-6-0)), and cross-correlation between predicted and observed values (Fig. [10\)](#page-9-0), ANFIS model constructed to predict  $k$  has the highest prediction performance.

<span id="page-9-0"></span>Table 7 Different parameter types and their values used for training ANFIS

ANFIS parameter type	Value
Number of nodes	78
Number of linear parameters	108
Number of nonlinear parameters	27
Total number of parameters	135
Number of training data pairs	146
Number of checking data pairs	49
Number of fuzzy rules	27

## 7 Results and conclusions

In this paper, use of some neural computing models—such as, artificial neural network (ANN) with different algorithms (MLP, Exact RBF, RBF trained with  $k$  means, and RBF trained with SOM) and artificial neuro-fuzzy inference system (ANFIS) models for prediction of permeability coefficient value of soils—was described and compared. It appears that there is a possibility of estimating  $k$  of coarse-grained soils from grain-size distribution curves by using the soft computing models.

The results of the present paper and their conclusions can be drawn as follows:

- (1) The result of the multiple regression analysis showed that the model performance is very low with the correlation coefficient of 0.587 obtained from crosscorrelation between observed and predicted values of k.
- (2) In order to predict the permeability coefficient, ANN models having three inputs, one output were applied successfully and exhibited reliable predictions. However, all four different algorithms of ANN have almost the same prediction capability, and accuracy of MLP was relatively higher than RBF models.
- (3) The ANFIS model for prediction of permeability coefficient revealed the most reliable prediction when compared with the ANN models.

The comparison of VAF, RMSE indices, and coefficient of correlations  $(R^2)$  for predicting k revealed that prediction performances of the artificial neuro-fuzzy inference system model are higher than those of four algorithms of artificial neural networks (MLP, Exact RBF, RBF trained with k means, RBF trained with SOM). In order to show the deviations from the observed values of  $k$ , the distances of



<span id="page-10-0"></span>

Fig. 12 Intervals of variations of predicted from observed values

the predicted values from the models constructed from the observed values were also calculated, and graphics were drawn (Fig. [11\)](#page-9-0). The deviation intervals (will be multiplied by  $10^{-6}$ ) (-0.000117 to  $+0.000111$ ) of the predicted values from ANFIS are smaller than the deviation intervals of ANN models (in MLP  $-0.000271$  to  $+0.000463$ , in Exact RBF  $-0.000336$  to  $+0.000646$ , in RBF trained with k means  $-0.000560$  to  $+0.000458$ , in RBF trained with SOM  $-0.000317$  to  $+0.00011$ ) (Fig. 12).

As is known, the potential benefits of soft computing models extend beyond the high computation rates. Higher performances of the soft computing models were sourced from greater degree of robustness and fault tolerance than traditional statistical models because there are many more processing neurons, each with primarily local connections.

The performance comparison also showed that the soft computing techniques are good tools for minimizing the uncertainties, and their use will also may provide new approaches and methodologies and minimize the potential inconsistency of correlations. The results of this paper will provide dissemination of important results of the use of soft computing technologies in soil sciences and serve as an example for engineering geologists, geotechnique and civil engineers engaged in this area of interest.

Acknowledgments Authors thank anonymous reviewer for very constructive critics and suggestions that led to the improvement of the article.

## References

- 1. Shepherd RG (1989) Correlations of permeability and grain size. Ground Water 27(5):633–638
- 2. Yilmaz I (2006) Indirect estimation of the swelling percent and a new classification of soils depending on liquid limit and cation exchange capacity. Eng Geol 85:295–301
- 3. Alyamani MS, Sen Z (1993) Determination of hydraulic conductivity from complete grain-size distribution curves. Ground Water 31(4):551–555
- 4. Hazen A (1892) Some physical properties of sands and gravels. Massachusetts State Board of Health, Annual Report, pp 539–556
- 5. Uma KO, Egboka BCE, Onuoha KM (1989) New statistical grain-size method for evaluating the hydraulic conductivity of sandy aquifers. J Hydrol 108:343–366
- 6. Krumbein WC, Monk GD (1943) Permeability as a function of the size parameters of unconsolidated sands. Trans Am Inst Min Metall Petroleum Eng 151:153–163
- 7. Kozeny J (1953) Das wasser in boden, grundwasserbewegung. Hydraulik 280–445
- 8. Rawls WJ, Brakensiek DL (1989) Estimation of soil water retention and hydraulic properties. In: Morel-Seytoux HJ (ed) Unsaturated flow in hydrologic modeling theory and practice. Kluwer, Dordrecht, pp 275–300
- 9. Jabro JD (1992) Estimation of saturated hydraulic conductivity of soils from particle size distribution and bulk density data. J Am Soc Agric Eng 35(2):557–560
- 10. Sperry JM, Peirce JJ (1995) A model for estimating the hydraulic conductivity of granular material based on grain shape, grain size, and porosity. Ground Water 33(6):892–898
- 11. Lebron I, Schaap MG, Suarez DL (1999) Saturated hydraulic conductivity prediction from microscopic pore geometry measurements and neural network analysis. Water Resour Res 35(10):3149–3158
- 12. Cronican AE, Gribb MM (2007). Literature review: equations for predicting hydraulic conductivity based on grain-size data. (Supplement to Technical Note entitled: Hydraulic conductivity prediction for sandy soils published in Groundwater 42(3):459–464, 2004). [http://coen.boisestate.edu/datedmaterial/](http://coen.boisestate.edu/datedmaterial/images/LITERATURE_REVIEW-final.pdf) [images/LITERATURE\\_REVIEW-final.pdf](http://coen.boisestate.edu/datedmaterial/images/LITERATURE_REVIEW-final.pdf)
- 13. ASTM (1990) Sec. 4, Vol. 04.08, soil and rock; dimension stone; geosynthetics. American Society for Testing and Materials, Designation, pp D 421, D 422
- 14. ASTM (2006) Standard test method for permeability for granular soils. American Society for Testing and Materials, Designation, pp D 4234–D 4268
- 15. Jin Y, Jiang J (1999) Techniques in neural-network based fuzzy system identification and their application to control of complex systems. In: Leondes CT (ed) Fuzzy theory systems, echniques and applications. Academic Press, New York, pp 112–128
- 16. Kaynar O, Yilmaz I, Demirkoparan F (2011) Forecasting of natural gas consumption with neural network and neuro fuzzy system. Energy Educ Sci Technol A Energy Sci Res 26:221–238
- 17. Singh TN, Kanchan R, Verma AK, Singh S (2003) An intelligent approach for prediction of triaxial properties using unconfined uniaxial strength. Min Eng J 5:12–16
- 18. Yilmaz I (2009) Landslide susceptibility mapping using frequency ratio, logistic regression, artificial neural networks and their comparison: a case study from Kat landslides (Tokat-Turkey). Comput Geosci 35(6):1125–1138
- 19. Yilmaz I (2009) Comparison of landslide susceptibility mapping methodologies for Koyulhisar, Turkey: conditional probability, logistic regression, artificial neural networks, and support vector machine. Environ Earth Sci 61(4):821–836
- 20. Rumelhart D, McClelland J (1986) Parallel distributed processing: explorations in the microstructure of cognition. Bradford books, MIT Press, Cambridge
- 21. Yilmaz I (2010) The effect of the sampling strategies on the landslide susceptibility mapping by Conditional Probability (CP) and Artificial Neural Networks (ANN). Environ Earth Sci 60(3):505–519
- 22. Park J, Sandberg IW (1993) Approximation and radial basis function networks. Neural Comput 5:305–316
- 23. Broomhead DS, Lowe D (1988) Multivariable functional interpolation and adaptive networks. Complex Syst 2:321–355
- <span id="page-11-0"></span>24. Moody J, Darken CJ (1989) Fast learning in networks of locallytunes processing units. Neural Comput 1(2):281–294
- 25. Park J, Sandberg IW (1991) Universal approximations using radial-basis-function network. Neural Comput 3(2):246–257
- 26. Xu K, Xie M, Tang LC, Ho SL (2003) Application of neural networks in forecasting engine systems reliability. Appl Soft Comput 2:255–268
- 27. Chen S, Cowan CFN, Grant PM (1991) Orthogonal least squares learning algorithm for radial basis function networks. IEEE Trans Neural Netw 2(2):302–309
- 28. Bianchini M, Frasconi P, Gori M (1995) Learning without local minima in radial basis function networks. IEEE Trans Neural Netw 6(3):749–755
- 29. Sheta AF, Jong KD (2001) Time-series forecasting using GAtuned radial basis function. Inf Sci 133:221–228
- 30. Foody GM (2004) Supervised image classification by MLP and RBF neural networks with and without an exhaustively defined set of classes. Int J Remote Sens 25(15):3091–3104
- 31. Rivas VM, Merelo JJ, Castillo PA, Arenas MG, Castellano JG (2004) Evolving RBF neural networks for time-series forecasting with EvRBF. Inf Sci 165:207–220
- 32. Harpham C, Dawson CW (2006) The effect of different basis functions on a radial basis function network for time series prediction: a comparative study. Neurocomputing 69:2161–2170
- 33. Sarimveis H, Doganis P, Alexandridis AA (2006) Classification technique based on radial basis function neural networks. Adv Eng Softw 37:218–221
- 34. Zhang R, Huang G, Sundararajan N, Saratchandran P (2007) Improved GAP-RBF network for classification problems. Neurocomputing 70:3011–3018
- 35. Yu L, Lai KK, Wang S (2008) Multistage RBF neural network ensemble learning for exchange rates forecasting. Neurocomputing 71:3295–3302
- 36. Matlab 7.1 (2005) Software for technical computing and modelbased design. The MathWorks Inc.
- 37. Alvarez GM, Babuska R (1999) Fuzzy model for the prediction of unconfined compressive strength of rock samples. Int J Rock Mech Min Sci 36:339–349
- 38. Finol J, Guo YK, Jing XD (2001) A rule based fuzzy model for the prediction of petrophysical rock parameters. L Petr Sci Eng 29:97–113
- 39. Yilmaz I, Yüksek AG (2008) An example of artificial neural network application for indirect estimation of rock parameters. Rock Mech Rock Eng 41:781–795
- 40. Yilmaz I, Yüksek AG (2009) Prediction of the strength and elasticity modulus of gypsum using multiple regression, ANN, ANFIS models and their comparison. Int J Rock Mech Min Sci 46(4):803–810
- 41. Jang JSR, Chuen-Tsai S (1995) Neuro-fuzzy modeling and control. Proc IEEE 83:378–406
- 42. Lee CC (1990) Fuzzy logic in control systems: fuzzy logic controller. I. IEEE Trans Syst Man Cybern 20:404–418
- 43. Lee CC (1990) Fuzzy logic in control systems: fuzzy logic controller. II. IEEE Trans Syst Man Cybern 20:419–435
- 44. Jang JR (1993) ANFIS: adaptive-network-based fuzzy inference system. IEEE Trans Syst Man Cybern 23:665–685
- 45. Loukas YL (2001) Adaptive neuro-fuzzy inference system: an instant and architecture-free predictor for improved QSAR studies. J Med Chem 44:2772–2783
- 46. SPSS 10.0.1 (1999) Statistical analysis software (Standard Version). SPSS Inc.