



# Can sonic tomography predict loss in load-bearing capacity for trees with internal defects? A comparison of sonic tomograms with destructive measurements

Daniel C. Burcham<sup>1</sup> · Nicholas J. Brazeel<sup>2</sup> · Robert E. Marra<sup>3</sup> · Brian Kane<sup>4</sup>

Received: 28 April 2018 / Accepted: 27 December 2018 / Published online: 5 January 2019  
© Springer-Verlag GmbH Germany, part of Springer Nature 2019

## Abstract

**Key message** Sonic tomography can be used to examine reductions in the load-bearing capacity of tree parts with internal defects, but the limitations of sonic tomography and mathematical methods must be considered.

**Abstract** The measurement and assessment of internal defects is an important aspect of tree risk assessment. Although there are several methods for estimating the reduced load-bearing capacity of trees with internal defects, the advancement of these methods has not kept pace with improvements to methods used to measure the internal condition of trees, such as sonic tomography. In this study, the percent reduction to the section modulus,  $Z_{\text{LOSS}}$  (%), caused by internal defects was estimated using 51 sonic tomograms collected from three tree species, and the accuracy of measurements was assessed using the destructively measured internal condition of the corresponding cross sections. In tomograms, there was a repeated underestimation of the percent total damaged area,  $A_D$  (%), and a repeated overestimation of the offset distance between the centroid of the trunk and the centroid of the largest damaged part,  $L_O$  (m). As a result,  $Z_{\text{LOSS}}$  determined using tomograms was mostly less, in absolute terms, than that determined from destructive measurements. However, the accuracy of these estimates improved when using colors associated with intermediate sonic velocities to select damaged parts in tomograms, in addition to the colors explicitly associated with the slowest sonic velocities. Among seven mathematical methods used to estimate  $Z_{\text{LOSS}}$ , those accounting for  $L_O$  were more accurate than others neglecting it. In particular, a numerical method incorporating greater geometric detail, called *zloss*, gave estimates that were consistently better than six other analytical methods.

**Keywords** Risk assessment · Decay · Strength loss

---

Communicated by Fourcaud.

✉ Daniel C. Burcham  
daniel\_christopher\_burcham@nparks.gov.sg

<sup>1</sup> Centre for Urban Greenery and Ecology, National Parks Board, Singapore 259569, Singapore

<sup>2</sup> Center for Agriculture, Food, and the Environment, University of Massachusetts Amherst, Amherst, MA 01003, USA

<sup>3</sup> Department of Plant Pathology and Ecology, Connecticut Agricultural Experiment Station, New Haven, CT 06504, USA

<sup>4</sup> Department of Environmental Conservation, University of Massachusetts Amherst, Amherst, MA 01003, USA

## Introduction

Several formulas have been used to estimate the strength loss (i.e., loss in load-bearing capacity) caused by internal defects in living trees, and most are based on the difference in the second moment of area,  $I$  ( $\text{m}^4$ ), between a hollow and solid trunk section (Kane et al. 2001).  $I$  represents the load-bearing capacity of a shape where the contribution of a material element to a total bending moment is proportional to the square of its distance ( $y$ ) from the neutral axis (Ennos 2012); it can be determined by summing the many, infinitesimally small moments distributed over a cross section of area ( $A$ ):

$$I = \int y^2 dA. \quad (1)$$

Practically, this means that wood situated near the trunk periphery contributes greater to overall rigidity. Coder (1989) used the formula to estimate the percent loss in  $I$ ,  $I_{\text{LOSS}}$  (%), of a hollow pipe relative to a solid rod:

$$I_{\text{LOSS}} = d^4/D^4, \quad (2)$$

where  $d$  and  $D$  are the diameters of hollow and solid circles, respectively. Wagener (1963) modified this formula as the cube of the same ratio:

$$I_{\text{LOSS}} = d^3/D^3. \quad (3)$$

It is unclear why Wagener (1963) chose this specific exponent. Most observe that it produces a larger and more conservative estimate over the range of possible  $d/D$  (Ciftci et al. 2014; Kane et al. 2001), but he implied that it offered a coarse approximation of strength loss, presumably as a compromise between the geometric properties governing bending stress ( $I \propto D^4$ ) and compression stress ( $A \propto D^2$ ) (Wagener 1963). Later, Smiley and Fraedrich (1992) modified this formula to approximate trees with open cavities as a sector of a circular annulus:

$$I_{\text{LOSS}} = d^3/D^3 + R(D^3 - d^3)/D^3, \quad (4)$$

where  $R$  is the ratio of cavity opening to stem circumference. For trees without a cavity opening, estimates given by Eq. 4 are identical to Eq. 3. Among the three formulas, only the latter was validated with empirical data (Smiley and Fraedrich 1992).

However, several limitations of these formulas diminish their applicability to many common situations. The formulas are appropriate for circular cylinders composed of isotropic, homogeneous material, and Wagener's (1963) and Coder's (1989) implicitly assume concentric areas of decay in which the decayed and solid areas share the same centroid. A circle is often an inexact approximation of the shape of a tree, especially near the base of those with pronounced buttress roots, and circles frequently do not accurately describe the shape of decayed areas. In addition, decay is often formed asymmetrically, so that its centroid is offset from that of the trunk, and these formulas ignore the potentially significant contributions of offset decayed areas (Kane and Ryan 2004).

To address these limitations, Ciftci et al. (2014) used the section modulus,  $Z$  ( $\text{m}^3$ ), to evaluate the loss in load-bearing capacity, taken as moment capacity, due to decay:

$$Z = I/y, \quad (5)$$

where  $y$  is the maximum perpendicular distance (m) between the neutral axis and outermost trunk fibers. The ratio is needed to calculate bending stress,  $\sigma$  ( $\text{N}\cdot\text{m}^{-2}$ ), for beams, or beam-like plant organs (Niklas 1992):

$$\sigma = My/I, \quad (6)$$

where  $M$  (N m) is a bending moment causing rotation about the neutral axis. Equation 6 shows that, for any loading situation, the maximum stress experienced by a cross section of any shape can be minimized by maximizing  $Z$  (Niklas 1992). Ciftci et al. (2014) estimated the percent loss in  $Z$ ,  $Z_{\text{LOSS}}$  (%), between a solid and hollow trunk section, and considered cases with both concentric and non-concentric decayed areas. The authors also considered the effects of material anisotropy on  $Z_{\text{LOSS}}$ , which was negligible (Ciftci et al. 2014).

Many of the limitations associated with the existing strength-loss formulas arise from the unavailability of analytical solutions to the moments of irregular shapes (Ciftci et al. 2014; Kane et al. 2001), but numerical approaches can be used to compute these values for any shape (Koizumi and Hirai 2006). Numerical analysis could address many of the limitations associated with existing approaches to estimating strength loss, including irregular geometry and non-concentric decayed areas, but this would require an accurate description of the size, position, and shape of decay in a trunk cross section.

Among consulting arborists, sonic tomography (SoT) is increasingly recognized as a useful way to evaluate the internal condition of trees (Smiley et al. 2011), offering reasonably accurate, non-invasive, and convenient assessments of the internal condition of the tree (Johnstone et al. 2010). Sonic tomography measures variation in acoustic transmission speeds, which is proportional to the ratio of wood stiffness to density (Arciniegas et al. 2014). The advantages and limitations of SoT have been documented by several studies (Brazee et al. 2011; Li et al. 2012; Ostrovsky et al. 2017; Wang et al. 2009). Although SoT generally depicts the internal condition of trees accurately, some authors reported that measurements often underestimate the size of decayed areas (Liang et al. 2007; Wang et al. 2009), overestimate the size of cracks (Wang et al. 2007), and suffer inaccuracies on irregularly shaped trunks (Gilbert et al. 2016). Notwithstanding these minor shortcomings, sonic tomography is a natural choice to provide the raw data necessary for a numerical approach to estimating the loss in load-bearing capacity of trees with internal defects. In this study, the existing analytical methods for estimating  $Z_{\text{LOSS}}$  were compared to a numerical estimate derived from sonic tomograms. The method was validated by applying it to sonic tomograms and the corresponding cross-sectional photographs from a previous study (Marra et al. 2018), in which trees were destructively harvested to assess the accuracy of interpretations derived from sonic tomograms.

The specific objectives of this study were to: (1) compare the estimates of internal damage in three hardwood species provided by SoT with internal damage measured on destructively

sampled trees; (2) compare analytical and numerical estimates of strength loss derived from SoT and destructively sampled trees; and (3) test whether geometric features of damaged parts (i.e., size, position, and shape) affect the accuracy of different approaches to estimating strength loss.

## Materials and methods

### Site and tree material

All tomograms and corresponding cross-sectional photographs used for this study were obtained from a previous study in which the accuracy of tomographic predictions was assessed by destructive sampling (Marra et al. 2018). In 2014, individuals of three species [American beech (AB, *Fagus grandifolia*); sugar maple (SM, *Acer saccharum*); yellow birch (YB, *Betula alleghaniensis*)] were chosen based on the appearance of signs and symptoms suggestive of internal decay. Trees were assessed using the PiCUS<sup>®</sup> Sonic Tomograph 3 (Argus Electronic GmbH, Rostock, Germany) at one-to-four levels on the lower trunk, with the lowest cross section typically positioned 50 cm above the soil line. Tomograms display the relative sound transmission speeds on a colorimetric scale: the greatest sonic transmission speeds, associated with non-decayed wood, are depicted using varying shades of brown; decreasing speeds associated with lower density-specific stiffness, and more advanced stages of decay, are depicted, in order, as green, violet, and blue (Fig. 1b). After felling trees, cross sections corresponding with each tomogram were excised from the trunk and photographed (Fig. 1c). For this study, only cross sections with internal defects detected by SoT were used for analysis. See Marra et al. (2018) for more details.

### Image analysis

Three separate image files were used for analysis: a geometry image showing only the blue trunk boundary line (Fig. 1a), a sonic tomogram showing the visualized decay pattern (Fig. 1b), and a reference photograph of the tree's destructively measured internal condition (Fig. 1c). The geometry and tomogram images were oriented identically without annotation and exported as JPEG files from the PiCUS<sup>®</sup> software. The size of the exported images was 770 × 770 pixels.

A tomogram is displayed by the PiCUS<sup>®</sup> software in a Cartesian coordinate plane. To extract boundary coordinates for the solid and damaged parts, an object was created to relate the intrinsic coordinates of the tomogram images to the spatial coordinates of a Cartesian coordinate system. Similarly, the recorded distances between measurement points on each trunk were used to relate the intrinsic coordinates of the reference

photographs to a Cartesian coordinate system. These objects used the calculated physical extent of each pixel to convert a pixel index (row, column) to a coordinate pair ( $x$ ,  $y$ ).

The geometry and tomogram images were segmented using specific ranges in the hue, saturation, brightness (HSV), and LAB color space, respectively (Table 1). Each sonic tomogram was segmented to select either violet and blue (VB) or green, violet, and blue (GVB). This distinction between color combinations was made, because the PiCUS<sup>®</sup> software excludes green areas when calculating the percent solid and damaged area in tomograms, but all parts of the cross section need to be classified as either solid or damaged for  $Z_{LOSS}$  calculations.

Reference images of each tree's destructively measured internal condition were manually binarized into black (0) and white (1) images using Adobe Photoshop CS6 Extended (Adobe Systems, Inc., San Jose, CA, USA) in which black and white, respectively, represented damaged and solid parts (Fig. 1d). The trunk boundary, excluding bark, was used to define an enclosed region of interest, and the extent of damaged parts was determined visually by the presence of discoloration, cavities, cracks, and decayed wood. Wood discolored by the host defensive response and heartwood formation was classified as solid parts. Visual identification of damaged parts in cross sections is consistent with most existing studies (Brazee et al. 2011; Gilbert and Smiley 2004; Liang and Fu 2012; Ostrovsky et al. 2017).

After selecting specific colors, the boundaries of visible features in the segmented images were traced to determine the intrinsic coordinates for the perimeter of the solid and damaged parts (Fig. 2a, b). These sets were converted from intrinsic to Cartesian coordinates using the associated reference object. Each set consisted of  $n$  clockwise-ordered coordinate pairs  $(x_i, y_i)$ ,  $\{i \in 1 \dots n\}$ , that collectively described a simple, closed curve enclosing a solid or damaged part.

### Numerical estimates

Consistent with the existing methods (Smiley et al. 2011), damaged wood parts were considered hollow, or missing, for the purposes of these calculations. Four parameters were computed for the individual shape(s) comprising each section, including the area,  $A$  ( $m^2$ ):

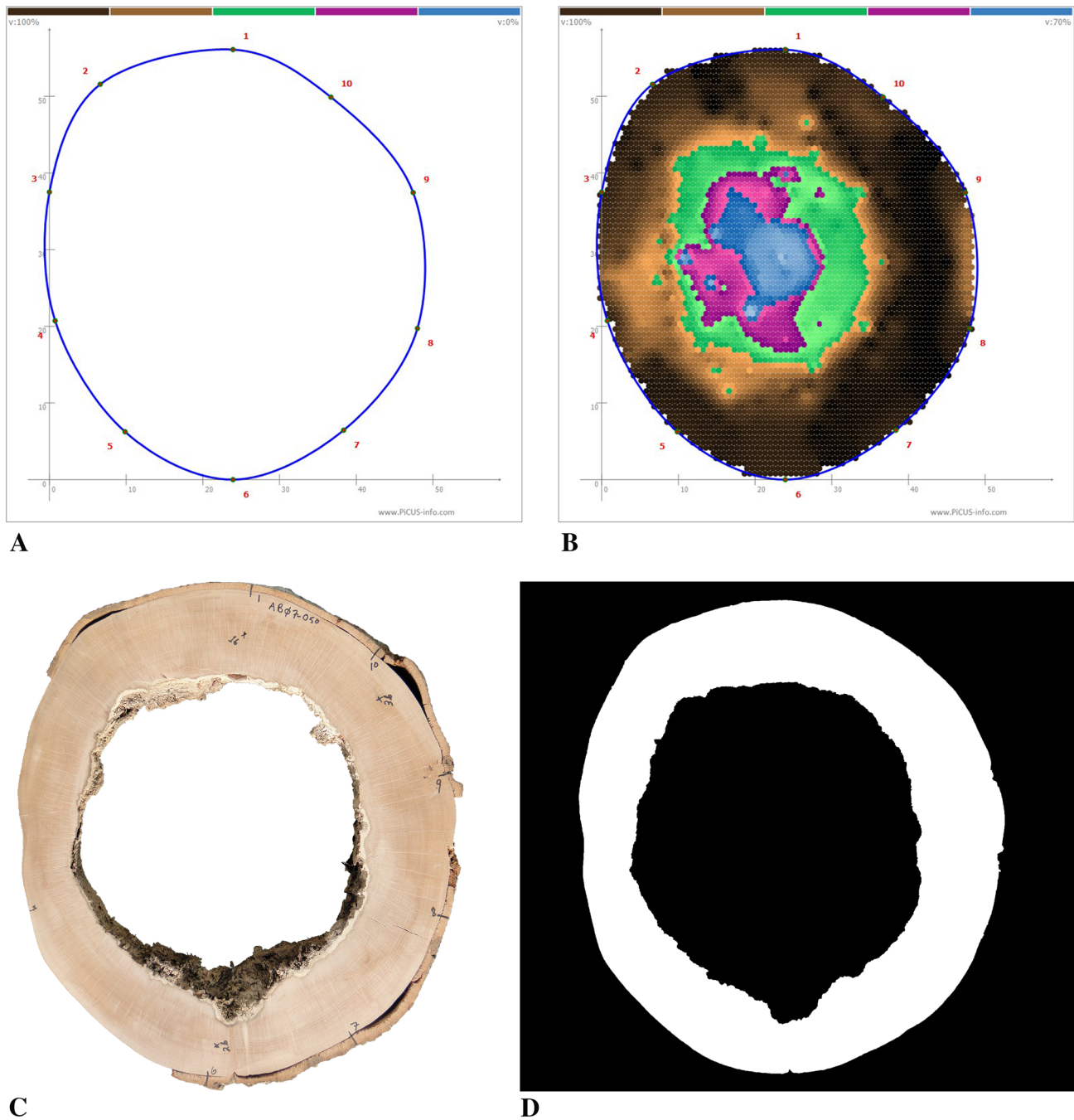
$$A = \int dA; \quad (7)$$

the first moment of area with respect to the  $y$ -axis,  $A_x$  ( $m^3$ ):

$$A_x = \int x dA; \quad (8)$$

the first moment of area with respect to the  $x$ -axis,  $A_y$  ( $m^3$ ):

$$A_y = \int y dA; \quad (9)$$



**Fig. 1** For each trunk cross section, three images were used for analysis, including a geometry file showing the blue trunk boundary line (a), a sonic tomogram showing the visualized decay pattern (b), and a photograph of the destructively harvested cross section (c). The reference photograph was used to produce a binary image (d), in which

black (0) and white (1), respectively, represent damaged and solid parts. This set of images depicts the internal trunk condition of one American beech (*Fagus grandifolia*) 50 cm above ground (AB07–050)

and the second moment of area with respect to the  $x$ -axis,  $I_{xx}$  ( $m^4$ ), as in Eq. 1:

$$I_{xx} = \int y^2 dA. \quad (10)$$

Green's theorem was used to reduce the formulas to a curve integral over the clockwise-ordered boundary coordinates enclosing each shape. See Steger (1996) for the complete derivation of the corresponding numerical formulas. Specifically,  $A$  was computed as follows:

**Table 1** Histogram thresholds used to select specific ranges in the HSV and LAB color space, respectively, associated with solid and damaged parts in sonic tomograms

	Geometry	Sonic tomogram	
Color(s)	Blue	Green, violet, blue (GVB) <sup>a</sup>	Violet, blue (VB)
Color space	HSV	LAB	LAB
Component 1	[0.01, 0.78] <sup>b</sup>	[20.92, 100.00]	[0.00, 100.00]
Component 2	[0.16, 1.00]	[− 26.90, 81.98]	[− 68.60, − 10.46]
Component 3	[0.00, 1.00]	[− 63.54, − 3.78]	[− 99.92, 62.94]

<sup>a</sup>For each sonic tomogram, either violet and blue (VB) or green, violet, and blue (GVB) was used to select damaged parts. In a PiCUS<sup>®</sup> sonic tomogram, the four colors used to visualize sonic velocities and the corresponding internal wood condition are as follows: brown, solid; green, intermediate; violet, damaged; and blue, damaged

<sup>b</sup>The ranges for each color component are expressed using interval notation

$$A = 1/2 \sum_{i=1}^n (x_i y_{i+1} - x_{i+1} y_i), \tag{11}$$

where  $(x_i, y_i)$ ,  $\{i \mid 1 \dots n\}$ , are the coordinate pairs for a given shape;  $A_x$  was computed as follows:

$$A_x = 1/6 \sum_{i=1}^n (x_i + x_{i+1})(x_i y_{i+1} - x_{i+1} y_i); \tag{12}$$

$A_y$  was computed as follows:

$$A_y = 1/6 \sum_{i=1}^n (y_i + y_{i+1})(x_i y_{i+1} - x_{i+1} y_i); \tag{13}$$

and  $I_{xx}$  was computed as follows:

$$I_{xx} = 1/12 \sum_{i=1}^n (y_i^2 + y_i y_{i+1} + y_{i+1}^2)(x_i y_{i+1} - x_{i+1} y_i). \tag{14}$$

For small strains, the location of the neutral axis coincides with the shape’s centroidal axis,  $\bar{y}$  (m), which is given by the following:

$$\bar{y} = A_y/A. \tag{15}$$

The corresponding  $x$ -coordinate of each shape’s centroid was similarly determined as follows:

$$\bar{x} = A_x/A. \tag{16}$$

For composite sections consisting of  $n$  smaller solid and hollow shapes, the centroid was determined as follows:

$$\bar{y} = \frac{\sum_{j=1}^n A_{y_j}}{\sum_{j=1}^n A_j}, \tag{17}$$

where  $A_{y_j}$  and  $A_j$  were multiplied by  $-1$  if the  $j$ th shape represented a void. Similarly, the parallel axis theorem was used to determine  $I_{xx}$  for composite sections as follows:

$$I_{xx} = \sum_{j=1}^n (I_{xx_j} + A_j c_j^2), \tag{18}$$

where  $c_j$  is the perpendicular distance between the neutral axis of the composite section and the centroid of the  $j$ th smaller shape. Similarly,  $I_{xx_j}$  and  $A_j$  were multiplied by  $-1$  if the  $j$ th shape represented a void. Ultimately,  $Z$  was computed as follows:

$$Z = I_{xx}/y, \tag{19}$$

where  $y$  is the maximum perpendicular distance between the section’s neutral axis and outermost trunk fibers. The reduction to  $Z$  for a hollow section, relative to a solid section with identical trunk geometry, was determined as a percent difference:

$$Z_{LOSS} = (Z_{SOLID} - Z_{HOLLOW})/Z_{SOLID}. \tag{20}$$

After calculation, the estimates obtained for a given orientation were stored, and the analysis was repeated after incrementally rotating each set of coordinate pairs about the respective section’s centroidal coordinates by an arbitrarily small angle. Each coordinate pair was rotated counter-clockwise about the  $z$ -axis using the following rotation matrix:

$$R_z(\alpha) = \begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}, \tag{21}$$

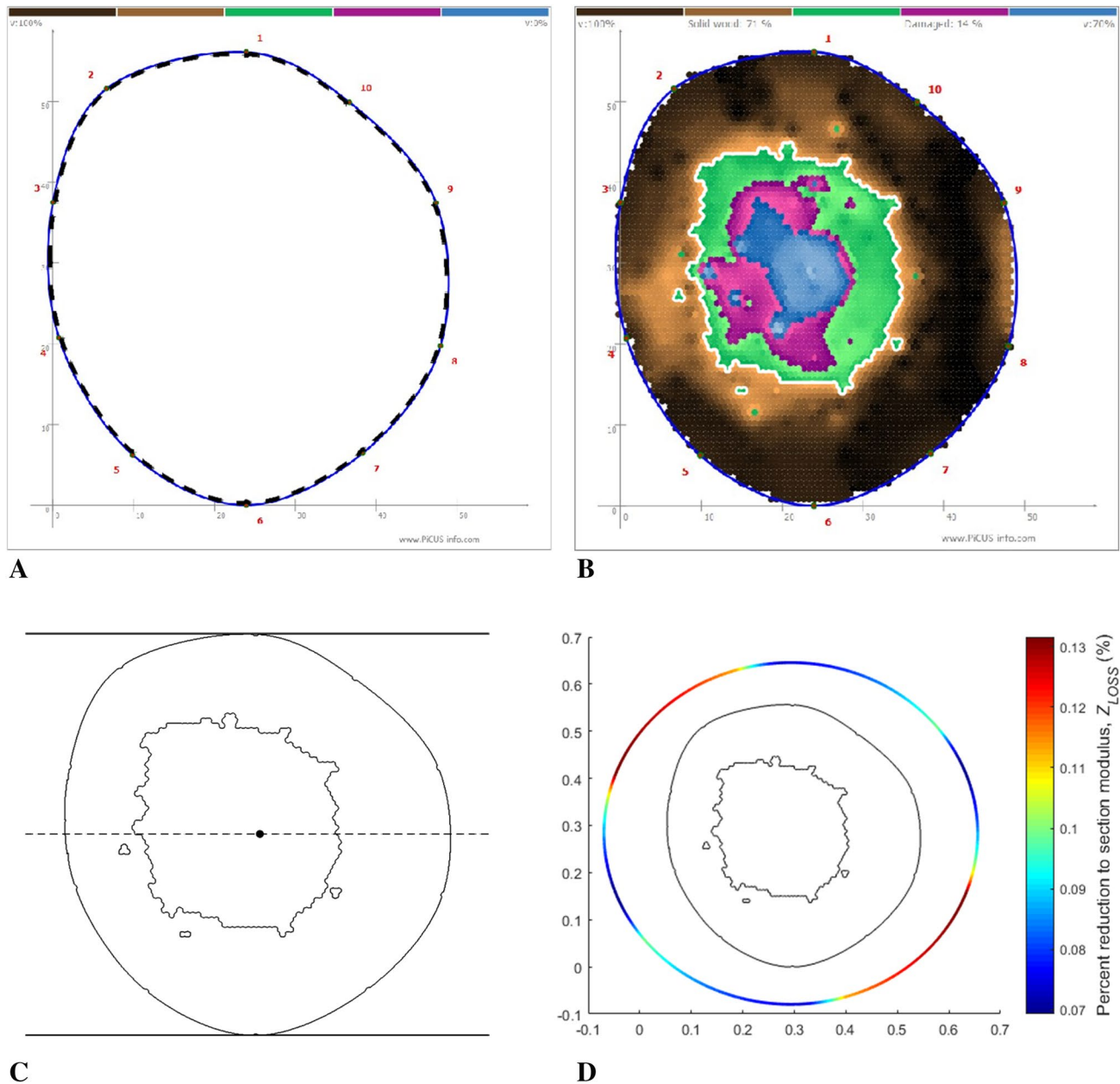
where  $\alpha$  (rad) is the incremental rotation angle. The complete rotation for each coordinate pair was achieved by the following matrix operation:

$$A' = R_x(\alpha)(A - B) + B, \tag{22}$$

where  $A$  is a vector in  $\mathbb{R}^2$  with elements  $[x_i, y_i]$  and  $B$  is a similar vector composed of a given section’s centroidal coordinates. After each incremental rotation, identical calculations were performed to compute  $Z_{LOSS}$  until the cumulative total rotation for a section equaled  $2\pi$  rad. The preceding image processing and numerical analysis steps were written as a MATLAB (MathWorks, Natick, MA, USA) function named *zloss* (Burcham 2017).

In addition, several attributes of the solid and damaged parts displayed in tomograms and binary images were calculated. The percent of total damaged cross-sectional area,  $A_D$  (%), was computed as follows:





**Fig. 2** Using specific ranges in the HSV and LAB color space, respectively, sonic tomograms were segmented to acquire the boundary of solid (**a**: dashed black line) and damaged (**b**: solid white lines) parts. For a given orientation, the perimeters of shapes comprising each hollow section were used to determine several features, including the neutral axis (**c**: dashed horizontal line), centroid (**c**: solid dot),

and the outermost trunk fibers oriented perpendicular to the neutral axis (**c**: solid horizontal lines). The  $Z_{LOSS}$  estimates are displayed as color intensity values on a circular annulus surrounding an outline of each hollow section (**d**). The red, green, blue continuous color scale represents directional  $Z_{LOSS}$  between the minimum and maximum values for a given cross section

$$A_D = \sum_{i=1}^n a_{D_i} / A_S, \quad (23)$$

where  $a_D$  is the area ( $m^2$ ) of  $i$ th damaged part and  $A_S$  is the area ( $m^2$ ) enclosed by the trunk boundary, excluding the bark. The offset length,  $L_O$  (m), between the centroid of

the trunk and the centroid of the largest damaged part was determined using the distance formula:

$$L_O = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}, \quad (24)$$

where  $(x_1, y_1)$  and  $(x_2, y_2)$ , respectively, are the centroidal coordinates of the trunk and largest damaged part

determined numerically using Eqs. 15 and 16. The roundness,  $R$  (dimensionless), of the trunk,  $R_T$ , and largest damaged part,  $R_D$ , was determined using the following:

$$R = 4A / \pi L^2, \tag{25}$$

where  $A$  is the area ( $m^2$ ), determined numerically using Eq. 11, and  $L$  (m) is the major axis of the shape, determined as the maximum distance between any two points on the boundary. The latter two attributes only considered the largest damaged part, because the existing analytical methods only explicitly consider one damaged area (Ciftci et al. 2014; Coder 1989; Smiley and Fraedrich 1992; Wagener 1963).

### Analytical estimates

To compute analytical estimates of  $Z_{LOSS}$ , two basic approaches described by Ciftci et al. (2014) were used to approximate irregular shapes as circles. Again, only the circular approximation of the largest damaged part in a tomogram was used in the associated  $Z_{LOSS}$  calculations. For the first method (“Ciftci I”), the irregularly shaped trunk and largest damaged part were approximated using a minimum circumscribed circle, “Ciftci I(a);” maximum inscribed circle, “Ciftci I(b);” and the average of these two circles, “Ciftci I(c).” The radius and centroidal coordinates of the minimum circumscribed and maximum inscribed circles were determined using the MATLAB functions *minbound-circle* and *incircle*, respectively, from the *matGeom* library (Legland 2015). For the second method (“Ciftci II”), the radius of the circular equivalent of an irregular shape was calculated as follows:

$$r = \sqrt{A/\pi}, \tag{26}$$

where  $A$  ( $m^2$ ) is the area of an irregular shape determined numerically using Eq. 11. To position the circular equivalent shape on the centroid of its irregular counterpart, the centroidal coordinates of the trunk and largest damaged part were determined numerically using Eqs. 15 and 16. The analytical estimates of  $Z_{LOSS}$  were determined using these radii and centroidal coordinates; see Ciftci et al. (2014) for more information about the associated calculations. Since  $I_{LOSS} = Z_{LOSS}$  for a hollow circle, Eq. 2 was used, as employed by Coder (1989), to compute analytical estimates of  $Z_{LOSS}$ . Likewise, Eq. 3 proposed by Wagener (1963) was used to compute analytical estimates, not strictly  $Z_{LOSS}$ , for comparison with the other available methods. For Eqs. 2 (“Coder”) and 3 (“Wagener”), the radius of the circular equivalent of an irregular shape, determined using Eq. 26, was used to calculate  $Z_{LOSS}$ .

### Statistical analysis

Three coefficients were computed to examine the accuracy of tomograms at depicting internal conditions, in terms of the size, position, and shape of damaged parts. Pearson’s product-moment correlation ( $r$ ) and Spearman’s rank-order correlation ( $\rho$ ) were computed to measure the strength of a general linear relationship of the form  $y = ax + b$  between features estimated from tomograms and destructive measurements, including  $A_D$ ,  $L_O$ ,  $R_T$ ,  $R_D$ , and their rank-order counterparts. Lin’s concordance coefficient ( $p_c$ ) was computed to measure the strength of a linear relationship of the form  $y = x$  (i.e., 1:1 similarity) between the same data sets. Cook’s  $D$ , measured during regression, was used to identify potential outliers in each comparison, with cases exerting influence greater than  $4/n$  inspected more closely (Marasinghe and Kennedy 2008).

**Table 2** For a set of 51 trunk cross sections, Pearson’s product-moment correlation ( $r$ ), Spearman’s rank-order correlation ( $\rho$ ), and Lin’s concordance correlation ( $p_c$ ) between geometric attributes derived from sonic tomograms and binary images of the destructively measured internal condition of trees

	$r$	$\rho$	$p_c$
$A_D$ (%)			
VB <sup>a</sup>	0.74**	0.80**	0.16
GVB	0.71**	0.77**	0.44
$L_O$ (m)			
VB	0.64**	0.64**	0.41
GVB	0.70**	0.68**	0.53
$R_T$			
–	0.82**	0.83**	0.81
$R_D$			
VB	0.22	0.26	0.20
GVB	0.55**	0.54**	0.53

Geometric attributes include  $A_D$  (%), the percent of total damaged cross-sectional area;  $L_O$  (m), the offset length between the centroid of the trunk and the centroid of the largest damaged part; and  $R$  (dimensionless), the roundness of the trunk,  $R_T$ , and largest damaged part,  $R_D$

\*\*denotes highly significant ( $p < 0.001$ ) correlations between geometric features derived from sonic tomograms and binary images

<sup>a</sup>For each sonic tomogram, either violet and blue (VB) or green, violet, and blue (GVB) was used to select damaged parts. In a PiCUS<sup>®</sup> sonic tomogram, the four colors used to visualize acoustic transmission speeds and the corresponding internal wood condition are as follows: brown, solid; green, intermediate; violet, damaged; blue, damaged

In addition, two linear models were fit to the error associated with various approaches to estimating  $Z_{LOSS}$  from sonic tomograms relative to the same computed numerically from binary images. Since  $Z_{LOSS}$  computed numerically from binary images was based on destructive measurements and accommodated the most geometric detail, it was assumed that it provided the best available approximation of the actual  $Z_{LOSS}$  for a measured section and offered a useful standard to distinguish among other methods based on SoT. First, analysis of variance (ANOVA) was used to test the effect of the mathematical methods and colors used to select damaged wood parts on the absolute difference (%) between maximum  $Z_{LOSS}$  determined using sonic tomograms and binary images. The fixed effects included mathematical methods used to estimate  $Z_{LOSS}$ : Ciftci I(a), Ciftci I(b), Ciftci I(c), Ciftci II, Coder, *zloss*, and Wagener; colors used to select damaged wood parts in sonic tomograms: violet and blue (VB) and green, violet, and blue (GVB); and their interaction: methods  $\times$  colors. For significant fixed effects, mean separation was performed using Tukey’s honestly significant difference.

Second, analysis of covariance was used to test the effect of the mathematical methods on the absolute difference (%) between maximum  $Z_{LOSS}$  determined using tomograms and binary images, after accounting for geometric features of cross sections. In total, eight covariates were tested for inclusion in the model:  $A_D$ ,  $A_D$  (error),  $L_O$ ,  $L_O$  (error),  $R_T$ ,  $R_T$  (error),  $R_D$ , and  $R_D$  (error). The covariates were computed from binary images of each section as described in Eqs. 23–26, and the error associated with each covariate was determined as the absolute difference between the

estimate from tomograms and binary images. Since  $A_D$  represented the percent of total damaged area, the fixed effect for colors was removed from this model. The form of the model was determined by iteratively testing the significance of a simple linear relationship between each covariate and the absolute difference (%) between maximum  $Z_{LOSS}$  determined using tomograms and binary images. The validity of statistical assumptions for linear regression was checked by testing the normality of observations and homoscedasticity, respectively, with the Kolmogorov–Smirnov statistic and the Spearman rank correlation between absolute studentized residuals and observations of the dependent variable (Kutner et al. 2004). For each of the selected covariates, the homogeneity of slopes among levels of the fixed effect was tested and, if rejected, an unequal slope model was fit for the associated covariate. For significant fixed effects, mean separation was performed using Tukey’s honestly significant difference at multiple values of each covariate. Statistical analyses were performed using SAS 9.4 (SAS Institute, Inc., Cary, NC, USA); the ANOVA and ANCOVA models were fit using proc glm, and  $p_c$  was computed using the CCC macro v9 (Crawford et al. 2007).

### Results

$A_D$ , the percent of total damaged cross-sectional area measured in sonic tomograms, was mostly less than binary images, but the difference was smaller when using GVB to select damaged parts in tomograms. On average,  $A_D$  measured in tomograms was 25% and 14%, respectively, less

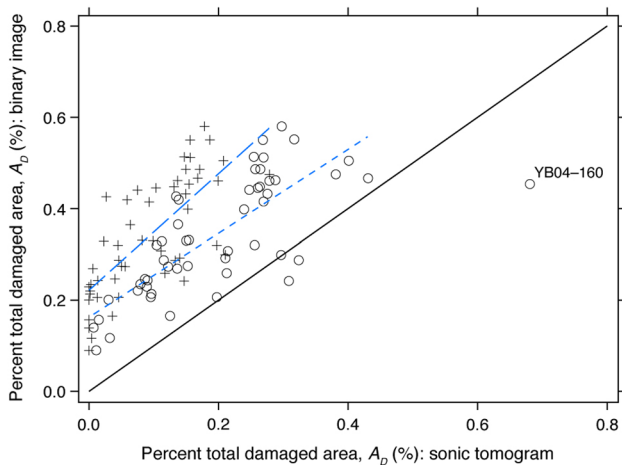
**Table 3** Parameter estimates, confidence intervals, and coefficients of determination for linear regression models fit to geometric attributes derived from sonic tomograms and binary images of the destructively measured internal condition of trees

	<i>b</i> (95% CI)	<i>p</i>	<i>a</i> (95% CI)	<i>p</i>	<i>r</i> <sup>2</sup>
$A_D$ (%)					
VB <sup>a</sup>	0.22 (0.18–0.26)	<0.001	1.27 (0.94–1.61)	<0.001	0.55
GVB	0.16 (0.11–0.21)	<0.001	0.92 (0.70–1.14)	<0.001	0.59
$L_O$ (m)					
VB	$2.18 \times 10^{-3}$ (–1.08 to 1.52) $\times 10^{-2}$	0.736	0.52 (0.39–0.64)	<0.001	0.62
GVB	$6.59 \times 10^{-4}$ (–1.37 to 1.50) $\times 10^{-2}$	0.927	0.60 (0.44–0.76)	<0.001	0.56
$R_T$					
–	0.20 (0.07–0.33)	0.003	0.75 (0.60–0.90)	<0.001	0.66
$R_D$					
VB	0.47 (0.32–0.63)	<0.001	0.22 (–0.07 to 0.51)	0.140	0.05
GVB	0.20 (0.00–0.40)	0.052	0.66 (0.32–1.00)	<0.001	0.25

Linear functions of the form  $y = ax + b$  were fit to the observations of geometric attributes:  $A_D$  (%), the percent of total damaged cross-sectional area;  $L_O$  (m), the offset length between the centroid of the trunk and the centroid of the largest damaged part;  $R$  (dimensionless), the roundness of the trunk,  $R_T$ , and largest damaged part,  $R_D$

<sup>a</sup>For each sonic tomogram, either violet and blue (VB) or green, violet, and blue (GVB) was used to select damaged parts. In a PiCUS<sup>®</sup> sonic tomogram, the four colors used to visualize acoustic transmission speeds and the corresponding internal wood condition are as follows: brown, solid; green, intermediate; violet, damaged; blue, damaged

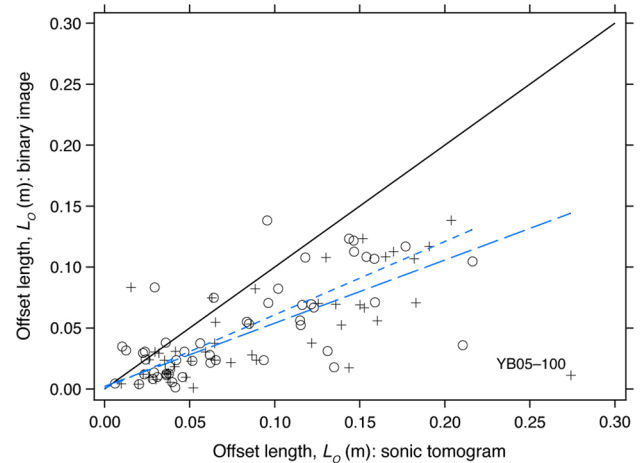




**Fig. 3** Scatter plot of the percent of total damaged cross-sectional area,  $A_D$  (%), measured in sonic tomograms against  $A_D$  measured in a reference binary image of the destructively measured internal condition of trees. For the estimates derived from tomograms, damaged parts were selected using either green, violet, and blue (GVB, circle) or violet and blue (VB, plus). Most values are located above the solid black 1:1 comparison line, indicating a repeated underestimation of  $A_D$  in tomograms relative to binary images. In contrast,  $A_D$  measured using GVB for one yellow birch (*Betula alleghaniensis*) trunk 160 cm above ground (labeled YB04-160) was overpredicted by 23%, a distinct outlier. Least-squares regression equations are  $y=0.22+1.27x$  (blue, long dash line) and  $y=0.16+0.92x$  (blue, short dash line) for  $A_D$  computed using VB and GVB, respectively. See Table 3 for model parameter estimates and fit statistics

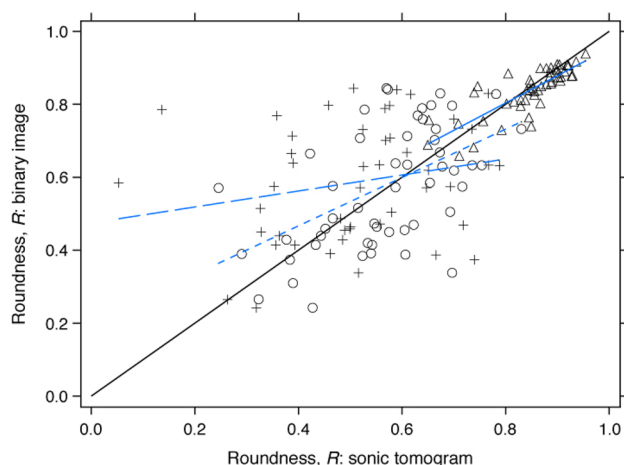
than binary images when using VB or GVB to select damaged parts. Significant correlations between  $A_D$  measured in tomograms and binary images indicated that the size of damaged parts in tomograms was proportional to their actual size in binary images, but the difference in  $p_c$  showed that  $A_D$  computed using GVB was closer to the actual  $A_D$  in binary images (Table 2). For one yellow birch (*Betula alleghaniensis*) section 160 cm above ground (YB04-160),  $A_D$  measured using GVB was overpredicted by 23%, and this value was a distinct outlier ( $D=2.12$ ) because of the disproportionately large green area in the associated tomogram. Excluding this outlier, regression indicated significant linear relationships between  $A_D$  measured from tomograms and binary images using GV ( $p < 0.001$ ) and GVB ( $p < 0.001$ ) (Table 3). For these functions, coefficients of determination indicated that  $A_D$  measured from tomograms using GV ( $r^2=0.54$ ) and GVB ( $r^2=0.59$ ) accounted for considerable variation in  $A_D$  measured from binary images, suggesting that the repeated underestimation of  $A_D$  in the examined cross sections was reasonably predictable (Fig. 3).

In contrast,  $L_O$  measured in sonic tomograms was mostly greater than in binary images, but the measurements differed less when using GVB to select damaged parts in tomograms. On average,  $L_O$  measured in tomograms was 4.4 cm and 3.2 cm, respectively, greater than binary images



**Fig. 4** Scatter plot of the offset length,  $L_O$  (m), measured in sonic tomograms against  $L_O$  measured in a reference binary image of the destructively measured internal condition of trees. For the estimates derived from tomograms, damaged parts were selected using either green, violet, and blue (GVB, circle) or violet and blue (VB, plus). Most values are located below the solid black 1:1 comparison line, indicating a repeated overestimation of  $L_O$  in tomograms relative to binary images. Uniquely,  $L_O$  measured using two colors for one yellow birch (*Betula alleghaniensis*) trunk 100 cm above ground (labeled YB05-100) was overpredicted by 26.3 cm, a distinct outlier. Least-squares regression equations are  $y=6.59 \times 10^{-4} + 0.60x$  (blue, long dash line) and  $y=2.18 \times 10^{-3} + 0.52x$  (blue, short dash line) for  $L_O$  computed using VB and GVB, respectively. See Table 3 for model parameter estimates and fit statistics

when using GV or GVB to select damaged parts. Significant correlations between  $L_O$  measured in tomograms and binary images indicated that the position of damaged parts in tomograms was proportional to their actual position in binary images, but the difference in  $p_c$  showed that  $L_O$  computed using GVB was closer to the actual  $L_O$  in binary images (Table 2). For one yellow birch cross section 100 cm above ground (YB05-100),  $L_O$  measured using VB was overpredicted by 26.3 cm. This value was a distinct outlier ( $D=2.11$ ), because the largest damaged part was depicted near the trunk periphery in the tomogram—a considerable distance from the largest damaged part at the center of the cross section in the corresponding binary image. Excluding this outlier, regression indicated significant linear relationships between  $L_O$  measured from tomograms and binary images using GV ( $p < 0.001$ ) and GVB ( $p < 0.001$ ) (Table 3). For these functions, coefficients of determination indicated that  $L_O$  measured from tomograms using GV ( $r^2=0.62$ ) and GVB ( $r^2=0.56$ ) accounted for considerable variation in  $L_O$  measured from binary images, suggesting that the repeated overestimation of  $L_O$  in the examined cross sections was reasonably predictable (Fig. 4). For these regression functions, the intercept was not significantly different from zero when using GV ( $p=0.736$ ) or GVB ( $p=0.927$ ) to select damaged parts in tomograms, indicating that the overestimation of



**Fig. 5** Scatter plot of the roundness,  $R$  (dimensionless), of the largest damaged part,  $R_D$ , and trunk,  $R_T$ , measured in sonic tomograms against the same measured in a binary image of the destructively measured internal condition of trees. For the estimates derived from tomograms,  $R_D$  was determined using either green, violet, and blue (GVB, circle) or violet and blue (VB, plus);  $R_T$  was computed using the blue trunk geometry line (triangle). Least-squares regression equations are  $y=0.47+0.22x$  (blue, long dash line) and  $y=0.20+0.75x$  (blue, short dash line) for  $R_D$  computed using VB and GVB, respectively; the equation for  $R_T$  is  $y=0.20+0.75x$  (blue, solid line). See Table 3 for model parameter estimates and fit statistics

$L_O$  in tomograms increased in proportion to the actual  $L_O$  in binary images (Fig. 4).

On average,  $R_T$  for sonic tomograms (mean 0.850) and binary images (mean 0.841) was greater than  $R_D$  measured in binary images (mean 0.570) and tomograms using GV (mean 0.512) or GVB (mean 0.570), indicating that a circle better approximated the shape of trunks than damaged parts for this set of trees. Among all geometric features examined in this study,  $r$ ,  $\rho$ , and  $p_c$  were the greatest for  $R_T$  measured in tomograms and binary images, indicating that  $R_T$  depicted in tomograms was very similar to the actual  $R_T$  in binary images (Table 2). Regression indicated a significant linear relationship between  $R_T$  measured from tomograms and binary images ( $p < 0.001$ ) with a high coefficient of determination ( $r^2 = 0.66$ ) (Table 3; Fig. 5).

In contrast, the shape of damaged parts in binary images, measured in terms of  $R_D$ , was poorly depicted in sonic tomograms, and this was especially true for damaged parts selected using only VB. Among all geometric features examined in this study,  $r$ ,  $\rho$ , and  $p_c$  were the lowest for  $R_D$  measured in tomograms and binary images, implying greater dissimilarity between the  $R_D$  measured using the two images. Regression indicated a significant linear relationship only between  $R_D$  measured in tomograms and binary images using GVB ( $p < 0.001$ ); the associated coefficients of determination indicated that  $R_D$  determined using GV ( $r^2 = 0.05$ )

**Table 4** Analysis of variance of the effect of mathematical methods and colors used to select damaged parts on the absolute difference (%) between maximum  $Z_{LOSS}$  determined using sonic tomograms and binary images of the destructively measured internal condition of trees

Effect <sup>a</sup>	df	<i>F</i>	<i>p</i>	Level	LS mean (SE) <sup>b</sup>
Colors	1, 700	41.77	<0.001	VB	0.23 (0.01)a
				GVB	0.17 (0.01)b
Methods	6, 700	13.42	<0.001	Ciftci I(a)	0.16 (0.01)a
				Ciftci I(b)	0.19 (0.01)a
				Ciftci I(c)	0.17 (0.01)a
				Ciftci II	0.19 (0.01)a
				Coder	0.27 (0.01)b
				<i>zloss</i>	0.16 (0.01)a
Colors × methods	6, 700	0.53	0.785	Wagener	0.24 (0.01)b

<sup>a</sup>Fixed effects include mathematical methods used to estimate  $Z_{LOSS}$  from sonic tomograms: Ciftci I(a), Ciftci I(b), Ciftci I(c), Ciftci II, Coder, Numerical, and Wagener; colors used to select damaged parts in sonic tomograms: violet and blue (VB) and green, violet, and blue (GVB); and their interaction: methods × colors. See the accompanying text for more information about the various mathematical methods used to compute  $Z_{LOSS}$

<sup>b</sup>Least squares (LS) means followed by the same letter are not significantly different at the  $\alpha = 0.05$  level

and GVB ( $r^2 = 0.25$ ) in tomograms accounted for little variation in  $R_D$  measured from binary images (Table 3).

Analysis of variance indicated that the mathematical methods and colors used to select damaged parts significantly affected the absolute difference (%) between  $Z_{LOSS}$  determined using tomograms and binary images, but these two factors did not interact to affect the absolute difference between  $Z_{LOSS}$  determined using the two image types (Table 4). Overall, the absolute difference (%) between  $Z_{LOSS}$  determined using tomograms and binary images was significantly less for estimates using GVB to select damaged parts than for others using VB. Overall, the average absolute difference in  $Z_{LOSS}$  was 6% less for estimates using GVB compared to others using only VB. Among mathematical methods, pairwise comparisons revealed that the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images was significantly greater for analytical methods neglecting the position of damaged parts (i.e., Coder and Wagener). Overall, the error associated with these estimates was between 5% and 9% greater than for the other methods, which did not differ significantly from one another (Table 4).

In terms of the actual difference between  $Z_{LOSS}$  determined using tomograms and binary images, all mathematical methods underestimated  $Z_{LOSS}$  in most cases. For Coder and Wagener, respectively,  $Z_{LOSS}$  determined using tomograms was, on average, 25% and 21% less than determined

numerically using binary images; these two methods underestimated  $Z_{LOSS}$  in 98% of all cases. For the remaining methods, the average actual difference was smaller, but the estimates determined using tomograms were still less than determined numerically using binary images in most cases. Among these methods, the average actual difference between  $Z_{LOSS}$  determined using tomograms and binary images was, in decreasing order: Ciftci I(b), 14%; Ciftci II, 11%; Ciftci I(c), 9%; *zloss*, 9%; Ciftci I(a), 4%.

Among all tested covariates,  $L_O$  ( $F = 26.72$ ;  $df = 7, 658$ ;  $p < 0.001$ ) and  $A_D$  (error) ( $F = 17.68$ ;  $df = 7, 658$ ;  $p < 0.001$ ) were selected as the only variables showing a significant linear relationship with the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images. Although the slopes describing the change in the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images over a unit change in  $L_O$  varied significantly among mathematical methods ( $F = 4.95$ ;  $df = 6, 658$ ;  $p < 0.001$ ), the same was not true for the slopes describing the change in this difference over a unit change in  $A_D$  (error) ( $F = 1.17$ ;  $df = 6, 658$ ;  $p = 0.322$ ). As a result, a common slope was used to describe the relationship between  $A_D$  (error) and the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images for all mathematical methods, and unequal slopes were fit to describe the relationship between  $L_O$  and the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images for each mathematical method

individually. Using this model, analysis of covariance revealed that mathematical methods significantly affected the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images, after accounting for  $L_O$  and  $A_D$  (error). Except for Coder, the intercepts associated with each method were not significantly different from zero, indicating that the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images is minimized to effectively zero for most mathematical methods when the largest damaged part is concentric and  $A_D$  is depicted accurately in tomograms. Except for *zloss*, all the slopes describing the relationship between  $L_O$  and the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images were significantly different from zero, indicating that, among all methods, the numerical approach was the least sensitive to changes in  $L_O$  (Table 5).

Mean separation, performed at six combinations of the two covariates selected to represent the observed range of  $A_D$  (error) and  $L_O$ , revealed that differences among mathematical methods existed only for  $L_O > 0$ . At  $A_D$  (error) = 0 and  $L_O = 0$ , there were no significant differences in the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images among the mathematical methods, and there were similarly no significant differences among methods at  $A_D$  (error) = 0.4 and  $L_O = 0$ , since a common slope was fit to all observations of  $A_D$  (error) and the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images. For all mathematical methods, the absolute

**Table 5** Analysis of covariance of the effect of mathematical methods on the absolute difference (%) between maximum  $Z_{LOSS}$  determined using sonic tomograms and binary images of the destructively measured internal condition of trees, after accounting for geometric features of the examined cross sections

Effect <sup>a</sup>	df	F	p	Level	Parameter estimate (95% CI)	p
Method	7, 664	2.07	0.045	Ciftci I(a)	0.02 (−0.020 to 0.062)	0.308
				Ciftci I(b)	0.01 (−0.029 to 0.052)	0.582
				Ciftci I(c)	0.02 (−0.025 to 0.057)	0.447
				Ciftci II	0.04 (−0.006 to 0.076)	0.093
				Coder	0.07 (0.031 to 0.113)	0.001
				<i>zloss</i>	0.04 (−0.006 to 0.076)	0.097
				Wagener	0.03 (−0.010 to 0.072)	0.136
$A_D$ (error)	1, 664	116.59	<0.001	–	0.46 (0.379 to 0.548)	<0.001
$L_O \times$ method	7, 664	26.74	<0.001	Ciftci I(a)	0.51 (0.153 to 0.868)	0.005
				Ciftci I(b)	1.02 (0.661 to 1.376)	<0.001
				Ciftci I(c)	0.72 (0.362 to 1.077)	<0.001
				Ciftci II	0.72 (0.360 to 1.075)	<0.001
				Coder	1.32 (0.959 to 1.674)	<0.001
				<i>zloss</i>	0.34 (−0.023 to 0.692)	0.067
				Wagener	1.43 (1.073 to 1.788)	<0.001

<sup>a</sup>Fixed effects include mathematical methods used to estimate  $Z_{LOSS}$  from sonic tomograms: Ciftci I(a), Ciftci I(b), Ciftci I(c), Ciftci II, Coder, Numerical, and Wagener; see the accompanying text for more information about the various mathematical methods used to compute  $Z_{LOSS}$ . Covariates include  $A_D$  (error) (%), the absolute difference between the percent of total damaged cross-sectional area measured using tomograms and binary images of the destructively measured internal condition of trees, and  $L_O$  (m), the offset length between the centroid of the trunk and the centroid of the largest damaged part. The form of the associated model is  $y_{ij} = \alpha_i + \beta_i w + \gamma x + e_{ij}$ , where  $\alpha_i$  denotes the intercept of the  $i$ th mathematical method,  $\beta_i$  denotes the slope of the  $i$ th mathematical method with respect to the covariate  $w$  ( $L_O$ ),  $\gamma$  denotes the overall slope with respect to the covariate  $x$  [ $A_D$  (error)], and  $e_{ij}$  denotes the experimental unit error

**Table 6** Mean separation for the analysis of covariance of the effect of mathematical methods on the absolute difference (%) between maximum  $Z_{LOSS}$  determined using sonic tomograms and binary

images of the destructively measured internal condition of trees, determined at six combinations of two covariates accounting for geometric features of the examined cross sections

$A_D$ (error) <sup>a</sup>	0			0.4			
	$L_O$ method	0	0.13	0.25	0	0.13	0.25
Ciftci I(a)		0.02 (0.02)a	0.09 (0.02)ab	0.15 (0.03)ab	0.21 (0.02)a	0.27 (0.02)ab	0.33 (0.03)ab
Ciftci I(b)		0.01 (0.02)a	0.14 (0.02)b	0.27 (0.03)bc	0.20 (0.02)a	0.33 (0.02)b	0.45 (0.03)bc
Ciftci I(c)		0.02 (0.02)a	0.11 (0.02)ab	0.20 (0.03)ab	0.20 (0.02)a	0.30 (0.02)ab	0.38 (0.03)ab
Ciftci II		0.04 (0.02)a	0.13 (0.02)ab	0.21 (0.03)ab	0.22 (0.02)a	0.31 (0.02)ab	0.40 (0.03)ab
Coder		0.07 (0.02)a	0.24 (0.02)c	0.40 (0.03)d	0.26 (0.02)a	0.43 (0.02)c	0.59 (0.03)d
<i>zloss</i>		0.03 (0.02)a	0.08 (0.02)a	0.12 (0.03)a	0.22 (0.02)a	0.26 (0.02)a	0.30 (0.03)a
Wagener		0.03 (0.02)a	0.22 (0.02)c	0.39 (0.03)cd	0.22 (0.02)a	0.40 (0.02)c	0.57 (0.03)cd

<sup>a</sup>Covariates include  $A_D$  (error) (%), the absolute difference between the percent of total damaged cross-sectional area measured using tomograms and binary images of the destructively measured internal condition of trees, and  $L_O$  (m), the offset length between the centroid of the trunk and the centroid of the largest damaged part. Within each column, least-squares (LS) means followed by the same letter are not significantly different at the  $\alpha=0.05$  level

difference between  $Z_{LOSS}$  determined using tomograms and binary images increased by 46% over a unit change in  $A_D$  (error) (note that the possible range for  $A_D$  (error) is [0, 1]). However, consistent differences arose among mathematical methods for  $L_O > 0$ , owing to the different slopes fit to observations of  $L_O$  and the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images for each method separately (Table 5). For these cases, the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images was greatest for Coder and Wagener, since these methods neglected  $L_O$ . The remaining methods, in decreasing order of the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images, were: Ciftci I(b), Ciftci II, Ciftci I(c), Ciftci I(a), and *zloss* (Table 6).

## Discussion

For decayed sections, most authors similarly observed that  $A_D$  was underestimated in sonic tomograms in a range of tree species (Deflorio et al. 2008; Gilbert and Smiley 2004; Liang et al. 2007; Liang and Fu 2012; Marra et al. 2018; Wang et al. 2007, 2009). In agreement with these findings, Wang et al. (2009) also reported that the average difference between  $A_D$  determined using sonic tomograms and destructive measurements was greater when using VB (mean 14%) than GVB (mean 2%) to select damaged parts. In other reports, authors only used two colors to select damaged parts in sonic tomograms, and the reported average underestimation of  $A_D$  ranged between < 1% (Ostrovsky et al. 2017) and 14% (Wang et al. 2009). However, some authors computed  $A_D$  using coarse grid systems with cell dimensions ranging between 5 mm (Gilbert and Smiley 2004) and 12.5 mm (Ostrovsky et al. 2017), contributing unknown error to the approximation.

It is possible that the underestimation of  $A_D$  arises from the reduced sensitivity of sonic tomography to low-velocity features (Li et al. 2012) that limits the detection of incipient decay (Deflorio et al. 2008), and practitioners should account for this limitation when interpreting tomograms, especially in light of the consensus among related studies. Others have reported, in agreement with this study, a strong linear relationship between  $A_D$  determined using tomograms and destructive measurements (Gilbert and Smiley 2004; Liang and Fu 2012). In a sample of 15 decayed sections, Liang and Fu (2012) reported much better agreement between  $A_D$  determined using sonic tomograms and destructive measurements; the slope of a linear model fit to these observations was much closer to one than in this study, with a high coefficient of determination ( $r^2=0.94$ ) despite using only VB to select damaged parts. Although Gilbert and Smiley (2004) also reported a strong linear relationship between the amount of decay depicted in tomograms and measured on the images of decayed cross sections ( $r^2=0.94$ ), the authors did not fit a linear regression model to the observations, precluding a comparison of model coefficients. Compared to existing reports, there was a greater underestimation of  $A_D$  in sonic tomograms in this study. Still, practitioners should use caution when considering the use of regression models from this study to adjust tomographic estimates, because the underlying observations were limited to three species at a single site. Although our sample of decayed sections was relatively large, it will be important to examine further the relationship between  $A_D$  determined using tomograms and destructive measurements across several sites and species in future work.

Conversely, most existing reports indicated that  $A_D$  was overestimated in sonic tomograms for sections with internal cracks (Liang et al. 2007; Wang et al. 2009; Wang and



Allison 2008). In this study, only one of the examined sections (SM05–100) contained a crack, but it occurred alongside internal decay, preventing a separate evaluation of this type of defect. Without adjustment, this means that  $Z_{LOSS}$  determined using tomograms would tend to be liberal and conservative for cracks and decay, respectively, and practitioners should consider these trends when computing  $Z_{LOSS}$  from tomograms. Future studies should examine the accuracy of tomograms, in terms of  $A_D$ , for each type of defect separately, taking care to separate those cracks present during tomographic measurement from others created by drying after felling.

Among related studies, this is the first report of a repeated overestimation of  $L_O$  in sonic tomograms. In a sample of 17 decayed sections, Gilbert and Smiley (2004) observed that, in terms of the location of damaged parts, 2% and 9% of  $A_D$  were false-positive and -negative estimates that did not match the internal condition of sections. However,  $L_O$  is arguably a better feature to examine, in terms of  $Z_{LOSS}$ , because damaged parts decrease  $I$  proportional to the square of this distance (Eq. 18). The observed repeated overestimation of  $L_O$  in sonic tomograms should contribute to an equivalent overestimation of  $Z_{LOSS}$ , proportional to  $A_D$  (Eq. 18). Like  $A_D$ , the difference between  $L_O$  determined using tomograms and binary images was greater when using VB than GVB to select damaged parts, further justifying the addition of color(s) representing intermediate acoustic transmission speeds when analyzing tomograms, despite its usual omission by the manufacturer's software.

The accuracy of  $Z_{LOSS}$  estimates improved when using GVB to select damaged parts, corroborating the direct comparisons between geometric attributes in this study and other reports that these colors should be used to select damaged parts (Marra et al. 2018; Wang et al. 2009). Among the evaluated methods, the difference between  $Z_{LOSS}$  determined using tomograms and binary images for Coder and Wagener was significantly greater than all other methods. Considering this difference, practitioners should avoid using methods neglecting  $L_O$  to estimate  $Z_{LOSS}$ , in agreement with Kane and Ryan (2004). Although Liang and Fu (2012) reported a much smaller difference between strength-loss estimates determined using tomograms and destructive measurements, the reported difference was determined only by the accuracy of tomograms, because the same method was applied to tomograms and destructive measurements in each case. In this study, the methods used to estimate  $Z_{LOSS}$  from tomograms were compared with an improved numerical method,  $zloss$ , applied to binary images.

The difference between  $Z_{LOSS}$  determined using tomograms and binary images did not vary with  $R_T$  or  $R_D$ , supporting the use of circles to approximate irregular shapes by the existing analytical methods (Ciftci et al. 2014; Coder 1989; Smiley and Fraedrich 1992; Wagener 1963). However,

some authors have reported that  $A_D$  (error)  $\propto R^{-1}$  (Gilbert et al. 2016; Rabe et al. 2004; Rust 2017) and the use of circles for highly irregular trunk shapes may be less appropriate in these situations. The selection of  $A_D$  (error) and  $L_O$  as covariates means that the accuracy of  $Z_{LOSS}$  estimates was primarily affected by the underestimation of  $A_D$  in tomograms and the actual  $L_O$  of the largest damaged part. Based on this analysis, it is apparent that the value of a method, relative to others examined in this study, depends largely on its consideration and approach to  $L_O$ ; all methods were similarly affected by the underestimation of  $A_D$  in sonic tomograms. After accounting for  $A_D$  (error) and  $L_O$ , the consistent ranking among methods used to estimate  $Z_{LOSS}$ , caused by the unequal slopes fit to each method for  $L_O$ , usefully revealed methods that should be considered for greater use by arborists. Uniquely, the slope fit to  $zloss$  was not significantly different from zero, and the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images was lowest for this method at all selected values of the covariates. As a result, the accuracy of this method was mostly determined by the error in estimating  $A_D$ , and this provides justification for using this method as a benchmark, since it was least sensitive to changes in  $L_O$ .

Among the remaining analytical methods proposed by Ciftci et al. (2014), Ciftci I(a) and I(c) gave better estimates, in terms of the absolute difference between  $Z_{LOSS}$  determined using tomograms and binary images, than Ciftci II and I(b). The former two methods relied, in whole or part, on circumscribed circles fit to the trunk and largest damaged part. Since  $R_T > R_D$  for the examined sections, the circumscribed circles enlarged the area of damaged parts (mean + 86%) more than trunks (mean + 19%), relative to their corresponding area in tomograms, resulting in an average increase to  $A_D$  of 7.5% and 2.5%, respectively, for Ciftci I(a) and I(c). The increased  $A_D$  usefully offset its underestimation in tomograms, explaining the improved estimates offered by these two methods. Notably, solutions were available in all cases using Ciftci I(a), but the same was not true for all cases using other methods. For example,  $Z_{LOSS}$  could not be estimated using Ciftci I(b), I(c), and II for one sugar maple cross section 80 cm above ground (SM28–080), because the damaged part was completely outside and did not intersect the solid trunk. Although Ciftci I(a) offered relatively superior estimates among the analytical methods proposed by Ciftci et al. (2014), it is useful to note that these methods are not strictly analytical, because they require image processing techniques, limiting their usefulness to practitioners.

Despite considering only the largest damaged part, the analytical estimates differed modestly from the numerical estimate computed from binary images in most cases. On average, the percent of total area occupied by the largest damaged part was 11% (SD 16%) less than  $A_D$ . Still, the

analytical methods gave sizeable underestimates of  $Z_{\text{LOSS}}$  in some cases, because they neglected to consider one or more additional damaged parts. In one American beech section 60 cm above ground (AB06–060), the largest damaged part was in the center of the section, but the analytical estimate omitted the contributions from the second largest damaged part at the trunk periphery, causing  $Z_{\text{LOSS}}$  to be underestimated by, on average, 16% among the six analytical methods.

The PiCUS Q74 software, like other sonic tomography devices, provides a built-in function to give an approximate estimate of the percent residual load-bearing capacity (Gocke 2017) equal to:

$$I_{\text{du}}/I_{\text{Du}} \times 100, \quad (27)$$

where  $I_{\text{du}}$  and  $I_{\text{Du}}$  are the second moments of area computed about the section's centroid using the diameter of the damaged part (d) and trunk (D). To determine these diameters, the software requires users to select the boundary between damaged and solid wood, and it computes the lengths along a radius formed by the centroid and user-selected location (A. Richter, personal communication). This excludes considerable information in the tomogram from the estimate. Since Eq. 27 corresponds to  $1 - \text{Eq. 2}$ , its performance can be considered equivalent to that ascribed to Coder in this study. Practitioners are cautioned against using this built-in function when eccentric decay is present, because Kane and Ryan (2004) demonstrated that Eq. 2 performed poorly in these cases.

It is possible that the image binarization process used in this study introduced unknown error into the  $Z_{\text{LOSS}}$  estimates derived from binary images. Although the existence of damaged wood was obvious in most of the examined sections, error may have occurred in determining the precise boundary between damaged and solid wood. In the future, authors should consider alternative methods to binarize images for  $Z_{\text{LOSS}}$  estimates. Likewise, the assumption of material isotropy may have introduced negligible error into the  $Z_{\text{LOSS}}$  estimates (Ciftci et al. 2014), and authors should consider these effects, when relevant material properties information is available, in future work.

## Conclusion

Among the evaluated methods,  $Z_{\text{LOSS}}$  was best estimated using sonic tomograms numerically with *zloss* or analytically with Ciftci I(a), and practitioners should consider using these methods to assess the severity of internal defects measured with sonic tomography. The numerical method *zloss* addressed the simplifying assumptions contained in many existing methods by accommodating more geometric detail in the associated

calculations, including irregular shapes and multiple offset damaged parts. Still, the repeated under- and overestimation, respectively, of  $A_{\text{D}}$  and  $L_{\text{O}}$  in tomograms limits the accuracy of  $Z_{\text{LOSS}}$  estimates based on tomography, and these limitations should be considered when interpreting estimates. It is important to note that  $Z_{\text{LOSS}}$  only estimates the reduced load-bearing capacity of the measured tree part (not the entire tree). Even more, the methods described in this article do not estimate the probability of tree failure, which requires a more thorough accounting of the total applied and resistive forces acting on a tree. There is little scientific consensus on a threshold value associated with a change in the likelihood of failure (Gruber 2008), but Kane (2014) showed that failure at an area with existing or simulated decay was more likely when  $I_{\text{LOSS}} > 30\%$ .

**Author contribution statement** DB and BK conceived and designed the study, NB and RM collected the data, DB analyzed data and wrote the manuscript, and all authors edited the manuscript.

**Funding** Funding for tomography and destructive measurements was provided by the National Science Foundation EARly-Concept Grants for Exploratory Research (EAGER) Program (Grant #DEB-1346258). Additional funding for numerical analysis was provided by the National Parks Board, Singapore.

## Compliance with ethical standards

**Conflict of interest** The authors declare that they have no conflict of interest.

## References

- Arciniegas A, Prieto F, Brancheriau L, Lasaygues P (2014) Literature review of acoustic and ultrasonic tomography in standing trees. *Trees* 28:1559–1567
- Brazee NJ, Marra RE, Gocke L, Van Wassenae P (2011) Non-destructive assessment of internal decay in three hardwood species of northeastern North America using sonic and electrical impedance tomography. *Forestry* 84:33–39
- Burcham DC (2017) *zloss*. GitHub, version 1.1. <https://github.com/danielburcham/zloss>. Accessed 29 Nov 2017
- Ciftci C, Kane B, Brena SF, Arwade SR (2014) Loss in moment capacity of tree stems induced by decay. *Trees* 28:517–529
- Coder KD (1989) Should or shouldn't you fill tree hollows? *Grounds Maint* 24:68–70 (72–73, 100)
- Crawford SB, Kosinski AS, Lin HM, Williamson JM, Barnhart HX (2007) Computer programs for the concordance correlation coefficient. *Comput Methods Progr Biomed* 88:62–74
- Deflorio G, Fink S, Schwarze FW (2008) Detection of incipient decay in tree stems with sonic tomography after wounding and fungal inoculation. *Wood Sci Technol* 42:117–132
- Ennos AR (2012) *Solid biomechanics*. Princeton University Press, Princeton
- Gilbert EA, Smiley ET (2004) Picus sonic tomography for the quantification of decay in white oak (*Quercus alba*) and hickory (*Carya* spp.). *J Arboric* 30:277–281

- Gilbert GS, Ballesteros JO, Barrios-Rodriguez CA, Bonadies EF, Cedeno-Sanchez ML, Fossatti-Caballero NJ, Trejos-Rodriguez MM, Perez-Suniga JM, Holub-Young KS, Henn LAW, Thompson JB, Garcia-Lopez CG, Romo AC, Johnston DC, Barrick PP, Jordan FA, Hershovich S, Russo N, Sanchez JD, Fabrega JP, Lumpkin R, McWilliams HA, Chester KN, Burgos AC, Wong EB, Diab JH, Renteria SA, Harrower JT, Hooton DA, Glenn TC, Faircloth BC, Hubbell SP (2016) Use of sonic tomography to detect and quantify wood decay in living trees. *Appl Plant Sci* 4:1–13
- Gocke L (2017) PiCUS Sonic Tomograph: Software Manual Q74. Argus Electronic GmbH, Rostock, Germany
- Gruber F (2008) Reply to the response of Claus Mattheck and Klaus Bethge to my criticisms on untenable VTA-failure criteria. Who is right and who is wrong? *Arboric J* 31:277–296
- Johnstone D, Moore G, Tausz M, Nicolas M (2010) The measurement of wood decay in landscape trees. *Arboric Urban For* 36:121–127
- Kane B (2014) Determining parameters related to the likelihood of failure of red oak (*Quercus rubra* L.) from winching tests. *Trees* 28:1667–1677
- Kane B, Ryan HDP (2004) The accuracy of formulas used to assess strength loss due to decay in trees. *J Arboric* 30:347–356
- Kane B, Ryan HDP, Bloniarz DV (2001) Comparing formulae that assess strength loss due to decay in trees. *J Arboric* 27:78–87
- Koizumi A, Hirai T (2006) Evaluation of the section modulus for tree-stem cross sections of irregular shape. *J Wood Sci* 52:213–219
- Kutner MH, Nachtsheim CJ, Neter J (2004) Applied linear regression models. McGraw-Hill Irwin, Boston
- Legland D (2015) *matGeom*. GitHub, <https://github.com/mattools/matGeom/>
- Li L, Wang X, Wang L, Allison RB (2012) Acoustic tomography in relation to 2D ultrasonic velocity and hardness mappings. *Wood Sci Technol* 46:551–561
- Liang S, Fu F (2012) Strength loss and hazard assessment of *Euphrates poplar* using stress wave tomography. *Wood Fiber Sci* 44:1–9
- Liang S, Wang X, Wiedenbeck J, Cai Z, Fu F (2007) Evaluation of acoustic tomography for tree decay detection. In: 15th international symposium on nondestructive testing of Wood Duluth, MN, US, pp 49–54
- Marasinghe MG, Kennedy WJ (2008) SAS for data analysis: intermediate statistical methods. In: Chambers J, Hardle W, Hand D (eds) *Statistics and computing*. Springer, New York, p 557
- Marra RE, Brazee N, Fraver S (2018) Estimating carbon loss due to internal decay in living trees using tomography: implications for forest carbon budgets. *Environ Res Lett* 13:105004
- Niklas KJ (1992) *Plant biomechanics: an engineering approach to plant form and function*. University of Chicago Press, Chicago
- Ostrovsky R, Kobza M, Gazo J (2017) Extensively damaged trees tested with acoustic tomography considering tree stability in urban greenery. *Trees* 31:1015–1023
- Rabe C, Ferner D, Fink S, Schwarze FW (2004) Detection of decay in trees with stress waves and interpretation of acoustic tomograms. *Arboric J* 28:3–19
- Rust S (2017) Accuracy and reproducibility of acoustic tomography significantly increase with precision of sensor position. *J For Landsc Res* 1:1–6
- Smiley ET, Fraedrich BR (1992) Determining strength loss from decay. *J Arboric* 18:201–204
- Smiley ET, Matheny N, Lilly S (2011) *Tree risk assessment*. International Society of Arboriculture, Champaign
- Steger C (1996) On the calculation of moments of polygons. Technical University of Munich, FGBV-96-04, Munich, pp 1–14
- Wagener WW (1963) *Judging hazard from native trees in California recreational areas: a guide for professional foresters*. Pacific Southwest Forest and Range Experiment Station, Forest Service, US Department of Agriculture, PSW-P1, Berkeley, pp 1–29
- Wang X, Allison RB (2008) Decay detection in red oak trees using a combination of visual inspection, acoustic testing, and resistance microdrilling. *Arboric Urban For* 34:1–4
- Wang X, Allison RB, Wang L, Ross RJ (2007) Acoustic tomography for decay detection in red oak trees. Forest Products Laboratory, Forest Service, US Department of Agriculture, FPL-RP-642, Madison, pp 1–7
- Wang X, Wiedenbeck J, Liang S (2009) Acoustic tomography for decay detection in black cherry trees. *Wood Fiber Sci* 41:127–137

**Publisher's Note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.