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Crown responses to neighbor density and species identity in a young mixed deciduous stand

Ignacio Barbeito • Catherine Collet • **François Ningre**

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Abstract

Key message Density was more important in shaping crown structure than neighbor species identity. Both species showed high crown plasticity at alternative levels, which may explain species coexistence in mixed broadleaved forests with functionally similar species.

Abstract Understanding crown response to local competition is essential to predicting stand development in mixed stands. We analyzed data from an 8-year-old field experimental plantation mixing two species according to a crossed gradient of density and species proportion to quantify the effect of a broad range of local neighborhood conditions on the development of young trees at multiple crown levels. We used Fagus sylvatica and Acer pseudoplatanus, as two model deciduous species. They are considered functionally equivalent at the young stages, but with contrasting architectural patterns. For both species: (1) changes in density explained more of the variation on crown development than species proportion (2) much of the effect of competition was accounted for by variables at the stem level, while branch and leaf development within crowns were not directly altered by competition. Both species were able to modify their crowns at the stem level to compete

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I. Barbeito $(\boxtimes) \cdot C$. Collet \cdot F. Ningre INRA, UMR1092, Laboratoire d'Etude des Ressources Forêt Bois (LERFoB), Centre INRA de Nancy, 54280 Champenoux, France

e-mail: ignacio.barbeito@nancy.inra.fr

I. Barbeito - C. Collet - F. Ningre AgroParisTech, UMR1092, Laboratoire d'Etude des Ressources Forêt Bois (LERFoB), ENGREF, 14 rue Girardet, 54000 Nancy, France

with intra- and inter-specific neighbors: Acer and Fagus were taller with a highest proportion of Fagus as neighbors; Fagus displayed a lower crown base when the proportion of Fagus decreased, while Acer had a lower crown base when the proportion of Fagus around it increased. Both species showed common shapes in allometric relationships but contrasting responses at alternative crown levels. Acer exhibited broader intra-specific variation in its height–diameter relationship and in its crown length, while Fagus displayed higher individual variation of branch development and leaf area than Acer. This study demonstrates that differences in crown development strategy of each species in response to changes in local neighborhood conditions are an important factor in maintaining species coexistence in broadleaved forests and designing mixtures that persist over time.

Keywords Fagus sylvatica · Acer pseudoplatanus · Competition - Allometry - Branch architecture - Leaf area

Introduction

Individual tree crown architecture, namely the position, size and orientation of the branches and foliar arrangement along the branches, is a primary determinant of forest function and productivity. At the tree scale, it plays a critical role in the competition for space. Tree crown architecture strongly influences the ability to compete with neighboring trees, as it determines the amount of light intercepted by the tree. At the same time, the competitive environment of a tree strongly affects its available space to grow in and its light environment and consequently its crown dimensions and architecture (Osada [2006](#page-14-0); Schröter et al. [2012\)](#page-14-0). Most studies to date have typically used simple response variables to study tree response to varying neighborhood conditions, such as variations in stem or crown dimensions (Purves et al. [2007;](#page-14-0) Davies and Pommerening [2008](#page-13-0)). Few studies have aimed at revealing the detailed responses of tree crown architecture (Lintunen and Kaitaniemi [2010](#page-14-0)), but such measurements may be essential to better understand stand development in spatially diverse stands such as mixed stands.

Overall, several studies show that crown size and architecture respond to a variety of exogenous factors such as local competition (Thorpe et al. [2010](#page-14-0)), site fertility (Dieler and Pretzsch [2013\)](#page-14-0), topography (Lang et al. [2012](#page-14-0); Antin et al. [2013](#page-13-0)) and climate (Lines et al. [2012\)](#page-14-0) and to endogenous factors such as tree size (Thorpe et al. [2010,](#page-14-0) Antin et al. [2013](#page-13-0)) and species identity (Purves et al. [2007,](#page-14-0) Weiskittel et al. [2010\)](#page-14-0). In all studies, endogenous factors appeared to be far more important than exogenous factors, with tree species and tree size being the primary drivers of most crown variables. Competition with neighboring trees is also a major factor, which has been shown to affect crown size and architecture through its various components: proximity, size and species identity of neighbors (Davies and Pommerening, [2008](#page-13-0); Dieler and Pretzsch [2013\)](#page-14-0). However, analyses regarding the combined effects of density and neighboring species identity on crown variables are presently scarce or dependent on the response variable examined. For example, Kaitaniemi and Lintunen [\(2010](#page-14-0)) found that the effect of density on height and diameter growth was more prominent than the effect of neighbor identity in 4- to 35-year-old mixtures of conifers and broadleaved species. However, in another study performed on similar mixtures, Lintunen and Kaitaniemi [\(2010](#page-14-0)) identified that many branch-level variables were mainly affected by neighbor species identity.

Studies analyzing the effects of competition on crown size and architecture have focused on particular sets of architectural parameters: crown length or width (Thorpe et al. [2010\)](#page-14-0), crown rise (Ilomäki et al. [2003](#page-14-0)), crown asymmetry (Rouvinen and Kuuluvainen [1997](#page-14-0)), branch angle and branch diameter (Mäkinen and Colin [1999;](#page-14-0) Lintunen and Kaitaniemi [2010\)](#page-14-0), or branch characteristics and leaf area (Medhurst and Beadle [2001;](#page-14-0) Osada [2006\)](#page-14-0); with very few attempts to include a response at multiple crown levels (Weiskittel [2003](#page-14-0)). Quantifying the effects of local competition on the various components of crown architecture may be essential to understanding individual tree responses and to predict species ability to compete with neighboring trees. Parameters describing the various crown components are strongly correlated within and among trees, and an integrated approach that takes into account these correlations is required to analyze the crown components, their interactions and their combined effects in response to competition (Pretzsch and Dieler [2012;](#page-14-0) Weiskittel et al. [2007\)](#page-14-0).

In this study, we focus on Fagus sylvatica L. and Acer pseudoplatanus L., two species with similar ecological niches that are commonly found in intimate mixture in Western and Central Europe (Hein et al. [2009](#page-14-0)). Despite their similar growth in the young stages (Hein et al. [2007](#page-14-0); Wagner et al. [2010](#page-14-0)), the two species show enhanced growth in mixture with the other species (Collet et al. [2014](#page-13-0)). The highest production observed in even mixtures suggests a complementary effect for resource acquisition. The species have contrasting crown architectural patterns (Bell [1991\)](#page-13-0), with Fagus conforming to Troll's architectural model while Acer follows Rauh's model. We hypothesize that the complementary effect observed between the two species may originate from differences in crown development and crown responses to competition.

The general objectives of the study are: to analyze crown response of Fagus and Acer to competition from neighboring trees, to estimate whether differences in crown development may explain the complementary effect observed between the two species in the young stages. More specifically, we aim to answer the following questions: (1) To what extent are species-specific relationships among crown components influenced by density, size and species identity of neighboring trees? (2) To what extent are the effects of competition on crown components accounted for indirectly by competition effects on stem parameters (diameter and height)? (3) Do the effects of competition on crown development differ between Acer and Fagus?

We used an experimental Fagus–Acer plantation where soil and climate were not limiting factors and where large gradients of density and species proportion allowed observing changes in crown architecture directly related to inter- and intra-specific competition for light or physical contact by neighboring trees. We developed a model describing tree crown at multiple levels (stem, growth units, branches and leaves) and analyzed relationships among crown components following a hierarchical approach where parameters reflecting higher level components were systematically introduced in models describing lower level components.

Materials and methods

Study site

The study was conducted in the forest of Haye, near Nancy, North-Eastern France (48°38'17.18"N, 6°8'43.03"E), located on a limestone plateau at approximately 400 m a.s.l.. The climate is oceanic with a continental trend (January temperature: 1.2 °C, July temperature: 18.3 °C, annual precipitation: 740 mm). The soil is a brunisol Fig. 1 Map of the experimental plot representing trees of the two species studied (Acer in grey and Fagus in black) over the density and the mixture gradients. Thick dotted lines represent the external borders of a 3 m buffer zone (i.e., radius of the neighborhoods used to compute competition indices), thick plain lines represent the external borders of the central zone, and fine plain lines represent the borders of the 25 plots used to select the 120 trees of sample 3. Average density and average species proportion of the 25 plots are indicated in the top and right margins of the figure

consisting of a silt eutrophic brown soil layered over limestone.

Experimental design

One-year Fagus and Acer saplings grown in nursery were planted on the site in November 1998 following a densitymixing double-clinal design (i.e., an experiment crossing two gradients that vary systematically; Deleuze et al. [1996](#page-14-0); Vanclay [2006\)](#page-14-0). The central zone of the study site $(65 \times 40 \text{ m})$ included 2,014 trees planted according to two perpendicular clines. The first cline was a density gradient, where local tree density varied exponentially with the location on the *x*-axis, ranging from $1,500$ to $25,000$ stem ha^{-1} and the second cline was a mixing gradient where the local proportion of the two species varied linearly with the location on the y-axis, from pure Fagus to pure Acer (Fig. 1). This central zone was surrounded by a 10-m-wide buffer zone with the same tree density and species mixing conditions. In the two zones, all trees were mapped. All other plants (mainly other tree species, Carex sp., Rubus sp. and Cytisus sp.) were removed periodically to avoid any competition other than from planted Fagus and Acer. The site was fenced to prevent browsing damage.

Sampling and tree measurements

The modular structure of crowns allows high structural variability at multiple hierarchical levels. Therefore, we designed a hierarchical sampling scheme for tree

measurements at three levels (stem, annual growth unit and branch) that were assessed within five nested samples (Table [1\)](#page-3-0).

Sample 1 contained all trees from the central zone (2,014 trees) and trees located in the first buffer zone at less than 3 m from the central zone (612 trees). To calculate competition indices for the trees of the central zone, stem height (H_{st} ; Table [2\)](#page-4-0) and diameter at 15 cm (D_{st} ; Table 2) were measured on these trees in 2006. Height of the crown base (i.e., height of the first living branch longer than 10 cm; Hcrown_{st}; Table [2\)](#page-4-0) was measured for every tree in the central zone (sample 2).

We considered trees as branched systems where the main stem is referred to as the first-order axis, the branches inserted on the stem as secondary branches, and so on $(Barthélémy and Caraglio 2007)$ $(Barthélémy and Caraglio 2007)$. A smaller subset including both species was defined to analyze the branching pattern (sample 3, Table [1\)](#page-3-0). To summarize the range of stand conditions being analyzed, the central zone was divided into 25 unequally sized plots with the purpose of having a similar number of trees in each density class (Fig. 1). The x-axis (corresponding to the density gradient) was divided into five classes of decreasing size when the density increased (plot size along the x-axis: 6, 7, 12, 15 and 20 m). The average density for each class was: 2,500, 5,500, 9,000, 16,500 and 21,000 tree.ha⁻¹. The y-axis (corresponding to the mixing gradient) was divided into two small outward classes with an almost ''pure'' composition (95 % of Acer or 95 % of Fagus) and three equally sized inward plots with various mixing conditions (25, 50

Level	Sample	Sample size	Definition	Variable	Unit
Tree level	Sample 1	$2,626$ trees	Stem diameter	D_{st}	mm
			Stem height	$H_{\rm st}$	m
	Sample 2	$2,014$ trees	Local dominant height	Hdom	m
			Local density	Dens	tree ha^{-1}
			Local mixing (proportion of Fagus)	Mix	% of Fagus
			Crown basis height	Hcrown	m
			Maximum crown basis height	$Hcrownmax_{st}$	m
			Reductor	$Hcrown_{st}$ / $Hcrownmax_{st}$	$\overline{}$
Annual GU level	Sample 3	120 trees	Number of second-order branches	Nbr_{GII}	$\overline{}$
			Relative height of the GU $(HGU/Hdom)$	$Hrel_{\text{GU}}$	cm
			Growth unit (GU) age	Age _{GU}	year
			Growth unit height	$H_{\rm GU}$	cm
			Growth unit length	$L_{\rm GU}$	cm
			Growth unit basal diameter	$D_{\rm{GU}}$	mm
			Sum of branch basal area on the GU	S_{GU}	mm ²
			Cross-sectional area at the base of the GU	Shase _{GU}	mm ²
			Cross-sectional area at the end of the GU	$Send_{\text{GH}}$	mm ²
Branch level			Branch insertion height	$H_{\rm br}$	cm
			Branch insertion height on its mother	Hins _{br}	cm
	Sample 4	1,080 second-order branches	Branch order	$Ord_{\rm br}$	no unit
			Branch insertion angle	$A_{\rm br}$	° to horizontality
			Branch diameter	$D_{\rm br}$	mm
			Branch length	$L_{\rm br}$	cm
	Sample 5	360 second-order branches	Branch cross-sectional area	$S_{\rm br}$	mm ²
		bearing 7,648	Branch volume	$V_{\rm br}$	dm ³
		higher order branches	Branch leaf area	$LfA_{\rm br}$	dm ²

Table 1 Sample description, sample size, definition of the variables measured on each sample, abbreviation and measurement units

or 75 % of Fagus and 75, 50 and 25 % of Acer). Each of the 15 inward plots included ca. 130 trees and each of the 10 outward ''pure'' plots ca. 30 trees. In each of the 25 plots, three trees per species were selected (in the ''pure'' plots, only one species was available), with a total of 120 trees (sample 3). In each plot and for each species, one tree was randomly selected from the 10 % smallest diameter trees of the plot, one tree from the 10 % largest trees and one tree from the 80 % intermediate trees. Tree dimension variability in the sample was maximized to account properly for possible size-dependent effects.

Stem and branch measurements were made on each of the 120 trees: the stem was marked every 20 cm from the ground and, at each mark, the average of two diameters measured in orthogonal directions was recorded. The scars left each year by the winter buds on the stem were located and their height along the stem (H_{GU}) was measured. They were used to determine the length (L_{GU}) and age (Age_{GU}) of the successive annual growth units on the stem. The insertion height (H_{br}) and basal diameter (D_{br}) of each living branch inserted on the stem were measured. On Acer and

Fagus, branch diameter does not vary linearly with the insertion height on the stem. Both species show an acrotonic growth pattern within each GU, where branches inserted near the top of the GU are larger (Nicolini et al. [2001](#page-14-0)). To model this pattern and to take into account branch distribution within the GUs, for each GU, the insertion height of each branch within the GU ($Hins_{br}$, Table 1) was computed as a percentage of GU length. Cross-sectional area (Sbase_{GU}, Table 1) at the base of each GU was obtained from stem taper measurements made every 20 cm along the stem, one immediately below the GU base and one immediately above the GU base and from the basal diameter of the branches inserted between these two stem measurements. For each GU, the cross-sectional area at the end of the GU (Send_{GU}, Table 1) was then considered identical to the cross-sectional area at the base of the following GU.

Branch length (L_{br}) and angle (A_{br}) were measured on nine second-order branches on each of the 120 trees of sample 3 (sample 4, 60 trees per species, Table 1). The definition of sample 4 was based on the branching data previously described. Each tree of sample 3 was divided

estimates were considered significant at $\alpha = 0.05$ level

into three equally sized height sections (lower, middle and upper) positioned between the lowest and the highest second-order branch of the tree. In each of the three height sections, three branches were randomly selected by basal diameter criteria, one from the 10 % smallest branches of the height section, one from the 10 % largest branches and one from the 80 % intermediate-sized branches.

Additional measurements on higher order branches were performed for the largest trees, per species and per plot of sample 4 (sample 5, 20 trees per species, Table [1](#page-3-0)). On the nine second-order branches per tree, all branches of higher order were identified (a total of 360 second-order branches and 7,648 higher order branches (up to seventh order) for both species). For each branch higher than second order, we measured insertion height of the branch ($Hins_{br}$) on its mother branch; branch length (L_{br}) ; branch basal diameter (D_{br}) and branch taper (for every 20 cm, the average of two diameters measured in orthogonal directions was recorded). The total volume carried by a branch (V_{br}) was calculated as the sum of the volume of the branch and the volumes of all higher order branches carried by that branch.

In October 2007, we collected leaves on branches of sample 5. Leaves of the second or higher order branches were pooled. All leaves were counted, flattened and scanned and total leaf area was estimated using Image-J (Schneider et al. [2012\)](#page-14-0). On large samples, a representative leaf subsample was scanned and both sample and subsample were weighted. The whole sample leaf area was estimated using its mass ratio to the subsample leaf area. The total leaf area per branch $(LfA_{\rm br})$ was calculated as sum of the leaf area of the axis and the leaf area of all higher order branches carried by the axis.

Data analysis and modeling

To analyze the effects of local inter-tree competition on the various stem and branch parameters, we computed for each individual tree three simple competition indices from measurements performed on all neighboring trees located in a 3 m circular neighborhood around the target tree:

- Local density (Dens), calculated from the total number of trees in the neighborhood;
- Local species proportion (Mix), calculated as the number of Fagus over the total number of trees in the neighborhood;
- Local dominant height (Hdom), calculated as the average height of the five tallest neighboring trees in the neighborhood (if less than five neighboring trees were available, Hdom was calculated over the total number of neighboring trees). At the GU level, the Hdom index was replaced by Hrel_{GU} (H_{GU}/Hdom) to account for the effect of GU location in relation to the upper canopy level.

The three indices had been selected after testing a wide range of competition indices that combined species, height, diameter and distance to target tree. The radius of the circular neighborhood (i.e., 3 m) was selected after testing a range of distances from 50 cm to 10 m (best correlation, results not shown).

For all data sets, we analyzed Fagus and Acer data separately, including the three competition indices within the explanatory variables. Our dataset presented a hierarchical structure with branches nested within GUs, and within trees. Therefore, random effects were explored for those levels (Table [2\)](#page-4-0). For all models, we tested a spatial varying model to take into account local spatial autocorrelation that may arise between neighboring trees (i.e., incorporating spatial linkages of proximity of the observations with a spatial weight matrix), and may result in a wrong estimation of model parameters and in model inaccuracy if not taken into account (Zuur et al. [2009](#page-14-0)). Additionally, for several of the models, we included an exponential variance submodel to account for residual heteroscedasticity. All analyses were conducted in the statistical program R version 2.14.1 (R Development Core Team 2011).

Stem-level variables

We analyzed stem-level variables collected on sample 1 trees using non-linear mixed models. To analyze the relation between height and base diameter (Eq. 1; Table [2](#page-4-0)), we followed Näslund ([1937](#page-14-0)). Hcrown_{st} (height of the crown base) was analyzed using a two-step process (Eqs. 2, 3; Table [2](#page-4-0)). First, we estimated an upper boundary for the relation Hcrown_{st} to H_{st} : we divided tree height into twenty equal-sized classes and we selected the two trees with the highest crown basis in each class. These trees were used to estimate maximum crown basis height (Hcrownmax $_{st}$), following Eq. 2 (Table [2\)](#page-4-0). In a second step, we calculated a reductor of Hcrownmax_{st} for each tree as the ratio of $Hcrown_{st}$ to the corresponding point on the boundary relation. A value of 1 for the reductor indicates that Hcrown_{st} for this tree reached the upper boundary, while a value close to 0 indicates that $Hcrown_{st}$ was close to the ground level (i.e., no self-pruning). We analyzed the relationship between the reductor and the explanatory variables using a non-linear model (Eq. 3, Table [2\)](#page-4-0).

Annual growth unit-level variables

At this level, we tested a random tree effect in the models to take into account possible correlations among GUs within trees. Growth unit basal diameter ($Dbase_{GU}$) and the sum of branch cross-sectional areas per GU (S_{GU}) were described as linear models of their parameters and were modeled only for second-order branches (Eq. 4, 5;

Table [2](#page-4-0)). The number of carried branches (Nbr_{GU}) on an annual growth unit (Eq. 6; Table [2](#page-4-0)) was modeled using a Poisson distribution following Mäkinen and Colin ([1999\)](#page-14-0).

Branch-level variables

At this level, we tested random tree and branch effects in the models to take into account possible correlations between GUs within trees, and among branches within the same second-order branch. As correlation amongst branches from a same cluster was likely, all the models included a single multilevel random effect combining tree identifiers with branch identifiers to take into account correlations among branches from the same tree as well as among $n + 1$ th order branches carried by the same *n*th order branch.

Branch length (L_{br}) was modeled as a linear regression of $D_{\rm br}$ for *Fagus*, and as a combination of a linear model and a negative exponential model (to account for small branches) for Acer (Eq. 8; Table [2](#page-4-0)). Branch insertion angle (A_{br}) was modeled as a linear regression of branch insertion height (Hins_{GU}) and D_{br} (Eq. 9, Table [2\)](#page-4-0). Branch volume (V_{br}) was a non-linear model adapted from Muukkonen [\(2007\)](#page-14-0), which describes branch volume as a power function of branch basal diameter (Eq. 10, Table [2](#page-4-0)). Branch leaf area (Lf A_{br}) was described as a non-linear model of branch cross-sectional area $(S_{\rm br})$ and branch order (Ord_{br}; Eq. 11; Table [2\)](#page-4-0).

Results

Stem-level variables

The shape of the $H_{\rm st} - D_{\rm st}$ (stem height – stem diameter) relationship did not differ between Acer and Fagus (Fig. [2](#page-7-0)). The $H_{\rm st} - D_{\rm st}$ relationship reached an asymptote at approximately 4 m at the lowest densities, and at 5.5 and 5 m at the highest densities for Acer and Fagus, respectively (representing an increase of 27 and 20 %, respectively; Fig. [3](#page-8-0); Table [2;](#page-4-0) Eq. 1). Density (Dens) and the proportion of Fagus in the local neighborhood (Mix) affected the slope and the asymptote of the $H_{st} - D_{st}$ allometry. For a given D_{st} value, high density caused considerably larger H_{st} values and the magnitude of this effect increased for larger trees. Both Acer and Fagus saplings tended to be taller with a highest proportion of *Fagus* as neighbors. For both species, the species proportion effect was of a smaller magnitude than the density effect (asymptote varied between 4.5 at the lowest percentage of Fagus proportion for both species, and 4.75 and 5 m for Fagus and Acer at the highest percentage of Fagus proportion, respectively; representing an increase of 5 and 10 %). The effect of Hdom (local dominant height) on H_{st} was significant and positive for both species.

Fig. 2 Fitted allometries for H_{st} (stem height) against D_{st} (stem diameter) in Acer and Fagus (Eq. 1; Table [2](#page-4-0); Sample number 1; Table [1\)](#page-3-0). The density indicated for observed individual tree values is the average density for the five classes in which the density gradient was divided. We also show the simulated densitydependent effects on the regression lines fixed at three levels of density (500, 12,000, 25,000), while keeping species proportions at its mean (0.5)

The upper boundary line of Hcrownmax_{st} (maximum crown basis height) against H_{st} was well described by a positive linear function for both species, with a lower slope for *Fagus* (0.[3](#page-8-0)9) than for *Acer* (0.46) (Fig. 3a; Table [2](#page-4-0); Eq. 2). For both species, the reductor could be modeled as a negative exponential function of D_{st} , meaning that for a given height, trees with a larger diameter had their crown base lower on the stem (Fig. [3b](#page-8-0); Table [2;](#page-4-0) Eq. 3). For both species, the relationship was a function of density. For a given H_{st} and D_{st} , trees growing at higher density showed a Hcrown_{st} closer to the maximum value (i.e., smaller crown length and higher reductor). In addition, Fagus showed a lower crown base (i.e., larger crown length and smaller reductor) when Fagus proportion decreased, while Acer had a lower crown base height when the proportion of Fagus around it increased. Crown base height was on average almost half for Fagus (2.86 cm) than for Acer (5.57 cm) and the difference between species increased when the proportion of Fagus decreased in the local neighborhood.

Annual growth unit-level variables

Most relationships at the annual growth unit-level (GU) were not directly affected by competition indices. For both species, $Dbase_{GU}$ (GU basal diameter) could be fit as a positive linear relationship of D_{st} combined with a negative interaction between $H_{\text{GU}}/H_{\text{st}}$ and D_{st} (Fig. [7,](#page-12-0) Table [2;](#page-4-0) Eq. 4; H_{GU}/H_{st} was not statistically significant). For both species, none of the three competition indices affected $Dbase_{\text{GU}}$.

 S_{GU} (sum of branch cross-sectional areas per GU) was a linear function of the difference between $Sbase_{\text{GH}}$ and $Send_{GU}$ (cross-sectional area at the base and end of the GU, respectively; Fig. [8;](#page-12-0) Table [2](#page-4-0); Eq. 5). The relationship was unaffected by Age_{GU} (GU age) or by competition indices in *Fagus*, but was affected by Age_{GU} and by Hrel_{GU} (GU height relative to the canopy level) in *Acer*. For a given difference between $Sbase_{GU}$ and $Send_{GU}$, Fagus exhibited a wider individual variability of S_{GU} than Acer, as shown by the adjusted R^2 of their respective model, resulting in lower correlation quality.

 Nbr_{GU} (number of branches per GU) varied as a linear function of GU length for both Acer and Fagus (Fig. [4](#page-9-0); Table [2](#page-4-0); Eq. 6). The slope of the relationship was affected by Age_{GU} and by Dens for both species: at a given GU length, older GUs or GUs from trees growing in high density plots carried fewer branches. The effect of Dens was less visible in younger GUs. The equations were insensitive to Mix and Hdom. The relationship showed an overall similar shape for both species but Fagus exhibited a density) in Acer and Fagus. The density indicated for individual tree values is the average density for the five classes in which the density gradient was divided. a Upper boundary line between $Hcrownmax_{st}$ (maximum crown basis height) and H_{st} (stem height); the *black* dots represent the two trees with the highest crown basis in each of the twenty equally sized classes in which tree heights were divided; the grey dots represent the rest of the trees (Eq. 2; Table [2](#page-4-0); Sample 2; Table [1](#page-3-0)) b Relationship between the reductor and D_{st} (stem diameter) (Eq. 3; Table [2](#page-4-0); Sample 2; Table [1](#page-3-0)). A value of 1 for the reductor indicates that the crown height for this tree reached the upper boundary, while a value close to 0 indicates that the height crown was close to the ground level

higher individual variation in Nbr_{GU} at a given GU length with Dens at a given age.

For second-order branches, D_{br} showed a clear acrotonic pattern (i.e., a pattern at the GU level) for Acer and for

Fagus (Table [2;](#page-4-0) Eq. 7). For both species, $D_{\rm br}$ increased as a cubic function of $Hins_{br}$ (branch insertion height). The slope of the relationship decreased for young branches, their acrotony being weaker. Additionally, for both species,

Fig. 4 Change in Nbr_{GU} (number of branches on the GU) with L_{GU} (GU length). The density indicated for individual tree values is the average density for the five classes in which the density gradient was divided. We also show (a) the simulated density effects on the regression lines for Acer; and **b** the simulated Age_{GU} (the age of GU on the stem) effects on the regression lines for Fagus (Eq. 6; Table [2](#page-4-0); Sample 3; Table [1](#page-3-0))

 D_{br} also depended linearly on Dbase_{GU} as larger GUs carried larger branches. Relationships for both species were unaffected by competition indices. In Fagus, there was a great dispersion of values for large branches resulting in an inferior model quality (Eq. 7; Table [2](#page-4-0)).

Branch-level variables

All relationships at the branch level were not directly affected by competition indices for both species. Several branch traits could be described at any branch order using D_{br} . Fagus showed a higher variation in L_{br} (branch length) and V_{br} (branch volume) for a given D_{br} than Acer (Figs. [9,](#page-13-0) [10](#page-13-0); Eqs. 8, 10; Table [2](#page-4-0)). For a given D_{br} , Acer showed on average longer branches than Fagus (Table [2;](#page-4-0) Eq. 8). This relation was independent of $Ord_{\rm br}$ (branch order). Branch angle (A_{br}) decreased with D_{br} and increased with $Hins_{br}$ (Table [2](#page-4-0); Eq. 9). For both species, V_{br} was expressed as a cubic function of D_{br} (Fig. [10](#page-13-0); Table [2](#page-4-0); Eq. 10). Acer exhibited a slightly steeper slope than Fagus with greater $V_{\rm br}$ for larger branches. Data variability increased for larger branches (Fig. [10](#page-13-0)) and could not be linked to any measured parameters.

For both species, LfAbr (branch leaf area) was expressed as a power function of S_{br} (branch cross-sectional area) with power coefficients slightly above 1 (Fig. [5;](#page-10-0) Table [2;](#page-4-0) Eq. 11). For a given cross-sectional area, Fagus showed a higher leaf area than Acer and a higher variability reflected by the larger data dispersion around the modeled line and the worse goodness of fit. LfA_{br} was significantly correlated to Ord_{br}, with higher branches (where the amount of light is smaller) having a smaller LfA_{br}

Discussion

In our study of an 8-year-old experimental plantation of Fagus and Acer, we found strong evidence for variation in crown structure in response to density and species identity of the local neighborhood. The variation occurred at alternative crown levels for the two species. This highlights the complexity of species interactions and the need for detailed information on crown development to better understanding species coexistence in mixed broadleaved stands.

Effects of size, density and species identity of neighbors

Even though our study was restricted to a juvenile stage, we observed that for most of the crown traits measured,

Fig. 5 Change in LfA_{br} (total leaf area) as a function of S_{br} (branch cross-sectional area) for first-order branches ($Ord_{\text{br}} = 1$) (Eq. 11; Table [2](#page-4-0); Sample 5; Table [1\)](#page-3-0)

Fig. 6 Scheme of the scaling relationships among the variables measured for both species at the stem, GU, and branch levels, as affected by the competition indices: density (Dens), mixing (Mix) and dominant height (Hdom). An arrow connecting two variables indicates a significant relationship between both variables for both species (Table [2](#page-4-0)) If the effect is significant for only one species, the arrow connecting two variables is dotted

larger trees exhibited greater variability than smaller trees, as shown by previous results (Mäkelä and Vanninen [1998](#page-14-0); Ilomäki et al. 2003). It is likely that the response of crowns to the local neighborhood will vary with stand development, although crowns of older Fagus trees have also demonstrated high plasticity in response to changes in the local canopy conditions (Schröter et al. [2012](#page-14-0); Dieler and Pretzsch [2013\)](#page-14-0) suggesting that the response to competition could be sustained over tree life.

Tree density significantly affected crown architecture as reported previously (Lang et al. [2012](#page-14-0)), whereas neighbor species identity had a significant but less pronounced role despite the large range in species proportions examined. This lends support to the findings of Kaitaniemi and Lintunen ([2010\)](#page-14-0), who found that the effect of density (in a more limited range than in our study) and neighbor size (calculated as a competition index) alone were more important than the effect of neighbor identity when exploring the effect of Larix sibirica Ledeb. and Pinus sylvestris L. on Betula pendula Roth. Overall, our results are consistent with previous findings, where information on the amount, size and species of neighboring trees was necessary to adequately describe tree crown architecture and branching arrangement (Sumida et al. [2002;](#page-14-0) Kaitaniemi and Lintunen [2008;](#page-14-0) Lintunen and Kaitaniemi [2010](#page-14-0)).

Models at the stem level were generally improved directly by the competition indices accounting for density (Dens) and

species proportion (Mix). However, at the GU and branch levels, most crown variables were not directly affected by competition, and could be mostly predicted through allometry, once the effect on some key covariates was accounted for. Most of the influence of the variations in density, neighbor identity and neighbor size were accounted for by the stem-level variables for both species and, for branch-level variables, secondarily by GU-level variables. One exception was branch number, which was affected by density and not by species identity as reported by Kaitaniemi and Lintunen [\(2010\)](#page-14-0). In general, we found that allometry between crown attributes was less variable than the differences in allometry between stem diameter and crown attributes, which is in agreement with the findings on tree allometry in Scots pine by Mäkelä and Vanninen ([1998](#page-14-0)). Similarly, several studies found that stem and crown properties were sufficient to predict reliable branch properties under contrasted competitive local environments (Hein et al. [2007](#page-14-0); Weiskittel et al. [2007;](#page-14-0) Weiskittel et al. [2010;](#page-14-0) Antin et al. [2013\)](#page-13-0).

Acer and Fagus respond to neighborhood competition at alternative crown levels

Despite common shapes in the relationships among all the variables measured at the three levels considered (i.e., stem, annual growth unit, and branch) for Acer and Fagus, the two species reacted differently to variation in their local neighborhoods. Crown attributes were modified at different levels for the two species. Species-specific effects of neighbor competition on height–diameter relationships and crown allometries were expected from previous neighborhood analysis (Coates et al. [2009;](#page-13-0) Harja et al. [2012\)](#page-14-0). Acer displayed higher intraspecific plasticity of crown length to changes in density, but both Acer and Fagus showed a similar plasticity of crown length to the neighboring species proportion. In our study, changes in the light environment are mostly a result of changes in density (results not shown). Given this, our results agree with the findings of (Petritan et al. [2009\)](#page-14-0) in an observational study of juvenile trees under varying light conditions beneath a shelterwood canopy in a mixed deciduous stand, where *Acer* showed a greater plasticity in crown shape than Fagus. In our experiment, the latter displayed a higher level of individual variability on branch development (i.e., branch diameter vs. volume, Fig. [10](#page-13-0); difference of branch crosssectional area at start and end vs. sum of branch cross-sectional area, Fig. [8](#page-12-0)) and on leaf area variation (Fig. [5](#page-10-0)) in response to changes in density and species proportion in its neighborhood. Although both species are defined as having similar resource use strategies (Collet et al. [2014\)](#page-13-0), the low degree of modification of the crown length with increasing shade in Fagus, together with the high degree of leaf area variability, indicates a greater ability of Fagus to maintain the height they acquired in periods of high light availability

(Collet et al. [2011](#page-13-0)), and to keep branches alive under shaded conditions, thus resisting to very low light environments.

Implications for predicting stand development in mixed-species forests

Our results suggest that responses of crown morphology should be inferred from a hierarchical model including variables at distinct scales (Fig. [6](#page-10-0)) rather than modular units that are autonomous with respect to their responses to local conditions (Kawamura [2010\)](#page-14-0). This could provide a more mechanistic understanding of how different strategies of crown development contribute to species coexistence in mixed stands. Our models provide a steady-state calculation, and as such they are not able to characterize temporal dynamics, including the growth of the studied crown attributes. However, the static relationships among attributes provide a useful foundation for the dynamic analysis, by identifying the key attributes on which to focus, and by simplifying the relationships to study. Our static approach can also contribute to the understanding of the various development constraints (biomechanical, physiological, etc.) that eventually shape crown morphology (Fournier et al. [2013\)](#page-14-0). Moreover, this approach provides the basis for a procedure to reconstruct crown geometry from a set of attributes that are relatively easy to measure in the stands, and that can afterwards be used as an input to growth models or light interception models (Lintunen et al. [2011\)](#page-14-0). Using the relationships we established, we could simulate vertical leaf distribution within a mixed stand to test hypotheses, such as if potential complementarity in the leaf area display between the two species could explain the higher productivity found in the mixing where the proportion of both Fagus and Acer in the stand is 50 % (Collet et al. [2014](#page-13-0)).

In mixed deciduous forests of temperate regions, shade tolerance is a trait that has been commonly reported to explain differences in crown plasticity (Ameztegui and Coll [2011\)](#page-13-0). Our results indicate that in mixed-species stands formed by functionally equivalent species, with similar shade tolerance and similar total tree height trends, species coexistence may be partly explained by differences in species architecture, such as previously identified for co-occurring broadleaved species of the genera Fagus, Tilia, Acer, Fraxinus and Carpinus (Frech et al. [2003](#page-14-0)). Furthermore, our results are in line with other experiences of shade-intolerant species in mountain forests (Parish et al. [2008;](#page-14-0) Vieilledent et al. [2010\)](#page-14-0), highlighting the importance of intraspecific differences in individual variability as a potential mechanism for the longterm persistence of mixed deciduous broadleaved forests.

Author contributions F.N. and C.C. designed the sampling scheme and the measurement protocol. I.B and C.C. wrote code, ran the models, and analyzed output data. I.B, C.C. and F.N. wrote the manuscript.

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Fig. 7 Relationship between D_{br} (branch basal diameter) and Age $_{\text{GU}}$ (age of the growth unit) for both species as a function of $D_{\rm st}$ (stem diameter) (Eq. 7; Table [2](#page-4-0); Sample 4; Table [1\)](#page-3-0)

Appendices

of interest.

See Figs. 7, 8, [9](#page-13-0), [10](#page-13-0).

Fig. 8 Relationship between S_{brGU} (the sum of crosssectional areas at the base of each GU) and the crosssectional areas at GU base (Sbase_{GU}) and GU distal end (Send_{GU}) for both species (Eq. 5; Table [2](#page-4-0); Sample 3; Table [1](#page-3-0)). Note that a single trendline is shown for both species because they are almost identical

 D_{br} (branch basal diameter) and L_{br} (branch length) for both species (Eq. 8; Table [2](#page-4-0); Sample 4; Table [1\)](#page-3-0)

Fig. 10 Relationship between D_{br} (branch basal diameter) and V_{br} (branch volume) for both species (Eq. 10; Table [2](#page-4-0); Sample 5; Table [1](#page-3-0))

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