RESEARCH ARTICLE

Transverse gust generation in a wind tunnel: a suction‑driven approach

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Abstract

The Andrew Fejer Unsteady Wind Tunnel was modifed to add a suction duct on top of the test section to generate a vertical velocity component (cross fow). The suction produced on the top was distributed by the individually controlled louvers at the inlet of the suction duct so that the velocity components in the test section vary both temporally and spatially. Steady and traveling-wave transverse fows were generated in the test section. We present theoretical models for the unsteady fow feld generated by this confguration and validate these models with experimental measurements. The results indicated that the transverse gusts generated in the test section were essentially irrotational, and a potential fow model makes relatively accurate predictions of the fow feld. The suction-driven approach greatly reduced the turbulence level in the fow feld relative to jet-driven cross fow approaches, and demonstrated high levels of repeatability. Traveling waves in 1 − cos form were generated and showed evident infuence on the fow angle of attack.

Graphical abstract

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1 Introduction

Studying the unsteady aerodynamics of wings interacting with various types of gusts is motivated by a desire for performance and reliability improvements across applications such as high-performance aircraft, unmanned aerial systems,

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micro aerial vehicles, helicopters, and high-efficiency wind turbines. In particular, an understanding of the underlying flow physics is crucial for aerodynamic applications including lift enhancement, active fow control, gust alleviation, or control-embedded design optimization.

A starting point for such investigations which still receives considerable contemporary attention is the study of a nominally two-dimensional airfoil encountering unsteady effects, caused by airfoil motion and/or a time-varying freestream velocity. Classical unsteady aerodynamic theories, based on potential flow, trace back to the early 20th century, such as Theodorsen's theory for airfoils undertaking periodic motions (Theodorsen [1935](#page-16-0)), and Wagner's indicial response function (Wagner [1925](#page-16-1); Walker [1931](#page-16-2)). In a similar vane, Küssner's function (Küssner [1936\)](#page-16-3) gives the response of a thin airfoil to a sharp-edged transverse gust, while Sears ([1941](#page-16-4)) and Greenberg ([1947](#page-15-0)) describe harmonic gusts in the transverse and streamwise direction, respectively. More recently, as reviewed in Jones [\(2020](#page-15-1)) and Jones and Cetiner [\(2021\)](#page-16-5), transverse (Corkery et al. [2018;](#page-15-2) Chowdhury et al. [2019](#page-15-3); Sedky et al. [2020\)](#page-16-6), vortical (Medina et al. [2018](#page-16-7); Eldredge and Jones [2019;](#page-15-4) Rockwood and Medina [2020](#page-16-8); Le Provost and Eldredge [2021\)](#page-16-9), and streamwise (Dunne and McKeon [2015;](#page-15-5) Leung et al. [2018](#page-16-10); He and Williams [2020c,](#page-15-6) [2020](#page-15-7)) gusts have received attention through both computational and experimental investigations. On the experimental side, Greenblatt ([2016\)](#page-15-8) reviewed earlier and more recent gust/unsteady fow generation approaches that are used in low-speed unsteady wind tunnels. Louver mechanisms at the upstream/downstream end of the test section are widely used in simulating large-scale turbulence (Makita [1991](#page-16-11)), surg-ing flows (Farnsworth et al. [2020](#page-15-9)), and periodic oscillating flows (Wei et al. [2019\)](#page-16-12). Meanwhile, active grids are utilized to produce atmospheric turbulence that has smaller length scales (Roadman and Mohseni [2009;](#page-16-13) Sytsma and Ukeiley [2011](#page-16-14); Knebel et al. [2011](#page-16-15)).

For cross-fow/transverse gusts, while some of the twodimensional velocity profles can be simulated by forced motions of the test objects, e.g., pitching (He and Williams [2020b](#page-15-10)) and/or plunging motions (Perrotta and Jones [2018](#page-16-16)), perturbations in the fows enable richer characterization of such unsteady flows, and closer-to-real conditions to be generated in the test facilities. In particular, direct jet and towing (Corkery et al. [2018](#page-15-2); Biler et al. [2021\)](#page-15-11), jet-vortex-generator arrays (Olson et al. [2021\)](#page-16-17), and perturbations on the wall (Fernandez et al. [2021](#page-15-12)) are some of the recent advances in efforts to generate transverse or cross-flow gusts in wind/ water tunnels. However, the realization of traveling cross flows is still less seen in previous studies, nor is there a trivial solution to create controlled velocity gradients in selected directions (He and Williams [2020c](#page-15-6); Gloutak et al. [2022\)](#page-15-13).

In this paper, we present a suction-driven approach to produce controlled, transverse gusts as traveling waves in the Andrew Fejer Unsteady Wind Tunnel (AFUWT) at the Illinois Institute of Technology. The AFUWT is a closedcircuit wind tunnel with unsteady fow capability that is controlled by louver mechanisms. It was one of the earliest university wind tunnels to produce unsteady fuctuations in the freestream (Miller and Fejer [1964\)](#page-16-18). Rennie et al. ([2019\)](#page-16-19) developed a low-dimensional model through the method of characteristics for the wind tunnel to produce longitudinal (streamwise) von Kármán spectrum gusts with open-loop control of the louvers. Further, He and Williams ([2020\)](#page-15-7) improved the wind tunnel's capability and performance of controlling streamwise fuctuations in selected frequency ranges, replicating the von Kármán and Dryden spectra in the gusts with diferent length scales and intensities, by introducing a spectral feedback loop to establish closedloop control for the wind tunnel. Recent modifcations to the AFUWT installed a suction duct on the top of the test section so the fow had a bypass passage, which will be shown in Sect. [2.1.](#page-2-0) The suction efect that was generated by the bypass created a secondary (vertical) velocity component for the test-section fow. In the meantime, an additional set of louver mechanisms that had similar configurations with what was used in Pfeifer and King [\(2018\)](#page-16-20) was instrumented in the suction duct, where the louvers were controlled individually to distribute the suction in the streamwise direction. Thus, the unsteady test capability of the AFUWT was extended to temporal and spatial (two-dimensional) cross-fow perturbations, in addition to the streamwise disturbances.

In addition to the wind tunnel engineering and experiments, we developed theoretical models relevant to these cross-fow capabilities, including a lumped element model for the flow rates (described in Sect. [2.3](#page-3-0)) and potential flow solutions for the fow feld (Sect. [2.4\)](#page-5-0). These theoretical models can provide preliminary guidelines for experimental settings, such as the fow rate allocation between the test section and the suction duct, the spatial suction distributions on the top of the test section, and predictions of the fowfeld within the test section in the presence of traveling wave gusts. Furthermore, these models allow us to analyze the suction-driven confguration more generally, which could enable further refnements to the design process for future unsteady wind tunnel upgrades.

Experimental results characterizing the modifed AFUWT are shown in Sect. [3](#page-7-0). The flow measurements and visualizations demonstrate that the suction-driven approach is able to generate both steady and traveling transverse fows. While we were able to create velocity gradients $\left(\frac{du}{dx}\right)$ and $\frac{dv}{dx}$ in the test section, the velocity profles, the waveforms, and the spectra of the gusts were not fnely adjusted, since those were beyond the scope of this paper. Both the amplitudes and wavelengths that were used in the early-stage traveling wave tests resulted in large scale gusts, where the gust ratio (the ratio of the magnitude of the transverse velocity

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component to the mean streamwise flow speed) was $\mathcal{O}(0.1)$ and the ratio of the wavelength to the test-section length was $\mathcal{O}(1)$. A recent study in an active-grid-controlled wind tunnel with a slightly larger test section $(0.8 \text{ m} \times 1.0 \text{ m} \times 2.6 \text{ m})$ (Wester et al. [2022\)](#page-16-21) also reported gust ratios on the same order of magnitude, with a transverse velocity component ranging between 0.03 and 0.1 of the mean streamwise fow speed.

The main objective of this paper is to demonstrate the feasibility of the suction-driven transverse gusts in the wind tunnel. Subsequently, the influence of the travelingwave gusts on velocity profile and flow angle of attack was documented.

2 Wind tunnel modifcation and theoretical models

2.1 Modifcation of the Andrew Fejer Unsteady Wind Tunnel

The original AFUWT incorporated a set of 4 louvers at the downstream end of the test section to enable control of the freestream fow speed, and generate longitudinal velocity fuctuations with desired velocity profles or gust spectra (details are described in Rennie et al. [2019](#page-16-19) and He and Williams [2020](#page-15-7)). The latest upgrade of the wind tunnel includes the construction of a suction duct onto the top of the test section. The difuser and the main fan were modifed or exchanged to meet the new working requirement, including the structure of the difuser, fow rate capacity of the fan, as well as fan blade pitch function which allows the blade pitch angle to be adjusted to adapt to low or high flow speed conditions.

Figure [1](#page-2-1) shows a schematic diagram of the modifed sections of the AFUWT. The features relevant to the main fow passing through the test section were retained from the previous confguration, including the downstream louvers, and the breather (which was always *closed* in the experiments presented in this paper) to the difuser. The breather is located in between the downstream louvers and the difuser, which is also the exit of the test section. We use downstream louvers to refer to the test section exit in the rest of this paper since they are most responsible for determining the streamwise fow rate. The ceiling of the test section was replaced by a sealed duct that covers the entire top of the test section with 10 sub-channels at the inlet, angled at 45° to the horizontal. Each channel consists of a louver mechanism, which through its rotation is able to change the blockage of the channel from completely blocked to fully open (these louvers are referred to as top louvers in the rest of this paper). The suction duct returns to the difuser through a straight channel and a curved exhaust. By sharing a pressure drop that was generated by the main fan, the duct created a certain amount of suction from the top of the test section, hence a vertical velocity component (cross flow) is generated in the test section in addition to the streamwise fow, the principles of which are discussed in Sect. [2.2](#page-3-1). The flow that diverge between the test section and suction duct merge in the difuser and return to the fan to complete the wind tunnel circuit.

The detailed confguration of the test section and the suction duct is shown in Fig. [2](#page-2-2). The test section had a length of $L_{TS} = 2.1 \text{ m}$ and cross-section dimensions of 0.61 m \times 0.61m. The coordinates are defined such that the *x*−axis is in the streamwise (horizontal) direction and the *y*− axis is in the vertical direction orientated at the bottom left

(a) Test section with suction duct

(b) Test section schematic diagram

Fig. 2 Test section details

Fig. 1 Modifed sections of the Andrew Fejer Unsteady Wind Tunnel

corner of the test section. The distances in *x*− and *y*− directions are normalized by test-section length L_{TS} and height H_{TS} respectively. A layer of honeycomb is placed in between the test section and the inlet of the suction duct to reduce the turbulent disturbances from the suction. Each top louver is individually driven by a Nanotec® PD4-C6018L4204- E-01 servo motor, which allows for independent control of the blockage area in each sub-channel. As a louver rotates from 0° (parallel to sub-channel walls) to 90 $^{\circ}$ (perpendicular to sub-channel walls), the blockage ratio in its sub-channel varies from 0 to 1. The motors are controlled through a dSPACE® DS1104 control box with a sampling rate of $F_s = 1000$ samples/s. Despite the potential coupling between the test section and the suction duct (as they share the same pressure source), the downstream louvers mainly control the mean flow u_0 and the longitudinal velocity fluctuation *u*′ , while the top louvers mainly enable temporal and spatial variance of the vertical velocity fuctuation *v*′ . In the results presented in this paper, the velocity quantities are normalized by the mean flow speed u_0 such that $u^* = u/u_0$ and $v^* = v/u_0$, the *z*−vorticity is normalized by the testsection length and mean flow speed where $\omega_z^* = \omega_z L_{\text{TS}}/u_0$, and time is scaled based on the convective time $t_c = L_{TS}/u_0$.

The velocity components in the test section were measured by a Dantec Dynamics® MiniCTA 54T42 *x*-wire anemometer as well as an Aeroprobe® Air Data Probe (5 holes). Time-resolved particle image velocimetry (PIV) was performed to visualize the fow felds at the center part of the test section. The PIV vector grid is 160×136 on a 504 mm \times 427 mm domain, thus, the spatial resolution is 3.15 mm $(0.0015L_{TS})$. The velocity vector fields are processed by the LaVision DaVis software with a 32 pixels by 32 pixels interrogation window with a 50% overlap. The data acquisition and louver control utilized a dSPACE® Micro-LabBox® system. The dSPACE system was operated at a sampling frequency of $F_s = 1000$ samples/s and the timeresolved PIV data were acquired at a rate of 100 image pairs per second. A low-pass filter at a cut-off frequency of 20 Hz was applied to the measured data.

2.2 Cross flow generation

The vertical velocity fluctuation v' in the test section is created by the suction from the suction duct. As the main fan runs, it creates a pressure drop Δ*p* between the inlet of the test section and the difuser. This pressure drop moves the air in the tunnel from the test-section inlet to the difuser exhaust. When the breather is closed, the flow rate Q_{in} at the inlet of the test section equals the flow rate Q_{out} where the two branches of fows merge in the difuser. Since the suction duct constructs a parallel flow path to the test section, the total flow rate Q_{in} is shared by the test section (Q_{TS}) and the suction duct (Q_{SD}), where $Q_{in} = Q_{TS} + Q_{SD}$ (see Fig. [2](#page-2-2)b) for parameter locations). While the drop in the test-section fow rate slows the fow speed in the longitudinal direction, the suction generated by the fow that goes into the suction duct drives the fow to move vertically in the test section, in addition to the horizontal movement. As a result, the crossfow feature of the wind tunnel is achieved by creating a vertical velocity component to the fow velocity. Note that the vertical velocity fuctuation is one-sided, since the suction on the top can only create positive velocity in the *y*− direction.

The major factor that affects the values of Q_{TS} and Q_{SD} is the fluid resistance of the test section R_{TS} and the suction duct R_{SD} , as well as the variable fluid resistance of the downstream louvers R_{LT} and the top louvers R_{LS} . Once the resistance is determined, the fow rates in these two sections are fxed in principle. On the other hand, downstream louvers and top louvers enables us to change the ratio of the resistance $\frac{R_{\text{TS}}+R_{\text{LT}}}{R_{\text{F}}+R}$ $rac{R_{\rm SB} + R_{\rm LR}}{R_{\rm SD} + R_{\rm LS}}$ by changing the blockage areas. As the resistance ratio changes, Q_{TS} and Q_{SD} change accordingly and can be controlled in designated manners within the system limits. Consequently, the *u* and *v* velocity components in the test section are controlled.

Since each louver is independently driven by a servo motor, this allows for individual control of the louver blockage. For example, the top louvers can rotate nonuniformly as a function of the *x*-coordinate. In other words, the suction/ fow rate can be spatially distributed along the suction-duct inlet (the top of the test section) in the streamwise direction as $\tilde{Q}_{SD}|_{H_{TS}}(t, x)$, where $\int_0^{L_{TS}} \tilde{Q}_{SD}|_{y=H_{TS}} dx = Q_{SD}$. The distributed fow rate leads to a nonuniform suction for the fow in the test section from the top; therefore, the vertical velocity fuctuation in the test section *v*′ varies as a function of both *t* and *x*. If we enforce a traveling-wave function to the louver motions (flow rate distribution), the propagated cross-flow fluctuation can be written in the form of $v'(g(x - c_w t))$, in which *g* is the waveform and c_w is the wave speed. Further, when a sinusoidal waveform is applied, the one-sided *v*′ is expressed as

$$
v' = \frac{1}{2} v_{\text{max}} \left[1 - \cos \left(\frac{2\pi f_{\text{w}}}{c_{\text{w}}} x - 2\pi f_{\text{w}} t \right) \right],\tag{1}
$$

where f_w is the wave frequency. Letting $c_w = u_0$, the crossflow becomes a sinusoidal traveling wave.

2.3 Flow rate characterization through lumped element method

The method of characteristics that was used in Rennie et al. [\(2019\)](#page-16-19) can continue to be applied for the modifed AFUWT to give a preliminary approximation of the fow rates in the test section and the suction duct. Through a lumped element model, the influence of the fluid resistance and the flow

Fig. 3 Lumped element model for the test section and the suction duct

inertia in the two branches, the test section and the suction duct, are taken into account to obtain estimates of the overall flow rate distributions in these two branches when a determined total fow rate is given at a fxed fan speed.

The test section and the suction duct are modeled as a parallel circuit as shown in Fig. [3.](#page-4-0) The basic assumption is the same as mentioned in Sect. [2.2;](#page-3-1) namely, the pressure drop Δp is determined by the fan speed only and does not change with the resistance. This allows for setting an artifcial Q_{in} without knowing the exact Δp value. For instance, a typical test-section inlet flow speed $V_{\text{in}} = 6 \text{ m/s}$ gives $Q_{\text{in}} = 2.23 \text{ m}^3/\text{s}$. A simplification of the wind tunnel confguration also applies here that the inlets and the exhausts of the test section and the suction duct are considered to be merged, respectively, so that the two sections start at the same location and intersect with each other at their ends. Use of the lumped element circuit in Fig. [3](#page-4-0) to represent the wind tunnel branches automatically assumes a linear fuid resistance in the model. While the realistic resistance may not be fully linear due to suction-duct geometry, flow speed variations, louver rotations, etc., these infuences are minimal in steady-state cases. Therefore, we keep this assumption for steady-state fow rate estimations.

With the given assumptions and the simplifications, Kirchhof's current law (continuity) gives

$$
0 = Q_{\rm in} - Q_{\rm TS} - Q_{\rm SD}.\tag{2}
$$

And Kirchhof's voltage law (momentum equation) gives

$$
0 = (R_{TS} + R_{LT})Q_{TS} + I_{TS}\frac{dQ_{TS}}{dt}
$$

$$
- (R_{SD} + R_{LS})Q_{SD} - I_{SD}\frac{dQ_{SD}}{dt},
$$
 (3)

in which $I_{TS} = \rho L_{TS}/A_{TS}$ and $I_{SD} = \rho L_{SD}/A_{SD}$ are the flow inertia (appears as the fow inertance) terms. The fow inertance of the suction duct is approximated by dividing the suction duct into the upward suction part (taking flow from the test section) and the horizontally fowing part (returning to the diffuser). The flow resistance $R_{\text{TS}} + R_{\text{LT}}$ (flow resistance of the test section and the downstream louvers) and $R_{SD} + R_{LS}$ (flow resistance of the suction duct and the top louvers) in Eq. [3](#page-4-1) are estimated based on the measurements from Feroz (2017) (2017) and Rennie et al. (2019) (2019) , where R_{SD} takes the corners into account. Combining Eqs. [2](#page-4-2) and [3](#page-4-1) while letting $R_1 = R_{TS} + R_{LT}$ and $R_2 = R_{SD} + R_{LS}$, we write

$$
\frac{dQ_{TS}}{dt} + \frac{R_1 + R_2}{I_{TS} + I_{SD}} Q_{TS} = \frac{R_2}{I_{TS} + I_{SD}} Q_{in}.
$$
\n(4)

Solving for Q_{TS} in Eq. [4](#page-4-3), we obtain the volume flow rates in the test section

$$
Q_{TS}(t) = \left[Q_{TS}(t_0) - \frac{R_2}{R_1 + R_2}Q_{in}\right] \exp\left(-\frac{R_1 + R_2}{I_{TS} + I_{SD}}t\right) + \frac{R_2}{R_1 + R_2}Q_{in},
$$
\n(5)

thus, in the suction duct

$$
Q_{SD}(t) = Q_{in} - Q_{TS}(t),
$$
\n(6)

where we define the initial condition as $Q_{TS}(t_0) = Q_{in}$, which also simulates step opening of the top louvers.

The ODE solutions for Q_{TS} and Q_{SD} from Eqs. [5](#page-4-4) and [6](#page-4-5) refect the fact that the steady-state fow rates are afected by the resistance ratio only, and we can change the weights of the fow rates by varying the resistance of the louvers.

An example result where $V_{in} = 6 \text{ m/s}$ (thus, $Q_{\text{in}} = 2.23 \text{ m}^3/\text{s}$ and the top louvers are fully opened while the downstream louvers are half opened is shown in Fig. [4.](#page-4-6) When the flow reaches steady state, the flow rates are $Q_{\text{TS}} = 1.50 \,\text{m}^3/\text{s}$ and $Q_{\text{SD}} = 0.73 \,\text{m}^3/\text{s}$. If we use the cross-section area of the test section and the inlet area of the suction duct to calculate the magnitudes of the horizontal

Fig. 4 Lumped element model estimation of the transient response of test-section velocity components

and vertical velocity components, respectively, we have $u_0 = 0.67V_{\text{in}}$ and $v_0 = 0.10V_{\text{in}}$. The lumped element calculation of the velocity components assumes a uniform velocity profle in the *y*−direction, which is not physically realistic. However, the model is still valuable since it gives preliminary predictions of the key parameters to be expected from the suction-driven architecture and these parameters can guide the adjustment of the potential flow model to enable quantitatively accurate predictions, which will be discussed in Sect. [2.4.](#page-5-0) The lumped element model also gives a general prediction of the average fow angle in the test section due to the vertical velocity component. For example, for the case considered in Fig. [4,](#page-4-6) the fow angle of attack is predicted to be 8.1° in the steady-state solution. Lastly, the lumped element model also predicts the existence of a time constant that governs how quickly the system responds to a change in parameters (e.g. changing the resistance by adjusting louver positions). Consequently, this suggests that the importance of the transient efects predicted by Eq. [6](#page-4-5) would depend on the timescales involved with the gust (e.g. the speed of a traveling gust).

2.4 Potential fow solutions

The flow field in the test section can be modeled as a superposition of a uniform fow in the horizontal direction and a distribution of sinks on the top in a channel. Using a methodology similar to that proposed in Greengard [\(1990](#page-15-15)), the boundary conditions of the channel can be enforced through the use of an infnite number of image sources/sinks above and below the actual cross fow location. Figure [5](#page-5-1) shows this formulation with 10 sinks and some of their images, showing the transverse gust velocity feld without a background freestream. Working in the complex plane (with complex variable *z̃*), we consider a channel with lower and upper walls at $\tilde{z} = 0$ and $\tilde{z} = iH_{TS}$ respectively. A source/sink at a location \tilde{z}_{sk} induces a complex velocity

$$
w = \frac{\tilde{Q}_{\rm sk}}{2\pi(\tilde{z} - \tilde{z}_{\rm sk})}.
$$
\n(7)

We wish to place a row of sinks along the top surface of the channel at location $\tilde{z}_{sk,j} = x_j + iH_{TS}$, with each sink having strength $\hat{Q}_{sk,j}$. To enforce a no penetration boundary condition at the lower surface, we place image sinks at $\tilde{z}_{sk,j} \pm i2kH_{TS}$, for all integers *k*. This gives a total complex velocity induced by these sinks of

$$
w = \sum_{j=1}^{n} \frac{\tilde{Q}_{sk,j}}{2\pi} \sum_{k=-\infty}^{\infty} \frac{1}{z - z_{sk} + i2kH_{TS}}.
$$
 (8)

As discussed in Greengard ([1990](#page-15-15)), the inner sum can be viewed as the Laurent series expansion of a coth function.

Fig. 5 Physical and image sinks in the potential fow model

Adding in the freestream velocity u_0 , this gives the total complex velocity within the channel as

$$
w = u_0 + \frac{1}{4H_{\text{TS}}} \sum_{j=1}^{n} \tilde{Q}_{\text{sk},j} \coth\left(\frac{\pi}{2H_{\text{TS}}}(\tilde{z} - \tilde{z}_{\text{sk},j})\right),\tag{9}
$$

where again $\tilde{Q}_{sk,j}$ is the strength (flow flux per unit length) of the sink at $\tilde{z}_{sk,j}$. Note also that in the limit of a continuous distribution of sinks, the sum in Eq. [9](#page-5-2) can be replaced by an integral. The potential flow solutions in this paper use 105 discrete sinks and their images, which gives a velocity feld that closely matches that from a continuous sink distribution.

Figure [6](#page-6-0) shows the test section flow field given by this analytical solution steady conditions, in which $u_0 = 4.03$ m/s and $\int_0^{L_{\text{TS}}} \tilde{Q} dx = Q_{\text{SD}} / [\text{m}] = 0.73 \text{ m}^2/\text{s}$ (from the ODE solutions in Sect. [2.3\)](#page-3-0). The top subplot shows the top louver opening ratio and the fow angle of attack extracted from the potential fow solution. The top louvers are fully opened in this case (the opening ratio is 1 for all *x*-locations), thus \tilde{Q} is uniformly distributed along the top boundary. The mean fow angle of attack at half test-section height is $\bar{\alpha}_{TS}|_{y=\frac{1}{2}H_{TS}} = 8.45^{\circ}$, which is comparable to that was obtained from the solution of the lumped element model. The u_0 -normalized velocity components *u*[∗] and *v*[∗] are shown in contours. The spatial deceleration in *u*[∗] (as seen in the middle

Fig. 6 Potential flow solution for $V_{in} = 6 \text{ m/s}$ and louvers fully opened

subplot) causes the flow angle of attack to increase throughout the test section, which is expected since more fow goes into the suction duct as x increases. The v^* contour at the bottom shows that the vertical velocity gradient d*v*∗∕d*x* is approximately zero, away from the streamwise inlet and outlet regions. Note that the potential fow model may not be accurate near these boundaries, as it does not account for features of the wind tunnel such as the louvers downstream of the test section.

To simulate the traveling-wave fow feld with the potential flow model, the flow flux distribution on the top boundary is allowed to vary with respect to both the time and position based on Eq. [1](#page-3-2). Assuming that the vertical velocity at the test-section ceiling/suction-duct inlet is proportional to the local fow fux of the sinks, the traveling cross fow can be determined by appropriately defning the fow fux distribution $\tilde{Q}(t, x)$ based on the blockages of each of the subchannels in the suction duct. This allows for time-varying solutions for the fow feld to be determined for given wave speeds and frequencies. We emphasize that this method assumes that the fow response to changing louver positions is immediate, and thus that the fow feld at a given time is only a function of the instantaneous louver position. Section [3.4](#page-10-0) will show how this approach can be modifed to incorporate the transient effects predicted by the lumped element model (Eq. [5\)](#page-4-4), with an empirically-determined time constant.

Two snapshots of the solution at a wave speed of 6 m∕s and a wave frequency of 1.5 Hz are shown in Fig. [7](#page-6-1). Note that the inlet flow speed of the test section V_{in} and the total flow flux $\int_0^{L_{\text{TS}}} \tilde{Q} dx$ at the suction-duct inlet are different from

Fig. 7 Snapshots of potential flow solution for traveling wave at $c_w = u_0 = 6 \text{ m/s}$ and $f_w = 1.5 \text{ Hz}$. The top row shows the spatial distribution of the louver opening ratio and fow angle in the middle

of the test section, while the remaining subplots show the predicted instantaneous velocity felds

those in the fully-opened solution in Fig. [6.](#page-6-0) The wave speed and frequency chosen here to match subsequent experiments, which consider a mean flow speed of $u_0 = 6 \text{ m/s}$ and a highest wave frequency of $f_w = 1.5$ Hz (see Sect. [3.6](#page-13-0)). From the left ($t = 0.6T$, where T is the period) to right columns $(t = 0.9T)$, the snapshots visually show how traveling characteristics are realized by a spatiotemporally-varying sink distribution on the top boundary. The louver, opening ratio shown in the top plots demonstrates the sinusoidal form of the sink distribution. Although the correlation between the suction strength and the louver opening ratio may not be fully linear in reality, it is reasonable to assume a linear relation between them in this simplifed theoretical analysis (comprehensive studies on the dynamic control of the tunnel could be the subject of future research). At $t = 0.6T$, the zero opening ratio is at $x = 0.67L_{TS}$ while the full opening point has not moved into the test-section domain (the half wavelength in this case $\frac{1}{2}\lambda_w = 2$ m is close to the test-section length since we specifed the wave speed to be the same as the mean flow speed). The effect of the spatial suction distribution is visualized in the velocity feld contours, especially, the *v*−component contours show the infuence of neighboring suction concentrations as one of them is moving out of the test-section exit to the right and the second peak is entering the test-section inlet from the left. When the time comes to 0.9*T*, the frst peak is completely out of the domain and the second peak has *traveled* into and dominated the test section. The fow angle of attack also "travels" with the mean flow as a result of the varying suction effect.

Through the fow rates from the lumped element model and the fow feld from the potential fow solutions, the theoretical analysis provides some knowledge of what to expect from the suction-driven approach. It also gives preliminary guidance on how to operate the wind tunnel in experiments, which are discussed in the next section. However, we are aware that these theoretical models are simplifed descriptions of the wind tunnel, so one should not expect a full replication of the fow parameters or the fow feld from the models. Nevertheless, the potential fow model has a good potential to include more comprehensive confgurations, e.g., modeling an airfoil encountering traveling waves, taking advantage of the experimental discovery of this paper that the transverse gusts generated are nominally *irrotational* as a beneft of the low-vorticity fow feld created by the suction-driven approach (see Sect. [3.5\)](#page-12-0).

3 Experimental results and discussions

The test-section flow field is measured using point hot wire/x wire measurements, 5-hole aeroprobe measurements, as well as particle image velocimetry (PIV) in baseline, steady suction, step input, and traveling wave tests. For the baseline

tests, the downstream louvers are fully open and the top louvers are fully closed, while the breather remains fully closed. The calibration is obtained through the 5-hole aeroprobe and the single-wire hot wire measurements. The overall flow speed uncertainty is ± 0.08 m/s for the minimum fan blade pitch case and is \pm 0.13 m/s for the maximum fan blade pitch. The calibration gives the operational envelope of the flow speed to be $0.3 - 18.0$ m/s $(50 - 1000$ rpm) and 0.6 − 28.3 m∕s (50 − 1200 rpm) for the minimum and maximum fan blade pitch angles, respectively.

3.1 Baseline fow feld

Figure [8](#page-8-0) shows an example baseline flow field at $u_0 = 3.3$ m/s that is measured by PIV within a sampling window $0.38L_{TS} \le x \le 0.62L_{TS}$ longitudinally and $0.15H_{TS} \le z \le 0.85H_{TS}$ vertically in the test section.

Figure [8a](#page-8-0) gives the normalized mean feld (averaged over 5 s) of u^* –, v^* –component, and *z*–vorticity ω_z^* from top to bottom. The relatively small color map scales make the spatial variations in the velocity and vorticity visible, however, the variations are in fact very small if we examine the absolute values and the corresponding standard deviations which are shown in Fig. [8b](#page-8-0). High standard deviation values at the corners of the PIV window indicate that most of the uncertainty comes from the PIV measurement noise at these locations, which raises the overall σ values. As we sort out where the noise comes from, the standard deviation values (in both space and time) in the center region of the test section are $\sigma_{u^*} = 0.0098, \sigma_{v^*} = 0.0094$, and $\sigma_{\omega_z^*} = 2.08$. Note that these σ values are the mean values among the entire PIV window which includes the noisy boundaries and corners. If we solely consider the inner region $(0.4L_{TS} \le x \le 0.6L_{TS})$, 0.25*H*_{TS} ≤ *y* ≤ 0.75*H*_{TS}), $\sigma_{\omega_z^*}$ varies between 1.22 and 1.65, for instance. Therefore, the inner region appears near-white due to both the high σ values at the corners that extend the overall color scale and the small σ values (relative to the noise caused by PIV measurement) calculated in the inner region itself. Nevertheless, the spatial variations of σ in the inner region are still observable on logarithmic color scales. For the *z*−vorticity, particularly, the mean value is $\omega_z^* = -0.003$, which gives that 95.5% (2σ range) of the variation of ω_z^* is within -0.003 ± 4.16 with the PIV measurement noise being taken into account. This background noise level becomes important when we compare the vorticity variations in the cross-fow cases later in Sect. [3.5](#page-12-0). On the other hand, spatial distributions of the standard deviation carry the information about how stable the low-vorticity condition is maintained in the test section, which cannot be obtained through time-averaged data in steady cases or instantaneous snapshots in dynamic cases.

Fig. 8 PIV measurement of mid-test-section baseline flow at $u_0 = 3.3$ m/s

3.2 Steady suction

In all transverse fow experiments, the downstream louvers are half open in order to properly distribute the total fow rate between the test section and the suction duct. By fully opening louvers 5 and 6 at the center of the ceiling while keeping the rest of the louvers fully closed, the suction duct generates steady suction from $0.4L_{TS}$ to $0.6L_{TS}$ as shown by the louver opening ratio in Fig. [9a](#page-9-0), which defects the fow upward in the test section. The actual flow field (averaged over 5 s) in the PIV window (Fig. [9b](#page-9-0)) is comparable to the potential fow feld in the same window (Fig. [9a](#page-9-0)). As a result, the experimentally-measured velocity components extracted along the horizontal center line agree with the potential fow predictions (top subplot of Fig. [9b](#page-9-0)). The spatial distribution the of fow angle of attack at the center line also agrees with the potential fow prediction (top subplot of Fig. [9](#page-9-0)a), reaching a peak of $\alpha_{TS_{\text{max}}}$, $|y=\frac{1}{2}H_{TS}} \approx 9^\circ$. We conclude that the steady suction configuration gives a flow field that is consistent with the potential flow model with appropriately-defined flow rates.

3.3 Transient response

Understanding the transient response of the fow feld to the louver input is essential for precise control of the transient cross-fow velocity that is generated. Figure [10](#page-9-1) shows the snapshots of the fow feld in the transient process, in which the $0.4L_{TS}$ to $0.6L_{TS}$ top louvers are opened or closed by step inputs. The repeated step inputs keep the louvers open for 4 s and then closed for 4 s in sequence. From top to bottom, each row shows the u^* , v^* , and ω_z^* contours from left to right at a certain moment in dimensional time. Flow feld at each time correspond to the louver status which changes from the beginning of the step opening $(t = 0.4 s)$, during the transient response to opening $(t = 0.6 s)$, approaching a steady state at maximum opening $(t = 4 s)$, in the transient related to step closing ($t = 4.47$ s), and to after closing ($t = 4.6$ s). The results show that both u^* and v^* contribute to the evolution of the fow feld as the louvers rotate. It is worth noting that the vorticity value in the test section remains at a very low level regardless of the operating status of the louvers/fow conditions (again, the color maps are magnifed by the small scale), which will be discussed more in Sect. [3.5.](#page-12-0)

Point velocity results of the transient response are obtained by measuring the vertical velocity component at the center of the test section ($x = 0.5L$ _{TS}, $y = 0.5H$ _{TS}, and the lateral location is at the middle of the test-section span). The vertical velocity measured by the *x* wire and PIV are shown in Fig. [11](#page-10-1). The top plot shows the phase-averaged *x*wire measurements of v^* with $u_0 = 2.2$ m/s over 25 tests and the bottom plot shows the phase-averaged *v*[∗] extracted from PIV measurements with $u_0 = 3.3$ m/s over 10 cycles. Both sets of data demonstrate good repeatability of the transient gusts. The non-zero mean *v*[∗] value that appears during the louver-closed phase is due to the small amount of leakage

Fig. 9 Steady suction test results at $u_0 = 2.0$ m/s, comparing experimental measurements with potential flow model predictions

Fig. 10 Snapshots of transient response of cross flow at $u_0 = 3.3$ m/s

Fig. 11 Point velocity measurements in the center of the test section for transient response to louver opening and closing

which generates low-level suction on the top. While this defnitely needs to be compensated in wing/model tests (e.g., through effective angle of attack offset), on the other hand, it also shows how sensitive the test-section fow is to the suction effect. With these data, the time constants of the opening stage τ_{open} and the closing stage τ_{close} are found for the two cases above, where $\tau_{\text{open}} = 0.41$ s and $\tau_{\text{close}} = 0.11$ s in the $u_0 = 2.2 \text{ m/s}$ case, and $\tau_{\text{open}} = 0.46 \text{ s}$ and $\tau_{\text{close}} = 0.10 \text{ s}$ for the $u_0 = 3.3$ m/s case. The time constants are comparable between the two cases with a slight diference associated with the mean flow speed.

Although the louvers open and close at the maximum rotational rate when a step input is given (in practice, the louvers take approximately 0.03 s to rotate 90° when responding to the step input from minimum to maximum), the fow responds asymmetrically to the two-step inputs. Such asymmetry is also found in Neuhaus et al. ([2021\)](#page-16-22) where the gust is controlled by an upstream active grid. There, the rising and falling times in the velocity step tests are reported to have dependency upon the step amplitude, with the rising time increasing with step amplitude, and the falling time having the opposite trend. In addition, Neuhaus et al. ([2021](#page-16-22)) reports oscillations in the velocity response that are most apparent for the large-amplitude step-down cases. In the present work (which utilizes the largest step amplitude possible for the setup), the rising time τ_{open} is significantly longer than the falling time τ_{close} . This is because a longer time is required for the suction efect to develop due to the fuid inertance in the suction duct, which echos the ODE solutions from Sect. [2.3](#page-3-0). In contrast, when the louvers close, the suction is shut down directly without much interaction with the suction duct, so that τ_{close} reflects the much shorter time that is required for the mean flow to remove the suction efect. The streamwise velocity will experience a temporary

influence due to the coupling in the flow rates and the suction effect. The *u*^{*} contours clearly show the acceleration and deceleration regions that are divided by the sink/suction center. Therefore, the rising phase is not a strict "step" in terms of the aerodynamic input to wings/models in the test section. Nevertheless, it does shift the flow condition from one steady state to another in less than half of a L_{TS} -based convective time ($\tau_{\text{open}} < 0.5t_c$) or, in terms of the typical wing/model scale, less than 5 chord-based convective times. We, therefore, expect to observe substantial transient effects during this process.

3.4 Traveling gusts

To perform experimental validation of traveling transverse gusts, we frst consider isolated, single-peak gusts. The test wave frequency is fixed at $f_w = 1$ Hz, while the wave speed has two values; one equal to the mean horizontal flow speed $c_w = u_0$ and one that is half of the flow speed $c_w = 0.5u_0$. Figure [12a](#page-11-0) and b show snapshots of these two cases respectively, as the gusts travel through the test section with a mean flow speed of $u_0 = 2.84$ m/s. Note that the PIV results shown in this section are for non-phase-averaged data, showing the real-time fow feld response to the traveling-suction gust. From left to right the snapshots at several points in time are shown as the gusts travel in the streamwise direction. The top rows show the spatial suction distribution on the test-section ceiling via the louver opening ratio (note that the discontinuity due to the fnite louver size in the real cases is not represented here) and the model-predicted and the PIV-measured fow angles of attack along the *x*-direction. The middle rows show the *v*[∗] contours of the potential flow simulated flow fields and the bottom rows are the v^* contours of the PIV-measured fow felds. By comparing the two cases, the fow angle of attack shows dependency upon the traveling wave speed. The PIV-measured flow angle of attack does not reach the value that is predicted by the potential fow model when the wave speed is the same as the mean flow speed in the given experimental configuration. Instead, the measured and predicted fow angles of attack have better agreement in the half wave speed ($c_w = 0.5u_0$) case. The difference is also shown by the doubled vertical velocity magnitude in the half wave speed case (note the diferent color map scales). This phenomenon may relate to (1) the transient behavior of the test-section velocity responding to the louver motions that was discussed in Sect. [3.3](#page-8-1); (2) the split of fow rates in the dynamic cases does not exactly follow the quasi-steady model predictions, of which the limitation was mentioned earlier. On the other hand, we do observe that the velocity gradients d*v*∗∕d*x* and d*u*∗∕d*x* (not shown in the plots) are generated and carried by the traveling gusts in experiments regardless of the wave speed. For instance, the elliptical contour lines in the PIV-measured *v*[∗] felds are well

Fig. 12 Traveling gust results at three instances of time, comparing fow angle and velocity feld measurements with potential fow model predictions

replicated by the potential fow model, which indicates similar velocity gradient patterns between the model predicted and the experimental results.

To improve the accuracy of the potential flow model predictions in dynamic cases, we could implement the transient response of the fow responding to the louver input into the potential fow model. As an initial attempt, the exponential behavior of the vertical velocity component in Fig. [11](#page-10-1) during the step-open stage can be approximated by a frst-order linear dynamical system of the sink strength responding to the louver input, which has a normalized step response $h(t)$ of the form

$$
h(t) = 1 - \exp(-\tau_{\text{open}}t)
$$
\n(10)

which is of the same general form as given by the lumped element model, Eq. [5.](#page-4-4) Hence, the fow feld response is no longer a function of the instantaneous louver opening ratio, but also depends on its time history. In particular, if the original potential fow model gives a sink strength of $\hat{Q}_{\text{input}}(t)$, the transient correction for each sink is given by

$$
\tilde{Q}_{\text{output}}(t) = \int_{\tau=0}^{t} \tilde{Q}_{\text{input}}(\tau)h(t-\tau)d\tau, \qquad (11)
$$

where the time constant τ_{open} in the step response $h(t)$ is determined according to the measurements in Fig. [11.](#page-10-1) To account for the diferent mean fow speed, here the value of τ_{open} is interpolated from the measurements so we have $\tau_{\text{open}} = 0.44$ s at $u_0 = 2.84$ m/s. In addition, a DC gain of 0.8 is implemented in the correction to obtain the correct step amplitude. Note that only τ_{open} is used to make the firstorder correction, although two time constants exist in the experimental results. Figure [13](#page-12-1) shows the efect that this modifcation has on the spatial sink strength distribution for the isolated gust traveling at $c_w = u_0$.

The potential flow fields modified by this transient correction are shown in Fig. [14,](#page-12-2) where we again compare the

Fig. 13 Spatial distributions of sink strength for an isolated transient gust with $c_w = u_0$, at three instances of time

predicted flow angle of attack and v^* contours to the experimental results. The magnitudes of both the flow angle of attack and *v*[∗] (note the change of the color map scale) of the $c_w = u_0$ case (shown in Fig. [14a](#page-12-2)) are corrected since the modifed sink strength does not have enough time to rise

to the maximum value. Meanwhile, the $c_w = 0.5u_0$ (shown in Fig. [14b](#page-12-2)) flowfield is comparatively unaffected by the transient-response modifcation (the gain and the time constant in the dynamical system are unchanged), which indicates that the transient efect of the fow responding to the louvers is less signifcant at this lower wave speed. However, we also notice that this initial modifcation of the potential flow model may not fully represent the transient behaviors of the wind tunnel. For instance, the louver-closing stage is not well modeled as the time constants τ_{open} and τ_{close} are indeed diferent according to the experimental measurements, however, here the frst-order system only applies the τ_{open} time constant. Therefore, there could be further investigation combining the transient response and the potential flow model in future work.

3.5 Irrotationality of the gusts

As mentioned in previous sections, low-vorticity conditions are maintained in the test section, both with and without

Fig. 14 Results for a traveling gust compared with predictions from the potential fow model with a transient response correction

transverse gusts. We will show, through quantitative comparison of the vorticity levels, that it is fair to state that we are able to generate nominally *irrotational* gusts in both steady and dynamic circumstances.

The average vorticity background noise is $\omega_{z_{\text{ben}}}^* = -0.003 \pm 4.16$ (with a 2σ confidence interval), as calculated in Sect. [3.1,](#page-7-1) of which the noise/high standard deviation values mainly come from the corners and the boundaries of the PIV window. This vorticity background noise and its uncertainty interval are plotted in gray shadow in Fig. [15.](#page-13-1) The phase-averaged vorticity felds of the transient and traveling gusts cases are plotted in thick colored lines with their 2σ uncertainty boundaries are plotted in thin lines, where the uncertainty intervals are calculated with respect to both space and phase. We observe that the suction efect, which results in the transverse fow, has very small infuence on the mean values of the vorticity in all cases, which fuctuate near zero between −0.14 and 0.11. However, the suction efect does increase the uncertainty levels to some degree as the mean σ values are raised by 17.3%, 34.6%, and 38.4% for the three transverse gust cases, respectively, in comparison to the background noise uncertainty. The spatial standard deviation distributions of the vorticity

Fig. 16 Spatial standard deviation map of test-section vorticity

in the transverse gust cases are mapped in Fig. [16](#page-13-2), from which we confirm again that most of the uncertainty comes from the corners and boundaries of the PIV measurement window so we may conclude that the vorticity fuctuations in the data are largely due to this measurement uncertainty.

To give some context to the claim that the gusts generated are nominally irrotational, we compare the present results with flow fields that can be found in previous studies where the flows are typically rotational. For instance, the normalized vorticity values of the shear layers near airfoils vary within $\omega_z^* = \pm 30, \pm 50$, and ± 40 in steady flows (simulation) at *Re* = 500 (Asztalos et al. [2021](#page-15-16)), in surging fows (experimental) at $Re = 98,000$ (He and Williams [2020c](#page-15-6)), and under dynamic stall conditions (experimental) at *Re* = 550, 000 (Deparday and Mulleners [2019\)](#page-15-17), respectively. In contrast with these vorticity values, the net vorticity in the transverse gust tests is maintained at very low magnitudes (especially, the mean) near zero with uncertainties that are on the same order of the background noise uncertainty, which indicates that the fow in the test section is irrotational during the generation and difusion of the gust. In addition, the irrotationality is well distributed in space at individual times as the standard deviation does not vary much spatially, except for the measurement errors near the boundaries that have been clarifed to be noise.

3.6 Traveling waves in 1 − **cos form**

By enforcing specific wave functions $(Eq, 1)$ $(Eq, 1)$ $(Eq, 1)$, the wing is tested under single-sided sinusoidal transverse gusts, of which the propagated vertical disturbances are of the $1 - \cos$ form (FAA [2014\)](#page-15-18). The control signals are given to each louver independently to enable the louvers open and close sinusoidally at the wave frequency, with phase delays between each louver signal applying the desired wave speed. For example, when we let $c_w = u_0 = 6$ m/s, the disturbances vary in space and "travel" with a phase speed that matches the mean fow speed. We observe that the vertical velocity profles are not single-frequency sinusoidal waves in actual experiments, due to the presence of higher-frequency harmonics. This is because the transverse gusts are only controlled in an open-loop manner, with prescribed louver **Fig. 15** Time-series variation of test-section vorticity motions. However, this does not jeopardize the objectives of

these traveling wave tests, since the transverse characteristics and the velocity variations are maintained and the results have good repeatability in all cases, as we will show by example velocity profles and efective angles of attack in Fig. [17.](#page-14-0) Wave frequencies $f_w = 0.5, 1.0$, and 1.5 Hz are tested, corresponding to wavelengths of $c_w/f_w = 5.72L_{TS}$, 2.86 L_{TS} , and 1.90 L_{TS} , respectively. The vertical disturbance amplitude varies between $0.08u_0$ and $0.1u_0$, which also gives the gust ratio. With reference to a typical chord length of a test object $c = 245$ mm and a typical mean flow speed $u_0 = 6 \text{ m/s}$, the corresponding reduced frequencies, $k = \frac{\pi f_w c}{u_0}$, are $k = 0.0641, 0.1282,$ and 0.1923. The example profiles (phase-averaged over 240, 120, or 80 cycles depending on the wave frequency) in Fig. [17](#page-14-0) demonstrate how the wave frequency affects the actual velocity/flow angle of attack. In all cases, $tu_0/L_{TS} = 0$ is referenced to the the moment when louver 5 is at 0° with a positive angular rate (in other words, when the louver crosses zero and starts to open). We observe phase shifts in the velocity profles, so in the fow angle of attack, from lower to higher frequencies. If we use 0.5 Hz case as a reference, the phase shifts 0.120*T* in 1.0 Hz case and 0.246*T* in 1.5 Hz case. It is worth noting that higher wave frequencies also reduce the harmonics of the main frequency in terms of power density, i.e., the energy of the harmonics decreases from 61.6% to 32.9% and 21.9% of the total energy within the $0 - 10$ Hz (mean removed) power spectra as the wave frequency increases.

4 Conclusions

We have presented a suction-driven approach to generate transverse gusts for steady cross fow, transient, and traveling wave conditions. The Andrew Fejer Unsteady Wind Tunnel was modified for this purpose, where an additional flow passage was added to the wind tunnel, through which a portion of the fow diverges from the main fow due to the suction that was generated. As the air fowed into two sections, the flow in the test section became two-dimensional. The suction duct covered and changed the original test-section ceiling into a series of louver mechanisms, while retaining the preexisting louvers downstream of the test section. The louvers manipulated the resistance in the horizontal and vertical directions as they changed the blockage areas. The fuctuations of vertical velocity component could then be produced by properly distributing the fow rate to the louvers both in time and space.

Theoretical models were developed to make estimations of the suction efect in the wind tunnel, and to provide preliminary benchmarks for the experiments. Analytical potential fow solutions for the fow felds under the three transverse fow conditions were presented and compared with experimental results. The potential flow results agreed well with the PIV and x-wire measurements, although more details of the fow feld were discovered from the results of the traveling waves, where the dependency of the fow angle of attack upon the gust wave speed was demonstrated. This dependency could not be predicted by the potential flow model, which assumes that the flow field is only a function of the instantaneous louver positions. However, by approximating the time history of the suction strength through a frst-order linear dynamic system that represents the transient process, the potential model predictions can be improved and compared to experimental results of dynamic gust cases to a certain degree.

Transient responses of the fow to the suction input were documented so that later design of a complete gust control system becomes feasible. This could, for example, eventually enable accurate control of gust velocity profles and/or spectra. In particular, we observed a substantial difference between the step open and close time constants. The signifcant rising time in the step open response was mostly due to the inertia of the fow in the suction duct. Therefore, one possible direction for improving the performance of future unsteady wind tunnels is to utilize a "running" suction duct in which the fow is constantly moving so it stands by to the demand from the test section. In the

Fig. 17 1 − cos gust profles, comparing the time evolution of the velocity and fow angle in the center of the test section

meantime, expanding the control capability of the tunnel to create more types of gusts (e.g. with diferent waveforms) could be another focus of future work.

The gusts generated by the wind tunnel have low turbulence levels and a high degree of repeatability. Besides the high-quality flow conditions in basic tests, the modified wind tunnel demonstrated promising potential for generating irrotational transverse gusts of diferent types. The fact that gusts are nominally irrotational allows for accurate potential fow predictions of the fow feld. The vorticity in the test section was kept at background noise level regardless of the fow conditions (steady, transient, or traveling gusts). Given that classical unsteady aerodynamic theories were developed based on potential fow assumptions, the tunnel provides a convenient experimental environment to apply, validate, and extend these classical theories. For example, exploring the wing-gust interaction in lowvorticity gusts could be one of the immediate impacts of this feature. Further, one could more directly model certain gust conditions by starting with potential fow models and adding modifcations to match experimental observations. For instance, one could consider a potential fow setup incorporating a 2-D wing in the test section, with a distribution of source/sink elements to model gusts. The inclusion of source/sink or doublet elements to model additional disturbances (Asztalos [2021](#page-15-19)) that could convect downstream over the wing in the test section (in additional to a traveling gust) is another example of a complex potential fow model that could be utilized.

From the PIV visualizations of the flow fields, we demonstrated that the wind tunnel could create velocity gradients, especially d*v*∕d*x*, that could be carried by the traveling wave gusts. X-wire measurements of $1 - \cos f$ form gust waves with diferent wave frequencies were generated to show the infuence of the gusts which included the fow angle of attack and the velocity gradients. The wind tunnel's transverse gust capability could be valuable in wing-gust studies that require the presence of traveling waves and spatial velocity gradients.

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Declarations

Conflict of interest The authors declare that they have no confict of interest.

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