

*Rapid communication*
**Type-I non-critically phase-matched second-harmonic generation in  $\text{Gd}_{1-x}\text{Y}_x\text{Ca}_4\text{O}(\text{BO}_3)_3$** 

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**Abstract.** Second-harmonic generation was  $z$ -cut observed  $\text{Gd}_{1-x}\text{Y}_x\text{Ca}_4\text{O}(\text{BO}_3)_3$  ( $\text{Gd}_{1-x}\text{Y}_x\text{COB}$ ) and the dependence of the phase-matching wavelength on the mixing ratio  $x$  has been investigated. The dependence on both temperature and angle tuning was examined as well. We found the suitable composition for noncritical frequency doubling at 930 nm, which is the lasing wavelength of Nd:YAlO<sub>3</sub> on the  $^4\text{F}_{3/2} \rightarrow ^4\text{I}_{9/2}$  transition.

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Recently, interest in the new nonlinear materials of the  $\text{ReCa}_4\text{O}(\text{BO}_3)_3$  family (Re = rare earth) has grown. In comparison to the conventional and established nonlinear materials, ReCOB combines some advantageous properties. As well as its good nonlinear optical properties, i.e. high nonlinear coefficients and transparency in the UV [1], it has good mechanical properties, allowing easy polishing. Furthermore, these materials have a high damage threshold and are non-hygroscopic. They melt nearly congruently and big crystals can be grown. The existence of large lattice sites offers the possibility of rare earth ion doping, and good lasing properties are already proved. This even makes ReCOB appropriate for self-frequency doubling.

Frequency doubling of Nd-doped ground-state lasers with wavelengths between 900 nm and 950 nm into the blue spectral region can be realized in GdCOB and YCOB by type-I critical phase matching. The orientation of the crystal ( $\theta$ ,  $\varphi$ ) that meets the phase-matching condition has to be calculated from the Sellmeier equations. Accordingly, critical phase-matching can be achieved in GdCOB at these wavelengths with the wave vector  $\mathbf{k}$  orientated either in the  $xy$  plane or in the  $zy$  plane of the indicatrix [2]. However, it is experimentally observed that “there is a lack of second-harmonic generation in the  $zy$  plane” [3]. In YCOB second-harmonic generation can be realized in this spectral range with crystals cut in the  $xy$  or  $zx$  plane [3]. The disadvantage of critical phase matching is the low angular acceptance and the pres-

ence of beam walk-off between the fundamental and the second harmonic.

In contrast, non-critical phase matching, which can be achieved by cutting the crystal along one of the main dielectric axes,  $x$ ,  $y$  or  $z$ , yields large angular acceptance bandwidths. One further advantage of non-critical phase matching is the lack of beam walk-off, so that the crystal can be very long in order to raise the efficiency of the frequency conversion.

In  $z$ -cut crystals, phase matching can be realized with the polarization of the fundamental and the second harmonic parallel to the  $y$  and  $x$  axes, respectively. In [1] the pure materials YCOB and GdCOB are investigated and Sellmeier coefficients are given. According to [1] the theoretical phase-matching wavelengths for  $z$ -cut YCOB and GdCOB are 840 nm and 966 nm, respectively. In [3] slightly different Sellmeier coefficients for YCOB are given. As a result, the phase-matching wavelength is calculated to be 827 nm. M. Yoshimura et al. [4] suggested growing  $\text{Gd}_{1-x}\text{Y}_x\text{COB}$  and tuning the non-critical phase-matching wavelength in the range from 827 nm to 966 nm by changing the compositional parameter  $x$ .

In the case of  $z$ -cut crystals, the output power of the second-harmonic is proportional to the square of the nonlinear coefficient  $d_{12}$ . Unfortunately this is the smallest of the nonlinear coefficients in YCOB ( $d_{12} = 0.43 \text{ pm V}^{-1}$ ) and in GdCOB ( $d_{12} = 0.24 \text{ pm V}^{-1}$ ) as well [3]. Indeed, there is no possibility to use  $x$ -cut or  $y$ -cut  $\text{Gd}_{1-x}\text{Y}_x\text{COB}$  as a type-I second-harmonic generator for neodymium ground-state lasers. Using the Sellmeier coefficients determined by M. Iwai et al. [1] one expects to tune the non-critical phase-matching wavelength in  $x$ -cut crystals from 1486 nm (YCOB) to 1633 nm (GdCOB);  $y$ -cut  $\text{Gd}_{1-x}\text{Y}_x\text{COB}$  seems to be interesting for non-critical second-harmonic generation into the UV. The range for phase matching extends from 735 nm (YCOB) to 838 nm (GdCOB). Also,  $y$ -cut  $\text{Gd}_{0.275}\text{Y}_{0.725}\text{COB}$  was reported for type-II phase matching at  $1.06 \mu\text{m}$  [5].

We have grown  $\text{Gd}_{1-x}\text{Y}_x\text{COB}$  of different compositions with the aim of second-harmonic generation in the spectral

region of neodymium ground-state lasers. We found that  $z$ -cut  $\text{Gd}_{0.84}\text{Y}_{0.16}\text{COB}$  converts the infrared radiation of  $\text{Nd}:\text{YAlO}_3$  emitted from the  ${}^4\text{F}_{3/2} \rightarrow {}^4\text{I}_{9/2}$  transition (930 nm) into blue light (465 nm) by non-critical type-I phase-matching.

## 1 Crystal growth of (Gd,Y)COB

The crystals have been grown using the Czochralski technique with radio-frequency induction heating [2]. The pulling process is automatized by the crucible weighing method. Because the melting temperatures of the mixed crystals lie between those of the  $\text{GdCOB}$  (1480 °C) [2] and  $\text{YCOB}$  (1510 °C) [6], an iridium crucible (40 ml) was used. The power of additional windings of the RF coil was coupled to a cylindrical afterheater. Both the crucible and the afterheater were embedded in alumina ceramics. This resulted in the axial temperature gradient above the melt surface being so flat that no remarkable thermal stress remained in the grown crystal. The crystal growth was performed in flowing nitrogen atmosphere. The growth rate was  $2 \text{ mm h}^{-1}$  and the rotation  $10 \text{ min}^{-1}$ . The starting materials  $\text{Gd}_2\text{O}_3$ ,  $\text{Y}_2\text{O}_3$ ,  $\text{CaCO}_3$ , and  $\text{B}_2\text{O}_3$  were of 5N and 4N quality. They were dried, mixed, and sintered following standard procedures. The melting behaviour of  $\text{GdCOB}$  and  $\text{YCOB}$  is reported to be congruent and nearly congruent, respectively [2, 6]. Therefore we mixed the (Gd,Y)COB corresponding to the aimed composition of the crystal. According to microprobe analysis (ems, camebax), the actual yttrium concentration is slightly higher than the concentration ratio of the starting powders. The average segregation coefficient for yttrium was found to be 1.12. Because the phase-matching experiments were performed in  $z$ -orientated rods, the crystals were grown perpendicular to the (801) plane, which is close to the  $z$  axis of the indicatrix. The crystal boules reached 65 mm in length and 18 mm in diameter and the yield was about 40%. Their habit was cylindrical without any facet.

## 2 Phase-matching measurements

### 2.1 Angle tuning

In Fig. 1 the dependence of the phase-matching wavelength  $\lambda_{\text{pm}}$  on the mixing parameter  $x$  is shown. The collimated beam from a Ti:sapphire laser with 600 mW output power was focussed ( $f = 40 \text{ mm}$ ) into crystals with different mixing ratios. The phase-matching wavelengths were determined by tuning the wavelength of the Ti:sapphire for maximum blue output power. The wavelengths were measured with a 1-m spectrometer.

The crystal containing 16% yttrium is appropriate for frequency doubling of  $\text{Nd}:\text{YAlO}_3$  lasing on the ground-state transition at 930 nm. This crystal is approximately 15 mm long and the phase-matching condition proved to be quite insensitive to variation of the angle  $\theta$  between the  $\mathbf{k}$  vector of the incident Ti:sapphire beam and the  $z$  axis. In Fig. 2 the phase matching-wavelength is shown as a function of the angle of the propagating beam to the  $z$  axis inside the crystal. The external angles are even larger since the refractive index is roughly 1.7. The saddle point in Fig. 2, which is characterised

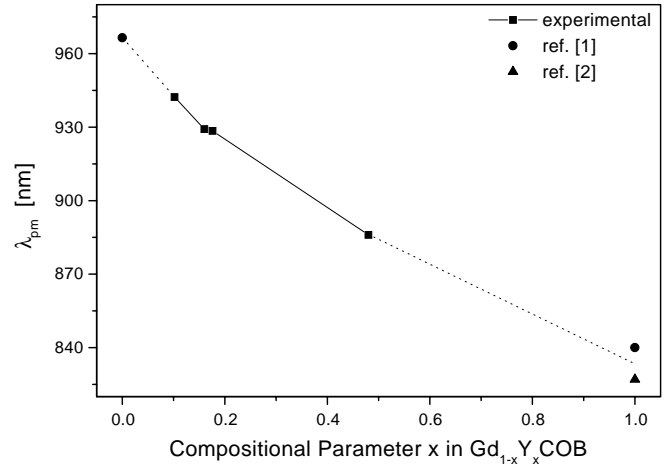


Fig. 1. Phase-matching wavelengths of  $z$ -cut  $\text{Gd}_{1-x}\text{Y}_x\text{COB}$  against the compositional parameter  $x$

by  $\partial\lambda_{\text{pm}}/\partial\theta = 0$ , corresponds to the case  $\mathbf{k} \parallel \mathbf{z}$ . In this adjustment the phase-matching wavelength of  $\text{Gd}_{0.84}\text{Y}_{0.16}\text{COB}$  was determined to be  $\lambda_{\text{pm}} = 929.3 \text{ nm}$  at room temperature.

Adjusting the angles  $\theta_{zx} \neq 0^\circ$  in the  $zx$  plane increases the phase-matching wavelength, while angles  $\theta_{zy} \neq 0^\circ$  in the  $zy$  plane yield shorter wavelengths. To check the observed wavelength tuning behaviour, calculations using the Sellmeier coefficients of pure  $\text{GdCOB}$  [1] were carried out. For angle tuning in both planes, the calculated wavelength dependence on angle tuning for  $\text{GdCOB}$  is compared with the measured dependence for  $\text{Gd}_{0.84}\text{Y}_{0.16}\text{COB}$ . In Fig. 3a,b the solid line (right-hand scale) shows the calculated dependence of the phase-matching wavelength on angle tuning for pure  $\text{GdCOB}$ . The left-hand scale refers to the measured wavelengths of  $\text{Gd}_{0.84}\text{Y}_{0.16}\text{COB}$ . Because of the difference in composition, the absolute values of the phase-matched wavelengths differ by almost 40 nm and therefore the scales were shifted against each other. Indeed, the measured wavelength dependence on angle tuning agrees well with the calculated one. As predicted by the theory for  $\text{GdCOB}$ ,

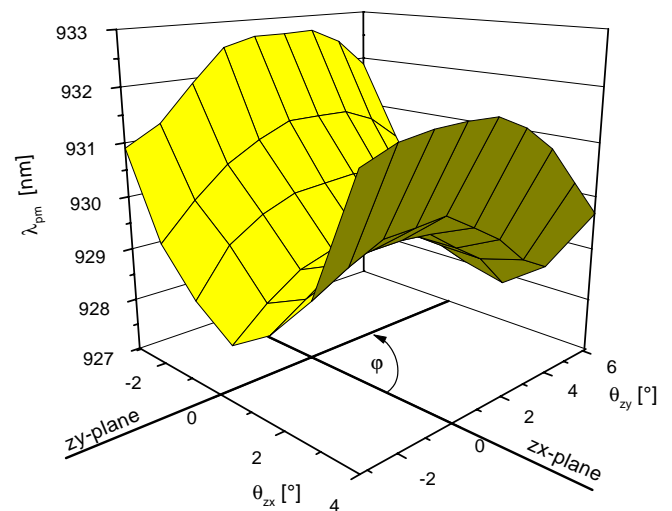
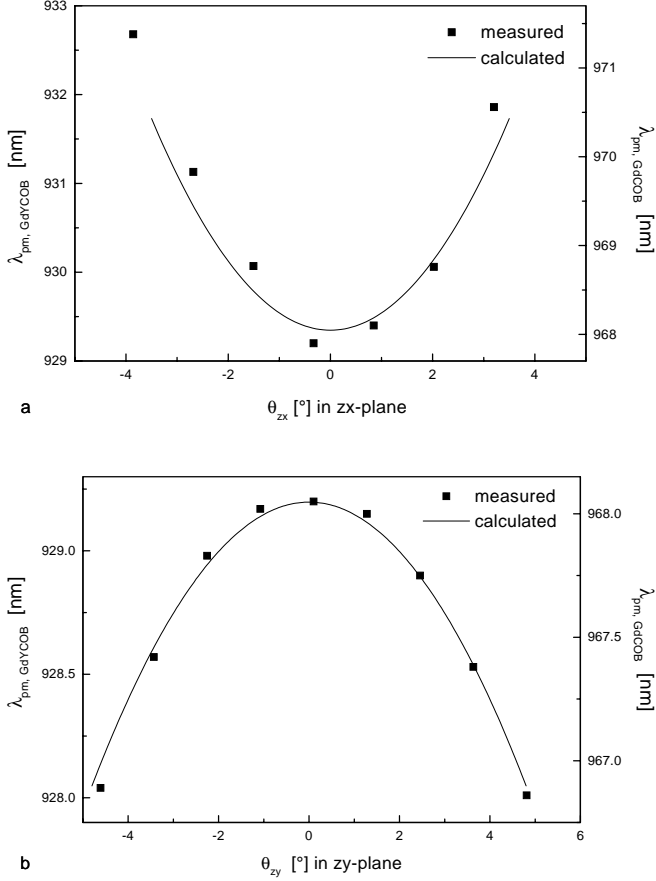


Fig. 2. Phase-matching wavelength as a function of angle tuning



**Fig. 3a,b.** Calculated phase matching of GdCOB (right scale) and measured phase matching of Gd<sub>0.84</sub>Y<sub>0.16</sub>COB (left scale) for variation of  $\theta$  in the  $zx$  and  $zy$  planes

the measured variation of the phase-matching wavelength is stronger for angle tuning in the  $zx$  plane than for tuning in the  $zy$  plane.

The angular acceptance bandwidth is defined by the FWHM of the  $\text{sinc}^2(\Delta k l/2)$  function, which is proportional to the power of the second-harmonic. The corresponding  $\Delta k_{FWHM}$  is given by

$$\Delta k_{FWHM} = \frac{1.772\pi}{l} \quad (1)$$

The dependence of  $\Delta k$  on  $\theta$  can be expressed as a series of powers:

$$\Delta k \approx \Delta k(0) + \left. \frac{\partial \Delta k}{\partial \theta} \right|_{\Delta k=0} \Delta \theta + \left. \frac{\partial^2 \Delta k}{\partial \theta^2} \right|_{\Delta k=0} \Delta \theta^2 + \dots \quad (2)$$

Since we are dealing with non-critical phase matching, the second derivative is the first non-vanishing term. With  $\Delta k = \Delta n 4\pi/\lambda$  and  $\Delta n = n_y(\lambda) - n_x(\lambda/2)$  the angular acceptance bandwidth is obtained by combining (1) and (2):

$$\sqrt{l\Delta\theta^2} = \left[ \frac{1.772\lambda}{4(\partial\Delta n/\partial\lambda)(\partial^2\lambda/\partial\theta^2)} \right]^{1/2} \quad (3)$$

$\partial^2\lambda/\partial\theta^2$  was obtained from a fit (harmonic approximation) to the experimental data shown in Fig. 3a,b. To determine

$\partial\Delta n/\partial\lambda$  for Gd<sub>0.84</sub>Y<sub>0.16</sub>COB we calculated the values for GdCOB and YCOB using the Sellmeier equations [1] and weighing them with the composition ratio. Thus for angle tuning in the  $zx$  and  $zy$  planes, the values for the internal angular acceptance bandwidths  $l^{1/2}\Delta\theta$  are 29.7 cm<sup>1/2</sup> mrad and 62.1 cm<sup>1/2</sup> mrad, respectively.

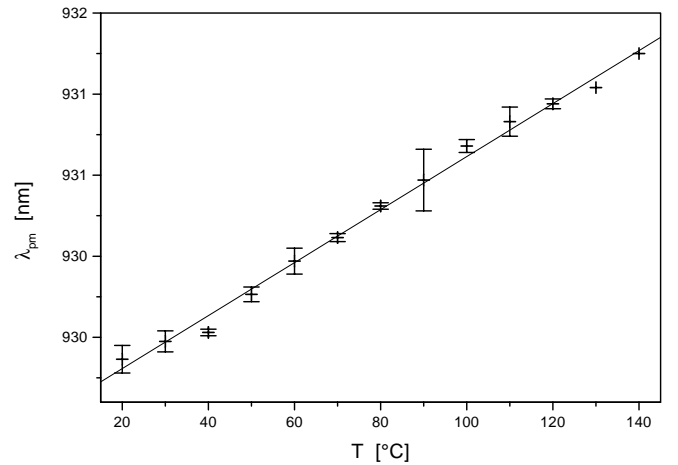
## 2.2 Temperature tuning

The influence of the temperature on the phase-matching condition was also examined. For this, the crystal was positioned in an oven. The  $k$  vector of the Ti:sapphire radiation was parallel to the  $z$  axis. The temperature was increased gradually from 20 °C up to 140 °C in steps of 10 °C. After temperature equilibrium was reached, the wavelength of the Ti:sapphire laser was tuned in such a way that the intensity of the generated blue light was maximum. In the same way, the phase-matching wavelengths were also measured while decreasing the temperature. Comparing the two measurements, we detected neither hysteresis nor any other anomaly. In Fig. 4 the phase-matching wavelengths, averaged from the readings at increasing and decreasing temperature, are drawn versus the temperature. It is found that there is only little variation of the phase-matching wavelength with the temperature. The correlation is linear in the temperature range from 20 °C to 140 °C and  $d\lambda_{pm}/dT$  was determined to be 0.016 nm/K.

With considerations analogue to those for the angular acceptance bandwidth, one obtains the temperature acceptance bandwidth. However, since the first derivative  $d\lambda_{pm}/dT$  does not vanish, the corresponding expression is

$$l\Delta T = \frac{1.772\lambda}{4(\partial\Delta n/\partial\lambda)(\partial\lambda/\partial T)} \quad (4)$$

According to this calculation, the value of the temperature acceptance bandwidth  $l\Delta T$  for Gd<sub>0.84</sub>Y<sub>0.16</sub>COB is 42.8 cm K which is 5.5 times that of LBO. This is in good agreement with the values for the pure materials GdCOB ( $l\Delta T = 38$  cm K) and YCOB ( $l\Delta T = 65$  cm K) [1].



**Fig. 4.** Phase-matching wavelength vs. temperature

### 3 Summary

We have presented  $z$ -cut  $\text{Gd}_{0.84}\text{Y}_{0.16}\text{COB}$  as a type-I non-critically phase-matched second-harmonic generator for 930-nm light. This composition is appropriate for frequency conversion of a Nd:YAlO<sub>3</sub> laser on the ground-state transition. Laser experiments are now in progress.

The dependence of the phase-matching wavelength on angle tuning was examined in the  $zx$  and  $zy$  planes. The internal angle acceptance bandwidths  $l^{1/2}\Delta\theta$  were determined to be 29.7 cm<sup>1/2</sup> mrad and 62.1 cm<sup>1/2</sup> mrad, respectively.

Temperature tuning was also investigated. The phase-matching wavelength is proportional to the temperature at least in the temperature range from 20 °C to 140 °C. The temperature acceptance bandwidth  $l\Delta T$  is 42.8 cm K.

The large acceptance bandwidths, the possibility of growing big crystals by the Czochralski technique and the high non-linearity, coupled with the possibility of active ion dop-

ing for self-frequency-doubling, make  $\text{Gd}_{1-x}\text{Y}_x\text{COB}$  a good candidate for commercial applications.

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