

# Cantilever-enhanced photoacoustic detection of hydrogen sulfide (H<sub>2</sub>S) using NIR telecom laser sources near 1.6 μm

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**Abstract** Sensitive detection of hydrogen sulfide (H<sub>2</sub>S) at different pressure levels using a cantilever-enhanced photoacoustic detector in combination with a telecom NIR L-band laser source is reported. Amplitude and wavelength modulation schemes for photoacoustic signal generation are compared. A detection limit ( $3\sigma$ ) of 8 ppmv was achieved for amplitude modulation mode with a 50-s averaging time for the H<sub>2</sub>S absorption near 1.6 μm. As compared to simulated spectra, the cantilever-enhanced photoacoustic detection approach in combination with the sufficiently stable and narrow bandwidth NIR laser is able to reproduce the rotationally resolved H<sub>2</sub>S spectrum at low pressures of 300 mbar.

## 1 Introduction

Sensitive detection of hydrogen sulfide (H<sub>2</sub>S) is essential for production control and environmental monitoring purposes in the field of petrochemical, paper and pulp as well as biotechnological processes. The occupational exposure limit recommended by the European Agency for Safety and Health at Work (OSHA) is 7.1 mg m<sup>-3</sup> (5 ppmv) [1]. The permissible exposure limit value for H<sub>2</sub>S, recommended by US National Institute for Occupational Safety and Health (NIOSH), is 10 ppmv, the Immediately Dangerous to Life and Health (IDLH) level is 300 ppmv and lethal concentrations are in the range of 2000 ppmv [2]. Although H<sub>2</sub>S

concentrations as low as 500 pptv manifesting in the characteristic odor of rotten eggs can already be detected by the human olfactory sense, the total loss of olfactory sensation starts at 150–200 ppmv [3]. Because of the wide occurrence of H<sub>2</sub>S in industrial processes and its often negative impact on process stabilities and product quality, its concentration needs to be tightly monitored. Furthermore, safety considerations and legal concentration limits also necessitate the accurate determination of H<sub>2</sub>S levels. In practice, concentrations ranging from sub-ppm levels at low pressures to several per cents at atmospheric conditions need to be monitored. Due to such diverse requirements, H<sub>2</sub>S analyzers based on different measurement technologies have been developed and are in industrial use. Apart from spectroscopic techniques based on absorption measurements, a range of other analytical techniques such as pulsed UV fluorescence [4], sulfur chemiluminescence [5], colorimetry employing a lead acetate tape [6], flame photometry as detector in gas chromatography [7] as well as electrochemical detection techniques ranging from potentiometric, galvanic, coulometric and amperometric detection [8] is frequently employed. It is interesting to note that in the petrochemical industry the lead acetate tape method is still in frequent use. Also, gas chromatographic methods are popular as they can be used to detect several components almost simultaneously, but this technique requires preparation and extraction of the sample gas leading to a time-consuming measurement. A general drawback of non-spectroscopic techniques is the fact that they do not allow for direct measurements. This, however, also applies to H<sub>2</sub>S detection based on UV fluorescence as this technique requires sample combustion as well as detection by chemoluminescence, where addition of reagents is required.

Most of the spectroscopic techniques are based on the detection of the absorption spectrum of the molecules in

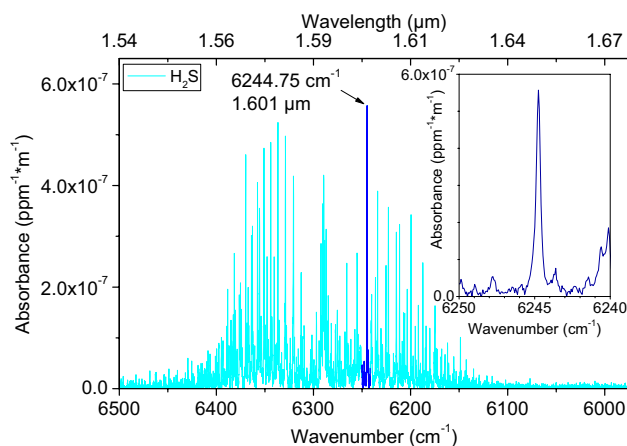
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the infrared (IR) spectral region. Sensors based on tuneable diode laser absorption spectroscopy (TDLAS) mostly utilize near-infrared diode lasers due to their distinguished properties, such as single-mode operation, good beam quality, high repetition rate, relatively narrow line width, large current tuning range, good operability, low power consumption and low investment costs [9–11]. When measuring H<sub>2</sub>S by IR spectroscopy, high sensitivities are difficult to achieve. This is due to the intrinsically weak linestrengths of the H<sub>2</sub>S ro-vibrational features within the spectral range covered by diode lasers. These are several magnitudes lower compared to other gases of industrial interest. For example, the absorbance of CH<sub>4</sub> at 1.646 μm is  $1.800 \times 10^{-5} \text{ ppm}^{-1} \text{ m}^{-1}$  compared to the H<sub>2</sub>S absorbance of  $5.573 \times 10^{-7} \text{ ppm}^{-1} \text{ m}^{-1}$  at 1.601 μm (factor 32) [12]. A way to overcome this drawback is to increase the interaction path length by using multipass gas cells [13–16]. This generally adds to the bulkiness of the systems, and hence, a small size is hardly achieved with H<sub>2</sub>S TDLAS sensors. The path length can be reduced by using wavelength modulation or balanced detection approaches, which furthermore improve the sensitivity of TDLAS sensors [17–19]. Although the detection of H<sub>2</sub>S concentrations of several ppb has been demonstrated by employing integrated cavity output spectroscopy approach (ICOS) [20], such sensitivities are difficult to obtain in field measurements as the robustness of this kind of systems remains limited [21, 22]. Possible alternatives to bulky multipass absorption or delicate sensing schemes based on cavity spectroscopy are photoacoustic H<sub>2</sub>S measurement strategies [23–26]. A fully developed and industry-tailored H<sub>2</sub>S sensor to meet the specific selectivity requirements based on photoacoustic spectroscopy employing dual-channel longitudinal-type resonator cell with capacitive microphone readout and a LOD of 0.5 ppmv is described in [23]. An interesting rather new development in this regard is the technique of cantilever-enhanced photoacoustic spectroscopy (CEPAS) [27]. In this paper, we report on our results on sensitive H<sub>2</sub>S detection at different pressure levels using a cantilever-enhanced photoacoustic detector in combination with a telecom NIR L-band laser source.

## 2 Spectral characteristics of H<sub>2</sub>S in the NIR region

The 6500–6000-cm<sup>-1</sup> near-infrared spectral region is of interest as it can be easily accessed with commercially available telecommunication laser technology. Furthermore, this spectral interval corresponds to an atmospheric window with very few cross-interactions stemming from other molecules. Vibrational overtone and combination bands of H<sub>2</sub>S can be located at 6450–6150 cm<sup>-1</sup> (refer to Fig. 1).



**Fig. 1** H<sub>2</sub>S absorption spectrum in the 6500–6000-cm<sup>-1</sup> region and single peak at 6250–6240 cm<sup>-1</sup> (inset) at 25 °C and 1013 mbar

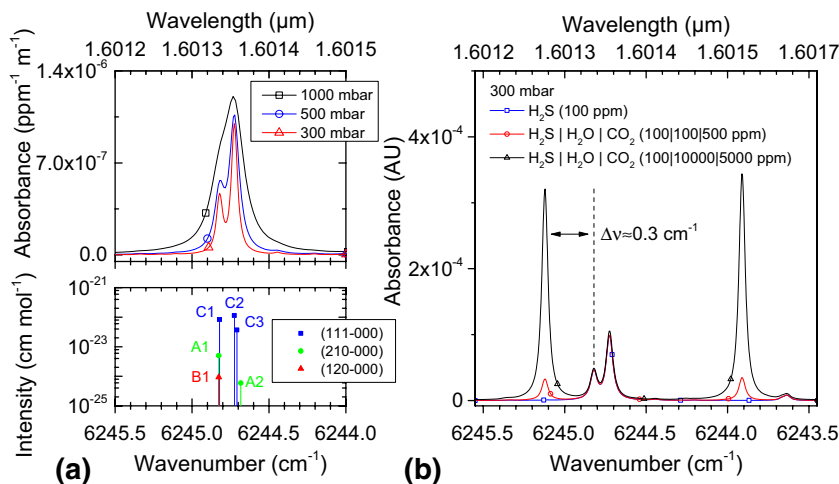
Regarding the spectral H<sub>2</sub>S features in the 1.6-μm region (6270–6220 cm<sup>-1</sup>), extensive research and simulation was conducted by Edwards et al. [28] and extended by Lechuga-Fossat et al. [29]. In this region, accurate line positions can be addressed to the (210) (111) and (102) bands. Resonances between these three states can be addressed to Coriolis interactions between the rotational levels of the (111) vibrational state and the levels of the (210) and (012) states as well as to Darling-Dennison interactions between the (210) and (012) vibrational states [29].

In this work, the strongest absorption feature around 6245 cm<sup>-1</sup> (1601 nm) corresponding to the 3 transition lines listed in Table 1 was chosen for selective H<sub>2</sub>S measurements. The rotational levels of H<sub>2</sub>S as a three-dimensional asymmetric top rotator with three different reciprocal moments of inertia are labeled by the three standard quantum numbers  $J$ ,  $K_a$  and  $K_c$  [30].

The absorption spectrum in this region is shown in Fig. 1, indicating an absorbance of  $5.57 \times 10^{-7} \text{ ppm}^{-1} \text{ m}^{-1}$  [12]. A HITRAN simulated H<sub>2</sub>S absorption spectrum around 6245 cm<sup>-1</sup> with a total pressure ranging from 1000 to 300 mbar is shown in Fig. 2a. Splitting of the H<sub>2</sub>S band into its strongest ro-vibrational transition components (111–000) can be observed at reduced pressures. Although the sensor investigation in this work was limited to certified H<sub>2</sub>S in N<sub>2</sub> mixtures, the possibility of water (H<sub>2</sub>O) and carbon dioxide (CO<sub>2</sub>) interference is investigated via simulation. Absorbance spectra at a total pressure of 300 mbar of 100 ppmv H<sub>2</sub>S in a standard air matrix with 100 ppmv water and 500 ppmv CO<sub>2</sub> content and 100 ppmv H<sub>2</sub>S in a possible process air matrix of 10,000 ppmv H<sub>2</sub>O and 5000 ppmv CO<sub>2</sub> are shown in Fig. 2b. Negligible spectral interference can be expected from H<sub>2</sub>O lines in this wave number region, whereas possible CO<sub>2</sub> interference has to be accounted for. Taking advantage of spectral line resolution

**Table 1** Transition line parameters of H<sub>2</sub>S in the 6245-cm<sup>-1</sup> region

Label	Position (cm <sup>-1</sup> )	Intensity (cm mol <sup>-1</sup> )	VS <sub>up</sub>	VS <sub>low</sub>	RQN <sub>up</sub> ( <i>J</i> , <i>K<sub>a</sub></i> , <i>K<sub>c</sub></i> )	RQN <sub>low</sub> ( <i>J</i> , <i>K<sub>a</sub></i> , <i>K<sub>c</sub></i> )
A1	6244.8265	5.013E-24	(210)	(000)	1, 1, 1	2, 2, 0
B1	6244.8264	9.338E-25	(120)	(000)	10, 5, 6	10, 8, 3
C1	6244.8212	8.299E-23	(111)	(000)	2, 1, 1	3, 1, 2
C2	6244.7252	1.140E-22	(111)	(000)	3, 1, 3	4, 1, 4
C3	6244.7084	3.698E-23	(111)	(000)	3, 0, 3	4, 0, 4
A2	6244.6832	5.918E-25	(210)	(000)	10, 8, 2	10, 9, 1

**Fig. 2** Simulated H<sub>2</sub>S absorption spectrum around 6245 cm<sup>-1</sup>, total pressure of 1000, 500 and 300 mbar (a). Absorbance spectra at a total pressure of 300 mbar of 100 ppmv H<sub>2</sub>S in a standard air matrix with 100 ppmv water and 500 ppmv CO<sub>2</sub> content and 100 ppmv H<sub>2</sub>S in a possible process air matrix of 10,000 ppmv H<sub>2</sub>O and 5000 ppmv CO<sub>2</sub> (b)

starting at a reduced pressure of 300 mbar, a sufficient separation of  $\sim 0.3$  cm<sup>-1</sup> from the interfering CO<sub>2</sub> transitions can be expected for the targeted H<sub>2</sub>S feature.

### 3 Cantilever-enhanced photoacoustic spectroscopy

Photoacoustic spectroscopy (PAS) is an established technique for sensitive gas analysis [31, 32]. The fundamental principle of PAS is based on the absorption of electromagnetic radiation by the target molecules, which are excited to higher electronic, vibrational, or rotational quantum states. The nonradiative relaxation processes by collisions with molecules produce local heating of the sample gas. Adiabatically generated pressure fluctuations by thermal expansion can be detected in the form of acoustic waves. The detection of the PA signal traditionally encompasses the use of sensitive microphones or other piezo-transducers.

The PA signal *S* measured by the transducer is given by the Eq. 1:

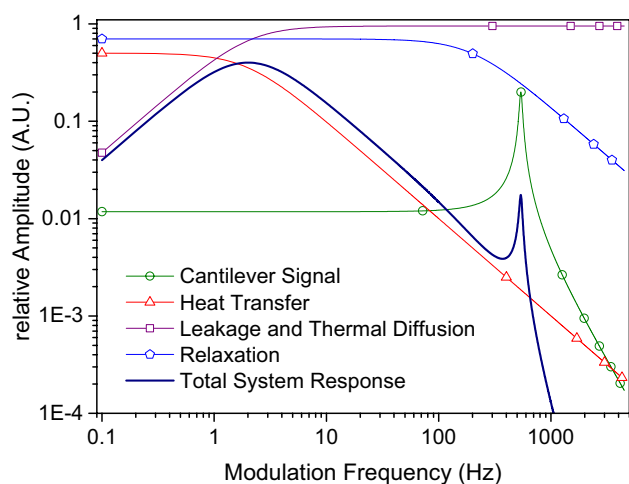
$$S = C * P(\lambda) * \alpha(\lambda), \quad \text{with} \quad C = \frac{G * (\gamma - 1) * L * Q}{f * V}, \quad (1)$$

where *C* is the frequency-dependent cell constant (V cm W<sup>-1</sup>), *P* the optical power of the laser source and  $\alpha$  the absorption coefficient which is related to the gas concentration (*N*, number density of molecules) and absorption

cross section ( $\sigma$ ) by  $\alpha = N\sigma$ , with *L* and *V* the length and the volume of the cell, respectively,  $\gamma = (c_p/c_v)$  the specific heat constant, *f* the modulation frequency, *G* the geometrical factor and *Q* the quality factor of the generated acoustic resonance.

The cell constant *C* is influenced by the geometry of the sample cell, the beam profile, the transducer response and the nature of the acoustic mode [32]. The absorption of modulated light generates an acoustic signal in the cell, which can be amplified by tuning the modulation frequency to one of the acoustic resonances of the sample cell. In this resonant case, the cell works as an acoustic amplifier and the absorbed laser power is subsequently accumulated in the acoustic mode of the resonator for *Q* oscillation periods, where *Q* is the quality factor, typically in the range of 10–300 [31].

Due to the relatively high sensitivity typically around  $5 \times 10^{-9}$  cm<sup>-1</sup> W Hz<sup>-1/2</sup>, PAS can potentially yield smaller sensors compared to traditional absorption methods [33]. However, PAS is a power scalable technique and therefore calls for excitation sources with high output powers [34]. Therefore, PAS applications usually utilize NIR distributed feedback (DFB) lasers, which typically provide output power between 10 and 40 mW. A further advantage of NIR laser sources in combination with PAS is the possibility of a fiber-coupled light output, which simplifies the optical complexity of the system. Telecommunication NIR diode



**Fig. 3** Model of different frequency-dependent components influencing the total cantilever-enhanced photoacoustic system response (calculated from [34])

lasers have been used by several groups in various photoacoustic applications with traditional capacitive microphones as the pressure sensing device [24].

A novel detection approach, developed by Wilcken and Kauppinen [35], utilizes a silicon cantilever as an optical microphone with interferometric measurement of the sensor displacement and is termed cantilever-enhanced photoacoustic spectroscopy (CEPAS) [27, 35, 36]. The frequency-dependent total system response combining the effects of the cantilever itself, gas heat transfer, relaxation pathways of the excited molecules and leakage through the gap and thermal diffusion to cell walls is discussed and derived in detail in [34, 35] and is depicted in Fig. 3.

The isolated response of the cantilever can be treated as constant until the resonance frequency is reached. Heat transfer and leakage through the gap between the frame and the cantilever and thermal diffusion effects to the cell walls dominate the shape of the response function at low frequencies, revealing a maximum of the total system response at the frequency range between 0.5 and 10 Hz. The total system response decreases due to contributions of heat transfer and relaxation mechanisms until the resonant frequency of the cantilever, where a local maximum is seen. After passing the resonance frequency, the total system response decreases rapidly, mainly due to relaxation mechanisms and the isolated cantilever response function. This fact is limiting the practicable measurement range well below the resonance frequency.

The optimum sensitivity achieved for the cantilever pressure transducer is superior to other cell designs using capacitive microphones, and the nonresonant operation of CEPAS cells can avoid the matrix influences on the PA signal [34, 37]. A sensitive TDL-PAS setup based on cantilever-enhanced detection of oxygen ( $O_2$ ) was demonstrated

by Cattaneo et al. [38]. A LOD of 20 ppmv could be achieved with a 30-mW DFB laser. Laurila et al. employed carbon dioxide ( $CO_2$ ) CEPAS detection. A normalized sensitivity of  $2.2 \times 10^{-9} \text{ cm}^{-1} \text{ W Hz}^{-1/2}$  for  $CO_2$  detection at 1572 nm was achieved [39]. Using a 4.7-W 532-nm Nd:YVO<sub>4</sub> laser, Peltola et al. [40] reported a normalized sensitivity of  $2.6 \times 10^{-10} \text{ cm}^{-1} \text{ W Hz}^{-1/2}$  for nitrogen dioxide ( $NO_2$ ) detection.

Such a high sensitivity suggests that reasonable detection limits for  $H_2S$  could also be achieved using medium power light sources such NIR laser diodes around 1600 nm.

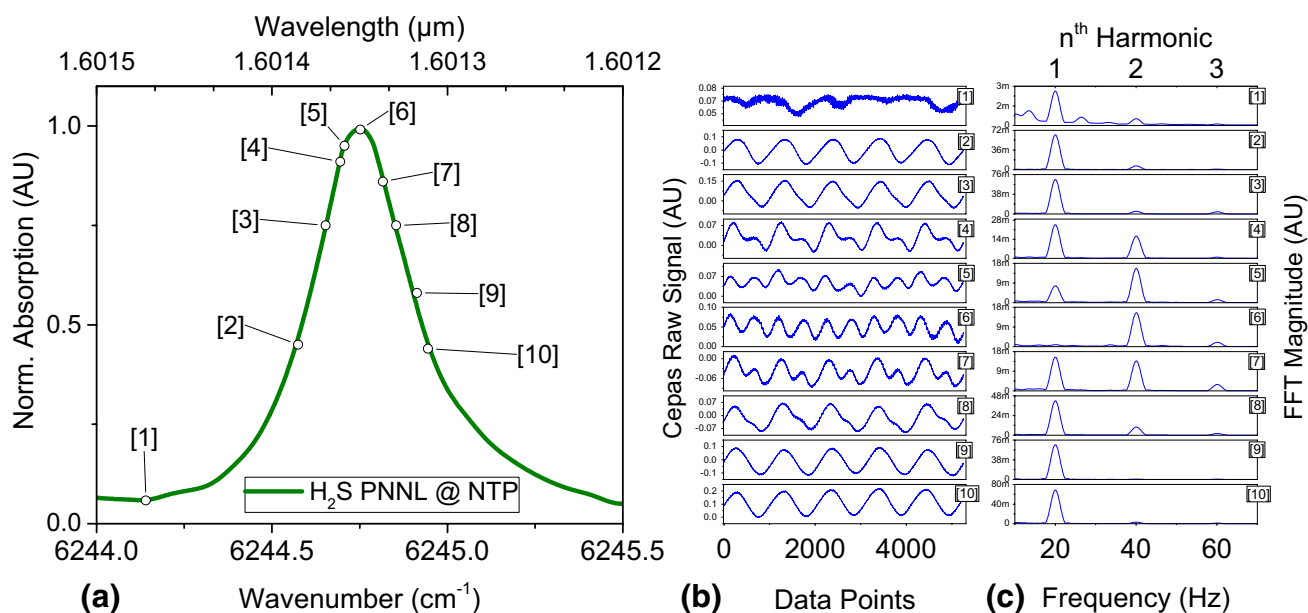
### 3.1 Modulation schemes in PAS

In the most basic form, the generation of the PA signal can be accomplished by modulating the laser injection current with a square waveform of 50 % duty cycle between laser threshold and the designated upper current level (amplitude modulation, AM).

In wavelength modulation (WM), the injection current itself is modulated or superimposed with an arbitrary periodic function. As a consequence, the emission wavelength is modulated at a certain depth (in wave numbers) and frequency  $f_0$ . Here the modulation depth and modulation frequency of the laser were driven with a triangular waveform in order to improve the harmonic signal components [41]. In general, a periodic modulation of the argument of a nonlinear transfer function produces an output signal that contains higher harmonics of the fundamental frequency [42]. Therefore, when performing wavelength modulation (WM), additional detection possibilities arise as higher harmonics of  $f_0$  can be extracted from the frequency-domain spectrum. When scanning the absorption line while performing WM, the analytical signal also contains information on the shape of the absorption line in the scanned region. A detailed overview of the underlying mechanisms of different modulation schemes is discussed in [43, 44].

In both modulation schemes, the resulting time-domain cantilever signal from the analog circuit module is digitized and subsequently Fourier-transformed, providing a frequency power spectrum. When amplitude or wavelength-modulated laser light with a modulation frequency of  $f_0$  is used as the excitation source, the fundamental and, respectively, higher harmonics can be extracted from the frequency-domain spectrum. Analysis of higher frequency components in AM is not considered as these frequencies do not contain additional information. Wavelength modulation (WM) schemes result in complex FFT spectra with contribution of all harmonics.

As an example, several positions along the  $H_2S$  peak around 1600 nm ( $6344.8 \text{ cm}^{-1}$ ) at normal temperature and pressure condition (293.15 K and 1013 mbar) with the according CEPAS raw signal waveforms and the postprocessed FFT signals are outlined for a WM detection scheme. Slowly



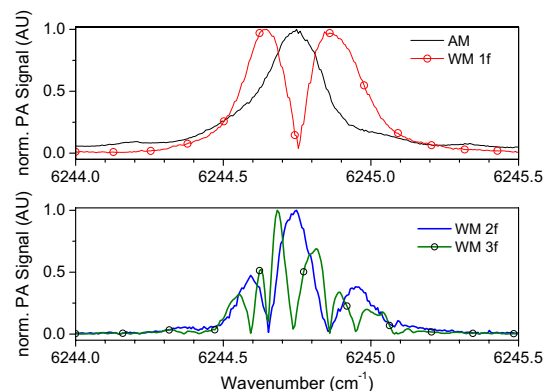
**Fig. 4** H<sub>2</sub>S absorption peak around 1600 nm (6245 cm<sup>-1</sup>) with outlined points (a) and cantilever raw signals (b) and FFT spectra for the outlined points 1–10 (c)

scanning the modulated laser emission wavelength over the characteristic peak of the target analyte H<sub>2</sub>S alters the interferometer signal of the cantilever as outlined in Fig. 4.

The H<sub>2</sub>S absorption peak transduces the WM modulated laser emission into an AM modulated waveform with varying amplitudes of the harmonic components. Starting at point (1), the FFT signal only shows a major contribution of the first harmonic component, whereas the second harmonic contribution increases following points (2–5), according to the slope of the H<sub>2</sub>S peak. Pure second harmonic components in the raw cantilever signal can be extracted at point (6). Nearly equal contributions from the harmonic components can be observed at point (7), whereas points (8–10) mark a continuous decrease in the second harmonic contribution.

Similar to the well-established wavelength modulation spectroscopy techniques, slow scanning over the absorption feature of interest and recording of the extracted  $n$ th harmonic component of the raw cantilever signal result in  $n$ th derivative ( $nf$ ) like spectra.

As opposed to recording the  $nf$  spectrum with TLAS and phase-locked loop (PLL) detection schemes, the phase information is not extracted by FFT. As a consequence derivative, WM-PA spectra only show absolute values. AM and WM PAS spectra up to the third harmonic of the H<sub>2</sub>S feature in the 6244.0–6245.5-cm<sup>-1</sup> spectral region are illustrated in Fig. 5. Slight distortions and asymmetry of the  $2f$  and  $3f$  lineshape wings can be attributed to amplitude modulation effects and due to interference from neighboring transitions.



**Fig. 5** Normalized PA H<sub>2</sub>S spectra at 1000 mbar recorded with AM and WM schemes

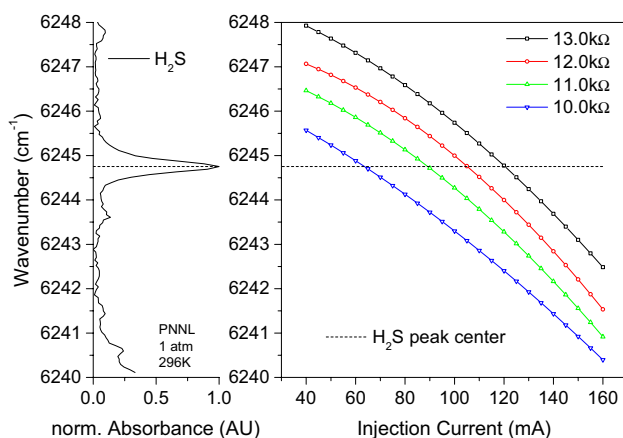
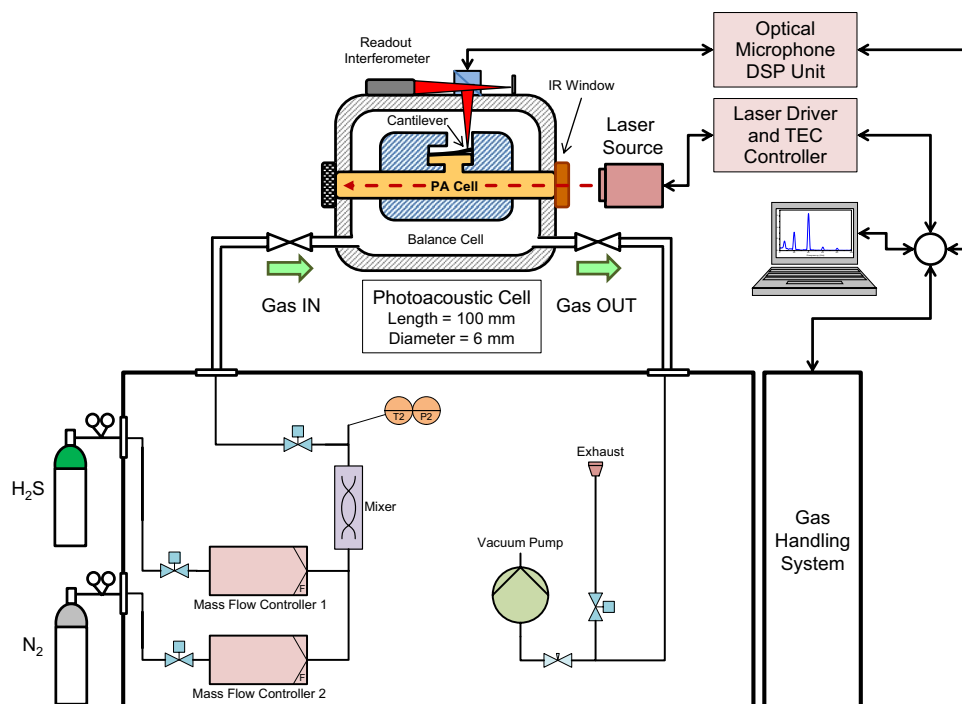
## 4 Experimental setup and sample preparation

The experimental setup was located on a vibration-isolated laser table and is shown in Fig. 6 along with a detailed view on the measurement cell for performing cantilever-enhanced photoacoustic measurements.

### 4.1 Laser and laser operation

The NIR light source (NLK 1556 STB) used was a pig-tailed InGaAs DFB telecom laser from NTT Electronics (Tokyo, Japan) operating in the L-band around 1600 nm with output power of 20 mW. This laser had an integrated TEC element and a single-mode fiber output and was

**Fig. 6** Schematics of the photoacoustic sensor setup



**Fig. 7** Laser tuning characteristics and H<sub>2</sub>S spectrum at 296 K and 1013 mbar in the tuning range of the laser

operated from 290 to 293 K with a maximum injection current of 130 mA. The side-mode suppression ratio was 35 dB. A temperature (TED200C) and current (LD205) controller both from Thorlabs (Newton, NJ, USA) were used to adjust and stabilize the operation temperature to 0.01 K and to control the injection current of the laser. Coarse control of the laser diode emission wavelength control was achieved by adjusting the laser temperature, whereas fine-tuning of the laser emission wavelength was accomplished by variation in the injection current. The output power of the laser source was monitored with the integrated photodiode and with a Gentec Solo 2 (Gentec-EO,

Quebec, Canada) power meter. The tuning characteristics for different laser temperatures (NTC values) and injection currents are shown in Fig. 7. Additionally, the H<sub>2</sub>S spectrum in the tuning range of the laser is shown as well.

#### 4.2 Cantilever-enhanced photoacoustic cell

The cell used in this work was a PA201 model manufactured by Gasera Ltd (Turku, Finland). The PA201 consists of the photoacoustic cell body with the interferometric cantilever microphone. The gas cell is located inside the body and the valves, and the connectors for the gas exchange are attached on the sample cell and balance cell sides of the cantilever. The gas exchange through the sample-in and sample-out ports is controlled with an external control unit. The lowest possible sample gas pressure was limited by the included pumping unit to 300 mbar. As shown in Fig. 6, the cantilever separates the gas volume inside the body into two parts: the photoacoustic (PA) cell and the balance cell. The PA cell (yellow) is a polished and gold-coated cylindrical stainless steel tube (inner diameter of 6 mm and length of 100 mm) closed with a ZnSe window on the front end and a beam dump in the rear end of the tube. The balance cell is used for compensating the acceleration noise and reducing the effective spring constant due to the reduced gas spring effect [34, 45]. The displacement of the silicon cantilever induced by the pressure wave from the dissipation of the absorbed infrared laser radiation is recorded by a compact Michelson interferometer. The carrier signals of the interferometer are calculated in an analog circuit module and

produce a signal proportional to the cantilever displacement. The time-domain signal from the analog circuit module is digitized and subsequently Fourier-transformed, providing a frequency power spectrum. The magnitude of the peaks is directly proportional to the cantilever displacement, and hence, a linear dynamic range can be achieved for quantitative analysis [34].

### 4.3 Operation by amplitude and wavelength modulation

Photoacoustic measurements were taken in amplitude modulation (AM) as well as wavelength modulation (WM) schemes. For AM experiments, the laser was electronically chopped with frequencies ranging from 10 to 700 Hz. The signal was recorded at the fundamental frequency of the resulting frequency power spectrum. In WM, the modulation depth and modulation frequency of the laser was driven with a sinusoidal waveform. The signal was recorded at the second harmonic of the resulting frequency power spectrum.

### 4.4 Gas sample preparation

Different H<sub>2</sub>S concentration levels were prepared by N<sub>2</sub> dilution from a 2000-ppmv H<sub>2</sub>S standardized gas bottle (matrix N<sub>2</sub>) with a mass flow and pressure-controlled gas handling system, developed in house.

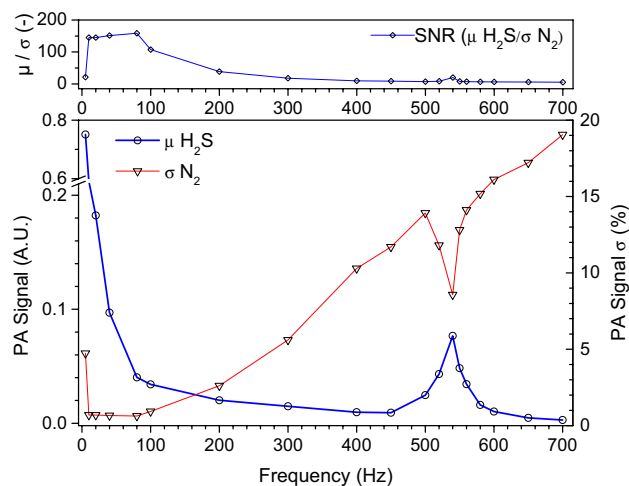
### 4.5 Reference measurement and reference data

Reference spectra were recorded on a Bruker Vertex 80v FT-IR spectrometer (Bruker Optics, Germany) with 0.075 cm<sup>-1</sup> spectral resolution. Additional spectral information and reference data in the 6300–6200-cm<sup>-1</sup> region was gained via simulation with the Hitran 2012 database [46].

## 5 Results and discussion

### 5.1 Influence of operational parameters of amplitude and wavelength modulation in CEPAS on the obtained signal-to-noise ratio

Following Eq. 1 and the different contributions to the total cantilever-enhanced photoacoustic signal  $S$  as outlined in Fig. 3, it is interesting to note that  $S$  is direct proportional to the laser power, concentration of the analyte, a possible Q factor of the photoacoustic cell, which in general refers to acoustic resonances of the measurement cell. In addition to these parameters and contributions, dependencies of  $S$  on further parameters such as modulation (chopping) frequency and depth and gas pressure are expected as well.



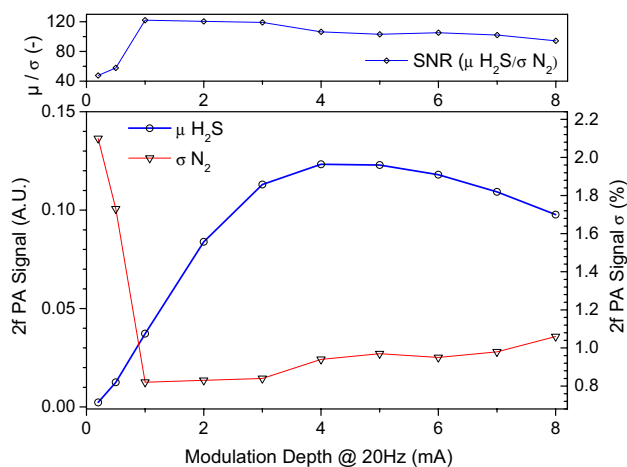
**Fig. 8** AM PA signal mean  $\mu$  and standard deviation  $\sigma$  for single-point measurement of 1000 ppmv H<sub>2</sub>S, 20 mW laser power

For investigating the influence of the chopping frequency on the AM signal, a concentration of 1000 ppmv H<sub>2</sub>S at a total gas pressure of 1013 mbar was applied. When aiming for an optimal signal-to-noise ratio, the dependency of the photoacoustic signal  $S$  as well as the corresponding noise level from a given chopping frequency is of interest. Figure 8 illustrates the dependency of the FFT-transformed interferometer signal with the chopping frequency for a H<sub>2</sub>S concentration of 1000 ppmv and a recording time of 100 s and a FFT block size of 16,384 samples (corresponding to 778.9 ms at a sampling rate of 21,035 samples s<sup>-1</sup>). For evaluating the signal-to-noise ratio (SNR,  $\mu/\sigma$ ), the relative standard deviation  $\sigma$  of the measured signal of the empty (N<sub>2</sub> filled) cell ( $\sigma_{N_2}$ ) was calculated and plotted together with the calculated mean  $\mu$  of the recorded photoacoustic signal with H<sub>2</sub>S present ( $\mu_{H_2S}$ ).

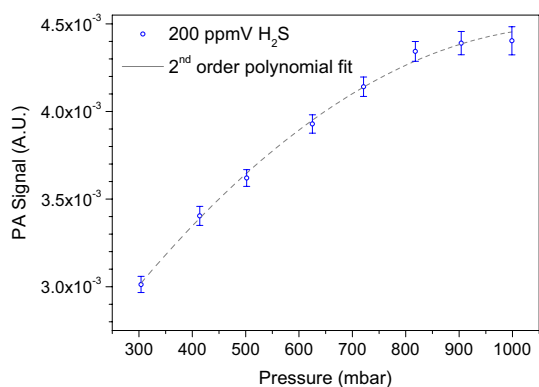
With the 20-mW laser, the optimal chopping frequency was in the range from 10 to 200 Hz with relatively stable interferometer signal better than 2 % in terms of standard deviation  $\sigma$ . A trend of increasing noise signal with higher chopping frequencies could be found. In the region of the resonance frequency of the PA cell, the interferometer signal stability is improved but could not reach the value of comparable signal magnitudes at 20–100 Hz chopping frequency. Judging from the obtained SNR of the PA signal ( $\mu_{H_2S}/\sigma_{N_2}$ ), optimal chopping frequencies in the 20- to 80-Hz range could be identified.

Concerning WM modulation, the influence of the modulation depth on the photoacoustic signal was investigated and is displayed in Fig. 9. The laser injection current of 100 mA was superimposed with a 20-Hz sinusoidal modulation current ranging from 0 to 8 mA.

The optimum modulation depth in terms of signal strength was found to be between 4 and 5 mA, although



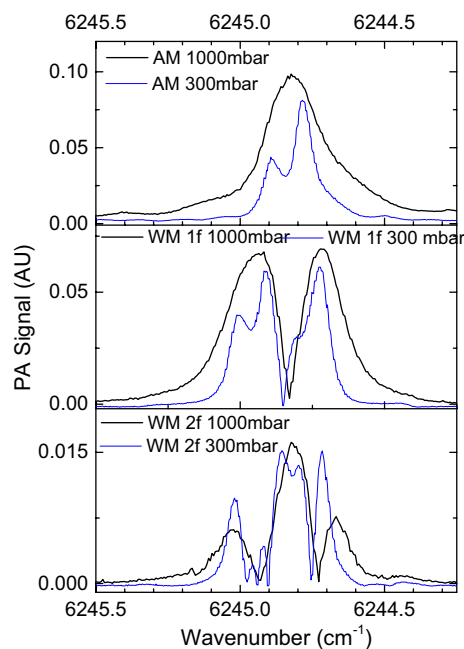
**Fig. 9** WM PA signal mean  $\mu$  and standard deviation  $\sigma$  for single-point measurement of 1000 ppmv  $\text{H}_2\text{S}$ , 100 mA injection current, 20 Hz superimposed modulation current



**Fig. 10** AM PA signal dependency on the total gas pressure, 100 mA injection current, 40 Hz chopping frequency

the  $2f$ -PA signal mean to its standard deviation ratio  $\mu/\sigma$  suggested a wide applicable range of modulation depths between 1 and 6 mA.

The PA signal dependency on the total gas pressure is shown in Fig. 10. The available pressure range from the system could be set from 300 to 1000 mbar. Unlike laser-based direct absorption spectroscopy, where the integrated absorbance is linearly scaling with increasing pressure, the photoacoustic signal pressure dependence is of nonlinear nature [47]. Several studies were conducted in order to address and deduce the sources of the pressure dependence of the photoacoustic sensitivity. For both resonant and non-resonant types of photoacoustic systems, slow vibrational relaxation in dilute mixtures due to the absence of suitable collision partners, the geometry of the cell and the pressure transducer and the strong pressure dependence of the Q factor could be identified as main contributors for the pressure dependence of the photoacoustic sensitivity [48–52].



**Fig. 11** AM,  $1f$  and  $2f$  spectra for 1000 ppmv  $\text{H}_2\text{S}$  in  $\text{N}_2$  at pressure levels of 1000 and 300 mbar. Splitting of the  $\text{H}_2\text{S}$  band into its ro-vibrational transition components can be observed at 300 mbar. The chopping frequency was 20 Hz, the modulation depth was 4 mA and the FFT time constant was 778.9 ms

In the case of complex matrices, it would be crucial to balance between improved peak resolution and decreased signal amplitude when applying low-pressure measurements.

## 5.2 Photoacoustic $\text{H}_2\text{S}$ spectrum in the range of 6245.5–6244 $\text{cm}^{-1}$

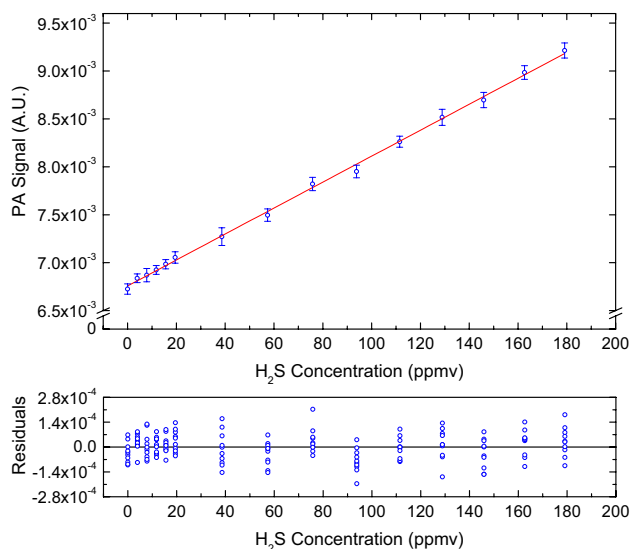
A recorded photoacoustic  $\text{H}_2\text{S}$  spectrum in the range of 6245.5–6244  $\text{cm}^{-1}$  at pressure levels of 1000 and 300 mbar is shown in Fig. 11. According to the applied modulation schemes, normal absorption spectra are obtained with AM, and spectra with derivative information are recorded with WM mode. At 300 mbar splitting of the  $\text{H}_2\text{S}$  band into its main ro-vibrational transition components of the (111–000) band could be observed (Figs. 12, 13).

## 5.3 Quantitative $\text{H}_2\text{S}$ measurements

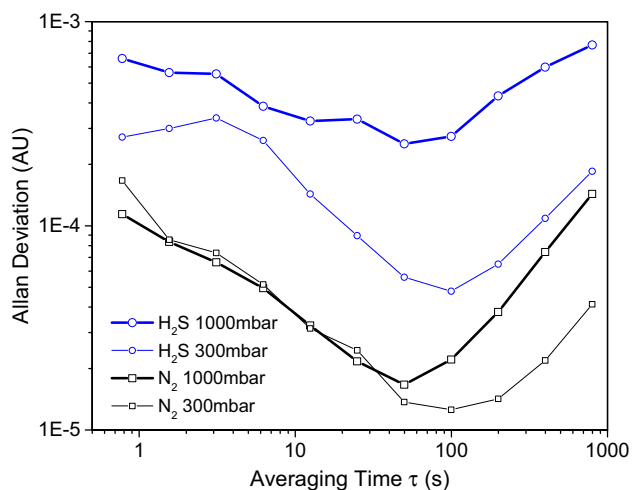
Due to the fact of higher signal amplitudes and better SNR for AM photoacoustic signals in comparison with WM signals, subsequent measurements were taken in AM fashion and at total gas pressures of 1000 mbar.

The resulting calibration curve in the range from 0 to 180 ppmv  $\text{H}_2\text{S}$  was recorded with the 20-mW laser, with an amplitude modulation frequency of 20 Hz, 100 mA injection current and FFT time constant of 778.9 ms. Each point of the calibration curve correlates to an averaging of 10 gas





**Fig. 12** AM CEPAS signals acquired at different concentration levels of H<sub>2</sub>S in N<sub>2</sub> ranging from 0 to 200 ppmv at 1000 mbar. The chopping frequency was 20 Hz, FFT time constant of 778.9 ms. The calculated LOD ( $3\sigma$ ) was 8 ppmv H<sub>2</sub>S at 50-s averaging time



**Fig. 13** AM CEPAS signals Allan plots for pure N<sub>2</sub> and 1000 ppmv H<sub>2</sub>S in N<sub>2</sub> at pressure levels of 1000 and 300 mbar. The chopping frequency was 20 Hz, the FFT time constant was 778.9 ms

samples which were individually drawn from the gas mixing setup. After successful measurement of the PA signal at the respective H<sub>2</sub>S concentration step, the photoacoustic cell was purged, new sample gas volume was drawn in and the valves were closed for data acquisition.

The resulting calibration curve of the photoacoustic detection of H<sub>2</sub>S yielded a limit of detection ( $3\sigma$ ) of 8 ppmv H<sub>2</sub>S in the gas stream. Analysis of the residuals provided a convenient means of confirming the linearity of the calibration data.

## 5.4 Long-term stability

In spectroscopic measurements, the stability of the system is an important issue, as long-term signal averaging is an effective means to improve the sensitivity and detection limit. One way to characterize the stability and long-term drifts is to measure the Allan variance of the signal. The Allan variance is a time-domain analysis technique developed in 1966 originally used for the assessment of frequency stability of precision oscillators [53]. The application of the Allan method to optical sensors has been discussed by Werle et al. [54] where the Allan variance is measured for equally timed sequences of the signal. In this context, the Allan variance can be expressed as:

$$\sigma^2(\tau) = \frac{1}{2(N-1)} \sum_{i=1}^{N-1} (\bar{y}_{i+1} - \bar{y}_i)^2$$

where  $\tau$  is the integration time,  $N$  is the number of consecutive observations, and variable  $\bar{y}_i$  is the average of  $i$  consecutive observations of the recorded signal.

The stability test of our setup was made with the DFB laser with pure N<sub>2</sub> and with H<sub>2</sub>S concentrations of 1000 ppmv with total pressures of 300 and 1000 mbar.

When working with a H<sub>2</sub>S concentration of 1000 ppmv in N<sub>2</sub>, minimum Allan deviation was observed with 50-s averaging time for 1000 mbar, whereas a minimum Allan deviation could be observed with up to 100-s averaging time for 300 mbar.

In the case of pure N<sub>2</sub> in the PA chamber, minimum Allan deviation was surveyed with 50-s averaging time for 1000 mbar and up to 100 s for the reduced pressure measurements as well, while the Allan deviation itself could be nearly reduced by the order of one magnitude.

For comparison, trace gas sensors based on direct optical absorption detection usually exhibit drifts that do not allow useful data averaging for time periods longer than 100–200 s [55].

The performance of the detection system is influenced by various noise sources. Measurements by Kauppinen et al. indicated that the ambient acoustic noise is the dominant noise source present in cantilever-enhanced PA arrangements. Lowering the pressure reduces the influence of the acoustic noise but also tends to decrease the signal amplitude. At low pressures, the limiting noise source is thermal noise. Compared to acoustic and thermal noise sources, the electric noise of the system is vanishingly small [36].

## 6 Conclusion

In conclusion, the compact and commercially available cantilever-enhanced photoacoustic unit PA201 from Gasera

was used for sensitive H<sub>2</sub>S detection. A 20-mW DFB laser emitting near 1601 nm was used as the excitation source. Our results show that 8 ppmv H<sub>2</sub>S levels can be detected with this method when employing amplitude modulation with a chopping frequency of 20 Hz.

As compared to simulated spectra, the cantilever-enhanced photoacoustic detection approach in combination with the sufficiently stable and narrow bandwidth NIR laser is able to reproduce the rotationally resolved H<sub>2</sub>S spectrum at low pressures of 300 mbar. Slowly scanning over the H<sub>2</sub>S peak of interest and recording the *n*th harmonic component of the Fourier-transformed interferometer signal yielded in the *n*th derivative like H<sub>2</sub>S spectrum.

The sensitivity of the system is expected to improve when employing laser sources in the Mid-IR as quantum cascades (QC) lasers or interband cascade (IC) lasers. Considering the constant improvement regarding the quality and power of IC and QC laser sources, an excess of 50 mW in optical power can be achieved in monomode continuous wave operation. For example, the intrinsic linestrengths of the H<sub>2</sub>S ro-vibrational features in the 2.7- $\mu\text{m}$  ( $\sim 3800\text{ cm}^{-1}$ ) region are up to a factor of 16 higher than compared to the linestrengths in the NIR region. Addressing the 8- $\mu\text{m}$  ( $1300\text{ cm}^{-1}$ ) region, an improvement up to a factor of 11 can be expected.

To facilitate process implementation of the CEPAS sensor system, further modifications to the sampling system might be required. These should focus on a continuous operation and achieving pressure levels of 100 mbar or lower as this could attribute for a pronounced matrix resolution due to spectral narrowing. In the case of complex sample matrices, it would be crucial to balance between improved peak resolution accompanied with an enhanced detection selectivity and decreased signal amplitude when performing measurements at reduced pressure.

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