

# PbF<sub>2</sub>–TeO<sub>2</sub> glasses and glass–ceramics: a study of physical and optical properties

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#### Abstract

Some physical and optical properties of  $xPbF_2 \cdot (100-x)TeO_2$  ( $0 \le x \le 90 \mod \%$ ) glasses and glass-ceramics have been studied. Density increases linearly with increasing PbF<sub>2</sub> content up to 70 mol% PbO, then tends to be constant for  $70 < PbF_2 \le 90 \mod \%$ . The molar volume remains constant in the first region then increases for PbF<sub>2</sub> > 70 mol%. The main factor which controls the molar volume is the change in free volume and packing density. There is a limited increase in conductivity with increasing PbF<sub>2</sub> content then it decreases for PbF<sub>2</sub> ≥ 50 mol%. Pb<sup>2+</sup> ions are the main charge carriers. The band gap  $E_g$  and the linear refractive index *n* change in an opposite manner where  $E_g$  increases with increasing PbF<sub>2</sub> content for PbF<sub>2</sub> ≤ 50 mol%, then it decreases sharply for PbF<sub>2</sub> > 70 mol%. For PbF<sub>2</sub> ≤ 50 mol%, the Urbach energy  $E_U$  decreases then seems to be constant for further additions. Metallization criterion *M* and molar refractivity  $R_m$  change in a similar manner to  $E_g$  and *n*, respectively.

Keywords  $PbF_2 \cdot TeO_2$  glasses and glass-ceramics  $\cdot$  Density  $\cdot$  Energy gap  $\cdot$  Conductivity

## 1 Introduction

Glasses containing oxide-fluoride systems have good optical properties and perfect thermal and chemical stability [1].  $PbF_2$  was able to form stable glasses due to its dual role as a modifier and former [2].  $PbF_2$  glasses can be believed as appropriate candidates for electrochemical applications [3], like power sources, particularly in the scope of solid-state batteries. Besides, they have prospective applications in IR fiber optics and laser windows [4].

The density of  $xPbO_2 \cdot (100-x)TeO_2 (13.6 \le x \le 21.8 \text{ mol}\%)$ and  $xPbF_2 \cdot (100-x)TeO_2 (13.7 \le x \le 26 \text{ mol}\%)$  glasses was measured [5]. It is found that it increases with increasing PbO and PbF<sub>2</sub> content, respectively. Also, the electrical

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conductivity of  $xPbF_2 \cdot (100-x)(PbO:TeO_2)$  ( $0 \le x \le 60 \mod\%$ ) glasses was studied by El Damrawi [6], it is stated that replacing PbO and TeO<sub>2</sub> by PbF<sub>2</sub> decreases the activation energy for conduction and increases the conductivity. The increase in conductivity is due to the increase in both the concentration and mobility of charge carriers. Transport of fluorine ions in those glasses is explained by the random site model.

The UV spectra of  $\text{TeO}_2$ -PbF<sub>2</sub> glasses were measured by Shiqing et al. [7]. It is found that with adding PbF<sub>2</sub> into tellurite glasses, the excitation energy of the absorption band decreases. This is because the polarizability of O<sup>2-</sup> is higher than that of F<sup>-</sup>. In addition, F<sup>-</sup> ions can break oxygens of the network (making them NBOs) and tighten the mobility gap.

In this work, we aim to study the density, electrical conductivity and optical properties of  $xPbF_2 \cdot (100-x)TeO_2$  glasses and glass-ceramics. Also, explore the role of F<sup>-</sup> and Pb<sup>2+</sup> ions in conductivity. This is an extended work of a previous study on the structure of these glasses [8].

# 2 Experimental

As start materials with high purity (99%, Sigma-Aldrich), reagent grades of  $PbF_2$  and  $TeO_2$  were used to prepare the investigated glasses and glass-ceramics. Batches were

melted in silica crucibles for 25 min, at 780–830 °C, depending on their respective compositions. The crucible was swirled repeatedly until the melt became visually homogeneous. Glass disks were obtained at room temperature after the melt was dropped on a steel plate and compressed by another one.

The density (*D*) was determined by applying the standard Archimedes method at room temperature for four samples of each glass. The used immersion liquid was Xylene. Density values are accurate to  $\pm 2\%$ .

The dc conductivity was determined by measuring the resistance in the range of  $10^3-10^{13} \Omega$  for samples with a thickness ranging between 1.5–3 mm. About  $\pm 0.04$  eV and  $\pm 5\%$  are considered as experimental errors for the activation energy and conductivity, respectively.

To determine the optical transition the optical properties were measured by UV–Visible–NIR Spectrophotometer (JASCO model V770) in the range 190–2000 nm through absorption spectra.

## 3 Results and discussion

### 3.1 Density and molar volume

Figure 1 shows the change of density *D* and the molar volume  $(V_m)$  with PbF<sub>2</sub> content. It is clear that *D* increases linearly with increasing PbF<sub>2</sub> content up to 70 mol% then it seems to have steady values with further additions of PbF<sub>2</sub>. The increase in *D* with increasing PbF<sub>2</sub> content may be due to that the molecular mass of PbF<sub>2</sub> (245.1968 g/mol) is larger than that of TeO<sub>2</sub> (159.5988 g/mol). Nevertheless, the constancy of *D* for PbF<sub>2</sub>  $\geq$  70 mol% indicates that the latter assumption is not the sole reason for increasing density. In *x*PbF<sub>2</sub>·(1–*x*)B<sub>2</sub>O<sub>3</sub> glasses where (30  $\leq x \leq$  80), Doweidar et al. [9] mentioned that



Fig.1 Experimental density and molar volume as a function of PbF<sub>2</sub> content. Density and molar volume values are accurate to  $\pm 2$  and  $\pm 1.5\%$ , respectively

the density of the glasses increases with increasing PbF<sub>2</sub> content. Also, the overall density of the structural units formed with addition of PbF<sub>2</sub> in the matrix (Pb<sup>2+</sup><sub>1/2</sub> [TeO<sub>3+1</sub>]<sup>-</sup>, TeO<sub>3/2</sub>F and PbF<sub>2</sub>) [8] is larger than that of TeO<sub>4</sub> ones and this leads to an increase in density. Vogel et al. [5] mentioned that in PbF<sub>2</sub>–TeO<sub>2</sub> glasses, density increases with increasing PbF<sub>2</sub> content.

Figure 1 represents the dependence of molar volume  $(V_m)$  on PbF<sub>2</sub> content. The  $V_m$  can be estimated from the experimental density data and the molecular mass (M) of glass by the following relation.

$$V_{\rm m} = M/D. \tag{1}$$

There is no change in  $V_{\rm m}$  for compositions with  ${\rm PbF}_2 \le 70 \text{ mol}\%$ , then it increases for  ${\rm PbF}_2 > 70 \text{ mol}\%$ . The constancy of  $V_{\rm m}$  for  ${\rm PbF}_2 \le 70 \text{ mol}\%$  points out to the dependence of *D* on the molecular mass. The change of  $V_{\rm m}$  with  ${\rm PbF}_2$  content (Fig. 1) might be correlated with the change in packing density ( $P_{\rm d}$ ) and free volume ( $V_{\rm f}$ ). The free volume ( $V_{\rm f}$ ) can be given as

$$V_{\rm f} = V_{\rm m} - \sum m_{\rm i} V_{\rm i} \tag{2}$$

where  $m_i$  is the number of ions (i) and  $V_i$  is the volume of such ion of type (i) whereas the later can be expressed as

$$V_{\rm i} = (4/3)\pi r_{\rm i}^3 \tag{3}$$

 $r_i$  denotes the radius of ion of type (i) [10] and *i* refers to Te<sup>4+</sup>, O<sup>2-</sup>, Pb<sup>2+</sup> and F<sup>-</sup> ions.  $V_i$  includes the volume of atoms and/or ions inside the unit and its surrounding space in the glass matrix. The packing density of the oxides can be given as [11]

$$P_{\rm d} = \sum m_{\rm i} V_{\rm i} / V_{\rm m} \tag{4}$$

Figure 2 shows the change of free volume and packing density with PbF<sub>2</sub> content. It is obvious from Fig. 2 that  $V_{\rm f}$  has almost constant values for PbF<sub>2</sub>  $\leq$  50 mol% and increases gradually for PbF<sub>2</sub>>50. However,  $P_{\rm d}$  behaves in a different manner at higher concentrations where it decreases gradually for PbF<sub>2</sub>>50 mol%, while constant for PbF<sub>2</sub> $\leq$  50 mol%. The constancy of  $V_{\rm f}$  and  $P_{\rm d}$  in the composition range  $0 \leq$  PbF<sub>2</sub> $\leq$  50 might be the reason for the constancy in  $V_{\rm m}$ . In addition, the volumes of the structural units related to PbF<sub>2</sub> $\geq$  50 mol% the increase in  $V_{\rm f}$  and the decrease in  $P_{\rm d}$  may be responsible for the increase in  $V_{\rm m}$  of the glass and the constancy of density D for PbF<sub>2</sub>> 70 mol%.



**Fig. 2** Dependence of the free volume  $(V_f)$  and packing density  $(P_d)$  on the PbF<sub>2</sub> content.  $V_f$  and  $P_d$  values are accurate to  $\pm 1$  and  $\pm 0.5\%$ , respectively

#### 3.2 Electric conduction

Figure 3 shows the variation of the natural logarithm of the direct current electrical conductivity ( $\log \sigma$ ) with the reciprocal of absolute temperature (1000/T) in PbF<sub>2</sub>–TeO<sub>2</sub> glasses and glass–ceramics. The change of  $\log \sigma$  with 1000/T is linear which reveals that the conduction process is ionic in nature according to Arrhenius equation

$$\sigma = \sigma_0 \exp(-E/kT). \tag{5}$$

Here  $\sigma_0$  is a constant. *T*, *k* and *E* are absolute temperature, activation energy for the conduction process and Boltzmann's constant, respectively.

Figure 4 shows the change of  $\log \sigma_{473} \sigma \log$  conductivity at 473 K) and *E* with PbF<sub>2</sub> content. There are two regions



Fig.3 Electric conductivity–temperature dependence of  $PbF_2\text{-}TeO_2$  glasses and glass–ceramics



Fig. 4 The electric conductivity's natural logarithm at 473 K and the activation energy as a function of  $PbF_2$  content

in the change of  $\log \sigma_{473}$  and *E*. The first region is for  $PbF_2 \leq 50 \mod \%$  where the conductivity increases by about 1.3 orders with increasing  $PbF_2$  content. However, in this region *E* decreases linearly with increasing  $PbF_2$  content. The second region is for  $PbF_2 \geq 50$  wherewith increasing  $PbF_2$  content  $\log \sigma_{473}$  decreases steadily up to 90 mol%  $PbF_2$ . In this region, *E* seems to be nearly constant.

The conductivity [12] is given by the following relation

$$s = cq\mu \tag{6}$$

where q, c and  $\mu$  are, respectively, the ionic charge, the concentration of mobile ions and the mobility of charge carrier. It is understood from Eq. (6) that  $\sigma$  depends on c and/or  $\mu$ . El Agammy et al. [8] showed that in the studied glasses  $N_4$ (the fraction of four coordinated tellurium atoms) decreases for  $PbF_2 \leq 30 \mod \%$  and the majority of F<sup>-</sup> ions enters the glass structure as terminal ones to convert TeO<sub>4</sub> units to  $(Pb_{1/2}^{2+}[TeO_{3+1}]^{-}$  and  $TeO_{3/2}F)$  units. A similar behavior of  $N_4$  was shown in NaF–TeO<sub>2</sub> glasses and glass–ceramics [13]. As the increase in conductivity for  $PbF_2 \leq 50 \mod \%$  is only 1.3 orders of magnitude and the electronegativity of F atom (3.98) is greater than that of O atom (3.44), we can infer that the bonding energy of Te-O is smaller than that of Te-F [14], it is presumed that the main charge carriers are  $Pb^{2+}$ ions and the transport of these ions is responsible for the conduction process. Considering that the conductivity depends on c and/or  $\mu$ , where the mobility represents the possibility of ease in movement of the ions under an external electric field. When  $PbF_2$  was modified up to 50 mol%,  $\sigma$ increased by just 1.3 orders. This might be due to the ionic radius of  $Pb^{2+}$  ions (1.19 Å) and the dependence of the free volume on PbF<sub>2</sub> content.

As shown in Fig. 2,  $V_{\rm f}$  is nearly constant up to 50 mol% PbF<sub>2</sub>. In this region, the number of charge carriers increases (Pb<sup>2+</sup> ions) by adding PbF<sub>2</sub>. It is then assumed

that the constancy in  $V_{\rm f}$  might limit the increase in the conductivity. Doweidar et al. [15] found a confined increase in conductivity in  $x \operatorname{CaF}_2 \cdot (100-x) \operatorname{B}_2 \operatorname{O}_3$  glasses. They stated that a decrease in  $V_{\rm f}$  with increasing  $\operatorname{CaF}_2$  content leads to a decrease in the mean mobility. Replacing  $\operatorname{TeO}_2$  by PbF<sub>2</sub> increases the charge carriers and might decrease the activation energy in this region.

In the second region (PbF<sub>2</sub> > 50 mol%), there is a gradual decrease in  $\log \sigma_{473}$  (Fig. 4) and E is nearly constant. For  $PbF_2 > 50$ , it is confirmed by X-ray diffraction and transmission electron microscopy [8] that amorphous and crystalline PbF<sub>2</sub> are the major phases in these glasses and glass-ceramics. Also, SEM [8] shows agglomerates of these phases as clusters of different sizes. Despite the increase of  $V_{\rm f}$  and cfor  $PbF_2 \ge 50 \text{ mol}\%$ , there is a decrease in  $\log_{473}$  and *E* is nearly constant. This may be due to that the majority of PbF<sub>2</sub> that enters the matrix tends to form its own crystalline and amorphous matrix as clusters which are not connected to each other's [8]. Also, the matrix of  $PbF_2$  might be the dominant in the glass in this region. This separation makes the continuous migration of Pb<sup>2+</sup> in continuous pathways of charge carriers more difficult and limits the conductivity. The bonding energy of Te-F bond is~683.7 eV [14] and that of Pb-F is about 684.1 eV [16], which are close to each other's. This leads to the assumption that F<sup>-</sup> ions do not contribute in the conduction process and the association of lead and fluorine ions may hinder the diffusion of the Pb<sup>2+</sup> ions which might limit the conductivity.

#### 3.3 Optical properties

### 3.3.1 Optical absorption spectra, optical band gap and refractive index

The optical absorption spectra of  $xPbF_2 \cdot (100-x)TeO_2$  glasses and glass–ceramics ( $10 \le x \le 90 \text{ mol}\%$ ) plotted as a function of the wavelength in the range of 190–2000 nm as shown in Fig. 5. The fundamental absorption peak is centered at ~ 280 nm and then with increasing PbF<sub>2</sub> content, especially for PbF<sub>2</sub> > 70 mol%, it shifts to higher wavelengths. The optical absorbance *A* is related to the absorption coefficient  $\alpha$  through the equation [17],

$$\alpha(\text{cm})^{-1} = 2.303(A/d) \tag{7}$$

where d is the sample thickness. In Davis and Mott equation [18],

$$(\alpha hv)^{1/m} = B(hv - E_g) \tag{8}$$

where *B* is a constant, *m* is an indicator that locates the optical transition type, *h*,  $E_g$  and *v* are Planck's constant, optical band gap and photon's frequency. The optical transition type must take the following values m = 1/2 and 2 for direct



Fig. 5 Absorption spectra of PbF<sub>2</sub>-TeO<sub>2</sub> glasses and glass-ceramics



Fig. 6 Plots of  $(\alpha hv)^{1/2}$  versus hv for PbF<sub>2</sub>-TeO<sub>2</sub> glasses and glass-ceramics

and indirect transition, respectively. Moreover, it is stated by many others [19–23] that indirect allowed transitions (m=2) are valid for oxide glasses.

Depending on that, Tauc plots were used to estimate the optical band gap. Figure 6 represents Tauc plots for the



**Fig. 7** Determination of the optical band gap  $E_g$  for indirect transition for the sample (PbF<sub>2</sub>=50 mol%)



Fig.8 Dependence of the linear refractive index n and band gap  $E_{\rm g}$  on PbF<sub>2</sub> content

variation of  $(\alpha hv)^{1/2}$  versus (hv). Figure 7 shows the method of estimating  $E_g$  [24–26]. Figure 8 shows the variation of the band gap on the content of PbF<sub>2</sub>. There are three regions for the variation. The first is for PbF<sub>2</sub>  $\leq$  50 mol% where  $E_g$ increases with increasing PbF<sub>2</sub> content. The second is for

 $50 \le PbF_2 \le 70 \mod \%$  where  $E_{g}$  is nearly constant. The last is for PbF<sub>2</sub> > 70 mol% where  $E_{g}$  decreases sharply then becomes constant. In the first region,  $E_g$  value varies from 2.7 to 3.03 eV. Previously, El Agammy et al. [8] deduced that in the studied glasses, PbF<sub>2</sub> completely modifies the structure for  $PbF_2 \le 10 \text{ mol}\%$  and plays the dual role (former and modifier) for  $PbF_2 > 10 \text{ mol}\%$ . In addition, the modifier  $PbF_2$  converts TeO<sub>4</sub> units to  $Pb_{1/2}^{2+}$  [TeO<sub>3+1</sub>]<sup>-</sup> and TeO<sub>3/2</sub>F units, while former  $PbF_2$  builds its own matrix. The increase of  $E_g$  in the first region might be due to that the rate of increase in  $C_{Pb(f)}$  (former part of PbF<sub>2</sub> (mol%)) is high [8], in contrary  $C_{Pb(m)}$  (modifier part of PbF<sub>2</sub> (mol%)) seems to decrease with low rate through this region. When  $C_{Pb(m)}$  increases it is expected that the concentration of NBO bonds increases in the matrix [8]. In this case, the increase in  $C_{Pb(f)}$  and decrease in  $C_{Pb(m)}$  might decrease the rate of forming NBO, and as a result  $E_{o}$  increases [23, 27, 28]. The constancy and the decrease in the second and last regions might be due to that the PbF<sub>2</sub> matrix becomes the dominant one, rather than the TeO<sub>2</sub> matrix. In addition, the sudden decrease that occurred for  $PbF_2 > 70 \text{ mol}\%$  might be due to the formation of more ordered structure and the noticed existence of  $PbF_2$  crystalline phases in this region [8]. Also, the main matrix seems to be mainly saturated with PbF<sub>2</sub>. In addition, Fig. 2 shows that  $V_{\rm f}$  has almost constant values for  $PbF_2 \leq 50 \text{ mol}\%$  and increases gradually for further additions of PbF<sub>2</sub>. However,  $P_d$  behaves in a different manner at higher concentrations. The increase in  $V_{\rm f}$  and decrease in  $P_{\rm d}$  for  $PbF_2 > 50 \mod \%$  may be responsible for increasing the molar volume of the glass and decreasing  $E_{\sigma}$  in this range.

Table 1 presents the values of the band gap, linear refractive index, molar volume, molar refractivity, metallization criterion and Urbach energy. Figure 8 shows the variation of the linear refractive index n on PbF<sub>2</sub> content. The refractive index n for glasses has been correlated to the band gap as follows [29],

$$\frac{n^2 - 1}{n^2 + 2} = 1 - \sqrt{\frac{E_g}{20}} \tag{9}$$

where the value 20 in this relation has dimension eV according to Duffy [30]. There are three regions for the variation of

**Table 1** Optical band gap  $E_{\rm g}$ ,linear refractive index n, molarvolume  $V_{\rm m}$ , molar refractivity $R_{\rm m}$ , metallization criterion Mand Urbach energy  $E_{\rm U}$ 

x (mol%)	$E_{\rm g}({\rm eV})$	n	$V_{\rm m}({\rm cm}^3)$	$R_{\rm m}~({\rm cm}^3)$	М	$E_{\rm U} ({\rm eV})$
10	2.71	2.48	27.61	17.44	0.368	0.54
20	2.80	2.45	27.67	17.32	0.374	0.47
30	2.86	2.44	27.52	17.11	0.378	0.47
40	2.95	2.41	27.36	16.85	0.384	0.36
50	3.03	2.39	27.61	16.87	0.389	0.34
60	3.00	2.40	27.87	17.08	0.387	0.32
70	2.99	2.40	27.91	17.11	0.387	0.36
80	2.30	2.62	28.95	19.13	0.339	0.33
90	2.29	2.62	30.07	19.90	0.338	0.35

*n* with PbF<sub>2</sub> content. The first is for PbF<sub>2</sub>  $\leq$  50 mol%. In this region, *n* decreases with increasing the content of PbF<sub>2</sub>. The second is for  $50 \leq$  PbF<sub>2</sub>  $\leq$  70 mol% where *n* is constant. The last one is that for PbF<sub>2</sub> > 70 mol% where *n* increases with increasing PbF<sub>2</sub> content. The *n* value varies from 2.39 to 2.62. These variations are due to the same structural changes that affect the variation of *E*<sub>g</sub>. Further, because energy gap is inversely proportional to refractive index according to Eq. (9), the structural changes and the variation of both *C*<sub>Pb(f)</sub> and *C*<sub>Pb(m)</sub> with PbF<sub>2</sub> [8] are responsible for the change of *n*. It is assumed that in the first region, the increase and decrease of *C*<sub>Pb(f)</sub> and *C*<sub>Pb(m)</sub>, respectively, limit the NBO formation and hence *n* decreases.

#### 3.3.2 Molar refractivity and metallization criterion

The molar refraction  $(R_m)$  of the studied glasses and glass-ceramics was estimated using the Lorentz-Lorentz equation,

$$R_{\rm m} = \left(\frac{n^2 - 1}{n^2 + 2}\right) V_{\rm m} \tag{10}$$

Figure 9 shows that the molar refraction is nearly constant for  $PbF_2 \le 70 \text{ mol}\%$  and then increases from 17.11 to 19.9 cm<sup>3</sup> for further additions from  $PbF_2$ . This behavior is similar to that of the molar volume and the refractive index with  $PbF_2$  content as shown in Figs. 1 and 8, respectively. This behavior is due to the dependence of the molar refraction on the refractive index and molar volume.

The following equation is used to estimate the metallization criterion (M) for PbF<sub>2</sub>-TeO<sub>2</sub> glasses and glass-ceramics [29],

$$M = 1 - \frac{R_{\rm m}}{V_{\rm m}} \tag{11}$$



Fig. 9 Dependence of metallization criterion M and molar refractivity  $R_{\rm m}$  on PbF<sub>2</sub> content

*M* anticipates the way of behaving of glass materials to metallization or insulation depending on the values of  $R_{\rm m}$  and  $V_{\rm m}$  [31]. Values of *M* change between 0.338 and 0.389 (Table 1), whereas Fig. 9 shows that *M* increases gradually for PbF<sub>2</sub>  $\leq$  70 mol% and then decreases suddenly for further additions of PbF<sub>2</sub>. This behavior is similar to that of  $E_{\rm g}$  (Fig. 8). These trends reveal that the glass material is closer to metallization behavior than insulation for PbF<sub>2</sub> $\leq$  70 mol%. On contrary, for PbF<sub>2</sub>> 70 mol% the insulating behavior is the dominant one. These results are consistent with the electrical conductivity results as shown in Fig. 3 where  $\log \sigma_{473}$  increases with increasing PbF<sub>2</sub> content for PbF<sub>2</sub> $\leq$  50 mol% then decreases steadily up to 90 mol% PbF<sub>2</sub>.

#### 3.3.3 Urbach energy

Urbach energy  $E_{\rm U}$  characterizes the range of the exponential tail of the absorption edge. The relation between Urbach energy and the absorption tails is given by,

$$\alpha(v) = \alpha_{\rm o} \exp\left(hv/E_{\rm U}\right) \tag{12}$$

where  $E_{\rm U}$  is the Urbach energy and  $\alpha_{\rm o}$  is a constant. Figure 10 shows plots for  $\ln(\alpha)$  against photon energy, E = hv, for determination of the Urbach energy  $E_{\rm U}$ . Figure 11 represents an example for estimating  $E_{\rm U}$  [32].

Figure 12 shows the change of  $E_U$  with PbF<sub>2</sub> content. The values of  $E_U$  lie between 0.32 and 0.54 eV which are in the range of amorphous semiconductors [27, 33].  $E_U$  decreases with increasing PbF<sub>2</sub> up to 50 mol% and seems to be constant for higher PbF<sub>2</sub> contents. This variation might be due to the formation of crystalline phases such as Te<sub>2</sub>O<sub>3</sub>F<sub>2</sub> and PbF<sub>2</sub> [8] which reinforces the possibility of formation of a matrix with a long-range order. This order in the glass



**Fig. 10** Logarithm of the absorption coefficient,  $\ln(\alpha)$ , against photon energy, hv



**Fig. 11** Logarithm of the absorption coefficient,  $\ln(\alpha)$ , against photon energy, *hv* for the sample (PbF<sub>2</sub>=80 mol%)



Fig. 12 Variation of the Urbach energy  $E_{\rm U}$  with PbF<sub>2</sub> content in

contributes to a reduction of  $E_{\rm U}$ . Analogous behavior of  $E_{\rm U}$  was noticed with TiO<sub>2</sub> [27].

## 4 Conclusion

In PbF<sub>2</sub>–TeO<sub>2</sub> glasses and glass–ceramics, *D* increases due to that the molecular mass of PbF<sub>2</sub> is larger than that of TeO<sub>2</sub>. The change in V<sub>f</sub> and P<sub>d</sub> is responsible for the change in V<sub>m</sub>. It is considered that Pb<sup>2+</sup> ions are the main charge carriers. For PbF<sub>2</sub>≤50, the constancy of V<sub>f</sub> causes a limited increase in conductivity. Whereas, for PbF<sub>2</sub>>50 mol% the conductivity decreases because PbF<sub>2</sub> tends to form its own crystalline and amorphous matrix in the form of clusters.  $E_g$ increases with increasing PbF<sub>2</sub> content for PbF<sub>2</sub>≤50 mol%, then it decreases sharply then becomes constant for PbF<sub>2</sub>>70 mol%. *n* changes in an opposite manner to that of  $E_g$ .  $E_U$  decreases with increasing PbF<sub>2</sub> up to 50 mol%. Then for further additions of  $PbF_2$ , it is nearly constant. These trends might be related to the structural variations that take place with modifying the network by  $PbF_2$ .

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