# Thickness-dependence of optical constants for Ta<sub>2</sub>O<sub>5</sub> ultrathin films

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Abstract An effective method for determining the optical constants of  $Ta_2O_5$  thin films deposited on crystal silicon (c-Si) using spectroscopic ellipsometry (SE) measurement with a two-film model (ambient–oxide–interlayer–substrate) was presented.  $Ta_2O_5$  thin films with thickness range of 1–400 nm have been prepared by the electron beam evaporation (EBE) method. We find that the refractive indices of  $Ta_2O_5$  ultrathin films less than 40 nm drop with the decreasing thickness, while the other ones are close to those of bulk  $Ta_2O_5$ . This phenomenon was due to the existence of an interfacial oxide region and the surface roughness of the film, which was confirmed by the measurement of atomic force microscopy (AFM). Optical properties of ultrathin film varying with the thickness are useful for the design and manufacture of nano-scaled thin-film devices.

## 1 Introduction

Recently, nanotechnology has advanced rapidly, and it is revolutionizing the microelectronic and optoelectronic applications. As traditional semiconductor technology encounters numerous scaling and economic challenges, smaller but more efficient devices with ultra thin films at the nanometer scale are created for information storage, processing, and display [1–3]. However, the optical properties and dielectric

Key Laboratory of Micro and Nano Photonic Structures, Ministry of Education, Department of Optical Science and Engineering, Fudan University, 200433 Shanghai, China e-mail: yxzheng@fudan.edu.cn properties of thin films at nanometer scale are different from the bulk one's due to the effect of surface and interface [4]. In order to get high performance of nano-scaled device, it is important to find how the optical properties of ultrathin films change with size shrinking. Up to date, this kind of study is not yet sufficient.

Owing to its large dielectric constant (high-k), high refractive index and good environment stability, tantalum pentoxide (Ta<sub>2</sub>O<sub>5</sub>) films have attracted great attention in both semiconductor sciences and optical sciences, and have found many applications such as antireflective layers [5], narrow-band interference filters [6], storage capacitors [7], gate dielectric [8], etc. Because of this wide field of applications, Ta<sub>2</sub>O<sub>5</sub> films have been extensively studied both experimentally and theoretically. For device applications in microelectronics, ultrathin film with high dielectric constant can replace SiO<sub>2</sub> as ultra-large-scale-integrated gate dielectric for its property equivalent to the one of a thinner SiO<sub>2</sub> film [9, 10]. On the other hand, the dielectric constant of ultrathin film is dependent on the thickness [11]. Several researches indicate that the dielectric constants and refractive indices of Ta<sub>2</sub>O<sub>5</sub> ultrathin films deposited on silicon drop because of the SiO<sub>2</sub> layer at the Ta<sub>2</sub>O<sub>5</sub>/Si-substrate interface [5, 12]. However, some other results show that the interfacial region is not pure SiO<sub>2</sub>, but a complex depthdependent ternary oxide of Si–Ta<sub>x</sub>– $O_y$  [13]. Therefore, it is worth further studying on this topic of clarifying the optical properties of Ta<sub>2</sub>O<sub>5</sub> ultrathin films. Generally speaking, a sufficient understanding of the optical properties of diverse ultrathin films, including Ta<sub>2</sub>O<sub>5</sub> ultrathin films, is very important for the development of related devices, and should be of wide interest in the field of nanotechnology.

Ellipsometry is now one of the popular tools for the characterization of ultrathin films for it can provide useful information about nanostructures [14, 15]. In this paper, we pre-

D.-X. Zhang · Y.-X. Zheng ( $\boxtimes$ ) · Q.-Y. Cai · W. Lin · K.-N. Wu · P.-H. Mao · R.-J. Zhang · H.-b. Zhao · L.-Y. Chen

sented an effective method to get the optical constants of the transparent  $Ta_2O_5$  thin films deposited on silicon using spectroscopic ellipsometry (SE), and the surface morphology of  $Ta_2O_5$  thin films was studied by atomic force microscopy (AFM).

### 2 Experimental details

The Ta<sub>2</sub>O<sub>5</sub> films with thickness range of 1-400 nm were deposited by electron beam evaporation (EBE) method at the same deposition conditions. Crystalline (100) n-type silicon with diameter of 2 inch, thickness of  $(350 \pm 20)$  µm and resistivity of 2–8  $\Omega$  cm, which was cleaned in an HF solution and de-ionized water to remove any native oxide material, was used as substrate. Over 30 samples have been prepared at the deposition rate of 0.2-0.4 nm/s. During deposition, the broadband optical monitoring (BOM) method was used to adjust the optical thickness and the deposition rate [16]. All the samples were characterized by a rotating-polarizeranalyzer ellipsometer (RPAE) [17, 18]. Ellipsometric parameters  $(\Delta, \Psi)$  of each film were acquired over the wavelength range of 300-820 nm with an interval of 10 nm at three different incident angles of 65°, 70°, and 75°, respectively. To attain high accuracy, each ellipsometric parameter  $(\Delta, \Psi)$  was acquired with a total of 40 000 sets of raw data using the RPAE with the accuracy of  $\Delta$  reaching 0.005° and the accuracy of  $\Psi$  reaching 0.01°. A simple two-film model was used to determine the optical constants and thickness of the investigated films, which was found to show good agreement between the calculated curves and the experimental data obtained from ellipsometric measurement [19–21].

#### 3 Results and discussions

In order to get the optical constants and physical thickness of  $Ta_2O_5$  films, an analytical model should be chosen to fit the ellipsometry parameters both physically meaningful and best fit. In our work, a two-film model which is suited to calculate the optical constants of dielectric films deposited on silicon was adopted to fit the ellipsometry parameters [4]. For  $Ta_2O_5$  was transparent dielectric material in the spectral range of 300–820 nm, the Sellmeier dispersion model was used to express the layer of  $Ta_2O_5$ , and it was given by [22, 23]

$$n^2 = 1 + \frac{B_n \lambda^2}{\lambda^2 - C_n^2} \tag{1}$$

where  $B_n$  is proportional to the density of effective electron states,  $C_n$  represents a wavelength parameter corresponding to the effective electron energy level. However, only a sample ambient/oxide/substrate model could not fit the measured data well, especially in long wavelength band where the fitting error for the data becomes noticeably large for the ultrathin-film samples. So an interlayer with silicon-induced gap states (SIGS) was introduced between oxide layer and substrate, which expressed the breaking down of the Si–Si bond of the Si substrate [24]. According to Refs. [24, 25], the decay of the interface states was limited to about 0.12 nm close to the interface. Therefore, the thickness of the SIGS layer was assumed to be 0.12 nm. A Lorentz oscillator dispersion model was used to express the SIGS layer, and it is given by [26, 27]

$$\varepsilon = 1 + \frac{A^2}{E_{\text{center}}^2 - E(E - i\Gamma)}$$
(2)

where  $\varepsilon$  is the dielectric function, A is the amplitude of the oscillator,  $E_{center}$  is the resonant energy, E is the photon energy, and  $\Gamma$  is the damping factor of the oscillator. In this model,  $E_{center}$  is assumed to be close to the energy gap of silicon, i.e.,  $E_{\text{center}} = 1.12 \text{ eV}$ , and  $\Gamma$  is set to zero. Considering the two-film model, the calculated curve of  $\tan \Psi$ and  $\cos \Delta$  can fit the measured data well. Furthermore, the effective electron energy level of Ta<sub>2</sub>O<sub>5</sub> films was assumed the same. After numerous fitting processes with samples of different oxide thickness,  $C_n$  could be determined. The bestfit results show that  $C_n$  has the value of 186 nm. Therefore, here are only three parameters unknown in this model,  $B_n$ , A, and the oxide thickness d of  $Ta_2O_5$  films. By fitting the measured data using this two-film model with the minimum root mean squared error (RMSE), these unknown parameters could be finally determined for each Ta<sub>2</sub>O<sub>5</sub> thin films. The results are shown in Fig. 1. Apparently, the calculated curves are in good agreement with the measured ones, which means that the two-film model used in the above fitting process is reasonable and acceptable.

With this fitting process, parameter  $B_n$  could be given by a function of the oxide thickness:

$$B_n = A_0 e^{-d_0/d} (3)$$

where  $A_0 = 3.19 \pm 0.03$ ,  $d_0 = 1.94 \pm 0.12$ . Therefore, an empirical dispersion formula for the ultrathin Ta<sub>2</sub>O<sub>5</sub> film was obtained by substituting (3) into (1), and was given by

$$n^{2} = 1 + 3.19 \exp(-1.94/d) \cdot \frac{\lambda^{2}}{\lambda^{2} - 186^{2}}$$
(4)

Figure 2 shows the refractive index of the  $Ta_2O_5$  thin films at wavelength of 550 nm with different thickness. In Fig. 2, the refractive index reduced sharply with decreasing thickness less than 40 nm, and the other ones remained constant when thickness was greater than 40 nm. The similar phenomenon is also observed at other wavelengths.

**Fig. 1** Experimental (*symbol*) and fitted (*line*) VASE data tan  $\Psi$  and cos  $\Delta$  for Ta<sub>2</sub>O<sub>5</sub> film in the spectral range of 300–820 nm at three incident angles (65°, 70°, 75°) with thickness of (**a**) ~10 nm and (**b**) ~75 nm





Fig. 2 Experimental and theoretical refractive indices at 550 nm for the  $Ta_2O_5$  films deposited on Si with different thicknesses

A simple inverse proportional function can be used to express the variation trend, which is given by

$$n = 2.15 - \frac{B}{d} \tag{5}$$

where *n*, *d* represent the refractive index and physical thickness of the Ta<sub>2</sub>O<sub>5</sub> thin films, respectively,  $B = 1.52 \pm 0.06$ .

To explain this phenomenon, a roughness layer and an interfacial oxide region were introduced into the structure of the film system. The global dielectric constant of the roughness/Ta<sub>2</sub>O<sub>5</sub>/interfacial oxide system can be evaluated by using a simple model which supposes that the three dielectric layers are represented by three capacitors in series

with the dielectric constants of three layers, respectively [5, 28]. The effective dielectric constant of the sandwich ( $\varepsilon_{eff}$ ) is then given by the following equation:

$$\frac{d}{\varepsilon_{\rm eff}} = \frac{d_{\rm roughness}}{\varepsilon_{\rm roughness}} + \frac{d_{\rm Ta_2O_5}}{\varepsilon_{\rm Ta_2O_5}} + \frac{d_{\rm oxide}}{\varepsilon_{\rm oxide}}$$
(6)

where d,  $d_{\text{roughness}}$ ,  $d_{\text{Ta}_2\text{O}_5}$ , and  $d_{\text{oxide}}$  are the physical thickness of the thin film, the roughness layer, the Ta<sub>2</sub>O<sub>5</sub> layer, and the interfacial oxide layer, respectively, while  $\varepsilon_{\text{eff}}$ ,  $\varepsilon_{\text{roughness}}$ ,  $\varepsilon_{\text{Ta}_2\text{O}_5}$ , and  $\varepsilon_{\text{oxide}}$  are the dielectric constants of the thin film, the roughness layer, the Ta<sub>2</sub>O<sub>5</sub> layer, and the interfacial oxide layer, respectively. Apparently, there is the relation

$$d = d_{\rm roughness} + d_{\rm Ta_2O_5} + d_{\rm oxide} \tag{7}$$

By substituting (7) into (6), it gives

$$\varepsilon_{\text{eff}} = \frac{\varepsilon_{\text{Ta}_2\text{O}_5}}{1 + \frac{1}{d} [(\frac{\varepsilon_{\text{Ta}_2\text{O}_5}}{\varepsilon_{\text{roughness}}} - 1) \cdot d_{\text{roughness}} + (\frac{\varepsilon_{\text{Ta}_2\text{O}_5}}{\varepsilon_{\text{oxide}}} - 1) \cdot d_{\text{oxide}}]}$$
$$= \frac{\varepsilon_{\text{Ta}_2\text{O}_5}}{1 + \frac{C}{d}} \tag{8}$$

where C is given by

$$C = \left(\frac{\varepsilon_{\text{Ta}_2\text{O}_5}}{\varepsilon_{\text{roughness}}} - 1\right) \cdot d_{\text{roughness}} + \left(\frac{\varepsilon_{\text{Ta}_2\text{O}_5}}{\varepsilon_{\text{oxide}}} - 1\right) \cdot d_{\text{oxide}}$$
(9)

The relation between the refractive index and the dielectric constant is given by the following equation, which is suitable for transparent material in the visible light region:

$$n = \sqrt{\varepsilon} \tag{10}$$

Fig. 3 AFM results with 2D and 3D images for  $Ta_2O_5$  films with thickness of (a) ~10 nm and (b) ~75 nm



From (8) to (10), by using Taylor expansion, we get

$$n_{\text{eff}} = \sqrt{\varepsilon_{\text{eff}}} = \sqrt{\varepsilon_{\text{Ta}_2\text{O}_5}} \cdot \left(\frac{1}{1+\frac{C}{d}}\right)^{1/2}$$
$$\approx \sqrt{\varepsilon_{\text{Ta}_2\text{O}_5}} \cdot \left(1 - \frac{1}{2} \cdot \frac{C}{d}\right)$$
$$= n_{\text{Ta}_2\text{O}_5} - \frac{n_{\text{Ta}_2\text{O}_5}}{2} \cdot \frac{C}{d} \approx 2.15 - \frac{C}{d}$$
(11)

While the refractive index of Ta<sub>2</sub>O<sub>5</sub> ( $n_{Ta_2O_5}$ ) has a value of 2.15 at wavelength of 550 nm. Finally we find that the equation has the same form as is used to express the trend of the refractive index versus thickness. Furthermore the parameter *C* can be acquired from (9). Here, we have assumed that *C* is a constant parameter in this approximate model for simplicity. The interfacial oxide layer is not pure SiO<sub>2</sub>, but is a complex depth-dependent ternary oxide of Si–Ta<sub>x</sub>–O<sub>y</sub>. Assuming the interfacial oxide layer mainly comes from contribution with oxidizing of the substrate, the refractive index and thickness can be determined by ellipsometry before deposition. The result showed the that the dielectric constant is 6.76, and the thickness is 2 nm, which accords with

[5, 13]. So the values of the interfacial oxide layer acquired from ellipsometry are appropriate. The dielectric constant of roughness layer is given by effective medium approximation (EMA) model. It can be described as a mixture of  $Ta_2O_5$  and air, with the following equation [29]:

$$\frac{\varepsilon_{\text{roughness}} - 1}{\varepsilon_{\text{roughness}} + 2} = f \cdot \frac{\varepsilon_{\text{Ta}_2\text{O}_5} - 1}{\varepsilon_{\text{Ta}_2\text{O}_5} + 2}$$
(12)

where *f* is the volume fraction of Ta<sub>2</sub>O<sub>5</sub>, and the dielectric constant of air is assumed having the value of 1. Assuming the thickness of roughness layer is 5 nm, and *f* is 0.75, from (12), we find that the dielectric constant  $\varepsilon_{roughness}$  is 3.09. According to (9) and (10), finally we estimate the value of *C* is 1.85, which approximates the experimental parameter *B*, which has a value of 1.52. This estimation has been confirmed by subsequent surface topography measurement on samples with thickness of 10 nm and 75 nm, respectively. The surface topography measurement was performed by AFM using non-contact head mode. The AFM images are shown in Fig. 3. According to former results, the Ta<sub>2</sub>O<sub>5</sub> thin-film of 10 nm has a minor refractive index, but the refractive index of 75 nm-thick Ta<sub>2</sub>O<sub>5</sub> film is close to those

of bulk  $Ta_2O_5$ . However, from the AFM images, the formations of  $Ta_2O_5$  films are both considered accumulating like "islands", with the thickness difference between peaks and valleys less than 5 nm.

#### 4 Conclusion

In summary, a series of Ta<sub>2</sub>O<sub>5</sub> films deposited on Si substrate have been prepared by EBE method. The optical properties of the samples were obtained from SE measurement, and found to vary for the ultrathin films. The refractive indices of Ta<sub>2</sub>O<sub>5</sub> films with thickness less than 40 nm reduce with the decreasing thickness, and those with thickness greater than 40 nm are close to the value of bulk Ta<sub>2</sub>O<sub>5</sub>. This phenomenon was attributed to the contribution of the interfacial oxide region and the roughness layer, and the AFM results confirmed this viewpoint. For detailed consideration in designing thin-film devices, the surface or interface effect must be considered in order to get high performance of devices, therefore, an ultrathin film for application cannot be considered as a single uniform layer but one usual layer together with two interface layers. The results are useful for the design and fabrication of optical thin-film devices, as well as microelectronic devices.

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