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Theoretical study of the local charge compensation and spectroscopic properties of B-type carbonate defects in apatite

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Abstract The structure and spectroscopic properties of selected models of B-type carbonate defects in apatite locally compensated by fluoride or hydroxyl ions are investigated using first-principles quantum mechanical calculations. Theoretical infrared absorption spectra and ¹³C, and ¹⁹F nuclear magnetic resonance chemical shifts are determined. Among the investigated models, only the clumped (CO_3^{2-}, F^-) defect, with the carbonate group close to the sloping face of the tetrahedral site and the F⁻ ion at the remaining apex, corresponds to previous experimental observations performed on carbonate-fluorapatite samples. Although the substitution of hydroxyl by fluoride ions is commonly observed in minerals, the clumped (CO_3^{2-}) , OH⁻) defects are unlikely to occur in apatite, considering both their theoretical spectroscopic properties and relative stability. Anionic F⁻ for OH⁻ exchange between channel and B sites displays a preference of ~20 kJ/mol for the local charge compensation by fluoride ions at the B-site, pointing to a significantly different behavior of F⁻ and OH⁻ ions

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in the charge compensation mechanism. This difference is ascribed to the poor H-bond acceptor character of available oxygen atoms surrounding the apex of the tetrahedral site. The explicit calculation of the infrared absorption spectra of the defect models is also used to interpret the significant difference observed in the linewidth of the v_2 and v_3 CO₃ infrared powder absorption bands of carbonated apatite samples. It is shown that for a concentration of 4.4 wt% of CO₂, long-range electrostatic effects already significantly contribute to the broadening of the v_3 CO₃ bands in apatite.

Keywords Apatite \cdot Carbonate substitution \cdot First-principles \cdot DFT \cdot FTIR \cdot NMR

Introduction

Apatite is a ubiquitous accessory phase in igneous, metamorphic and sedimentary rocks. It is the major constituent

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L. Ségalen CNRS, UMR 7193, ISTEP, 75005 Paris, France of some carbonatite and anorthosite (Knudsen and Gunter 2002). Sedimentary apatite deposits, referred to as phosphorites, are the main natural resources in phosphorus (McConnell 1973; Dymek and Owens 2001). Apatite also occurs as the principal inorganic component of bones and dental enamel of vertebrates (Elliott 2002). This motivates active researches for biomedical applications, whereas other technological applications include the storage of radioactive wastes and the production of fertilizers, detergents and phosphoric acid (McConnell 1973; Hughes and Rakovan 2002).

The flexibility of apatite structure enables significant variations of its chemical composition. Anionic substitutions lead to modifications of the chemical occupation of channel sites (F, OH and Cl) and to the incorporation of significant amounts of carbonate in geological and biological samples (Elliott 1994, 2002). The carbonate ion can substitute in the phosphate tetrahedral site (B-type carbonate defect) or in the structural channels centered on the hexagonal symmetry axis (A-type carbonate defect). Depending on the formation conditions of apatite, FTIR and NMR spectroscopic investigations (e.g., Regnier et al. 1994; Michel et al. 1995; Tacker 2008; Mason et al. 2008, 2009; Fleet 2009) reveal the occurrence of these various modes of carbonate incorporation. Inferences from spectroscopic observations are also supported by structure refinements using X-ray or neutron diffraction (e.g., LeGeros 1965; Schuffert 1990; Leventouri et al. 2000; Wilson et al. 1999, 2004, 2006) although the small grain size and twinning of low-temperature apatite samples appear as limiting factors. More recently, single-crystal structure refinements performed on high-quality apatite crystals synthesized under high-pressure conditions shed light on the structural environment and incorporation mechanisms of carbonate groups in apatite (Fleet and Liu 2004, 2007, 2008; Fleet 2009; Fleet et al. 2011).

The carbonate for phosphate substitution in the apatite structure requires adding a negative charge to maintain the local electrostatic balance. A number of potential charge-compensating mechanisms have been suggested, corresponding to various subtypes of B-type carbonate defects (e.g., Ivanova et al. 2001; Wilson et al. 2004; Nokhrin et al. 2006; Antonakos et al. 2007).

In low-temperature carbonated fluorapatite samples ("francolite"), the observation of excess fluorine ions has led to the proposal that the carbon for phosphorus substitution is coupled to a fluorine for oxygen substitution (e.g., McClellan and Lehr 1969). Local charge compensation of carbonates by F^- or OH^- ions, resulting in the formal species $(CO_3OH)^{3-}$ and $(CO_3F)^{3-}$, has been considered early because F^- and OH^- ions naturally occur in the apatite structure (e.g., Elliott 1964; McClellan and Lehr 1969; Vignoles et al. 1988; Binder and Troll 1989). However, the

local character of the charge compensation has been further questioned by several theoretical and experimental studies (e.g., Regnier et al. 1994, 1996; Pan and Fleet 2002; Mason et al. 2009). The existence of a clumped (CO_3^{2-}, F^-) defect in natural carbonated fluorapatite ("francolite" type carbonate) has been recently confirmed by direct spectroscopic observations and theoretical modeling (Yi et al. 2013).

In comparison, carbonate incorporation at the B-site of F-free hydroxyapatite seems to systematically involve more complex mechanisms. For example, Rietveld refinement of X-ray diffraction patterns of synthetic or biologic carbonate-bearing apatite samples has suggested that Ca vacancies may compensate the charge imbalance, although the position of the vacancies with respect to the carbonate group remains uncertain (e.g., Wilson et al. 1999, 2006; Ivanova et al. 2001). Pasteris et al. (2012) observed a correlation between incorporation of carbonate at B-site and depletion of channel OH groups. A coupled substitution involving parallel replacement of Na⁺ for Ca²⁺ was also proposed on the basis of compositional data from natural carbonate-bearing apatites (McConnell 1952; Ames 1959) and has been confirmed by the synthesis of Na and carbonate-bearing apatites (e.g., Bonel et al. 1973; Fleet and Liu 2008). More specifically, a coupled mechanism involving both A-type carbonate groups and Na for Ca substitution has been proposed from structure determination of A-B apatite single crystals (Fleet 2009). Such mechanism is supported by the observation of characteristic ratios of Na to A and B carbonates. Although the role of A-type carbonate in the charge compensation of B-type carbonate is not intuitively obvious, it is explained by the steric repulsion between the channel carbonate oxygen atom and neighboring phosphate oxygen atom, promoting the formation of an oxygen vacancy at the tetrahedral site (Fleet 2009). In natural samples, other coupled substitutions, e.g., involving a concomitant replacement of SiO_4^{4-} for PO_4^{3-} , have been established on the basis of compositional data from hightemperature carbonate-bearing apatite in igneous rocks (e.g., Sommerauer and Katz-Lehnert 1985; Comodi et al. 1999).

Interestingly, the carbonated fluorapatite samples investigated by Fleet (2009) display a B/A ratio >1 and a spectroscopic signature that could be ascribed to isolated carbonate groups. In comparison, high-pressure synthetic hydroxyapatite samples display a B/A ratio <1. This contrasted behavior is somehow surprising because the fluorine for hydroxyl substitution is commonly observed in minerals and synthetic compounds (e.g., Robert et al. 1999, 2013) and the charge compensation of cationic vacancies by protons is a usual incorporation mechanism of OH groups in nominally anhydrous minerals (e.g., Bell and Rossman 1992; Keppler and Smyth 2006). In addition, simple electrostatic considerations suggest that local electrostatic charge compensation mechanisms are energetically more favorable than more remote mechanisms. Therefore, there is no obvious reason explaining why hydroxyl ions would be less efficient than fluoride ions for the local charge compensation of B-type carbonate groups in apatite.

In the present study, we compare the respective roles of fluoride and hydroxyl ions in the local charge compensation of carbonate at B-site, using a first-principles theoretical modeling approach. Computational simulations can indeed provide important information on the atomic-scale structure of carbonate defects in apatite (e.g., Peeters et al. 1997, Astala and Stott 2005, Rabone and de Leeuw 2007, de Leeuw 2010, Ulian et al. 2013a, b), and the theoretical modeling of spectroscopic properties makes it possible to test atomicscale models of defects in minerals against experimental observations (e.g., Balan et al. 2013). After a detailed presentation of the clumped (CO₃²⁻, F⁻) defect recently recognized in natural fluorapatite samples (Yi et al. 2013), we determine the theoretical structural, nuclear magnetic and vibrational properties of stable models of clumped $(CO_3^{2-},$ F^{-}) and (CO₃²⁻, OH⁻) defects in apatite and we discuss the specificity of OH groups as charge-compensating species. Finally, theoretically determined infrared absorption properties are used to explain the contrasted characters of the v_2 and $v_3 CO_3$ absorption bands observed in the infrared spectrum of many synthetic or natural apatite samples.

Theoretical methods

The stable structure and spectroscopic properties of models of carbonate-substituted apatite were computed within the density functional theory (DFT) framework, using the generalized gradient approximation (GGA) for the exchangecorrelation functional as proposed by Perdew et al. (1996). The structural and vibrational calculations were performed using the PWscf and PHonon codes of the Quantum Espresso package (Giannozzi et al. 2009). The ionic cores of Ca, P, O, F and H were described by ultra-soft pseudopotentials from the Quantum Espresso library (http://www. quantum-espresso.org). The electronic wave functions and charge density were expanded in plane waves using 50 Ry and 500 Ry cutoffs, respectively. Models of carbonate defect were built by incorporating one carbonate group in a fluorapatite primitive cell (42 atoms). The cell parameters were fixed at the theoretical relaxed cell parameters of pure fluorapatite (a = 9.48 Å, c = 6.90 Å; Balan et al. 2011). The sampling of the Brillouin zone for the electronic integration was restricted to a single k-point (-.5, -.87,-.68; in Cartesian coordinates and $2\pi/a$ units). The fixedcell optimization of atomic positions was done until the residual forces were less than 10^{-4} Ry/a.u. The harmonic low-frequency dielectric tensor (Baroni et al. 2001) of the theoretical equilibrium structure was calculated following the procedure described in previous studies (e.g., Balan et al. 2001, 2011).

The NMR chemical shifts were obtained on the same structural model by calculating the shielding of the nuclei relative to the electronic current induced by the external magnetic field. This current was calculated using the GIPAW approach, which allows reconstructing the allelectron magnetic response from the pseudo-wave functions (Pickard and Mauri 2001). The calculations were performed using the PWscf and GIPAW codes of the Quantum Espresso package (Giannozzi et al. 2009). For this calculation, norm-conserving pseudo-potentials were used and the wave functions kinetic energy cut-off was increased to 80 Ry. The integral over the Brillouin zone was done using a Monkhorst-Pack $2 \times 2 \times 2$ k-point grid. The isotropic chemical shift σ_{iso} is defined as $\sigma_{iso} = -(\sigma - \sigma^{ref})$, where σ is the isotropic shielding (one-third of the trace of the NMR shielding tensor) and σ^{ref} is the isotropic shielding of the same nucleus in a reference system. In our calculations, absolute shielding tensors are obtained. To fix the scales, $\sigma^{\rm ref}$ was chosen by comparing experimental and calculated σ^{iso} values in calcite (CaCO₃) for ¹³C and in fluorapatite $(Ca_5(PO_4)_3F)$ for ¹⁹F. It should be noticed that for ¹⁹F, a scaling factor k = 0.68 was applied since previous GIPAW calculations recommended this correction to obtain accurate predictions (Griffin et al. 2010).

Results

Theoretical models of carbonate defects in apatite

The B-type models correspond to the substitution of a CO_3^{2-} group for a PO_4^{3-} group in the apatite structure. The corresponding defects have a positive charge that requires a charge balance mechanism. Models B_H and B_F involve a local charge compensation of the carbonate defect by a monovalent anionic species, OH⁻ and F⁻ ions, respectively. Additional calculations were performed on the A-type carbonate to enable a thorough comparison of its spectroscopic properties with those of the B-type models. The relaxed structure of B- and A-type models is displayed in Figs. 1, 2, 3 and 4, in which the atom labeling follows usual conventions for apatite, whereas oxygen atoms belonging to carbonate groups are labeled following Fleet and Liu (2008). Note that Yi et al. (2013) used an unconventional labeling of atoms, differing from that in the present study.

The model B_F has been briefly described in Yi et al. (2013). Using the fluorapatite primitive cell, the distance between image carbonate groups due to periodic boundary conditions is larger than 6 Å. Calculations of the B_F model using a $2 \times 2 \times 2$ apatite super-cell lead to a nearly identical





Fig. 1 Theoretical model of B-type carbonate locally compensated by a fluoride ion (B_F model) in fluorapatite (O = *red*, F = *green*, P = *light pink*, C = *black*, Ca = *light blue*). *Top*: view along the *c*-axis. *Bottom*: view along the *b*-axis. Selected distances are indicated in Å. The model is identical to that discussed by Yi et al. (2013)

geometry and orientation of the carbonate group, with modifications of interatomic distances smaller than 0.01 Å. This large-cell (336 atoms) calculation confirms that the interaction between the periodic images of the carbonate defect is already weak in the primitive-cell model. Primitive-cell models of neutral carbonate defects with local charge compensation thus provide a realistic picture of these carbonate defects, consistent with the previous findings of Ulian et al. (2013a). It should be also noted that the concentration of ~4.4 wt% of CO_2 considered in the primitive-cell models is not unrealistic (e.g., McClellan and Lehr 1969). In contrast, defect models involving remote charge compensation mechanisms or the use of a homogeneous charge-compensating electrostatic background require larger super-cell to achieve a full convergence of the defect properties (Astala and Stott 2005).

In the B_F model (Fig. 1), the carbonate group is located on the basal face of the tetrahedral site, forming an angle of 32° with respect to (001) plane. The C–O bond lengths (Table 1) range between 1.294 Å (C–O(9)) and 1.306 Å (C–O(8)), leading to O–O distances ranging between 2.23 and 2.26 Å. Compared with the phosphate-occupied tetrahedral site, the carbonate group substitution leads to a

Fig. 2 Theoretical model of B-type carbonate locally compensated by an OH⁻ group (B_H_1 model) in fluorapatite (O = *red*, F = green, P = light pink, C = black, Ca = light blue, H = deep blue). *Top* view along the *c*-axis. *Bottom* view along the *b*-axis. Selected distances are indicated in Å. The OH⁻ group points to the O(9) atom of the carbonate group

contraction of the basal face (theoretical O-O distances of the phosphate site range between 2.49 and 2.57 Å; Balan et al. 2011) and a $\sim 3^{\circ}$ tilt away from the phosphate tetrahedron. The theoretical isolated B F carbonate defect thus displays a smaller distortion but a tilt angle very similar to that experimentally determined for the carbonate group in A-B fluorapatite (Fleet and Liu 2008). This tilt angle significantly differs from that observed in Na-bearing hydroxyapatite, which reaches 18° (Fleet and Liu 2007). The local electrostatic charge compensation of the defect is ensured by a fluoride ion located at the remaining apex of the tetrahedral site, thus corresponding to the substitution of a fluorine for an O(3) atom. The environment of the fluoride ion is similar to that previously suggested for excess fluoride anion in high-pressure synthesized fluorapatite and authigenic francolite by Fleet and Liu (2008). The distance between the fluoride ion and the carbon atom is 2.47 Å. This distance is significantly larger than the expected C…F distance for a bonded interaction (e.g., 1.46 Å from ionic radii, Shannon 1976), whereas the planar carbonate geometry attests for the sp2 hybridization of carbon. Thus, the clumping of



Fig. 3 Theoretical model of B-type carbonate locally compensated by an OH⁻ group (B_H_2 model) in fluorapatite (O = *red*, F = green, P = light pink, C = black, Ca = light blue, H = deep blue). Top view along the *c*-axis. Bottom view along the *b*-axis. Selected distances are indicated in Å. The OH⁻ group points to the O(3) atom of a neighboring phosphate group

carbonate and fluoride ions in fluorapatite does not involve any direct bonding between the two species. However, the fluoride ion is still located at a crystal site. It is shifted by only 0.4 Å from the position of the O(3) atom in the phosphate-occupied tetrahedral site. It does not migrate to the interstitial position previously observed in the modeling of a carbonate-fluorapatite cluster (Regnier et al. 1994).

For comparison, two configurations of clumped (CO_3^{2-}, F^-) defects with the carbonate group located on one of the nonequivalent vertical faces of the PO₄ tetrahedron and the fluorine ion at the remaining apex have been also investigated. They are referred to as B_F_V_1 and B_F_V_2, corresponding to a carbon location at the center of the (O(8), O(3), O(3)) or (O(9), O(3), O(3)) triangles, respectively (Table 1). Although stable, they were found to be less favorable than the B_F model by 18 kJ/mol (B_F_V_1) and 10 kJ/mol (B_F_V_2). This is consistent with experimental observations indicating that the CO₃ groups are preferentially located on the sloping faces of the tetrahedral sites of apatite (Elliott 1994; Suetsugu et al. 1998; Fleet 2009).



Fig. 4 Theoretical model of A-type carbonate in fluorapatite (O = red, C = black, Ca = light blue). *Top* view along the *c*-axis. The *z* coordinate of Ca atoms is indicated. *Bottom* view along the *b*-axis. Selected distances are indicated in Å. In this case, no charge compensation is required as the carbonate group replaces two OH⁻ groups

 Table 1
 Selected bond lengths of relaxed theoretical models of carbonate fluorapatite

	d C-O(3) (Å)	d C-O(8) (Å)	d C-O(9) (Å)	d CF (Å)	d OH (Å)
B_F	1.299	1.306	1.294	2.47	_
B_F_V_1	1.295	1.311	-	2.51	_
B_F_V_2	1.302	-	1.302	2.45	_
B_H_1	1.295	1.299	1.303		0.972
B_H_2	1.301	1.303	1.293		0.978

In the models of B_H type, the fluoride ion of model B_F is replaced by a hydroxyl group pointing toward the center (B_H_1) or the outside (B_H_2) of the tetrahedral site. The model B_H_1 is more stable than model B_H_2 by ~27 kJ mol⁻¹.

In model B_H_1 (Fig. 2), the OH group points toward the oxygen O(9), which displays the longest distance to the carbon atom (1.303 Å). The carbonate geometry (Table 1) and orientation is still close to that observed for the B_F model. The O(H)…C distance is 2.56 Å, slightly longer than the F…C distance in model B_F. A relatively short O–H bond length of 0.972 Å is observed, with O(H)…O and (O)H…O distances of 2.85 and 1.98 Å, respectively. Attempts to locate the H atom between O(4) and O(8) or between O(4) and O(3) did not lead to stable configurations, and the corresponding models always relaxed to a configuration with the OH group pointing toward O(9). The B_H_1 defect geometry differs from that of the equivalent defect in hydroxyapatite previously obtained using empirical potentials (Peroos et al. 2006). In this last case, the hydrogen-bond interaction involves two oxygen atoms of the carbonate group with (O)H…O bond distances between 2.15 and 2.41 Å.

After relaxation, the B_H_2 defect (Fig. 3) displays two almost identical C–O bond lengths at 1.302–1.303 Å and a third shorter C–O(9) bond (1.294 Å; Table 1). The O(H)…C distance is similar to that of B_H_1 at 2.54 Å. The OH group points to the O(3) oxygen of a neighboring phosphate group. Its length is 0.979 Å, slightly longer than in model B_H_1 and consistent with a shorter O(H)…O distance of 2.74 Å.

In addition, four models of clumped (CO_3^{2-}, OH^-) defects with the CO₃ group vertically orientated and the OH group pointing inward or outward the tetrahedral site have been investigated. All the relaxed configurations were less favorable than the B_H_1 model, by 22 to 66 kJ/mol. As for the B_H_1 and B_H_2 models, the outward configurations were significantly less stable (by ~40 kJ/mol) than their inward counterparts.

Constant-volume calculations of the structure of B-type defects were also performed using a hydroxyapatite primitive cell. These calculations lead to very similar orientation and geometry of the defects. For example, the B_F defect in hydroxyapatite displays a C…F distance of 2.48 Å and an angle of 33° with respect to the (001) plane. Mutual substitution of OH⁻ and F⁻ ions in apatite channel is thus not expected to significantly affect the isolated B-type carbonate defects. The energy change related to the exchange of OH⁻ and F⁻ ions between channel and B-site positions was calculated in the fluorapatite and hydroxyapatite cells. In both cases, a configuration with the OH group at the channel site and the F ion at the B-site is preferred by about 17 kJ/mol (in fluorapatite) to 22 kJ/mol (in hydroxyapatite). In comparison, the OH for F substitution in channel sites only displays a small stabilization (2.3 kJ/mol) of the mixed configuration with respect to an equivalent mixture of the pure end-members. For this last calculation, the system cell parameters were free to relax. Although consistently negative, the stabilization energy is slightly smaller than the 7 kJ/mol value obtained by De Leeuw et al. (2002) using the Perdew-Wang GGA functional.

The relaxed structure of the A-type model is in good agreement with the results of the previous theoretical works of Peeters et al. (1997), Astala and Stott (2005) and Ulian et al. (2013a). The carbonate molecule is nearly vertically oriented with one C–O bond perpendicular to the c-axis of apatite structure and the carbon position at z = 0.5 (Fig. 4). The carbonate group is nearly symmetric with respect to the (001) plane. The C–O distances are 1.27 Å for the horizontal C–O(5) bond and 1.30 Å for the two other bonds. The corresponding average C–O bond length (1.29 Å) is identical to that previously determined by Ulian et al. (2013a) using the B3LYP functional.

Theoretical NMR results

The theoretical ¹³C and ¹⁹F NMR parameters of B-type defect in fluorapatite are summarized in Table 2 together with the experimental values reported for fluorinated apatites, francolite (Yi et al. 2013) and stafellite (Mason et al. 2009), as well as ¹³C parameters reported for synthetic carbonated hydroxyapatites (Beshah et al. 1990).

Considering the B-type carbonate models, ${}^{13}C$ calculated values are close to 170 ppm, in good agreement with the experimental data. We note, however, that the B_F_V_1 and B_F_V_2 models, which display vertically orientated carbonate groups, lead to slightly overestimated values (>171 ppm). The calculated ${}^{13}C$ value for the A-type model is 164.7 ppm, slightly underestimated compared to its experimental counterparts (165.5 ppm, Beshah et al. 1990;

	B_H_1	B_H_2	B_F	$B_F_V_1$	$B_F_V_2$	А	B-type exp.	A-type exp.	Channel F exp.	B-site F exp.
¹³ C	170.8	170.7	169.8	171.4	171.7	164.7	170±1 ^{a,b,c}	165.5 ^a 168.6 ^b	_	-
¹⁹ F	-100.3	-100.7	-102.1	-105.0	-107.2	-	_	-	-102 ^c -99.8 ^b	-
	-103.2	-104.1	-103.3	-102.2	-102.6	_	_	_		_
	-	-	-84	-67.5	-76.5	-	-	-	-	-88° -86.6 ^b

Table 2 Theoretical and experimental ¹³C and ¹⁹F NMR chemical shift (ppm) of carbonate fluorapatite

^a Beshah et al. (1990)

^b Mason et al. (2009)

^c Yi et al. (2013)

168.6 ppm, Mason et al. 2009). A calculation using a double cell size along the c-axis, ensuring a separation of the A-type channel carbonate ions by fluorine ions, insignificantly changed the 13 C chemical shift to 165 ppm.

The ¹⁹F chemical shift parameters cover a larger range from -67.5 ppm in model B_F_V_1 to -104.1 ppm in model B H 2. In all models, one at least of the fluorine sites (located in the structural channels) shows a chemical shift around -102 ppm consistent with the experimental 19 F parameters of pure fluorapatite (Yi et al. 2013). In the models B H 1 and B H 2, the other channel site is calculated around -100 ppm. In model B F, the chemical shift of the fluoride ion located at the B-site is computed at -84.0 ppm. It is experimentally observed around -86.6 ppm in the "stafellite" sample investigated by Mason et al. (2009) and -88 ppm in the "francolite" sample of Yi et al. (2013). Interestingly, the two less stable fluorinated models with a vertical orientation of the carbonate group lead to ¹⁹F chemical shifts of -67.5 and -76.5 for the B F V 1 and B_F_V_2 models, respectively. This corresponds to a significantly poorer agreement with experimental observations.

The occurrence of clumped (CO_3^{2-}, F^-) defects with vertically orientated carbonate groups can therefore be ruled out both from energetic considerations and from the lack of agreement with NMR spectroscopic observations. Considering that the clumped (CO_3^{2-}, OH^-) defects with vertically orientated carbonate groups are significantly less stable than the chemically equivalent B_H_1 model and that experimental observations consistently indicate that B-type carbonate groups in hydroxyapatite occupy the sloping faces of the tetrahedral sites (e.g., Wilson et al. 2004, 2006; Fleet 2009), models with vertically orientated carbonate groups will not be considered in any further details in the present study.

Theoretical vibrational properties of carbonate defects in apatite

The vibrational transverse optical (TO) modes (using the definition given by Baroni et al. (2001), i.e., the modes

coupled with a zero macroscopic electric field) of the defective apatite structure (models B_F, B_H_1, B_H_2 and A) have been obtained by diagonalization of the theoretical dynamical matrix (Table 3). Compared with experimental ones, the theoretical frequencies of apatite are underestimated by about 5%, an effect related to the use of the generalized gradient approximation to the exchangecorrelation functional (e.g., Balan et al. 2011). The commonly observed IR-active vibrational modes of carbonate in apatite are related to the antisymmetric stretching of C–O bonds (v_3 modes) and to the motion of the C atom perpendicularly to the plane of the carbonate molecule (v_2 out-of-plane bending mode). In all cases, these v_2 and v_3 internal modes are well defined and do not display any significant contribution from the phosphate groups of the host structure.

In apatite, the twice-degenerated v_3 modes of the free carbonate ion are split by the site distortion. The v_3 CO₃ stretching modes are calculated between 1,300 and $1,600 \text{ cm}^{-1}$. The splitting is significantly larger for the A-type model (90 cm^{-1}) than for B-type models (from 14 cm^{-1} in B H 1 to 40 cm⁻¹ in B F). The B H 2 model, in which the OH group points out of the tetrahedral site, and the fluorinated B F model display very similar $v_3 CO_3$ wavenumbers. The v_3 CO₃ wavenumbers are in fact broadly correlated to the involved C-O bond length (Fig. 5). The high-frequency v_{3b} component is related to the vibration of the shorter C–O bond, whereas the low-frequency v_{3a} component involves the coupled motion of the two remaining longer C-O bonds. Consistent with the experimental observations of Suetsugu et al. (1998), the v_{3h} band of the A-type defect, which involves the shorter C-O(5) bond, is polarized perpendicularly to the c-axis. The average $v_3 CO_3$ wavenumber (Table 3) of the A-type defect $(1,467 \text{ cm}^{-1})$ is significantly higher than that of B-type defects $(\sim 1,400 \text{ cm}^{-1})$, reflecting the comparatively shorter average C–O bond length of the A-type defect. This 67 cm⁻¹ shift is consistent with the one experimentally observed between the v_3 mode of B-type (1,443 cm⁻¹, Regnier et al. 1994)

Table 3 Theoretical transverse optical frequency and IR cross section (in parentheses, $(D/Å)^2/amu$) of selected vibrational modes of carbonate fluorapatite. Experimental frequencies are reported for comparison

	$v_2 CO_3 (cm^{-1})$	$v_{3a} CO_3 (cm^{-1})$	$v_{3b} CO_3 (cm^{-1})$	$v_3 CO_3 average$ (cm ⁻¹)	Splitting of $v_3 CO_3 (cm^{-1})$	OH stretching
B_H_1	771 (9.68)	1,396 (26.5)	1,410 (26.2)	1,403	14	3,697
B_H_2	807 (4.74)	1,379 (25.9)	1,418 (30.5)	1,398.5	39	3,578
B_F	813 (4.11)	1,376 (27.2)	1,416 (30.9)	1,396	40	-
B Exp.*	864 - 866	1,400-1,440	1,450-1,470	_	25-50	-
А	826 (3.65)	1,422 (25.0)	1,512 (25.8)	1,467	90	-
A Exp.*	878-880	1,450–1,470	1,540–1,550	_	70–100	-

* Suetsugu et al. (1998); Tacker (2008); Yi et al. (2013)



Fig. 5 Correlation between the wavenumber of the v_3 CO₃ modes and the length of C–O bonds. *circles*: A-type, *squares*: B_F, *diamonds*: B_H_1, *triangles*: B_H_2

and A1-type (1,502.5 cm⁻¹; Fleet et al. 2011) carbonates in fluorapatite.

The v_2 carbonate mode of the B_H_2 and B_F models is calculated at 807 and 813 cm⁻¹, respectively, whereas that of the A-type model is calculated at 826 cm⁻¹ (Table 3). The 13 cm⁻¹ difference observed between the B_F and A models is consistent with the difference experimentally observed between the B2 and A-type signals in fluorapatite (16 cm⁻¹, Fleet 2009). A significantly lower wavenumber is computed for the B_H_1 model, at 771 cm⁻¹. A contribution involving the OH group of the defect is observed in the v_2 mode of B_H_1 model and, to a lesser extent, of B_H_2 model.

The change of selected vibrational frequencies has been investigated as a function of the cell volume (Table 4). Approximate values of the mode-Grüneisen parameters were obtained by computing the frequency changes induced by an isotropic increase in the cell parameters of 1 %. The two v_3 CO₃ stretching modes display positive mode-Grüneisen parameters, consistent with the reverse correlation observed between the C–O stretching frequencies and C–O bond lengths. The v_2 CO₃ modes of models B_H and B_F display a significant and negative mode-Grüneisen parameter, whose magnitude is larger for the B_H models than for the B_F model. In comparison, the v_2 CO₃ mode frequency of the A-type model weakly depends on the unit-cell volume.

Finally, we note that the presence of substituted carbonate groups modifies the symmetry of the structure and leads to significant modifications of the vibrational modes of

 Table 4
 Approximate mode-Grüneisen parameter* of selected vibrational modes of carbonate and phosphate in fluorapatite

Mode	B_H_1	B_H_2	B_F	A	F-apatite
$v_2 CO_3$	-0.24	-0.25	-0.16	-0.02	_
$v_{3a} CO_3$	0.16	0.31	0.32	0.25	-
$v_{3b} CO_3$	0.31	0.17	0.21	0.35	-
$v_1 PO_4$	0.40	0.45	0.48	0.41	0.51

* Approximate mode-Grüneisen (1912) parameters, $\tilde{\gamma}_i$, are defined by $\tilde{\gamma}_i = -\frac{V \Delta \omega_i}{\omega_i \Delta V}$ where $\Delta \omega_i$ is the angular frequency variation of the *i*th vibrational mode induced by a ΔV change of the cell volume

surrounding phosphate groups. However, such effects are expected to lead to modifications of the vibrational properties of the host structure at a relatively long spatial scale and cannot be fully accounted for using the present modeling strategy (see, e.g., Lazzeri and Thibaudeau 2006).

Theoretical infrared absorption spectrum of carbonate fluorapatite

The IR absorption cross sections of IR-active vibrational modes were obtained from the Born effective charge tensors and atomic displacements (Table 3). The two v_3 CO₃ stretching modes of B- and A-type carbonate models display comparable cross sections with a slightly stronger absorption for the high-frequency component. This suggests that fits of the v_3 CO₃ stretching modes in unpolarized spectra should be performed by using pairs of absorption bands with similar intensities. A slight enhancement of the v_3 CO₃ absorption is also observed for the B-type models with respect to the A-type model. The v_2 CO₃ bending mode of the B_H_2 and B_F models displays a similar cross section, slightly stronger than that of the A model. Such moderate difference is, however, probably difficult to evidence from powder IR absorption experiments, given the uncertainties related to the baseline subtraction and to the fit of partially overlapping contributions from A-type and B-type signals (Fleet 2009). Together with a lower frequency, the v_2 CO₃ mode of the B_H_1 model displays an absorption cross section significantly stronger than that of the two other B-type models.

Although IR cross sections provide information on the absorption properties of carbonate defects in fluorapatite, it does not fully account for the spectroscopic properties of experimental powder samples. In particular, it does not account for the influence of macroscopic electrostatic effects related to the finite size of the absorbing particles (e.g., Fuchs 1975; Ruppin 1977, 1978). A better description of the IR absorption properties relies on the computation of the dielectric properties of the material, then making it possible to derive a theoretical absorption spectrum for a given experimental setup. In the case of a pure crystal, the dielectric tensor

is obtained from the transverse vibrational modes and Born effective charge tensors (see, e.g., Balan et al. 2001, 2011). In the case of a defective crystal, the determination of the dielectric tensor is not as straightforward because the structural models are obtained using periodic boundary conditions. Two aspects have to be considered when modeling the properties of the defective crystal. First, the dielectric tensor should reflect the fact that the substitution may randomly occur on equivalent sites of the cell. The dielectric tensor of carbonate-bearing apatite is thus expected to display a uniaxial symmetry, even though the periodic model presents a lower symmetry. Second, even though the cell size is sufficient to lead to a realistic local structure and to minimize the interaction between image defects, long-range electrostatic interactions related to the polarization of absorbing defects can still occur.

The proper modeling of these two points raises significant difficulties, and in the following, we adopt a simplified approach in which each aspect is treated separately. First, the potential long-range electrostatic interaction between the defects is neglected, and the absorption spectrum of the defective apatite is computed by simply averaging the perpendicular components ε_{xx} and ε_{yy} of the dielectric tensor



Fig. 6 Theoretical powder infrared absorption spectrum of carbonate apatite models, calculated assuming that spherical apatite particles are inserted in a homogeneous KBr matrix. The wavenumbers of the v_2 and v_3 CO₃ modes are indicated. The wavenumber of v_3 CO₃ modes differs by about 5 cm⁻¹ from the corresponding transverse optical mode frequencies (Table 3)

of the defect model, ε_{zz} remaining unchanged and all the nondiagonal components vanished. A theoretical powder infrared absorption spectrum can then be calculated from the averaged dielectric tensor in assuming that isolated spherical apatite particles are inserted in a homogeneous KBr matrix (Fig. 6).

Compared with pure fluorapatite, carbonate defects lower the symmetry of the structure of apatite, leading to new IR-active vibrational modes. As shown in Fig. 6, models with different carbonate defect display very different shape of the intense $v_3 \text{ PO}_4$ vibrational band. The weaker $v_1 \text{ PO}_4$ band is also affected, and five nondegenerated IRactive vibrational modes of the defective apatite structure are related to the v_1 vibration of the PO₄ group. The corresponding wavenumbers are spread over 5–10 cm⁻¹.

For all the models, macroscopic electrostatic effects affect the intense absorption bands, which are shifted to higher frequency from the corresponding transverse optical frequency (Fig. 6). The v_3 CO₃ stretching bands are shifted by $\sim 5 \text{ cm}^{-1}$. Compared with bare IR cross sections (Table 3), the relative intensity of the v_3 CO₃ bands is also affected. The less absorbing $v_2 \text{ CO}_3$ and $v_1 \text{ PO}_4$ bands are less affected by macroscopic electrostatic effects. This is related to the weakness of the associated depolarization field in the absorbing particle. We note, however, that in the case of defects, the macroscopic depolarization field will depend on the defect concentration and that such macroscopic electrostatic effects may increase with the carbonate concentration. As shown by the present calculations, they can already be observed in the investigated system that contains 4.4-4.5 wt% of CO₂.

Independent of the powdered nature of some apatite samples, electrostatic interactions can also occur at a microscopic scale between substituted carbonate groups. This effect can be assessed by considering the dispersion of the carbonate vibrational modes in the investigated models, recalling that vibrational modes at the boundary of the Brillouin zone correspond to out-of-phase vibrations in adjacent cells, whereas those at the center of the Brillouin zone correspond to the in-phase vibration of the whole periodic system. Theoretical phonon frequencies have thus been computed at the high-symmetry K and M points of the

Table 5 Theoretical phonon frequencies (cm^{-1}) computed at the center (Γ) and high-symmetry K and M points of the hexagonal Brillouin zone for model B_F

	Г	М	К	
$v_2 CO_3$	813	813	814	
$v_{3a} CO_3$	1,376	1,389	1,383	
$v_{3b} CO_3$	1,416	1,420	1,425	
$v_1 PO_4$	911	911	911	

hexagonal Brillouin zone for model B_F (Table 5). The v_2 CO₃ mode displays a negligible dispersion, consistent with the weakness of the associated polarization and IR absorption cross section. In contrast, the v_3 CO₃ modes show a significant shift to higher wavenumbers, ranging from 4 to 13 cm⁻¹.

Therefore, at a concentration level of ~4.4 wt% CO₂, the v_3 CO₃ absorption bands appear as significantly affected by electrostatic effects occurring both at the macroscopic scale in the absorbing particles and at the microscopic scale, due to the random distribution of the defects in the crystal. In comparison, the v_2 CO₃ and v_1 PO₄ are less affected and should provide a better insight into the atomic-scale properties of the defective crystal. Although these calculations were performed on model B_F, these observations also stand for the other models because the electrostatic interactions mostly depend on the microscopic polarizability of the carbonate group.

Discussion

Constraints on B-type carbonate incorporation mechanisms

The occurrence of various charge balance mechanisms explains the variability of the vibrational spectroscopic parameters reported in the literature for the B-type carbonates. The position of the $\nu_{3a}\,CO_3$ band may vary from 1,405 to 1,430 cm⁻¹, whereas the v_{3b} CO₃ band occurs in the 1,451–1,475 cm⁻¹ range (Elliott 1964; Bonel et al. 1973; Featherstone et al. 1984; Sommerauer and Katz-Lehnert 1985; Vignoles et al. 1988; Apfelbaum et al. 1992; Suetsugu et al. 1998; Comodi et al. 1999; Fleet and Liu 2004; Wilson et al. 2004). The position of the v_{3h} CO₃ band is more difficult to precisely determine as this region usually presents overlapping contributions from A-type and B-type carbonates. The narrower $v_2 CO_3$ band can also be used to obtain insights into the CO₃ substitution mechanisms and provides evidences for the occurrence of more than two types of carbonate defects in high-pressure carbonated apatite samples (Fleet 2009). There is a general agreement that the band at ~878 cm^{-1} corresponds to A-type substitution (Elliott 1994) and the band at ~871 cm^{-1} is related to a B-type substitution (e.g., Bonel et al. 1973; Leventouri 2006; Fleet 2009). The clumped (CO_3^{2-}, F^-) defect displays a characteristic narrow band at $\sim 864 \text{ cm}^{-1}$ (Yi et al. 2013). This suggests that the B2 signal reported at 864 cm^{-1} by Fleet (2009) is related to the occurrence of the "francolite"-type defect in synthetic carbonated fluorapatite samples. A broader band at ~862 cm^{-1} in biological samples is attributed to a labile component (Rey et al. 1989) but could correspond to a different orientation of A-type channel carbonates (A2-type; Fleet 2009).

The present theoretical results provide specific constraints that could be used to demonstrate or to rule out the occurrence of specific carbonate incorporation mechanism. Consistent with experimental observations, the relative energy of the carbonate defects rules out the occurrence of configurations with vertically orientated carbonate groups. Considering the systematic shift observed between experimental and theoretical wavenumbers and the weak sensibility of ¹³C NMR values to small modification of the carbonate group environment, bare theoretical vibrational frequencies and ¹³C NMR chemical shifts cannot be directly used to prove the occurrence of a given defect configuration. In contrast, the splitting of the $v_3 CO_3$ bands and the relative position of the $v_2 CO_3$ among the defects appear as more relevant parameters. The ¹⁹F NMR parameters are also highly sensitive to slight modifications of the environment of fluoride ions. In particular, the theoretical IR and ¹⁹F NMR spectroscopic properties of models B_F and A compare very well with those experimentally observed for the "francolite" and A-type carbonate defects, respectively (Tables 2, 3).

Among the investigated models of clumped $(CO_3^{2-},$ OH-) defects, the infrared spectroscopic properties of model B H 1 (local compensation of carbonate group by an hydroxyl group pointing along an edge of the tetrahedral site) unfavorably compare with experimental constraints: the IR calculated spectrum displays a much too low splitting value (14 cm⁻¹) and a too low $v_2 CO_3$ wavenumber, which is downshifted by 42 cm⁻¹ from the francolite defect. The spectroscopic properties of the closely related B H 2 model (local compensation of carbonate group by a hydroxyl group pointing out of the tetrahedral site) are in better agreement with experimental IR observations. However, the significantly lower stability (~27 kJ/ mol) of B H 2 with respect to the chemically equivalent B_H_1 model makes it unlikely to occur in apatite samples. In addition, when both F⁻ and OH⁻ ions are present in the structure, F⁻ ions compete successfully for the local charge compensation of carbonate groups at the B-site. Taken together, these observations suggest that a local charge compensation of B-type carbonate groups by hydroxyl ions is unlikely to occur in apatite.

Considering the easy substitution of weakly bonded OH⁻ groups by F⁻ ions in a number of minerals (e.g., Robert et al. 1993, 1999) and the very common implication of protons in the charge-compensating mechanisms of cationic vacancies in oxide and silicate minerals (e.g., Bell and Rossman 1992; Keppler and Smyth 2006), the absence of clumped (CO₃²⁻, OH⁻) defects is somehow counter-intuitive. However, it can be understood from qualitative bond valence considerations. In fact, microscopic models of OH groups associated with cationic vacancies in nominally anhydrous minerals have shown that the most stable

configurations correspond to an efficient valence compensation of oxygen atoms through donation and acceptation of hydrogen bonds, such as, in the hydrogarnet (Nobes et al. 2000) or hydrozircon (Balan et al. 2013) defects. In the present case, both the O(9) oxygen of the carbonate group (in B_H_1) and the O(3) oxygen of the neighboring phosphate group (in B_H_2) have their valence fully compensated by the coordinating Ca and P atoms (B_H_2) or Ca and C atoms (B_H_1), making them poor H-bond acceptors. The slightly longest O(H)...O distance (and weaker H-bond) observed in the B_H_1 model is consistent with the greater stability of this model, but in both cases, the presence of an OH group at the apex of the tetrahedral site is significantly less favorable than that of a fluoride ion.

Broadening mechanism of infrared absorption bands of carbonate groups in apatite

The powder infrared spectrum of carbonate-bearing apatite often reveals significant differences in the width of the various bands ascribed to carbonate groups, the v_3 CO₃ bands being significantly broader than the v_2 CO₃ band (e.g., Fleet 2009). For example, the average FWHM of the v_3 CO₃ bands of B-type carbonate in sedimentary carbonate fluorapatite (francolite) is ~20 cm⁻¹, while that of the v_2 CO₃ band in the same sample is only ~4 cm⁻¹ (Yi et al. 2013). In dental enamel, they are ~40 and ~8 cm⁻¹, respectively (e.g., Roche et al. 2010).

The theoretical results presently obtained on the various models of B-type carbonate sites may help to determine the origin of this difference. Besides instrumental resolution, several factors contribute to the width of infrared absorption bands of powdered materials. The homogeneous linewidth is related to the decay of the excited state through anharmonic mode-mode coupling. It leads to Lorentzian band shapes and depends on temperature (Salje et al. 2000). Although measurable, the variation of linewidth of apatite absorption bands with temperature is weak. Thus, homogeneous processes do not appear as the main source of broadening in natural or synthetic apatite samples (Balan et al. 2011; Yi et al. 2013). The inhomogeneous linewidth does not depend on temperature and stems from a distribution of vibrational frequencies within the sample. This distribution can arise from elastic strain fields related to interfaces or point defects, as well as from the occurrence of a nonuniform macroscopic electric field, within the same particle or due to a distribution of particle shapes. For arbitrary particle shapes, the powder absorption bands are usually centered on the frequency computed for spherical particles and display a width similar to the splitting between longitudinal and transverse optical modes (e.g., Balan et al. 2011).

In the case of the weakly absorbing bands of apatite, such as the $v_2 CO_3$ or $v_1 PO_4$ band, the electrostatic effects

are small because the induced polarization is also small. Thus, the linewidth of these bands mostly stems from microscopic inhomogeneous processes. Theoretical mode-Grüneisen parameters provide an assessment of the sensitivity of the vibrational modes to elastic strain fields. From Table 4, the contribution of microscopic distortions to the band broadening should not vary by more than a factor of ~2 between the various absorption bands of B-type carbonate groups. In turn, the significantly larger width experimentally observed for the v_3 CO₃ modes most likely stems from electrostatic effects related to the dielectric properties of the particles or to long-range interactions between the substituted carbonate defects. Examination of the shift of absorption bands in the spectrum of spherical particles and of the dispersion of the corresponding vibrational modes (assessed from the vibrational frequencies computed at the high-symmetry points of the Brillouin zone, Table 5) indicates that the expected magnitude of these broadening effects is within 10 to a few tens of cm^{-1} . The present theoretical results thus point to previously unrecognized effects contributing to the width and complexity of v_3 CO₃ absorption bands. Besides the overlap of different signals, these effects modify the band shape and explain why standard fitting approaches may fail to properly account for the $v_2 CO_3$ absorption bands in apatite.

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