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## Crystal structure and cation lone electron pair activity of $\text{Bi}_2\text{S}_3$ between 0 and 10 GPa

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**Abstract** Crystal structure of  $\text{Bi}_2\text{S}_3$  was refined at eight distinct hydrostatic pressures in the range 0–10 GPa using a CCD equipped 4-circle diffractometer and a diamond-anvil cell. Coefficients of the BM3 equation of state are as follows: zero-pressure volume  $498.4(7) \text{ \AA}^3$ , bulk modulus  $K_0$  36.6(15) GPa and its pressure derivative 6.4(5). The bulk of compression takes place in the structural space between  $\text{Bi}_4\text{S}_6$  ribbons, where lone-electron pairs are accommodated. Eccentricity of Bi in its coordination polyhedra decreases in the process, with long Bi–S distances decreasing, whereas the opposing short Bi–S distances stay constant or even increase in length. All these phenomena are compatible with the movement of lone-electron pairs of Bi closer to the parent atom at increasing pressure.

**Keywords** Bismuthinite · High pressure · Lone electron pair · Equation of state

### Introduction

Stibnite,  $\text{Sb}_2\text{S}_3$ , and bismuthinite,  $\text{Bi}_2\text{S}_3$ , have recently become an object of renewed studies as simple representatives of compounds with active lone electron pairs on cations. The structure of  $\text{Sb}_2\text{S}_3$  at ambient conditions was originally determined by Hofmann

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(1933) and revised by Šćavničar (1960), Bayliss and Nowacki (1972) as well as by Łukaszewicz et al. (1997); that of  $\text{Bi}_2\text{S}_3$  by Kupčik and Veselá-Nováková (1970). They were re-refined by Lundegaard et al. (2003) and Kyono and Kimata (2004).

Low-temperature structure refinements on  $\text{Sb}_2\text{S}_3$  were made by Kyono et al. (2002) and by Lundegaard (2003) whereas the high/low temperature transformation of this compound has been repeatedly approached by diverse physical methods and hotly discussed since the first paper of Rinkevichius and Mikalkevichius (1967) on the pyroelectric effect. The latest contributions, with diametrically opposing points of view, have been published by Sørensen and Lundegaard (2004) who interpret the low-temperature  $\text{Sb}_2\text{S}_3$  as orthorhombic with pronounced multiple-diffraction effects whereas Kuze et al. (2004) indicate a series of phase transformations from Pbnm via  $\text{P2}_1\text{nm}$  to a monoclinic/triclinic modification below 290 K. The acentric group  $\text{P2}_1\text{nm}$  was already suggested by McKee and McMullan (1975), among others. The two more recent works also contain an exhaustive list of references on this problem. Structures of different members of the  $(\text{Bi,Sb})_2\text{S}_3$  solid solution series at ambient conditions were published by Kyono and Kimata (2004).

High-pressure study of  $\text{Sb}_2\text{S}_3$  to 10 GPa was a subject of publication by Lundegaard (2003) (referred to as [1] in the rest of the paper); the analogous study of  $\text{Bi}_2\text{S}_3$  is the subject of the present contribution.

### Experimental

A synthetic bismuthinite was used for this study. For structure analyses a series of X-ray intensity data was collected in the pressure range 0–10 GPa using a CCD-equipped Bruker AXS 4-circle diffractometer, and a DXR-6 Diacell diamond-anvil cell (DAC). The data were collected at 298 K using graphite-monochromatized  $\text{MoK}\alpha$  radiation. One zero-pressure data set with crystal loaded in DAC and seven high-pressure

data sets were collected. For this experiment a 220  $\mu\text{m}$  hole was drilled into a steel gasket preindented to a thickness of 80  $\mu\text{m}$ . A 1:4 ethanol:methanol mixture was used as hydrostatic pressure medium. Unit-cell parameters of quartz were used for pressure calibration (Angel et al. 1996). The data was integrated with SAINT+, and XPREP (Bruker 2000) was used for numerical face-indexed absorption correction. Beryllium plugs were used in the optical access holes in the beryllium backing plates. It was therefore possible to calculate the X-ray path length through the DAC-components using the setting angles for each reflection, and from that it was simple to correct the intensities for absorption due to the DAC-components. All the structures were refined with anisotropic atomic displacement parameters (ADP) for Bi and isotropic for S, using SHELXL-97 (Sheldrick 1997). The structures were all refined in the  $Pnma$  space group, indicated by the intensity statistics and systematic extinction, to  $R$ -values of  $\approx 0.04$  (Table 1). No phase transition was detected in the pressure range 0–10 GPa.  $F_0/F_c$  tables are deposited.

## Results and discussion

### Equation of state

The EoS for bismuthinite was determined using the post-integration unit-cell parameters, because, as it is demonstrated below, satisfactory EoS parameters can be obtained this way when using the applied experimental setup where the intensities are collected from a large set of exposures with a very high spatial resolution.

In paper [1] the unit-cell parameters were first determined from a set of at least 20 reflections, the

positions of which were determined with the eight positions centring procedure (Angel et al. 1996). Using this procedure the setting angles for an individual reflection are determined with a precision better than  $0.01^\circ$ , therefore resulting in very precise unit-cell parameters. The second set of parameters in [1] was obtained from the centring information for a large number of reflections obtained from the SAINT+ integration and was in excellent agreement with the first high precision unit-cell parameters. The zero-pressure volume, bulk modulus and its pressure derivative determined from fitting a third-order Birch-Murnaghan (BM3) equation of state to the post-integration unit-cell parameters of stibnite were found to be  $487.1(6) \text{ \AA}^3$ , 27.9(10) GPa and 7.5(5), respectively, which is in very good agreement with the values  $487.73(6) \text{ \AA}^3$ , 26.91(14) GPa and 7.9(1) found in [1] using the eight positions centring procedure.

Unit-cell parameters of  $\text{Bi}_2\text{S}_3$  were found to alter smoothly with pressure. The zero-pressure bulk modulus, and its pressure derivative were determined from fitting a BM3 equation of state (Birch 1947) to the unit-cell volume data. By substituting the cube of the unit-cell edges for the volume in the equation, a BM3 EoS was fitted to the unit-cell edges (Table 2). The zero-pressure “bulk modulus” obtained from fitting is equal to minus one-third of the inverse of the zero-pressure linear

**Table 2** Parameters of the BM3 equation of state

BM3	Zero-pressure value	$K_0$ (GPa)	$K'$
$V$	$498.4(7) \text{ \AA}^3$	36.6(15)	6.4(5)
$a$	$11.282(26) \text{ \AA}$	17.8(41)	14.6(36)
$b$	$3.9728(11) \text{ \AA}$	80.6(31)	2.5(6)
$c$	$11.131(5) \text{ \AA}$	35.0(12)	3.7(3)

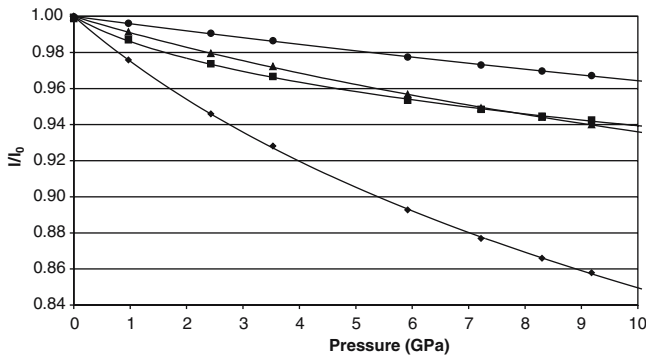
**Table 1** Experimental data for  $\text{Bi}_2\text{S}_3$

Pressure (GPa)	0.0001	0.97	2.43	3.53	5.92	7.22	8.30	9.18
Crystal data								
$a$ ( $\text{\AA}$ )	11.269(2)	11.136(3)	10.987(2)	10.907(3)	10.758(2)	10.701(3)	10.659(2)	10.634(2)
$b$ ( $\text{\AA}$ )	3.9717(3)	3.9574(4)	3.9353(3)	3.9191(4)	3.8833(3)	3.8655(4)	3.8525(3)	3.8423(3)
$c$ ( $\text{\AA}$ )	11.129(2)	11.035(2)	10.903(2)	10.822(2)	10.650(2)	10.565(2)	10.510(2)	10.463(2)
$V_{uc}$ ( $\text{\AA}^3$ )	498.08	486.32	471.41	462.58	444.89	437.03	431.56	427.56
$\rho$ ( $\text{g/cm}^3$ )	6.856	7.022	7.244	7.383	7.676	7.814	7.913	7.987
$\mu$ ( $\text{mm}^{-1}$ )	71.63	73.36	75.68	77.13	80.196	81.64	82.67	83.446
Data collection								
# Measured reflc.	1,419	1,440	1,401	1,381	1,315	1,286	1,281	1,263
# Unique reflc.	254	244	237	236	222	214	217	212
# Observed reflc. <sup>a</sup>	214	201	200	202	195	186	187	179
$R_{\text{int}}$	0.0824	0.0944	0.1095	0.0937	0.0865	0.1115	0.0913	0.1144
$2\theta_{\text{max}}$ ( $^\circ$ )	46.48	46.52	46.46	46.48	46.52	46.42	46.46	46.50
Range of $h, k, l$	$-9 \leq h \leq 10$ $-4 \leq k \leq 4$ $-11 \leq l \leq 11$	$-9 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 11$	$-9 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 11$	$-9 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 11$	$-8 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 10$	$-8 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 10$	$-8 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 10$	$-8 \leq h \leq 9$ $-4 \leq k \leq 4$ $-10 \leq l \leq 10$
Refinement								
$R1$ ( $ F_0  > 4\sigma$ )	0.0419	0.0422	0.0352	0.0434	0.0429	0.0423	0.0390	0.0395
w $R2$	0.0863	0.1010	0.0771	0.0966	0.0973	0.0871	0.0817	0.0790
Goof	1.145	1.186	1.112	1.204	1.155	1.122	1.148	1.242
# Parameters	23	23	23	23	23	23	23	23

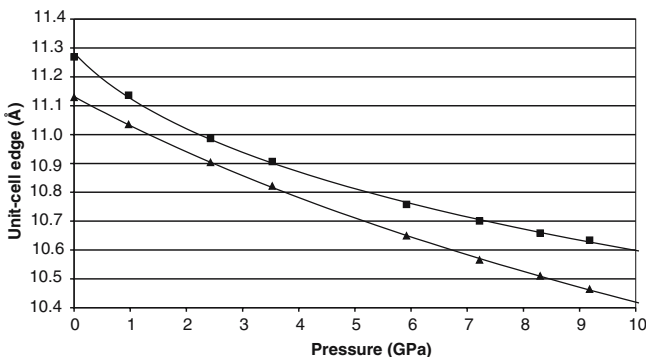
<sup>a</sup>Criterion for observed reflection is  $|F_0| > 4\sigma$

compressibility  $\beta_0$  of the unit-cell axis. The zero pressure compressibility is defined as  $\beta_0 = l_0^{-1}(\partial l/\partial P)_{P=0}$  where  $l_0$  is the length of the unit-cell edge at zero pressure. Comparing the values of bismuthinite and stibnite it can be seen that the latter is generally more compressible with the exception of the  $b$ -axis direction which itself is the least compressible direction in both structures.

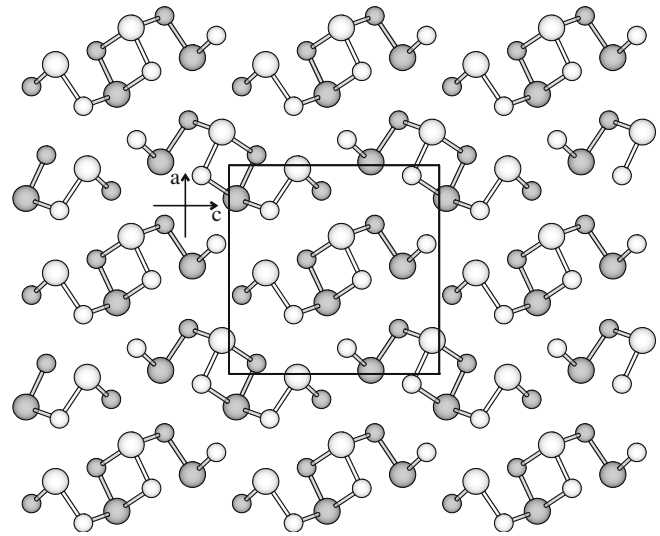
The evolution of unit-cell parameters with increasing pressure is shown in Figs. 1 and 2. The crossing of  $a$  and  $c$  parameters that was observed in stibnite at 1.12 GPa (Fig. 3 in [1]) is not found in bismuthinite, but there is a minimum difference in these values at approximately 2.5 GPa (Fig. 2). This difference can be understood in connection with relative sizes of the largely non-compressible rods in the structure of these two compounds. The thickness of the rods, expressed by e.g. the shortest Bi2–S1 or Sb2–S1 distances (see Fig. 4, 9) is substantially larger in  $\text{Bi}_2\text{S}_3$  (2.59 Å) than in  $\text{Sb}_2\text{S}_3$  (2.45 Å). On the other hand, their extension perpendicular to this direction expressed as the distance between marginal S atoms is practically the same: 8.01 Å in  $\text{Bi}_2\text{S}_3$  and 8.03 Å in  $\text{Sb}_2\text{S}_3$  (all values refer to room temperature). As seen in Fig. 4, the rods have their extended direction oriented at a low angle to the  $c$ -axis.



**Fig. 1** Evolution of unit-cell parameters of bismuthinite with increasing pressure. Values are given relative to their zero pressure value. Squares indicate  $a$ , circles  $b$  and triangles  $c$  value. Rhombs stand for unit-cell volume

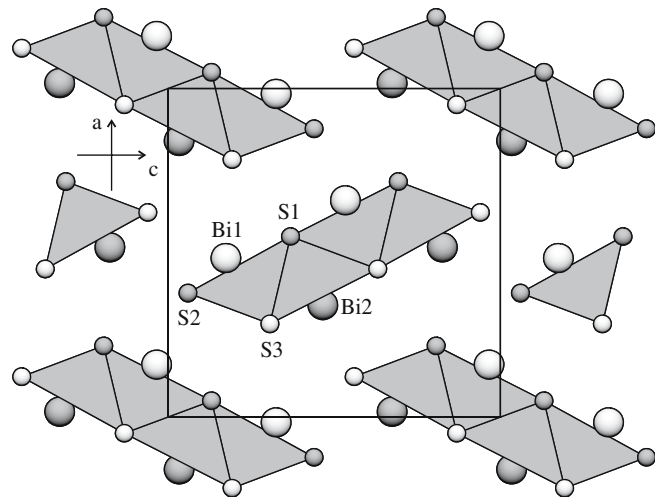


**Fig. 2** Observed  $a$  and  $c$  unit-cell parameters of bismuthinite. The lines are obtained by fitting a BM3 equation of state to the unit-cell parameters. Squares indicate  $a$ , triangles  $c$  parameter



**Fig. 3** Structure of bismuthinite in the  $Pnma$  setting. Grey circles represent atoms on the  $y=0.25$  mirror plane, white circles represent atoms on the  $y=0.75$  mirror plane. Large circles are Bi atoms and small circles are S atoms. For atom labels see Fig. 4

The compression of the structure is achieved mostly by a decrease of the inter-rod space. In the first phase of compression this is accompanied by the fastest decrease in the  $a$ -axis which is longer than the  $c$ -axis in both compounds at ambient pressure. In stibnite this makes the  $a$ -axis period shorter than that of the  $c$ -axis, while in bismuthinite with thicker rods this situation is never achieved. The trend in compressibility along the two axes changes at higher pressures. For stibnite the  $a$  and  $c$ -axes stay equal up to 10 GPa, while for bismuthinite after 5 GPa the compressibility along the  $c$ -axis is even larger than along the  $a$ -axis.



**Fig. 4** Grey polyhedra represent the rod volume ( $V_{rod}$ ) and the rest of the unit-cell volume is defined as the lone electron pair volume ( $V_{lone}$ ). Grey circles represent atoms on the  $y=0.25$  mirror plane, white circles represent atoms on the  $y=0.75$  mirror plane. Large circles are Bi atoms and small circles are S atoms

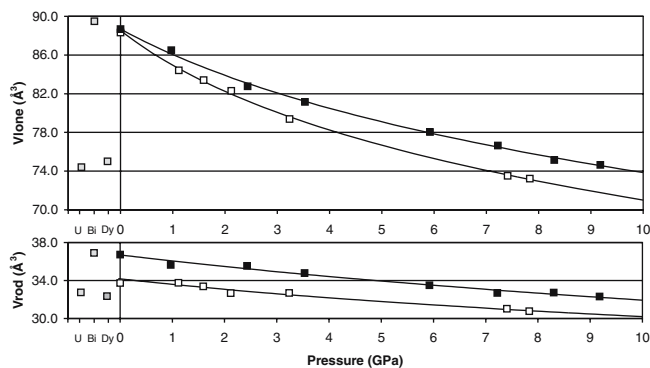
## Structure data

The atom positions of the refined bismuthinite structures are given in Table 3, and the ADP are given in Table 4. Tables with the full anisotropic ADPs are deposited.

As in [1], related sulfides without the lone electron pair will be compared to bismuthinite, in order to gain insight in the pressure effect on the lone electron pair. The related sulfides are  $\text{Dy}_2\text{S}_3$ , and  $\text{U}_2\text{S}_3$  but also a zero-pressure refinement of  $\text{Bi}_2\text{S}_3$  has been added to this study (see [1] for references). The values for these three structures have been plotted in a column to the left of the zero-pressure axis to avoid overlap. The convention used is that black points refer to high-pressure bismuthinite data, white points refer to high-pressure stibnite data and grey points are zero-pressure values for  $\text{Dy}_2\text{S}_3$ ,  $\text{Bi}_2\text{S}_3$  and  $\text{U}_2\text{S}_3$  (In Figs. 5, 6, 7, 8). The effective ionic radii of the trivalent ions  $\text{Sb}^{3+}$ ,  $\text{Dy}^{3+}$ ,  $\text{Bi}^{3+}$  and  $\text{U}^{3+}$  are 0.76, 0.91, 1.03 and 1.03 Å, respectively (Shannon 1976).

## Principal features

Similar to stibnite, the crystal structure of bismuthinite consists of tightly-bonded rods  $\text{Bi}_4\text{S}_6$  in a herring-bone arrangement (Fig. 3). All Bi atoms have three short, strong bonds to sulfur, accompanied by two to three longer and weaker bonds, whereas their lone electron



**Fig. 5** Calculated inter-rod volume ( $V_{\text{lone}}$ ) and rod volume ( $V_{\text{rod}}$ ). *Black squares* represent the bismuthinite pressure data. *White squares* represent stibnite pressure data, and the *grey squares* represent zero pressure data for  $\text{Dy}_2\text{S}_3$ ,  $\text{Bi}_2\text{S}_3$  and  $\text{U}_2\text{S}_3$ . The curves are obtained by fitting a BM3 equation of state to the volumes

pairs are oriented into the inter-rod space. As already ascertained by the structure determinations quoted above, the activity of lone electron pairs in  $\text{Bi}_2\text{S}_3$  is less pronounced than in  $\text{Sb}_2\text{S}_3$ , with lesser differences between various categories of M–S distances as a consequence.

Unlike stibnite, bismuthinite forms a complete solid solution with  $\text{CuPbBiS}_3$  and is a parent structure to a series of superstructures resulting from a low-temperature dissociation of the  $\text{Bi}_2\text{S}_3$ – $\text{CuPbBiS}_3$  solid solution. It is also related to the homeotypic  $\text{M}_2\text{S}_3$  sulfides of the elements without a lone electron pair effect—Nd, Dy and U.

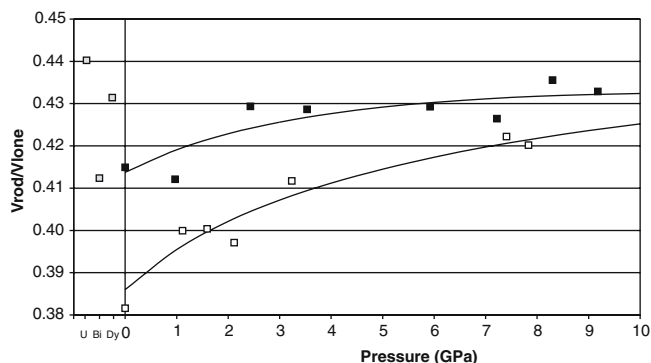
**Table 3** Atom positions

Press. (GPa)	0.0001	0.97	2.43	3.53	5.92	7.22	8.30	9.18
<b>Bi1</b>								
<i>x</i>	0.0164(2)	0.0123(2)	0.0077(2)	0.0049(2)	−0.0004(2)	−0.0029(2)	−0.0046(2)	−0.0056(2)
<i>z</i>	0.6745(2)	0.6746(2)	0.6744(1)	0.6744(2)	0.6744(2)	0.6744(2)	0.6746(2)	0.6748(2)
<b>Bi2</b>								
<i>x</i>	0.3406(3)	0.3381(3)	0.3347(2)	0.3331(3)	0.3292(2)	0.3275(2)	0.3263(2)	0.3253(2)
<i>z</i>	0.4661(2)	0.4658(2)	0.4660(1)	0.4663(2)	0.4668(2)	0.4674(1)	0.4674(2)	0.4677(2)
<b>S1</b>								
<i>x</i>	0.0494(16)	0.0503(16)	0.0526(12)	0.0527(15)	0.0523(14)	0.0493(13)	0.0534(14)	0.0529(14)
<i>z</i>	0.1311(11)	0.1266(11)	0.1294(9)	0.1280(11)	0.1297(10)	0.1296(9)	0.1301(10)	0.1296(10)
<b>S2</b>								
<i>x</i>	0.3773(17)	0.3742(16)	0.3744(13)	0.3737(15)	0.3754(13)	0.3745(13)	0.3752(13)	0.3724(13)
<i>z</i>	0.0604(12)	0.0603(12)	0.0591(9)	0.0610(11)	0.0599(10)	0.0607(10)	0.0613(10)	0.0602(11)
<b>S3</b>								
<i>x</i>	0.2165(16)	0.2171(17)	0.2200(12)	0.2211(17)	0.2207(13)	0.2232(14)	0.2225(14)	0.2223(15)
<i>z</i>	0.8069(12)	0.8062(12)	0.8033(9)	0.8026(13)	0.7983(10)	0.7990(10)	0.7966(10)	0.7963(10)

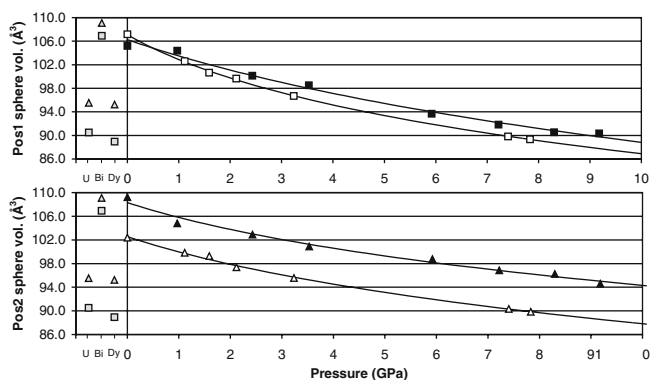
The *y* coordinate is 0.2500(0) for all atom positions in the table

**Table 4** Atomic displacement factors

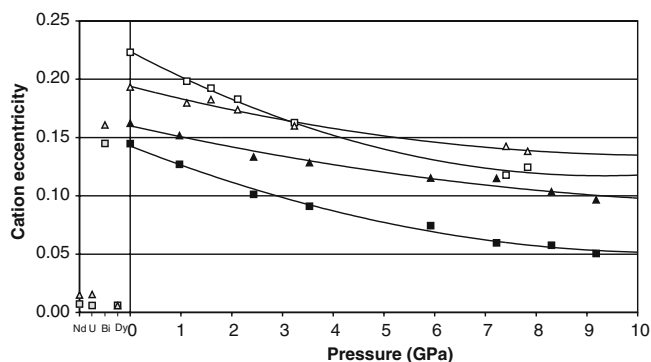
Press. (GPa)	0.0001	0.97	2.43	3.53	5.92	7.22	8.30	9.18
<b>Bi1</b>								
$U_{\text{eq}}$	0.0204(10)	0.0192(11)	0.0168(9)	0.0173(11)	0.0161(10)	0.0160(9)	0.0157(9)	0.0155(9)
<b>Bi2</b>								
$U_{\text{eq}}$	0.0210(10)	0.0223(11)	0.0200(8)	0.0209(10)	0.0182(10)	0.0177(10)	0.0167(9)	0.0171(10)
<b>S1</b>								
$U_{\text{iso}}$	0.019(3)	0.014(3)	0.015(2)	0.012(3)	0.014(3)	0.011(2)	0.012(3)	0.013(3)
<b>S2</b>								
$U_{\text{iso}}$	0.022(3)	0.016(3)	0.017(2)	0.014(3)	0.015(3)	0.016(3)	0.014(3)	0.015(3)
<b>S3</b>								
$U_{\text{iso}}$	0.019(3)	0.018(3)	0.015(2)	0.021(3)	0.012(3)	0.013(2)	0.015(3)	0.013(3)



**Fig. 6** Observed ratio between the rod volume and the lone electron pair volume. *Black squares* represent the bismuthinite pressure data. *White squares* represent stibnite pressure data, and the *grey squares* represent zero pressure data for  $\text{Dy}_2\text{S}_3$ ,  $\text{Bi}_2\text{S}_3$  and  $\text{U}_2\text{S}_3$



**Fig. 7** Fitted sphere volume for the two seven-coordinated cation positions. *Squares* indicate position 1 and *triangles* position 2. *Black symbols* represent the bismuthinite pressure data. *White symbols* represent stibnite pressure data, and the *grey symbols*



**Fig. 8** Cation eccentricities for the two seven-coordinated cation positions. *Squares* indicate position 1 and *triangles* position 2. *Black symbols* represent the bismuthinite pressure data. *White*

## Modules

Similar to [1], the crystal structure of bismuthinite has been divided into rod volumes, comprising the four columns of square pyramids in the  $\text{Bi}_4\text{S}_6$  rods, and the inter-rod volume, defined as the volume influenced by lone electron pairs. This treatment allows us to separate the bulk effects of pressure on these qualitatively different bonding environments. As illustrated in Fig. 4, this division is based on the geometry of anion framework.

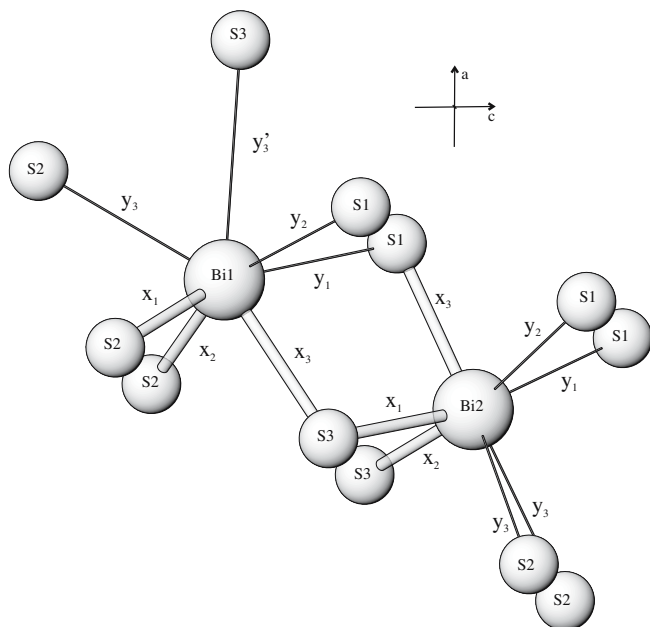
Figure 5 illustrates a much larger compressibility of the inter-rod volume compared to the rod volume. The lone-pair compressibility for  $\text{Sb}_2\text{S}_3$  is initially more pronounced, gaining and maintaining a difference of about  $3 \text{ \AA}^3$  for pressures up to 10 GPa. The rod volume of  $\text{Sb}_2\text{S}_3$  is smaller by about  $3 \text{ \AA}^3$  already at ambient pressure, and maintains this difference up to and through 10 GPa.

The ratio between the rod volume and the interrod volume changes much more for  $\text{Sb}_2\text{S}_3$  than for  $\text{Bi}_2\text{S}_3$  (Fig. 6). The left-hand side of Fig. 6 shows that with rising pressure the ratio in  $\text{Bi}_2\text{S}_3$  approaches that in  $\text{U}_2\text{S}_3$  and  $\text{Dy}_2\text{S}_3$ , two compounds without steric lone electron pair activity.

## Coordination polyhedra

The two independent Bi positions, Bi1 at the margin of the  $\text{Bi}_4\text{S}_6$  ribbon and Bi2 placed around the centre of the ribbon, differ in their coordination and pressure behaviour. Both are seven-coordinated but, in relation to the  $4 \text{ \AA}$  axis, Bi1 polyhedron is a monocapped “lying” prism whereas Bi2 a similar “standing” prism. The total volume of a sphere circumscribed to the coordination polyhedron of Bi1 is very close, and develops nearly parallel to, that of Sb1 in stibnite (Fig. 7). However, the values for the no. 2 position are markedly higher for bismuth. The more pronounced compressibility of Sb1 up to about 3.5 GPa is the only important difference between  $\text{Sb}_2\text{S}_3$  and  $\text{Bi}_2\text{S}_3$ .

The same trend is obvious from the plot of cation eccentricity (Fig. 8) expressed as a fraction of sphere radius (Balic-Zunic and Makovicky 1996). When comparing the Sb and Bi cation eccentricity with those of U and Dy, it is clear that the structure type alone does not force eccentricity upon the cations involved, but it is the lone electron pair of Sb and Bi that generates the eccentricity of cation positions in these sulfides. Cation eccentricity is therefore a very good parameter to quantify the lone electron pair activity. Results show that the compression mechanism in  $\text{Sb}_2\text{S}_3$  and  $\text{Bi}_2\text{S}_3$  up to 10 GPa is of the same kind. The stereo-chemical expression decreases, but it is still visible at the highest applied pressures. For Sb it is at all pressures more expressed than for Bi. The examination of trends (see especially Figs. 6, 8) shows that the general structural characteristics of  $\text{Sb}_2\text{S}_3$  only at 5 GPa resemble

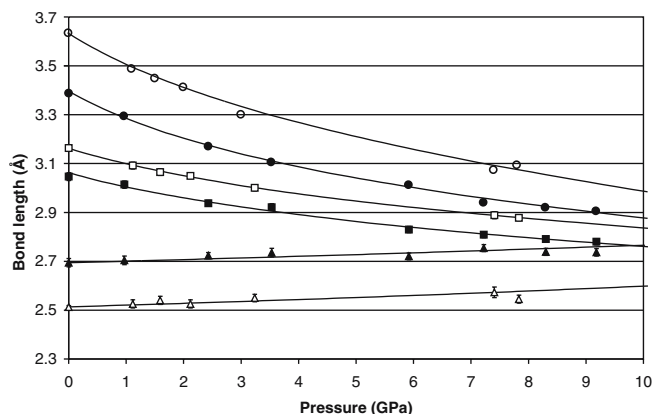


**Fig. 9** Bond pairs as defined for the two coordination polyhedra. Bond pairs  $y_3:x_3$  are composed of a short  $x_3$ -bond and a longer opposing  $y_3$ -bond

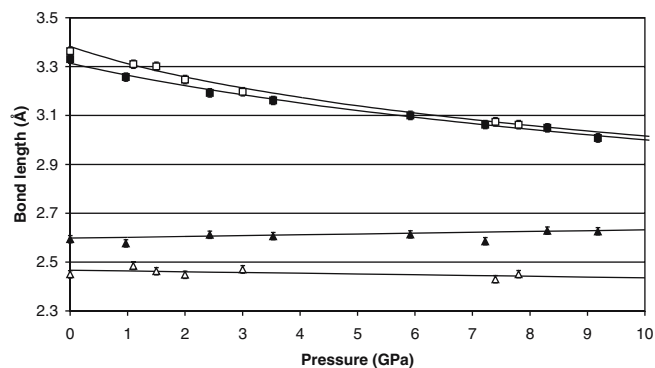
completely those of  $\text{Bi}_2\text{S}_3$  at room pressure. Comparison of Figs. 5, 6 and 7 with Fig. 8 suggest that the distortions of the structure motif, introduced by the accommodation of the lone electron pair, are largely eliminated at the pressures where the lone electron pair activity is sufficiently reduced.

### Bond lengths

Figures 9, 10, 11 demonstrate the influence of pressure on selected individual Bi–S bonds in the coordination polyhedra of the Bi1 and Bi2 positions and offer a

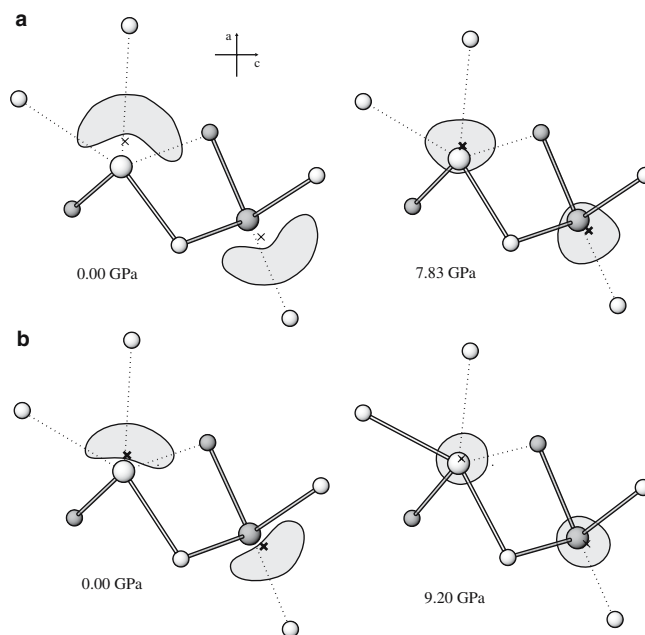


**Fig. 10** Plot of the  $y_3'$ ,  $y_3$  and  $x_3$  bonds for cation position 1. *Black symbols* represent the bismuthinite data and *white symbols* represent stibnite data. *Circles, squares and triangles* represent the  $y_3'$ ,  $y_3$  and  $x_3$  bonds, respectively



**Fig. 11** Plot of the  $y_3:x_3$  bond pair for cation position 2. *Black symbols* represent the bismuthinite data and *white symbols* represent stibnite data. *Squares and triangles* represent the  $y_3$  and  $x_3$  bonds, respectively

comparison with the behaviour of Sb1 and Sb2. The bonds selected are the apical short bonds  $x_3$  of the square coordination pyramids  $\text{MS}_5$  and the opposing long distances, below the base of the pyramid, denoted as  $y_3$  (Fig. 9). Both cation positions show a similar trend: as the long  $y_3$  distances show a non-linear decrease with increasing pressure, the short apical  $x_3$  distances show a slight linear increase in the entire range of pressures studied. Corresponding trends in the remaining pairs of opposing bonds in each polyhedron contribute to the trend in eccentricities shown in Fig. 8. Trends observed in  $\text{Sb}_2\text{S}_3$  are the same, but the



**Fig. 12** Schematic model explaining the changes in coordination for Sb atoms in stibnite (a) and the changes in coordination for Bi atoms in bismuthinite (b). The *cross* marks the position of the centroid calculated using the procedure of Balic-Zunic and Makovsky (1996). For atom labels, see Fig. 9

difference in bond lengths of the  $x_3$  and  $y_3$  bonds/distances is more pronounced. Thus, the equalisation of the  $x_3$  and  $y_3$  bond length for Bi1 at about 10 GPa will occur for Sb1 at much higher pressures, if at all. The additional, longest Bi1–S3 distance ( $y'_3$ ) is nearly parallel to the initially 'softest' [100] direction. It is the fastest decreasing distance in the  $M_2S_3$  structure when pressure increases. The  $y'_3:x_3$  trend copies in principle the  $y_3:x_3$  trend for Bi1 but with a double decrease in the  $y'_3$  distance. The equalisation of the  $x_3$  and  $y'_3$  distances can be predicted at about 13 GPa.

### Lone electron pairs

The seemingly contradictory behaviour of short M–S bonds with pressure is typical for the lone electron pair elements As, Sb and Bi. Berlepsch et al. (2001) demonstrated the hyperbolic interdependence of the opposing bond lengths in the coordination polyhedra of these  $M^{3+}$  cations. Increase in the long M–S distance leads to the decrease in the opposing bond length along a hyperbolic trajectory in the plot of opposing bond distances, and vice versa. This is obviously true also for the case of increasing pressure although the hyperbolic trend at any pressure differs from that at ambient conditions (Lundegaard 2003).

A qualitative explanation of this effect is illustrated in Fig. 12. The customary shape of the volume occupied by the lone electron pair is shaded in this picture and the centroid of the relevant coordination polyhedron is indicated by a cross. Assignment of the lone electron pair volumes is supported by semiquantitative calculations using the ABINIT package (Gonze et al. 2002) based on density functional theory using pseudopotentials and a plane wave basis (Lundegaard 2003). The very asymmetric configuration in  $Sb_2S_3$  and  $Bi_2S_3$  at ambient conditions (for differences see Fig. 12) becomes much more symmetric at high pressure, with the centroids approaching closely the cation sites. By implication, the loci of the lone electron pair in the coordination polyhedra follow, enveloping partly the cations. Thus, their repulsive action on the S atoms situated at the long M–S distances decreases, whereas their influence on the S atoms which are tightly bonded to M, increases.

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