#### **REVIEW**

# **A critical review on recent developments and applications of microchannels in the field of heat transfer and energy**

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#### **Abstract**



There is a rapid movement towards miniaturization in the field of micro-electronics, medical, defence, and space applications as well as an increase in thermal load density in the field of solar power. This has resulted in the requirement for technologies to be developed which enable the rapid removal of high thermal load from the components for effective and safe operation. Microchannel cooling has been one of the areas which has been investigated to provide the solution as required. This paper aims to looks at the different types of microchannels being developed, review the performance of microchannels being developed with different working fluids, explore the various structures utilized of microchannels and explore the use of microchannel in the various applications with regards to field of thermal management. Finally, future needs are proposed for extending the research and enlarging its application fields. This review paper serves as guidance for researchers to design and predict the performance of microchannel heat sinks (MCHS).

## **1 Introduction**

In the recent times there is a growing push towards miniaturization in the field of electronics. This combined with the high-power draw has created situations where the specific heat flux is very high. For example, computer processors typically have a thermal design power (TDP) of 100 W and even upwards of 250 W [\[1,](#page-35-0) [2](#page-35-1)] which is dissipated over an area of less than  $20 \text{ cm}^2$ , thus resulting in a specific thermal flux of about 10-15 W/  $\text{cm}^2$ . In the application of power electronics, the specific thermal flux is in the order of 1000 W/  $\text{cm}^2$  [[3](#page-35-2)]. In the field of renewable energy, the specific thermal flux is, in the applications of concentrator photo-voltaics, in the order of 1370 kW/m<sup>2</sup> [[4\]](#page-35-3) with potential to reach values greater than  $10000 \text{ kW/m}^2$  [\[4](#page-35-3)]. The issues due to limitation of heat dissipation that arise in the above cases have directly led to the push towards development of new and novel solutions. One such method that has garnered a lot of attention is the use of microchannels.

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Microchannel based heat sinks have been studied in various configurations to improve the heat dissipation characteristics of cooling solutions employed in a wide variety of applications which content with high heat flux dissipation issues. They have been used extensively in the electronics industry; medical, consumer grade micro-electronics, military & space applications, refrigeration & cryogenic applications, solar cells to name a few [[5,](#page-35-4) [6\]](#page-35-5). Microchannels can be defined as elements which can be used for heat transfer where the classical theories cannot accurately establish the friction factor and heat transfer. Alternatively, it can also be defined a microscale system as one whose typical phenomena are typically not observed in a macro system [\[7](#page-35-6)]. There has been some debate regarding the exact definition of what constitutes a microchannel. However, in general, they can be described as fluid flow paths which have a hydraulic diameter less than 1 mm [\[7](#page-35-6), [8\]](#page-35-7). We can illustrate the effectiveness, advantages, and the rough theory behind the use case of single-phase flow microchannels by applying the classical relationship (1) developed for channels in macroscopic scale. Here *h* is the convective heat transfer coefficient of the flow, *d* is the hydraulic diameter, and *k* is the thermal conductivity of the fluid.

$$
Nu = \frac{h \cdot d}{k} = const \Rightarrow h \propto \frac{1}{d}
$$
 (1)

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Considering a laminar flow which is fully developed and with a constant Nusselt number, implying that the HTC (heat transfer coefficient) is mathematically inversely proportional to the diameter [[8\]](#page-35-7). This is an indicator of the performance potential of microchannel systems. Microchannels have been shown to offer measurable benefits over other heat transfer systems. Microchannels have been shown to have superior heat transfer performance, far more compact and lightweight, reduced heat sink size, low rate of coolant flow, larger available heat transfer area per unit fluid flow volume and uniform wall temperature distributions [\[9,](#page-35-8) [10\]](#page-35-9). Experimentation on microchannel systems have shown that they offer elevated heat dissipation capabilities with values exceeding  $10000 \text{ kW/m}^2$  which can be efficiently dissipated with the help of flow boiling regime via latent heat transport [[11](#page-35-10)].

The sections below, we attempt to summarize some of the different microchannel structures and geometric designs of microchannels popularly used. The advantages, disadvantages, and the suitability of different geometries in microchannels are elucidated. Different phase regimes used along with use of nanofluids in microchannels are also explored and the advantages, disadvantages and challenges faced in each listed. Applications of microchannels are also listed and progress in each domain is reviewed. Lastly, the challenges and future prospects for MCHS are offered. This review aims to be an effective guide for future advancement of high-performance MCHS.

## **2 Structure and geometric design of microchannels**

The structure and geometry of microchannels heavily influence the performance they offer. Extensive research has been done into gaining understanding of that mechanisms of heat transfer in microchannels. Effects of thermal boundary layer, fluid mixing, flow velocity etc. have been studied [\[5\]](#page-35-4). In order to reduce pumping losses and large pressure gradients, several geometries of microchannels have been explored concurrently. This paper aims to look at some of the widely used microchannel structures in both the single and multi-phase flows.

#### **2.1 Straight channels**

As the name suggests, straight cut microchannels are microchannels whose profiles are manufactured along a straight locus. The profiles themselves may be of different shapes.

Kumar and Kumar [\[12](#page-35-11)] carried out 3-D numerical simulations on rectangular MCHS with arc shaped grooves to examine the fluid flow and transfer of heat characteristics.



<span id="page-1-0"></span>**Fig. 1** Structure of MCHS [\[18\]](#page-36-2)

Groove depth along with the Reynold's number were varied and Nusselt number, Poiseuille number, and performance factor were analysed to compute the effect of groove structure and depth on the hydrodynamic and thermal characteristics of the microchannel. Grooves were found to result in the generation of pseudo secondary flows which had an impact in reducing the viscous forces in laminar region but had no effect with higher Reynold's numbers and actually reduced effective heat transfer. Law and Lee [\[13](#page-35-12)] conducted analysis comparing pressure and flow boiling and heat transfer characteristics in straight microchannels. FC-72 dielectric fluid was used, and results indicated a reduced pressure drop in straight finned microchannels as compared to oblique microchannel.

Alam et al. [[14](#page-36-0)] and John Mathew et al. [\[15\]](#page-36-1) conducted comparative analysis to characterize flow boiling heat transfer and pressure drop in micro gap and MCHS (microchannel heat sinks). While investigating micro gap heat sinks, the study showed that MCHS had superior performance with



<span id="page-1-1"></span>**Fig. 2** Structure of MPFHS [[18](#page-36-2)]



<span id="page-2-0"></span>**Fig. 3** Maximum temperature of heater surfaces plotted against fow rate for two heat sinks at Power of 48 W. [\[19\]](#page-36-5)

regards to heat transfer at small heat flux caused due to early formation of slug/annular flow. Balasubramanian et al. [[16,](#page-36-3) [17](#page-36-4)] investigated heat transfer during flow boiling, pressure drop and instabilities in straight and expanding microchannels. Observations indicated that pressure drop (lower by 30%), wall temperature fluctuations and was lower in expanding microchannels with greater observed heat transfer performance. Thin film evaporation was determined to be the predominant mechanism of heat transfer with high heat fluxes. In straight microchannels, lower heat transfer coefficients were observed when the pressure drop fluctuations amplitudes rose.

Jasperson et al. [[18\]](#page-36-2) conducted research comparing microchannel (MCHS) (Fig. [1](#page-1-0)) and micro-pin-fin heat sinks (MPFHS) (Fig. [2](#page-1-1)) focusing on the thermo-hydraulic performance & also considering the manufacturability. It was determined that MPFHS have superior performance (lower thermal resistance) at flow rates above 60g/min albeit with a greater pressure drop penalty (nearly double) as compared to MCHS. In terms of manufacturability, casting (for mass production) would yield a similar costing. However, for prototyping in which micro-end milling and micro-EDM are utilized, microchannels are the more cost-effective option as the tool path (thus machining time & tool life) is nearly a third that require for micro-pin-fin manufacturing.

Xia et al. [[19\]](#page-36-5) researched the characteristics of flow and heat transfer in rectangular and staggered complex corrugated microchannels experimentally as well as numerically. Pressure drop was found to be greater for rectangular microchannel heat sinks (RMCHS) as compared to the staggered complex corrugated channel microchannel heat sinks (CMCHS). However, heat transfer characteristics were superior in CMCHS as compared to RMCHS with the maximum and average temperatures being lower for higher flow rates. Figure [3](#page-2-0) shows variation of average temperature on heater surface with rate of flow for two heat sinks at 48W. Observations indicate that the average temperature reduces with a rise of rate of flow for both the heat sinks. The maximum temperature of CMCHS was below that observed in RMCHS when flow rate was greater than 80 ml/min. However, the reverse was true when flow rate was less than 80 ml/min. The average temperature observed in CMCHS in comparison with RMCHS is lower by approximately 1.2 °C.







<span id="page-4-0"></span>**Fig. 4** Zigzag microchannel of ZSMHS: (**a**)  $\alpha = 30^{\circ}$ , (**b**)  $\alpha = 45^{\circ}$ , (**c**)  $\alpha = 60^{\circ}$ , (**c**)  $\alpha = 90^{\circ}$  [[25](#page-36-11)]

## **2.2 Wavy channels**

It has been determined that utilization of wavy walls (or corrugations) in heat exchangers can improve characteristics of heat transfer. This is attributed to superior mixing of the fluid by the wavy surfaces. This is even more important in the current scenario where even greater levels of improvement in heat exchanger performance is pursued to meet the ever-increasing industry requirements and calls for greater heat transfer performance.

While Mondal et al. [[23](#page-36-9)] studied the fabrication of wave microchannels, Aliabadi et al. [[24\]](#page-36-10) researched the flow and heat transfer characteristics observed in chevron channel MCHS using numerical simulations. The results were promising and showed a noticeable increase in thermal performance and reduced thermal resistance. Peng et al. [[25\]](#page-36-11) examined the performance of zigzag serpentine microchannel heat sinks (ZSMHS) (Fig. [4](#page-4-0)) by experimentally determining the heat transfer characteristics. They found that lower incidence angles, lowered the drop in pressure and friction coefficient with the lowest values being observed at 30° and the maximum at 90°. Also, the reduction in incidence angles improved the heat transfer performance (heat transfer coefficient & thermal resistance).

G.D. Xia et al. [\[26\]](#page-36-12) researched the effects of different geometric structures in MCHS on the heat transfer and fluid flow characteristics with numerical techniques. Optimal geometric parameters for greatest heat transfer and flow distribution were determined by studying the effects of different types of inlet and outlet configurations, header shapes and along with different microchannel shaped (Fig. [5](#page-5-0)). It was determined that average temperature and maximum temperature of the heat sink A was higher as compared to the values determined for heat sink B and C.

Zhou et al. [[27\]](#page-36-13) performed optimization of geometric parameters of a wavy wall (Fig. [6](#page-6-0)) by combining response surface methodology (RSM) with finite volume method (FVM) simulation. β (Comprehensive heat transfer index) was used to investigate if the augmentation of heat transfer offsets the rise in the drop in pressure. The impacts of amplitude and wavelength of wave, Reynolds number and β were investigated. It was observed that as the Re numbers increases proportionally with the convective HTC. It was observed that heat transfer was up to 2.8 times greater in wavy microchannels as compared to straight microchannels. An increase of Re number results in increase of pressure drop for all geometries with a greater drop in pressure in wavy MCHS. Using the aforementioned methods, it was determined that the optimal amplitude was 40 μm and wavelength 100 μm.



**S.N. Reference Enhancement Solution** 



**Operating** 

**Dimensions Working** 

## **2.3 Pin fins**

Structures used in Micro pin fin heat sinks (MPFHS) have demonstrated the ability to disrupt and also re-develop boundary layers, while also increasing flow mixing via vortices [[9](#page-35-8)]. Feng et al. [[29](#page-36-15)] conducted a numerical investigation of the geometrical parametric effects of circular MPFHS to effects on heat transfer and fluid flow in an interrupted MCHS. The author worked on an interrupted microchannel with double circular pin-fins in each microchamber (IMCDCP). The design aimed to fuse the advantages of microchamber and circular pin-fin in the enhancement of heat transfer. Parameters such as diameters, spacing and height were altered and changes in the Nusselt's and Reynold's numbers were recorded. IMCDCP was found to improve heat transfer and reducing wall temperature. As compared to smooth microchannels, the IMCDCP with height of 0.08mm, pin-fin diameters of 0.12 mm, channel width of 0.55 mm operating under conditions yielding Reynold's number of 530, resulted in a 42% heat transfer performance improvement over smooth microchannels setup.

**Enhancement Efect**

Ferster et al. [[30\]](#page-36-16) investigated the effects of spacing, geometry and fin count of pin-fins in additively manufactured MPFHS. The arrays of triangular, star, and spherical pin-fins (Fig. [7\)](#page-8-0) were fabricated using direct metal laser sintering (DMLS) technique. Results indicated that triangular and cylindrical geometries had the greatest values for augmentation of heat transfer. Streamwise spacing had a small but measurable effect on friction factor and a direct correlation with performance with regards to heat transfer (with decreasing spacing).

Jasperson et al. [\[18\]](#page-36-2) performed comparative studies between MCHS and MPFHS (Fig. [8\)](#page-8-1) taking into account thermo-hydraulic performance as well as its' manufacturability. Above 60 g/min, the thermal resistance of HPFHS was

<span id="page-5-0"></span>



<span id="page-6-0"></span>**Fig. 6** Schematics of (**a**) MCHS, (**b**) straight MCHS and (**c**) wavy MCHS [[27](#page-36-13)]

observed to fall below that of MCHS. The more complicated flow and strong vortices in the wake at high flow rate was attributed. Thus, the HPFHS can be chosen in such operating conditions. While methods for prototyping like micro-EDM, micro-end-milling etc. result in higher manufacturing costs, methods used in mass manufacturing such as casting and extrusion result in cost parity. Moreover, ongoing research in spindle speeds and feed rates suggests that cost for prototyping itself would reduce, thus resulting in comparable costing during prototyping phase as well.

Lan et al. [[31\]](#page-36-17) determined the hydrothermal performance & entropy generation of rectangular microchannels with offset and truncated pin-fins with variable fluid properties. As observed in earlier cases, as compared to smooth MCHS, MPFHS enhance the performance with regards to heat transfer. This was attributed to extension of area available for transfer of heat, redevelopment of thermal boundary layer and generation of vortices. However, there is an increase in resistance to fluid flow. There is a correlation between the increase in pin-fin length and the increase in resistance to heat transfer and increased flow. While offset in pin-fins can increase heat transfer up till a point, beyond which there is a reduction (Fig. [9](#page-9-0)). In Fig. [9](#page-9-0) for MC–0.75–0, no offset value exists for adjacent pin-fins, thus the equal area was available for fluid flow on either side of each pin-fin. With offset, two adjacent between pin-fins ( $W<sub>rc</sub> > 0$ ), on either side of each pin-fin, different sizes of flow passage were formed. Thus, greater volume of fluid passed through the side with the larger flow passage. Values of PEC were found to vary from 1.00 to 1.43. The highest value of PEC achieved was 1.43 for microchannel MC–0.75–0.6 ( $W_{rc} = 0.6$ ) at Re = 530.

Soleymani et al. [[32](#page-36-18)] worked on a hybrid design viz microchannels with pin fins (rounded rectangular & NACA 0024 air foil) at hotspot region (Fig. [10](#page-11-0)). Different pitch angles were also looked at for the air foil shape relative to fluid flow direction (Fig. [11](#page-11-1)). It was seen that rectangular pin fin and higher angles of air foil pin-fin had lower thermal resistance albeit with greater pumping power requirements. Tillius et al. [[33](#page-36-19)] conducted optimization studies of short micro pin-fins in MCHS.





## **2.4 Oblique**

Oblique microchannels are those which have straight microchannels parallel to the direction of the flow and have (secondary) oblique cuts at an angle to the original (Fig. [12](#page-11-2)). Oblique fins have several advantages. They can augment heat transfer by modulating the flow, and by breaking the boundary layer and causing it to be reinitialized periodically thus reducing the thermal boundary layer thickness. Also, the secondary flows created by the obliquely positioned channels improve mixing of the fluid increasing the HTC by as much as 80% (Fig. [13\)](#page-12-0) [[39–](#page-36-25)[42](#page-36-26)].

Lee et al. [[39](#page-36-25)] researched the enhancement of thermal dissipation in MCHS with the utilization of oblique fins. Using numerical simulations, it was determined that by adjusting the sizing of the secondary channels, an adequate supply of flow (in this case, 12%) could be diverted so as to disrupt the boundary layer whilst causing a negligible pressure to drop. Ansari et al. [\[43](#page-36-27)] performed comparative and optimization studies using numerical techniques on oblique and rectangular fin MCHS both with parallel and offset fins. It was found that oblique-fin offset MCHS have the lowest thermal resistance at the equivalent pumping power. Law and Lee [[44\]](#page-36-28) conducted comparative (experimental) studies between straight



<span id="page-8-0"></span>**Fig. 7** 2-Dimensional models for each pin shape [\[30\]](#page-36-16)

and oblique finned (10°) microchannels to analyse temperature and pressure instabilities. It was determined that the temperature and pressure instabilities present in RSMCs are generally mitigated in obliquely finned microchannels while also augmenting heat transfer characteristics. The improved flow stability observed is linked to the ability of oblique fins to reduce flow reversals. Law et al. [\[45\]](#page-36-29) conducted studies looking at the impact of altering the oblique angles (10°, 30°, 50°) on the pressure and flow boiling characteristics in oblique finned MCHS. Heat transfer was observed to rise with increase in oblique angle due to reduction of flow rates in the secondary channels. A considerable rise in pressure drop with rise in angle from 10° to 30° and marginal rise from 30 $\degree$  to 50 $\degree$  was seen. Lee et al. [\[46](#page-36-30)] investigated the use of obliquely finned microchannels for hotspot mitigation. A group of oblique fins with a dissimilar pitch and higher density were created at regions where hotspots were expected (Fig. [14\)](#page-12-1). This resulted in additional secondary flow and thus greater boundary layer redevelopment which provided more effective heat dissipation capability at region with high flux.

Lee et al. [\[47](#page-36-31)] performed a parametric study to enhance fluid flow and heat dissipation in obliquely finned MCHS. It



<span id="page-8-1"></span>**Fig. 8** MPFHS manufactured by micro-end-milling [[18](#page-36-2)]

was determined that the optimum performance was obtained using a channel width of 100 μm and an oblique angle of 27°. Mou et al. [[48\]](#page-36-32) researched the effects of flow migration in obliquely finned microchannel arrays on flow and heat transfer. As from other authors, heat transfer performance was determined to be affected by variations of secondary flow. Reynold's number was found to affect coolant migration, flow stability and heat transfer performance. With higher values of Re enhancing heat transfer for surfaces in secondary channels. Vinoth et al. [[49](#page-36-33)[–51](#page-37-0)] investigated the effects of various channel cross section (square, semicircular and trapezoidal), as shown in Fig. [15](#page-14-0), on the heat dissipation and flow characteristics of obliquely finned MCHS. Trapezoidal cross section microchannels (as compared to square and semicircle respectively) were found to have the highest Nusselt number increased by 8.54% and 26.4% and rate of heat dissipation by increased 3.13% and 5.87% albeit with an increased pressure drop (due to higher friction factor) of by 24% and 16.8%. Addition of nanoparticles increased the heat transfer rate by 4.6%.

Lan et al. [[52](#page-37-1)] performed an experimental and numerical examination on the temperature uniformity of different oblique MCHS. The types investigated were variable density alternating obliquely truncated microchannel (AOT-MC), traditional rectangular straight microchannel (RS-MC), and varying density alternating obliquely truncated microchannel with oblique fins (AOTF-MC) as shown in Fig. [16.](#page-15-0) The enhanced design AOTF-MC showed an increase of up to 63.23% and 111.59% for the Nusselt number and 40.20% and 55.16% reduction for the temperature in comparison with the AOT-MC and the RS-MC, respectively.



<span id="page-9-0"></span>**Fig. 9** (a) Velocity profile and (b) temperature profile for microchannels at various  $W_{rc}$  at  $Re = 397$  and  $H_{rc} = 0.75$  (y = 0.2 mm) on x–z plane [[31](#page-36-17)]

Panse et al. [\[53](#page-37-2)] conducted a study on an alternating offset oblique microchannel (Fig. [17\)](#page-16-0) to determine its thermoshydraulic performance using a numerical parametric study. Over a range of Reynold's numbers (200-800), 3 parameters; relative oblique channel width  $(\alpha)$ , and oblique angle  $(\theta)$ , relative fin offset width  $(β)$ , on thermo-hydraulic performance (THP) were evaluated. The optimal geometry was found,  $\alpha$ =0.5,  $\theta$ =60°, and  $\beta$ =0.25, obtained the maximum THP of

2.41 at Re=800. Far et al. [\[54\]](#page-37-3) studied the impact of variation of pin-tip clearance on the oblique finned microchannel performance (numerically) with a nano encapsulated phase change material (NEPCM) slurry at different concentrations. Results indicated that NEPCM slurry enhanced the cooling performance but increased the Euler number. Tip clearance ratio of 0.2 - 0.375 with NEPCM slurry and 0.16-0.26 with water were found to be optimal.





#### **2.5 Porous**

Porous structures can be introduced in MCHS via surface structures or with the construction of the MCHS itself in a porous manner. Introduction of porous structures has shown to greatly improve the performance of the microchannels [[55\]](#page-37-4). The porous structure provides sites for nucleation and subsequent growth while also increasing area available for heat transfer. This reduces the level of wall superheat for boiling initiation [[9](#page-35-8)]. Sarafan et al. [\[56\]](#page-37-5) numerically examined mass transfer and thermal dissipation during fluid flow (non-Newtonian power law) in a porous MCHS. It



<span id="page-11-0"></span>**Fig. 10** Microchannel pin-fn hybrid heat sink confguration [[32](#page-36-18)]

was determined that with rising power index, as the fluid tends to thicken and the viscosity increases and thus the shear stress increases, there is a reduction of heat transfer rate. Li et al. [[57\]](#page-37-6) determined that convective heat transfer was greatly improved with porous microchannels. This was attributed to the disruption and redevelopment of the thermal boundary layers which was in turn caused by the intensified fluid mixing in porous regions. Dehghan et al. [\[58,](#page-37-7) [59](#page-37-8)] sought to analytically determine the heat transfer performance (HTP) for porous media filled MCHS. To widen the scope of application, several factors were considered (effects of the porous medium shape parameter, the conduction heat transfer within the walls, the slip flow regime, the heat transfer amongst the solid and fluid phases of the porous material, and internal heat generations within the two phases of the porous material). It was determined that using hyper-porous materials greatly enhance HTP. Negligible effects of wall conduction resistance, especially in slip flow regime, on HTP have been deduced. Haddad et al. [\[60\]](#page-37-9), using numerical techniques, investigated the development of free-convection gas flow in a vertically oriented filled porous medium open-MCHS. It was determined that skin friction, by using modified extended Darcy-Brinkman-Forchheimer model, increased by decreasing Knudsen number and Grashof number, increasing the Darcy number. Also, it was seen that HTC was found to decrease with increase in Knudsen number, in thermal conductivity ratio, reduction in



<span id="page-11-2"></span>**Fig. 12** Plan view of MCHS with oblique fns [[39](#page-36-25)]

Darcy number, Grashof Number and Biot number. Jia et al. [[61\]](#page-37-10) conducted experimental studies to compare flow boiling and pressure drop characteristics in porous wall (PW) and rectangular (Rec) MCHS. PW-MCHS, like in other studies, have a lower temperature superheat. CHF of PW MCHS increase with mass flux and delay premature dryout in comparison to Rec-MCHS. The CHF rise can be attributed to wicking effects created by pin-fin arrangement. Mondal and De [\[62\]](#page-37-11) attempted to quantify mass transfer in the porous microchannel. Permeation was found to cause rise in mass transfer coefficient by a factor of 5 as compared to impervious walled conduits.

Various configurations of porous materials have also been studied. Zargartalebi et al. [[63\]](#page-37-12) examined the flow dynamics and thermal dissipation characteristics in partially porous pin finned (in in-line and staggered configurations) MCHS. It was determined that as the height of the porous media reduced, the flow through the medium was by-passed, more so in the staggered pin-fin configuration than the inline. With higher height of porous media, the reverse is true, that is staggered configuration outperforms the inline configuration.

<span id="page-11-1"></span>





<span id="page-12-0"></span>**Fig. 13** Local HTC profle for microchannel heat sinks [\[39\]](#page-36-25)

The friction ratio of staggered over in-line configuration, at a critical porous height, was found to suddenly increase indicating the forced flow through the medium.

Deng et al. [[64](#page-37-13)] looked to characterize flow boiling observed in porous MCHS with re-entrant microchannels. Use of traditional metal sintering fabrication techniques to manufacture  $\Omega$ -shaped re-entrant microchannels was done (Fig. [18](#page-16-1)). Comparisons with solid microchannels showed a significant wall superheat indicating lower thermal impedance, lower boiling instabilities and a 100% - 400% increase in HTC. At low heat fluxes, nucleation boiling governed heat transfer mechanism while at high thermal loads, forced convective boiling which is linked with thin film evaporation contributed greatly to thermal transfer. Hung et al. [[65\]](#page-37-14) numerically investigated the effects of channel outlets enlargement (Fig. [19](#page-17-0)) on thermodynamic performance of porous MCHS. It was determined that



<span id="page-12-1"></span>**Fig. 14** Design of Heat sink for enhanced variable fn pitch equipped MCHS for single hotspot [\[46\]](#page-36-30)

although a pressure drop was accompanied by a higher Nusselt number, it could be mitigated by raising either the width enlargement ratio or height enlargement ratio of the channel output. Also, the heat transfer effectiveness increased with the increase of the ratio, for the same pumping power. Lu et al. [[66](#page-37-15)] studied ways to incorporate wavy and porous designs (Fig. [20\)](#page-17-1) into one to lower drop in pressure and reduce thermal resistance simultaneously. Pressure drop decrease was attributed to a combined effect of permeation and slip effects of the fluid. Heat transfer enhancement was credited to enhanced mixing due to Dean vortices, elongated flow route due to increase in equivalent channel length and forced permeation due to impingement.





# **2.6 Nanostructures**

As seen in prior examples, an increase in surface area has corresponded to a rise in the HTC observed. Nanostructures offer a wide variety of unique properties; large specific area, high thermal conductivity, wettability manipulation etc [\[9](#page-35-8), [68](#page-37-17)].

Ghosh et al. [[69\]](#page-37-18) used facile fabrication method to manufacture nanostructures on microchannels to improve flow boiling heat transfer. Sharp needle like superhydrophobic nanostructures of CuO were formed on surface of microstructures using a simplistic and self-regulating chemical oxidation technique. Like in previously discussed studies,

<span id="page-14-0"></span>



the authors found an appreciable increase in performance of heat transfer, with a reduced pressure drop as well as reduced average amplitude of fluctuations as compared to PW-MCHS. Existence of a capillarity-fed thin-film evaporation regime in NSM was determined which as well was not detected in the case of PW-MCHS. Nagayama et al. [\[70\]](#page-37-19) investigated the applications of surfaces with nanostructure in parallel-(SS) plate microchannel for augmentation of thermal dissipation. Four cases (Fig. [21](#page-18-0)) were examined; Ni nanostructure plated SS, Ni-St nanostructure plated SS, Ni-St and alumina plated SS and FeCl<sub>3</sub> and fluoride etched SS. Nanostructures of 1μm layer thickness of approximately 50 nm are produced amongst the microscale structures that ranged from 1000 nm to 3000 nm. The larger contact angle (Fig. [22](#page-18-1)) was found for case 1, as compared to the bare surface, while the surface hydrophility was found to be improved for the other cases. The hydrophilic nanostructured surfaces obtained higher HTC.

Alam et al. [[71\]](#page-37-20) researched to determine the flow boiling characteristics in Silicon Nanowire (SiNW) MCHS while

comparing it's performance to rec-MCHS using HFE-7100 as coolant. The SiNW MCHS showed higher effective wall flux for the wall superheat, higher effective HTC, and lower drop in pressure (ergo lower pumping power) for same vapour quality, higher heat transfer (up to 400%) and lesser boiling instability (up to 70%) over a variety of mass flux rates. Flow visualization captured using high speed cameras (Fig. [23](#page-19-0)) showed that explosive bubble nucleation rather than discrete bubble nucleation was experienced in SiNW MCHS. Explosive boiling was followed by vapour bubbles coalescing to form annular flow.

Yang et al. [[72](#page-37-21)] studied the use of Nanowire-Coated Microchannels for the heat transfer enhancement during flow boiling using HFE-7000 as coolant. Enhancement of HTC of up to 344% along with a decline in required pumping power by 40% was observed. CHF was enhanced by 14.9% at mass flow rate of 1018 kg/m<sup>2</sup>•s was observed. However, the trend observed in CHF was non-monotonic and value reduced at elevated mass flux.





# **3 Solution approaches**

On the path to determine the performance of microchannels, researchers have opted for many different techniques often in conjunction with each other to arrive at their conclusions. The three main techniques used have been experimental, analytical & numerical. Experimental techniques utilize a physical setup with the equipment running at the target conditions. Several parameters need to be taken into consideration simultaneously to avoid a deviation from expected results. Inaccuracies in setup, as well as measurement have to be factored in. Also, there is a need to repeat the experiment to prevent any transients from causing deviations. Analytical studies require solving of theoretical equations with the requisite initial as well as boundary conditions (and assumptions if any) to arrive at a solution. Numerical methods utilize different numerical methods which are utilized to solve the theoretical equations with initial and

<span id="page-15-0"></span>

<span id="page-16-0"></span>

boundary conditions applied. The numerical methods, if employed have to be validated initially with relevant experimental data if it is going to be used to be used for simulation of unknown conditions.

In the paper we are going to examine some of the experimental setups used and advantages and challenges in each, analytical as well as numerical techniques utilized.

#### **3.1 Experimental**

In experimental methods, the microchannels are setup with a known and a predictable thermal load being supplied. Coolant is supplied at a known rate across the microchannel and temperature at the inlet and outlets measured. Depending upon the experimental requirements, the load can be varied, and the effects measured. A setup used by Mathew et al. [\[15\]](#page-36-1) is shown in (Fig. [24](#page-19-1)). The schematic represents the general setup which is used in many research studies albeit with a few differences. The pump, usually a positive displacement type pumps the fluid through a heat exchanger to the test section. A by-pass or pressure relief valve placed after the pump is used to discharge the fluid back to the reservoir in case of over pressure or emergency shut down or even to adjust the system flow rate [[79](#page-37-28)]. The heat exchanger maintains the passing fluid at a pre-set temperature. It is physically located as close to the test section as well as (*usually*) positioned after the pump to reduce the possibility of heat influx into the fluid due to increased piping requirements and to ensure that work input by pump does not alter the fluid temperature. The test section is supplied with a predefined and constant thermal load usually with the help of resistance heating coils. A power supply unit is used to energize the coils and maintain a constant load. The fluid after passing through the test section is sent to a reservoir via an air-cooled condenser. The condenser is substituted by a heat exchanger if the fluid exiting the test section has not undergone phase change. In several experimental studies, the phase change/ bubble formation/ flow studies in the test section need to



<span id="page-16-1"></span>**Fig. 18** SEM imagery of re-entrant porous MCHS: (**a**) MCHS cross section (**b**) Single re-entrant MCHS cross section (**c**) MCHS top view [[64](#page-37-13)]



<span id="page-17-0"></span>**Fig. 19** Diagram of porous MCHS and computational domain [[65](#page-37-14)]

be studied. To facilitate the same, the test section is usually covered by a transparent acrylic top cover and a camera (usually high speed) is fitted overhead to capture the flow. A data acquisition system (DAQ) is typically utilized to capture the different parameters (pressure, temperature, flow rate etc.) that are required. Pressure transducers, temperature probes, flow meters etc. are used to capture the pressure, temperature, and flow data.

Several variations of the above setup exist depending upon the requirements of the experiment. Gear pumps [[15,](#page-36-1) [80\]](#page-37-29) are used quite often used. Other types of pumps that may be used are HPLC [\[81](#page-37-30)], peristaltic [[82\]](#page-37-31), volumetric [\[83](#page-37-32)] etc. Target flow rates are usually 5 g/s - 35 g/s and are varied using a flow control valve and monitored using a rotameter/ flowmeter. A filter is generally used after the pump to prevent contaminants being driven to the test section.

Temperature monitoring is usually done using thermocouples. J-, K- & T- type thermocouples are often used. Each of the thermocouples utilized have a particular temperature range as well as an accuracy. Selection is done after analysing the approximate temperatures expected and knowing the required accuracy. The Table [1](#page-21-0) [[84](#page-37-33)] gives an indication of how the operating temperature limits and the uncertainty of measurement of each thermocouple type. Thermocouples are usually embedded within the test piece in holes drilled for the purpose (Figs. [25](#page-20-0) and [26](#page-20-1)).

Pressure measurement has been done absolute and differential pressure transducers [\[82](#page-37-31)]. Thermocouples and pressure transducers are coupled to a standalone data acquisition (DAQ) system which is able to read data from the thermocouple and record data to internal or external data storage unit against a time domain. Some researchers [[81\]](#page-37-30) use a dedicated DAQ while others use a data logger (like NI) [\[82](#page-37-31)] which can be interfaced to (and controlled from) a computer.

The test section houses the test piece (microchannel), a source of known heat flux and the requisite sensors measuring the performance of the MCHS. The microchannels are generally embedded within a Teflon or acrylic block which are shaped to directs flow through the MCHS while simultaneously reducing leakage heat flux to the surroundings. The inlet and outlet channels, also known as plenum, also house the pressure transducers. The top cover (e.g., Fig. [25\)](#page-20-0) can be made of a transparent plexiglass which will allow observation and recording of the experimentation using a camera. It must be ensured that leakage around the MCHS does not occur. Heat flux is provided using cartridge heaters, strip heaters, plate heaters [[75,](#page-37-24) [82,](#page-37-31) [85](#page-37-34), [86](#page-37-35)] etc. Power to the heater is regulated and monitored carefully to ensure accurate thermal flux input to the test section.

Following the recording of experimental data, the data needs to be post processed to be converted to a relevant form. Parameters such as heat transfer coefficient can be calculated.

$$
h_{\rm exp} = \frac{q_{\rm app} f_{\rm eff}}{A_{\rm d} (T_{\rm S} - T_{\rm f\_in})}
$$
 (2)

where  $q_{app}$  is the applied device power,  $A_d$  is the footprint area of the device,  $T_{fin}$  is the measured temperature of the coolant at inlet, and  $T<sub>s</sub>$  is the local surface temperature of the



<span id="page-17-1"></span>**Fig. 20** (**a**) Wavy MCHS; (**b**) periodic unit (simulation domain); (**c**) wavy length and magnitude; (**d**) porous fnned MCHS [[66](#page-37-15)]



<span id="page-18-0"></span>**Fig. 21** SEM imagery of the SS plates with nanostructures [[70](#page-37-19)]

cold plate below the heater thermocouple [[87\]](#page-37-36). Parameters such as thermal resistance, Reynolds, Prandtl and Nusselt numbers can also be calculated. Factoring the least count of each of the instruments, error analysis/ uncertainty needs to be factored in.

Hedau et al. [\[86](#page-37-35)] experimentally (and numerically) determined the impact of variation of number of parallel microchannels on thermal dissipation during flow boiling. It was observed that vapour bocking the outlet was the primary source for oscillations and instabilities in the drop in pressure. A reduction in surface temperature by 45.5 °C, a rise in pressure drop by 37% as well as a rise in HTC by 240% was observed when there was a change in the number of channels from 6 to 14. The local temperature of the chip and local Nusselt numbers can be measured with the help of a highresolution IR-range Imaging. Kadam et al. [[88\]](#page-37-37) investigated single-phase heat transfer in MCHS and their performance augmentation. Two configurations of the open MCHS were manufactured and analyzed: the plain open MCHS and the extended open MCHS, with the later providing superior thermal performance, a 9% improvement in heat flux and an 18% improvement in HTC albeit with an 18% greater drop in pressure.

Markal et al. [[89\]](#page-38-0) researched flow boiling in Rec-MCHS (with square cross section) and the influence of hydraulic diameter on it. Effects of mass and heat flux, and vapor quality on the thermal dissipation and total pressure drop were studied and it was found that hydraulic diameter had a substantial impact on both of the local two-phase HTC and the overall pressure drop. Yang et al. [[90](#page-38-1)] conducted performance evaluation of with regards to thermal dissipation observed in single-phase array pin fin MCHS with different configurations (Triangular, square, pentagonal, hexagonal and circular cross sections). The pin fin shapes were found to impact drop in pressure and rate of thermal dissipation for attaining improved cooling performances of the single-phase array MCHS. Peles et al. [\[91](#page-38-2)] investigated forced convection in pin fin MCHS. It was determined that large amounts of heat flux can be dissipated with a reduced wall temperature compared to plain walled MCHS. HTC for micro-scaled pinfins were found to be very high.

#### **3.2 Analytical**

Analytical solutions are mathematical solutions to mathematical expressions with stated boundary and initial conditions. The advantages of analytical solutions are two-fold; one of transparency, with the solution presented to math expressions modelled after the physical phenomenon, offering a strong and unambiguous understanding into how different parameters and variables and interactions between the variables themselves alter the outcome. The other advantage is efficiency. Algorithms and models conveyed with analytical solutions are quite often more efficiently expressed than using equivalent numerical models/techniques. E.g., for solutions of ordinary differential equations, analytical methods will arrive at a much more accurate solution quicker as compared to numerical techniques [[92\]](#page-38-3). Equations used to arrive at analytical solutions however form the basis for numerical methods.

In the field of microchannel fluidics, analytical solution techniques have not been widely used due to the



<span id="page-18-1"></span>**Fig. 22** Contact angles of water droplets on various surface structured SS plate [\[70\]](#page-37-19)



<span id="page-19-0"></span>**Fig. 23** Annular fow patterns at various heat and mass fuxes between (**a**) Plain wall and (**b**) SiNW MCHS [\[71\]](#page-37-20)

complexity of the equations and the types of flow and flow conditions experienced. There are however a few notable examples. M. Dehghan et al. [[59\]](#page-37-8) conducted an analytical investigation examining forced convection across the entrance zone of a MCHS filled with porous material (Fig. [27](#page-21-1)). Energy conservation equation within solid and fluid phases of the porous materials was taken into account ([3\)](#page-19-2) [\[59\]](#page-37-8). Assumption of high Peclet number was taken.

$$
\rho c_p u \frac{\partial T_f}{\partial x^*} = k_{f, \text{ eff}} \frac{\partial^2 T_f}{\partial y^{*2}} + h_{sf} a_{sf} \left( T_s - T_f \right) + S_f,
$$
  
\n
$$
0 = k_{s, \text{ eff}} \frac{\partial^2 T_s}{\partial y^{*2}} - h_{sf} a_{sf} \left( T_s - T_f \right) + S_s.
$$
\n(3)

Here,  $\rho$  is fluid density (kg.m<sup>-3</sup>),  $c_p$  is specific heat at constant pressure (J.kg<sup>-1</sup>.K<sup>-1</sup>), *u* is Darcian velocity (m.s<sup>-1</sup>),  $T_f$ is Temperature of fluid phase  $(K)$ ,  $k_{f, \text{eff}}$  is effective thermal conductivity of the fluid phase  $(W.m^{-1}.K^{-1})$ ,  $x^*$  and  $y^*$  are dimensional coordinates  $(m)$ ,  $h<sub>sf</sub>$  is fluid-solid heat transfer coefficient (W.m<sup>-2</sup>.K<sup>-1</sup>),  $a_{sf}$  is specific surface area (m<sup>-1</sup>).

The equation was converted into parametric form [\(4](#page-19-3)) to yield an exact solution in the form of [\(5](#page-19-4)) [[59](#page-37-8)].

<span id="page-19-3"></span>
$$
\left(\theta_s - \theta_f\right) = \Delta NE = \frac{1}{Bi} \frac{\partial^2 \theta_f}{\partial y^2} + \frac{1}{Bi} \omega_s + O\left(Bi^{-2}\right) \tag{4}
$$

<span id="page-19-4"></span><span id="page-19-2"></span>
$$
\theta(x, y) = \frac{(\omega_s + \omega_f + 1)}{k} x + \frac{3(y - 1)^2 - 1}{6(k + 1)} - \sum_{n=1}^{\infty} \left[ \frac{2}{k\sigma_n} exp(-\sigma_n x) cos(n\pi y) \right]
$$
(5)

Here  $\theta_s$  and  $\theta_f$  is dimensionless temperature of solid and fluid respectively, Δ*NE* is LTNE intensity, *Bi* is Biott

<span id="page-19-1"></span>



<span id="page-20-0"></span>**Fig. 25** (**a**) Copper test block (all dimensions are in mm), and (**b**) exploded view of the test section [[82](#page-37-31)]

Number, *x*, *y* are dimensionless coordinates, half of the channel gap  $(m)$ ,  $k_{s, \text{eff}}$  is effective thermal conductivity of the fluid phase  $(W.m^{-1}.K^{-1}),$ 

$$
\theta = \frac{(T - T_i)k_{s, \text{eff}}}{q''_{w}H}, x = \frac{x^*k_f}{\rho c_p H^2 u} = \frac{x^* / H}{Pe}, y = \frac{y^*}{H},
$$
  

$$
k = \frac{k_{f, \text{eff}}}{k_{s, \text{eff}}}, \omega = \frac{SH}{q''_{w}}, Bi = \frac{h_{sf} a_{sf} H^2}{k_{s, \text{eff}}}
$$

Equation and corresponding solution for Nusselt number were also determined. Pavuluri et al. [[93](#page-38-4)] while developing a numerical solution looked at arriving at an analytical solution for spontaneous imbibition in a rectangular MCHS. Starting with the Hagen–Poiseuille equation for average velocity, they arrived at the equations for dimensionless velocity  $(6)$  $(6)$  and time  $(7)$  $(7)$   $[93, 94]$  $[93, 94]$  $[93, 94]$  $[93, 94]$ .

$$
U^* = \frac{U_{\rm m}}{U_{\rm ref}} = \frac{6hU_{\rm m}\mu_n \hat{J}}{(h^2 + 6h\lambda + 6\lambda^2)\sigma\cos(\theta)}
$$
(6)

<span id="page-20-1"></span>**Fig. 26** Copper heat sink with indications for the thermocou-

and (**b**) isometric views [\[15\]](#page-36-1)

<span id="page-20-3"></span>
$$
t^* = \frac{t}{t_{\text{ref}}} = \frac{(h^2 + 6h\lambda + 6\lambda^2)\sigma\cos(\theta)t}{6h\mu_n\hat{\downarrow}^2}
$$
(7)

 $U^*$  is dimensionless velocity,  $U_m$  is meniscus velocity,  $U_{\text{ref}}$ is reference velocity, *t* ∗ is dimensionless time, h is Height of the channel,  $\lambda$  is Slip length (m),  $\sigma$  is Surface tension between fluids  $(kg/s^2)$ ,  $\theta$  is equilibrium contact angle, t is time. Numerical solutions agreed with the analytical results.

## **3.3 Numerical**

<span id="page-20-2"></span>Numerical techniques are used to study the bounds of validity of analytical solutions and extend research into time (and or other variable) dependant problem numerical solution is obtained. Dey et al. [\[95\]](#page-38-6) explored the impact of varying gravity conditions on the characteristics of thermal dissipation of R134a in MCHS. The general process followed in numerical computation is given below [\[96](#page-38-7)]:



| Thermocouple<br>type | Temperature<br>Range | Uncertainty  |
|----------------------|----------------------|--|
| S                    | 0-1600 °C            | $\pm 1$ °C up to 1100 °C<br>$\pm 0.003 \times (T - 767)$ °C > 1100°C |
| R                    | 0-1600 °C            | $\pm 1$ up to 1100 °C<br>$\pm 0.003 \times (T - 767) > 1100$ °C      |
| B                    | $200-1700$ °C        | $\pm 0.0025 \times (T - 767)$ 600-1700 °C                            |
| E                    | $0-800$ °C           | $+1.5$ °C  |
| J                    | 0-760 °C             | $+1.5$ °C  |
| K                    | 0-1100 °C            | $+1.5$ °C  |
| N                    | 0-1100 $°C$          | $+1.5$ °C  |
| Т                    | $-185-400$ °C        | $+0.5$ °C  |

<span id="page-21-0"></span>**Table 1** Thermocouple temperature measurement range and uncertainty [\[84\]](#page-37-33)

1. Creation of a mathematical model.

- 2. Formation of an applicable numerical method.
- 3. Execution of the method to find a solution.
- 4. Solution validation.

Abiev [[97\]](#page-38-8) used CFD calculations for slug flow in MCHS to determine bubble velocity, Taylor circulation and mass transfer model. Bordbar et al. [[98\]](#page-38-9) looked to understand application of numerical simulations in studies of slug flow in MCHS. Jang and Choi [[99](#page-38-10)] looked to determine the performance with respect to cooling of nanofluids (6 nm Cu-H<sub>2</sub>O and 2 nm diamond-  $H_2O$ ) in MCHS. Results showed that performance with respect to cooling had an enhancement of approximately 10% in comparison to that of a MCHS with water. Nanofluids decrease both the thermal resistance as well as the variation in temperature difference between the coolant and the microchannel wall with heat flux.

Kuppusamy et al. [\[100\]](#page-38-11) examined the enhancement of thermodynamic characteristics of MCHS with secondary flows. The secondary flows caused the regeneration of the



<span id="page-21-1"></span>**Fig. 27** Schematic diagram of the problem [\[59\]](#page-37-8)

hydrodynamic and thermal boundary layer thus resulting in lower thermal resistance (reduced by 76.8%) and greater heat transfer performance (increased by 146%) albeit with some pressure penalty (up to 6%). Kuppusamy et al. [[101\]](#page-38-12) also investigated trapezoidal grooved microchannel heat sink (TGMCHS) utilizing nanofluids studying the thermal and fluid flow fields. Results show that TGMCHS have a superior performance as compared to rec-MCHS.

Shen et al. [[102](#page-38-13)] conducted thermal performance studies numerically on staggered flow alternation structure (SFAS) equipped Double-layer Microchannel Heat Sinks (DL-MCHSs) (Fig. [28](#page-21-2)). Best position of SFAS with respect to thermal performance in the DL-MCHSs was observed to be on the basis on different locations and multi-flow directions and it had the advantage of not having an appreciable pressure drop penalty.

Leng et al. [[103\]](#page-38-14) conducted optimization studies on double-layered MCHS (DL-MCHS) considering their thermal resistance and bottom wall temperature. Channel width, channel number, bottom channel height, and bottom coolant inlet velocity were the search variables used for attaining optimization of heat sink performance. Wu et al. [\[104\]](#page-38-15) conducted parametric performance analysis on Double-Layered MCHS (DL-MCHS) while comparing them to single layered MCHS (SL-MCHS). With taller aspect ratio (lower microchannel breadth) and larger channel number (small width ratio), DL-MCHS were found to be better able to handle conditions where higher pumping power was provided. Xia et al. [\[105\]](#page-38-16) investigated numerically fan-shaped re-entrant cavities and internal ribs equipped (FRCR) MCHS (Fig. [29](#page-22-0)) with regards to their thermal performance. Friction factor of the FRCR for  $e/D<sub>h</sub> > 0$ , was determined to be 1.2-6.5 times greater



<span id="page-21-2"></span>**Fig. 28** Detailed schematic diagram of diferent working fow directions for P-DL-MCHS (P-DMHS): (**a**) concurrent (**b**) counter current and for S-DLMCHS (S-DMHS) (**c**) concurrent fow (**d**) lower-inlet counter current (**e**) upper-inlet counter current [[102](#page-38-13)]



<span id="page-22-0"></span>**Fig. 29** (**a**) Structure of a parallel MCHS and (**b**) the numerical domain [\[105\]](#page-38-16)

values determined for the rectangular MCHS, however the observed Nusselt number of FRCR was found to be 167% more and having a dependence on the Reynolds number (Fig. [30](#page-22-1)).

Szczukiewicz et al. [\[106\]](#page-38-17) worked on numerical simulations of two-phase boiling in MCHS. The authors modelled and highlighted the significance of the thermal inertia of the liquid film trapped between vapour slugs and the wall and flow recirculation in the liquid between two bubbles on the determination of HTC.

## **4 Microchannels with single and multi phase flow**

#### **4.1 Single phase**

Single phase cooling solutions utilize the fluids' sensible heat capacity to provide cooling in the MCHS.



<span id="page-22-1"></span>**Fig. 30** Nuave vs Re for various rib heights [[105](#page-38-16)]

Yang et al. [[107\]](#page-38-18) investigated the cooling of hybrid MCHS with a combination of manifold with secondary oblique channels (MMC-SOC) using HFE-7100 in single phase. The outcomes indicated MMC-SOC heat sinks could concurrently decrease the thermal resistance (by 24%) and drop in pressure (by 11%) in comparison to conventional manifold microchannel (MMC) heat sink. Arie et al. [[108\]](#page-38-19) performed modelling using numerical techniques and optimization of thermal performance of a single-phase flow MMC plate heat exchanger (Figs. [31](#page-23-0) and [32](#page-25-0)).

Evaluating the performance of the optimized MMC with a chevron-type plate heat exchanger, (a commonly used plate heat exchangers) indicated that the MMC for three differing chevron angles had a better performance in terms of Nusselt number and friction factor.

Chauhan et al. [[109](#page-38-20)] investigated the use of single-phase MCHS cooling for hotspot mitigation on microprocessors. To compare the baseline design for a typical microprocessor to an optimized device, a computational model was developed. Dede [[110\]](#page-38-21) investigated the use of single-phase microchannel cold plate (Fig. [33\)](#page-25-1) for thermal management in hybrid vehicle electronics. A favourable thermal-fluid performance was observed in the multi-pass branching microchannel cold plate.

Oudah et al. [[112\]](#page-38-22) researched the impact of hybrid sandblasted patterns on single-phase MCHS considering their heat transfer performance. The modified surface with hybrid micro-sandblasting of elliptical patterns (HSEP) was found to improve the thermal dissipation performance considerably in comparison to the performance observed with the bare surface (BS) microchannel. Fully sandblasting (FS) lower surface of the MCHS however, enhanced the thermal dissipation performance only marginally. The drop in pressure observed in the HSEP was seen to increase slightly in comparison to the FS and BS. Sahar et al. [\[113,](#page-38-23) [114\]](#page-38-24) examined the thermal dissipation and pressure drop properties in single-phase rectangular MCHS with various



<span id="page-23-0"></span>**Fig. 31** (**a**) Single pass and single manifold (SPSM), (**b**) Single MMC [\[108](#page-38-19)]

configurations. In the single channel configuration (hydraulic diameter of 561 μm); four models were numerical examined; 2-D and 3-D thin-wall (heat flux applied from the bottom), 3-D thin-wall (heating on three side) and 3-D full conjugate models. 3D full conjugate model was exclusively used in the multichannel configuration (25 channels, hydraulic diameter of 409 μm). The aspect ratio was found to not affect the HTC while the friction factor and the Nusselt number were found to increase with the increase in hydraulic diameter. Sharma et al. [[115](#page-38-25)] investigated the thermo-fluidic and energetic properties of a manifold

MCHS utilizing recovered hot water (from cooling hot components and intended to be used to cool hotter components) as working fluid. The large fluid flow rate and elevated fluid temperatures were determined to cause turbulent flow conditions in the manifolds (inlet and outlet) of the heat sink with primarily laminar flow conditions observed in MCHS. Entropy generation due to heat transfer was contributed greatly to the net entropy generation in the heat sink. Use of hot water was determined to reduce the heat transfer component of entropy generation meaningfully, resulting in greater  $2<sup>nd</sup>$  law efficiency.





μm

μm

Expt.  $W = 0.21$  mm  $H = 2$  mm Aspect ratio = 9.5  $chip size =$ 10 x 10 mm, 12 x 12 mm

 $H = 320, 287, 302$ 

 $W/cm<sup>2</sup>$  $Q_v = 4.7, 6.5, 8.6$  $\text{cm}^3\text{/s}$ 

 $Q_v = 0.83 \times 10^{-5}$ to 1.67 x 10<sup>-5</sup>  $m^3/s$ 

DI water  $Q = 40, 60, 85$  W

# **4.2 Two‑phase**

et al. [\[116](#page-38-27)]

9 Zhang et al. [\[117](#page-38-28)] **MCHS** 

Rectangular **MCHS** 

A shift to two-phase cooling schemes was done to utilize the coolant sensible as well as latent heat capacities, which allow rejection of greater quantity of heat than that possible in single-phase schemes, while maintaining lower temperatures. The heat flux is generally maintained below critical heat flux (CHF) levels to provide optimal cooling.

Radwan et al. [[118](#page-38-29)] investigated the use of flow boiling (two-phase) in Double layered-MCHS (parallel & counter flow) using Ethyl Alcohol and Novec-7000 as coolant for thermal management in concentrated photovoltaic systems. The effects of changing the coolant type, coolant flowrate, simulated solar light concentration ratio, and heat sink design on the solar cell temperature distribution were investigated experimentally. It was determined that the twophase flow boiling considerably lowered the maximum temperature in the cells and attained a much more consistent temperature distribution within the solar cell. It was also found to improve electrical efficiency. However, the parallel flow configuration was found to attain effective cooling only at higher flow rates in comparison to the counter flow

resistance

resistance

efective in reducing the thermal

Analytical method was developed to predict the pressure drop and thermal



<span id="page-25-0"></span>**Fig. 32** Stacked manifold-microchannel plate heat exchanger [[108\]](#page-38-19)

configuration. In parallel flow, the use of ethanol as coolant resulted in higher efficiency at higher flow rates. However, in counter flow, the Novec-7000 results in higher efficiency values at all flow rates. Pourfattah et al. [\[119\]](#page-38-30) performed analysis of the thermal characteristics of a manifold MCHS with  $H_2O/CuO$  nanofluid flow (Fig. [34](#page-26-0)) using two phase simulation. The results obtained showed the HTC and friction coefficient was improved by raising the in/out ratio at a steady Reynolds number. Also, there is substantially greater impact of in/out ratio at higher values of Re. The highest value of performance evaluation criterion was achieved with an in/out ratio of 0.25 and at the Re of 100 and solid concentration 2 vol%.

Chinnov et al. [[120\]](#page-38-31) studied the flow patterns for Twophase flow in horizontal rectangular microchannels with the height of  $0.1-0.5$  mm and breadth of 9–40mm. Fluorescence induced by lasers and Schlieren imaging were implemented to study the time-dependent liquid flow within the MCHS. Observations indicated that instabilities of the liquid flow present near the lateral walls had a considerable influence on the regime transition in the two-phase flow. Cho and

Wang [\[121\]](#page-38-32) studied flow dynamics, experimentally and numerically, of two-phase flow in MCHS with heterogenous surfaces. The channel surfaces have three hydrophilic channel walls and one hydrophobic one. Both the smooth or rough surfaces were considered for the hydrophobic surface (roughness:  $0.226 - 0.550 \mu m$  rms (smooth surface) and  $21.5 - 28.9$  μm (rough surface)). Surface wetting property and roughness were found to affect the liquid flow. Water in liquid form was found to be present preferentially in the two hydrophilic corners with one hydrophobic channel wall. Frequent slug formation occurred in the case of solely hydrophilic channel as compared with channel with a hydrophobic wall. Surface roughness affected two-phase flow. Wang et al. [[122\]](#page-38-33) performed analysis of pressure drop fluctuations during two-phase boiling of FC-72 in microchannels with a hydraulic diameter of 0.571 mm, 0.762 mm and 1.454 mm (the aspect ratio  $(W_{in}/d_{in})$  is 20, 20 and 10). Low-amplitude high-frequency fluctuations and high-amplitude lowfrequency fluctuations were found to be caused by vapour slug cluster passage and the periodic reversal and rewetting flow respectively. Micro-channel hydraulic diameter was demonstrated to have an impact the pressure drop fluctuation which was found to be significantly chaotic with the increase in channel size.

Keepaiboon and Wongwises [\[123](#page-38-34)] examined the flow boiling in a singular rectangular MCHS using R-134a refrigerant as coolant and considering flow patterns and thermal dissipation characteristics. It was determined that flow pattern was affecting the HTC significantly. HTC measured at greater saturation temperatures was found to be higher than values measured at lower saturation temperatures. The HTC was found to rise with the rise in mass flux especially in high heat flux ranges. Thiangtham et al. [\[124\]](#page-38-35) researched the flow patterns and thermal dissipation characteristics in MCHS (27 channels and a hydraulic diameter of 0.421 mm) during boiling of R-134a. It was determined that variation of flow pattern was sensitive to variation of heat flux and saturation temperature. At lower heat flux, rise in heat flux increased HTC and flow patterns observed were bubbly and slug flow. At higher heat fluxes, HTC rose with rise in mass flux and flow patterns observed were wavy and annular.



<span id="page-25-1"></span>**Fig. 33** Multi-pass branching microchannel cold plate [\[110](#page-38-21)]

<span id="page-26-0"></span>



## **5 Nanofluids**

Nanofluids can be utilized as a replacement of water or water-based coolants. Nanofluids are a stable mixture of base fluid, typically water, and nanoparticles suspended in it forming a colloidal solution which can be considered as single phase and/or multi-phase fluid depending on the volume fraction of the nanoparticles mixed in the base fluid. A surfactant (cetyl trimethyl ammonium bromide (CTAB), polyvinylpyrrolidone, Sodium dodecyl sulphate (SDS), and SDBS etc.) is added to ensure stability of the solution. Nanoparticles generally used are metals (Cu, Zn, Al, Fe etc.) or metal oxides  $(AI_2O_3, ZnO, CuO$  etc.). An advantage of nanofluids is the high HTC which can be in the order of over 2 magnitudes greater than the base fluids (Fig. [35](#page-27-0)) [[125](#page-38-36)]. Several researchers have looked into combining the advantages of nanofluid and MCHS for enhanced heat transfer.

Sarafraz et al. [[126](#page-38-37)] conducted studies characterising fluid flow and thermal dissipation properties of an aqueous-graphene nanoplatelet (GNP) nanofluid in MCHS. Enhancement of the HTC and Nu by approximately 80% was shown using pure water as the baseline. The highest value in pressure drop was by 18.3% and was seen at highest Reynold's number and greatest mass concentration of the GNP nanofluid. Arani et al. [\[127](#page-38-38)] studied (numerically) use of nanofluid made with water and single-wall carbon nanotubes (SWCNT) used in a truncated double-layered MCHS as a means of enhancement of heat transfer. The enhancement of Reynolds number, volume fraction of nanoparticles and dimensionless slip velocity coefficient were found to cause substantial increase of heat transfer and decline in thermal resistance of surface. Azizi et al. [\[128](#page-39-0)] investigated convective heat transfer in a cylindrical MCHS (Fig. [36\)](#page-27-1) with Cu-H<sub>2</sub>O nanofluid as coolant. With  $0.05$ ,  $0.1$  and  $0.3$ wt% concentration, the Nusselt numbers of nanofluids were increased by approximately 17%, 19% and 23% (Fig. [37\)](#page-27-2) in comparison to values obtained for pure water for similar



<span id="page-27-0"></span>**Fig. 35** Thermal conductivity comparison of common polymers, liquids, and solids [[125](#page-38-36)]



<span id="page-27-1"></span>**Fig. 36** Cylindrical microchannel heat sink [[128](#page-39-0)]

Reynolds numbers. Reynold's numbers above 900 resulted in a reduction of Nusselt's number.

Bahiraei et al. [\[129\]](#page-39-1) studied the effectiveness of hybrid (graphene–silver nanoparticles in aqueous solution) nanofluids in MCHS equipped with secondary channels and ribs. A 17% enhancement in the convective HTC was seen with the concentration increasing from 0 to 0.1% at  $Re = 100$ .



<span id="page-27-2"></span>**Fig. 37** Nu ratio vs Re for various nanoparticle concentrations using values for pure water as baseline at a constant heat flux of  $3.5 \text{ W/cm}^2$  [[128](#page-39-0)]

A reduction of surface temperature by 3.42 K and 13.88 K was seen at  $Re = 100$  to 500. Greater pumping power requirements were experienced at higher Reynold's numbers and concentrations. Hatami et al. [[130](#page-39-2)] researched the use of Cu-H<sub>2</sub>O nanofluids in MCHS focusing on thermal and flow analysis. Raising the volume fraction of the nanoparticles, was observed to increase the Brownian motion of the particles (which transmits and disperses thermal energy to the surroundings), thus the coolant and wall temperature differential was found to reduce. Hung et al. [[131\]](#page-39-3) investigated the performance with respect to heat transfer with use of  $(Al_2O_3, SiO_2, CuO H_2O)$  nanofluid in Double Layered-MCHS. The study indicated a connection between the thermal resistance and channel number. The values of channel width ratio or channel aspect ratio observed were first found to decrease then increase. An average of 26% enhancement in thermal performance was seen with a 1%  $Al_2O_3$ - H<sub>2</sub>O nanofluid solution over that of pure water. Al-Baghdadi et al. [[132\]](#page-39-4) conducted a CFD analysis on  $(A<sub>1</sub>, O<sub>3</sub>)$ ,  $SiO<sub>2</sub>$ , CuO H<sub>2</sub>O) nanofluid based MCHS. The MCHS working with coolant of  $Al_2O_3$ - H<sub>2</sub>O was found to have the highest value of the HTC for entire considered range of Reynolds numbers. Tokit et al. [[133\]](#page-39-5) conducted studies to determine the thermodynamic performance of an optimized design of interrupted-MCHS (IMCHS) cooled with  $(Al_2O_3, CuO, and$  $SiO<sub>2</sub> - H<sub>2</sub>O$ ) nanofluids. Nu for IMCHS were found to be significantly greater than values observed for conventionally designed MCHS albeit a slightly greater value of drop in pressure. The highest value of thermal augmentation was calculated for alumina based nanofluids, followed by copper oxide based, and then for Silica based nanofluids. Nu was observed to be directly proportionally with the volume fraction of nanoparticle and inversely proportional with the diameter of the nanoparticle.





# **6 Applications**

In the previous sections, different geometry, working fluids, and solution approaches are discussed thoroughly. Each of these mentioned studies were obviously investigated for a certain application of microchannels in the various engineering fields. Microchannels have been developed for high heat flux removal applications with compact geometric requirements. These unique set of challenges exist in a wide area of applications. In the subsequent section, few of those applications are discussed.

## **6.1 Cooling of electronic circuits**

The power densities seen in commercial and consumer grade electronics have been on the rise [\[2](#page-35-1), [135](#page-39-7)] and effective cooling along with compactness of design are increasingly being sought after [\[1](#page-35-0), [3\]](#page-35-2). Several cooling techniques are being investigated, microjet cooling [\[136](#page-39-8)], PCM [\[137](#page-39-9)], microchannel cooling etc. In this section we will look at the use of microchannel either as a standalone system or as a part of a combination of technologies being developed or used in electronic circuits.

Jiang et al. [\[138](#page-39-10)] experimented with the use of Electroosmotic Microchannel closed-loop cooling system for thermal management in VLSI circuits (Fig. [38\)](#page-30-0). Results indicated the ability of the system to remove  $38 \text{ W/cm}^2$  and maintain the temperature of the chip below 100 °C.

Chen et al. [\[139](#page-39-11)] investigated the use of interconnected microchannels with re-entrant cavities (IMRCs) for pool boiling enhancement deionized water as the working fluid for cooling of high-powered electronics. IMRCs exhibit a significant rise in pool boiling heat transfer as compared with results obtained for smooth copper plates (SCPs). Silvério et al. [\[140](#page-39-12)] developed and tested an integrated multi-microchannel heat sink (27 rectangular channels in parallel with



<span id="page-30-0"></span>**Fig. 38** Experimental apparatus for characterization of the MCHS heat exchanger [[138](#page-39-10)]

hydraulic diameter  $D_h$ = 0.096 mm, L/ $D_h$ = 104 and relative roughness of 2.4%) for electronics cooling. Results indicated, in the absence of latent cooling, the chip temperature was maintained below 358 K ( $T_{w, avg}$  = 338.4 K). The heat flux measured at the peak was  $108 \text{ kW/m}^2$  and a corresponding flow rate of 3.050 L/h. With latent heat cooling, the heat flux extracted rose to 266 W•m<sup>2</sup> for a corresponding flow rate of 1.300 L/h ( $Re = 277$ ). Bahiraei et al.  $[141]$  studied MCHS (Fig. [39\)](#page-30-1) with hybrid nanofluid with regards to thermodynamic performance and 2nd law characteristics. The nanofluid used contained graphene–silver nanoparticles. Surface temperature was determined to reduce by increasing either velocity or concentration. The maximum temperature observed on the heating surface was found to reduce by raising the concentration and velocity at the inlet, reducing the chances of formation of hot spots.

Hou et al. [\[142](#page-39-14)] investigated the use of two-phase flow (with refrigerant R1234yf) microchannel thermal management systems (Fig. [40](#page-31-0)) for power electronics with heat dissipation of over 500  $W/m^2$  with a maximum heat flux of about  $750 \text{ W/m}^2$ . From observations, the thermal management system had the capacity to handle a heat flux of 5260 kW/m<sup>2</sup> while maintaining the junction under 120 °C.

Jaikumar and Kandlikar [[143\]](#page-39-15) studied using open MCHS with porous fin on tops and with FC-87 as the coolant used for enhanced pool boiling for cooling of electronics. A peak value of CHF of  $370 \text{ kW/m}^2$  was attained (270 % improvement using plain chip as baseline). The improvement in pool boiling was attained due to presence of additional nucleation sites and/or rise in the area available for thermal dissipation. Jung et al. [[144](#page-39-16)] researched methods for cooling of power electronics with high fluxes in excess of 10 MW/m<sup>2</sup>. For single- and two-phase, Water and R245fa refrigerant were used as working fluids respectively. The three cooling methods investigated were the device substrate copper cold-plate with bonded MCHS module, the device substrate with embedded MCHS directly etched into it and 3D manifold with inlet and outlet module on embedded MCHS. The first method provided the least thermal resistance. Laguna et al. [[145](#page-39-17)] investigated the use of microfluidic cell cooling for electronics. From observations, temperature uniformity was enhanced along the whole system while lowering requirements of pumping power by 89.2 % in comparison to the baseline as measured for conventional MCHS technology.

Sakanova et al. [\[146\]](#page-39-18) performed optimization and comparative studies of DL-MCHS and double sided MCHS with water/Alumina nanofluid for cooling of power electronics. The microchannels were incorporated within the Copper-layer of direct bond copper. Based on the optimal geometry, the sandwich structure with counter flow in comparison to single layer (SL), DL with unidirectional flow and DL with counter flow, showed a decline in thermal resistance by 59%, 52% and 53% respectively. Sharma et al. [\[147](#page-39-19)] conducted energy efficient hotspot targeted optimized MCHS etched onto the reverse side of the chips for thermal management of the electronics. For a value of 1500  $kW/m<sup>2</sup>$  and 3000 kW/m<sup>2</sup> as heat flux at the hotspot, the requirement of the pumping power for optimized designs was determined to be 0.23% and 0.17% respectively of the total power consumption by the chip.

<span id="page-30-1"></span>

<span id="page-31-0"></span>**Fig. 40** SiC power module assembly on the MCHS with two-phase flow boiling [[142\]](#page-39-14)



## **6.2 As heat exchangers**

Redo et al. [[148\]](#page-39-20) performed characterization studies of two-phase flow of R410a. The flow was simulated for air-conditioning systems within the vertical header of a microchannel heat exchanger (MCHE) with multiple horizontally oriented microchannel flat tubes. Pan et al. [[149\]](#page-39-21) examined the performance of MCHE with fan shaped cavities (FSC) with regards to heat transfer. Effects of structural parameters on the performance of the MCHE was studied. The performance of the MCHE with FSCs, from the results, indicate that it is superior to that without FSCs and has a lower pressure drop. Hu et al. [[150\]](#page-39-22) established experimentally the impact of outdoor air-side fouling on frost growth on thermal dissipation characteristics of a MCHE for a heat pump outdoor coil. Fouling induced reduction in initial airflow by about 3.5% was found to increase thermal dissipation and growth rates of frost. Heavier fouling was found to decrease both rates. When growth of frost was normalized to thermal dissipation, it was determined to be enhanced by fouling. Mahvi and Garimella [[151](#page-39-23)] studied two-phase flow distribution of saturated R134a refrigerant in MCHE headers with several header geometries (Fig. [41](#page-31-1)). It was observed that the liquid distribution remained nearly constant as the inlet quality was raised, but there was a marked improvement in vapor distribution.

At low qualities there exist restrictions on the drop in pressure across each flow path. This forces the liquid to distribute more uniformly and enhance the overall distribution. It was determined that the distribution was not greatly affected by the header inlet mass flux. It was observed that greater quantities of liquid were transported to downstream channels by the rise in the momentum of the liquid phase in the header. This, however, resulted in low liquid flow rates in the channels closest to the inlet port. Glazar et al. [[152\]](#page-39-24) investigated the effects of different microchannel shapes in compact heat exchangers using an open wind tunnel. Results showed that effectiveness of heat transfer reduced with the increase of air velocity at inlet. The optimal results were attained with microchannels of hexagonal and diamond shape. However, lowest pressure drop was observed in rectangular shapes cross section. Kwon et al. [[153\]](#page-39-25) investigated the application of air-cooled MCHE (cross flow, 1 cm<sup>3</sup>, R245fa refrigerant) for high power density applications. A maximum power density of 60 MW/ $m<sup>3</sup>$  was measured for an air inlet temperature of 27 °C refrigerant inlet temperature at 80 °C.

Li and Hrnjak [\[154](#page-39-26)] performed validation studies for lubrication effect incorporated model of MCHE. A new model was developed and validated against experimental results (R134a-PAG 46 oil) at different circulation ratios for oil (0.1%-8.3%). Results from numerical studies showed that addition of lubricant improved distribution



<span id="page-31-1"></span>**Fig. 41** Header geometries investigated [\[151](#page-39-23)]

of refrigerant. Mazaheri et al. [[155\]](#page-39-27) developed a four layer MCHE (counter-current arrangement) (Fig. [42\)](#page-32-0) and conducted two-phase flow analysis with nanofluid flow. The nanofluid was taken as the Hot fluid, while for the cold fluid, water was selected. Nanoparticles improved the heat exchange capacity and led to better performing heat exchange rate. Increase in channel number resulted greater overall HTC owing to greater and intense impingement of flow which causes greater disruption of the thermal boundary layer.

Mohammadian et al. [[156\]](#page-39-28) conducted studies on twophase flow counter flow MCHE (CFMCHE) with alumina/ water nanofluid flow. Reducing particle size and raising concentration of nanoparticles was found to have superior effectiveness, lower pumping power as well as a reduction of temperature within the solid phase of CFMCHE. Reynolds number was found significantly affect the performance of system with its' reduction was found to increase the effectiveness while the thermal dissipation contribution of entropy was also seen to reduce. The pumping and frictional power contribution of entropy was found to reduce with decrease of Reynold's Number. Shi et al. [[157](#page-39-29)] used surrogate model coupled with genetic algorithm to optimize the inlet of ceramic MCHE. By optimization, the fluid flow nonuniformity was lowered by 68.2% and decrease in the drop in pressure was by 6.6%. This resulted in the fluid flow uniformity in the heat exchanger improving substantially albeit with the penalty of a small pressure drop. Yih and Wang [\[158](#page-39-30)] characterised the thermo-hydraulic performance of a MCHE for the purpose of waste heat recovery. The overall heat transfer increased with air flow while the



<span id="page-32-0"></span>**Fig. 42** Arrangement of the 4-layer MCHE w/implemented arrange-

effectiveness decreased with air flow for a given oil flow rate. With an increase in air inlet temperature, the effectiveness was found to increase. A higher thermal conductivity was attributed to this. Zhou et al. [[159](#page-39-31)] examined the flow and heat transfer properties of parallel-flow double layered MCHE (Fig. [43](#page-32-1)). The increasing height and width were found to influence the velocity profile. Greater widths and lower heights were determined to increase average Nusselt number for simultaneously thermally and hydrodynamically developing flow.

Zhou et al. [\[160](#page-39-32)] investigated the flow and heat transfer properties of MCHE embedded with different shape micropillars (Fig. [44\)](#page-33-0). From the results, the  $Nu/Nu_0$ ratio for micropillars of type A, B and C was found to be 1.65–1.9, and for micropillars of type D and E, was 1.6–1.7. A 20–40% increase in the pressure loss was however observed in the type D and E as compared to microchannel without micropillars, and an increase of above 60% for the type A, B and C.

#### **6.3 As heat pipes**

Heat pipes are heat-transfer devices which combine the concepts of both thermal conductivity and phase transition to effectively move heat between two solid interfaces. Due to the very HTC for boiling as well as for condensation applications, heat pipes are considered to be very effective thermal conductors.

Wei et al. [[161\]](#page-39-33) studied the mechanisms of flow and heat transfer using CFD analysis under zero gravity conditions of a Ω-shape microchannel aluminium-ammonia grooved heat pipe (GHP) (Fig. [45](#page-33-1)). Results indicated that the GHP was adept of moving thermal energy over relatively large distances with a small difference of temperature. Li et al. [\[162](#page-39-34)] examined the thermodynamic performance of microchannel heat pipe (MCHP) at varied tilt angles and evaporator temperatures. The heat pipe consisted of 2 flat-panel MCHS in parallel. Each microchannel was equipped with micro-fins



<span id="page-32-1"></span>**Fig. 43** Parallel - flow double layered MCHE [\[159\]](#page-39-31)

<span id="page-33-0"></span>



to augment transfer of heat. The working fluid undergoes phase change in the evaporator side and is transported to the condenser side due to pressure differential created due to temperature difference. The latent heat is released at the condenser side, and the working fluid condenses undergoing phase change (back to liquid form) and drawn back to the evaporator side usually by means wicking effect. The fluctuations in temperature observed in the MCHP were found to increase proportionally with the tilt angle. This fluctuation was attributed to the effect of gravity. The temperature difference was found to increase with the increase of evaporator temperature at low tilt angle. However, relation between the variation of the temperature difference and evaporator temperatures whilst at higher tilt angle was no longer a simple one.

Modjinou et al. [[163\]](#page-39-35) performed research comparing different temperature management systems for photovoltaic devices. They compared macro encapsulated phase change materials (PCM), MCHP and conventional thermal management systems using mathematical models, experimentation, and simulation. The results indicated 36.71%, 35.53% and 31.78% respectively to be the combined average photo-thermal and electrical efficiency. As compared to the other solutions, MCHP had the advantage of passively and effectively transferring and absorbing heat. R134a was used as refrigerant and copper was simulated instead of aluminium for the MCHP to prevent faster freezing damages. Aluminium is known to diffuse heat better while copper, as a heat transfer media, is known to be a better. Thus, to achieve steady state faster, MCHP using copper as material is preferred over those made with aluminium. Li et al. [\[164,](#page-39-36) [165](#page-40-0)] developed and performed analysis of a MCHP present in an evacuated tube solar collector with an integrated thermoelectric generation system, the structure of which is shown in Fig. [46](#page-34-0). The solar radiation impinges on the MCHP evaporator and is absorbed due to the selective absorbing coating. The heat is conducted through Thermoelectric generator (TEG) is rejected to the cooling water, thereby increasing the electrical output generated by TEG. The results indicated a superior thermal performance of the system with the advantage of electricity production.

Shittu et al. [\[166\]](#page-40-1) conducted a study experimentally as well as analysis of exergy of photovoltaic-thermoelectric with flat plate microchannel. The hybrid photovoltaic-thermoelectric was able to exploit a broader solar spectrum thus converting

<span id="page-33-1"></span>



<span id="page-34-0"></span>**Fig. 46** MCHP equipped evacuated tube solar collector with an integrated thermoelectric generation system [\[164](#page-39-36)]

more energy from the sun while enhancing electrical conversion efficiency of PV system by effective cooling. Results showed a marked improvement over PV only systems and uncooled PV systems. In addition, heat water was made available for domestic or industrial consumption. 69.53% and 56.57% were the highest and lowest thermal efficiencies obtained respectively.

Song et al. [\[167](#page-40-2)] developed a hybrid condenser equipped heat pump. The hybrid condenser combined a flat plate MCHP with a thermoelectric generator (TEG) and Fresnel photovoltaic (FPV) evaporator. The TEG was fitted between the CPV and absorber plate in the evaporator. It can be used to convert the thermal energy contained in the PV into electricity. This, however, inhibited the dissipation of heat from the PV, thus adversely impacting the performance of the PV. The TEG was found to improve the electrical and total performance of the system if TEG is placed in the condenser. This was done to convert the thermal energy that would be rejected into electrical energy without impacting the heat dissipation capacity of PV. The MCHP collects thermal energy from condenser to attain a large density of heat flow as well as a high output of TEG. The setup with the TEG in this configuration, shows an improvement of electrical efficiency by 10.83% and improvement of total exergy efficiency by 6.02%.

#### **6.4 Thermal management of photovoltaic cells**

Solar power is a key area where cooling technologies are being researched and new technologies developed. There exists a correlation between photovoltaic efficiency with the temperature of the photovoltaic (PV) cells. In addition, with the use of concentrated photovoltaics (CPV) which experience high solar concentration ratios and attain elevated temperatures, (and have conversion efficiencies up to 46% as compared to 20% for flat plate collectors), the temperature of the cells turns into a critical parameter  $[168]$  $[168]$ . Thus, there is a need to provide effective cooling for these systems to reach peak net output power whilst ensuring the safe operation of the system components.

Abo-Zahhad et al. [[169](#page-40-4)] investigated stepwise variation of width microchannel cooling in thermal management application in high concentrator solar cells. Various parameters such as the cell temperature, electrical efficiency, thermal efficiency, electrical thermal, and total exergy efficiency, and thermal resistance of the heat sinks were shown, from the results, to be impacted by the design of the heat sink as well as the mass flow rate of the coolant. At a concentration ratio of 1000 suns and elevated coolant flowrate (1000 from 25 g/min), saw a drop in the temperature of the solar cell (344.7 K to 313 K) with non-uniformity of the temperature in the solar cell reducing from 288.5 K to 282 K. Acharya [\[170](#page-40-5)] studied the flow and thermal characteristics of a hybrid Alumina–copper/ water nanofluid flow within a MCHS impinged by radiative solar energy. From observation, solar radiation fostered transport of heat at suction. A lower velocity profile was observed for suction with the use of hybrid nanofluid in comparison to ordinary nanofluid. However, a completely opposite phenomenon was observed whilst injection. Ahlatli et al. [\[171](#page-40-6)] examined the thermal performance of carbon nanotube nanofluids (0.01%, 0.05%, 0.1%, and 0.5% weight fraction) in solar collectors with microchannels . The measured heat transfer, pressure drop, and pump power increased with the rise of the weight fraction of nanofluids. With the use of nanofluids, the heat transfer was found to be greater than that of the (distilled water) base fluid. With quartz being used at the upper surface of the MCHE resulted in the high-weight-fraction nanofluids becoming more effective.

#### **7 Conclusions and future scope**

This review included different geometric designs, coolant phases, types, and application of microchannels currently being investigated which has tremendous applications in the different engineering domains. The review is primarily focused on the various geometric designs of the microchannels, coolants used as well as the operating modes which are derived and optimized with the help of numerical simultion and extensive experimentation. It is vital to appreciate the factors such as thermal conductivity, thermal resistance, and fluid flow distribution in the microchannels which influence the thermodynamic performance and drop in pressure as observed in the microchannels.

The review looked at the different commonly used structures of MCHS. Different coolant combinations and performance of each was also discussed. Six structures were looked at: straight microchannels, wavy microchannels, pinfin microchannels, oblique finned microchannels, porous microchannels and microchannels with nanostructures. It was determined that while each of these microchannels had their unique advantages, though the simpler geometry of straight microchannels provided an economical shape for ease of manufacturing, the microchannels with relatively complex shapes provided a greater HTC in comparison with the straight microchannels. The advantages arose from the ability of the microchannels to cause redevelopment of the thermal boundary layer, thus reducing the resistance to heat transfer to the coolant. As a result, a significant increase in Nusselt number was observed. Use of variation in location, geometry, and number of microchannels also had the advantage of being able to be used for hotspot mitigation. The geometries however also increased the resistance to flow thus increasing the pumping power requirements. Use of different working fluids was also looked at. Use of singlephase system simplified the implementation by eliminating the complexity of modelling phase transitions. This however, also limited the amount of heat transfer to the coolant as it was limited by sensible heat capacity of the fluids. In Two-phase systems, the latent heat capacity of the fluid is also utilized. This greatly improves the usable heat capacity of the fluid. Tools have been developed to predict flow and heat transfer as well as to predict the onset of dry out. Use of nanofluids in MCHS was also looked at. Nanofluids offer HTC ranges which are magnitudes higher than those observed in single-phase and in some two-phase systems. There was a marked increase of Nusselt number observed for comparable Reynold's numbers in case of nanofluid flow vs single-phase fluid flow. Several combinations of nanofluid were investigated. Studies have been conducted using experimental setups as well as numerically. The numerical studies offered the option of use of complex physical structures as well as conditions (constant heat flux, absence of gravity etc.) which would have been difficult to recreate. Numerical techniques were also used for different optimization studies. Purely experimental studies as well as some analytical studies were also looked at. Some of the applications of MCHS for thermal management in electronic circuits, heat exchangers, heat pipes in photovoltaic cells were also looked at. Uses in VLSI, hotspot mitigation in electronics, waste heat recovery systems, combined solar and heating systems were covered. In each, the use of microchannels and related technology helped improve the performance of the system.

From the above it is clear that significant work has been carried over the years by numerous researchers broadening our knowledge in the domain and pushing the boundaries of science. Combining design features is one promising method to improve achievable performance. Further studies could include the use of hydrophilic and hydrophobic coatings as well as other nanostructures in MCHE and MCHP to aid in heat transfer as the study is limited. Use of such treatments could enhance the removal of heat and improve the performance of MCHE & MCHP. Similarly, research into geometries that allow the rapid removal of nucleating bubbles and slugs away from the heat transfer surface can be furthered and combined for improving heat transfer along with the further development of designs that are more rapidly deployable. Use of bio inspired surfaces for the purpose of heat transfer enhancement and drag reduction can also be further researched and incorporated into designs.

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**Data availability** Data will be available on request.

#### **Declarations**

**Conflict of interest** The authors declare that there is no confict of interest.

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