ORIGINAL ARTICLE

Effects of tube shape on the distribution of film thickness and heat transfer performance in falling film evaporation

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Abstract

The evaporative condenser has broad application prospects because of its high heat transfer efficiency. In order to explore the efect of tube shape on the flm thickness and heat transfer performance of evaporative condenser. In this study, 2-D computational models of diferent tube shapes were built to simulate the fow behavior and heat transfer characteristics of falling flm, and the reliability validation on simulation data was performed by the comparison of experimental value. The model contains one round tube and four half-oval tubes, and the fve tubes have a equality of perimeter. The liquid flm distribution, heat transfer coefficient and dimensionless temperature were calculated and analysed, respectively. It concluded that the water flm gets thinner and thinner with the tube shape becoming narrow and long, and the average liquid flm thickness of four half-oval tubes are about 3.7–11.4% lesser than that of round tube. Furthermore, the dimensionless temperature of the half-oval tubes is smaller in contrast with round tube, which indicates a larger heat transfer coefficient. The mean heat transfer coefficient of the four half-oval tubes nearly increased by 3.2% , 6.5% , 8.7% and 11.3% on the basis of round tube, respectively.

Nomenclature

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x Arc length, mm

- $x \sin \theta$ is location, $= x/l$,
-
- $y/(m \cdot s)$
- $w/(m \cdot K)$
- cient, N/m
- n^2/s
- rature,
	- $(0 \leq \theta \leq 1)$
-
- *i* ckness, η=d⁄δ
-
- l Liquid
- sat Saturation
- w Wall

1 Introduction

Falling-flm technique has a large number of applications, such as evaporative condenser, wet cooing tower, and other process of heat and mass transfer $[1-3]$ $[1-3]$ duo to the merit of high energy efficiency and water conservation $[4, 5]$ $[4, 5]$ $[4, 5]$ $[4, 5]$. In a falling flm evaporation system, the water drop to the top of the tube surface from the spray nozzles, and then cover the tube wall, forming a water flm fnally. The heat and mass transfer efficiency is greatly affected by flow characteristics over the horizontal tube. The thicker flm thickness means a higher thermal resistance, which is bad for the heat transfer. Thus, falling flm evaporation that has important meaning and potential value on energy saving is worthy to further investigate.

So far significant headway of flow characteristic in falling-film evaporation has been performed. Nusselt [[6\]](#page-10-3) first put forward the theory of falling flm and presented a classical empirical formula for the two-dimensional flm thickness under sheet flow.

$$
\delta = \left(\frac{3\mu_l \Gamma}{\rho_l (\rho_l - \rho_g) \sin \varphi}\right)^{1/3} \tag{1}
$$

With above defnition, the Reynolds number was given as follow:

$$
Re = \frac{4\Gamma}{\mu_l} \tag{2}
$$

Lin et al. [[7\]](#page-10-4) simulated the liquid flm distribution and heat transfer coefficient for three circular tubes with different diameter under the condition of Reynolds number varying from 368 to 800, and showed that the infuence of Reynolds number on the two parameters is larger than the tube diameter. Chen et al. [\[8](#page-10-5)] utilized laser-induced fuorescence method to measure water and seawater liquid flm thickness outside circular tubes, they found that there is no obvious diference in liquid flm thickness between the two fuid. Hou et al. [[9\]](#page-10-6) gauged the water flm thickness outside circular tube bundles with a displacement micrometer, and based on Nusselt correlation, developed a new expression for flm thickness of which the tube diameter and pitch were taken into account. Xu et al. [\[10\]](#page-10-7) conducted a measurement for flm thickness over round tubes with the JDC-II device, and presented a empirical expression to predict the fuctuation intensity of falling flm in the case of diferent Reynolds number. Zhang et al. [\[11\]](#page-10-8) performed an experiment to research the flm thickness distribution outside a corrugated tube, which revealed that the dryout phenomenon barely appears on the tube surface duo to the special structure of the tube. Gstoehl et al. [\[12](#page-10-9)] measured the flm thickness for water, water–glycol mixture, ethylene glycol three kinds of fuid outside a horizontal circular tube, which showed that Nusselt falling flm theory agrees well before the 90°circumference angle, however has some deviation when the circumference angel is larger than 90°. Zhou et al. [\[13](#page-10-10)] built a 3D model to research the falling flm thickness over the round tube wall, they pointed out flm thickness increases as Reynolds number increasing, while dry spot at the bottom of the tube also increases at same time. Wang et al. [\[14\]](#page-10-11) derived expressions of liquid film thickness for diferent fow region under column fow with a 3D model. Qiu et al. [[15](#page-10-12)] studied the flm thickness distribution of diferent fuid on the wall of horizontal tube, they showed that liquid viscosity is the major factor that leads to the different jet flow. Qiu et al. $[16]$ $[16]$ used a three dimensional model to study flow characteristics of one and two liquid column around a horizontal tube, they concluded that the falling flm of one liquid column has a uniform distribution, in contrast, the falling flm of two liquid column forms a uplift duo to collision of liquid flm. Yan et al. [[17\]](#page-10-14) adopted a high-speed camera and IC measure method to implement a measurement of water flm thickness over a round tube, they concluded that the nozzles-holes confgurations is a key factor for the distribution of falling flm. Li et al. [[18\]](#page-10-15) developed a 3D model to study water flm distribution over round tube surface under the infuence of counter-current wind speed, and found the location of thinnest flm thickness will move upward along the perimeter direction when wind is imposed in the case of droplet and column fow condition. Parken et al. [\[19](#page-10-16)] implemented a experiment on heat transfer performance of evaporation and boiling around horizontal brass tubes, the mean heat transfer coefficient were calculated and analysed, finally, the expressions of mean heat transfer coefficient to diferent evaporation process were presented. Pu et al. [[20\]](#page-10-17) simulated the flow and heat transfer process for falling film over fat tubes with a 2D model, the result revealed heat transfer coefficient increases as tube shape of flat tubes get narrow and long. Li et al. [[21\]](#page-10-18). conducted an experiment to research falling flm evaporation of three enhanced tube and a smooth tube in the condition of small Reynolds number and convective evaporation, which derived heat transfer performance over tube with enhanced inner surface is better than that of smooth tube. Qi et al. $[22]$ studied the heat transfer coefficient around diferent tube shape with seawater as working fuid, it found that the elliptical tube is about 20–25% higher than circular tube. Ji et al. [\[23](#page-10-20)] experimentally study heat transfer performance of R134a that evaporate in the form of liquid flm under the action of gas velocity, they showed that the larger gas velocity is beneficial to the uppermost two tubes. Zhao et al. [[24\]](#page-10-21) simulated the liquid flm distribution in circumferential direction over a round tube, they point out that surface tension has a great influence on the flow behavior of liquid flm, then derived expressions of liquid flm thickness for diferent range of circumferential angle.

It can be learn from the literature survey above that most previous researches pay attention to circular tube, but few study focused on non-circular tube in the area of falling flm evaporation. Pu et al. [[20\]](#page-10-17) and Qi et al. [[22\]](#page-10-19) have proved that the special tubes possess a better heat transfer performance than round tube in the area of desalination. Nowadays, the round tubes dominate in evaporative condenser, the superiority of non—circular tubes has not been appreciated. It is believed that gravity component of half-oval tube in fow direction is larger than round tube. So leads to a higher velocity of falling flm, which means a thinner water flm thickness compared with circular tube. Thus, more details and extensive studies are needed to model horizontal falling flm behaviour of half-oval tubes and clarify the mechanisms of fow enhancement. In other words, half-oval tube is benefcial to the heat transfer for falling flm technique. Therefore it is necessary to investigate the performance that liquid flm evaporates over half-oval tube.

The primary objective of this paper is to state that halfoval tube has superiority in contrast with round tube in the process of falling evaporation. The falling flm distribution and heat transfer coefficient were calculated. A test rig was built to verify the simulation data of liquid flm thickness, moreover by comparison of the experiment value of previous literature, the reasonability of heat transfer coefficient was also demonstrated. The simulation data manifest good consistency with the values of experiment, which indicates the reliability of the model. In addition, the dimensionless temperature inside liquid flm at diferent circumferential dimensionless location are calculated to reveal the distribution of thermal boundary layer around circular and half-oval tubes.

2 Numerical model

2.1 The geometric parameters of two kinds of tube

As shown in Fig. [1](#page-2-0), the half-oval tube is formed by a upper semicircle and a lower half ellipse, In this paper, the half-oval

Fig. 1 Schematic diagram of circular and half-oval tube

tube (ϵ = 3.2) was selected as benchmark, then make sure that the perimeter is same and change the ratio of b to a to attain the circular tube and the other 3 half-oval tubes. The tubes parameters are list in Table [1](#page-2-1). The ratio of b to a is defined as ε . That is to say, the half-oval tube become narrow and long as ε increases, so the gravity component in perimeter direction gets larger.

2.2 Computational model and governing equations

The software of FLUENT 16.0 is used to conduct the simulation. VOF model is a surface tracking method under fxed Euler grid, which can obtain the interface of two or more incompatible fuids. So the VOF model is utilized to simulate the two phase fow because it can accurately extract the edge of water film compared with other multiphase flow model. The gas-liquid interface can be identifed by the water volume fraction of 0.5. The range of volume fraction is 0 to 1, and the volume fraction of all the phases add up to 1. The volume fraction of 1 indicate that a grid cell is flled with liquid or gas, therefore there is no other phase in that grid. Water vapor is set to the frst phase duo to the small density, so water liquid is secondary phase.

The continuity equation of VOF model is written as:

$$
\frac{\partial u_x}{\partial x} + \frac{\partial u_y}{\partial y} = 0 \tag{3}
$$

The continuity equation of secondary phase is as follow:

$$
\frac{\partial}{\partial t} \left(\alpha_w \rho_w \right) + \nabla \cdot \left(\alpha_w \rho_w \overrightarrow{u_w} \right) = S_m \tag{4}
$$

Momentum equation:

$$
\frac{\partial(\rho \vec{\mu})}{\partial t} + \nabla \cdot (\rho \vec{u} \vec{u}) = \nabla \left[\mu \left(\nabla \vec{u} + \nabla \vec{u}^T \right) \right] - \nabla p + \rho \vec{g} + F_{vol} \tag{5}
$$

Energy equation:

$$
\frac{\partial(\rho E)}{\partial t} + \nabla \cdot (\rho E \vec{u}) = \nabla (k \cdot \nabla T) + \nabla \cdot (\rho \vec{u}) + S_e \tag{6}
$$

Evaporation scheme.

Number	Tube type	ε (b/a)	b (mm)	a (mm)
A	Circular tube		13.93	13.93
B	Half-oval tube 1	2	21.14	10.57
\mathcal{C}	Half-oval tube 2	3.2	26.20	8.20
D	Half-oval tube 3	4	28.52	7.13
Е	Half-oval tube 4	5	30.65	6.13

Table 1 Tube type parameters

Heat and mass transfer process for gas liquid phase is calculated by Lee model according to previous paper [\[7](#page-10-4)]. In order to use Lee model, the continuity equation need to be amended.

$$
\frac{\partial}{\partial t} \left(\alpha_g \rho_g \right) + \nabla \cdot \left(\alpha_g \rho_g \overrightarrow{u_g} \right) = m_{lg} - m_{lw} \tag{7}
$$

In Lee model, the evaporation process that water evaporates into vapor occurs if water temperature is larger than T_{sat} . In contrast, the counterpart process is condensation that gas condenses into liquid. The above two process was described by the following equations:

$$
m_{lg} = -\omega_{eff} \cdot \alpha_w \rho_w \frac{T_l - T_{sat}}{T_{sat}} T_l > T_{sat} \tag{8}
$$

$$
S_e = -\text{coeff} \cdot \alpha_w \rho_w \frac{T_l - T_{sat}}{T_{sat}} H \tag{9}
$$

$$
m_{gl} = \text{coeff} \cdot \alpha_g \rho_g \frac{T_{sat} - T_g}{T_{sat}} T_g < T_{sat} \tag{10}
$$

$$
S_e = \text{coeff} \cdot \alpha_g \rho_g \frac{T_{sat} - T_g}{T_{sat}} H \tag{11}
$$

where $\nabla = \frac{\partial}{\partial x} \vec{i} + \frac{\partial}{\partial y} \vec{j} + \frac{\partial}{\partial z} \vec{k}$, *coeff* is set as 0.1 based on the literature [\[25](#page-10-22)].

The continuum surface force scheme presented by Brackbill [\[26](#page-10-23)] was used to calculate the surface tension of liquid flm. The source term of surface tension which is in the momentum equation can be calculated using the following expression.

$$
F_{vol} = \sigma k \nabla \alpha \tag{12}
$$

The thermophysical parameters of mixture can be obtained by adding the product of volume fraction α and parameters of each phase:

$$
\rho = \left(1 - \alpha_l\right)\rho_g + \alpha_l \rho_l \tag{13}
$$

$$
\mu = (1 - \alpha_l)\mu_g + \alpha_l \mu_l \tag{14}
$$

$$
E = \frac{(1 - \alpha_l)\rho_g E_g + \alpha_l \rho_l E_l}{(1 - \alpha_l)\rho_g + \alpha_l \rho_l} \tag{15}
$$

$$
\alpha_l + \alpha_g = 1 \tag{16}
$$

Local and mean heat transfer coefficient are described below:

$$
h = \frac{q}{T_w - T_i} \tag{17}
$$

$$
h_{ave} = \frac{1}{l} \int_{0}^{l} h dx
$$
\n(18)

2.3 The grid model and boundary conditions

The boundary layer mesh was used to improve the quality of mesh, The thickness of frst layer mesh next to the tube surface is 0.01 mm, which can extract liquid flm thickness

Table 2 Physical property parameters

Physical parameter	Water liquid	Water vapor	
Density, $kg/m3$	997	0.0231	
Viscosity, $kg/(m \cdot s)$	8.94e-04	9.87e-06	
Surface Tension, N/m	0.072		
Specific heat $kJ/(kg \cdot K)$	4.183	1.878	
Thermal conductivity, $W/(m \cdot K)$	0.595	0.0186	

Fig. 3 Grid independence verification ($\varepsilon = 3.2$, Re=1104)

accurately. As illustrated in Fig. [2,](#page-3-0) velocity inlet and pressure inlet are in the top area. The volume fraction of water in velocity inlet is set to 1. The width of water inlet is 1 mm with a spray height of 10 mm. The inlet water temperature and the saturation temperature are 298.15 K and 303.15 K respectively. The tube surface is stationary wall boundary condition and the heat fux to wall is 30 Kw. The left side is defned as symmetry boundary condition, and the remaining two brim are pressure outlet.

2.4 Fluid properties and assumptions

The Reynolds number range for the transition from laminar to turbulent flow is 4000 to 6000 $[27]$ $[27]$, which means that the flow is laminar if the Reynolds number is less than 4000. The Reynolds number range of this study is 938 to 1430, so the fow is considered to be laminar.

Fig. 4 Verification of time step independence ($\varepsilon = 3.2$, Re=1104, $X = 0.5$

Reasonable simplifcation can consider the major factors and ignore the minor ones to accelerate the computational rate under the premise that simulation result is close to the experimental value. For the purpose of simplifying the simulation process, some assumptions are given as follows: (a) The contact angel is set to 0° , (b) Liquid water is incompressible. (c) The operating condition is considered as adiabatic. (d) Pressure is constant in the computational domain. (e) No properties diference of fuid exits in the simulation process. Table [2](#page-3-1) display the parameters of two fuid.

2.5 Mesh independence

The mesh density is a decisive factor for the result of simulation. An appropriate mesh density can not only ensure the accuracy of simulation results but also reduce the simulation

(a) Mean heat transfer coefficient $(D = 25.4 \text{ mm})$ (b) Falling film thickness in circumferential direction ($D = 25.4$ mm, $Re = 574$)

Fig. 6 Reliability verifcation of model

time. The model was divide by the quadrilateral mesh to improve the mesh quality and calculate the flm thickness accurately.

Figure [3](#page-4-0) indicated that the mean flm thickness is almost a constant data when grid number of the model is greater than 51932. It is obvious that 51392 is a appropriate number of grids, so the following simulation was carried out in the condition of 51932 grid number. In the same principle, the proper grid number of other tubes are obtained.

Time step is also a crucial factor which effect the accuracy of simulation result. The following time steps were used to perform the validation of time step independence: 0.005, 0.01, 0.02, 0.05 and 0.1 ms. Figure [4](#page-4-1) reveals that the flm thickness tends to be stable when time step is less than 2×10 -5 s. Thus, the final time step was chose to be 2×10^{-5} s by many times of explorations and comparing the simulation data and experimental results.

2.6 Solution methods

According to previous literature and comparison of diferent simulation methods, the following solution methods are

(a) Round tube (b) half-oval tube

Fig. 7 The component force of gravity for diferent tube shape

adopted: PISO algorithm is applied for velocity–pressure coupling, which has a faster iteration speed. Pressure interpolation scheme utilizes Body Force Weighted model because gravity is considered in the simulation process. The spatial discretization of momentum and energy employ Second order upwind. Geo-Reconstruct method is used to capture the boundary of water flm.

Fig. 9 Film thickness of diferent tube.

3 Model verification

The experimental platform was established to prove the reality of numerical model. Figure [5](#page-4-2) presented the schematic diagram of experiment device. The experimental table contains three parts: the water circulation equipment, image acquisition system and measurement device of liquid flm. The test tube was a horizontal half-oval tube ($\varepsilon = 3.2$) which made of aluminum alloy. The test tube and distribution tube have the same length that is 150 mm. The distribution tube

0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.45 0.50 0.55 0.60 0.65 0.70 0.75 0.80 0.85 Film thickness(mm) $x^{0.5}$ $-$ Re=938 Re=1104 Re=1420

Fig. 8 Film velocity of diferent tube shape in circumferential $direction(Re=1104)$

Fig. 10 Comparison of flm thickness under shape in circumferential direction(Re=1104) different Reynolds number (ϵ = 3.2)

has a special structure to make sure the 7 spray holes whose radius is same with the simulation model have the equal spray density. To measure the flm thickness with laserinduced fluorescence method, the dye of Rhodamine B with intense fuorescence was added into water. The dye can generate fuorescent light with a wavelength range of 578–610 nm when irradiates by green laser $[28]$ $[28]$, Thus it is easy to distinguish the water flm when take pictures through a flter. MATLAB is used to process all the photos. Parken calculated the mean heat transfer coefficient with a experiment in the condition of evaporation [\[19\]](#page-10-16), which is similar with our simulation condition. The simulation model of circular tube whose diameter is 25.4 mm was built, the mean heat transfer coefficient under different Reynolds number and the flm thickness in circumferential direction under the condition of $Re = 574$ were compared with experiment value in the paper of Parken et al. [[19\]](#page-10-16) and Zhao et al. [\[29](#page-10-26)], respectively. As illustrated in Figs. 5 and $6(a)$ $6(a)$, (b), (c) the variation trend of falling flm thickness and average heat transfer coefficient are similar with experimental value, and the diference of each point between simulation data and experimental values are within 9.8%.

4 Results and discussion

4.1 Velocity and liquid film thickness under different tube shape

The liquid film flows along the circumference in a combined function of gravity, surface tension, viscous force. As shown in Fig. [7](#page-6-0) the component force of gravity in flow direction of half-oval tube is larger than that of round tube, which indicates that the liquid flm has a greater acceleration when fows along the circumferential direction. And the component force of gravity is in proportion to ε , which means that the velocity of liquid flm increases as the tube shape gets narrow and long. As illustrated in Figs. [6](#page-5-0)[-8](#page-6-1), the flm velocity increases along the perimeter direction. The slope of the tangent line for flm velocity curve gets smaller and smaller with X increasing. The flm velocity gradually increases since water column collide tube surface because of the efects of gravity. Then several kinds of forces are almost balanced when circumferential dimensionless location is close to 1, so the flm velocity is nearly a constant value. As ε increases, the component of gravity in flow direction increase, which leads to a increase in flm velocity. The mean flm velocity of tube B, C, D, E are approximately 4.5%, 7.6%, 11.2%, 14.5% greater than that of the round tube.

A larger velocity make the falling flm is not easily accumulate on the tube wall. That is to say, a greater velocity indicates a thinner flm thickness. As described in Figs. [7](#page-6-0)-[9,](#page-6-2) mean flm thickness of tube B, C, D, E are about 3.7%, 6.3%, 8.6%, 11.4% lesser than that of the round tube respectively. The relationship between flm thickness and Reynolds number is similar to the circular tube, Figs. [8-](#page-6-1)[10](#page-6-3) shows a larger Reynolds number also results in a thicker liquid flm thickness on the half-oval tube.

4.2 Heat transfer performance under different tube shapes

The heat transfer coefficient of the five tubes for different circumferential dimensionless location are illustrated in Figs. [9-](#page-6-2)[11.](#page-7-0) The variation tendency of heat transfer coefficient frst obviously lower and gradually become stable along the perimeter direction. The heat transfer coefficient has a visible diference at top half of the tube wall, that phenomenon resembles the distribution of liquid flm. The reason is that the impact of water column impingement is lager on the top area of the tube wall, the liquid flm is strongly disturbed and thus has a larger heat transfer coefficient. For any one of the five tubes, heat transfer coefficient in the upper area play a dominate role in overall heat transfer performance. The local heat transfer coefficient is in direct proportion to ϵ . Contrasted with the circular tube, half-oval tube has a greater velocity and thinner flm thickness, so it can improve the heat transfer performance. To be precise, the mean heat transfer coefficient over half-oval tube B, C, D, E are about 3.2%, 6.5%, 8.7%, 11.3% greater than that of the round tube respectively.

The dimensionless temperature θ is introduced to further understand the mechanism that heat transfer coefficient change with ε . The dimensionless temperature inside the liquid film is illustrated in Figs. $10-12(a)$ $10-12(a)$ $10-12(a)$, (b), (c), (d), (e). In all the fve tubes, the dimensionless temperature

Fig. 11 Heat transfer coefficient for different tube shapes $(Re = 1104)$

Fig. 12 Dimensionless temperature distribution of diferent tubes (Re=1104)

gradually increases along the circumferential direction, it decreases faster in the upper part than that in the lower part, which indicates that the local temperature gradient gets smaller and thermal boundary layer becomes thicker along the perimeter direction. This means that local heat transfer performance gets worse and worse with the increase of circumferential angle.

The dimensionless temperatures of diferent tubes at 0.1, 0.5 and 0.9 circumferential dimensionless location are compared in Figs. [11-](#page-7-0)[13](#page-9-1) The dimensionless temperature distribution shows a similar trend at the three circumferential dimensionless location, the dimensionless temperature decreases with ε increasing. This further accounts for that half-oval tubes have a smaller thermal boundary layer and higher heat transfer efficiency than round tube A.

5 Conclusions

The falling flm distribution and heat transfer performance over five tubes with the same perimeter and different shape was calculated by using a 2-D model. Half-oval tubes is better than round tube in flm thickness, dimensionless temperature and heat transfer coefficient. The larger the ε , the more obvious the advantage of half-oval tube. According to the discussion and analysis above, it can be came to the following conclusions:

(1) The flm thickness increases with Reynolds number increasing, and presents a variation trend that frst rapidly decreases and then almost becomes stable in circumferential direction. The flm thickness gradually decreases with ϵ from 1 to 5. The mean film thickness over halfoval tubes are approximately 3.7–11.4% lesser than that of circular tube.

(2) The mean flm velocity of four half-oval tubes are nearly 4.5–14.5% higher than that of round tube.

(3) Local heat transfer coefficient gets smaller along the perimeter direction, and becomes larger and larger as ε increasing. The mean heat transfer coefficient over halfoval tube B, C, D, E are about 3.2%, 6.5%, 8.7%, 11.3% larger than that of round tube.

(4) In summary, Half-oval tube ($\varepsilon = 5$) has the thinnest film thickness and largest heat transfer coefficient.

Declarations

Conflict of interest The authors declared that there is no confict of interest.

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