## ORIGINAL



# Mechanical properties of Japanese black pine (*Pinus thunbergii* Parl.) planted on coastal sand dunes: resistance to uprooting and stem breakage by tsunamis

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# Abstract

Given that Japanese black pine trees (Pinus thunbergii Parl.) are predominant in the coastal forests of Japan and are part of the defence structure against tsunamis, the quantification of their resistance to tree damage is necessary. The resistance of Japanese black pine to uprooting and stem breakage and its bending properties were estimated by a tree-pulling test and bending test of green logs in conjunction with the published literature. A general equation to estimate the critical turning moment for uprooting was developed using diameter at breast height and tree height as predictor variables. For moduli of elasticity and rupture of stems (MOE and MOR), medians [5th and 95th percentile values] were 5.41 [3.78, 6.82] GPa and 35.0 [28.7, 41.8] MPa, respectively. With the obtained critical turning moment and MOR, the critical tsunami water depth was estimated by numerical simulations using modelled trees. The numerical simulations revealed that Japanese black pine trees on coastal sand dunes tended to be more vulnerable to uprooting than stem breakage, with taller and more slender trees showing less resistance to stem breakage. The results on the mechanical properties of Japanese black pine are of use to those in the wood science community as well as coastal managers who need to know the mechanical strength of Japanese black pine to help evaluate their resistance against tsunamis.

# Introduction

Study on the response of trees to stress has taken many different vantage points. Some studies have examined the effects of insect stressors (e.g. Kimmins 1972; Hollinger 1986; Konta 2001), drought (e.g. Williams et al. 2013) or forest management (Pretzsch and Rais 2016) on trees and forests. Other studies have focused

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on the mechanical strength of wood and examined the effects of air temperature (Schmidt and Pomeroy 1990; Silins et al. 2000), ice storms (Lemon 1961; Seischab et al. 1993; Nock et al. 2016), snow capping (Cannell and Morgan 1989; Kinar and Pomeroy 2015) and wind (e.g. Merrill 1948; Bascuñán et al. 2006; Auty and Achim 2008) on tree trunk and/or branch bending or breakage. The structural analysis of tree trunks and branches has also been utilized to better understand the effects of complex loading on deflection (Morgan and Cannell 1987). A thorough and comprehensive understanding of the physical breakage of tree branches and stems is important from many perspectives, ranging from the development or validation of theories on the mechanical properties of wood to the management of forest buffer zones.

Coastal forests play a vitally important role in mitigating the deleterious effects of strong wind, blown sand, airborne salt and tsunamis (Murai et al. 1992; Suzuki et al. 2016). The protective role of coastal forests against tsunamis has attracted concerted attention since the 1998 Papua New Guinea tsunami (Dengler and Preuss 2003), the 2004 Indian Ocean tsunami (Danielsen et al. 2005; Forbes and Broadhead 2007; Rossetto et al. 2007), and the tsunami caused by the Great East Japan Earthquake in 2011 (Tanaka et al. 2013; FFPRI 2015). On the other hand, coastal forests are sometimes destroyed by tsunamis. To evaluate the effect of coastal forests as a part of multi-defence structure against tsunamis, the quantification of their resistance to tree damage is necessary. In Japan, Japanese black pine (*Pinus thunbergii* Parl.) is the most popular species for planting in these shelterbelt coastal forests because of its ability to grow in the most severe coastal environments and persist, despite sand saltation and salt exposure (Oda 2003; Nakashima and Okada 2011; Suzuki et al. 2016). Few studies, however, have been conducted on estimating the resistance of Japanese black pine to tree damage.

There are two main types of tree damage by a tsunami: uprooting and stem breakage (Tanaka et al. 2013). The resistance to uprooting is determined from root-soil plate anchorage, which in turn depends on the root-soil plate weight, depth and diameter of the root-soil plate, as well as the soil properties (Coutts 1986; Peltola et al. 1999). The root anchorage is influenced by soil and rooting conditions (Nicoll et al. 2006), but no direct evidence for a reduction in the resistance due to soil saturation can be detected because the additional weight of the water in the soil compensates for any loss of soil strength (Gardiner et al. 2016). Since it is difficult to estimate the weight and the size of a root-soil plate nondestructively, the root anchorage is estimated by aboveground tree size, such as stem diameter at breast height  $(D_{\rm BH})$ , tree height  $(H_{\rm tr})$  and stem mass, with the results from tree-pulling tests (Peltola et al. 2000; Nicoll et al. 2006; Kamimura et al. 2012). From the tree-pulling tests, the critical turning moment at the stem breakage point is obtained. When the tree is uprooted, the stem breakage point is assumed at the tree base. In general, larger trees have larger root anchorage due to larger root-soil plates. Previous studies have estimated the critical turning moment by power regression with  $D_{\rm BH}$  (e.g. Fukami et al. 2011), linear regression with  $H_{\rm tr} \times D_{\rm BH}^2$  (e.g. Cucchi et al. 2004; Peltola et al. 2000; Todo et al. 2015) or linear regression with stem mass (e.g. Achim et al. 2005; Gardiner et al. 2000). The stem mass is mechanistically the best-fit variable to estimate the critical turning moment (Peterson and Claassen 2013); however, it is a difficult quantity to obtain non-destructively. Therefore,  $D_{\rm BH}$  and  $H_{\rm tr}$  are the most accessible predictors to estimate a tree's resistance to uprooting.

Despite the dominance of Japanese black pine trees in these coastal forests, rather few studies have estimated their resistance to uprooting. The existing studies on the resistance of Japanese black pine to uprooting (Imai and Suzuki 2005; Kondo et al. 2006; Ono and Ishikawa 2012; Imai et al. 2013; Miyata et al. 2013; Noguchi et al. 2014) had small sample sizes based on smaller trees and fewer trees > 0.2 m in  $D_{\rm BH}$ . Therefore, the present comprehensive estimation of the critical turning moment for Japanese black pine is based on an integration of all of the previous data from past studies plus new data from larger trees with a  $D_{\rm BH}$  > 0.2 m.

The resistance to stem breakage is determined by the bending strength of the stem. The modulus of rupture (MOR) of tree stems has been measured by bending tests as the bending strength, simultaneously obtaining the modulus of elasticity (MOE) (Koizumi 1987; Tanaka et al. 1994; Ruel et al. 2010; Ido et al. 2013). MOE and MOR vary among and within tree species, and are influenced by wood properties. For example, larger annual ring width causes lower MOE and MOR because the relative percentage of earlywood is higher (Koizumi 1987; Kato and Nakatani 2000). Cambial age is one of the variables that were found to influence the MOE because juvenile wood was more elastic than mature wood. The MOE increased with age and gradually reached a maximum (Koizumi 1987; Leban and Haines 1999; Bascuñán et al. 2006; Auty and Achim 2008; Sattler et al. 2014). In addition, MOR decreased with the number of branch knots and presence of rot (Ruel et al. 2010; Gardiner et al. 2016).

Whereas there are a litany of studies examining the bending strength and elasticity of timbers in wood science, for example, as the database summarized in Forest Products Laboratory (1999), there is a dearth of information on stem breakage from living Japanese black pine trees or green logs. Therefore, the actual measurement of MOE and MOR for green logs is necessary for estimating the resistance of Japanese black pine to stem breakage. MOR of fresh stems was measured by Imai et al. (2013) and estimated by Noguchi et al. (2014) to quantify the critical bending stress to trigger stem breakage, but the sample sizes were small with three and one trees, respectively.

There are many forces acting on structures in tsunamis (Federal Emergency Management Agency 2012), including direct hydrostatic and hydrodynamic forces from water inundation, impact forces from water-borne debris, and scour and slope/foundation failures (Tanaka et al. 2013). Numerical simulations are useful to evaluate the resistance of Japanese black pine trees against tsunamis. For example, Noguchi et al. (2012) evaluated the partial damage and the mitigation effect of the inundation flow by coastal forests composed of Japanese black pine. Tanaka et al. (2013) confirmed the efficacy of the coastal forest to trap debris (including large trees and car debris) in tsunamis by calculating critical  $D_{\rm BH}$  of Japanese black pine trees. The influence of tree size on tree damage rate and type was verified from calculations of critical tsunami flow velocity (Torita et al. 2014). These studies confirmed the effectiveness of the numerical simulations by comparison with field surveys of damaged trees by the tsunami of the Great East Japan Earthquake in 2011. Applications of numerical simulations better clarify the resistance of Japanese black pine trees in coastal forest to damage by tsunamis and their ability to mitigate damage.

With specific regard to Japanese black pine trees growing on coastal sand dunes, the objectives of this study were to: (1) quantify the resistance to uprooting in relation to tree size; (2) quantify the resistance to stem breakage in relation to wood properties; and (3) estimate resistance to tree damage by tsunamis through numerical simulations. By examining live trees in the field, this study will augment the database on the mechanical properties of tree strength for Japanese black pine and supply coastal managers with relevant data on the ability of Japanese black pine to survive from interactions with tsunamis.

## Materials and methods

#### Tree-pulling test and estimation of the resistance to uprooting

A tree-pulling test was conducted on six Japanese black pine trees on the coastal sand dunes of Kaga National Forest (Ishikawa, Japan (36°18'N, 136°16'E)) in September 2014 to measure their resistance to uprooting. The six trees were between 89 and 98 years old, with  $D_{\rm BH}$  ranging from 0.2 to 0.3 m and  $H_{\rm tr}$  ranging from 10.5 to 15.3 m (Table 1). The maximum root clump depth ranged from 1.9 to 3.2 m, with a mean root clump mass of 268.1 kg (Table 1).

A soft polyester yarn sling was positioned on the tree stem between 2 and 4 m above ground and connected to a steel wire which was pulled by a backhoe until peak tensile load was confirmed (Fig. 1). Tensile load was measured by a 100-kN capacity load cell (TR2110H, Minebea, Nagano, Japan) or 20-kN capacity load cell (LUX-B-20KN-I, Kyowa Electronic Instruments, Tokyo, Japan) connected between the polyester sling and steel wire and recorded by a 100 Hz datalogger (EDS-400A, Kyowa Electronic Instruments, Tokyo, Japan) and a laptop computer. The angle between the pulled stem and vertical direction ( $\alpha$ , rad) and the angle between the tensile direction and horizontal direction ( $\beta$ , rad) were acquired from video feed positioned at a right angle to the tensile direction. After the tree-pulling tests, each stem was segmented into logs, and both the logs and foliage were subsequently weighed. In addition, the root clumps of each tree were excavated, and root mass, maximum rooting depth and length of eight root radii (every 45°) were measured.

According to Nicoll et al. (2005), the turning moment at the stem breakage point ( $M_{\text{total}}$ , N m, Eq. 1) is calculated as the sum of the turning moment by tree pulling ( $M_{\text{pull}}$ , N m, Eq. 2) and the turning moment by tree weight ( $M_{\text{gravity}}$ , N m, Eq. 3) as per the below equations:

$$M_{\rm total} = M_{\rm pull} + M_{\rm gravity} \tag{1}$$

$$M_{\text{pull}} = P_{\text{T}} \left( h_{\text{p}} - h_{\text{b}} \right) \cos \left( \alpha - \beta \right)$$
<sup>(2)</sup>

$$M_{\text{gravity}} = g(h_{\text{g}} - h_{\text{b}}) \sin \alpha \int_{h_{\text{b}}}^{h} w(z) dz$$
(3)

		Abovegrou	nd					Root clump			Pulling test				
#	Age (year)	$D_{ m BH}( m cm)$	$D_0$ (cm)	$H_{\mathrm{tr}}(\mathrm{m})$	$H_{\rm cb}$ (m)	Stem vol- ume (m <sup>3</sup> )	Total mass (kg)	Maximum depth (m)	Mean radius (m)	Mass (kg)	Breakage type <sup>a</sup>	$h_{\rm p}({\rm m})$	$h_g$ (m)	$h_{\rm b}$ (m)	$M_{ m max}$ (10 <sup>3</sup> N m)
-	97	24.5	30.7	14.4	5.5	0.398	345.0	3.2	2.2	190.6	SB	3.0	5.1	0.5	55.9
0	93	20.1	25.5	10.5	2.2	0.163	249.0	1.9	3.0	202.8	U	2.0	4.1	0	38.9
Э	89	28.5	29.5	11.1	3.1	0.328	576.9	2.0	2.3	319.3	U	3.1	4.1	0	79.7
4	92	30.1	36.2	15.3	4.4	0.485	728.7	2.0	3.1	384.9	U	4.0	6.0	0	102.6
5	98	23.8	29.5	11.7	4.1	0.306	397.7	2.4	3.6	267.9	U	2.2	4.6	0	69.5
9	98	28.4	31.3	14.5	3.5	0.404	527.9	2.5	2.7	243.2	U	3.0	5.3	0	85.7
$D_{\rm BH}$	$_{\rm H}$ stem diamet ravity. $h_{\rm h}$ hei	ter at breast l ght at broker	height (1.5 1 point, M	$(10^{\circ} M), D_0 S$	stem diame al turning 1	ster at the tre moment for t	e base, H <sub>u</sub> tre ree breakage	se height, $H_{\rm cb}$	, the heigl	ht of crown b	ottom, <i>h</i> <sub>p</sub> hei	ight at pu	od gulli	int, $h_{\rm g}$ he	ight at centre

 Table 1
 Descriptive statistics and pulling test data for Japanese black pine trees in this study

<sup>a</sup>SB stem breakage, U uprooted



**Fig.1** Schematic diagram of the tree-pulling test, where  $P_{\rm T}$  denotes tensile load,  $\alpha$  and  $\beta$  denote the angles between the pulled stem and vertical direction and between the tensile direction and horizontal direction, respectively, and  $h_{\rm g}$ ,  $h_{\rm p}$ , and  $h_{\rm b}$  denote the heights of centre of gravity, pulling point and stem breakage point, respectively

where  $P_{\rm T}$  is tensile load (N),  $h_{\rm p}$ ,  $h_{\rm b}$  and  $h_{\rm g}$  are the heights of pulling point (m), stem breakage point (m) and centre of gravity (m), respectively, g is the acceleration of gravity (m s<sup>-2</sup>), and w(z) is the mass of the tree at height z (m). The maximum  $M_{\rm total}$ was considered as the critical turning moment for tree breakage ( $M_{\rm max}$ , N m). When the tree was uprooted,  $h_{\rm b}$  was zero and  $M_{\rm max}$  was considered the critical turning moment for uprooting ( $M_{\rm Currow}$ , N m).

The resistance of Japanese black pine trees to uprooting was estimated by  $M_{C_{uproot}}$  based on a combination of current experimental results and the past literature with similar pulling tests on Japanese black pine trees inhabiting coastal dunes (Table 2; Imai and Suzuki 2005; Kondo et al. 2006; Ono and Ishikawa 2012; Imai et al. 2013; Miyata et al. 2013; Noguchi et al. 2014). The resistance to uprooting is normally predicted from the estimate of the root-soil plate weight (Peltola et al. 1999) or stem weight (Gardiner et al. 2000); however, these data were insufficient from the data set.  $M_{C_{uproot}}$  was estimated by a power regression with  $D_{BH}$  using 71 samples and a linear regression with  $H_{tr} \times D_{BH}^2$  using 46 samples.

## Bending test and the resistance to stem breakage

Fifteen straight stem logs from differing heights and eight straight coarse root sections were sampled from the pulled trees to measure both the MOE and MOR within 7 days of the pulling test. The pulled trees were covered with plastic sheets to minimize desiccation. Straight coarse root sections were preferentially selected

	Number of trees	$D_{\rm BH}({\rm cm})$	$H_{\mathrm{tr}}\left(\mathrm{m} ight)$	$M_{C_{uproot}} (10^3 \text{ N m})$
This study	5	20.1-30.1	10.5-15.3	38.9-102.6
Imai and Suzuki 2005	18	6.5-13.2	5.5-11.5	1.5-10.6
Kondo et al. 2006	5	10.7-22.9	9.1-13.9	6.8-65.1
Ono and Ishikawa 2012	12	14.0-40.3	NA	7.6–198.7
Imai et al. 2013	15	8.1-22.0	6.0 - 13.3	1.7-49.2
Miyata et al. 2013	13	15.7-29.2	NA	23.7-98.0
Noguchi et al. 2014	3	9.0-13.7	4.8-6.9	2.7-12.6
Total or range	71	6.5-40.3	4.8–15.3	1.5–198.7

**Table 2** Tree size and critical turning moment of Japanese black pine trees on coastal sand dunes gained by tree-pulling tests in this study and the past literature

 $D_{\rm BH}$  stem diameter at breast height (1.3 m),  $H_{\rm tr}$  tree height,  $M_{C_{unroot}}$  critical turning moment for uprooting

because the straight samples were desirable for the bending test. Sample properties are summarized in Table 3. Bending properties were measured using a universal testing machine of 1000-kN capacity (UH-1000kNXR, SHIMADZU, Kyoto, Japan). For purposes of computation, all of the logs were considered to represent tapered cylinders to calculate volume and wood density. Three-point bending tests (Fig. 2) were conducted on the selected logs. Since no standard exists for such tests, the bending tests for round timber described in Ido et al. (2013) were followed. The MOE was calculated by Eq. 4 considering the effect of taper, according to Sawada (1983):

$$MOE = \frac{Pl^3}{48l_m\delta_m} \frac{(1+\tau)^2}{4\tau} = \frac{Pl^3}{3\pi D_m^4\delta_m} \frac{(1+\tau)^2}{4\tau}$$
(4)

$$\tau = \frac{D_1}{D_2} \tag{5}$$

where *P* is load (N), *l* is the length between two supporting points (m),  $I_m$  is the second moment of area at the mid-span (m<sup>4</sup>),  $\delta_m$  is the deflection of the mid-span (m),  $D_m$  is the mean diameter at the mid-span,  $\tau$  is taper, and  $D_1$  and  $D_2$  are the mean diameters at thicker and thinner supporting points, respectively. Six displacement gauges (SDP-200D and CDP-100, Tokyo Sokki Kenkyujo Co., Ltd., Tokyo, Japan) were used to measure  $\delta_m$ . The displacement of both sides of a log at two supporting points and a compression point were measured. The MOR was calculated by Eq. 6 considering the effect of taper:

$$MOR = \frac{Pl}{4Z_{m}} \frac{(1+\tau)^{2}}{4\tau} = \frac{2Pl}{D_{m}} \frac{(1+\tau)^{2}}{\tau}$$
(6)

where  $Z_{\rm m}$  is the section modulus at the mid-span (m<sup>3</sup>). After the bending test, a disc (~3 cm thick) was extracted at 20 cm from the bending point in the thinner direction

Tree #	Log							Disc <sup>a</sup>			Mechanical pr	operty
	$D_{\rm m}({ m cm})$	2	<i>L</i> (m)	<i>l</i> (m)	$H_{\rm C}$	$\rho_{\rm W_{-fresh}}$ (kg m <sup>-3</sup> )	$\rho_{\rm W_{-dry}}$ (kg m <sup>-3</sup> )	Cambial age (year)	ARW (mm)	MC (%)	MOE (GPa)	MOR (MPa)
Stem												
1	16.2	0.645	4.02	3.6	0.493	7.979	377.9	30	2.40	159.3	4.76	28.3
1	8.9	0.454	2.64	1.8	0.264	908.5	399.6	17	2.53	127.4	5.43	33.1
1	5.0	0.667	1.27	0.9	0.132	1069.8	475.3	8	2.69	125.1	5.41	42.2
2	13.9	0.640	3.65	2.7	0.586	1064.9	466.1	23	2.81	128.5	6.44	39.7
2	9.2	0.575	2.21	1.8	0.314	1124.6	476.1	12	3.30	136.2	4.04	30.0
2	4.6	0.613	1.23	0.9	0.105	992.6	384.7	9	3.24	158.0	3.16	41.6
3	9.6	0.278	3.04	1.8	0.279	1160.1	461.0	12	3.21	151.6	4.17	30.8
4	25.2	0.636	6.07	5.4	0.719	1020.1	451.4	62	1.94	126.0	6.42	35.0
4	14.8	0.492	4.06	2.7	0.392	1108.0	470.9	17	4.05	135.3	6.24	39.2
4	9.9	0.394	2.06	1.8	0.196	831.0	328.5	L	4.82	152.9	4.76	34.4
5	15.1	0.511	4.00	3.6	0.462	876.4	383.9	21	3.33	128.3	7.15	40.2
5	22.2	0.724	4.31	4.0	0.816	797.0	337.9	63	1.58	135.8	6.42	35.5
6	18.6	0.778	4.23	3.6	0.566	976.3	401.0	24	3.69	143.5	6.68	36.6
6	13.8	0.594	3.22	2.7	0.310	1100.7	418.7	15	4.33	162.9	4.99	30.4
6	6.5	0.334	2.01	1.8	0.131	1002.6	388.2	8	3.24	158.3	4.08	28.9
Median	13.8	0.594				1002.6	401.0	17.0	3.24	136.2	5.41	35.0
5th percentile	4.9	0.317				820.8	335.1	6.7	1.83	125.7	3.78	28.7
95th percentile	4.9	0.740				1135.3	475.5	62.3	4.48	160.4	6.82	41.8
Root												
1	8.8	0.782	1.69	0.9		870.2	499.7	26	1.51	74.1	7.94	49.9
2	12.5	0.749	1.56	0.9		967.8	528.3	27	2.20	83.2	5.93	49.7

Tree #	Log						$Disc^{a}$			Mechanical p	operty.
	$D_{\rm m}$ (cm)	z	<i>L</i> (m)	<i>l</i> (m) <i>H</i>	$\Gamma_{\rm C} = \rho_{\rm W_{-fresh}}  ({\rm kg}  {\rm m}^{-3})$	) $\rho_{\rm W_{-dry}}  (\rm kg \ m^{-3})$	Cambial age (year)	ARW (mm)	MC (%)	MOE (GPa)	MOR (MPa)
2	11.1	0.650	1.02	0.0	881.4	500.3	29	1.81	76.2	3.83	32.3
3	5.1	0.622	1.61	0.9	923.3	515.2	21	1.08	79.2	2.02	36.1
4	7.1	0.653	1.52	0.9	909.5	474.3	22	1.53	91.7	12.66	48.7
5	6.0	0.924	1.86	1.8	1036.6	571.6	12	2.32	81.4	5.45	44.2
6	12.0	0.463	2.22	1.8	1068.5	532.0	31	1.84	100.8	6.94	46.0
6	3.9	0.664	0.96	0.9	908.7	535.1	11	1.55	69.8	9.29	64.4
Median	8.0	0.659			916.4	521.8	24.0	1.68	80.3	6.44	47.4
5th percentile	4.3	0.519			874.1	483.2	11.4	1.23	71.3	2.65	33.6
95th percentile	12.3	0.874			1057.3	558.8	30.3	2.28	97.6	11.48	59.3

span,  $\rho_{W_{\rm fresh}}$  fresh wood density,  $\rho_{W_{\rm dy}}$  dry wood density, ARW average annual ring width, MC moisture content, MOE modulus of elasticity, MOR modulus of rupture <sup>a</sup>Disc was sampled at 20 cm from the bending point of the log in the direction of log taper



of the log. From the disc, cambial age, average annual ring width and moisture content (by the oven-dry method) were determined.

## Estimation of the resistance to tree damage against tsunamis

To estimate the resistance to tree damage against tsunamis, a numerical simulation for modelled trees was conducted. Two different tree shapes were created with  $H_{\rm tr}/D_{\rm BH}$  values of 50 and 70, respectively, with  $H_{\rm tr}$  ranging from 2 to 16 m. Stem profiles of the modelled trees were determined by the Behre hyperbola (Bruce 1972) in Eq. 7 as:

$$D' = \frac{L'}{a+bL'} \tag{7}$$

where D' is relative stem diameter standardized by diameter at L'=0.9, L' is relative tree length from the tree top standardized by  $H_{tr}$ , and a and b are constants chosen to match a tree's general profile. Thus, stem diameter at height z (D(z), m) was calculated in Eq. 8 as:

$$D(z) = D(0.1H_{\rm tr}) \frac{\frac{H_{\rm tr}-z}{H_{\rm tr}}}{a+b\frac{H_{\rm tr}-z}{H_{\rm tr}}}$$
(8)

where  $D(0.1H_{tr})$  was calculated in Eq. 9 with  $D_{BH}$  and  $H_{tr}$  as:

$$D(0.1H_{\rm tr}) = D_{\rm BH} \frac{a + b \frac{H_{\rm tr} - 1.3}{H_{\rm tr}}}{\frac{H_{\rm tr} - 1.3}{H_{\rm tr}}}$$
(9)

Based on data from the five pulled trees (Table 1), a=0.590 and b=0.344 were applied, respectively, by the least-squares method (Fig. 3). Tree #3 was not used, because the tree was forked at 3.6 m. The horizontal projected area of the stem less than height  $z [0 \le z \le H_{\rm tr}] (S_{\rm st}(z), m^2)$  was calculated as:

$$S_{\rm st}(z) = \int_{0}^{z} D(z) \mathrm{d}z \tag{10}$$

The crown profile of the trees was assumed to be of circular cone shape. Thus, the horizontal projection areas of the trees were triangular. A crown length of  $0.7H_{\rm tr}$ 



**Fig. 3** Relationship between relative stem diameter (D') and relative tree length from the tree top (L') of five Japanese black pine trees in this study. Dashed line indicates regression curve shown in Eq. 7

was applied as determined from the six pulled trees (Table 1), and thus the height of crown bottom ( $H_{cb}$ , m) was  $0.3H_{tr}$ . Total projected branch areas ( $A_{br}$ , m<sup>2</sup>) or needle areas ( $A_{nd}$ , m<sup>2</sup>) of a tree were estimated  $D(H_{cb})$  using the following equations for Japanese black pine derived from Noguchi et al. (2012):

$$A_{\rm br} = 32D \big(H_{\rm cb}\big)^{1.7} \tag{11}$$

$$A_{\rm nd} = 813D \big(H_{\rm cb}\big)^{2.4} \tag{12}$$

where  $D(H_{cb})$  was calculated from Eq. 8. The branch and needles were uniformly distributed within the canopy crown area. The horizontal projected branch and needle areas lower than height *z*, i.e. submerged by a tsunami (Fig. 4:  $S_{br}$  and  $S_{nd}$ , respectively, m<sup>2</sup>), were calculated as:

$$S_{\rm br}(z) = \begin{cases} 0[z \le H_{\rm cb}] \\ A_{\rm br} \left( 1 - \frac{(H_{\rm tr} - z)^2}{(H_{\rm tr} - H_{\rm cb})^2} \right) & [H_{\rm cb} < z \le H_{\rm tr}] \\ A_{\rm br} [z > H_{\rm tr}] \end{cases}$$
(13)

$$S_{\rm nd}(z) = \begin{cases} 0[z \le H_{\rm cb}] \\ A_{\rm nd} \left(1 - \frac{(H_{\rm tr} - z)^2}{(H_{\rm tr} - H_{\rm cb})^2}\right) & [H_{\rm cb} < z \le H_{\rm tr}] \\ A_{\rm nd} [z > H_{\rm tr}] \end{cases}$$
(14)

Deringer



**Fig. 4** Horizontal projected areas of submerged branches and needles ( $S_{br}$  and  $S_{nd}$ , respectively) by tsunami of height *z* calculated by crown diameter ( $D_{crown}$ ), tree height ( $H_{tr}$ ), height of crown bottom ( $H_{cb}$ ). Total projected branch area is  $A_{br}$ 

For the hydrodynamic forces due to water inundation by tsunamis (F), the resultant force acting on a tree is (Tanaka et al. 2013):

$$F = F_{\rm drag} + F_{\rm impulse} = (1 + k_{\rm di})F_{\rm drag}$$
(15)

where  $F_{drag}$  is drag force,  $F_{impulsive}$  is impulsive force caused by the leading edge of a surge of water impacting a tree, and  $k_{di}$  is the ratio of impulsive force to drag force. For  $k_{di}$ , a value of 1.5 was assigned in accordance with Federal Emergency Management Agency (2012) and Tanaka et al. (2013). Further, uniform water flow was applied with no vertical velocity gradient for a tsunami in accordance with Torita et al. (2014). The drag force by tsunami with a certain water height ( $H_W$ , m) to a tree was separately calculated with tsunami loads to stem ( $F_{st}$ ), branches ( $F_{br}$ ) and needles ( $F_{nd}$ ) by Eqs. 16–18 according to Tanaka et al. (2013) and Torita et al. (2014):

$$F_{\rm st}(z) = \frac{1}{2} \left( 1 + k_{\rm di} \right) \rho u^2 S_{\rm st}(z) C_{D_{\rm st}} = \frac{1}{2} \left( 1 + k_{\rm di} \right) (Fr)^2 \rho g H_{\rm ts} S_{\rm st}(z) C_{D_{\rm st}}$$
(16)

$$F_{\rm br}(z) = \frac{1}{2} \left( 1 + k_{\rm di} \right) \rho u^2 S_{\rm br}(z) C_{D_{\rm br}} = \frac{1}{2} \left( 1 + k_{\rm di} \right) (Fr)^2 \rho g H_{\rm ts} S_{\rm br}(z) C_{D_{\rm br}}$$
(17)

$$F_{\rm nd}(z) = \frac{1}{2} (1 + k_{\rm di}) \rho u^2 S_{\rm nd}(z) C_{D_{\rm nd}} = \frac{1}{2} (1 + k_{\rm di}) (Fr)^2 \rho g H_{\rm ts} S_{\rm nd}(z) C_{D_{\rm nd}}$$
(18)

where  $\rho$  is water density (=999.97 kg m<sup>-3</sup>), *u* is flow velocity (m s<sup>-1</sup>) and *Fr* is the Froude number (=  $u/\sqrt{gH_{ts}}$ ). *Fr* determines the relationship between flow water depth and flow velocity. 0.7 and 1.0 were applied for *Fr* because Tanaka et al. (2013) reported (from the previous literature) that *Fr* of most of the tsunami flow to be between 0.7 and 1.0. 0.85, 0.81 and 0.056 were applied for the drag coefficients of stem ( $C_{D_{st}}$ ), branch ( $C_{D_{br}}$ ) and needle ( $C_{D_{nd}}$ ) of Japanese black pine, respectively, as derived from Noguchi et al. (2012).

The turning moment of the stem at height z in water flow, M(z), was calculated by the below equations as:

$$M(z) = M_{\rm st}(z) + M_{\rm br}(z) + M_{\rm nd}(z)$$
(19)

$$M_{\rm st}(z) = \left(F_{\rm st}(H_{\rm W}) - F_{\rm st}(z)\right)H_{g_{\rm st}}(H_{\rm W}, z)$$
<sup>(20)</sup>

$$M_{\rm br}(z) = \left(F_{\rm br}(H_{\rm W}) - F_{\rm br}(z)\right)H_{g_{\rm br}}(H_{\rm W}, z)$$
(21)

$$M_{\rm nd}(z) = \left(F_{\rm nd}\left(H_{\rm W}\right) - F_{\rm nd}(z)\right)H_{g_{\rm nd}}\left(H_{\rm W}, z\right)$$
(22)

where  $H_{g_{st}}(H_W, z)$ ,  $H_{g_{br}}(H_W, z)$ , and  $H_{g_{nd}}(H_W, z)$  is height of the centre of gravity of stem, branches and needles in water flow between *z* and  $H_W$ , respectively. The turning moment at the tree base was M(0). Bending stress of the stem at height *z* in water flow,  $\sigma(z)$ , was calculated by Eq. 23, following Noguchi et al. (2012), as:

$$\sigma(z) = \frac{|M(z)|}{Z(z)} = \frac{32|M(z)|}{\pi D(z)^3}$$
(23)

where  $Z_z$  is the section modulus of stem at height z.

Critical tsunami water depth for tree damage was calculated by the balance between the tsunami load and the resistance of trees. The balance between M(0) and  $M_{C_{uproot}}$  was used for uprooting and that between  $\sigma(z)$  and MOR was used for tree breakage. In the calculations, variations for both  $M_{C_{uproot}}$  and MOR were applied. A range of  $\pm 30\%$  of  $M_{C_{uproot}}$  was used to account for the variation of root-soil anchorage related to soil conditions. 5th and 95th percentile values of MOR values from the bending tests were applied for stem bending strength to consider the variation of wood properties.

## Statistical analysis

All statistical analyses were calculated using the R software package, version 3.3.1 (R Core Team 2016). A one-way analysis of variance (ANOVA) was used to test the differences between two groups. The significance of correlations among variables was examined by the Spearman rank method. The performance of regression models was evaluated by  $R^2$  calculated as follows:

$$R^{2} = \frac{\left[\operatorname{cov}(\hat{y}_{i}, y_{i})\right]^{2}}{\operatorname{var}(\hat{y}_{i})\operatorname{var}(y_{i})}$$
(24)

where  $\hat{y}_i$  and  $y_i$  are the predicted and observed values, respectively.

## **Results and discussion**

## Resistance to uprooting

In the tree-pulling test, one tree (tree #1) experienced stem breakage at a height of 0.5 m, while the other five trees were uprooted (Table 1). Thus, tree #1 was

eliminated from the analysis on uprooting resistance. A combination of the present experimental results and those of previous studies (Table 2) shows that  $M_{C_{uproot}}$  increases with  $D_{BH}$  and  $H_{tr} \times D_{BH}^2$  (Fig. 5). The following relationships were found between  $M_{C_{uproot}}$  and  $D_{BH}$  and  $H_{tr}$ :

$$M_{C_{\rm uproot}} = 2.22 \times 10^6 D_{\rm BH}^{2.63} \quad \left(R^2 = 0.949\right) \tag{25}$$

$$M_{C_{\rm uproot}} = 8.09 \times 10^4 H_{\rm tr} D_{\rm BH}^2 \quad (R^2 = 0.964)$$
(26)

The 95% prediction interval of  $M_{C_{uproot}}$  had a range of ± 11 242 N m as calculated from Eq. 26 (Fig. 5b).

## Wood properties and resistance to stem breakage

Table 3 summarizes the bending properties of the stem logs and coarse root sections. The coarse root sections were relatively more rigid than the stem logs. The stem logs had significantly lower dry wood density (p < 0.001), larger average annual ring widths (p < 0.001), higher moisture content (p < 0.001) and lower MOR values (p = 0.001) than the coarse root sections, whereas no significant differences were found for  $D_{\rm m}$ , taper, cambial age, fresh wood density and the MOE between the stem logs and coarse root sections.

For stem logs, medians [5th and 95th percentile values] of MOE and MOR were 5.41 [3.78, 6.82] GPa and 35.0 [28.7, 41.8] MPa, respectively. The MOR in the study was similar to previous studies (Imai et al. 2013; Noguchi et al. 2014).

Table 4 summarizes the correlation coefficients among wood properties. Both stem logs and coarse root sections had significant positive correlations between cambial age and  $D_{\rm m}$  (p < 0.001). Older stem logs and coarse root sections were thicker objects. MOE and MOR were significantly positively correlated for the coarse root sections (p=0.028) but not for the stem logs. With regard to the stem logs, MOE



**Fig. 5** Critical turning moment for uprooting  $(M_{C_{uprovel}})$  of Japanese black pine on coastal sand dunes related to diameter at breast height  $(D_{BH})$  and tree height  $(H_{tr})$  in this study (*circle*) and previous studies (*cross*). Solid line indicates regression expression in Eqs. 25 and 26, and *dashed line* indicates 95% prediction interval generated by a combination of this study and previous studies

was significantly correlated with cambial age (p=0.028),  $D_{\rm m}$  (p=0.0049), and moisture content (p=0.032) and MOR were significantly correlated with moisture content (p=0.027). In principle, the MOE and MOR correlate with wood moisture content between 8% and fibre saturation (about 30%). After this point, the correlations with moisture content may be spurious. Consequently, thicker and older stem logs were more rigid. In contrast, the coarse root sections have no significant correlations with wood properties.

Because Japanese black pine trees grow under difficult environmental conditions, their crown forms are often asymmetrical. Since it is assumed the stem logs were tapered cylinders (for purposes of computation), it is possible that this has led to the insignificant correlations between MOE and MOR for stem logs. Further, branch knots on the stem would influence MOR estimates and reduce MOR (Ruel et al. 2010; Gardiner et al. 2016). The knot factor (fknot) (Gardiner et al. 2000) should be considered to obtain better MOR estimates of the stem logs.

#### Critical tsunami water depth

The numerical simulations revealed that the critical tsunami water depth varied with tree shape (Fig. 6). The critical tsunami water depth was greater for taller trees.

	Cambial age	$D_{\rm m}$	τ	ARW	$ ho_{W_{fresh}}$	$\rho_{\rm W\_dry}$	MC	MOE
Stem								
$D_{\rm m}$	0.940***							
τ	0.541*	0.450 <sup>ns</sup>						
ARW	-0.483 <sup>ns</sup>	-0.261 <sup>ns</sup>	-0.386 <sup>ns</sup>					
$\rho_{\rm W~fresh}$	$-0.270^{ns}$	-0.196 <sup>ns</sup>	$-0.225^{ns}$	0.146 <sup>ns</sup>				
$\rho_{\rm W \ dry}$	$-0.107^{ns}$	-0.111 <sup>ns</sup>	0.011 <sup>ns</sup>	0.043 <sup>ns</sup>	0.861***			
MC	-0.281 <sup>ns</sup>	-0.171 <sup>ns</sup>	-0.186 <sup>ns</sup>	0.386 <sup>ns</sup>	0.032 <sup>ns</sup>	-0.389 <sup>ns</sup>		
MOE	0.738**	0.700**	0.454 <sup>ns</sup>	-0.125 <sup>ns</sup>	-0.361 <sup>ns</sup>	-0.036 <sup>ns</sup>	-0.561*	
MOR	$-0.050^{ns}$	$-0.064^{ns}$	0.361 <sup>ns</sup>	0.004 <sup>ns</sup>	-0.139 <sup>ns</sup>	0.132 <sup>ns</sup>	-0.575*	0.450 <sup>ns</sup>
Root								
D <sub>m</sub>	0.905***							
τ	$-0.452^{ns}$	-0.119 <sup>ns</sup>						
ARW	0.190 <sup>ns</sup>	0.429 <sup>ns</sup>	0.310 <sup>ns</sup>					
$\rho_{\rm W~fresh}$	0.119 <sup>ns</sup>	0.214 <sup>ns</sup>	-0.190 <sup>ns</sup>	0.595 <sup>ns</sup>				
$\rho_{\rm W \ dry}$	-0.333 <sup>ns</sup>	-0.214 <sup>ns</sup>	0.190 <sup>ns</sup>	0.643 <sup>ns</sup>	0.595 <sup>ns</sup>			
MC	0.476 <sup>ns</sup>	0.524 <sup>ns</sup>	$-0.333^{ns}$	0.381 <sup>ns</sup>	0.762*	$-0.024^{ns}$		
MOE	-0.143 <sup>ns</sup>	$-0.071^{ns}$	0.190 <sup>ns</sup>	-0.119 <sup>ns</sup>	-0.214 <sup>ns</sup>	-0.214 <sup>ns</sup>	0.048 <sup>ns</sup>	
MOR	$-0.286^{ns}$	$-0.095^{ns}$	0.429 <sup>ns</sup>	$-0.095^{ns}$	-0.238 <sup>ns</sup>	0.048 <sup>ns</sup>	$-0.262^{ns}$	0.786*

Table 4 Correlation coefficients among wood properties

 $D_{\rm m}$  mean diameter at the mid-span,  $\tau$ - taper, *ARW* average annual ring width,  $\rho_{\rm W\_fresh}$  fresh wood density,  $\rho_{\rm W\_dry}$  dry wood density, *MC* moisture content, *MOE* modulus of elasticity, *MOR* modulus of rupture \*p < 0.05; \*\*p < 0.01; \*\*\*p < 0.001, *ns* not significant at p < 0.05

Critical tsunami water depth decreased with a higher Froude number because of greater *u* for the same tsunami water depth. The trees with  $H_{tt}/D_{BH}=50$  generally had higher resistance to tree breakage than uprooting; however, the difference was slight (Fig. 6a, c).

On the other hand, the trees with  $H_{\rm tr}/D_{\rm BH} = 70$  exhibited a different relationship of resistance to tree breakage and uprooting (Fig. 6b, d). In general, the resistance to tree breakage was higher than uprooting when  $H_{\rm tr} < 6$  m, whereas the opposite was true when  $H_{\rm tr} > 8$  m. To clarify the difference, the modelled trees were subtracted with  $H_{\rm tr} = 4$  and 16 m (Fig. 7). The increase in  $H_{\rm tr}/D_{\rm BH}$  resulted in decreased resistance to uprooting and tree breakage, but the resistance to tree breakage decreased more. Accordingly, taller trees with higher  $H_{\rm tr}/D_{\rm BH}$  values were more vulnerable to tree breakage than uprooting.

Shuto (1987) summarized the maximum inundation depth in five cases of large tsunamis from 1896 to 1983 in coastal forests of Japan. The observed tsunami depth at 43 sites ranged from 0.5 to > 10 m. Critical tsunami water depth for the modelled trees of Japanese black pine was less than 6 m in this study, even for taller and



**Fig. 6** Critical tsunami water depth related to tree height ( $H_{tr}$ ) for uprooting (*bold line and light bar*) and stem breakage (*dashed line and dark bar*) for different  $H_{tr}/D_{BH}$  values and *Fr* (Froude number) of tsunamis. For uprooting, the range of the floating bar is calculated using the critical turning moment from Eq. 26 and a range of  $\pm 30\%$ , respectively. For stem breakage, the range of the floating bar is calculated by median and 5th and 95th percentile values of MOR, respectively



**Fig. 7** Critical tsunami water depth related to  $H_{tr}/D_{BH}$  and Fr for uprooting (*light bar*) and stem breakage (*dark bar*) for different tree heights ( $H_{tr}$ ) subtracted from Fig. 5

larger diameter trees (Fig. 6). Large tsunamis could destroy most of Japanese black pine trees; however, trees taller than 6 m can resist against tsunamis with water depth < 2 m. Thus, these trees can contribute to mitigating the force of tsunamis.

From the numerical simulation, the resistance to uprooting was, in general, lower than the resistance to stem breakage regardless of tree size (Fig. 6). This finding is substantiated by direct field observations from the huge tsunami caused by the Great East Japan Earthquake in 2011 where more Japanese black pine trees experienced uprooting than stem breakage in coastal areas (Sato et al. 2012). The risk of uprooting is usually higher than stem breakage for smaller trees because smaller trees have less sufficiently developed root systems and smaller root-soil plate anchorage. The current findings indicate that the increase in root-soil plate anchorage due to the increase in tree size was less consequential for Japanese black pine trees on coastal sand dunes. Even though Japanese black pine is a typically deep-rooted tree species (Karizumi 2010), high groundwater levels in some coastal substrates could disturb the deep extension of roots, thereby lowering root-soil plate anchorage (FFPRI 2015). For the present trees, the tree-pulling test had a higher  $M_{C_{uproot}}$  than that estimated by Eq. 25 (Fig. 5a) because they had relatively larger diameters and root clump depths (Table 1). Tree #1, which experienced stem breakage, had the largest root depth of 3.2 m (Table 1). Although it is not known how large the root clumps of Japanese black pine trees were in previous studies, deep extension of root clumps would increase  $M_{C_{unreal}}$  of Japanese black pine more than the estimation by Eqs. 25 and 26. Additionally, it is important to increase stem thickness.

# Conclusion

This is the first study to estimate the resistance of Japanese black pine trees on coastal sand dunes by employing both numerical simulation and physical measurements of the critical turning moment to uprooting and stem bending strength. The regression equation for the critical turning moment to uprooting, computed MOE and MOR values, and the numerical simulation method should be useful to those in the wood science community as well as coastal managers who need to know the mechanical strength of Japanese black pine to help evaluate their resistance against tsunamis. When tree height is same, lower  $H_{\rm tr}/D_{\rm BH}$  trees (i.e. thicker trees) have a greater critical tsunami water depth. Adequate forest thinning to increase  $D_{\rm BH}$  is important to increase the resistance of Japanese black pine trees to tree damage by tsunamis. Accordingly, those Japanese black pine forests along the coast with larger trees and with low  $H_{\rm tr}/D_{\rm BH}$  values and deep root clumps are the best able to buffer the adverse impacts of tsunamis and resist against tsunamiinduced tree damage. To increase the accuracy of the numerical simulation, additional studies are necessary to measure actual root-soil plate properties, consider soil conditions and to obtain better MOE and MOR values of the stem logs with the knot factor (fknot).

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