#### **RESEARCH**



# **Study of the hydrogen evolution properties of cluster Co. MoS (***n***=1–5) using density functional theory**

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#### **Abstract**

To investigate the hydrogen evolution ability of the cluster  $Co<sub>n</sub>MoS$  ( $n=1-5$ ), this paper based on density functional theory, using the B3LYP generalization and def2-TZVP basis set. In this paper, the cluster was structurally optimized and theoretically analyzed by the Gaussian09 package under multiple spin multiplexes. The optimized conformation of the cluster was mostly in stereo form; in the frst step of the hydrogen evolution reaction, the analysis of the cluster HOMO diagram and the water molecule LUMO diagram, the energy level diference, the d-band center, Gibbs free energy and adsorption energy showed that the electrons of confgurations 5-a and 4-a were more likely to jump from the HOMO orbital to the water molecule LUMO orbital, and 5-a and 4-a showed excellent activity, they finally formed the  $Co<sub>n</sub>MoS-H<sub>ads</sub>$  model; in the second step of the hydrogen evolution reaction, the Co atom were a potential active site, and analysis of energy level differences and bond level revealed that the configurations  $5a-H_{ads}$  and  $4a-H_{ads}$  showed good desorption capacity compared to the other confgurations, and their adsorbed H atoms were more readily shed to complete the reaction with more rapid hydrogen evolution; in summary, confgurations 5-a and 4-a were determined to be the favored confgurations of the cluster with excellent catalytic activity.

**Keywords** Cluster Co<sub>n</sub>MoS  $\cdot$  Density functional theory  $\cdot$  Energy level difference  $\cdot$  *d*-band center  $\cdot$  Bond level

## **1 Introduction**

In this world, the search for clean energy sources has become crucial for the sustainable development of society, among which hydrogen energy, as a relatively ideal clean energy source, has received a lot of attention from researchers [[1,](#page-9-0) [2](#page-9-1)]. At the same time, the type of catalyst adopted for efficient and green catalytic production has become a new issue. In recent years, transition metal-based materials have been preferred by researchers due to their abundant sources, low cost and excellent properties [\[3](#page-9-2)[–7\]](#page-9-3), and the Co-Mo-S system has shown good results as a catalyst for hydrogen evolution reactions in the applications. Li et al. [\[8](#page-9-4)] designed an open structure Co-Mo-S which showed high electron transfer efficiency

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and more active sites in the hydrogen evolution reaction, indicating that Co-Mo-S exhibited excellent hydrogen evolution ability. Zhou et al. [[9\]](#page-9-5) produced a synthesis of the Co-Mo-S system by a hydrothermal method and the study showed that the system has high catalytic hydrogen evolution activity and the excellent performance of the catalyst can be attributed to the electron pair interactions and larger surface area. Xu et al. [\[10](#page-9-6)] found that the Co-Mo-S material exhibited high catalytic hydrogen evolution activity and stability even after four cycles under light reaction, which indicated that this material has a promising development in the feld of green energy. Fan et al. [\[11](#page-9-7)] argued that the formation of the Co-Mo-S phase in the composite led to its high catalytic activity in the chemical reaction of hydrogen release. Wang et al. [\[12](#page-9-8)] had synthesized a three-dimensional mesh Co-Mo-S material, and they had evaluated the material using electrochemical techniques and found that the material exhibited excellent activity and stability for hydrogen evolution reactions due to its abundant catalytic active sites and fuent electron transport pathway. Lu et al. [[13\]](#page-9-9) constructed Co-Mo-S nanomaterials, which were tested to have excellent hydrogen evolution properties derived

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from the abundance of catalytic active sites, efficient electron transfer and  $MoS<sub>2</sub>$  edge distribution of the Co promoter. The Co-Mo-S nanomaterials produced by Li et al. [\[14](#page-9-10)] demonstrated high activity and persistence in hydrogen evolution experiments due to electronic interactions between Mo and  $\cos_2$ , abundant active reaction sites and good electrical conductivity, and the study provides a good direction for research in the feld of sustainable energy. Wang et al. [[15](#page-9-11)] found that the large  $\cos_2$  exchange current density combined with the high  $MoS<sub>2</sub>$  electrochemical bilayer capacitance combined to enhance the hydrogen evolution activity of Co-Mo-S catalysts. Experiments by Ren et al. [\[16\]](#page-9-12) showed that Co-Mo-S exhibited signifcant activity, excellent electrochemical durability and near 100% faraday efficiency when used as a hydrogen evolution electrode. Liu et al. [[17\]](#page-9-13) demonstrated that Co-Mo-S can rapidly transfer the trapped electrons to the active site, efectively improving the hydrogen evolution efficiency. Huazhong University of Science and Technology et al. [\[18](#page-9-14)] prepared CoMoS nanomaterials by a solvothermal technique, which exhibited good catalytic properties for hydrogen evolution in the alkaline electrolyte, and it was found that the electron transfer from Co to  $MoS<sub>2</sub>$  and the solvothermal treatment time had significant effects on the catalytic activity. The Co-Mo-S hydrogen evolution catalysts fabricated by China University of Petroleum [\[19\]](#page-9-15) using low-temperature sulfdation method have good performance and stability. Guo et al. [[20](#page-9-16)] prepared Co-Mo-S nanomaterials with high catalytic activity, low overpotential and good stability in the hydrogen evolution reaction.

The macroscopic experimental studies of Co-Mo-S as a catalyst for the hydrogen resolution reaction of water are abundant, but the microscopic theoretical research is lacking, resulting that it is difficult to fully understand the microscopic mechanism of Co-Mo-S catalysts in the hydrogen evolution reaction. Therefore, in order to gain insight into the micromechanics and properties of the Co-Mo-S system involved in hydrogen evolution reactions, the cluster  $Co<sub>n</sub>MoS$  (1–5) was designed based on the literature [[14\]](#page-9-10) as the object of research. In this paper, the hydrogen evolution properties of this cluster are investigated at the microscopic level based on density functional theory [[21](#page-9-17), [22\]](#page-9-18), with a view to explaining its excellent hydrogen evolution ability from a theoretical perspective and providing a theoretical basis for subsequent studies on the infuence of more Co atoms on hydrogen evolution activity.

# **2 Theoretical foundation**

#### **2.1 Calculation method**

This paper also used the B3LYP function because of its excellent integration performance and the fact that it is still the default function for many researchers in the transition

metal system. The subject of this paper was the Co-Mo-S system, which contains elements after the ffth period (Mo), and relativistic efects in theoretical calculations could afect the reliability of the results. The 3-zeta basis set def2-TZVP, which contains a pseudopotential and has a high accuracy, was selected for this paper. This basis set was calculated using the stuttgart small nucleus pseudopotential for the ffth period and beyond, and the all-electron basis set for the frst four periods, which was perfectly adequate for the system under study. Luo et al. [[23–](#page-9-19)[25\]](#page-9-20) used B3LYP/def2-TZVP to investigate the properties of transition metal systems, and their results also confrmed the accuracy and reliability of the density functional and basis set. Meanwhile, in this paper, the theoretical bond length of the Co-Mo-S system (Co-S: 0.227 nm, Mo-S: 0.240 nm, Co-Mo: 0.281 nm) was found to be similar to the experimental value  $[26]$  $[26]$  (Co-S: 0.221 nm, Mo-S: 0.241 nm, Co-Mo: 0.285 nm) after using this density functional and basis set, and the theoretical bond length of the Co-Mo system (Co-Mo: 0.248 nm) was also calculated to be in perfect agreement with the experimental value  $[27]$  $[27]$  $[27]$  (Co-Mo: 0.248 nm). For the initial configuration of a system with a small number of atoms, it is generally obtained by designing a large number of structures. For example, Juárez-Sánchez et al.  $[28, 29]$  $[28, 29]$  $[28, 29]$  $[28, 29]$  calculated  $(CuS)<sub>N</sub>$  $(N=1-6)$  and VF<sub>n</sub>  $(n=1-7)$  When the initial structure is obtained, the above method is adopted.

In this paper, we designed as abundant as possible clusters of  $Co<sub>n</sub>MoS$  ( $n=1-5$ ) with multiple initial configurations of diferent spin multiplicity and diferent morphologies at the B3LYP/def2-TZVP quantum chemistry level, based on density functional theory. This paper also adopted the Gaussian09 package and the Multiwfn package [\[30\]](#page-10-4) for full frequency validation and geometric confguration optimization and data machining. The optimized results were obtained by excluding unstable conformations that contained virtual frequencies and morphologically similar conformations, resulting in 21 optimized stable conformations. The optimization conditions for convergence to be satisfed are: maximum force  $< 0.00045$ , root mean square force  $< 0.00030$ , maximum displacement  $< 0.00180$  and root mean square displacement  $< 0.00120$ . All the above calculations and data machining were done on the computer HP-Z440.

#### **2.2 Mechanism of hydrogen evolution reaction**

The research in this paper was performed under neutral condition. In this experiment, the cluster  $Co<sub>n</sub>MoS$  $(n=1-5)$  (hereinafter indicated by M) was used as the theoretical object of the hydrogen evolution reaction, and the mechanism of this cluster when it occurs in catalytic hydrogen evolution is known according to the literature [[14\]](#page-9-10). The reaction was mainly divided into the following two steps, where  $H_{ads}$  represent the hydrogen atoms

adsorbed to the cluster. The interatomic force analysis of the M-H structure resulting from the Volmer reaction showed that the Chemical Bond interaction between the H atom and the attached metal atom is dominant. Therefore, the theoretical analysis could be mostly satisfied without considering the van der Waals correction.

*Step 1*

 $M + e^- + H_2O \rightarrow M - H_{ads} + OH^-$  (Volmer step)

*Step 2* There are two reaction pathways in this reaction step, as follows:

 $M - H_{ads} + e^- + H_2O \rightarrow M + H_2 + OH^-$ (Heyrovsky step)

 $2M - H_{ads} \rightarrow 2M + H_2$ (Tafel step)

## **3 Results and discussion**

#### **3.1 Stable configuration of cluster Co<sub>n</sub>MoS (***n* **= 1–5)**

The final 21 stable conformations of the cluster  $Co<sub>n</sub>MoS$  $(n=1-5)$  are obtained, and the geometrical conformational morphology and relative energies are shown in Fig. [1](#page-3-0). In Fig. [1,](#page-3-0) "*n*-a" show the most stable configurations of the cluster  $Co<sub>n</sub>MoS$  for  $n = 1-5$ , and the energy of the most stable configuration is set to 0 eV. The energy of "*n*-a" is used as a reference standard to calculate the relative energy of " $n - m$ " ( $m = b$ , c, d, e, f) and rank the cluster configurations according to the lowest to highest energy. The number in brackets at the top of the "*n* − *m*" configuration indicate the spin multiplicity.

Figure [1](#page-3-0) shows that all the configurations in cluster  $Co<sub>1</sub>MoS$  are planar triangles; cluster  $Co<sub>2</sub>MoS$  contains planar and triangular cone shapes; cluster  $Co<sub>3</sub>MoS$  has a tetragonal cone shape for configuration 3-a, five configurations from 3-b to 3-f are all triangular biconical, and configurations 3-b and 3-c, and configurations 3-d and 3-f have the same geometry, but have different spin multiplicity; the cluster  $Co<sub>4</sub>MoS$  contains five stable configurations, all of which are single-capped triangular bipyramidal, with mirror-symmetric configurations 4-d1 and 4-d2; the cluster  $Co<sub>5</sub>MoS$  contains six double-capped triangular bipyramidal configurations, of which configurations 5-c and 5-d are identical in terms of the relative positions of the atoms at different spin multiplets.

In this paper, the most and second most stable configurations of each size cluster are selected for theoretical analysis of the hydrogen evolution properties.

## **3.2 Thermodynamic stability of the cluster Co, MoS (***n***=1–5)**

The correction energy, Gibbs free energy, binding energy, and Gibbs free energy variation of the optimized confguration of the cluster  $Co<sub>n</sub>MoS$  are listed in Table [1](#page-4-0). The smaller the value of the correction energy and the Gibbs free energy variation, the higher the stability, while the reverse is achieved for the binding energy, the larger the value, the more stable the conformation, that is the tighter the bonding between the atoms. The binding energy  $(E_{BE})$  and Gibbs free energy variation  $(\Delta G)$  were calculated as follows.

$$
E_{\text{BE}} = nE_{\text{ZPE}}(\text{Co}) + E_{\text{ZPE}}(\text{Mo}) + E_{\text{ZPE}}(\text{S}) - E_{\text{ZPE}}(\text{Co}_{n}\text{MoS})
$$

 $\Delta G = G(\text{Co}_n\text{MoS}) - nG(\text{Co}) - G(\text{Mo}) - G(\text{S})$ 

From Table [1,](#page-4-0) the corrected and Gibbs free energies for configurations  $n-a$  ( $n=1-5$ ) to  $n-b$  increase gradually and the binding energy decreases for the same size cluster, indicating that configurations  $n$ -a are the most stable configurations in each size cluster.

# **4 4 Analysis of the hydrogen evolution properties of the cluster ConMoS(***n***=1–5)**

## **4.1 Study of hydrogen atom adsorption properties of clusters**

## 4.1.1 Analysis of cluster Co<sub>n</sub>MoS HOMO diagrams **and LUMO diagrams of water molecules**

From frontline orbital theory it can be seen that the highest energy occupied orbital HOMO and the lowest energy unoccupied orbital LUMO determine the state of a chemical reaction. When the cluster  $Co<sub>n</sub>MoS$  reacts with a water molecule, microscopically it is the electrons that leap from the HOMO orbital of the cluster to the LUMO orbital of the water molecule, forming the  $M-H<sub>ads</sub>$  structural model and thus the frst step in the hydrogen evolution reaction. Figure [2](#page-5-0) shows the HOMO orbital diagrams for the alpha and beta electrons of the cluster ConMoS optimized confguration and the LUMO orbital diagram for the water molecule. Conformation 2-b is a single multiplet state and has only one class of HOMO diagrams due to its closed shell. The graph shows the positive phase of the orbital wave function in lighter shades and the negative phase of the orbital wave function in darker shades, with the area covered by the two representing the region where the cluster is active during hydrogen evolution reactions. The HOMO orbital of the cluster is phased with the LUMO  $(n=1-5)$ 

<span id="page-3-0"></span>**Fig. 1** Optimized stable configuration of cluster Co<sub>n</sub>MoS



orbital of the water molecule, which makes it easier for the electrons to complete the leap and for the hydrogen evolution reaction to proceed. It is easy to see from Fig. [2](#page-5-0) that the LUMO orbital of the water molecule is surrounded by dark shades, indicating that the water molecule is more likely to react with the negative phase of the cluster. The negative phase morphology of the cluster of optimized  $Co<sub>n</sub>MoS$  conformations varies in size, indicating that each conformation has a diferent degree of activity. The dark coverage of the  $\alpha$ -HOMO diagrams for configurations 1-a, 1-b, 4-b and 5-a is larger than that of the respective *β*-HOMO diagrams from Fig. [2](#page-5-0), indicating that *α*-HOMO plays a major role in the reaction of the above confgurations with water molecules; confguration 2-a, 3-a, 3-b, 4-a and 5-b are the opposite, with more dark parts of the *β*-HOMO diagram than the *α*-HOMO diagram, meaning that when these confgurations interact with water molecules, electrons tend to fow more from the *β*-HOMO to the LUMO of the water molecule. Overall, the *α*-HOMO of confgurations 4-b and 5-a and the *β*-HOMO of confgurations 3-b, 4-a and 5-b are more active in the hydrogen evolution reaction with water molecules.

<span id="page-4-0"></span>**Table 1** The energy parameters of the stable confguration of the cluster Co<sub>n</sub>MoS (Unit: eV)

Configuration	$E_{\rm ZPE}$	G	$E_{\rm BE}$	$\Delta G$
$1-a$	0.000	0.000	0.000	0.000
$1-h$	0.564	0.547	$-0.564$	0.547
$2-a$	0.000	0.000	0.000	0.000
$2-h$	2.051	2.097	$-2.051$	2.097
$3-a$	0.000	0.000	0.000	0.000
$3-b$	0.010	0.057	$-0.010$	0.057
$4-a$	0.000	0.000	0.000	0.000
$4-b$	0.609	0.649	$-0.609$	0.649
$5-a$	0.000	0.000	0.000	0.000
$5-b$	0.325	0.321	$-0.325$	0.321

#### **4.1.2 Orbital energy level diferences between the cluster ConMoS and water molecules**

The energy level diference can be used to further determine the activity of the hydrogen evolution reaction between molecules. According to the frontier orbital theory, the smaller the energy level diference between the reactants and the energy level diference between the HOMO orbital of the reactant and the LUMO orbital of the water molecule is less than 6.004 eV (about 579 kJ/mol) [\[31](#page-10-5)], the easier the reaction will be. The results of the energy level diference calculations for the optimized conformations of the cluster  $Co<sub>n</sub>MoS$  are shown in Fig. [3](#page-6-0). As is seen from Fig. [3,](#page-6-0) the energy level diferences of the optimized conformations of the cluster  $Co<sub>n</sub>MoS$  are all less than 6.004 eV, indicating that the reaction between each conformation and the water molecule is possible. The energy level diference of confguration 5-a (4.932 eV) is the smallest of all the optimized confgurations, indicating that confguration 5-a is more likely to react with water molecules and adsorb hydrogen atoms than other confgurations, completing the electron transfer more quickly and leading to the frst step of the hydrogen evolution reaction. The energy level diference gives the following reaction activity for each optimized configuration:  $5-a > 3-b$  $>2-b>4-b>4-a>5-b>3-a>1-b>1-a>2-a$ .

#### 4.1.3 Cluster Co<sub>n</sub>MoS d-band center

The d-band center model enables the description and prediction of the extent of the activity capacity of a material surface. The d-band center is defned essentially as the difference between the central position of the fractional density of states corresponding to the d-state of the material surface and the Fermi energy level. The theory bases on the fact that the d-band of a substance mixes with the orbitals of small molecule reactants when adsorption occurs on the surface of the substance with other small molecule reactants, when the bonding and anti-bonding states appear. The higher the d-band energy of a substance relative to the Fermi energy level, the higher the energy of the antibonding state relative to the Fermi energy level, which means that it will be less occupied, and thus the bonding capacity will be weakened, and the stronger the bonding between the substance and the small molecule reactant will be when it adsorbs. The d-band center energy values of the cluster  $Co<sub>n</sub>MoS$  are calculated by the wave function software Multiwfn and plotted in Fig. [4.](#page-6-1) In general, the lower the d-band center value of the cluster, the stronger its ability to adsorb hydrogen atoms. The lowest d-band center value (17.465 eV) for confguration 5-a, indicating that confguration 5-a contains the most superior ability to bind hydrogen atoms compared to the others, which is consistently with the conclusions obtained from the analysis of energy level diferences. The relationship between the activity intensity of the clusters when adsorbed with hydrogen atoms is introduced by the d-band center:  $5-a > 5-b > 4$  $a > 3-a > 4-b > 2-a > 3-b > 2-b > 1-b > 1-a$ .

#### **4.1.4 Cluster Gibbs free energy and adsorption energy**

To further evaluate the catalytic activity of the adsorbed hydrogen in the Volmer reaction for each confguration, we introduced the Gibbs free energy and the adsorption energy. The Gibbs free energy and adsorption energy of hydrogen adsorbed in conformation 1-b were not discussed because the M-H structure resulting from conformation 1-b does not exist stably. The energy calculation equations were as follows.

$$
\Delta G_{H*} = G(\text{Co}_n \text{MoS} - \text{H}) - G(\text{Co}_n \text{MoS}) - \frac{1}{2}G(\text{H}_2)
$$
  

$$
\Delta E_{ad} = E(\text{Co}_n \text{MoS} - \text{H}) - E(\text{Co}_n \text{MoS}) - \frac{1}{2}E(\text{H}_2)
$$

 $\Delta G_{\text{H*}}$  represented the Gibbs free energy change of the adsorbed hydrogen and *E*ad represented the adsorption energy. The nearer the Gibbs free energy  $(|\Delta G_{\text{H*}}|)$  was to 0 eV, the better the catalytic activity of the catalyst [\[32](#page-10-6)[–34](#page-10-7)].

It is easily seen from Fig. [5](#page-7-0)a that the Gibbs free energy of confguration 1a was closest to 0, indicating that it had a high catalytic capacity compared to the other confgurations. The catalytic ability of confguration 2b was weaker than that of the other confgurations. The relationship based on the Gibbs free energy gave the ability to catalyze activity as follows: 1-a>3-b>2-a>3-a>5-a>5-b>4-a>4-b>2-b.

The change of the adsorption energy of the cluster after the adsorption of hydrogen could be seen in Fig. [5b](#page-7-0), where too large and too small values of the adsorption energy are not beneficial for the efficient conduct of the reaction. With too large a value, the H atoms were strongly combined with

<span id="page-5-0"></span>**Fig. 2** HOMO diagram of the optimized confguration of cluster Co<sub>n</sub>MoS and LUMO diagram of water molecule



the clusters and it was more difficult for the H atoms to shed the clusters after the catalytic reaction occurred. The value was too small and again it was difficult to have an active efect. For this cluster, confgurations 2-a, 3-a, 4-a, 4-b, 5-a, 5-b were more active than the other confgurations.

In the first step, the water molecules first adsorbed onto the clusters, after which the clusters combined with H to form the M-H structure and OH− detachment occurred. The combined HOMO diagram, energy level difference, d-band center, Gibbs free energy and adsorption energy



<span id="page-6-0"></span>**Fig. 3** Frontier orbital energy levels for the reaction of clustered Co  $n$ MoS with H<sub>2</sub>O



<span id="page-6-1"></span>Fig. 4 d-band center of cluster Co<sub>n</sub>MoS optimized configuration

analysis of the cluster  $Co<sub>n</sub>MoS$  optimized configuration indicate that the cluster had varying degrees of activity in each optimized configuration in the first step of the hydrogen evolution reaction. Conformation 5-a has better hydrogen evolution activity than the other conformations, meaning that electrons can jump from the HOMO orbital to the LUMO orbital of the water molecule more rapidly. The results of the above analysis are ranked, and the final conclusion was that the strength of the activity of each configuration in the first step of the hydrogen evolution reaction was:  $5-a > 3-b > 5-b > 3-a \approx 4-a > 4-b > 2-a > 1-a$  $\approx$ 2-b > 1-b.

# 4.2 Research of cluster (Co<sub>n</sub>MoS)-H<sub>ads</sub> desorption **process**

This paper mainly discussed the Heyrovsky step, the Tafel step will be analyzed during the planned further research. After the reaction of the cluster  $Co<sub>n</sub>MoS$  with water to complete the frst step of the hydrogen evolution process, the  $(Co_nMoS)$ -H<sub>ads</sub> (M-H<sub>ads</sub>) model is formed and the results are shown in Fig. [6.](#page-7-1) In particular, the  $M-H<sub>ads</sub>$  conformation of conformation 1-b cannot be steadily present after verifcation by the Gaussian09 package. It is easy to see from the fgure that the H atoms are all bound to the Co atoms, indicating that the Co atoms are potential catalytically active sites for this cluster.

### 4.2.1 Cluster (Co<sub>n</sub>MoS)-H<sub>ads</sub> and H<sub>2</sub>O frontline orbital **energy level diferences**

To obtain more accurate information on the catalytic activity of M-Hads in the second step of the hydrogen evolution reaction (desorption reaction), the energy level diference is introduced for determination, and the details are shown in Fig. [7](#page-8-0). The energy level difference of each  $M-H<sub>ads</sub>$  confguration of this cluster is less than 6.004 eV, and it can be concluded that each  $M-H<sub>ads</sub>$  structure is capable of reacting with water molecules. In particular,  $5a-H<sub>ads</sub>$  has the smallest energy diference (5.339 eV) in the M-Hads structure, indicating that  $5a-H_{ads}$  is the most readily available for desorption reactions in which hydrogen atoms can be desorbed, which means that it is the most active. The relationship between the activity capacity of the  $M-H<sub>ads</sub>$  model for the second hydrogen evolution reaction, judging from the energy level difference, is:  $5a-H_{ads} > 4a-H_{ads} > 3b-H_{ads} > 3a-H_{ads} >$  $5b-H<sub>ads</sub> > 4b-H<sub>ads</sub> > 2b-H<sub>ads</sub> > 2a-H<sub>ads</sub> > 1a-H<sub>ads</sub>.$ 

# 4.2.2 Cluster (Co<sub>n</sub>MoS)-H<sub>ads</sub> bond level

Figure [8](#page-8-1) shows the bond level information for each of the  $M-H<sub>ads</sub>$  models. In this section the bond level between the Co atoms adsorbing H atoms and the H atoms are introduced to further determine the difficulty of the desorption reaction for each M- $H_{ads}$  model. The larger the bond level, the stronger the bond between the two atoms and the less likely to break; the smaller the bond level, the weaker the bond, resulting in the H atom falling off easily and the reaction being completed with the hydrogen evolution. The fgure shows that  $2a-H<sub>ads</sub>$  have the smallest bond level, which means that the adsorbed H atoms are easily shed and hydrogen precipitates more quickly.  $1a-H_{ads}$  has the largest bond level of all the M-Hads models, indicating that Co–H bonds are the most difficult to break and proceed more slowly than the rest of the confgurations in the hydrogen evolution reaction. Based on bond levels, the  $M-H<sub>ads</sub>$  model for easy completion of



<span id="page-7-0"></span>Fig. 5 Energy variation of adsorbed hydrogen in the optimized configuration of the cluster ConMoS

<span id="page-7-1"></span>

hydrogen evolution reactions is ranked as follows: 2a-H<sub>ads</sub>  $>4a-H<sub>ads</sub>$  $>2b-H<sub>ads</sub>$  $>4b-H<sub>ads</sub>$  $>5a-H<sub>ads</sub>$  $>5b-H<sub>ads</sub>$  $>3a-H<sub>ads</sub>$  $>$ 3b-H<sub>ads</sub> $>$ 1a-H<sub>ads</sub>.

For the second step of the hydrogen evolution reaction, the analysis of the M-H<sub>ads</sub> model energy level difference and bonding level ranking judgment,  $M-H<sub>ads</sub>$  model



<span id="page-8-0"></span>**Fig. 7** The frontier orbital energy level diference of the reaction between M- $H_{ads}$  and  $H_2O$ 



<span id="page-8-1"></span>**Fig. 8** Bond level of M-H<sub>ads</sub> optimized configurations

and water molecule reactivity relationship is:  $4a-H_{ads} > 5a$  $-H_{ads} > 2a-H_{ads} > 2b-H_{ads} \approx 4b-H_{ads} > 3a-H_{ads} \approx 3b-H_{ads} \approx$  $5b-H_{ads} > 1a-H_{ads}$ .

In the frst step of the reaction, both the energy level difference and the d-band center analysis showed that confguration 5-a exhibited the best hydrogen evolution activity. The conclusions from the analysis of the HOMO diagram and the adsorption energy also indicated that confguration 5-a also has a better activity. In the second step of the hydrogen evolution reaction, the conformation  $5a-H<sub>ads</sub>$  contained the best activity capacity in the energy level diference analysis. In both the energy level diference and bond level analyses, the conformation 4a-Hads had the second best activity capacity. Considering the activity of each confguration in the twostep hydrogen evolution reaction, confgurations 4-a and 5-a showed an excellent ability to complete the electron transfer and precipitate hydrogen more quickly in both steps.

## **5 Conclusion**

In this paper, the hydrogen evolution properties of the most and least stable conformations of the cluster  $Co<sub>n</sub>MoS(1–5)$ were analyzed at the theoretical level based on density functional theory with the support of Gaussian09 and Multiwfn software.

- (1) Cluster  $Co<sub>n</sub>MoS$  (1–5) contained 21 stable configurations, mostly in stereospecifc form.
- (2) hydrogen evolution reaction in the frst step

This step involved the leap of electrons from the HOMO orbital of the cluster to the LUMO orbital of the water molecule, with the  $\alpha$ -HOMO of configurations 1-a, 1-b, 4-b and 5-a being more efficient to interact with the water molecule and the  $\beta$ -HOMO of configurations 2-a, 3-a, 3-b, 4-a and 5-b being more active in the reaction. All configurations had an energy level diference of less than 6.004 eV, meaning that all were able to interact electronically with water normally, with configuration 5-a being the most active. Analysis of the d-band center revealed that confguration 5-a had the lowest value and its ability to adsorb hydrogen atoms was the strongest. Analysis of Gibbs free energy and adsorption energy resulted the activity of confgurations 5-a and 4-a can't be neglected. Overall, the conformations 5-a and 4-a showed superior activity in the frst step of the reaction compared to the other conformations.

#### (3) hydrogen evolution reaction in the second step

After the reaction in the previous step, the  $M-H<sub>ads</sub>$  model was formed and the Co atom was found to be a potential active site for the cluster by calculation. From an energy level difference perspective, the M- $H_{ads}$  model still allowed the reaction to proceed smoothly and the conformation  $5a-H<sub>ads</sub>$  had the smallest energy level difference and the highest activity capacity. The bond level analysis revealed that the conformation  $2a-H_{ads}$  had the smallest bond level and the H atom was easily shed. Overall, the confgurations  $4a-H<sub>ads</sub>$  and  $5a-H<sub>ads</sub>$  showed good desorption in the second step of the reaction.

The combined analysis of the two steps showed that confgurations 5-a and 4-a are the key confgurations of the cluster involved in catalytic hydrogen evolution reactions. This conclusion will provide theoretical guidance for the macroscopic experimental study of the clusters as catalytic materials. Based on the present results, it was reasonable to suppose that when Co-M-S contains more Co atoms, its

hydrogen precipitation activity may subsequently become excellent. Further research will be required to obtain the exact circumstances.

**Author contributions** Z-Y W contributed to writing, data management, methodology. Z-G F contributed to conceptualization, project Management. J W contributed to article proofreading. Z-L M contributed to verifcation, methodology. Q-Q H contributed to article proofreading, software. T-H W contributed to article proofreading, data management. X-X Z and J S contributed to proofreading the article.

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**Data availability** If necessary, the data of this study can be provided to the corresponding author within a reasonable range.

**Code availability** This article does not apply the term.

#### **Declarations**

**Conflicts of interest** The authors declare that they have no confict of interest.

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