#### **REGULAR ARTICLE**



# **Quantum chemical investigation of the ground‑ and excited‑state acidities of a dihydroxyfuranofavylium cation**

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#### **Abstract**

The two hydroxyl groups of the 4′,7-dihydroxyfurano-3,2′-favylium cation (**1**), a synthetic analog of the aurone pigments of plants, have been shown to have different relative acidities in the ground state  $(S_0)$  and the lowest excited singlet state  $(S_1)$ . In the ground state, the 4′-OH group is slightly more acidic, while in the excited state, the molecule is strongly photoacidic and deprotonation occurs preferentially from the 7-OH group. In order to compare the relative acidities of these two OH groups via quantum chemical methodology, a common reference state was employed in which an explicit water molecule was hydrogen-bonded to each of the OH groups of 1. The relative acidities of the two OH groups were then inferred from the diferential change in energy along the coordinate for proton transfer to the explicit water molecule via time-dependent density functional calculations (B3-LYP with Grimme's D3 dispersion correction; TZVP basis set; and PCM to simulate an aqueous environment). The calculated acidity changes confrm the experimentally observed inversion in the relative acidities between  $S_0$  and  $S_1$ . The enhanced photoacidity of  $S_1$  was also mirrored in the natural transition orbitals and the decrease in the negative change on the oxygen atoms of the OH groups. Employing a common reference state with an explicit water as the proton acceptor should thus serve as a convenient strategy for exploring the relative ground- and excited-state acidities of the OH groups of natural or synthetic dyes, especially when the values are not readily accessible through experiment.

**Keywords** Anthocyanins · Flavylium cation · DFT · Excited-state proton transfer

## **1 Introduction**

Anthocyanins are the primary natural pigments responsible for most of the red, blue and purple colors of fowers, fruits and leaves  $[1-3]$  $[1-3]$ . Anthocyanin and many of their synthetic favylium cation analogs have a complex pH-dependent chemistry  $[1-8]$  $[1-8]$  $[1-8]$ . Thus, at strongly acidic pH, the exclusive

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form is the visibly colored favylium cation form. At pH values above ca. pH 3, attack of water on the favylium cation can result in formation of the near colorless hemiketal form that can then undergo ring-opening tautomerism to the corresponding near colorless chalcones. In hydroxyfavylium cations, deprotonation to form the neutral conjugate base form of the favylium cation contributes an additional equilibrium to the multiequilibrium system. In the lowest excited singlet state, natural anthocyanins and synthetic hydroxyfavylium and pyranofavylium cations are strong photoacids, undergoing ultrafast adiabatic excited-state proton transfer (ESPT) to water on a picosecond time scale [[8–](#page-4-2)[10\]](#page-4-3).

Among the molecular ancestors of anthocyanins, the aurones, which are responsible for the yellow color of some flowers, possess an additional furan ring in their molecular structure (Scheme [1](#page-1-0)). Recently, synthetic furanofavylium analogs of aurones have been shown to exhibit similar multistate equilibria to those of anthocyanins and synthetic favylium cations [[11,](#page-4-4) [12\]](#page-4-5). Particularly interesting are the acid–base properties of the ground and lowest excited singlet states of the 4′,7-dihydroxyfurano-3,2′-favylium cation (**1**)

<span id="page-1-0"></span>

in aqueous solution. Thus, unlike the analogous 4′,7-dihydroxyfavylium cation (**2**), in which the 7-hydroxy group is ca. 1 pK unit more acidic than the 4′-OH group in the ground state, compound **1** was found to deprotonate preferentially at the 4′-OH group in the ground state (Scheme [1\)](#page-1-0). In contrast, in the lowest excited singlet state, the ESPT to water occurred preferentially from the 7-OH group [\[11](#page-4-4)].

Given the complexity of much of the chemistry of these natural plant pigments and their synthetic analogs, there is a growing interest in the development of computational quantum chemical methodological approaches for the rationalization and prediction of the ground and excited state properties of dyes or pigments related to anthocyanins, pyranoanthocyanins and their synthetic analogs [[13–](#page-4-6)[19\]](#page-4-7). Knowledge of this type is particularly important for tailoring or adapting the structure in order to optimize the color, stability and properties for a given potential application. In the present work, we report a straightforward and expeditious quantum chemical approach for comparing the relative acidities of OH groups of pigments of this type in both the ground and singlet excited state. The approach is tested by calculations on compound **1** that verify both the strongly enhanced acidity of the excited state and the experimentally observed [[12\]](#page-4-5) inversion in the ground- and excited-state acidities of the 4′-OH and 7-OH groups of the furanofavylium cation **1**.

## **2 Computational details**

Density functional theory (DFT) was used for the characterization of stationary points and potential energy curve pathways of the proton detachment from the hydroxyl groups of the compounds in both the ground  $(S_0)$  and first excited singlet  $(S_1)$  states. For the DFT calculations, the widely

used the hybrid exchange-correlation functional B3-LYP [[20](#page-4-8)] was employed with the D3 dispersion correction of Grimme [\[21](#page-4-9)]. The basis set TZVP [\[22](#page-4-10), [23\]](#page-4-11) was used in all calculations. The Gaussian09 [[24](#page-4-12)] program suite was used to perform the calculations. The non-specifc efects of the polar solvent environment were simulated using the polarizable continuum model (PCM) [[25,](#page-5-0) [26](#page-5-1)] implemented using the self-consistent reaction feld (SCRF) [[25](#page-5-0), [27](#page-5-2)] approach in Gaussian09. The wave function analysis program Theo-DORE [\[28,](#page-5-3) [29](#page-5-4)] was used for the natural transition orbital (NTO) [\[30](#page-5-5)] analysis.

Initially, the ground-state structures of the isolated systems were fully optimized by means of the B3-LYP/TZVP approach. The frst singlet excited state of the furanofavylium was optimized using TD-DFT with the same functional taking the corresponding optimized geometry of  $S_0$  as the starting point for the  $S_1$  calculations. The potential curves for proton transfer to a single water molecule were computed in the polar environment by stepwise elongation of the O–H bond of the hydroxyl group of interest in 0.1 Å increments using the same method employed for the calculation of the stationary points. All structures were reoptimized using water as a polar environment with the dielectric constant of 78.39. The theoretical absorption spectrum was calculated from the vertical excitation energies  $(E_i)$  for the first 10 excited states and the corresponding oscillator strengths  $(f<sub>i</sub>)$  employing, as in previous work  $[18, 19]$  $[18, 19]$  $[18, 19]$ , as a sum of superimposed Gaussian functions centered on each  $E_i$  [[31](#page-5-6)]:

$$
\varepsilon(\bar{v}) = 26954 \sum_{i} \left( \frac{f_i}{\Delta_{1/2}} \right) \exp\left[ -2.733 \left( \frac{E - E_i}{\Delta_{1/2}} \right)^2 \right] \quad (1)
$$

where  $\Delta_{1/2}$  is the spectral bandwidth (full width at half maximum) in eV, assumed to be 0.36 eV, and  $\varepsilon(\bar{v})$  is the molar absorption coefficient in units of  $M^{-1}$  cm<sup>-1</sup>. The published absorption spectrum [[12](#page-4-5)] was digitized with the online application WebPlot Digitizer [\[32](#page-5-7)].

# **3 Results and discussion**

The starting point for our calculations on the furanofavylium cation **1** was the adoption of a common reference state for the two OH groups of the molecule. This reference state was constructed by hydrogen bonding each of the two OH groups to an explicit water of hydration, followed by minimization of the geometry in a continuum aqueous-like medium (Fig. [1](#page-2-0)). In addition to creating a common initial reference state against which to compare the acidity of the two OH groups, the specifc water molecules served as discreet proton acceptors, found to be necessary in prior computational studies to reproduce experimental acidity trends. Employing a single discrete water molecule as the proton acceptor rather than a larger water cluster proved, in preliminary calculations, to be a necessary expedient due to complications in maintaining entirely equivalent water clusters hydrogenbonded to the two OH groups during geometry optimization.

The B3-LYP/TZVP energies for the 10 lowest excited singlet states of the furanoflavylium cation **1** with the two discrete water molecules in a PCM aqueous environment (Table [1](#page-2-1)) were employed to construct the theoretical absorption spectrum. As shown in Fig. [2](#page-2-2), the theoretical spectrum based on overlapping Gaussians with a bandwidth of 0.36 eV agrees satisfactorily with the experimental spectrum reported in water at  $pH$  1 [[12](#page-4-5)] over virtually the entire UV–visible spectrum. The hole (occupied) and particle (virtual) components of the natural transition orbitals (NTOs) [\[30](#page-5-5)] associated with the transition to the first excited singlet state  $(S_1)$ , depicted in Fig. [3,](#page-3-0) are dominated by the HOMO and LUMO, respectively, as is generally the case for favylium cations.

By employing a common reference state for the two OH groups, the relative acidities of the two OH groups of the molecule can be rather straightforwardly inferred by



<span id="page-2-1"></span>**Table 1** B3-LYP/TZVP/PCM vertical excitation energies and the corresponding oscillator strengths for the 10 lowest excited singlet states of the furanofavylium cation **1** with the two discrete water molecules in a PCM aqueous environment

<b>State</b>	$\Delta E$ (eV)	Oscillator strength
$S_1$	2.824	0.8551
$S_2$	3.336	0.1752
$S_3$	3.588	0.0099
$\mathbf{S}_4$	4.071	0.0143
$S_5$	4.768	0.1228
$\mathbf{S}_6$	4.880	0.0071
$S_7$	5.181	0.0026
$\mathbf{S}_8$	5.349	0.4548
$S_9$	5.410	0.1493
$S_{10}$	5.533	0.0001

comparing the relative change in the energy of the molecule upon increasing the O–H distance of either the hydrated 4′-OH group or the hydrated 7-OH group, derived from TD-DFT calculations on the system. Figure [4](#page-3-1) shows the difference between the two OH groups, as the relative change in energy in dimensionless units  $(=\Delta E(\text{in eV})/0.059 \text{ V})$ , in the ground state and in the lowest excited state of compound **1** when only the 4'-OH bond or only the 7-OH bond was selectively stretched. All structures were reoptimized for each fxed O–H distance, using water as a polar environment. In the ground state, this diference should asymptotically approach  $\Delta pK_a$ , i.e., the differences between the  $pK_a$ s of the two OH groups upon complete proton transfer to water, and, for the excited singlet state, the value of  $\Delta pK_a^*$  for ESPT.

The upper curve in Fig. [4](#page-3-1) corresponds to the dimensionless energy diference between stretching the 7-OH or the 4′-OH bond along the coordinate for proton transfer to water in the ground state, i.e., [E(7-OH)-E(4′-OH)]/0.059 V. The denominator (0.059 V) is the Nernst´s law change in



<span id="page-2-0"></span>**Fig. 1** B3-LYP/TZVP optimized structure of the 4′,7-dihydroxy-3,2′ furanofavylium cation **1** with two discrete water molecules in a PCM aqueous environment. Atom color code: green—C; red—O; grey—H

<span id="page-2-2"></span>**Fig. 2** Comparison of the B3-LYP/TZVP/PCM predicted absorption spectrum (red curve) with the normalized experimental spectrum [[12](#page-4-5)] at pH 1 in water (black curve)

<span id="page-3-0"></span>**Fig. 3** The NTO hole/particle pair for the  $S_1$  state of the furanofavylium cation **1** with two discrete water molecules in an aqueous environment. B3LYP/TZVP/PCM calculations. Isovalue =  $\pm 0.03$  *e*/Bohr<sup>3</sup>

4'-OH

7-OH

 $1.0$ 

 $0.8$ 



 $\overline{A}$ 

3

 $\overline{c}$ 

 $\overline{1}$ 

 $\Omega$ 

 $0.0$ 

 $0.2$ 

 $4.2 - ( \Delta E^* - \Delta E ) 0.059$ 



<span id="page-3-1"></span>**Fig. 4** Diference in the potential energy as a function of stretching  $(\Delta x)$  of only the 7-OH bond compared to that stretching only the 4′-OH bond in the ground state (black curve) or in the lowest excited singlet state (red curve), expressed as [*E*(7−OH)−*E*(4′−OH)]/0.059V

potential for a unit change in the pH, which converts the calculated energy difference into a  $\Delta pK_a$  value. The positive trend of the curve clearly indicates that the energy increases more rapidly along this coordinate for the 7-OH bond than for the 4′-OH group, i.e., that the 4′-OH group is slightly more acidic of the two. Although the value of  $\Delta pK_a$  that can be inferred from the trend of the curve is not large, only ca. 0.3–0.4 pK units, it is clearly in line with the experimental data pointing to the greater acidity of the 4′-OH group. In contrast, the lower curve, which corresponds to the analogous energy difference in the lowest excited singlet state,  $S_1$ , shows that ESPT from the 7-OH group to water is favored over that from the 4'-OH group by more than  $1 \text{ pK}^*$  unit. This approach appears to be more sensitive to diferences in acidity than a simple comparison of a parameter such as the natural charges on the oxygen atoms of the two OH groups. Thus, for the ground state, the two natural charges on these oxygens are found to be the same (-0.638 *e*). Nonetheless, in line with the increased acidity of the lowest excited singlet state, both natural charges decrease in  $S_1$ , with the 4<sup> $-$ </sup>OH oxygen atom slightly more negative than the 7-OH oxygen atom (− 0.606 *e* vs. 0.596 *e*, respectively).

Figure [5](#page-3-2) compares the changes in the calculated groundand excited-singlet-state energies, relative to the energy of

<span id="page-3-2"></span>**Fig. 5** Diference between the potential energy changes in the lowest excited singlet state (Δ*E*\*) and in the ground state (Δ*E*) relative to the equilibrium geometry for selective stretching of either the 4′-OH bond (black curve) or the 7-OH bond (red curve), expressed as  $4.2-(\Delta E^*-\Delta E)/0.059$ , i.e., taking the ground state  $pK_a$  of 4.2 as the reference point

 $0.4$ 

 $0.6$ 

 $\Delta$ x O-H,  $\rm \AA$ 

the corresponding equilibrium geometries, along the coordinate for proton transfer to water for each of the two OH groups of the furanofavylium cation **1**. Taking the experimental ground state  $pK_a$  in water of 4.2 as the reference point, the predicted value of  $pK<sub>a</sub>$ <sup>\*</sup> for ESPT from the 4'-OH group is of the order of 1, while the 7-OH group is predicted to be between ca.  $-0.5$  and  $-1$ . This latter value is in reasonable agreement with the experimental value of  $pK<sub>a</sub>$ <sup>\*</sup> of ca. − 0.1 for the 7-OH group derived from the analysis of the pH dependence of the picosecond time-resolved fuorescence decay of the furanofavylium **1**.

## **4 Conclusions**

The adoption of a common reference state with an explicit water molecule hydrogen-bonded to each of the two OH groups of the furanofavylium cation **1** permits inferences about the relative acidities of the two OH groups via expeditious TD-DFT calculations along the coordinate for proton transfer to the explicit water molecule. The calculated results for the relative acidities agree with the experimental fnding [\[12\]](#page-4-5) that there is an inversion in the relative acidities of the two OH groups in going from the ground to the excited singlet state  $(S_1)$ . Moreover, the NTOs (Fig. [3\)](#page-3-0) for the  $S_1$  state clearly point to the origin of the enhanced photoacidity of  $S<sub>1</sub>$  compared to the ground state. Thus, the electronic excitation results in a signifcant shift of the electron density from the A and B rings and the oxygen atoms of the attached OH-groups into the C-ring upon electronic excitation. This strategy of employing a common reference state with an explicit water as the proton acceptor should serve as a convenient approach for natural or synthetic dyes with multiple OH groups, especially when the relative acidities are not readily accessible through experiment.

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