#### **REGULAR ARTICLE**



## **Unveiling the efects of doping small nickel clusters with a sulfur impurity**

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#### **Abstract**

Small free-standing Ni clusters have been widely investigated during the last decade, but not many of their derived chalcogenides, despite their interest in technology and the new prospects that the nanoscale may open. The present work uncovers the effects of the S-doping on the structural, electronic, and magnetic properties of  $Ni<sub>n</sub>$ ,  $n = 1-10$  clusters. Density functional theoretical calculations within the generalized gradient approximation for the exchange and correlation were conducted to explore the structural, electronic, and magnetic properties of the resulting Ni<sub>n</sub>S chalcogenide nanoparticles. The sulfur impurity is always adsorbed on the threefold hollow sites available on the nickel host, in qualitative agreement with recent results of S adsorption on Ni(111) surfaces. S-doping tends to enlarge the average Ni–Ni inter-atomic distance but enhances the thermodynamical stability of Ni clusters. It also increases the vertical ionization energy and electron afnity. However, S-doping has a small efect on the magnetism of small Ni clusters. According to the spin-dependent HOMO–LUMO gap, most of these clusters are good candidates as molecular junctions for spin fltering at low bias voltage.

**Keywords** Ab initio calculations · Doping · Electronic properties · Magnetic properties · Nickel · Sulfur

## **1 Introduction**

The chalcogenides are an important class of materials from the technological viewpoint due to their signifcant electrical, optical, and chemical characteristics. The applications of chalcogenide materials include a variety of chalcogenide glasses, infrared sensors, solar energy conversion, and window layer  $[1-6]$  $[1-6]$  $[1-6]$ . Among chalcogenide nanomaterials, nickel sulfde NiS presents potential applications in photoconduction [[7](#page-9-2)]. In general, sulfur compounds such as transition metal sulfdes have important applications in superconduction [[8,](#page-9-3) [9](#page-9-4)], biochemical systems [[10](#page-9-5), [11\]](#page-9-6), and catalysis  $[12-14]$  $[12-14]$  $[12-14]$ . As thin films and at the nanoscale, the chalcogenides as it happens with most materials present a wide range of new properties inherent to the quantum confnement, which deserve to be explored by the Scientifc Community. The main characteristic of nanomaterials comes from the sensitivity of their electronic properties with their morphologies, size, and composition that can be completely diferent from their mesoscopic and macroscopic counterparts, thus offering new prospects for developing a wide range of new applications.

Small free-standing Ni clusters have been widely investigated from diferent theoretical approaches [\[15–](#page-9-9)[43](#page-9-10)] and experimentally [\[44,](#page-9-11) [45](#page-9-12)] during nearly two decades. However, no studies have been carried out so far regarding the efects of doping small nickel clusters with a light impurity. Oxygen and sulfur impurities are particularly interesting in this context, due to their abundance, their diferent electronegativity as compared with Ni, and the relevance of nickel oxide and chalcogenides. By doping the pure Ni*n* clusters with an electronegative element like sulfur, local charge transfer is expected which could induce a partial ionic contribution to the local bonding in the system. The aim of the present work is to perform a systematic theoretical study of the evolution of the structural, electronic, and magnetic properties of small Ni clusters when doped with a single sulfur impurity. We performed density functional theoretical calculations of  $Ni<sub>n</sub>S$  clusters in the size range of  $n = 1-10$ .

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We determined the most stable atomic arrangements, the absolute and relative stabilities, the electronic structure and magnetic properties, and electronic indicators such as ionization potentials and electron affinities.

A description of our theoretical approach is done in the next section. The results are presented in Sect. [3](#page-1-0) in which we frst present the structural properties and then we discuss the stability and electronic properties. The main conclusions are summarized at the end.

## **2 Computational method**

Calculations were conducted within the density functional theory, using a plane wave basis set and the projected augmented wave (PAW) approach for the core interactions, as implemented in the VASP code [\[46\]](#page-9-13). We considered the  $3d^84s^2$  valence configuration for Ni, and  $3s^23p^4$  for S. A plane wave energy cutoff of 300 eV was taken. The exchange and correlation effects were treated in the generalized gradient approximation (GGA) by using the Perdew–Burke–Ernzerhof functional [[47](#page-9-14)]. A cubic supercell with lateral size of 15 Å was employed for all the calculations. Only the  $\Gamma$  point was taken for integrations in the Brillouin zone. The cluster geometry was optimized, without symmetry constraints, until the force on each atom was less than 0.001 eV/Å, and the total energy was converged to  $10^{-6}$  eV. For charged clusters, corrections to the total energy were included by considering the full dipole moment in all directions. The corrections were calculated as the energy diference between a monopole, dipole, or quadrupole in the current supercell and the same monopole, dipole, or quadrupole placed in a vacuum. Furthermore, the quadrupole corrections originating from the expectation value of  $r<sup>2</sup>$  were also taken into account.

The lowest-energy structures of pure Ni*n* clusters were obtained by considering various initial confgurations with diferent symmetries. Most of the inputs used were taken from previously published works. For doped Ni<sub>n</sub>S clusters, we considered various initial atomic arrangements with the S atom occupying the diferent sites, and also by adsorbing it on all possible sites of several bare Ni*n* low-lying isomers (frst, second, and sometimes third isomers) calculated beforehand. We checked that the results remain unchanged after small displacements of the atoms around their equilibrium positions and also for higher cutoff energies and even more stringent convergence criteria. The relative stability of diferent isomers was further checked by performing calculations in diferent spin states to be sure of the total spin of the putative ground state. Although we did not employ an unbiased structural search, we believe that our sampling should be sufficient due to the small size of the clusters.

With the VASP code, the local charges and spin magnetic moments are computed by projecting the plane wave components of the eigenstates onto spherical waves inside slightly overlapping atomic spheres of Wigner–Seitz radius. Because this projection depends on the choice of the atomic radius, the sum of the local charges and moments is not necessarily and always identical to the total cluster values. In order to overcome this issue when analyzing the local magnetic moments distribution, we performed the analysis by using Bader's method [[48–](#page-9-15)[50](#page-9-16)] which is based on partitioning the cluster into atomic volumes by locating the zero-fux surfaces of the electron density feld.

The accuracy of the calculation method is checked by comparing the calculated bond length, vibration frequency, ionization potential, and electronic affinity of both  $Ni<sub>2</sub>$  and  $S_2$  dimers, with available experimental data. The results for  $Ni<sub>2</sub>$ , summarized in Table [1,](#page-1-1) show a fairly good agreement between the calculated and the measured values of the different quantities considered. As for the calculations for  $S_2$ , the consistency of the results with the experimental data can be found in our previous paper on  $Fe<sub>n</sub>S<sub>2</sub>$  clusters [\[51](#page-9-17)]. Moreover, additional test calculations for hexagonal bulk NiS (NiAs structure) give lattice parameters of 3.45 and 5.20 Å in good agreement with the measured values of 3.44 and 5.32 Å [\[52](#page-9-18)].

## <span id="page-1-0"></span>**3 Results and discussion**

#### **3.1 Structural properties**

In order to extract conclusions about the efect of S-doping on the structural and electronic properties, we have frst determined the putative ground state of the corresponding pure Ni*n* clusters which we also compare with previous results available in the literature. The atomic confgurations adopted by the putative minimum energy structure of  $Ni<sub>n</sub>$  and  $Ni<sub>n</sub>S$  ( $n = 1-10$  $n = 1-10$  $n = 1-10$ ) clusters are displayed in Figs. 1 and [2](#page-2-1). Only the geometries of the putative ground state are described along the text, except if certain isomers are energetically competitive with the ground state. Information

<span id="page-1-1"></span>**Table 1** Calculated values of bond length  $r$ , vibrational frequency  $\omega$ , ionization potential IP, and electronic affinity EA for  $Ni<sub>2</sub>$  dimer, compared to experimental data

$Ni2$ dimer	r(A)	$\omega$ (cm <sup>-1</sup> )	IP $(eV)$	$EA$ (eV)
This work Exp. works	2.09 $(2.15)^{a}$	320 $259.2 + 3.0^b$ 381 <sup>e</sup>	7.91 $7.65^{\circ}$	1.0 0.93 <sup>d</sup>

 $a^{a}$  [[53](#page-9-19)],  $b^{b}$  [[54](#page-9-20)],  $c^{c}$  [\[44\]](#page-9-11),  $d^{d}$  [\[45\]](#page-9-12),  $e^{c}$  [\[55\]](#page-9-21)



<span id="page-2-0"></span>**Fig. 1** Putative ground-state structures of Ni<sub>n</sub>,  $n = 2-6$  (first line) and Ni<sub>n</sub>S,  $n = 1-5$  (second line) clusters, with their corresponding point-group symmetry and total magnetic moment ( $\mu_B$ ). Bond lengths are given in Å and the local spin moments are given (in  $\mu_B$ ) inside the atomic spheres



<span id="page-2-1"></span>**Fig. 2** Putative ground-state structures of  $\text{Ni}_n$  ( $n = 7-11$ ) and  $\text{Ni}_n\text{S}$  $(n = 6-10)$  clusters, with their corresponding point-group symmetry and total magnetic moment  $(\mu_B)$ . The local spin moments are given

about all the low-lying isomers found in the present work can be obtained from the authors upon request.

# **3.1.1 Nin clusters**

We note that neutral  $\text{Ni}_{n}$  clusters have been the subject of several theoretical studies [\[15](#page-9-9)–[30,](#page-9-22) [32–](#page-9-23)[37](#page-9-24), [39](#page-9-25)[–43\]](#page-9-10) against which we can benchmark our theoretical approach. Let us note that our group already performed DFT calculations [[43\]](#page-9-10)

(in  $\mu_B$ ) inside the atomic spheres, whereas the bond lengths are given

in Table [2](#page-3-0) according to the labels of the diferent atoms

$\mathrm{Ni}_7$	Ni <sub>8</sub>	Ni <sub>9</sub>	Ni <sub>10</sub>	Ni <sub>11</sub>
$r_{12} = r_{25} = r_{51} = 2.32$ $r_{34} = r_{46} = r_{63} = 2.32$ $r_{14} = r_{45} = r_{35} = 2.35$ $r_{32} = r_{26} = r_{16} = 2.35$ $r_{17}=r_{27}=r_{57}=2.32\,$	$rr_{16} = r_{26} = 2.36$ $r_{17}=r_{27}=2.35\,$ $r_{14}=r_{23}=2.37\,$ $r_{36}=r_{46}=2.28\,$ $r_{35}=r_{45}=2.37\,$ $r_{38}=r_{48}=2.36\,$ $r_{37}=r_{47}=2.29\,$ $r_{58} = 2.32$ $r_{12} = 2.34$	$r_{14} = r_{16} = r_{17} = r_{19} = 2.37$ $r_{26} = r_{29} = r_{34} = r_{37} = 2.37$ $r_{25} = r_{28} = r_{35} = r_{38} = 2.36$ $r_{45} = r_{65} = r_{78} = r_{98} = 2.35$ $r_{46} = r_{79} = 2.36$ $r_{47} = r_{69} = 2.24$ $r_{85} = 2.32$	$r_{15} = r_{35} = r_{31} = 2.41$ $r_{26} = r_{46} = r_{24} = 2.42$ $r_{27}=r_{48}=r_{69}=2.28\,$ $r_{37}=r_{57}=r_{39}=2.28\,$ $r_{19}=r_{18}=r_{58}=2.28\,$ $r_{14} = r_{16} = r_{32} = 2.41$ $r_{36} = r_{52} = r_{54} = 2.41$	$r_{12}=r_{13}=2.37\,$ $r_{24} = r_{35} = 2.38$ $r_{45} = 2.43$ $r_{26} = r_{36} = 2.31$ $r_{46} = r_{56} = 2.60$ $r_{16} = 2.33$ $r_{27} = r_{37} = 2.38$ $r_{47} = r_{57} = 2.42$ $r_{17} = 2.32$ $r_{48}=r_{58}=2.38\,$ $r_{67} = 2.59$ $r_{68} = 2.31$ $r_{411} = r_{511} = 2.28$ $r_{711} = 2.28$ $r_{92}=r_{103}=2.37\,$ $r_{94}=r_{105}=2.32\,$ $r_{96} = r_{106} = 2.37$ $r_{98} = r_{108} = 2.36$

<span id="page-3-0"></span>**Table [2](#page-2-1)** Inter-atomic distances  $r_{ii}$  ( $\hat{A}$ ) in Ni<sub>n</sub>,  $n = 7-11$  clusters according to the labels of the different atoms of Fig. 2

for pure Ni clusters by using the SIESTA code [[56](#page-9-26), [57\]](#page-9-27) with the same approximation for exchange and correlation (GGA–PBE) as in the present work. This method is based on norm-conserving pseudopotentials and linear combinations of atomic orbitals as basis sets for which we used triple-*𝜁* with double polarization functions. In general, our present results for nickel clusters are similar to those previously obtained with the SIESTA code [\[43\]](#page-9-10). There exist nevertheless some exceptions like  $Ni<sub>5</sub>$  for which VASP gives a trigonal bipyramid of D3*h* symmetry and total moment of  $4 \mu_B$ , whereas SIESTA gave a square pyramid of  $C_{4v}$  symmetry and  $6 \mu_B$  of total moment. However, we point out that the first isomer of Ni<sub>5</sub> with total moment of  $6 \mu_B$  is found at only 0.03 eV of energy above the putative ground state with total moment of  $4 \mu_{\text{B}}$ . Apart from slight relaxations, our optimized geometries of neutral Ni*n* clusters, displayed in Figs. [1](#page-2-0) and [2](#page-2-1), are also consistent with previous results published elsewhere, except for few sizes in which a similar scenario as in the previously mentioned case of  $\text{Ni}_5$  in the SIESTA versus VASP benchmark occurs. Diferent approaches at the DFT level are known to give rise sometimes to slightly different energetic ordering of the low-lying isomers. It is for this reason that recalculating the pure Ni clusters at the same level of accuracy as the S-doped clusters is appealing for providing a consistent analysis (Table [3](#page-4-0)).

#### **3.1.2 NinS clusters**

We discuss frst the general trends. We fnd that the S atom tends to occupy a threefold hollow site on the Ni*n* host clusters, in qualitative agreement with recent DFT calculations [[58\]](#page-9-28) where it was shown that the sulfur adsorption on the Ni(100) and Ni(110) surfaces takes preferably place on the most coordinated sites.

The computed average Ni–Ni distance (AD) in both Ni*<sup>n</sup>* and Ni<sub>n</sub>S clusters is plotted as a function of cluster size *n* in Fig. [3](#page-4-1)a. In pure nickel clusters, it increases up to  $n = 5$  and then it keeps nearly constant to stabilize around a value of 2.35 Å. The situation is diferent in the S-doped clusters, where the Ni–Ni distance increases with respect to that of the pure Ni*n* clusters although with a lower slope. Let us now analyze in some detail the structures of the diferent clusters.

The ground state of  $Ni<sub>2</sub>S$  is an isosceles triangle  $(C<sub>2</sub>v)$ symmetry), with Ni–S and Ni–Ni bond lengths of 2.03 and 2.32 Å, respectively. Its total magnetic moment of  $2\mu_B$ results from a parallel magnetic coupling between the Ni atoms  $(2 \times 0.82 \mu_B)$  and the S atom  $(0.36 \mu_B)$ . We note that S-doping considerably enhances the Ni–Ni bond length, as in the pure  $Ni<sub>3</sub>(D<sub>3h</sub>)$  these bond lengths are 2.21 Å, and even smaller in Ni<sub>2</sub> (2.09 Å), both pure clusters having also  $2\mu_B$ .

For  $Ni<sub>3</sub>S$ , the putative ground state is a trigonal pyramid of C<sub>s</sub> symmetry and total moment of  $2 \mu_B$ , as that of Ni<sub>3</sub>. The local moments on Ni atoms are  $2 \times 0.64$  and  $0.66 \mu_B$ whereas the induced moment on S is very small  $0.06 \mu_{\rm B}$ . A trigonal pyramid of  $C_{3v}$  is the first isomer, lying at just  $0.02$ eV above the ground state. The pure  $Ni<sub>4</sub>$  is a tetrahedron  $(D<sub>2</sub>)$ with total moment of  $4 \mu_{\text{B}}$ . In this case, substitutional doping reduces the total magnetic moment. Doping also enhances the average Ni–Ni inter-atomic distance.

<span id="page-4-0"></span>





<span id="page-4-1"></span>**Fig. 3 a** Calculated average Ni–Ni distance (AD), **b** second energy difference  $(\Delta_2 E)$ , and **c** binding energy (BE) as function of cluster size  $n = 1-10$ 

 $Ni<sub>4</sub>S$  is a trigonal bipyramid of  $C<sub>3*v*</sub>$  symmetry and 4  $\mu$ <sup>B</sup> of total moment. The two non-equivalent Ni–Ni bond lengths  $(2.32 \text{ and } 2.29 \text{ Å})$  are slightly larger than those of Ni–S bonds (2.18 Å). The local Ni moments are  $3 \times 0.98$  and 0.93  $\mu_B$  whereas the S atom is noticeably polarized (0.13  $\mu_B$ ). The same atomic arrangement, but with a  $C_s$  symmetry and the same total moment  $(4 \mu_B)$  is found as the first isomer at only 0.01 eV above. The pure  $Ni<sub>5</sub>$  is a trigonal bipyramid of  $D_{3h}$  symmetry and total moment of 4  $\mu_B$ , meaning that doping here does not modify the magnetic moment.

The putative lowest-energy structure of  $Ni<sub>5</sub>S$  is a Ni<sub>5</sub> distorted trigonal pyramid capped by the S atom on one of its threefold hollow sites. It has  $C_s$  symmetry and a total moment of  $4 \mu_{\rm B}$ . The pure Ni<sub>6</sub> cluster is a square bipyramid of  $D_{4h}$  symmetry and 8  $\mu_B$  of total moment resulting from the distribution of the moments of the base atoms  $(4 \times 1.33 \mu_B)$ and the apex atoms  $(2 \times 1.34 \mu_B)$ . This Ni<sub>6</sub> structure with D<sub>4*h*</sub> symmetry is energetically quasi-degenerated ( $\Delta E = 0.01$  eV) with the same atomic arrangement having  $C_i$  symmetry. Substitutional doping reduces the total moment and leads to an important atomic rearrangement.

For  $Ni<sub>6</sub>S$ , the putative ground state is obtained from the  $Ni<sub>6</sub>$  square bipyramid where the S atom is adsorbed on a threefold hollow site giving rise to a Ni–Ni bond breaking on the base. It has  $C_s$  symmetry and a moment of  $6 \mu_B$ . A similar atomic arrangement but with  $C_{3v}$  symmetry and the same total magnetic moment as pure  $Ni<sub>6</sub>$  (8  $\mu$ <sub>B</sub>), is found as the first isomer at only 0.04 eV above. The  $Ni<sub>7</sub>$  cluster is an  $Ni<sub>6</sub>$  octahedron capped by the seventh Ni atom on one of its threefold hollow site. It is of  $C_s$  symmetry and bears a total moment of  $8 \mu_B$ . As expected, the effect of enlarging the average Ni–Ni inter-atomic distance upon S-doping decreases as increasing the size of the Ni cluster.

The putative lowest-energy structure of  $Ni<sub>7</sub>S$  is a distorted pentagonal bipyramid of C*s* symmetry where the S atom caps one of its threefold hollow sites. It bears a total moment of  $6 \mu_{\rm B}$ . The reduction of the magnetic moment of the host cluster upon S-doping (by  $2 \mu_B$ ) that takes place for Ni<sub>7</sub>S as well as for  $Ni<sub>6</sub>S$  is less marked than for the smaller clusters discussed above; for larger clusters, as we will see, this efect disappears. We will come later to this point when discussing the electronic properties. Ni<sub>8</sub> has a bisdisphenoid configuration with  $C_{2v}$  symmetry and total magnetic moment of 8  $\mu_{\rm B}$ .

 $Ni<sub>8</sub>S$  is a  $Ni<sub>6</sub>$  octahedron capped by two Ni and one S atoms on threefold hollow sites. It has C*s* symmetry and total moment of  $8 \mu_B$ . The putative lowest-energy structure of Ni<sub>9</sub> is a trigonal prism tricapped of  $C_{2v}$  symmetry and total moment of  $8 \mu_{\rm B}$ .

The putative ground state of  $Ni<sub>9</sub>S$  is an octahedron  $Ni<sub>6</sub>$ capped by three Ni atoms and the S atom, on threefold hollow sites. It has the same symmetry  $(C_{3v})$  and same total moment  $(8 \mu_B)$  as the putative lowest-energy structure of  $Ni<sub>10</sub>$  where one of the Ni atoms is replaced by S (Fig. [2](#page-2-1)).

Finally, the lowest-energy structure of  $Ni<sub>10</sub>S$  is a distorted pentagonal bipyramid of C*s* symmetry and total moment of  $8 \mu_B$ , capped by three Ni atoms on threefold hollow sites. It was obtained by substituting the tenth atom of the  $Ni<sub>11</sub>$ cluster by the S atom (Fig. [2](#page-2-1)).

#### **3.2 Stability and electronic properties**

The binding energies (BEs) per atom for both  $\text{Ni}_n$  and  $\text{Ni}_n\text{S}$ clusters  $(n = 1-10)$  are plotted in Fig. [3c](#page-4-1). BE is calculated from the following expressions

$$
BE(Nin) = [-E(Nin) + nE(Ni)]/n,
$$
\n(1)

$$
BE(NinS) = [-E(NinS) + nE(Ni) + E(S)]/(n + 1).
$$
 (2)

First, we notice that the general behavior of the BE of pure Ni<sub>n</sub> clusters as function of size is consistent with previous theoretical results [[26](#page-9-29), [27](#page-9-30), [32,](#page-9-23) [36](#page-9-31), [39](#page-9-25), [42,](#page-9-32) [43](#page-9-10)]. BEs of Ni*n*S clusters are larger than those of pure Ni*n*, particularly for the smallest sizes for which the Ni/S rate is larger. As expected, BEs of pure and doped clusters tend to converge to each other as increasing cluster size. This refects the obvious fact that a single S atom is averaged with an increasing number of Ni atoms. For clusters larger than those investigated here, it is expected that the S atom will continue to occupy preferentially the most coordinated hollow sites, as it occurs in surfaces [[58\]](#page-9-28), with concomitant local relaxations but without afecting the rest of the host cluster. The binding energy indicates that S-doping enhances the thermodynamical stability of the Ni clusters. This binding increase is related to the strong S–Ni bonding, refected in the kind of adsorption site (the S atom is bonded with three Ni atoms in a threefold hollow site). As we will see later, the strong S–Ni bond is favored by a partial ionic contribution due to charge transfer from Ni to S as a consequence of the diferent electronegativities of the two elements (S is more electronegative than Ni).

A further evidence of the strong S–Ni bonding is provided by the single-atom fragmentation energies. We considered two single-atom fragmentation channels of Ni*n*S, involving one Ni atom or the S atom. These quantities, plotted in Fig. [4](#page-5-0)a, are defned in terms of total energies as follows:

$$
\Delta_{\mathcal{S}} = E[\text{Ni}_n] + E[\text{S}] - E[\text{Ni}_n\text{S}],\tag{3}
$$

$$
\Delta_{\rm Ni} = E[Ni_{n-1}S] + E[Ni] - E[Ni_nS].
$$
\n(4)

One can see from Fig. [4](#page-5-0)a that  $\Delta_{\rm S}$  is larger than  $\Delta_{\rm Ni}$ , for any size *n*, showing that the desulfurization (removing the S atom) of Ni*n*S systems requires more energy than extracting the less bonded Ni atom of the cluster. In other words, it is easier to dissociate Ni than S atom from the Ni<sub>n</sub>S system which suggests that the Ni–S bonding is stronger than the Ni–Ni one. The lowest Ni fragmentation energy corresponds to the extraction of one Ni atom from  $Ni<sub>4</sub>S$  and the largest desulfurization energy corresponds to the removing the S atom from  $Ni<sub>3</sub>S$  and  $Ni<sub>4</sub>S$ . The maximum difference  $(2.77 \text{ eV})$  between the two energies is obtained for Ni<sub>4</sub>S. One can connect the low energy required to dissociate one Ni atom from the  $Ni<sub>4</sub>S$  cluster to the enlargement of the Ni–Ni inter-atomic distances which takes place upon S-doping of  $Ni<sub>4</sub>$  (Fig. [3](#page-4-1)a). Besides, the apex Ni atom in the trigonal



<span id="page-5-0"></span>**Fig. 4** Fragmentation energies of Ni*n*S clusters via the loss of a Ni  $(\Delta_{\text{Ni}})$  or a S ( $\Delta_{\text{S}}$ ) atom, as a function of cluster size  $n = 1-10$  and calculated charge transfer to the sulfur atom in neutral  $\text{Ni}_n\text{S}$  clusters, as function of cluster size  $n = 1-10$  (**b**)

bipyramid of  $Ni<sub>4</sub>S$  is the less-bounded atom due to the repulsion with its Ni neighboring atoms, induced by the charge transfer to the S atom (Fig. [4b](#page-5-0)).

In order to discuss the relative stability of a cluster of a given size *n* with respect to its neighboring sizes, we computed the second energy difference, defined as  $\Delta_2 E(n) = E(n+1) + E(n-1) - 2E(n)$ . This quantity is plotted in Fig. [3](#page-4-1)b. For S-doped clusters, the most remarkable feature is the noticeable peak at  $n = 3$  indicating the high stability of  $Ni<sub>3</sub>S$  for which the completion of the threefold bonding of S with Ni takes place. Notice that this correlates with the largest desulfurization energy corresponding to the removal of the S atom from  $Ni<sub>3</sub>S$ . For pure Ni clusters,  $Ni<sub>6</sub>$ stands out as particularly stable. As we will see later, these relative stabilities are also refected in electronic properties like the ionization potential and the electronic affinity.

The vertical ionization potential (VIP) and the vertical electronic affinity (VEA) are important quantities that can be used to characterize the global reactivity of the Ni<sub>n</sub>S clusters by means of conceptual DFT indicators [\[59](#page-9-33)]. The VIP and VEA for both the pure and doped nickel clusters are plotted in Fig. [5,](#page-6-0) as a function of cluster size *n*, where we included the calculated values obtained for the pure Ni*n* clusters as well as experimental data reported for them [\[44,](#page-9-11) [45](#page-9-12)]. The VIP (VEA) of Ni<sub>n</sub>S clusters is calculated as the energy difference between the neutral clusters and the cationic (anionic) counterparts with the structure of the ground-state neutral cluster. Except the result of Ni atom, for which the diference between the experimental and the calculated values reaches ∼ 0.68 eV, the calculated VIPs for Ni*n* clusters follow the experimental data [[44](#page-9-11)] rather well as a function of cluster size. This gives further support to our putative ground-state structures. Unfortunately, experimental data concerning VIP and VEA of S-doped nickel clusters are not available so far. However, one can bring out some trends concerning the effect of S-doping on VIP of Ni<sub>n</sub>S by comparing their calculated values with those of the pure Ni*<sup>n</sup>* clusters. From Fig. [5](#page-6-0), one can see that S-doping produces in general a slight increase of the VIP, except for  $n = 2$  and 6. We also note that the VIPs decrease as a function of size in a more monotonic fashion for the S-doped Ni clusters than for the pure ones. As for the calculated values of VEAs for Ni*n* clusters, they agree also rather well with the experimental data, except for  $n = 3$  for which the difference in the absolute values amounts to 0.28 eV. The VEA of pure Ni clusters increases quite linearly with *n* between  $n = 2$  and 9 and then decreases slightly for  $n = 10$ . The VEA increases upon S-doping by about 11%. It follows almost the same slope as of pure nickel clusters as a function of cluster size *n*. The enhancements of both VEA and VIP of S-doped clusters with respect to those of pure Ni*n* are consistent with the higher binding energy of the S-doped clusters as compared with the pure ones (Fig. [3c](#page-4-1)).



<span id="page-6-0"></span>Fig. 5 Vertical ionization potential (VIP), vertical electronic affinity (VEA), electronegativity  $(\chi)$ , and chemical hardness  $(\eta)$  of Ni<sub>n</sub> (open triangle) and  $\text{Ni}_n\text{S}$  (filled square) as function of the cluster size  $n =$ 1–10

From VIP and VEA, one can evaluate the electronegativity (the negative of the electronic chemical potential  $\mu$ ):

$$
\chi = -\mu = \frac{1}{2}(\text{VIP} + \text{VEA}),\tag{5}
$$

and the chemical hardness (or fundamental gap, except for a constant factor):

$$
\eta = E_{\text{gap}} = \frac{1}{2}(\text{VIP} - \text{VEA}).\tag{6}
$$

These quantities are plotted in Fig. [5](#page-6-0) as a function of the cluster size *n* for the pure and doped nickel clusters. Both  $\chi$ and  $\eta$  of Ni<sub>n</sub> clusters display qualitatively the same behavior as the ionization energy as function of the size *n*. They decrease between  $n = 2$  and 4 and then increase up to  $n = 6$ after which it decreases again up to  $n = 10$ . Thus, both quantities present a local maximum at  $n = 6$  and a local minimum at  $n = 4$  which correlates with the relative high stability of  $Ni<sub>6</sub>$  clusters and the low stability of  $Ni<sub>4</sub>$  already observed through the second diference in the energy (Fig. [3b](#page-4-1)). The

electronegativity of S-doped Ni clusters is equal or higher than that of the pure ones. The chemical hardness  $\eta$  does not change much, and the most noticeable change occurs for  $n = 4$ .

Let us discuss now the magnetic behavior of the pure and S-doped nickel clusters. The total magnetic moment as a function of cluster size *n* of both sets of clusters is plotted in Fig. [6](#page-7-0)a. We have also plotted the magnetic moments per atom (Fig. [6b](#page-7-0)) and included, for the sake of comparison, the available experimental data for pure  $Ni<sub>n</sub>$  clusters [[60](#page-9-34)]. Our values are smaller than the experimental ones, as it is also the case for almost all ab initio calculations on nickel clusters [\[26,](#page-9-29) [33](#page-9-35), [35,](#page-9-36) [40](#page-9-37), [42](#page-9-32)]. Those discrepancies between theory and experiment remain an open question, although the problem may arise from the additional orbital moment contributions or isomerization efects as suggested by some authors [[31,](#page-9-38) [38\]](#page-9-39).

The S-doping of Ni<sub>n</sub> clusters affects Ni<sub>6</sub>S and Ni<sub>7</sub>S by reducing their total moment from 8  $\mu_B$  in Ni<sub>6</sub> and Ni<sub>7</sub> to 6  $\mu_B$ . We note that for both  $Ni<sub>6</sub>S$  and  $Ni<sub>7</sub>S$  clusters, the magnetic state with  $8 \mu_B$  is only  $\sim 0.03$  eV higher in energy than the ground state with  $6 \mu_B$ . This small effect of S-doping on the total spin polarization of Ni*n* clusters is consistent with the weak hybridization between the S and Ni orbitals. To analyze this with two examples, we compare the density of states (DOS) of  $\text{Ni}_5\text{S}$  (Ni<sub>6</sub>S) with that of Ni<sub>5</sub> (Ni<sub>6</sub>) (Figs. [7,](#page-7-1) [8](#page-8-0)). In both cases, the hybridization is weak and involves molecular orbitals far from the Fermi level. For  $Ni<sub>5</sub>S$  the



<span id="page-7-0"></span>**Fig. 6** Total magnetic moments (**a**) and magnetic moments per atom (**b**) of  $\text{Ni}_n\text{S}$  and  $\text{Ni}_n$  as a function of cluster size  $n = 1-10$ 



<span id="page-7-1"></span>**Fig. 7** Total spin-polarized density of states projected on the 5 Ni atoms and on the S atom of the putative ground state of  $\text{Ni}_5\text{S}$  (bottom panel), as compared to the total DOS of the host  $\text{Ni}_5$  (top panel). The vertical dashed line indicates the Fermi energy. A Gaussian smearing (0.1 eV) of the states has been used in the plot

geometry of the host  $Ni<sub>5</sub>$  cluster is essentially preserved (Fig. [1\)](#page-2-0), and no signifcant rearrangement of both spin-up and spin-down states takes place upon S-doping, the total moment being preserved (Fig. [7\)](#page-7-1). In  $Ni<sub>6</sub>S$ , however, we observe an important electronic states rearrangement for both spin components upon S-doping (Fig. [8\)](#page-8-0), associated with a structural change. The spectrum rearrangement is accompanied by a spin fip from the majority to minority spin states, giving rise to a decrease of  $2 \mu_B$  upon doping.

Finally, we plot in Fig. [9](#page-8-1), as a function of cluster size, the spin-up and spin-down HOMO–LUMO gaps of Ni*n*S in their putative lowest-energy structures. The HOMO–LUMO gap of each spin channel is a key quantity for spin-dependent electronic transport at low voltages. The S-doped clusters with  $n \leq 4$  and  $n = 8$ –10 have relatively large HOMO–LUMO gaps for spin-up states ( $\sim$  2.38–1.20 eV), whereas, except for  $n = 3$ , spin-down states have small gaps (∼ 0.60–0.04 eV). The situation is somewhat diferent for pure Ni*n* clusters where the largest HOMO–LUMO gaps for spin-up states are obtained for  $n = 2-3$  and for sizes larger than  $n = 5$ . Ni<sub>6</sub>(Ni<sub>4</sub>) displays the largest (lowest) gap 2.46 (0.23 eV) which refects the high (low) stability of this cluster (Fig. [3](#page-4-1)b). One can note that the total gap of  $Ni<sub>4</sub>$  is the smallest one as refected in its low stability from the



<span id="page-8-0"></span>**Fig. 8** Total spin-polarized density of states projected on the 6 Ni atoms and on the S atom of the putative ground state of  $\text{Ni}_6\text{S}$  (bottom panel), as compared to the total DOS of the host  $\text{Ni}_6$  (top panel). The vertical dashed line indicates the Fermi energy. A Gaussian smearing (0.1 eV) of the states has been used in the plot



<span id="page-8-1"></span>**Fig. 9** HOMO–LUMO gap for spin-up and spin-down electrons of  $\text{Ni}_n\text{S}$  (a) and  $\text{Ni}_n$  (b) as function of cluster size  $n = 1-10$ 

calculated second diferences of energy for pure Ni*n* clusters (Fig. [3b](#page-4-1)). The gaps corresponding to spin-down states are relatively small, and nearly zero for  $n > 4$ , indicating that these clusters are good candidates as molecular junctions for spin fltering at low bias voltage.

However, the absolute value of the HOMO–LUMO gap has to be taken with care, since it is not a well-defned quantity in DFT that tends to underestimate it due to the lack of electronic correlations. Hybrid functionals such as BLYP, B3LYP, B3PW91, HSE06, among others are designed to better describe part of the exchange and/or correlation efects and, thus, give better absolute values for the HOMO–LUMO gaps than functionals like PBE that otherwise are built from physical grounds and work well for a wide spectrum of properties. To the best of our knowledge, only one theoretical work using B3LYP functional [\[61](#page-9-40)] was devoted to nickel sulfide clusters  $(NiS)<sub>n</sub>$ ,  $n = 3-5$ . In order to estimate the discrepancy between the HOMO–LUMO value obtained with PBE and B3LYP, we calculated at the PBE level the ring structure proposed for  $(NiS)<sub>3</sub>$  in this reference. The PBE HOMO–LUMO gap (0.50 eV) underestimates the B3LYP one  $(1.04 \text{ eV})$  in about 50%. Other quantities such as ionization potential (IP) and electron afnity (EA) and derived quantities are expected to be less affected since they are obtained as energy diferences between ground states calculated at the DFT level, so that they are well-defned indicators within the DFT as opposed to the HOMO–LUMO gap. This is confrmed by the calculated VIPs and VEAs for Ni*n* clusters which follow the experimental data rather well as a function of cluster size, as indicated in Fig. [5](#page-6-0). For the ring structure proposed for  $(NiS)_3$  in reference [\[61](#page-9-40)], our calculated values of VIP and VEA, 5.65 and 3.5 eV, respectively, are within 13 and 18% of those of B3LYP, 5 and 4 eV, respectively [\[61](#page-9-40)].

## **4 Conclusions**

The main conclusions of our DFT-GGA study of S-doped  $Ni<sub>n</sub>S$  clusters ( $n = 1-10$ ) can be summarized as follows.

- 1. The S atom tends to occupy a threefold hollow site, in agreement with DFT calculations [[58\]](#page-9-28) of sulfur adsorption on Ni surfaces, which was shown to take place preferentially on the most coordinated sites. A further evidence of the strong S–Ni bonding is provided by the single-atom fragmentation energies: a Ni atom can be extracted from Ni*n*S with a lower energy cost than the S atom.
- 2. S-doping enhances the thermodynamical stability of the Ni clusters. The increase of binding energy upon S-doping is related to the strong S–Ni bonding, also favoured by a partial ionic contribution due to charge

transfer from Ni to S. According to the second diferences in energy,  $Ni<sub>3</sub>S$  is particularly stable with respect to the neighboring sizes. All atoms of this cluster are involved in the threefold bonding, and it has the largest desulfurization energy among the investigated clusters.

- 3. S-doping only affects the magnetic moment of  $Ni<sub>6</sub>S$  and  $Ni<sub>7</sub>S$  by reducing their total moment from 8  $\mu$ <sub>B</sub> in Ni<sub>6</sub> and  $\text{Ni}_7$  to 6  $\mu_\text{B}$ . The spin-polarized densities of states show a weak hybridization between the S and Ni orbitals, but strong enough structural changes upon doping, in few cases, to produce an electronic states rearrangement consistent with a change of total moment.
- 4. S-doped clusters with  $n \leq 4$  and  $n = 8$ –10 have relatively large HOMO–LUMO gaps for spin-up states. However, the gaps corresponding to spin-down states are small, and nearly zero for  $n > 4$ , indicating that most of these clusters are good candidates as molecular junctions for spin fltering at low bias voltage.

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