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Advanced CNC thread milling: a comprehensive canned cycle for efficient cutting of threads with fixed or variable pitch and radius

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Abstract

This paper presents the design, implementation, and experimental validation of a novel canned cycle for CNC milling machines, enabling the precise and efficient cutting of threads with fixed or variable pitch and radius. Conventional canned cycles are limited to fxed pitch threads, restricting the versatility of CNC milling machines in thread machining applications. The development process involves integrating a sophisticated control algorithm into the CNC milling machine's software, giving the operator remarkable control over the thread cutting process. This algorithm allows the operator to choose between external or internal threads, set both initial and fnal radii, determine initial and fnal pitches, specify the number of turns, and select the left or right-hand thread type. Such fexibility enables the creation of threads with diverse geometries. Furthermore, the proposed canned cycle provides the capability to switch between roughing and fnishing passes by adjusting the step motion along the prescribed helical curve.

Simulation tests conducted under various threading cases clearly demonstrate the efficiency of the proposed canned cycle. These results showcase its capability to address a wide range of machining scenarios, ofering practical solutions applicable across a spectrum of applications.

Keywords CNC machining · Canned cycles · Thread cutting · Interpolation algorithms

Nomenclature

- H Height of the spiral, mm
- *m* Slope of the cone's lines with respect to the $x y$ plane
- *n* Total number of turns
- n_0 Angular velocity, rev/min
- *n*(*t*) Number of turns of a helix at time *t*
- p_f Final pitch of the helix, mm
- p_i Initial pitch of the helix, mm
- $p(t)$ Pitch of the helix at time *t*, mm
- R_f Final radius of the helix, mm
- *Ri* Initial radius of the helix, mm
- $r(t)$ Radius of the helix at time t , mm
- T Time required for traversing a complete revolution, min
- *t* Time variable, min

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- t_f Time it takes the cutting tool to complete the process, min
- $x(t)$ $x Ax$ *x* position of the cutting tool at time *t*, mm
- $y(t)$ $y Ax$ *y* position of the cutting tool at time *t*, mm
- z_0 Calibration constant for the initial position on the *z* axis
- $z(t)$ *z* Axis position of the cutting tool at time *t*, mm τ Normalized time

1 Introduction

The evolution of Computer Numerical Control (CNC) machining has brought about a revolution in manufacturing processes, not only enhancing precision and efficiency but also addressing the challenges posed by complex geometries and demanding machining applications. This paper deals with the domain of CNC thread milling, introducing an innovative approach through the development and implementation of a comprehensive canned cycle.

A canned cycle is a predefned machining operation that entails a sequence of machine movements to perform various machining tasks like drilling, pocketing, slotting, boring, and

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Fig. 1 Helix with variable radius and pitch

tapping. It aims to simplify programming by consolidating multiple commands into a single block, utilizing G-code to defne machining operations that would typically necessitate multiple blocks $[1, 2]$ $[1, 2]$ $[1, 2]$. Continuous efforts are made by CNC manufacturers to incorporate new canned cycles into their controllers, specifcally designed to handle intricate

Fig. 3 Helix with constant radius and variable decreasing pitch $(R_i = R_f = 40, \text{pi} = 16, \text{pf} = 4, \text{ n} = 8)$

and complex geometries [[3,](#page-14-2) [4\]](#page-14-3). This is easily concluded by comparing the canned cycles available nowadays with the older ones.

Centered on programming and facilitating the precise and efficient cutting of threads within a user-friendly environment, incorporating both fxed and variable pitch and radius, the presented canned cycle addresses limitations posed by conventional canned cycles, which primarily target fxed pitch threads. In the precise domains of engineering and manufacturing, the use of variable pitch threads is necessitated by diverse potential applications. These applications encompass manufacturing components for automotive vehicle engines, fasteners for aerospace systems, industrial

Fig. 2 Helix with constant radius and variable increasing pitch $(R_i = R_f = 40, \text{pi} = 4, \text{pf} = 16, \text{ n} = 10)$

Fig. 4 Helix with variable radius and variable increasing pitch $(Ri=50, Rf=80, pi=5, pf=25, n=8)$

Fig. 5 Helix with variable radius and variable decreasing pitch $(Ri=50, Rf=80, pi=25, pf=5, n=8)$

devices, robots manufacturing parts [[5–](#page-14-4)[8\]](#page-14-5) and the creation of medical implants [\[9–](#page-14-6)[12\]](#page-14-7). The mentioned references constitute a sample of recent related research work.

The foundation of work's innovation lies in the integration of a sophisticated control algorithm into the CNC milling machine's software. This integration empowers operators with an unprecedented level of control over the thread cutting process. Operators can seamlessly choose between external or internal threads, defne initial and fnal radii, determine initial and fnal pitch, specify the number of turns, and even select the thread's direction. This fexibility allows for the creation of threads with diverse geometries, signifcantly broadening the applicability of CNC milling machines in thread machining applications. Furthermore, the proposed canned cycle provides the means to switch

Fig. 6 Helix with variable radius and constant pitch $(Ri = 50, Rf = 80,$ $pi=15$, $pf=15$, $n=8$)

between roughing and fnishing passes. This is achieved through precise regulation of the step motion along the prescribed helical curve, adding another layer of adaptability to the machining process.

To validate the effectiveness of the approach, extensive simulation tests have been conducted under various threading cases. The results clearly demonstrate the efficiency of the proposed canned cycle, showcasing its capability to address a wide spectrum of machining scenarios.

The present study represents an evolution of prior research [\[13\]](#page-14-8), wherein plans were discussed to extend the scope by incorporating cases with variable radius and pitch, along with predefned initial and fnal radii and pitches, with the number of turns also pre-selected. The current work builds upon and extends the fndings from the previous research, resulting in a signifcant expansion of the capabilities of the proposed new canned cycle.

In the following sections, the paper presents the mathematical formulation of helix equations (Section [2\)](#page-2-0), CNC parametric programming (Section [3](#page-6-0)), and the design and formulation of the interpolation algorithm (Sections [4](#page-6-1) and [5](#page-8-0)). Implementation issues (Section [6](#page-8-1)) and comprehensive test results (Section [7\)](#page-10-0) are then discussed. In the conclusion (Section [8](#page-12-0)), the paper highlights the innovative canned cycle's contribution to advancing CNC thread milling.

2 Mathematical formulation of helix equations

To facilitate the cutting of threads with constant or variable radius and pitch on a 3-axis CNC milling machine, it is crucial to have the ability to generate 3D motion along a helix

Fig. 7 Helix with initial radius set to zero and variable Increasing pitch ($\text{Ri}=0$, $\text{Rf}=40$, $\text{pi}=0$, $\text{p}f=20$, $\text{n}=7$)

D CODE	FUNCTION	EXAMPLE	EXPLANATION
D ₀₀	ASSIGNMENT	D00 Q1 P01 20	Assignment of the value 20 to parameter Q1
D ₀₁	ADDITION	D01 O2 P01 O3 P02 O4	The result of $(Q3 + Q4)$ is assigned to Q2
D ₀₂	SUBTRACTION	D02 Q5 P01 Q6 P02 8	The result of $(Q6 - 8)$ is assigned to Q5
D ₀₃	MULTIPLICATION	D03 O8 P01 O9 P02 -2	The result of $(-2)(Q9)$ is assigned to Q8
D ₀₄	DIVISION	D04 Q10 P01 Q11 P02 4	The result of $Q11/4$ is assigned to $Q10$
D ₀₅	SOUARE ROOT	D05 O12 P01 O13	The square root of Q13 is assigned to $Q12$
D ₀₆	SINE	D06 O14 P01 O15	The result of $sin(Q15)$ is assigned to Q14
D ₀₇	COSINE	D07 Q16 P01 Q17	The result of $cos(Q17)$ is assigned to $Q16$
D ₀₉	IF EQUAL, JUMP	D09 P01 Q20 P02 5 P03 1	If $Q20$ is equal to 5, jump to label 1
D10	IF NOT EOUAL, JUMP	D10 P01 Q21 P02 Q22 P03 2	If Q21 is not equal to Q22, jump to label 2
D11	IF GREATER, JUMP	D11 P01 Q23 P02 0 P03 3	If Q23 is greater than 0, jump to label 3
D ₁₂	IF LESS, JUMP	D12 P01 O24 P02 0 P03 4	If $Q24$ is less than 0, jump to label 4
D ₁₃	CALCULATE ANGLE	D13 O30 P01 O25 P02 O26	The result of $arctan(Q25/Q26)$ is assigned to Q30

Table 1 Heidenhain Control System Parameter Guide

with the specifc characteristics. This involves solving the parametric equations $x(t)$, $y(t)$, $z(t)$ of the helix within the framework of an interpolation algorithm.

When examining a conical helix, which is a helix situated on the curved surface of a cone, its parametric equations can be formulated as follows [[14](#page-14-9), [15](#page-14-10)]

 $x(t) = r(t)\cos(2\pi n(t)),$ (1)

 $y(t) = r(t)\sin(2\pi n(t)),$ (2)

$$
z(t) = z_0 + mr(t) \tag{3}
$$

where,

Table 2 Summary of thread features along with the corresponding assigned input

parameters (Q)

tf the time it takes the cutting tool to complete the process.

t the time variable, with $0 \le t \le t_f$.

r(t)- the radius of the helix at time *t*.

- *n(t)-* the number of turns of a helix at time *t*.
- *m* the slope of the cone's lines with respect to the $x y$ plane.
- *z0* a constant.

In the following stage of the modeling process, the defnition of a function, labeled as r(t), is undertaken to embody ideal construction specifcations. The preferred input parameters for the model, as illustrated in Fig. [1](#page-1-0), include:

 R_i the initial radius of the helix.

 R_f the fnal radius of the helix.

pi the initial pitch of the helix.

 p_f the fnal pitch of the helix.

n the number of turns.

Then $r(t)$ should be calibrated accordingly accommodating these special parameter values. Assuming linear increase of the pitch from p_i to p_f , $p(t)$ can be expressed in the form:

$$
p(t) = p_i + (p_f - p_i) \frac{t}{t_f}.
$$
\n(4)

If T represents the time required for traversing a complete revolution, then $z(t)$ at time t is given by:

$$
z(t) = \frac{1}{T} \int_{0}^{t} p(s)ds = \frac{1}{T} \int_{0}^{t} \left(p_i + (p_f - p_i) \frac{t}{t_f} \right) ds
$$

= $\frac{p_i t}{T} + \frac{(p_f - p_i)t^2}{2T t_f} + C$ (5)

Supposing that $z(0) = 0$, then obtain that $C = 0$. As a result:

$$
z(t) = \frac{p_i t}{T} + \frac{(p_f - p_i)t^2}{2Tt_f}.
$$
\n(6)

Assuming that the helix is traversed with constant angular velocity, n_0 (rev/min), implies that $T = \frac{1}{n_0}$, and $t_f = \frac{n}{n_0}$, which gives that $\frac{T}{t_f} = \frac{1}{n}$. Given this, Eq. ([6\)](#page-4-0) simplifies to:

$$
z(t) = np_i \frac{t}{t_f} + \frac{n(p_f - p_i)}{2} \left(\frac{t}{t_f}\right)^2.
$$
 (7)

Fig. 8 Main program fowchart

Equation ([3](#page-3-0)) suggests that the radius $r(t)$ can then be expressed as:

$$
r(t) = \frac{1}{m} (z(t) - z_0) = \frac{1}{m} \left(n p_i \frac{t}{t_f} + \frac{n (p_f - p_i)}{2} \left(\frac{t}{t_f} \right)^2 - z_0 \right).
$$
\n(8)

Given that $r(0) = R_i$ and that $r(t_f) = R_f$, obtain that:

$$
z_0 = -mR_i, \text{ with } m = \frac{n(p_f + p_i)}{2(R_f - R_i)} \tag{9}
$$

A simple calculation then gives that:

$$
r(t) = R_i + \frac{2p_i(R_f - R_i)}{p_f + p_i} \frac{t}{t_f} + \frac{(p_f - p_i)(R_f - R_i)}{p_f + p_i} \left(\frac{t}{t_f}\right)^2
$$
\n(10)

Given the constant angular velocity n_0 , one can also derive $n(t) = n_0 t$. Thus, the corresponding equations of motion are given by:

$$
x(t) = \left(R_i + \frac{2p_i(R_f - R_i)}{p_f + p_i} \frac{t}{t_f} + \frac{(p_f - p_i)(R_f - R_i)}{p_f + p_i} \left(\frac{t}{t_f}\right)^2\right) \cos(2\pi n_0 t),
$$
\n(11a)

$$
y(t) = \left(R_i + \frac{2p_i(R_f - R_i)}{p_f + p_i} \frac{t}{t_f} + \frac{(p_f - p_i)(R_f - R_i)}{p_f + p_i} \left(\frac{t}{t_f}\right)^2\right) \sin(2\pi n_0 t),\tag{11b}
$$

$$
z(t) = np_i \frac{t}{t_f} + \frac{n(p_f - p_i)}{2} \left(\frac{t}{t_f}\right)^2 \tag{11c}
$$

Since $0 \le t \le t_f$, dividing by t_f gives that $0 \le \frac{t}{t_f} \le 1$ and thus define $\tau = \frac{t}{t_f} = \frac{n_0 t}{n}$. Thus, the equations of motion in terms of the new variable τ with $0 \le \tau \le 1$, can be written as follows:

$$
x(\tau) = \left(R_i + \frac{2p_i(R_f - R_i)}{p_f + p_i}\tau + \frac{(p_f - p_i)(R_f - R_i)}{p_f + p_i}\tau^2\right)\cos(2\pi n\tau),\tag{12a}
$$

$$
y(\tau) = \left(R_i + \frac{2p_i(R_f - R_i)}{p_f + p_i}\tau + \frac{(p_f - p_i)(R_f - R_i)}{p_f + p_i}\tau^2\right) \sin(2\pi n\tau),\tag{12b}
$$

$$
z(\tau) = np_i \tau + \frac{n(p_f - p_i)}{2} \tau^2.
$$
 (12c)

Notice that the fnal height of the workpiece *H* is given by $H = z(1) = n \frac{p_f + p_i}{2}$.

It can be easily shown that these equations are also valid for $R_i = R_f$ as the equations of motion reduce to:

$$
x(\tau) = R_i \cos(2\pi n \tau), \tag{13a}
$$

$$
y(\tau) = R_i \sin(2\pi n \tau),\tag{13b}
$$

$$
z(\tau) = np_i \tau + \frac{n(p_f - p_i)}{2} \tau^2.
$$
 (13c)

Moreover, swapping the sine and cosine functions in the initial two Eqs. $(12a)$ $(12a)$ and $(12b)$, allows for either a lefthand or right-hand thread type. The validation of Eqs. (12)

Fig. 9 Subprogram fowchart

is illustrated in the plots of Figs. [2](#page-1-1), [3,](#page-1-2) [4,](#page-1-3) [5](#page-2-1), [6](#page-2-2) and [7](#page-2-3) using representative values for pitch, radius and number of turns.

3 CNC parametric programming

CNC parametric programming serves as a fexible platform accessible in widely adopted controllers, known by various names depending on the provider controller. Fanuc custom macro B, Fadal macro, Okuma user task, Sinumeric and Heidenhain parametric technique are among the most widely used. Numerous research studies [\[16](#page-14-11)[–20\]](#page-14-12) have utilized this platform to resolve complex machining cases. This section aims to provide a detailed explanation of Heidenhain's parametric programming, the chosen programming language for this study. For a comprehensive understanding of the language, readers are directed to Lynch's in-depth book on the subject [\[21](#page-14-13)].

Within the Heidenhain control system, parameters are denoted by the letter Q followed by an integer. These parameters can be assigned numerical values directly or via arithmetic or trigonometric operations. Furthermore, the Q parameters can undergo dynamic updates during program execution and continuous checks to determine adherence to specific conditions, thereby influencing the program flow. In addition to the Q parameters, the letter D is employed to encode various functions, with specifc functions represented by numbers 1 to 13 (refer to Table [1](#page-3-1)). The table presented herein has been adopted from the reference [\[13](#page-14-8)] mentioned earlier in the introduction. To illustrate the language's structure, the table provides examples and explanations for each individual D code. It is significant to emphasize that Q parameters and fxed numerical values can coexist within the same function, allowing enhanced fexibility in programming.

4 Design of the interpolation algorithm

The interpolation algorithm is designed to handle a broad spectrum of thread geometries under desired cutting conditions. In this regard, the operator is empowered with the

Table 4 List of G-code for the Subprogram-1

capability to defne any of the features outlined in Table [2.](#page-3-2) Each feature is correspondingly assigned to a Q parameter, constituting the input values for the algorithm.

The development of the G-code algorithm is achieved through a main program and two subprograms. The main program initiates thread data by configuring parameters Q1-Q11 (refer to Table [2](#page-3-2)), positions the cutter at the starting point, and directs the execution fow to one of the two subprograms. These subprograms are formulated to address either a right-hand or a left-hand thread. The structure of the

Fig. 10 A single-form thread cutter **Fig. 11** External thread milling

Fig. 12 Internal thread milling

main program and the two subprograms is depicted in the flowcharts of Figs. [8](#page-4-1) and [9](#page-5-2) respectively.

While the fowchart of the subprogram (Fig. [9\)](#page-5-2) illustrates the scenario of a right-hand thread, a similar fowchart can be easily created for the left-hand thread case by interchanging the sine and cosine functions in the frst two Eqs. [\(12a\)](#page-5-0) and [\(12b\)](#page-5-1).

5 Formulation of the G‑code algorithm

The G-code algorithm is developed within the Heidenhain control framework. Furthermore, it can be effortlessly adapted for integration with any other CNC control system supporting parametric programming. Entering the necessary thread data and cutting conditions into the G-code algorithm is achieved through the utilization of Q parameters, as detailed in Section [4.](#page-6-1)

The flowcharts presented in Figs. [8](#page-4-1) and [9](#page-5-2) serve as the foundation for developing the G-code parametric algorithm, illustrating the logical structure of both the main program and the two subprograms. The corresponding code, along with accompanying comments, can be found in Tables [3](#page-6-2) and [4](#page-7-0). Table [3](#page-6-2) outlines the main program, while Table [4](#page-7-0) details subprogram 1. Subprogram 2 maintains the same structure but exchanges the sine and cosine functions in the frst two Eqs. $(12a$ $(12a$ and $12b)$.

6 Implementation

6.1 Practical aspects

A suitable cutter for threading on a CNC milling machine is the single form cutter depicted in Fig. [10](#page-7-1). Figures [11](#page-7-2) and [12](#page-8-2) illustrate the same cutter during the milling process for an external and internal thread respectively.

Fig. 13 Thread milling – Case: constant radius

Fig. 14 Thread milling – Case: variable radius (**a**) Internal threading (**b**) External threading

The zero-reference point is located at the upper surface of the workpiece, aligning with the center of the helix. The algorithm directs the rotating cutter diferently based on the thread type, whether internal or external. For internal threads, the cutter is moved linearly to the starting position with coordinates $X = Ri - r$, $Y = 0$, $Z = 0$. Alternatively, for external threads, the starting position is at coordinates $X=Ri+r$, $Y=0$, $Z=0$. The starting position is indicated in Figs. [13](#page-8-3) and [14](#page-9-0) for cases involving a constant and variable radius, respectively.

After positioning the cutter at the starting position, the algorithm directs the fow to one of the two subprograms based on the desired thread direction. Upon completion of the machining process, the tool frst retracts from the workpiece before moving to a safe height above the top surface.

6.2 G‑codifcation

Typically, canned cycles are standardized and encoded using a G-code accompanied by a set of parameters. It's essential to highlight that CNC controllers deliberately reserve certain G-codes for potential future applications, enabling customized implementations and enhanced fexibility. Specifcally, within the Heidenhain control

N270 L4*
N280 G98 L3*
N290 G90 G00 X+0 Y+Q4 Z+20*

framework, the unassigned G101 code has been chosen for the proposed implementation. The required supplemental data for the canned cycle can be conveyed through parameters P01 to P10 in a statement following the structure given in Fig. [15.](#page-9-1)

7 Test results

Simulation tests (depicted in Figs. [16](#page-10-1), [17](#page-10-2), [18,](#page-11-0) [19,](#page-11-1) [20,](#page-12-1) [21,](#page-12-2) [22](#page-13-0) and [23](#page-13-1)) have been carefully chosen to showcase the efficiency of the proposed canned cycle, encompassing all

31 H +22 V z

Fig. 17 TEST-2: Left-hand thread on constant radius with increasing pitch $(R_i = R_f = 40,$ $pi=4$, $pf=16$, $n=10$, precision τ = 0.001)

Fig. 18 TEST-3: Left-hand thread on variable radius with increasing pitch $(R_i = 50,$ $R_f=80$, pi = 5, pf = 25, n = 8, precision τ =0.001)

possible threading cases it is capable of handling. TEST-1 and TEST-2 simulate the same threading scenario but with different precision steps, offering a valuable capability for both roughing and fnishing passes. TEST-3 represents a left-hand thread with a variable radius and increasing pitch, while TEST-4 demonstrates a right-hand thread with a variable radius and decreasing pitch. TEST-5 maintains the settings of TEST-4 but incorporates an increased number of turns. TEST-6 focuses on a left-hand thread with a variable radius and constant pitch. TEST-7 examines a case of a left-hand thread with an initial radius set to zero and a variable increasing pitch. While all previous tests relate to external threads, the fnal TEST-8 illustrates a case of an internal thread. In all instances, the traced path displayed in the graphical simulation corresponds to the center of the cutting tool.

Fig. 19 TEST-4: Right-hand thread on variable radius with decreasing pitch $(R_i=40,$ $R_f = 90$, pi = 20, pf = 4, n = 7, precision τ = 0.001)

Fig. 20 TEST-5: Right-hand thread on variable radius with decreasing pitch $(R_i=40,$ R_f =90, pi = 20, pf = 4, n = 10, precision τ =0.001)

8 Conclusions

The work presented in this paper built upon the foundations laid in previous mentioned research. As predicted in that earlier work, the present study advanced and extended the capabilities of the thread canned cycle to encompass threads with predefned start and ending radii, start and ending pitches, and the desired number of turns, applicable to both left- or right-hand, internal or external threads. Moreover, the proposed canned cycle seamlessly transitions between roughing and fnishing passes, allowing precise regulation of step motion along the prescribed helical

Fig. 21 TEST-6: Left-hand thread on variable radius with constant pitch $(R_i=40, R_f=80,$ pi=15, pf=15, n=10, precision τ =0.001)

Fig. 22 TEST-7: Left-hand thread with initial radius set to zero and increasing pitch $(R_i=0, R_f=40, pi=0, pf=20,$ $n=8$, precision $\tau=0.001$)

÷

curve. The introduced canned cycle surpasses the limitations of conventional cycles, which are confned to fxed pitch threads, by providing a comprehensive solution for diverse threading requirements.

Simulation tests confrm the adaptability of the proposed canned cycle across diverse threading conditions. The graphical outputs, combined with the mathematical formulation of helix equations and CNC milling machine simulations across various threading cases, collectively verify the efficiency, and validation of the proposed canned cycle.

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Declarations

Competing of interests The authors have no competing interests to declare that are relevant to the content of this article.

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