CRITICAL REVIEW

Viscosity measurements in semi‑solid metal processing: current status and recent developments

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Abstract

Semi-solid metal processing (SSMP) is an ideal method of producing high-quality products with fewer defects in casting technology. Viscosity is the most important physical and chemical property for the fow behaviour of the SSMP. Currently, there are several approaches, both theoretical and experimental, to evaluate the viscosity of semi-solid metals. This paper comprehensively reviews the single point and multi-point viscometry for SSMP. Features, similarities, and limitations of diferent viscometers for SSMP applications are then compared. The efect of infuencing factors on the viscosity behaviour of SSMP is also highlighted. The importance of the non-dendritic globular microstructure and the instantaneous drop in viscosity caused by the scattering of solid particles during SSMP are explained. It is expected that the study will assist the researcher in identifying the best method of viscosity measurement during SSMP.

Keywords Semi-solid metal processing · Viscosity · Properties · Behaviour · Viscometer

1 Introduction

Fleming and his colleagues introduced the semi-solid metal processing (SSMP) at MIT in the 1970s [\[1\]](#page-21-0). SSMP has been widely known as an important technology for over 50 years. SSMP involves the processing of alloys between solidus and liquidus temperatures. Generally, SSMP consists of two main categories: rheo route and thixo route [[2\]](#page-21-1). The rheo route involves preparing a liquid phase semi-solid metal (SSM) slurry and transferring directly into a die or mould to form the component. In rheo routes, liquid metal alloy emulsion is stirred during solidifcation [[3](#page-21-2)]. This method uses the same concept similar to mechanical stirring, producing globular microstructure feedstock billet [\[4](#page-21-3)]. Thixo route is based on three steps: frst, the preparation of a feedstock billet having a globular and non-dendritic microstructure. The second step is to reheat the feedstock billet for a particular time to obtain a semi-solid structure between the solid and the liquid state. The third step is to obtain the shape of the mush state, which has thixotropic characteristics [[5](#page-21-4)]. Several advantages were found with thixo route over the rheo routes [[6\]](#page-21-5).

Viscosity properties play an important role in the dieflling behaviour of the SSM process during the casting process [\[7](#page-21-6)]. Density, molecular weight, solid fraction, particle size, distribution, chemical analysis, pouring temperature, and solidifcation time are among the important metallurgical parameters afecting the viscosity of the SSM process [[8,](#page-21-7) [9](#page-21-8)]. SSMP viscosity measurements are normally based on the physical properties, chemical reaction, and low viscosity of metals. SSMP is a short-term behaviour; therefore, special attention needs to be paid during viscosity measurement. Problems in the study of the viscosity properties of certain pure metals (Al, Mg, Cu, Zn, Fe, and Si) and alloys have been explained by several researchers [\[10](#page-21-9)[–13\]](#page-21-10).

Rheology is a branch of physics that studies the fow and decay of materials [[14\]](#page-21-11). The rheological property of SSMP is equal to the value of fuidity behaviour in liquid metals. Viscosity and fow behaviour is important in the casting process of commercial products such as automotive spare parts, aerospace equipment, electronic parts, machinery, and construction materials. SSMP is suitable for the processing of high-quality goods

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Fig. 1 (**a**) Typical micrographof dendritic microstructure (**b**) Globular microstructure of the semi-solidalloy sample [\[30\]](#page-21-24)

with low gas porosity, lower shrinkage, and light metals such as aluminium, magnesium, and copper [\[15\]](#page-21-12). It has been found that the SSMP method is the best way to eliminate the shortcomings of conventional casting and produce better products [\[16,](#page-21-13) [17\]](#page-21-14). However, the viscosity and flow behaviour needs to be controlled efficiently to avoid typical casting defects. Therefore, emphasis should be given to the viscosity measurement method of SSMP.

There are numerous methods to calculate the viscosity of metals during diferent processing stages. A standard method typically used to measure the viscosity of SSMP is the capillary, oscillating vessel, oscillating body or plate, falling ball or body, draining vessel, oscillation levitation, concentric cylinder, cone, and cone plate, drop-forge. Some of these methods were compiled and studied by Brooks et al. [\[18](#page-21-15)] for liquid metal viscosity measurement. However, the viscosity value of the SSMP was not included in the measurement.

Many researchers have studied a viscometer with two basic types, which consists of Newtonian and non-Newtonian fluids [[19](#page-21-16)[–21\]](#page-21-17). However, only several studies have provided a detailed discussion on SSMP viscosity measurement. Besides, it should be noted that there are still some aspects that are unclear or contradictory in the literature regarding SSMP viscometer [[22](#page-21-18)[–24\]](#page-21-19). Nonetheless, there has been limited information available in the literature on the SSMP viscometer.

This review article aims to provide a brief description of the SSMP's viscosity behaviour and various viscosity measurement methods. Factors infuencing the viscosity and rheo/thixo methods of SSMP are also discussed. In particular, it provides an

insight on its viscosity measurement methods followed by a discussion on limitations. Overall, the review will be useful for new researchers in selecting the best from the existing viscometer or designing a new viscometer with desirable characteristics.

2 Characterization of SSMP

SSMP is the formation of a non-dendritic shape microstructure using mechanical agitation of solidifying metals within the solid–liquid temperature range. The dendritic shape is a typical microstructure in the casting process, whereas advanced globular grains in the liquid matrix are predominant microstructures in the SSMP [\[25\]](#page-21-20). Many researchers have described algorithms for the dendritic to globular morphology [\[26](#page-21-21)[–29](#page-21-22)]. Non-dendritic spherical morphology is vital for a better understanding of SSMP. The microstructure of thixotropic behaviour of semisolid aluminium–silicon alloy is shown in Fig. [1.](#page-1-0)

The non-dendritic nature of the solid phase gives exclusive rheological properties to the metal slurries. Metal slurry with a solid phase of up to 50% would fow homogeneously with an efective viscosity that is greater than liquid alloy. As metal emulsions are formed into parts, the higher viscosity would lead to less turbulent mould flling, producing high-quality parts by minimizing the entrapment of air and particles [\[31\]](#page-21-23). The semisolid state in general consists of both the liquid and solid-state where non-dendritic solid particles are scattered in the liquid matrix and becomes liquid due to the instantaneous drop in viscosity. Semi-solid billets produced in the rheo casting process can remain in a solid state and can be easily cut with an ordinary knife when the shear force is applied, as shown in Fig. [2.](#page-1-1)

Fig. 2 Photo sequence illustrating the billets sliced by an ordinary knife [\[31\]](#page-21-23)

SSMP is consistent with the thixotropic behaviour of alloys with non-dendritic microstructure [\[32\]](#page-21-25). Due to its microscopic structure in SSMP, it contains solid spheroids in a liquid matrix. The viscosity depends on the time and shear rate so that if sheared, it flows, and if it is permissible to stand, it thickens again. This activity contributes to laminar rather than turbulent die flling. Besides, it avoids defects such as porosity, and improves mechanical properties. Therefore, several researchers are interested in examining the microstructure of SSM [\[33](#page-21-26)[–36\]](#page-22-0). The viscosity of SSM emulsions depends on the process parameters and the metallurgical properties of the alloy [\[37](#page-22-1)]. Several study results suggest that temperature and applied shear strength, solid fraction and its morphology, dendritic or spherical and solid particle size, and distribution are important parameters afecting the viscosity of a semi-solid billet [\[38–](#page-22-2)[40](#page-22-3)]. SSMP alloys have undergone several changes over the past fve decades. Nevertheless, despite the intense competition of traditional casting and, in particular, die-casting processes, and the emergence of additive manufacturing (AM), there seems to be a resurgence in core technology [\[41\]](#page-22-4). The following provides a detailed overview of the rheology of SSM and its process evolution, as well as a more recent development, an indication for future prospects.

3 Viscosity

Viscosity is a direct measurement of the internal friction of fuid during SSMP. The viscosity and fow behaviour of SSMP is an important characteristic of fller capacity in the casting process. It leads to the kinetic performance required for the design and material deformation. The viscosity is considered in terms of microstructural evaluation [[42](#page-22-5)]. Many researchers have reported that pressure, molecular weight, shear rate, temperature pouring time, and holding time infuence the viscosity behaviour [[37,](#page-22-1) [43](#page-22-6)]. Newton's law of viscosity defnes the relationship between shear stress and the shear rate of fuid under mechanical stress. The ratio of shear stress to shear rate is constant for a given temperature and pressure and is defined as the coefficient of viscosity. The viscosity diagram based on the shear stress and shear rate is shown in Fig. [3](#page-2-0). In an SSMP, the fluid continues to flow only

Fig. 3 Illustration diagrams for viscosity in terms of shear stress and shear rate [[46](#page-22-17)]

as long as the shear stress and shear ratio are applied over the SSM fuid [[44\]](#page-22-7). The SSMP viscosity varies greatly depending on the shear rate and the slight temperature change [\[45](#page-22-8)].

Molten liquids and liquid metals should flow better into the die cavity during the casting process. The viscosity of the SSMP depends on the effects of the flow process, especially on the squeeze casting and thixotropic processes [\[47](#page-22-9)]. In the very short-term behaviour of SSMP, the cooling rate and internal and external variables affect the flow behaviour of semi-solid emulsions. Nevertheless, during the SSMP, it is possible to create better products by accurately predicting the defned fow behaviour, pressure, temperature, shear rate, and time of the SSM emulsion. Therefore, viscosity calculation is signifcant in the casting process.

3.1 Effect of pressure on viscosity

As the pressure increases, the distance between the atoms in the material decreases and, thus, the viscosity of the liquid is increased. Moreover, casting under pressure will improve the excellent metallurgical quality of the matrix alloys. Pressure loss is the cause of the cessation of mould flling during the fow of semi-solid emulsion. Therefore, pressure is very important for mould flling capacity in casting processes [\[48](#page-22-10)]. The viscosity of liquids other than water increases exponentially with isotropic pressure, and the viscosity decreases frst before further increasing rapidly. The importance of viscosity and pressure is evident when using the high/low pressure die casting process [\[49](#page-22-11)].

3.2 Effect of temperature on viscosity

Temperature and thermal conductivity greatly afect the viscosity and microstructure of SSMP [\[39](#page-22-12)]. On the other hand, the viscosity of the SSMP decreases as the temperature increases [\[22](#page-21-18)]. Temperature gives the activation energy to the molecules of the material that causes them to move [\[50](#page-22-13)]. This movement only occurs when the liquid molecules pass each other. The ease of fow depends on the attractive force between molecular chains and molecules. In SSMP, it is necessary to maintain a constant temperature throughout the process [\[51](#page-22-14)].

3.3 Effect of shear rate on viscosity

The shear rate is an important behaviour of the flow process, the rate at which the fuid is sheared or worked during fow. High viscosity fuids can stay in the same place depending on the shear rate, while low viscosity fuids can spread quickly. Many researchers [[52–](#page-22-15)[54\]](#page-22-16) have explained that the viscosity of a fuid can signifcantly afect the viscosity of SSMP based on the shear rate. Figure [4](#page-3-0) shows the most common types of fluid flow curves.

Fig. 4 Typical fow curve for (**a**) shear stress versus shear rate and (**b**) viscosity versus shear rates [\[55\]](#page-22-25)

The behaviour of the fluids and the effect of viscosity on the shear rate are illustrated in Table [1](#page-3-1). According to several reviews and articles based on the shear rate for rheological studies of materials [\[56](#page-22-18)[–58](#page-22-19)], fuids with Newtonian behaviour behave at a certain shear rate, when the viscosity of the fuid is constant. But collisions between small molecules or atoms scatter the particle energy as the shear rate changes in other behaviour fuids. Similarly, when the shear stress of Newtonian fuids is high, they may become non-Newtonian. If the relationship between the shear rate and the shear stress is non-linear, then the fuid may be non-Newtonian. In a semisolid metal processing system with a non-dendritic microstructure, the viscosity varies based on the shear-thinning or thickening behaviour. Increasing the shear rate and coupled with the material's deformation causes the SSMP's viscosity to decrease involving.

3.4 Effect of time on viscosity

Viscoelastic materials are naturally time-dependent, and the rheological properties difer while examining them at diferent frequencies and shear rates [[59\]](#page-22-20). In a thixotropic process, the viscosity of SSM fuid decreases with time at a constant shear rate. It takes a long time to reach a constant viscosity value due to the changes in shear rate due to thixotropy, and the sample always achieves the same equilibrium value [\[16](#page-21-13)].

Rheopexy behaves contrary to thixotropy, increasing viscosity with respect to time, not reaching equilibrium viscosity [[60\]](#page-22-21). The time-dependent shear rate and viscosity changes are shown in Fig. [5](#page-4-0).

4 Viscosity measurements methods

Rheometry is used to determine rheological parameters. One of the essential parameters in rheometry is the viscosity measurement of fuids. In particular, the viscosity of any fuid is determined by its fow behaviour. A study of the rheological behaviour of SSM reveals the need for viscosity and viscometer [\[61](#page-22-22)]. Many viscometers are in use to measure dynamic shear viscosity or viscosity based on the material, measurement method, measuring instruments and sources of measure-ment errors [[62](#page-22-23)]. The most common techniques used to calculate the viscosity of SSMP are the capillary method, oscillating method, a falling body, draining vessel method, oscillating levitated drop method, concentric cylinder method, cone and plate method, parallel plate rotary method, and parallel plate compression method [\[63\]](#page-22-24). The description of the classifcation is given in Fig. [6.](#page-4-1) Viscometers are classifed according to the behaviour, properties, and application method. The following of this review describes the types, measurement methods, features, and limitations of a viscometer.

Fig. 5 Schematic diagram showing the viscosity of the thixotropic behaviour of semi-solid emulsions with time and shear rate [[60](#page-22-21)]

4.1 Capillary method

The capillary viscometer is known as the best viscometer for measuring the viscosity of Newtonian fuids. Nevertheless, SSM and non-Newtonian fuid viscosity can be measured by adjusting the shear rates within two minutes [[19,](#page-21-16) [20](#page-21-27)]. Viscosity is measured in terms of the time it takes for the fuid to exit through the capillary tube under pressure applied on a given amount of SSM [[64\]](#page-22-26). To calculate the viscosity of the capillary tube viscometer, the fow rate, pressure drop, radius of the capillary and the length and shear rate of the capillary, and shear stress must be considered. The capillary viscometer measures the viscosity based on the Hagen Poiseuille equation as in Eq. [\(1](#page-4-2)) as follows.

where P is the pressure drop along the length of the capillary in Pa, *R* is the radius of the tube in m. *L* is the length of the capillary in m; Q is the flow rate m³/s through the tube. This is related to the pressure drop in the capillary tube and the shear viscosity of the fuid to tested at low rates.

The capillary viscometer for SSMP is a single-point system used to calculate viscosity by measuring the fow rate and pressure diference of SSM fuids between two terminals, as shown in Fig. [7](#page-5-0). It is directly proportional to the capillary pressure drop in the capillary tube and inversely proportional to the flow rate. Equal focus on both fuid entry and outfow and the length, diameter, and design of the capillary are taken into account to reduce the kinetic energy efect, and the design and construction of the capillary should also clearly illustrate the jet formation or surface tension that occurs during exit $[65]$ $[65]$ $[65]$. It is better to use a capillary viscometer with diferent capabilities depending on the SSM measurement methods. A capillary viscometer with diferent designs and pressure capabilities is required to suit the SSMP of rheo and thixo routes.

In rheo method viscosity measurements, a device that refects the amount of fuid in a pressure vessel is required. Moreover, the fluid pressure and temperature must be measured before the fuid enters the capillary tube [[66\]](#page-22-28). The most tedious techniques are to accurately measure the amount of SSM fuid placed in a pressure vessel and to record the amount of fuid discharged during the process. For diferent SSM and non-Newtonian fuid measurements, adjusting the pressure using tubes with diferent diameters is the operating range. The data from the density and

Fig. 7 Schematic diagram of capillary viscometer for the (**a**) rheo route method [\[18\]](#page-21-15) and (**b**) Thixo route method [\[24\]](#page-21-19)

 (a)

viscosity study of SSM fuids, the measured pressure, tubes of known diameter, and the volume of the fuid fowing through the pipe at a given time will help to understand the problems involved in designing a new viscometer [\[67](#page-22-29)]. The capillary tube must be longer to obtain a stable laminar low regime. End efects may lead to incorrect results when the ratio of length to the inside diameter of the capillary tube is low. It has been predicted that when the ratio between length and radius is greater than sixty-fve, the entrance efect due to sudden constriction of the fuid streamlines are negligible [[19](#page-21-16)]. Although increasing the applied pressure increases viscosity and measured relaxation time, studies have shown there is no relaxation time [\[54\]](#page-22-16). The kinetic energy at the capillary inlet leads to a drop in pressure [\[68\]](#page-22-30).

Capillary viscometers are very useful for measuring the viscosity of SSMP, but there are some drawbacks in their use. During the dynamic viscosity calculation of SSM, it is not advisable to use similar metals as capillary bodies owing to the high melting point, pressure, and volumetric flow of metals and alloys. In a study related to SSMP pouring temperature and holding temperature efects, aluminium alloys are often set at the temperature range of about 1200 ℃ [\[69\]](#page-22-31). Nevertheless, Pb, Bi, Zn, Cd, Sb, Ga, In, Sn, Cu, and Ag are successfully measured to 1100 \degree C with a percentage of accuracy \pm 0.5. Depending on the high temperature, high shear stress, and density of diferent fuids, changes in the size of the capillary tubes are required. This is closer to the accuracy processing condition than the rotary viscometer. In SSMP viscosity measurement, a major error can occur due to losses and end edge efects. Features of capillary viscometers are presented in Table [2.](#page-5-1)

4.2 Oscillating‑type method

The oscillating-type viscometer can be classifed into two types: oscillating vessel viscometer and oscillating body or plate viscometer [\[70](#page-22-32)].

4.2.1 Oscillating vessel method

Oscillating vessel viscometer is commonly used for liquids and liquid metals viscosity and density measurements [\[71](#page-22-33)]. It is ideal for measuring the low viscosity of SSM alloys such as Al-Cu and Al-Cu-Si [\[11\]](#page-21-28). The viscosity of SSMP is calculated based on the frequency and duration of the oscillating vessel. It is better than a capillary viscometer in measuring low viscosity more accurately and easily.

A schematic diagram and photo view of the oscillating viscometer is shown in Fig. [8](#page-6-0). A is the oscillating initiator it is connected with the suspension wire, B is the He–Ne laser and photodetectors placed on a vibration-free table, C is the furnace, D is the thermocouple, it is used to measure the temperature, E is the temperature controller for the furnace, F is the inert gas intake, G is the vacuum system, H is the vibration-free table, I is the inertial disc and mirror, J is the quartz window for the laser beam, K is the layout of the electronic instruments including a timer interval counter, multimeter, computer for data acquisition, and control, and L is the schematic diagram.

The samples were placed on a cylindrical aluminium crucible and covered with a molybdenum lid. Molybdenum screwed to a suspension rod, which is suspended through a length torsion wire. Torsion wire is connected with a rotary solenoid to initiate oscillations, and suspension wire is set to sink inside the water. The laser beam is mounted directly on the flat mirror located on the suspension wire. The torque system, which is set to oscillate around its vertical axis, will occur with the gradual humidity of the vessel's motion [[74](#page-23-2)]. The continuous oscillation of the vessel is measured with the help of a light source attached to the suspension wire (Fig. [8](#page-6-0)). The angular displacement and oscillating time of the vessel holding the viscosity measuring fluid should be measured. The motion of the oscillation vessel is calculated by the solution of the second-order differential equation presented in Eq. [\(2\)](#page-6-1).

$$
I_0 = \left(\frac{d^2\theta}{dt^2}\right) + \mathcal{L}\left(\frac{d\theta}{dt} + f\theta\right) = 0\tag{2}
$$

When I_0 is the moment of inertia of the oscillating vessel, *t* is the absolute time, *L* is the function of the density and viscosity of the sample of fuids, and *f* is the constant force of the torsional wire, Roscoe analysis [[75](#page-23-3)] viscosity equation is presented in Eq. ([3\)](#page-6-2),

$$
\eta = \left(\frac{I_0 \delta}{\pi R^3 H Z}\right)^2 \frac{1}{\pi \rho T} \tag{3}
$$

where η is the viscosity, δ is the logarithmic decrement, *R* is the inner vessel radius, *H* is the sample height in the vessel, ρ is the density of the sample, and T is the oscillation period.

In the study of Beckwith and Newell research, the numerical error is smaller than the Roscoe analysis, and the diference in viscosity value is less than 0.5%, so this error is measured by ignoring the test error. Moreover, the shape, dimensions, symmetrical design, and high oscillation frequency are considered signifcant [[76](#page-23-4)]. The efect of surrounding air resistance may afect the measurement. To precisely determine the viscosity of the SSM process, the oscillating cup is heated by the electromagnet through the tube of the heating furnace. The temperature gradient of the sample is controlled by changing the temperature of heating furnaces. Nevertheless, the sample still has a temperature gradient. Therefore, the insulating layer of the

Torsion wire

Fig. 8 Oscillating vessel viscometer with (**a**) photo view [[72](#page-22-34)] and (**b**) schematic diagram [[73](#page-22-35)]

thermal insulation layer outside the heating device can be increased to reduce the temperature gradient. Studies show that as the thickness of the insulating layer increases by more than 10 mm, the temperature gradient decreases [\[77](#page-23-5)].

When measuring the viscosity of Zn-Al alloys with an oscillating cup viscometer, uncertainty appears to be between 3 and 5%. A more sophisticated viscometer must be developed for alloys with diferent alloys and at diferent temperature ranges [\[72\]](#page-22-34). The temperature and concentration dependencies of the viscosity for liquid Cu-In-Sn alloys with a liquid state have inherent microscopic parts with a short distance range. The viscosity of low viscosity liquid Cu-In-Sn alloys obtained at high-temperature dependencies up to 800 ℃ was successfully measured using the oscillating shipping method [[78\]](#page-23-0). In 2001, Brooks et al. [[79\]](#page-23-6) reconstructed oscillating viscometer to calculate the decrement of logarithmic and the period of the oscillations by using multiple diode arrays to the decaying waveform. It has been upgraded to measure the viscosity of high melting point materials with maximum temperature capacities ranging from 1200 to 1650 ℃ [[79](#page-23-6)]. It is known that this viscometer can be upgraded to a wide range of temperatures with a radius error of less than 0.5%. Furthermore, the main advantages of this device are the relatively small size of the model, the good consistency of the temperature feld, and the fully automatic calibration system.

4.2.2 Oscillating vessel or plate method

It is also an oscillating vessel–type viscometer, but the plate or body is completely immersed in the liquid, as shown in Fig. [9.](#page-7-0) Viscosity is calculated based on the displacement and oscillation time of the vessel or plate. The calculation methods are the same for both.

This system also measures the amplitude of the oscillation as a function of time. The oscillations are formed

Fig. 9 Diagram of an oscillating body/plate viscometer [\[18\]](#page-21-15)

according to the total humidity experienced by all parts of the suspended system [\[80](#page-23-7)]. The oscillations and frequency patterns vary due to plate/body oscillations on the free surface depending on the operating conditions. Moreover, the natural frequency of each vibration mode is in excellent agreement with the predictions obtained by splashing theory in the case of stationary liquids [\[81](#page-23-8)]. Although oscillatingtype viscometers are suitable for measuring low viscosity, rapid measurement, and easy cleaning and maintenance of the device, the lack of standard instruments can cause measurement problems. Especially in liquids of varying viscosity, it has a measurement error of $\langle 2\%,$ but for metals, up to 30% of the measurement error is associated with high temperatures. There appear to be some issues in the equation and accurate measurements of the vessel as the vessel or plate size increases. Therefore, errors related to the viscosity and density of the fuid, various cup or plate shapes, sizes, and the frequency of oscillations need to be studied [[76](#page-23-4)]. It is essential to moisten the cylinder wall with the liquid that is tested for accurate results. Sometimes, slippage between the liquid wall interface and errors can occur due to the low humidity of the viscous forces [[82\]](#page-23-9).

4.2.3 Falling ball method

In a falling ball or counterbalanced viscometer, the ball is placed into the liquid as if it were in an oscillating body/plate type. This method designed for liquid metals by considering the time taken to pull a ball from liquids at a constant force. Calibration to the standard reference of viscosity and sample density is essential to obtain viscosity values [\[83](#page-23-1)].

 The sample ball is mounted on a cylinder containing fuid kept at a constant temperature. The loading pin should be released, and the ball brought to the starting position. The distance the ball passes at the specifed time is outlined. A stainless steel spherical ball attached via a platinum–rhodium wire is lifted from the SSM fuid at a very slow speed by the opposite weight motion [\[84\]](#page-23-10), which is represented in Fig. [10.](#page-8-0) High temperature and low viscosity fuids such as Fe and FeS were successfully measured by ultrafast synchrotron X-ray imaging using the advanced falling ball viscosity measure-ment [\[85\]](#page-23-11). A wide viscosity measurement range of 10^{-3} to $10⁷$ Pa s is determined. Although it is suitable for measuring materials with diferent temperatures and pressures, there are some difficulties in measuring viscoelastic fluids. The shearing stress caused by the strain on the structure in the semisolid state is continuous and must be recorded. The results of a study by Jo et al. [[86](#page-23-12)] show that the speed of a falling sphere in a fuid can be monitored and accurately measured using two linear image sensors and by graphically mapping the terminal speed to facilitate its subsequent processing. The main disadvantage of the falling ball requires a certain distance to reach the free-falling. Also, the thermal expansion

Fig. 10 Schematic diagram of (**a**) counterbalanced viscometer and (**b**) falling ball weight and velocity diagram [\[18\]](#page-21-15)

of the falling ball at a high temperature is another drawback. Moreover, high shear devices are intensive, more expensive, and need a skilled worker [[87\]](#page-23-13).

4.2.4 Oscillating levitation method

The oscillating levitation method is used to avoid container wall from being damaged by the sample when measuring viscosity, surface tension, pressure, and thermal-depended properties. It is called the "container-free" method. One of the three diferent processes, electromagnetic, electrostatic, and aerodynamic, is used to heat the material in the levitation technique [[88\]](#page-23-14). Melting and solidifying a levitated sample during container-free measuring process avoids contact with a container. The frequency induced by an electromagnetic levitator is fve times greater than the surface oscillation. As shown in Fig. [11,](#page-8-1) the high-speed camera records frequencies radially mounted perpendicular to the coil axis. Sample temperature is monitored by a pyrometer [[89\]](#page-23-15).

Microgravity and viscosity tests are often performed using frequency oscillations and scattering of oscillations. The frequency of the surface oscillations of fuid is based on the assumption that the surface tension relates to Rayleigh's

formula, but it must be adjusted for solids and SSM [[90\]](#page-23-16). For example, many problems arise when the viscosity of molten molybdenum, tantalum, osmium, rhenium, and tungsten is measured with the advanced process by the oscillating drop levitated method. Surface tensions of these metals must be evaluated due to the diference in the density of the fuids and the impact of the sample mass and droplets, the frequency of high-density metals, the effect of possible contamination, and the temperature dependence viscosity. The last concern is the efect of positioning the force on the latter measurement. Although the improved process minimizes the efect, the levitated model is not free from external forces.

Fig. 11 Diagram of oscillating levitated viscometer [[91](#page-23-17)]

The density, surface tension, and viscosity of liquid oxides such as Al_2O_3 accurately are measured by a laser-heated aerodynamic levitation system. Although the current system works well, determining viscosity, high precision data, and high melting for liquid oxide properties has drawbacks inherent to the current technique [\[92](#page-23-18)]. The Wunderlich and Mohr literature predicts that the viscosity of viscous fuids from 7.4 to 15 mPa can be calculated with an initial sample decay of 5 to 10% in the 220 K temperature range [\[93](#page-23-19)]. This measurement method works best on the properties of laser melting droplets to calculate the surface tension and viscosity of metals reinforced by nanoparticles [\[94](#page-23-20)]. Surface tension is considered essential for measurements [\[95\]](#page-23-21). Figure [12](#page-9-0) represents the oscillating types of viscometers and their features.

4.3 Draining vessel method

The fluid flows through a hole at the bottom under the effects of gravity, including surface tension efects, density, and viscosity. Viscosity is measured by the time taken for the sample volume and the amount of fuid exiting through a hole [[18\]](#page-21-15). Molten aluminium is mostly measured by this technique [\[96\]](#page-23-22), as shown in Fig. [13](#page-10-0) where the viscosity is calculated by using Eq. ([4\)](#page-9-1).

$$
\eta = \frac{2a\rho r_o Q_{exp}}{\left[\left(\frac{Q_{exp}}{\sqrt{2g(h_{exp} - \frac{\sigma}{\rho gr_o})}}\right) - \pi r_o^2 b\right]}
$$
(4)

where η is the viscosity(Nsm⁻²), *a* is the polynomial constant that describes the slope of the discharge coefficient curve (no units), *b* is the polynomial constant that describes the y-intercept of the discharge coefficient curve (no units), ρ is the density (kg/m³), *r* is the orifice radius, *Q* is the volumetric flow rate of the experiment (m^3/s) , *h* is the experimental liquid head above a point of reference (m), *g* is the gravitational constant (m/s²), and σ is the surface tension of a liquid (N/m).

The induction coil is used in this technique, and the induction coil is turned off and tested after the sample has melted. The electromagnetic forces generated from the induction coil create loops into the melting point, usually ignored in calculations. The temperature change of the measured fuid afects the viscosity [\[96\]](#page-23-22). Despite the advantages,

Fig. 12 Types of oscillating viscometer and its features

Fig. 13 Diagram of draining vessel viscometer [\[18\]](#page-21-15)

such as the simplicity of the design and the absence of moving elements, surface tension and normal pressure are the main problems [[97](#page-23-23)].

4.4 Rotary method

The rotary viscometer is widely used to study the rheological properties of non-Newtonian fuids [\[98](#page-23-24)]. In low viscosity liquid metals, such as SSMP, there must be a uniform and constant shear rate in the melt to calculate the viscosity parameters. The rotational viscometer involves holding the fuid in a container or over a plate and rotating the area to measure the shear stress produced [[99\]](#page-23-25). They are classifed into concentric cylinder (coaxial cylinder) method, cone and plate rotary method, and parallel plate rotary method. The main physical characteristics of the rotational viscometer must be calculated before the viscosity measurements are computed to determine the marginal efect of the container and bob systems. The fuids of the SSM process, which exhibit normal pressure efects, generate pressure in the direction of fuid movement as the pop and plate rotate on the viscometer. Thus, turbulent vortices occur at higher rotational speeds due to higher fow rates.

4.4.1 Concentric cylinder method

It consists of two concentric cylinders with diferent diameters. The outer cylinder cup and inner cylinder pop are located in the same centre to rotate the cup or pop. The fuid's torque and shear rate are measured in angular defection with a torque gauge setup on the pop. Concentration cylinder measurement systems require relatively large sample volumes [\[100\]](#page-23-26). Working with SSM fuids and cylindrical suspensions in coaxial cylinder systems, low viscosity makes them more sensitive to large areas, so they produce better data with lower shear rates and viscosity. The resulting angular velocity of a given torque is calculated from the conformational curves of the SSMP fuid viscosity values. Based on the experimental study results, there are issues such as end effects, wall slip, inertia and secondary flows, viscous heat efects, eccentricities, and the need for space between cylinders [[101,](#page-23-27) [102\]](#page-23-28).

4.4.1.1 Searle‑type viscometer In the Searle-type viscometer, the outer cylinder (cup) is fxed, and the inner cylinder (bop) is set to rotate, for example, Stormer viscometer and Brookfeld viscometer [\[103](#page-23-29)]. The inner cylinder (bop) of the Searle-type viscometer is connected to a torque measuring unit, and pop are separated from the torque measuring unit through a steel tube, as shown in Fig. [14](#page-11-0) [[104\]](#page-23-30). The electric heating furnace is used to provide a constant temperature. The temperature is controlled by using thermocouples embedded in diferent places inside the body of the machine. The viscosity is calculated by using Eq. [\(5](#page-10-1)) as follows.

$$
\eta = \frac{T}{4\pi LN} \left(\frac{1}{r_i^2} - \frac{1}{r_o^2} \right)
$$
 (5)

where T is the measured torque, L is the liquid altitude inside the cylinder, *N* the angular speed of the rotor, *η* is the viscosity, r_i is the inner cylinder radius, and r_o is the outer cylinder. According to Hirrari et al. [[106\]](#page-23-31), semi-solid alloys using this method provide excellent results on the efects of the rheological compounds of the solid, the cooling rate, and the shear rate on the SSM liquid viscosity. It can be geometrically expressed in terms of the fow behaviour of a fuid.

In a Searle-type viscometer, the rapidly rotating fuid moves outward near the inner cylinder, causing the "Tailor vortices" in the fuids due to barriers between the cylinders. Hence, the flow becomes turbulent due to the increasing rotational speed. Also, fow is turbulent due to the high temperature, shear stress, the variation of dynamic viscosity coefficients, and different grades of steel and alloy oxidation compounds. In the Searle-type viscometer, it is advantageous to use a pop of zirconium and alumina compounds to measure the viscosity of steel and alloy [\[107\]](#page-23-32). The rheological behaviour of the pseudoplastic and thixotropic properties of alloy A 201 has been studied using a Searletype viscometer $[101]$ $[101]$. The steady-state flow curve with the shear rate of 60 to 260 s^{-1} has been estimated in the analysed shear rate range. Moreover, the power-law indexes were 35% and 45% for a fraction of solid 1.35 and 1.49, respectively.

Searle type is a high sensitivity viscometer that is generally suitable for low shear rates. The fow curves of plastic, pseudoplastic and dilatants difer in diferent dimensions

Fig. 14 Searle-type viscometer of (**a**) Schematic drawing [[105\]](#page-23-36) and (**b**) Rotational view [\[37\]](#page-22-1)

of the inner and outer cylinders and rotational speed [\[108](#page-23-33)]. Nevertheless, Searle-type viscometer curves are more accentuated. Searle-type viscometer flows wider thixotropic loops. In measuring the viscosity of this type of viscometer, it is essential to note the high Taylor vortex formation in SSM fuids. Taylor loops dissipate energy and cause an increase in torque measurements.

4.4.1.2 Couette-type viscometer The Couette-type viscometer, developed by Corey in the 1970s, also excels at measuring the rheological properties of SSM fuids [\[109](#page-23-34)]. It is slightly diferent from the Searle-type viscometer. The pop is fxed and designed to rotate the cup, and the inner cylinder is connected to a torque measuring unit, as shown in Fig. [15](#page-11-1), for example, Macmichael viscometer. Both cup and the bob are made up of stainless steel, the cup and bob surfaces are precisely shaped, and the spacing between the two surfaces must be equal at all points, or the fuid rise in the cylinder is signifcantly asymmetric. The centre of the cylinder is set to be symmetrical, and the height of a given radius of fuid is averagely recorded. Due to the precise construction of the instrument, the SSM fuid viscosity values are closely detected [\[110](#page-23-35)]. This method proposed for higher shear rate measurements, which means shear rates above

 $100,000 \text{ s}^{-1}$. The Couette-type viscometer method allows the smallest angular velocities to measure the large viscosity (ca 10^{11} Pa s). In the Berberian study, small angles can be measured over a long period of time at temperatures as low as 105 to 123 K, 3.2×10^{11} Pa s [\[111](#page-23-37)].

This method helps measure shear thin and time-dependent behavioural materials. In time-dependent measuring, fow characteristics and shear rates may change rapidly, so it is best to use automatic control and recorded systems. Although this method is used in a Newtonian or non-Newtonian fuid, Gücüyener et al. [\[113\]](#page-24-1) strongly recommend non-Newtonian behaviour. Still, errors associated with the severity of the end effects are more common at higher shear rates, and therefore they should be corrected [[113\]](#page-24-1). Other methods for assessing viscosity are challenging to viscosity measurement due to the efects of oxidation and pollution. Therefore, the Couette-type rotating viscometer is ideal for measuring the viscosity of high-temperature and high shear fuids [[114\]](#page-24-2). Studies by Wunderlich and Brunn [[115](#page-24-3)] show that the shear rate contributes signifcantly to the viscosity measurement of the Couette-type viscometer and that there is a limit to the apparent shear viscosity by determining the gap and width in the surfactant sample [[115](#page-24-3)]. The cooling shaft can be installed in a temperature control bath for a rotating cup type to control the temperature. The coefficient value of the dynamic viscosity of the SSM fuid during SSMP can be accurately measured in terms of shear rate and time. But the yield values are diferent from the Searletype viscometer.

4.4.1.3 Vane viscometer The vane is set in the centre of the cylinder to be completely immersed in the liquid as shown in Fig. [16.](#page-12-0) The vane rotates at a constant speed and is usually

operated in rate control mode. The torque produced by the SSM fuid is measured by a torque measuring unit set with the vane [\[116](#page-24-4)]. During the vane rotation, the SSM fuid that rotates between the cylinder and the vane acts as another body, which gives the yielding surface equivalent to the cylindrical surface of the vane; this cylindrical body is called a rigid cylinder so that no secondary flow occurs between the blades. To measure the SSM fuid's viscosity, the mechanical force, resistance, time, and associated shear pressure exerted by the rotation of the vane must be calculated. Vane-type pops can lead the secondary flows; this can affect the torque measurements. Grooved bob is used to prevent slip and reduce torque [\[117\]](#page-24-5).

Vane-type viscometer measures the fow characteristics of the non-Newtonian fuids and low strain modulus and shear state. Its simplicity of fiction, ease of cleaning, and elimination of outer wall slippery efects are specifc advantages of a vane-type viscometer [[119\]](#page-24-6). The discussion on the comparison of concentrated cylinder viscometers is shown in Table [3](#page-13-0).

4.4.2 Cone and plate method

The sensitivity of the rotational resistance of the sample fuid placed between a fxed plate and the rotating cone is measured by the accurate torque meter attached to the cone, as shown in Fig. [17](#page-13-1) with the calculation for viscosity is presented in Eq. (6) (6) .

$$
\eta = \frac{3T\theta COS^2\theta \left(1 - \theta^2/2\right)}{2\pi\omega r^3} \tag{6}
$$

where η is the viscosity(pas), θ is the cone angle (rad), *T* is the torque, *ω* is the angular velocity (rad/s), and *r* is the radius of the cone(m).

Searle-type viscometer	Couette-type viscometer	Vane-type viscometer
• Cup is stationary, but bob rotates •Low shear rate and high-temperature materials •It is necessary to produce a transparent quartz- based outer cylinder to observe the Taylor vortices in molten metals \bullet More sensitive •Alignment setting is challenging	\bullet Cup is rotating, but bob is stationary • High shear rate and high-temperature materials •Cleaning is difficult • Most suitable for shear-thinning time depended on fluids • Causing error to occur in misalignment settings	• Cup is stationary, but the vane rotates • The simplicity of fiction •Ease of cleaning • Elimination of extreme wall slippery effects • Mostly suitable for non-Newtonian fluids • Vane-type pops can affect torque measurements and lead to secondary flows

Table 3 Concentric cylinder viscometers comparative analysis

Low viscosity liquids measured ranging from 1 to 50,000 poizes, and the shear rate ranged from 0.0002 to 9000 s^{-1} [\[121\]](#page-24-8). Since the strain and shear rate are calculated using angular displacement and spacing, the larger the error may be in the spacing system when the smaller cone angle. Depending on which cone angle to use, the shear rate variations against the spacing can be corrected compared to the propagation of the interval. Newtonian fuid in a cone and plate flow, the shear rate for a spontaneously wide spacing is close to the cone, and when the cone angle approaches $p=2$, the viscometer spacing becomes very narrow. The fuid rarely discharges from the shear stress, so the viscosity of the Newtonian fuid is measured by controlling the fuid in the space between the cone that rotates perpendicular to the stationary disc [[122\]](#page-24-9). Noori et al. [[123](#page-24-10)] explained that the viscosity of a cone and plate could be used to accurately measure the viscosity of liquid metals with very small particles. This method is practically feasible for determining zero shear viscosity. However, the particle in the test sample should be fve to ten times smaller than the gap in the cone. If the particles are large, the particles may stick to the cone's surface, resulting in noise and afecting the measurement. Substances with higher solids are more likely to be discharged from the interval under higher shear rates. Therefore, due to this limitation, the cone and plate method is seldom being used [\[124](#page-24-11)].

4.4.3 Parallel plate rotational method

Mooney viscometer consists of two parallel circular plates, the lower plate is stationary, and the upper plate is rotating, as shown in Fig. [18](#page-14-0). A parallel plate rotary viscometer is

Fig. 17 Cone and plate viscometer with (**a**) general view [[112](#page-24-0)] and (**b**) inner view [\[120](#page-24-12)]

Fig. 18 Parallel pate rotational viscometer with (**a**) photo view and (**b**) constructional view of disc and plate

used to measure the viscosity of liquid metals, aluminium alloys, and composites. Because it is used with a separation between plates, it is not as sensitive to the gap setting and is therefore suitable for testing samples with a temperature gradient. Thick materials and non-uniform particles cannot be measured using a cone and plate viscometer [\[125](#page-24-13)]. Random particles of diferent shapes of molten metal can be easily measured with a parallel plate rotational viscometer. This can be used to predict a wide range of viscosity from softening to melting.

The main disadvantage of parallel plates rotary viscometer is that the shear rate and the data output vary greatly with the temperature variation of the sample $[126]$ $[126]$ $[126]$. The sample is likely to shrink during the test. Furthermore, the torque produced varies according to the quantity of the sample, thus affecting the viscosity value $[127]$. Table [4](#page-14-1) provides a comparison of cone and plate viscometer and parallel plate rotary viscometer.

4.5 Sliding plate method

Sliding plate viscometers are generally considered to be the best way to evaluate the viscosity of fne-grained materials. The sliding plate–shaped viscometer consists of two fat parallel plates. The lower plate is stationary, and the upper plate creates a controlled deformation of the shear rate by moving at a constant speed. At the same time, a load cell is used to measure the total shear force. It is used to create a constant shear force using the weight suspended from a pulley. It is necessary to apply a uniform temperature and pressure to the fuid. Furthermore, the moving plate is set to move at the close with the fuid at a minimum gap so that the frictional force and shear stress associated with it is measured while moving, as represented in Fig. [19.](#page-15-0) Multiple sources of error can be found by changing the interval; explicit shear stress decreases when gaps are reduced at a constant shear rate. Furthermore, friction error can occur due to end and edge efects and surface tension. Normal stress differences cannot be determined using force measurements. There

are problems in measuring high shear rates fuids due to total strain and the maximum displacement of the sliding plate [\[128,](#page-24-16) [129](#page-24-17)]. The viscosity is calculated by using Eq. [\(7\)](#page-15-1) as follows.

$$
\eta = \frac{Fh}{AV} \tag{7}
$$

where F is the force and h is the height of the sample. A is the area of the moving plate and *V* is the velocity [[130](#page-24-18)].

4.6 Parallel plate compression method

The parallel plate compression viscometer was frst constructed and used by Laxman and Flemming [[131](#page-24-19)] to study Sn–Pb semi-solid metals. It is easier to measure viscosity for SSMP than any other viscometer. Based on this, the drop forge viscometer is designed and built by Yurko and Flemmings in 2002 to measure the viscosity of semi-solid aluminium alloy. Drop forge viscometer can be used to calculate shear rates greater than 10^3 s⁻¹ at times less than 10 ms than other viscometers. For a parallel plate viscometer, the top plate is suspended and then allowed to come under the infuence of gravity. As a result, the upper plate semi-solid sample is compressed at high speeds. The fall of the plate is measured with the help of a high-speed digital camera, and the fuid's viscosity is determined [[132\]](#page-24-20). The minimum viscosity obtained in this method depends on the maximum achieved shear rate but not the shear duration. A very rapid decrease in viscosity with increasing shear rate, in line with a relatively slow increase in viscosity with decreasing shear rate, requires some modifcations to this method of measuring viscosity. In 2006, a new parallel plate compression machine for commercial-scale was designed and tested for viscosity measurement by Lashkari and Gomashchi [[133](#page-24-21)]. The parallel plate compression viscometer consists of two parallel plates. Commonly, both plates are made from graphite, and boron nitride–coated refractory material to prevent them from sticking to the billet. Deadweight is added to the

upper plate to provide the force on the billet during compression. During the test, the controlled upper plate, with the help of pneumatic action, is released towards the lower plate under its weight. It is based on monitoring and recording the changes in test object height with time. It consists of dead weight, a pneumatic controller, guide shafts, and a resistant heating furnace. The test piece is placed between two parallel plates, and deadweight is applied to the top of the billet outside by a guided platen through two or four straight vertical axes. The billet sample is kept inside a furnace to keep its temperature constant during the compression test, as shown in Fig. [20](#page-15-2). In the parallel-plate compression viscometer, viscosity is calculated using the Stefan equation. For this, the motion and continuity equations are reduced as shown in Eqs. (8) (8) and (9) (9) .

$$
\frac{\partial P}{\partial r} = \mu \frac{\partial^2 v_r}{\partial z^2} \tag{8}
$$

$$
\frac{1}{r}\frac{\partial}{\partial r}(rv_r) + \frac{\partial v_z}{\partial z} = 0\tag{9}
$$

Dead weight

Fig. 20 Schematic diagram of the parallel plate compression viscometer [[134\]](#page-24-22)

where *p* is the pressure, *v* is the velocity, μ is the viscosity, *r*, *h*, and *z* are coordinate systems with the origin of the *z*-axis, and v_r and v_z are the velocity components of r and z directions. Equation ([10\)](#page-16-0) refers to the Stefan equation.

$$
F = \frac{-3\mu V^2}{2\pi h^5} \left(\frac{dh}{dt}\right)
$$
 (10)

where *F* is the applied force on the specimen, μ is the viscosity, *h* is the height, *v* is the specimen volume, and the compression velocity is dh/dt.

$$
m_p \left(\frac{d^2 h}{dt^2}\right) = \frac{-3\mu v^2}{2\pi h^5} \left(\frac{dh}{dt}\right)
$$
 (11)

$$
\mu = -2\pi h^5 m_p \left(g + \frac{d^2 h}{dt^2} \right) / 3v^2 \frac{dh}{dt}
$$
 (12)

The applied force is the mass of the plate multiplied by the deceleration, $m_p (d^2 h/dt^2)$. Hence, the Stefan equation balanced the applied force of viscosity experiments conducted at high and low forces as shown in Eq. ([11](#page-16-1)), from which the equation for viscosity is summarized by Eq. [\(12](#page-16-2)).

The result of the strain–time graph obtained by recording the displacement of the top platen with time is treated mathematically to calculate the viscosity of the SSM billet [\[135\]](#page-24-23). The liquid–solid temperature range on the parallelplate drop-forge viscometer is measured using an extensive displacement laser sensor of the cylinder model, which efectively analyzes the viscosity time dependence and shear rate. However, the measurement system for SSM viscosity should further improve the shear fow rate, RAM speed and billet slip. The comparison between a sliding plate viscometer and a parallel plate compression viscometer is presented in Table [5.](#page-16-3)

5 Critical analysis of viscometers

Capillary viscometer measures the viscosity based on Poiseuille's law. It is also easy to measure the viscosity of a fuid with two SSMP techniques, such as rheo and thixo routes.

Accurate measurements can be made in 2 to 3 min. Depending on the pressure and density of the fuid, the capillary tube with a diameter of 1.5, 1.0, and 0.5 mm and a length/diameter ratio of 16 mm is used on the capillary viscometer. It can be measured accurately up to 0.5% at temperatures up to 1200 °C. Capillary tubes are very small, so difficult to clean. In SSMP viscosity measurement, the effects of wall slip, wall adhesion, and wall edge illustrate major issues, such as the high melting fracture, high shear stress, and shear rate. However, capillary viscometer functionality is easy in measuring viscosity and density, and requires a small amount of sample fuid, and temperature control is simple and inexpensive. Capillary viscometers provide a direct measurement of viscosity for fow rate, pressure, and various dimensions.

The oscillating vessel viscometer measures the viscosity of rheo route fuids with a maximum temperature of 1500 °C at SSMP with an error less than 0.5% using highly sensitive industrial equipment. Furthermore, the main advantages of this device are the relatively small size of the model, the excellent stability of the temperature, and the fully automatic calibration system. Oscillating-type viscometer is suitable for low viscosity materials. It is an accurate calibration method; maintenance and cleaning are easy to compare than the capillary method. But standardized vessel or plate sizes should be determined. In measuring the viscosity of a fuid, potential errors related to the shape and size of the vessel, densities, and frequency of oscillation should be explored. The viscosity and density cannot be determined simultaneously. It is necessary to moisten the vessel or plate and cylinder wall with the liquid. Sometimes, the slippage between the fuid wall interface can cause errors due to the low humidity of viscous forces. The main concern is the lack of commercial equipment.

A falling spherical counter balanced viscometer can measure viscosity in a few seconds based on the amount of resistive viscous motion of a fluid as it rises upward from the liquid due to the opposite weight of the ball immersed throughout the stationary SSM fluid. Simple design, easy to measure fluids at high temperatures and high pressures but are not suitable for viscoelastic

Table 5 Comparative analysis of parallel plate sliding method and parallel plate compression method

Parallel plate sliding method	Parallel plate compression method
• The lower plate is fixed, the upper plate sliding over the fluid (upper plate move horizontal wise)	• The lower plate is fixed, the upper plate compresses the fluid (upper plate move vertical wise)
• Suitable for rheo routes	• Suitable for thixo routes
• Viscosity measured based on horizontal force, pressure, and velocity	• Viscosity measured based on vertical force, pressure, time
• Accurate measurement is difficult	• Accurate measurement is possible
•It can only measure the liquid with a thin particle	• Particle size is no matter
•Normal stress differences cannot be determined using force measure-	• Easy to design and set up errors are less likely to occur
ments	• Higher ram speed, high acceleration,
• Edge failure is much less	billet slipping is the main
	disadvantage

fluids. Since a certain distance is required to reach the free fall, the time associated with gravity, the weight of the falling object, and the thermal expansion of the ball at high temperatures are the main disadvantages. High shearing equipment uses accessories' parts that are intensive, maintenance is expensive, and ultra-skilled labour is required.

Viscosity is calculated by measuring the shear rate produced by holding the liquid in a container or plate and rotating that part on a rotary viscometer. Concentration cylinder methods are best suited for low viscosity fluids less than ten psi of SSMP rheo route fluids. Determining the shear stress and shear rate on a rotary viscometer is only possible if the shear gap is very short. Therefore, the spacing between the cylinders should be set to less than 0.99. For the SSMP method, direct measurements of the shear ratios are available only if the shear rate across the shear interval is constant or very high. The vane is submerged in the fluid and rotates at a constant speed, resulting in a uniform pressure distribution throughout the cylinder. Secondary flow does not occur. The main advantages of vane-type viscometers are its ease of fabrication, ease of cleaning, and the elimination of serious wall slippery effects. Table [6](#page-18-0) presents the advantages, limitations, and principles of various viscometers.

In rotary plate viscometers, the temperature of the sample is more likely to decrease, thus varying the shear rate and output of the sample. The rotational viscometer is selected depending on the particle size in the sample and the nature of the fuid. It is practically possible to determine the zero shear viscosity in a cone and plate viscometer calibration. The size of the particle material in the sample must be fve to ten times smaller than the cone diameter to avoid the resulting noise and error in measurement at higher shear rates. The small-angle can lead to errors arising, so importance is given to eccentricities and alignment settings. Figure [21](#page-20-0) briefy presents the main essences of the various viscometers.

Sliding plate viscometers are commonly used to assess the viscosity of microscopic materials. The temperature and pressure of the SSM fuid must be maintained uniformly throughout the measurement. The viscosity is measured by placing the stationary plate and the moving plate close to the fuid at minimum intervals. Furthermore, error friction is likely to occur due to gap, end and edge efects and surface tension. There are problems with measuring high shear rate fuids. The parallel plate compression method is suitable to measure the viscosity during SSMP's thixo method. In this method, the viscosity is measured accurately in vertical force, pressure, and time. Particle size is a no matter; plate settings and measurement methods are easy; thus, chances of errors are minimal.

6 Future perspective and direction for viscosity measurement

The capillary viscometer is known as the best viscometer for measuring the viscosity of Newtonian and non-Newtonian fuids for reasons such as simplicity, accuracy, and similarity to process fows as extrusion dies and no free surface. However, problems in the range of shear ratios must be solved during the viscosity measurement of non-Newtonian fuids [[136\]](#page-24-24). It is necessary to develop a viscometer that can measure the viscosity of liquids at multiple shear rates in a short period [[137\]](#page-24-25). Capillary viscometers are currently unavailable for evaluating the rheology of dispersions with shear-dependent viscosities. Especially in the viscosity measurement of molten metal at high temperature, the efects of the wall edge efect such as wall slip and wall adhesion should be noted. There are signifcant issues such as high shear stress and shear rate [[138\]](#page-24-26). It is recommended to apply a thin layer of coating on the capillary tube inside to reduce the wall effect. The length and diameter of the capillary tube must be determined during the new viscometer design, depending on the surface tension, particle size, and cooling rate of the molten metal. In case of turbulence at the capillary entrance and outlet, numerical errors may occur, thus reducing the accuracy of the evaluation process. Turbulence can be corrected by taking samples into account. Furthermore, a continuous shear rate scanning process should be performed. The capillary viscometer for semi-solid metals requires more attention [[139\]](#page-24-27).

Oscillation viscometers provide many advantages, including high precision, high sensitivity to small changes in viscosity, quick accumulation of data, and easy cleaning [[140](#page-24-28)]. However, it only works at a certain shear rate. After the measurement, any errors caused by the viscometer or measurement procedure could not be corrected, and viscosity values often give diferent test results, even for melts of pure components. Therefore, the performance of the oscillating cup viscometer should be further improved to obtain reliable viscosity data of molten metals. Difficulties in measuring high viscous fuids need to be addressed [\[141](#page-24-29)]. Emphasis is needed on accurate time measurement on the oscillating viscometer. No one pays attention to the error caused by environmental vibration and noise. A direct counter of the pulse time interval can be selected to measure the viscosity-related attention time to deal with this. Moreover, improvements are needed on the commercially oscillating viscometer.

The falling ball viscometer measures the viscosity based on the relative balance between the forces of pressure, viscosity, and gravity. The special feature of this method is that the wall does not infuence the rate of fall of the ball. However, the ball's density, diameter, and metal material

thixo process

thixo process

make a large diference in the viscosity value. Moreover, it challenging to maintain a constant temperature along the entire length of the pipe and requires a large amount of test material compared to other viscometers [\[142\]](#page-24-30). When measured in this method, the viscosity is greatly afected by the inertia, drag force, and lift force. When measuring viscosity at high-temperature conditions, the problems caused by the thermal expansion defect of the falling ball, and the distance it takes to reach the free-fall must be minimized $[143]$ $[143]$. In addition, the cost of using high shear devices and the need for a skilled worker also should be minimized.

For Newtonian fluids, the viscosity from torque and rotational speed is very easy to estimate with a rotational viscometer. Rotational rheometers for SSM are used to examine the viscosity by shearing for a certain time. Problems using a rotary viscometer for SSM fuids and completely viscous materials should be eliminated. Computational rheology should be used to evaluate the processing of data collected from a rotational rheometer. The major error in coaxial cylinder viscometers is that the end efect that arises from pulling the fuid on the ends of the bob should be corrected. Problems that arise are the shear rate and apparent viscosity, and the shear rate varies across the fuid [\[144\]](#page-24-32).

Wall slip is another phenomenon that affects rheological measurements on all types of rotary viscometers. Surface tension causes secondary forces when there is a tiny symmetry variation in the viscosity measurement system, which is more dominant at lower shear rates. As a result, the material appears to be strong in shear thinning, albeit almost Newtonian [\[145\]](#page-24-33). Vane-type bobs are not suitable as they can lead to secondary flows that affect torque measurements. However, a groove prevents the bob from slipping without significantly affecting torque [[146](#page-24-34)]. The Searle- or Couettetype viscometer has a low wall slip efect. Nevertheless, the turbulent vortices that occur at both viscometers at high rotational speeds greatly affect the measurements. Viscous heat effects, eccentricities, and the need for space between cylinders must be adjusted. There are no suitable viscometers to measure viscosity at high temperatures. Therefore, most rheological experiments have been performed using low-temperature alloys [[17\]](#page-21-14).

The cone and plate do not allow the representative fuid to enter the narrow part of the viscometer as there is a suspended substance in the fuid. Therefore, the gap should be fve to ten times smaller than the average particle diameter of the particle material in the sample. The result of measuring the larger particle is noisy data or jam. This defect can be corrected by adjusting the cone angles and increasing the rotational speed [[147\]](#page-24-35). Furthermore, the viscosity measurement is considered to be best implemented within a closed system.

Fig. 21 Critical analysis of SSMP viscometers in the tabular diagram

The dual sliding plate and rotary parallel plate viscometers have normal pressure, shear rate, temperature, and end efect problems. When a parallel plate rotary viscometer measures SSM viscosity, the shear rate shows greater variation with sample temperature. The sample is likely to shrink during the test. Therefore, it is essential to keep the pressure and temperature constant throughout the measurement [\[148](#page-24-36)]. The torque produced varies depending on the quantity of the sample.

In a parallel plate compression viscometer, the ram speed is high, and higher acceleration occurs, making it difficult to measure viscosity. It is recommended that a hydraulic pressure be used instead of a dropforge and pneumatic pressure. Also, the pressure and temperature variation should be recorded with the help of a computer $[149]$ $[149]$. It helped to maintain accurate measurements.

7 Conclusions

In this review, the basic features of semi-solid metal processing, viscosity behaviour, and various methods of viscometry are illustrated. The following are the key fndings of the study:

- It is inferred that the viscosity of SSM is greatly affected by time-dependent properties, such as temperature, pressure, and shear rate.
- The viscosity measurements from the capillary, oscillating vessel, concentric cylinder, and vibration methods are

reliable while draining vessel and sliding plate viscometers are not accurate.

- In rotary-type viscometers, problems such as setting the gap between the cylinders, secondary fow, and surface tension in the concentric cylinder methods are of signifcant concern in torque and shear rate calculations.
- However, the concentric cylinder method is much better than the conical and parallel plate rotation method when viewed in terms of errors such as end and edge efects.
- The wall effects and the various errors caused by losses significantly affect the accuracy of the capillary viscometer. In the same way, the RAM speed, billet slip, and calibration issues afect the viscosity measurement in a parallel plate compression viscometer.
- Therefore, it can be concluded that there is no efficient and specifc viscometer to measure viscosity in the thixo method.
- The various parameters of the liquid metal particles, chemical reactions, accuracy, and numerical models need to be assessed for each viscometer.
- Therefore, further investigations are needed to design a standard viscosity measurement method of SSM to be useful for future researchers for practical purposes.

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Declarations

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Consent for publication The participants provided informed consent for the publication of their statements.

Competing interests The authors declare no competing interests.

References

- 1. Mehrabian R, Spencer B (1976) United States Patent (19)
- 2. Atkinson HV (2013) Alloys for semi-solid processing. Solid State Phenom 192–193:16–27. [https://doi.org/10.4028/www.scientifc.](https://doi.org/10.4028/www.scientific.net/SSP.192-193.16) [net/SSP.192-193.16](https://doi.org/10.4028/www.scientific.net/SSP.192-193.16)
- 3. Omar MZ, Alhawari K (2014) An overview of semi-solid metal processing. Aust J Basic Appl Sci 369–373
- 4. Mohammed MN, Omar MZ, Salleh MS, Alhawari KS, Kapranos P (2013) Semisolid metal processing techniques for nondendritic feedstock production. Sci World J 2013. [https://doi.org/10.1155/](https://doi.org/10.1155/2013/752175) [2013/752175](https://doi.org/10.1155/2013/752175)
- 5. Nafsi S, Ghomashchi R (2005) Semi-solid metal processing routes: an overview. Can Metall Q 44:289–304. [https://doi.org/](https://doi.org/10.1179/cmq.2005.44.3.289) [10.1179/cmq.2005.44.3.289](https://doi.org/10.1179/cmq.2005.44.3.289)
- 6. Husain NH, Ahmad AH, Rashidi MM (2017) An overview of thixoforming process. IOP Conf Ser Mater Sci Eng 257. [https://](https://doi.org/10.1088/1757-899X/257/1/012053) doi.org/10.1088/1757-899X/257/1/012053
- 7. Kim NS, Kang GG (2000) An investigation of fow characteristics considering the efect of viscosity variation in the thixoforming process. J Mater Process Technol 103:237–246. [https://doi.](https://doi.org/10.1016/S0924-0136(99)00441-0) [org/10.1016/S0924-0136\(99\)00441-0](https://doi.org/10.1016/S0924-0136(99)00441-0)
- 8. Beltyukov A, Olyanina N, Ladyanov V (2019) The viscosity of liquid Co-Si-B alloys. J Mol Liq 281:204–215. [https://doi.org/](https://doi.org/10.1016/j.molliq.2019.02.064) [10.1016/j.molliq.2019.02.064](https://doi.org/10.1016/j.molliq.2019.02.064)
- 9. Gancarz T, Jourdan J, Gasior W, Henein H (2018) Physicochemical properties of Al, Al-Mg and Al-Mg-Zn alloys. J Mol Liq 249:470–476.<https://doi.org/10.1016/j.molliq.2017.11.061>
- 10. Dobosz A, Plevachuk Y, Sklyarchuk V, Sokoliuk B, Gancarz T (2018) The application of liquid metals in cooling systems: a study of the thermophysical properties of eutectic Ga-Sn-Zn with Al additions. Int J Heat Mass Transf 126:414–420. [https://](https://doi.org/10.1016/j.ijheatmasstransfer.2018.05.045) doi.org/10.1016/j.ijheatmasstransfer.2018.05.045
- 11. Dogan A, Arslan H (2016) Geometric modelling of viscosity of copper-containing liquid alloys. Philos Mag 96:459–472. [https://](https://doi.org/10.1080/14786435.2015.1133938) doi.org/10.1080/14786435.2015.1133938
- 12. Jonas I, Hembree W, Yang F, Busch R, Meyer A (2018) Industrial grade versus scientifc pure: infuence on melt properties. Appl Phys Lett 112:1–5.<https://doi.org/10.1063/1.5021764>
- 13. Gao S, Jiao K, Zhang J (2019) Review of viscosity prediction models of liquid pure metals and alloys. Philos Mag 99:853–868. <https://doi.org/10.1080/14786435.2018.1562281>
- 14. Jethra R (1994) Viscosity measurement. ISA Trans 33:307–312. [https://doi.org/10.1016/0019-0578\(94\)90101-5](https://doi.org/10.1016/0019-0578(94)90101-5)
- 15. Cheng J, Gröbner J, Hort N, Kainer KU, Schmid-Fetzer R (2014) Measurement and calculation of the viscosity of metals - a review of the current status and developing trends. Meas Sci Technol 25. <https://doi.org/10.1088/0957-0233/25/6/062001>
- 16. Nafsi S, Ghomashchi R (2016) Semi-solid processing of aluminum alloys
- 17. Bakhtiyarov S, Siginer DA (2019) Rheoprocessing of semisolid aluminum alloys. Encycl Alum Its Alloy. [https://doi.org/10.](https://doi.org/10.1201/9781351045636-140000239) [1201/9781351045636-140000239](https://doi.org/10.1201/9781351045636-140000239)
- 18. Brooks RF, Dinsdale AT, Quested PN (2005) The measurement of viscosity of alloys - a review of methods, data and models. Meas Sci Technol 16:354–362. [https://doi.org/10.1088/0957-](https://doi.org/10.1088/0957-0233/16/2/005) [0233/16/2/005](https://doi.org/10.1088/0957-0233/16/2/005)
- 19. Srivastava N, Burns MA (2006) Analysis of non-Newtonian liquids using a microfuidic capillary viscometer. Anal Chem 78:1690–1696.<https://doi.org/10.1021/ac0518046>
- 20. Ram A, Tamir A (1964) A capillary viscometer for non-newtonian liquids. Ind Eng Chem 56:47–53.<https://doi.org/10.1021/ie50650a009>
- 21. Wunderlich BK, Bausch AR (2013) Diferential capillary viscometer for measurement of non-Newtonian fuids. RSC Adv 3:21730–21735. <https://doi.org/10.1039/c3ra42921k>
- 22. Han SH, Kang CG, Sung JH (2007) Investigation of viscosity properties for rheology forming of AM50A magnesium alloy. J Mater Process Technol 187–188:335–338. [https://doi.org/10.](https://doi.org/10.1016/j.jmatprotec.2006.11.195) [1016/j.jmatprotec.2006.11.195](https://doi.org/10.1016/j.jmatprotec.2006.11.195)
- 23. Lashkari O, Ghomashchi R (2006) The implication of rheological principles for characterization of semi-solid Al-Si cast billets. J Mater Sci 41:5958–5965. [https://doi.org/10.1007/](https://doi.org/10.1007/s10853-006-0280-8) [s10853-006-0280-8](https://doi.org/10.1007/s10853-006-0280-8)
- 24. Shah A, Brabazon D, Looney L (2008) Design of a capillary viscometer with numerical and computational methods. Int J Manuf Technol Manag 15:246–252. [https://doi.org/10.1504/](https://doi.org/10.1504/IJMTM.2008.019663) [IJMTM.2008.019663](https://doi.org/10.1504/IJMTM.2008.019663)
- 25. Pola A, Tocci M, Kapranos P (2018) Microstructure and properties of semi-solid aluminum alloys: a literature review. Metals (Basel) 8.<https://doi.org/10.3390/met8030181>
- 26. Lashkari O, Ghomashchi R, Ajersch F (2007) Deformation behavior of semi-solid A356 Al-Si alloy at low shear rates: the efect of sample size. Mater Sci Eng A 444:198–205. [https://](https://doi.org/10.1016/j.msea.2006.08.067) doi.org/10.1016/j.msea.2006.08.067
- 27. Proni CTW, Robert MH, Zoqui EJ (2015) Efect of casting procedures in the structure and fow behaviour of semisolid A356 alloy. Arch Mater Sci Eng 73:82–93
- 28. Das P, Samanta SK, Chattopadhyay H, Dutta P, Barman N (2013) Rheological characterization of semi-solid A356 aluminium alloy. Solid State Phenom 192–193:329–334. [https://](https://doi.org/10.4028/www.scientific.net/SSP.192-193.329) [doi.org/10.4028/www.scientifc.net/SSP.192-193.329](https://doi.org/10.4028/www.scientific.net/SSP.192-193.329)
- 29. Sheykh-jaberi F, Cockcroft SL, Maijer DM, Phillion AB (2019) Comparison of the semi-solid constitutive behaviour of A356 and B206 aluminum foundry alloys. J Mater Process Technol 266:37–45. <https://doi.org/10.1016/j.jmatprotec.2018.10.029>
- 30. Deepak Kumar S, Ghose J, Mandal A (2019) Thixoforming of light-weight alloys and composites: an approach toward sustainable manufacturing. Elsevier Inc
- 31. Atkinson HV (2005) Modelling the semisolid processing of metallic alloys. Prog Mater Sci 50:341–412. [https://doi.org/](https://doi.org/10.1016/j.pmatsci.2004.04.003) [10.1016/j.pmatsci.2004.04.003](https://doi.org/10.1016/j.pmatsci.2004.04.003)
- 32. Sołek KP, Rogal Ł, Kapranos P (2017) Evolution of globular microstructure and rheological properties of StelliteTM 21 alloy after heating to semisolid state. J Mater Eng Perform 26:115–123.<https://doi.org/10.1007/s11665-016-2421-9>
- 33. Canyook R, Petsut S, Wisutmethangoon S, Flemings MC, Wannasin J (2010) Evolution of microstructure in semi-solid slurries of rheocast aluminum alloy. Trans Nonferrous Met Soc China (English Ed 20:1649–1655. [https://doi.org/10.](https://doi.org/10.1016/S1003-6326(09)60353-8) [1016/S1003-6326\(09\)60353-8](https://doi.org/10.1016/S1003-6326(09)60353-8)
- 34. Atkinson HV, Liu D (2008) Microstructural coarsening of semi-solid aluminium alloys. Mater Sci Eng A 496:439–446. <https://doi.org/10.1016/j.msea.2008.06.013>
- 35. Agarwal M, Srivastava R (2016) Infuence of solid fraction casting on microstructure of aluminum alloy 6061. Mater Manuf Process 31:1958–1967. <https://doi.org/10.1080/10426914.2015.1127956>
- 36. Flemings MC, Martinez RA (2006) Principles of microstructural formation in semi-solid metal processing. Solid State Phenom 116– 117:1–8. [https://doi.org/10.4028/www.scientifc.net/ssp.116-117.1](https://doi.org/10.4028/www.scientific.net/ssp.116-117.1)
- 37. Lashkari O, Ghomashchi R (2007) The implication of rheology in semi-solid metal processes: an overview. J Mater Process Technol 182:229–240.<https://doi.org/10.1016/j.jmatprotec.2006.08.003>
- 38. Qin RS, Fan Z (2001) Fractal theory study on morphological dependence of viscosity of semisolid slurries. Mater Sci Technol 17:1149–1152.<https://doi.org/10.1179/026708301101511086>
- 39. Lipchitz A, Harvel G, Sunagawa T (2015) Experimental investigation of the thermal conductivity and viscosity of liquid In-Bi-Sn eutectic alloy (Field's metal) for use in a natural circulation experiental loop. Int Conf Nucl Eng Proceedings, ICONE 2015-Janua:
- 40. Gecu R, Acar S, Kisasoz A, Guler KA, Karaaslan A (2017) Aging of A356 aluminum billets produced by semi- solid metal processing. 3–5
- 41. Kapranos P (2019) Current state of semi-solid net-shape die casting. Metals (Basel) 9:1–13.<https://doi.org/10.3390/met9121301>
- 42. Koke J, Modigell M (2003) Flow behaviour of semi-solid metal alloys. J Nonnewton Fluid Mech 112:141–160. [https://doi.org/](https://doi.org/10.1016/S0377-0257(03)00080-6) [10.1016/S0377-0257\(03\)00080-6](https://doi.org/10.1016/S0377-0257(03)00080-6)
- 43. Wannasin J, Canyook R, Burapa R, Sikong L, Flemings MC (2008) Evaluation of solid fraction in a rheocast aluminum die casting alloy by a rapid quenching method. Scr Mater 59:1091– 1094. <https://doi.org/10.1016/j.scriptamat.2008.07.029>
- 44. Franco JM, Partal Pedro (2010) Non-Newtonian fuids. Rheology 1
- 45. SoŁlek K, Korolczuk-Hejnak M, Karbowniczek M (2011) An analysis of steel viscosity in the solidifcation temperature range. Arch Metall Mater 56:593–598. [https://doi.org/10.2478/](https://doi.org/10.2478/v10172-011-0063-3) [v10172-011-0063-3](https://doi.org/10.2478/v10172-011-0063-3)
- 46. Acharya PC, Suares D, Shetty S, Fernandes C, Tekade RK (2018) Rheology and its implications on performance of liquid dosage forms. Elsevier Inc
- 47. Sołek K, Korolczuk-Hejnak M, Ślęzak W (2012) Viscosity measurements for modeling of continuous steel casting. Arch Metall Mater 57:333–338.<https://doi.org/10.2478/v10172-012-0031-6>
- 48. Ma Z, Zhang H, Song W, Wu X, Jia L, Zhang H (2020) Pressuredriven mold flling model of aluminum alloy melt/semi-solid slurry based on rheological behavior. J Mater Sci Technol 39:14– 21.<https://doi.org/10.1016/j.jmst.2019.07.048>
- 49. Zhu BW, Li LX, Liu X, Zhang LQ, Xu R (2015) Efect of viscosity measurement method to simulate high pressure die casting of thin-wall AlSi10MnMg alloy castings. J Mater Eng Perform 24:5032–5036.<https://doi.org/10.1007/s11665-015-1783-8>
- 50. Ferreira IL, de Castro JA, Garcia A (2019) On the prediction of temperature-dependent viscosity of multicomponent liquid alloys. Contin Mech Thermodyn 31:1369–1385. [https://doi.org/](https://doi.org/10.1007/s00161-019-00753-7) [10.1007/s00161-019-00753-7](https://doi.org/10.1007/s00161-019-00753-7)
- 51. Atkinson HV, Rassili A (2010) A review of the semi-solid processing of steel. Int J Mater Form 3:791–795. [https://doi.org/10.](https://doi.org/10.1007/s12289-010-0889-7) [1007/s12289-010-0889-7](https://doi.org/10.1007/s12289-010-0889-7)
- 52. Volpe V, Pantani R (2018) Determination of the efect of pressure on viscosity at high shear rates by using an injection molding machine. J Appl Polym Sci 135:1–7.<https://doi.org/10.1002/app.45277>
- 53. Omar MZ, Atkinson H V., Palmiere EJ, Howe AA, Kapranos P (2006) Viscosity - shear rate relationship during the thixoforming of HP9/4/30 steel. Solid State Phenom 116–117:677–680. [https://](https://doi.org/10.4028/www.scientific.net/ssp.116-117.677) [doi.org/10.4028/www.scientifc.net/ssp.116-117.677](https://doi.org/10.4028/www.scientific.net/ssp.116-117.677)
- 54. Reynolds C, Thompson R, McLeish T (2018) Pressure and shear rate dependence of the viscosity and stress relaxation of polymer melts. J Rheol (N Y N Y) 62:631–642.<https://doi.org/10.1122/1.5012969>
- 55. Carlesso (2008) The foaming behavior of alkane emulsifed ceramic suspension: from LAPES to HAPES. 1–91. [https://doi.](https://doi.org/10.13140/RG.2.2.20992.12803) [org/10.13140/RG.2.2.20992.12803](https://doi.org/10.13140/RG.2.2.20992.12803)
- 56. McLelland ARA, Henderson NG, Atkinson HV, Kirkwood DH (1997) Anomalous rheological behaviour of semi-solid alloy slurries at low shear rates. Mater Sci Eng A 232:110–118. [https://](https://doi.org/10.1016/s0921-5093(97)00105-6) [doi.org/10.1016/s0921-5093\(97\)00105-6](https://doi.org/10.1016/s0921-5093(97)00105-6)
- 57. Lashkari O, Ajersch F, Charette A, Chen XG (2008) Microstructure and rheological behavior of hypereutectic semi-solid Al-Si alloy under low shear rates compression test. Mater Sci Eng A 492:377–382.<https://doi.org/10.1016/j.msea.2008.05.018>
- 58. Brabazon D, Browne DJ, Carr AJ (2002) Mechanical stir casting of aluminium alloys from the mushy state: process, microstructure and mechanical properties. Mater Sci Eng A 326:370–381. [https://doi.org/10.1016/S0921-5093\(01\)01832-9](https://doi.org/10.1016/S0921-5093(01)01832-9)
- 59. Favier V, Atkinson HV (2011) Micromechanical modelling of the elastic-viscoplastic response of metallic alloys under rapid compression in the semi-solid state. Acta Mater 59:1271–1280. <https://doi.org/10.1016/j.actamat.2010.10.059>
- 60. Modigell M, Pola A, Tocci M (2018) Rheological characterization of semi-solid metals: a review. Metals (Basel) 8:1–23. <https://doi.org/10.3390/met8040245>
- 61. He M, Wang Y, Forssberg E (2004) Slurry rheology in wet ultrafne grinding of industrial minerals: a review. Powder Technol 147:94–112.<https://doi.org/10.1016/j.powtec.2004.09.032>
- 62. Kulisiewicz L, Delgado A (2010) High-pressure rheological measurement methods: a review. Appl Rheol 20:130181– 1301815.<https://doi.org/10.3933/ApplRheol-20-13018>
- 63. Assael MJ, Kalyva AE, Antoniadis KD, Michael Banish R, Egry I, Wu J, Kaschnitz E, Wakeham WA (2010) Reference data for the density and viscosity of liquid copper and liquid tin. J Phys Chem Ref Data 39. <https://doi.org/10.1063/1.3467496>
- 64. Walters K, Jones WM (2010) Measurement of viscosity, 4th edn. Elsevier
- 65. Kestin J, Sokolov M, Wakeham W (1973) Theory of capillary viscometers. Appl Sci Res 27:241–264. [https://doi.org/10.1007/](https://doi.org/10.1007/BF00382489) [BF00382489](https://doi.org/10.1007/BF00382489)
- 66. Shin S, Keum DY (2003) Viscosity measurement of non-Newtonian fuid foods with a mass-detecting capillary viscometer. J Food Eng 58:5–10. [https://doi.org/10.1016/S0260-8774\(02\)00327-8](https://doi.org/10.1016/S0260-8774(02)00327-8)
- 67. Nowak J, Odenbach S (2016) A capillary viscometer designed for the characterization of biocompatible ferrofuids. J Magn Magn Mater 411:49–54.<https://doi.org/10.1016/j.jmmm.2016.03.057>
- 68. Iida T, Guthrie RIL, Morita Z (1988) An equation for the viscosity of liquid metals. Can Metall Q 27:1–5. [https://doi.org/10.](https://doi.org/10.1179/cmq.1988.27.1.1) [1179/cmq.1988.27.1.1](https://doi.org/10.1179/cmq.1988.27.1.1)
- 69. Bakhtiyarov SI, Overfelt RA (1999) Measurement of liquid metal viscosity by rotational technique. Acta Mater 47:4311–4319. [https://doi.org/10.1016/S1359-6454\(99\)00307-9](https://doi.org/10.1016/S1359-6454(99)00307-9)
- 70. Dinsdale AT, Quested PN (2004) The viscosity of aluminium and its alloys - a review of data and models. J Mater Sci 39:7221– 7228.<https://doi.org/10.1023/B:JMSC.0000048735.50256.96>
- 71. Kehr M, Hoyer W, Egry I (2007) A new high-temperature oscillating cup viscometer. Int J Thermophys 28:1017–1025. [https://](https://doi.org/10.1007/s10765-007-0216-9) doi.org/10.1007/s10765-007-0216-9
- 72. Nunes VMB, Lourenço MJV, Santos FJV, Nieto De Castro CA (2010) Viscosity of industrially important Al-Zn alloys. I-quasi-eutectic alloys Int J Thermophys 31:2348–2360. [https://doi.org/10.1007/](https://doi.org/10.1007/s10765-010-0848-z) [s10765-010-0848-z](https://doi.org/10.1007/s10765-010-0848-z)
- 73. Deng Y, Zhang J, Jiao K (2018) Viscosity measurement and prediction model of molten iron. Ironmak Steelmak 45:773–777. <https://doi.org/10.1080/03019233.2018.1491171>
- 74. Zhu P, Lai J, Shen J, Wu K, Zhang L, Liu J (2018) An oscillating cup viscometer based on Shvidkovskiy algorithm for molten metals. Meas J Int Meas Confed 122:149–154. [https://doi.org/](https://doi.org/10.1016/j.measurement.2018.02.023) [10.1016/j.measurement.2018.02.023](https://doi.org/10.1016/j.measurement.2018.02.023)
- 75. Roscoe R (1958) Viscosity determination by the oscillating vessel method I: theoretical considerations. Proc Phys Soc 72:576– 584. <https://doi.org/10.1088/0370-1328/72/4/312>
- 76. Alan D, Newell GF Theory of oscillation type viscometers : The Oscillating Cup. 450–465
- 77. Mao Z, Zhang T (2017) Numerical analysis of an improved heating device for the electromagnetically driven oscillating cup viscometer. Adv Mech Eng 9:1–6.<https://doi.org/10.1177/1687814017729075>
- 78. Yakymovych A, Vus V, Mudry S (2016) Viscosity of liquid Cu-In-Sn alloys. J Mol Liq 219:845–850. [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.molliq.2016.04.055) [molliq.2016.04.055](https://doi.org/10.1016/j.molliq.2016.04.055)
- 79. Brooks RF, Day AP, Andon RJL, Chapman LA, Mills KC, Quested PN (2001) Measurement of viscosities of metals and alloys with an oscillating viscometer. High Temp - High Press 33:73–82.<https://doi.org/10.1068/htwu139>
- 80. Solomons C, White MS (1967) Oscillating plate viscometry. 305–315
- 81. Busciglio A, Montante G, Kracík T, Moucha T, Paglianti A (2017) Rotary sloshing induced by impeller action in unbaffled stirred vessels. Chem Eng J 317:433–443. [https://doi.org/10.](https://doi.org/10.1016/j.cej.2017.02.099) [1016/j.cej.2017.02.099](https://doi.org/10.1016/j.cej.2017.02.099)
- 82. Nunes VMB, Queirós CSGP, Lourenço MJV, Santos FJV, Nieto de Castro CA (2018) Viscosity of industrially important Zn–Al alloys part II: alloys with higher contents of Al and Si. Int J Thermophys 39:1–10. <https://doi.org/10.1007/s10765-018-2388-x>
- 83. Quqazeh M, Aldabbas HA, Krishan MM, Musa N (2016) Characteristics and analysis for mechanical instrumentation used to measure fuid viscosity. 1–6
- 84. Elahi SH, Abdi H, Shahverdi HR (2013) Investigating viscosity variations of molten aluminum by calcium addition and stirring. Mater Lett 91:376–378. <https://doi.org/10.1016/j.matlet.2012.09.109>
- 85. Kono Y, Kenney-Benson C, Shibazaki Y, Park C, Shen G, Wang Y (2015) High-pressure viscosity of liquid Fe and FeS revisited by falling sphere viscometry using ultrafast X-ray imaging. Phys Earth Planet Inter 241:57–64.<https://doi.org/10.1016/j.pepi.2015.02.006>
- 86. Jo RS, Jo HS, Chai A (2017) Development of low-cost visionbased falling sphere viscometer. Proc 2017 IEEE Int Conf Signal Image Process Appl ICSIPA 2017 279–283. [https://doi.org/10.](https://doi.org/10.1109/ICSIPA.2017.8120621) [1109/ICSIPA.2017.8120621](https://doi.org/10.1109/ICSIPA.2017.8120621)
- 87. Elahi SH, Adelnia H, Shahverdi HR (2012) A simple accurate method for measuring viscosity of liquid metals at high temperatures. J Rheol (N Y N Y) 56:941–954.<https://doi.org/10.1122/1.4709431>
- 88. Lohöfer G (2020) Viscosity measurement by the oscillating drop method: the case of strongly damped oscillations. Int J Thermophys 41:1–13. <https://doi.org/10.1007/s10765-020-2608-z>
- 89. Mohr M, Wunderlich RK, Koch S, Galenko PK, Gangopadhyay AK, Kelton KF, Jiang JZ, Fecht HJ (2019) Surface tension and viscosity of Cu 50 Zr 50 measured by the oscillating drop technique on board the international space station. Microgravity Sci Technol 31:177–184.<https://doi.org/10.1007/s12217-019-9678-1>
- 90. Ishikawa T, Paradis PF, Okada JT, Kumar MV, Watanabe Y (2013) Viscosity of molten Mo, Ta, Os, Re, and W measured by electrostatic levitation. J Chem Thermodyn 65:1–6. [https://](https://doi.org/10.1016/j.jct.2013.05.036) doi.org/10.1016/j.jct.2013.05.036
- 91. Arashiro EY, Demarquette NR (1999) Use of the pendant drop method to measure interfacial tension between molten polymers. Mater Res 2:23–32.<https://doi.org/10.1590/s1516-14391999000100005>
- 92. Kargl F, Yuan C, Greaves GN (2015) Aerodynamic levitation: thermophysical property measurements of liquid oxides. Int J Microgravity Sci Appl 32:320212. [https://doi.org/10.15011/](https://doi.org/10.15011/ijmsa.32.320212) [ijmsa.32.320212](https://doi.org/10.15011/ijmsa.32.320212)
- 93. Wunderlich RK, Mohr M (2019) Non-linear effects in the oscillating drop method for viscosity measurements. High Temp - High Press 49:233–251.<https://doi.org/10.32908/hthp.v48.648>
- 94. Ma C, Zhao J, Cao C, Lin TC, Li X (2016) Fundamental study on laser interactions with nanoparticles-reinforced metals-part II: effect of nanoparticles on surface tension, viscosity, and laser melting. J Manuf Sci Eng Trans ASME 138. [https://doi.org/10.](https://doi.org/10.1115/1.4033446) [1115/1.4033446](https://doi.org/10.1115/1.4033446)
- 95. Xiao X, Hyers RW, Wunderlich RK, Fecht HJ, Matson DM (2018) Deformation induced frequency shifts of oscillating droplets during molten metal surface tension measurement. Appl Phys Lett 113:1–4.<https://doi.org/10.1063/1.5039336>
- 96. Assael MJ, Kakosimos K, Banish RM, Brillo J, Egry I, Brooks R, Quested PN, Mills KC, Nagashima A et al (2006) Reference data for the density and viscosity of liquid aluminum and liquid iron. J Phys Chem Ref Data 35:285–300. [https://doi.org/10.1063/1.](https://doi.org/10.1063/1.2149380) [2149380](https://doi.org/10.1063/1.2149380)
- 97. Gancarz T, Moser Z, Gąsior W, Pstruś J, Henein H (2011) A comparison of surface tension, viscosity, and density of Sn and Sn-Ag alloys using diferent measurement techniques. Int J Thermophys 32:1210–1233.<https://doi.org/10.1007/s10765-011-1011-1>
- 98. Barber EM, Muenger JR, Villforth FJ (1955) A high rate of shear rotational viscometer. Anal Chem 27:425–429. [https://doi.org/10.](https://doi.org/10.1021/ac60099a030) [1021/ac60099a030](https://doi.org/10.1021/ac60099a030)
- 99. Malik MM, Jeyakumar M, Hamed MS, Walker MJ, Shankar S (2010) Rotational rheometry of liquid metal systems: measurement geometry selection and fow curve analysis. J Nonnewton Fluid Mech 165:733–742.<https://doi.org/10.1016/j.jnnfm.2010.03.009>
- 100. Gabrysh AF, Eyring H, Ma SM, Liang K (1962) Automatic rotational viscometer and high-pressure apparatus for the study of the non-newtonian behavior of materials. Rev Sci Instrum 33:670–682. <https://doi.org/10.1063/1.1746649>
- 101. Blanco A, Azpilgain Z, Lozares J, Kapranos P, Hurtado I (2010) Rheological characterization of A201 aluminum alloy. Trans Nonferrous Met Soc China (English Ed 20:1638–1642. [https://](https://doi.org/10.1016/S1003-6326(09)60351-4) [doi.org/10.1016/S1003-6326\(09\)60351-4](https://doi.org/10.1016/S1003-6326(09)60351-4)
- 102. Li Y, Mao W, Zhu W, Yang B (2014) Rheological behavior of semisolid 7075 aluminum alloy at steady state. China Foundry 11:79–84
- 103. Nishimura K (1996) Viscosity of fuidized snow. Cold Reg Sci Technol 24:117–127. [https://doi.org/10.1016/0165-232X\(95\)00023-5](https://doi.org/10.1016/0165-232X(95)00023-5)
- 104. Jeng SC, Chen SW (1996) Determination of the solidifcation characteristics of the A356.2 aluminum alloy. Mater Sci Forum 217–222:283–288. [https://doi.org/10.4028/www.scientifc.net/](https://doi.org/10.4028/www.scientific.net/msf.217-222.283) [msf.217-222.283](https://doi.org/10.4028/www.scientific.net/msf.217-222.283)
- 105. Riyaaz (2018) Searle viscosity diferential fowmeter. Int J Pure Appl Math 118
- 106. Hirai M, Takebayashi K, Yoshikawa Y (1994) Efect of chemical composition on apparent viscosity of semisolid alloys. Isij Int 33:1182–1189.<https://doi.org/10.2355/isijinternational.33.1182>
- 107. Korolczuk-Hejnak M, Migas P (2012) Analysis of selected liquid steel viscosity. Arch Metall Mater 57:963–969. [https://doi.org/](https://doi.org/10.2478/v10172-012-0107-3) [10.2478/v10172-012-0107-3](https://doi.org/10.2478/v10172-012-0107-3)
- 108. Vieira EA, Kliauga AM, Ferrante M (2004) Microstructural evolution and rheological behaviour of aluminium alloys A356, and A356 + 0.5% Sn designed for thixocasting. J Mater Process Technol 155– 156:1623–1628.<https://doi.org/10.1016/j.jmatprotec.2004.04.358>
- 109. Corey H, Creswick N (1970) A versatile recording Couette-type viscometer. J Texture Stud 1:155–166. [https://doi.org/10.1111/j.](https://doi.org/10.1111/j.1745-4603.1970.tb00720.x) [1745-4603.1970.tb00720.x](https://doi.org/10.1111/j.1745-4603.1970.tb00720.x)
- 110. Manrique LA, Porter RS (1975) An improved Couette high shear viscometer. Rheol Acta 14:926–930. [https://doi.org/10.1007/](https://doi.org/10.1007/BF01515893) [BF01515893](https://doi.org/10.1007/BF01515893)
- 111. Berberian JG (1980) A method for measuring small rotational velocities for a couette-type viscometer. Rev Sci Instrum 51:1136–1137.<https://doi.org/10.1063/1.1136361>
- 112. Barnes H (2011) Viscosity measurement. Thermopedia. [https://](https://doi.org/10.1615/AtoZ.v.viscosity_measurement) doi.org/10.1615/AtoZ.v.viscosity_measurement
- 113. Gücüyener IH, Kok MV, Batmaz T (2002) End effect evaluation in rheological measurement of drilling fuids using Coutte coaxial cylinder viscometer. Energy Sources 24:441–449. [https://](https://doi.org/10.1080/00908310252889942) doi.org/10.1080/00908310252889942
- 114. Hembree W, Bochtler B, Busch R (2018) High-temperature rotating cylinder rheometer for studying metallic glass forming liquids. Rev Sci Instrum 89:.<https://doi.org/10.1063/1.5039318>
- 115. Wunderlich AM, Brunn PO (1989) The complex rheological behavior of an aqueous cationic surfactant solution investigated in a Couette-type viscometer. Colloid Polym Sci 267:627–636. <https://doi.org/10.1007/BF01410440>
- 116. Cullen PJ, O'Donnell CP, Houška M (2003) Rotational rheometry using complex geometries - a review. J Texture Stud 34:1–20. <https://doi.org/10.1111/j.1745-4603.2003.tb01052.x>
- 117. Modigell M, Pape L (2008) A comparison of measuring devices used to prevent wall slip in viscosity measurements of metallic suspensions. Solid State Phenom 141-143:307-312. [https://doi.](https://doi.org/10.4028/www.scientific.net/ssp.141-143.307) [org/10.4028/www.scientifc.net/ssp.141-143.307](https://doi.org/10.4028/www.scientific.net/ssp.141-143.307)
- 118. Soualhi H, Kadri EH, Ngo TT, Bouvet A, Cussigh F, Tahar ZEA (2017) Design of portable rheometer with new vane geometry to estimate concrete rheological parameters. J Civ Eng Manag 23:347–355. <https://doi.org/10.3846/13923730.2015.1128481>
- 119. Barnes HA, Nguyen QD (2001) Rotating vane rheometry-a review. J Nonnewton Fluid Mech 98:1–14. [https://doi.org/10.](https://doi.org/10.1016/S0377-0257(01)00095-7) [1016/S0377-0257\(01\)00095-7](https://doi.org/10.1016/S0377-0257(01)00095-7)
- 120. Bataineh KM (2014) Numerical investigation of secondary fow efect in cone-plate viscometer. Comput Fluids 101:105–113. <https://doi.org/10.1016/j.compfluid.2014.06.009>
- 121. Markovitz H, Elyash LJ, Padden FJ, DeWitt TW (1955) A coneand-plate viscometer. J Colloid Sci 10:165–173. [https://doi.org/](https://doi.org/10.1016/0095-8522(55)90023-4) [10.1016/0095-8522\(55\)90023-4](https://doi.org/10.1016/0095-8522(55)90023-4)
- 122. Giacomin AJ, Gilbert PH (2017) Exact-solution for cone-plate viscometry. 175101
- 123. Falah NM (2016) Study the fow behavior of GNPs flled water and polymer using cone-on-plate viscometer. 488–494
- 124. Hellström LO, Samaha M, Wang K, Smits A, Hultmark M (2015) Errors in parallel-plate and cone-plate rheometer measurements due to sample underfll. Meas Sci Technol 26. [https://doi.org/10.](https://doi.org/10.1088/0957-0233/26/1/015301) [1088/0957-0233/26/1/015301](https://doi.org/10.1088/0957-0233/26/1/015301)
- 125. Viscoelastic O, Simulation F, Shuichi T, Michal KZ, Naoki W (2009) Evaluation of parallel plate type rheometer using an 37:113–120
- 126. Renuka A, Muthtamilselvan M, Doh DH, Cho GR (2020) Entropy analysis and nanofuid past a double stretchable spinning disk using homotopy analysis method. Math Comput Simul 171:152–169.<https://doi.org/10.1016/j.matcom.2019.05.008>
- 127. Song Y, Won C, Kang S, hoon, Lee H, Park SJ, Park SH, Yoon J, (2018) Characterization of glass viscosity with parallel plate and rotational viscometry. J Non Cryst Solids 486:27–35. [https://doi.](https://doi.org/10.1016/j.jnoncrysol.2018.02.003) [org/10.1016/j.jnoncrysol.2018.02.003](https://doi.org/10.1016/j.jnoncrysol.2018.02.003)
- 128. Dealy JM, Giacomin AJ (1993) Sliding plate and sliding cylinder rheometers. Rheol Meas 383–404. [https://doi.org/10.1007/](https://doi.org/10.1007/978-94-017-2898-0_12) [978-94-017-2898-0_12](https://doi.org/10.1007/978-94-017-2898-0_12)
- 129. Koran F, Dealy JM (1999) A high pressure sliding plate rheometer for polymer melts. J Rheol (N Y N Y) 43:1279–1290. <https://doi.org/10.1122/1.551046>
- 130. Roselli RJ, Diller KR (2011) Biotransport: principles and applications
- 131. Laxmanan V, Flemings MC (1980) Deformation of semi-solid Sn-15 Pct Pb alloy. Metall Trans A 11:1927–1937. [https://doi.](https://doi.org/10.1007/BF02655112) [org/10.1007/BF02655112](https://doi.org/10.1007/BF02655112)
- 132. Yurko JA, Flemings MC (2002) Rheology and microstructure of semi-solid aluminum alloys compressed in the drop-forge viscometer. Metall Mater Trans A Phys Metall Mater Sci 33:2737–2746. <https://doi.org/10.1007/s11661-002-0396-7>
- 133. Lashkari O, Ghomashchi R (2007) A new machine to characterize microstructural evolution of semi-solid metal billets through viscometery. Mater Des 28:1321–1325. [https://doi.org/](https://doi.org/10.1016/j.matdes.2006.01.023) [10.1016/j.matdes.2006.01.023](https://doi.org/10.1016/j.matdes.2006.01.023)
- 134. Lashkari O, Nafsi S, Ghomashchi R (2006) Microstructural characterization of rheo-cast billets prepared by variant pouring temperatures. Mater Sci Eng A 441:49–59. [https://doi.org/](https://doi.org/10.1016/j.msea.2006.05.075) [10.1016/j.msea.2006.05.075](https://doi.org/10.1016/j.msea.2006.05.075)
- 135. Fukui Y, Nara D, Kumazawa N (2015) Evaluation of the deformation behavior of a semi-solid hypereutectic Al-Si alloy compressed in a drop-forge viscometer. Metall Mater Trans A Phys Metall Mater Sci 46:1908–1916. <https://doi.org/10.1007/s11661-015-2777-8>
- 136. Malagutti L, Mollica F, Mazzanti V (2020) Error amplifcation in capillary viscometry of power law fuids with slip. Polym Test 91:106816.<https://doi.org/10.1016/j.polymertesting.2020.106816>
- 137. Lee E, Kim B, Choi S (2020) Hand-held, automatic capillary viscometer for analysis of Newtonian and non-Newtonian fuids. Sensors Actuators, A Phys 313:112176. [https://doi.org/10.](https://doi.org/10.1016/j.sna.2020.112176) [1016/j.sna.2020.112176](https://doi.org/10.1016/j.sna.2020.112176)
- 138. Fischer F, Bartz J, Schmitz K, Brouwer L, Schwarze H (2018) A numerical approach for the evaluation of a capillary viscometer experiment. BATH/ASME 2018 Symp Fluid Power Motion Control FPMC 2018 1–12.<https://doi.org/10.1115/FPMC2018-8815>
- 139. Chou TC, Lee J, Hsiai TK, Tai YC (2017) A vacuum capillary viscometer that measures the viscosity of biofuids. TRANS-DUCERS 2017 - 19th Int Conf Solid-State Sensors, Actuators Microsystems 1547–1550. [https://doi.org/10.1109/TRANSDUC-](https://doi.org/10.1109/TRANSDUCERS.2017.7994355)[ERS.2017.7994355](https://doi.org/10.1109/TRANSDUCERS.2017.7994355)
- 140. Sieben M, Hanke R, Büchs J (2019) Contact-free determination of viscosity in multiple parallel samples. Sci Rep 9:1–10. [https://](https://doi.org/10.1038/s41598-019-44859-z) doi.org/10.1038/s41598-019-44859-z
- 141. Zhu P, Lai J, Wu K, Zhang Z, Huang X, Zhang L, Liu J (2017) An attenuated time measurement based on pulse interval for oscillating cup viscometer. Proc - 2017 Chinese Autom Congr CAC 2017 2017- Janua:3109–3111.<https://doi.org/10.1109/CAC.2017.8243309>
- 142. Abbas KA, Abdulkarim SM, Saleh AM, Ebrahimian M (2010) Suitability of viscosity measurement methods for liquid food variety and applicability in food industry - a review. J Food, Agric Environ 8:100–107
- 143. Reilly A, Miller A, Jamali S, Newaz and (2020) A high precision falling-ball viscometer using a fast camera. 1–8
- 144. Kurkin EI, Chertykovtseva VO, Zakhvatkin YV (2020) Processing a brookfeld rotational viscometer measurement results in the MATLAB. Key Eng Mater 834 KEM:82–89. [https://doi.org/10.](https://doi.org/10.4028/www.scientific.net/KEM.834.82) [4028/www.scientifc.net/KEM.834.82](https://doi.org/10.4028/www.scientific.net/KEM.834.82)
- 145. Wang G, Du H, Guo B (2018) Determination of viscosity and wall slip behavior of a polymer-gel used for leakage control from Couette viscometry data. J Energy Resour Technol Trans ASME 140. <https://doi.org/10.1115/1.4038384>
- 146. Bakhtiyarov S, Siginer DA (2019) Rheoprocessing of semisolid aluminum alloys. Encycl Alum Its Alloy 2395–2406. [https://doi.](https://doi.org/10.1201/9781351045636-140000239) [org/10.1201/9781351045636-140000239](https://doi.org/10.1201/9781351045636-140000239)
- 147. Lang L, Alexandrov S, Lyamina E, Manh DV (2020) The Behavior of Melts with Vanishing Viscosity in the Cone-and-Plate Rheomete. Appl Sci 10(1):172.<https://doi.org/10.3390/app10010172>
- 148. Jiang T, Li J, Zhang S (2020) Design of a new structure for rotary viscometer. IOP Conf Ser Mater Sci Eng 782. [https://doi.org/10.](https://doi.org/10.1088/1757-899X/782/2/022102) [1088/1757-899X/782/2/022102](https://doi.org/10.1088/1757-899X/782/2/022102)
- 149. Simlandi S (2018) Rheological behaviour of semisolid A356 alloy slurry during cooling – an overview. 4:784–787

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