**ORIGINAL ARTICLE**

# **A new monitoring scheme of an air quality network based on the kernel method**

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#### **Abstract**



Air pollution is classified as one of the most dangerous type on the human health, the environment, and the ecosystem. However, air pollution results in climate change and affects people's health. For a number of years, monitoring the air quality has become a very urgent and necessary topic. Moreover, safety and health have been attracting attention as one of the important topics to evaluate, firstly, the degree of air pollution and predict pollutant concentrations accurately. Then, it is crucial to establish a more scientific air quality monitoring to ensure the quality of life. In this paper, new reduced air quality monitoring is suggested to enhance the Fault Detection (FD) of an air quality monitoring network. Furthermore, a sensor FD procedure based on Reduced Kernel Partial Least Squares (RKPLS) is proposed to monitor an air quality monitoring network. The main contribution of the suggested procedure is to enhance the FD of an air quality monitoring network in terms of computation time and false alarm rate, using just the important latent components, compared to standard Kernel Partial Least Squares (KPLS).

**Keywords** Air pollution · Air quality · KPLS · Reduced KPLS · SPE · Fault detection

# **1 Introduction**

Concerning the environment, indoor air pollution is consistently ranked among the top highly important risks that can destroy public health, life quality, vegetation, and even mon-

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uments. Because of human activities, industrial effluents, and meteorological factors, air is vulnerable to be polluted by pollutants like nitrogen oxides (*NO*<sup>2</sup> and NO), ozone, and carbon oxides. Thus, air quality process monitoring is becoming increasingly essential and important to protect the public health and the environment  $[1-3]$  $[1-3]$ . Accordingly, the development of robust and accurate air quality monitoring is highly desirable.

Air quality monitoring networks have been reported in the literature  $[4-6]$  $[4-6]$  to make sure that air quality standards and preventive measures reduce the undesirable change effect in many pollutants. As a consequence, using data of air quality networks is crucial to achieve the desired objectives.

Moreover, the validation and monitoring of sensor networks are very important steps. Generally, the research can be divided to evaluate the air quality monitoring network, according to the following techniques: process modeling, sensor Fault Detection (FD), sensor fault isolation, and correction [\[7\]](#page-9-4). In this work, the main purpose of this manuscript is to propose a new technique to improve the sensor FD phase. To ensure good public health,

air quality monitoring has been carried out by several techniques. In the literature  $[8, 9]$  $[8, 9]$  $[8, 9]$ , monitoring approaches can be divided into two significant categories: model-based and data-driven methods.

For process monitoring, model-based approaches always utilize the process model predictions to make decisions concerning the existence or absence of faults [\[10](#page-9-7)[–12\]](#page-9-8). However, several data-based monitoring methods have been developed in the literature [\[47\]](#page-10-0), such as principal component analysis (PCA) [\[13–](#page-9-9)[15\]](#page-9-10), independent component analysis (ICA) [\[16\]](#page-9-11), and partial least squares (PLS) [\[17,](#page-9-12) [18\]](#page-9-13). Several data-based monitoring methods, in the literature, have been used to construct models that can be often utilized in the process monitoring step. The data-based approaches to the monitoring and modeling of real applications, especially air quality networks, usually depend on the quality of used data. Especially, the PCA technique tries to extract linear relations among the considered variables and then represents them with orthogonal principal components. The PCA technique is particularly adapted to reveal linear relationships among the plant variables without formulating them explicitly, as indicated in [\[19,](#page-9-14) [20\]](#page-9-15).

However, the PLS, as a data-driven method, has shown good performances and has been widely used in modeling, monitoring, and diagnosis in many fields of chemistry, analytical, physical, and clinical chemistry, as well as the air quality system. The PLS method, which can extract relationships between two sets of variables, inputs/outputs, can build a linear learning model with linear latent variables (LVs) [\[21\]](#page-9-16). Unlike the PCA, which captures variations in input data with a descending order of variance, the PLS model finds an optimum pair of latent variables in the input data related to the output ones, such that these transformed variables have the largest covariance.

In this context, several extended PLS techniques have been proposed in the literature. The statistical process based on the PLS method has been frequently studied to have good detection results. In [\[22\]](#page-9-17), the authors suggested the monitoring methods with multiblock PLS models and showed as well the performance of the FD of the PLS technique. The authors of [\[23\]](#page-9-18) applied the recursive PLS algorithm in order to update the PLS model with the latest process data. Later, another method, called the total PLS model, was developed by Zhou et al. [\[24\]](#page-10-1) for output-relevant process monitoring.

From another perspective, the Kernel PLS (KPLS) approaches have become one of the simple, popular, elegant, and fast techniques at the level of the development of the soft measurement model for nonlinear systems relative to other nonlinear approaches [\[25–](#page-10-2)[27\]](#page-10-3). The KPLS method provides, at the same time, good monitoring performances by finding those LVs that present a nonlinear correlation with the response variables, besides improving model understanding. The main advantage of the KPLS method is that it does not involve any nonlinear optimization [\[28\]](#page-10-4) utilizing the kernel function or the stabilization problem, hence making it as simple as standard PLS.

For the KPLS method, the number of latent variables selected for KPLS may be larger than that for linear PLS. However, computation time (CT), selected for the KPLS method, may increase during the identification phase according to the number of samples for the storage of the symmetric kernel matrix of a KPLS monitoring model. To achieve the modeling and monitoring objectives, a new Reduced Kernel Partial Least Squares (RKPLS) method is developed to predict the concentrations of various pollutants and to help understand the modification of air quality networks. The main goal of this paper is to use the advantages of the KPLS technique by introducing it as a part of a new proposed method for air quality networks. Then, the suggested RKPLS method is carried out.

In summary, we develop the RKPLS technique that aims to enhance the data validation of air quality monitoring networks. In this study, the main principle is to treat the problem of CT and the storage of variables. The air quality is a real system that presents several variables. Thus, the treatment of these variables takes a long time. The aspect of the suggested method is to select, using a projection of all LVs, just the important variables. These selected variables consist in presenting a faster and even more effective monitoring process.

In the proposed method, we consider only the set of observations that approximate the retained important components to produce a reduced size of the kernel matrix. Nevertheless, for a large and complex system, our proposal is mainly based on a reduced Gram matrix, so the training time decreases rapidly with a reduced number of observations.

To overcome large datasets, a FD method is developed. The faults sensor or abnormal changes in measured air quality must be detected effectively and quickly using the detection index Squared Prediction Error (SPE). In this task, the FD method uses the SPE index and the Exponentially Weighted Moving Average (EWMA) to improve this phase. The FD performances of the developed RKPLS-based SPE technique and RKPLS-based EWMA-SPE technique are illustrated in terms of False Alarm Rate (FAR), Good Detection Rate (GDR), and CT.

The paper is outlined as follows. The concepts of PLS and KPLS are introduced in Section [2.](#page-2-0) In Section [3,](#page-3-0) the proposed RKPLS method is described. Next, Section [4](#page-4-0) details the selection of the kernel parameter principle using the Tabu search algorithm. In Section [5,](#page-5-0) the application results on an air quality monitoring process are given to illustrate the performance of the suggested reduced approach. The conclusion is presented in Section [6.](#page-9-19)

### <span id="page-2-0"></span>**2 Preliminary**

# **2.1 Standard PLS method**

First of all, we are interested in the basic PLS method, which is an extension of the proposed RKPLS method. The general principle is to extract, using the input and output data matrices, LVs to build a linear multivariable model.

The input data  $X = \begin{bmatrix} x_1, \ldots, x_N \end{bmatrix}^T \in \Re^{N \times m}$  contain *N* samples with *m* process variables and the output data  $Y = \begin{bmatrix} y_1, \ldots, y_N \end{bmatrix}^T \in \Re^{N \times J}$  comprise *N* observations with *J* quality variables.

In PLS, we project the input/output data in a lowdimensional space characterized by an *L* number of latent variables [\[29\]](#page-10-5). The PLS method decomposes the input and output data as follows:

$$
\begin{cases}\nX = TP^T + E \\
Y = UQ^T + F\n\end{cases} (1)
$$

where  $T = [t_1, t_2...t_l]$  and  $U = [u_1, u_2...u_l]$  are the score vectors,  $P=[p_1, p_2...p_l]$  and  $Q=[q_1, q_2...q_l]$  are the loadings for X and Y, respectively. Thus, the E and F matrices are, respectively, the PLS residuals of the input data X and the output data Y.

#### **2.2 Theory of the KPLS method**

#### **2.2.1 Kernel function**

Actually, systems have a nonlinear structure. Because of the limitation of the standard PLS for the nonlinear system, several methods have been developed. According to the trend and popular methods, the kernel technique has received a lot of attention [\[25,](#page-10-2) [30\]](#page-10-6).

The KPLS method is characterized by the kernel matrix (Gram matrix) which consists in building nonlinear latent components with an approximately linear computational cost.

Therefore, the main idea is to transform the nonlinear data (input and output) in a higher-dimensional space, called the feature space  $F$ , as illustrated in Eq. [2.](#page-2-1) In this case, the KPLS method is formulated in a feature space of traditional PLS to its nonlinear kernel form [\[31,](#page-10-7) [48\]](#page-10-8).

$$
\Phi: x_i \in \mathfrak{R}^N \to \Phi(x_i) \in F \tag{2}
$$

Furthermore, we cannot determine the nonlinear mapping of each observation from the batch process. A Mercer kernel  $k(.,.)$  is proposed to overtake this problem [\[32\]](#page-10-9). Equation [3](#page-2-2) <span id="page-2-2"></span>presents the product of two mapped samples to determine the kernel function:

$$
k(x_i, x_j) = \langle \Phi(x_i), \Phi(x_j) \rangle = \Phi(x_i) \Phi(x_j)^T
$$
 (3)

where  $\Phi(x_i) \in \mathbb{R}^{1 \times S}$ ,  $i = 1, ..., N$  and *S* is the dimension of the feature space.

In the literature, many kernel functions have been commonly defined and used. Table [1](#page-3-1) presents the different kernel functions where  $p$ ,  $\beta_0$ ,  $\beta_1$ , and *c* are determined using the cross-validation technique.

In a high-dimensional space and prior to calculation, the mean centering of the Gram matrix K must be performed, as presented by Eq. [4:](#page-2-3)

<span id="page-2-3"></span>
$$
K \leftarrow \left(I_n - \frac{1}{n} 1_n 1_n^T\right) K \left(I_n - \frac{1}{n} 1_n 1_n^T\right) \tag{4}
$$

where  $1_n$  is a vector of ones whose length is *N*, and  $I_n$  is an *N*-dimensional identity matrix.

### **2.2.2 KPLS function monitoring**

The PLS kernel algorithm was given by Lindgren et al. [\[33\]](#page-10-10) with a large number of samples. The Gram matrix  $K \in$  $\mathbb{R}^{N \times N}$  [\[34\]](#page-10-11) can be presented according to Eqs. [3](#page-2-2) and [4,](#page-2-3) as follows:

$$
K = \Phi(X)\Phi(X)^{T}
$$
 (5)

For nonlinear systems, a traditinal KPLS algorithm is given as follows:

#### **Algorithm 1** KPLS algorithm

**Input:** N×M input data matrix X and N×L output data matrix Y

**Output:** Input score matrices T, output score matrix U Step 1: Calculate kernel matrix and then center; Step 2: Set i=1,  $K_1 = K$ ,  $Y_1 = Y$ ; Step 3: Random initialized  $u_i$  equal to any column of  $Y_i$ ; Step 4:  $t_i = K_{i_m}^T u_i, t_i = t_i / ||t_i||;$ Step 5:  $c_i = Y_i^T t_i$ ; Step 6:  $u_i = Y_i c_i, c_i = c_i / || c_i ||;$ Step 7: If  $t_i$  converges, go to Step 7; else return to Step 3; Step 8: Deflate K and Y; Step 9: Repeat steps 3 to 6 to extract more latent variables; Step 10: Obtain cumulative matrices T and U.

<span id="page-2-1"></span>According to Algorithm 1, the deflation step is obtained by the rank-one reduction of K and Y [\[28\]](#page-10-4). Using a new T score vector, the K and Y matrices are deflated as:

$$
K = K - ttT - KttT + ttT KttT
$$
 (6)

$$
Y = Y - tt^T Y \tag{7}
$$

<span id="page-3-1"></span>

where  $I_n$  is an *N*-dimensional identity matrix.

After calculating the loadings and scores, the KPLS model is described as:

$$
\begin{cases}\n\widehat{Y} = KU(T^TKU)^{-1}T^TY \\
\widehat{Y}_t = K_tU(T^TKU)^{-1}T^TY\n\end{cases}
$$
\n(8)

where  $Y$  presents the prediction outputs of the training samples,  $Y_t$  is the prediction outputs of the testing samples, and  $K_t$  denotes the kernel matrix of the test samples.

# <span id="page-3-0"></span>**3 Suggested RKPLS method**

In many domains, large datasets have been presented. The training data, using the kernel method, has had a great success with an elegant treatment of data for monitoring systems. As a result, this number of observations must be stored in a memory.

Specifically, the KPLS technique presents a great disadvantage when the number of observations increases. This necessitates the use of large computer memory and training time [\[35\]](#page-10-12). Then, the learning time and CT for detection go up rapidly with the number of observations. Despite the fact that the KPLS technique solves the problem of nonlinearity, the calculation and memory problem that arise are posed for dynamic processes being monitored.

The dimensional kernel matrix (Gram matrix) is limited in this method  $[36, 37]$  $[36, 37]$  $[36, 37]$ .

The main goal of the proposed RKPLS method is to reduce CT. From *N* measurement variables defined by the data matrix, we just choose the important observations. In this case, we obtain a parameter number of the kernel matrix equal to the L number of the selected latent components.

As a first step, we consider Eq. [9,](#page-3-2) which consists in the approach of the latent variables  ${w_i}_{i=1..P}$  in the transformed input data  $\phi\left(x_{Latent}^{(j)}\right) \in \phi\{x^i\}_{i=1...M}$  in order to get, as a second step, the highest projection value [\[29\]](#page-10-5).

$$
\phi\left(x_{Latent}^{(j)}\right) = \alpha_j * k_j(x), \qquad j = 1, 2..L \tag{9}
$$

Generally, we can select the projection of all transformed data vectors  $\phi\{x^i\}_{i=1...M}$  from the latent variables  $w_j$  to

<span id="page-3-3"></span>obtain the most loaded samples in terms of information  $x_{Latent}^{(j)} \in \{x^{(i)}\}_{i=1...M}$ , as depicted in Eqs. [10](#page-3-3) and [11:](#page-3-4)

$$
\begin{cases}\n\phi\left(x_{Latent}^{(j)}\right)_j = \max_{i=1,..,M} \phi(x^i)_j \\
and \\
\phi\left(x_{Latent}^{(j)}\right)_{i \neq j} < \varsigma\n\end{cases} \tag{10}
$$

where  $\zeta$  is a given threshold.

Furthermore, the RKPLS method consists in determining the reduced dataset by choosing the variables that have the highest projection variance in the direction of the selected latent components.

Then, the reduced data matrix of  $\left\{ x_{Latent}^{(j)} \right\}_{j=1...L}$ can be defined by Eq. [11:](#page-3-4)

<span id="page-3-4"></span>
$$
X_r = \begin{bmatrix} x_{Latent}^{(1)} & x_{Latent}^{(2)} & \dots & x_{Latent}^{(L)} \end{bmatrix}^T
$$
 (11)

Consequently, the reduced data matrix  $X_r$  given a reduced kernel matrix  $K_r$  related to the kernel function  $k$ and the number of the selected variables is indicated in Eq. [12:](#page-3-5)

<span id="page-3-5"></span>
$$
K_r = \begin{bmatrix} k(x_1, x_1) & \dots & k(x_1, x_L) \\ \vdots & \ddots & \vdots \\ k(x_L, x_1) & \dots & k(x_L, x_L) \end{bmatrix} \in R^{L \times L}
$$
 (12)

The main algorithmic steps of the suggested RKPLS are shown in Algorithm 2 as follows:

#### **Algorithm 2** RKPLS algorithm

**Input:** N×M input data matrix X and N×L output data matrix Y

**Output:** Reduced input score matrices T, reduced output score matrix U

Step 1: Acquire an initial standardized block of training data  $\{x_i\}_{i=1..N}$  and scale them,

Step 2: Construct the kernel matrix K and scale it,

<span id="page-3-2"></span>Step 3: Project  $\{\phi_i\}_{i=1..N}$  on the component latent  $\{w_i\}$ and choose  $x_{Latent}^{(i)}$  which satisfies Eq. [10,](#page-3-3)

Step 4: Construct the reduced kernel matrix  $K_r \in R^{L \times L}$ following Eq. [12,](#page-3-5)

Step 5: Estimate the reduced KPLS model,

Step 6: Determine the control limits of the SPE chart present in the next section.

#### **3.1 FD indices**

The traditional PLS–based monitoring method uses, in general, the Hotelling's  $T^2$  and the SPE or the Q-statistic, which are expressed respectively in terms of Mahalanobis and Euclidian distances [\[38,](#page-10-15) [39\]](#page-10-16). Therefore, the process monitoring step of the nonlinear PLS version (KPLS and the proposed RKPLS) is similar to that used in the PLS method. The  $T^2$  statistic index is, usually, a way of measuring the projections of the observations in the feature space at various time samples  $[40]$ .  $T^2$  is calculated as illustrated in Eq. [13:](#page-4-1)

<span id="page-4-1"></span>
$$
T^2 = X^T \,\widehat{W}\,\widehat{\Lambda}^{-1}\,\widehat{W}^T\,X\tag{13}
$$

where the diagonal matrix containing the eigenvalues is defined by

 $\widehat{\Lambda} = diag(\lambda_1, \lambda_2, \cdots, \lambda_l)$ , and  $\widehat{W}$  is the weights matrix. The control limit is calculated for the  $T<sup>2</sup>$  index, utilizing the F-distribution, as follows:

$$
T_{\alpha}^{2} = \frac{l(N-1)}{N-l} F_{l,N-l,\alpha}
$$
 (14)

where  $\alpha$  is the significance level, l is the number of retained principal components, *N* is the number of observation in the dataset, and  $F_{l,N-l}$  is the Fisher *F* distribution.

On the one hand, the SPE index allows FD in the residual subspace. The essential goal is to detect a new event for a new observation [\[41\]](#page-10-18). Furthermore, the SPE is computed as the sum of squares of the residuals by the KPLS model. To ensure the FD of the kernel method, the SPE is usually used in this step. Then, this index is characterized by the sensibility to model errors and also the addiction to the retained number.

The SPE, obtained from PLS, is given by Eq. [15:](#page-4-2)

$$
SPE = \|X - \widehat{X}\|^2 = \|(I - \widehat{W}\widehat{W}^T)X\|
$$
\n(15)

In this case, the confidence limit is presented in the Eq. [16.](#page-4-3) This index is determined using the  $\chi^2$  distribution. The process is considered abnormally functioning for the SPE index if:

<span id="page-4-3"></span>
$$
SPE(k) > g\chi_{h,\alpha}^2\tag{16}
$$

where *g* and *h* are presented respectively by  $\frac{b}{2a}$  and  $\frac{2a^2}{b}$ . In this case, *a* is the estimated mean of the SPE and *b* is the variance of the SPE.

On the other hand, the EWMA can be applied to residues. The EWMA is used to improve the quality of the FD procedure and essentially reduce the FAR. This type of filter is considered to monitor variables in each data point. The EWMA chart presents many advantages. The performance of the EWMA is characterized by the ability to better detect small faults. Furthermore, the EWMA control limit consists in improving the detection abilities of small faults to the SPE chart [\[42\]](#page-10-19). The general expression of the EWMA applied to residues is given by:

$$
Z_i = \lambda \bar{X}_i + (1 - \lambda) Z_{i-1}, \quad i = 1..N \tag{17}
$$

where  $\lambda$  is chosen such that  $0 < \lambda \leq 1$ , *i* is defined as the sample number,  $\lambda$  is defined as the smoothing parameter,  $\overline{X}_i$  is defined by the average of the *i*th sample, and *Zi*−<sup>1</sup> depends on the past information. The initial value is initialized following the average of the preliminary samples.

#### **3.2 Flowchart of proposed method**

To detail the principle of the RKPLS method, a flowchart is shown in Fig. [1.](#page-5-1) The flowchart represents the necessary steps of the FD for the suggested RKPLS.

# <span id="page-4-0"></span>**4 Selection of kernel parameter using Tabu search algorithm**

#### **4.1 Principle**

<span id="page-4-2"></span>The kernel function is the core of the kernel method which helps it get an optimal solution. In general, the RBF kernel, as a nonlinear kernel function, is a reasonable first choice. Parameter  $\sigma$  is a key element of the RBF kernel and directly exerts considerable influence on the generalization ability of the KPLS method. The selection of the kernel function and the corresponding parameter are the key of KPLS. The *σ* parameter of the kernel function has an effect on the partitioning outcome in the feature space. If the value of *σ* is too large, it will lead to overfitting. If the value of *σ* is too small, it will lead to underfitting. In this part, we present an approach to select what is an optimal Gaussian kernel parameter to use when applying the proposed RKPLS technique. The optimal kernel parameter is defined as the one that can improve the fault detection performance. For many industrial applications, minimizing the false alarm rate may be the greatest performance criterion. Therefore, the choice of the Gaussian kernel parameter needs to be selected based on the given application. The Tabu search algorithm is applied to optimize the kernel parameter to use when applying the RKPLS algorithm.

#### **4.2 Initial solution**

In this study, the determination of the initial solution in the Tabu search algorithm is to optimize  $\sigma$  for the current RKPLS model. Firstly, an initialization solution is presented randomly. To reduce the search space referring

<span id="page-5-1"></span>**Fig. 1** Representation of



to the previous literature using the RKPLS model, it is recommended to introduce the constraints of parameter  $\sigma$ , which respectively attribute to the range  $\sigma \in [2^{-6}, 2^6]$ . The solution is computed by appending the nearest unused neighbor values of the parameter while improving the FD performance. The process is repeated until all the neighbors are visited.

# <span id="page-5-0"></span>**5 Application**

In this section, the RKPLS monitoring scheme is evaluated on the air quality network process.

# **5.1 Description of air quality monitoring**

AIRLOR, the air quality monitoring network located in Lorraine (France), consists of 20 stations located in rural, peri-urban, and urban sites. Each monitoring station, for this model, consists of a set of sensors for measuring the concentrations of pollutants: carbon monoxide (CO), oxides of nitrogen (NO and  $NO_2$ ) measured by the same analyzer, dioxide sulfur  $(SO_2)$ , and ozone  $(O_3)$  [\[38,](#page-10-15) [43\]](#page-10-20). On the other hand, some stations (more precisely seven stations) are dedicated to the recording of additional meteorological parameters. Figure [2](#page-5-2) shows an example of an air quality station.

<span id="page-5-2"></span>

**Fig. 2** Air quality monitoring station

#### **5.2 Air quality settings**

The air quality, in general, is a secondary pollutant produced by complex photochemical reactions between primary pollutants, more precisely the nitrogen oxides NO, *NO*2, and VOC emitted into the atmosphere [\[44,](#page-10-21) [45\]](#page-10-22). Then, the sensors, principally of the ozone concentration  $(O_3)$ and nitrogen oxides (NO and *NO*2), monitor and detect the functioning abnormalities. On the one hand,  $O_3$  is a secondary pollutant whose spatial distribution of the maximum values is rather homogeneous at our local scale. Whereas, the nitrogen oxides are primary pollutants which are more localized because their concentrations directly depend on the sources of emissions. Owing to its adverse health effects, tropospheric ozone has become one of the most studied topics in the recent decade. However, we can wonder about the performances of technical KPLS, which is the interest of the following section.

The air quality is produced through a complex series of reactions involving nitrogen oxides (*NO*<sup>2</sup> and NO) and volatile organic compounds (VOC) which are formed in the lower atmosphere by chemical reactions and secondary pollutants [\[44,](#page-10-21) [46\]](#page-10-23).

In turn, each monitoring station contains a set of sensors dedicated to measuring the following concentrations of pollutants: CO (carbon monoxide), NO and *NO*<sup>2</sup> (oxides of nitrogen),  $SO_2$ , and  $O_3$ , respectively [\[1\]](#page-9-0).

In this paper, we consider just six neighbor measurement stations. In this situation, matrix X contains 18 variables, respectively, named  $v_1$  to  $v_{18}$ , of  $O_3$  and nitrogen oxides  $(NO<sub>2</sub>$  and NO) collected from each station.

Furthermore, the essential purpose is to detect the functioning abnormalities of the sensors, principally those

of the nitrogen oxides (NO and  $NO_2$ ) and the ozone concentration  $O_3$ . Then, sensor faults, whose magnitude is approximately 20% of measurement for  $O_3$ , are simulated and 1080 samples are obtained.

To validate the two objective functions, the size and FAR, from the Tabu search algorithm, the optimal value of  $\sigma$  is equal to 25.37.

Nevertheless, the training data  $X_{training}$  has 200 samples, among 1080, and the same choice for the testing data *Xtest ing*. For the next simulation results, two fault scenarios representing two different types of faults are generated to show the performance of the developed FD method.

- For the first example, fault 1 is a step bias of the sensor measuring ozone  $O_3$  of variable  $v_7$ . The fault is introduced between instances 50 and 100. Figures [3](#page-6-0) and [4](#page-7-0) show the detection index SPE for this fault.
- For the second example, the sensor measuring the nitrogen oxides *NO*2, of the variable *υ*12, is assumed to be faulty with a step bias representing the fault 2. The fault is introduced between instances 150 and 200.

#### **5.3 Case 1: Fault in ozone <sup>O</sup><sup>3</sup>**

As a first try, we present a fault in ozone  $O_3$  for the station 3 in sample intervals of [50 to 100].

The FD results of the KPLS-based SPE and KPLS-based EWMA-SPE techniques are depicted in Fig. [3.](#page-6-0)

The FD results of the proposed RKPLS-based SPE and RKPLS-based EWMA-SPE techniques are illustrated in Fig. [4.](#page-7-0) More precisely, these figures represent, respectively, the time evolution of the SPE different indices and the evolution of the different EWMA-SPE indices.

<span id="page-6-0"></span>

**Fig. 3** Monitoring faults in ozone  $O_3$  using KPLS in sample intervals of [50 to 100]

<span id="page-7-0"></span>

**Fig. 4** Monitoring faults in ozone *O*<sup>3</sup> using proposed RKPLS in sample intervals of [50 to 100]

The compared performances of the suggested RKPLS for the air quality system in terms of FAR, GDR, and CT are summarized in Table [2.](#page-7-1)

The proposed RKPLS provides a reduced kernel matrix with 44 observations. According to Table [2,](#page-7-1) the suggested RKPLS method has a less FAR compared to the classical KPLS. To show the performance of the proposed RKPLS methods, we determine the CT of the different methods. However, the RKPLS-based SPE and RKPLSbased EWMA-SPE techniques show better FD results compared to the conventional KPLS-based SPE and KPLSbased EWMA-SPE techniques for the test of faults in ozone *O*3, as illustrated in Figs. [3](#page-6-0) and [4.](#page-7-0)

## **5.4 Case 2: Fault in nitrogen oxides (NO2)**

Here, we present a fault in the nitrogen oxides *NO*<sup>2</sup> for station 4 in sample intervals of [150 to 200]. To evaluate the obtained results, Fig. [5](#page-8-0) depicts the FD results of the KPLSbased SPE and KPLS-based EWMA-SPE techniques.

Afterwards, Fig. [6](#page-8-1) shows the FD results of the proposed RKPLS-based SPE and RKPLS-based EWMA-SPE techniques. These figures represent, respectively, the time evolution of the different SPE indices and the evolution of the different EWMA-SPE indices.

The detection results out of both simulated methods, KPLS and RKPLS, using the SPE and EWMA-SPE statistics in the failure condition are provided in Table [3.](#page-8-2)

The result of the application of the suggested RKPLS method to the air quality process is demonstrated in Figs. [5](#page-8-0) and [6.](#page-8-1) For this test, the FD results show also that the suggested RKPLS technique gives a GDR for a single fault in the nitrogen oxides  $NO<sub>2</sub>$  compared to the KPLS with some FAR.

Furthermore, Table [3](#page-8-2) shows that the proposed RKPLSbased SPE and RKPLS-based EWMA-SPE techniques provide better results compared to both conventional KPLSbased SPE and EWMA-SPE.

Finally, the reduced technique based on SPE and EWMA-SPE shows better fault detection performances

<span id="page-7-1"></span>

<span id="page-8-0"></span>

**Fig. 5** Monitoring faults in the nitrogen oxides *NO*<sup>2</sup> using KPLS in sample intervals of [150 to 200]

<span id="page-8-1"></span>

**Fig. 6** Monitoring a faults in the nitrogen oxides *NO*<sup>2</sup> using proposed RKPLS in sample intervals of [150 to 200]

<span id="page-8-2"></span>**Table 3** Summary of good detection rates, false alarm rates, and computation time for TEP data for case 2: fault in nitrogen oxides *NO*<sup>2</sup>

| Chart/fault detection metric | FAR $(\%)$ | GDR $(\%)$ | CT(s)  |
|------------------------------|------------|------------|--------|
| <b>KPLS-based SPE</b>        | 17.67      | 94         | 0.2263 |
| KPLS-based EWMA-SPE          | 15.33      | 95.58      | 0.2263 |
| <b>RKPLS-based SPE</b>       | 10.66      | 97.9       | 0.1368 |
| RKPLS-based EWMA-SPE         | 5.33       | 100        | 0.1368 |

with FAR, GDR, and also CT, as illustrated in Tables [2](#page-7-1) and [3.](#page-8-2)

# <span id="page-9-19"></span>**6 Conclusion**

To avoid the high levels of air pollution, in this paper, we have proposed a new fault detection method applicable to the air quality process monitoring using the RKPLS technique. To control the pollution rate and protect human health, a reduced KPLS method has been opted for. The purpose of this suggested method is to detect the functioning abnormalities of the sensors, principally those of the ozone concentration  $(O_3)$  and nitrogen oxides (NO and  $NO_2$ ). Afterwards, a reduced optimized RKPLS technique has been suggested in order to extend the advantages of the KPLS models to the air quality process.

This paper aims to improve RKPLS for fault detection. Nevertheless, the RKPLS-based SPE and RKPLS-based EWMA-SPE fault detection performances are assessed and compared to those of the classical KPLS-based SPE. Firstly, an optimal and reduced kernel parameter using the important latent components has been selected in order to enhance the use of the classical KPLS model. Secondly, the developed detection method has utilized, at the first time, the different indices of the SPE and then has combined the various indices of the SPE and EWMA to detect and modify the average residual of the air quality model. The developed RKPLS-based SPE method has shown improved FD at the level of FAR, GDR, and the CT, mostly, when compared to the KPLS-based SPE. However, using the EMWA, we get better FD results in all cases, compared to the methods based on the SPE. The RKPLS-based EMWA-SPE technique has indicated a slightly weak FAR. Furthermore, the performance of the RKPLS method is good compared to KPLS. To do that, the results have demonstrated the efficiency of the developed technique in terms of FAR, GDR, and CT compared with the conventional fault detection KPLS. The relevance of the suggested monitoring technique has been shown for fault detection on air quality monitoring network data.

In fact, the RKPLS method is suggested in a static version. For a dynamic nonlinear system, an online version can be proposed.

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