ORIGINAL ARTICLE

CAD/tolerancing integration: a new approach for tolerance analysis of non-rigid parts assemblies

A. Korbi¹ · M. Tlija¹ · B. Louhichi² · A. BenAmara¹

Received: 11 April 2018 /Accepted: 12 June 2018 /Published online: 28 June 2018 \odot Springer-Verlag London Ltd., part of Springer Nature 2018

Abstract

The tolerancing integration in CAD model is among the major interests of most mechanical manufacturers. Several researches have been established approaches considering the geometrical and dimensional tolerances on the CAD modelers. However, the hypothesis of rigid parts is adopted in the digital mock-up. Thus, several physical factors are neglected; especially the deformations. In this regard, this paper presents a model for considering both tolerances and deformations in CAD model. The dimensional and geometrical tolerances are taken into account by the determination of assemblies configurations with defects basing on the worst case tolerancing. The finite elements (FE) computations are realized with realistic models. A method for modeling the realistic mating constraints, between rigid and non-rigid parts, is developed. Planar and cylindrical joints are considered. The proposed tolerance analysis method is highlighted throughout two cases study: the first comprises planar joints and the second comprises cylindrical parts in motion.

Keywords $CAD \cdot GD&T \cdot Realistic mating \cdot Non-rigid component and tolerance analysis$

1 Introduction

The design of a mechanical assembly is a dynamic activity that is not limited to its geometric modeling. Thus, the design improvement requires the integration and the consideration of other technical approaches and disciplines for the analysis of assembly functional behavior to meet the standards and the functional requirement (FR). Several research studies approved the hypothesis of the need to consider tolerances in the calculation and the simulation stages of the product [\[1,](#page-9-0) [2](#page-9-0)]. However, the modeling of the assembly functional behavior requires the

 \boxtimes A. Korbi anis.Korbii@gmail.com

> M. Tlija tlija.mehdi@gmail.com

B. Louhichi borhen.louhichi@etsmtl.ca

- ¹ National Engineering School of Monastir, Mechanical Engineering Laboratory (LGM_ENIM), University of Monastir, 5019 Monastir, Tunisia
- ² National Engineering School of Sousse, Mechanical Laboratory of Sousse (LMS_ENISo), University of Sousse, 4023 Sousse, Tunisia

consideration of two factors: the geometrical and dimensional defects as well as the deformations caused by external loads. The above defects subsequently affect the FR and the efficiency of the assembly [\[3](#page-9-0)].This paper establishes a new CAD tool for tolerance analysis of non-rigid parts assemblies. The paper is organized as follows. First, a literature review of tolerancing methods of rigid and deformable parts are presented, followed by a synthesis section. Section [3](#page-2-0) describes the proposed tolerance analysis method of non-rigid parts assemblies. The method to define mating constraints between non-rigid and rigid parts is highlighted. Two case studies are given in Section [4](#page-5-0) to illustrate the validity of the proposed method. The conclusion and perspectives for this work are presented at the end.

2 State of the art

This paper can be positioned under the research works belonging to two themes: (1) Tolerancing of rigid parts; (2) Tolerancing of non-rigid parts.

2.1 Tolerancing of rigid parts

Based on models for the representation of a toleranced geometry [\[4](#page-9-0), [5](#page-9-0)], several studies contributed to the development of tolerancing approaches taking into account the tolerance stuck-up, such as the T-Map [\[6](#page-9-0)], the linearization of the transition matrix [\[7](#page-9-0)], and the domains [[8](#page-9-0)].Additionally, CAT tools, as independent packages or inserted in commercial CAD modelers, provide tolerance analysis and synthesis [\[9](#page-9-0)], e.g., tecnomatix variation analysis (VSA), 3-DCS integrated into Catia V5©, and mechanical advantage from Cognition Co [\[10\]](#page-9-0). These tools are based on the parametric approach as well as the worst case and the statistical tolerancing. An analyzed dimension (FR) is expressed with an algebraic function to quantify the relationships between CAD assembly dimensions. This mathematical function is exploited in a Monte Carlo simulation in order to analyze the sensitivities and to extract the variation contributors list according to their effects on the FR [[11\]](#page-9-0). The major limitations of these tools are the consideration of dimensional defects in most cases for tolerance analysis and the use of Monte Carlo method which is characterized by an important simulation time as well as the lack of a clear and automated strategy for the redefinition of assembly constraints. Zhu et al. proposed a new CAD method for tolerance analysis of rigid planar parts based on the Skin Model Shape (SMS) concept to represent a toleranced geometry [\[12](#page-9-0)].The new approach overcomes the limitations of (3DCS), a CAT tool incorporated into CATIA V5©, that consist on the use of SMS concept to represent dimensional variations or form defects in assembly [\[13\]](#page-9-0). Indeed, the authors improved SMS method by considering positional and orientation defects during the tolerancing process. The assembly process (assembly sequences (AS)) and the contact evolution between parts are neglected in the above models and tools. Thus, Anselmetti et al. [\[14\]](#page-9-0) and Dantan et al. [\[15\]](#page-10-0) proposed approaches considering these two aspects. This et al. [\[16\]](#page-10-0) and Louhichi et al. [[9\]](#page-9-0) established a model allowing the use of the assembly with defects in digital mock-up (DMU) for the inspection of the tolerance impacts on the FR during the assembly operation (parts motion). Jbira et al. improved the above model to consider form defects [[17](#page-10-0)].

2.2 Tolerancing of non-rigid parts

Liu et al. proposed a method for the tolerance analysis of an assembly of flexible sheets metal. In order to estimate the assembly FR, a mathematical model, called method of influence coefficients (MIC), is proposed in the case of sheets metal arranged together in series or in parallel configurations [\[18\]](#page-10-0). Subsequently, this model evaluates the deformations effects on the choice of individual components tolerances. Camelio et al. improved the above method by considering the case of multi-station compliant sheet metal assembly lines [\[19,](#page-10-0) [20\]](#page-10-0). In order to analyze the dimensional variations, the method considered part deviations, fixture variations, and tooling errors. Säderberg et al. presented an approach to investigate the impact of the spot welding position deviations on the geometrical quality of sheet metal assemblies [[21\]](#page-10-0). The

position defects of the spot welding are caused by parts geometrical variations, variation in the positioning of the parts to be assembled, and tooling errors. The CAT software, RD&T [\[22](#page-10-0), [23\]](#page-10-0), is used to conduct the simulation. Wärmefjord et al. established a control chart for monitoring the variations caused by deviations in the contact between parts and locators in the assembly fixtures [[24](#page-10-0)]. Lee et al. proposed a tolerance analysis approach by considering the weld distortion effects for precision control in ship block assembly process [\[25\]](#page-10-0). Hermansson et al. established a model for the control of the geometrical variations of flexible cables and hoses in automotive industry [\[26\]](#page-10-0). In order to avoid interference between the final assembly components, this method computed the optimal tolerance envelopes for each deformable part. Samper et al. presented a tolerancing approach useful in the case of hyper static mechanisms or assemblies with external loads [[27](#page-10-0)]. This approach considers the 3D elastic displacements of flexible components during the 3D tolerancing process through the using of four models. Mazur et al. presented a multiobjective tolerances analysis and synthesis tool. This process integration and design optimization (PIDO) platform considers an assembly subjected to loads [\[28\]](#page-10-0). PIDO integrates CAD/CAE and uncertainty quantification tools (Monte Carlo or expansion chaos polynomial (PCE)) [\[29\]](#page-10-0) as well as multiobjective genetic algorithms [[30\]](#page-10-0). Stuppy considered the deviation due to the deformation factor for tolerance analysis of a crank mechanism [\[31](#page-10-0)]. Jeang et al. developed a method for the statistical dimension and tolerance design for mechanical assembly under thermal impact [[32](#page-10-0)]. Pierre et al. considered thermos-mechanical strains in the strategy of tolerance analysis [\[33\]](#page-10-0). Irfan et al. used the FE simulation as a virtual tool to establish a model for tolerance allocation in assembly design [\[34](#page-10-0)]. Jayaprakash developed an optimal tolerance design approach for mechanical assembly considering both thermal impact and inertia [\[35](#page-10-0)]. Benichou et al. considered the thermal expansion of parts integrated within functional tolerancing [\[36](#page-10-0)]. Ting et al. improved the Jacobian torsor model to consider non-rigid parts for tolerances analysis and synthesis [[37\]](#page-10-0). The model computes the influence of several factors, e.g., gravity, temperature, and mounting stresses. Guo et al. established a tolerance analysis method considering geometrical deviations and parts deformations [\[38\]](#page-10-0).The geometrical defects are computed by homogeneous transformation matrix. The part deformations are deduced from FE simulation taking into account the normal and friction forces on the contact surface. An elastic contact model between planar surfaces of deformable parts is developed. The method is tested using an assembly of two machined parts.

2.3 Synthesis

Despite their importance as tools for tolerance analysis and synthesis of rigid part assemblies, the approaches presented in [\[4](#page-9-0)–[17\]](#page-10-0) do not satisfy the industrial needs to consider deformation factor in the tolerancing process. The methods in [\[18](#page-10-0)–[26\]](#page-10-0) investigated the assembly variation propagation of thin-wall parts such as automotive bodies. Those methods are limited to the cases of fixed and welding process and unusable with assemblies including other mechanical links as planar and revolute joints. Moreover, most of the methods developed in [\[18](#page-10-0)–[38\]](#page-10-0) using non-rigid parts for tolerancing are still limited since they are based on mathematical and statistical computations without a realistic representation of a toleranced geometry in CAD tools. The AS and the contact evolution during the assembly operation should be considered in the tolerance analysis step. Thus, this paper proposes a new CAD method for tolerance analysis of non-rigid parts assemblies while considering the geometrical defects and deformation impacts.

3 Tolerance analysis method of non-rigid parts assemblies

The developed method combines between several engineering disciplines such as CAD, the FE calculation, and tolerancing. Thus, this method is a multidisciplinary tool allowing the analysis of geometrical and dimensional tolerances. The flow chart in Fig. 1 presents an overview of the proposed method and the main steps are as following:

3.1 Extract CAD data

The CAD data are extracted from the assembly model while considering the following aspects as inputs:

The assembly sequence (AS) is deduced according the mating order specified in the tree of CAD feature manager.

- Functional requirement (FR): The FR is read from the assembly model.
- & Assembly sequence: The fixed component is considered as the assembly base. The joint type is determined according to the mating constraints linking each parts couple.

3.2 Generation of assembly components with geometrical and dimensional defects

This step is based on the model established by Tlija et al. [\[3](#page-9-0)] and Louhichi et al. [\[9](#page-9-0)]. In fact, the dimensional tolerances are taken into account by the representation of the components in two worst configurations: the maximum and the minimum material configurations. The geometric deviations between the ideal and realistic configurations of a part are defined by the small displacement torsor (SDT) and the worst case tolerance theory.

Form defects are neglected compared to those of position and orientation. All realistic configurations are generated by the modeling of the geometrical tolerances by the displacements of the corresponding faces. This task depends on the type of tolerance, the shape of the tolerance zone, and the tolerance value already assigned.

3.3 FE simulation of the most stressed component

This step focuses on the simulation of loads applied on the most stressed component in the assembly considered as nonrigid with dimensional and geometrical defects, using the FE computation. Using the results of the FE simulation, the extraction of the mesh nodes coordinates and the nodal displacements is established.

Fig. 1 Overview of the proposed method

3.4 Determination of points cloud of the deformed model

The final points coordinates of each deformed face are computed by adding the values of the displacements resulting from the FE calculation to the points coordinates of initial face (Eq. 1). This step is automated using visual basic for application (VBA) of Solidworks and MS Excel. In Eq. $1, [C_n]$ is the matrix of the final nodes coordinates of the deformed face, [D] is the matrix that contains the nodal displacements of the initial face after deformation and $[C]$ is the matrix of the initial nodes coordinates of a face (before deformation).

$$
[Cn] = [D] + [C]
$$
 (1)

3.5 Reconstruction of deformed faces

The above points cloud are triangulated and converted to stereolithography (STL) format using digitized-shape editor module of CATIAV5. The reference surface of each triangle is generated as described in Fig. 2. Thus, the deformed face is modelled by elementary faces.

3.6 Updating constraints of realistic assembly

The assembly of components with defects requires the update of the initial mates between parts while respecting an objective function of the assembly (OFA) specified by the designer. The OFA is deduced automatically from the nominal CAD assembly and comprises the following data:

- AS (scenario) order.
- The joint type.
- The direction corresponding to each AS.
- No-interference between components assembly.
- Contact between components.

Fig. 2 The reconstruction steps of a single deformed face of non-

In this paper, the developed method for updating mates is limited to the case of joint defined between planar or cylindrical faces of a couple of rigid parts (Rigid/Rigid (R/R))or between a rigid part and non-rigid one (rigid/non-rigid (R/NR)).

In nominal configuration, coincidence constraint between two nominal faces (Co: F&F) is considered. In realistic configuration, the above constraint is conserved or redefined according to the OFA. In the case of R/R joint, the sub-algorithm detailed in [[9](#page-9-0)] is used. In the case of R/NR joint, three mate types are defined as indicated in Fig. [3](#page-4-0), such as (n) is the number of the assembly constraints:

- Co: F1&F2: F2 is a reference plane defined by three triangulation vertices (non-aligned).Those vertices are the closest three points to the rigid face F1 according to the AS direction.
- Co: F1&E: The edge E is defined by two triangulation vertices closest to F1 according to the AS direction.
- Co: F1&V: The Vertex E is the closest to F1 according to the AS direction.

3.6.2 Case of assembly with cylindrical joint

In case of an assembly with cylindrical joint, the mating constraint between two nominal parts as a hole H and a pin P is generally provided by a coaxiality constraint between two ideal axes L_a and L_b (Co: $L_a \& L_b$), such as L_a and L_b are the nominal axes of the cylindrical surfaces H_a of H and P_b of P respectively. In the realistic configuration, two algorithms are developed to extract the new axes L'_{a} and L'_{b} respectively of the realistic surfaces H'_a and P'_b :

- The realistic axis L'_b of the pin is obtained basing on the oriented bounding box (OBB) of P'_b . The start and the end points of the axis L_b represent the centers of the most distant sides of the OBB (Fig. [4](#page-4-0)a).
- The realistic axis L'_{a} of the hole is determined using a sub-algorithm based on the concept of the feature operation (Association, Construction, etc.) of ISO-GPS standard [[39,](#page-10-0) [40](#page-10-0)] and using the steps in Fig. [5](#page-5-0) [\[41](#page-10-0)].
- \bullet After obtaining H'_a and P'_b, the coaxiality constraint in the nominal configuration (Co: $L_a \& L_b$) (Fig. [4](#page-4-0)b) can be replaced by a coincidence relation between two realistic

rigid part

Fig. 3 Sub-algorithm used to update mates in case of (R/NR) joint

axes L'_{a} and L'_{b} (Fig. 4c) or between the realistic axis L'_{a} and a vertex V on L'_b (Fig. 4d) according to OFA.

3.6.3 Constraints validation

The detection of the interferences and the contact between each components couple is necessary for the final validation of all constraints. Thus, the elementary triangular surfaces of a deformed face are particularly exploited for the detection of interferences between components in the realistic assembly (Fig. [6](#page-5-0)).

Without losing generality, the method used to establish the contact between two functional faces F_m and F_f of two

Fig. 4 a Determination of realistic axis of reconstructed cylindrical pin; b nominal cylindrical assembly; c realistic cylindrical assembly with (Co:L $\chi_a \& L'_b$; d realistic assembly with (Co: L'_{b} &V)

components, in the case of an assembly with planar joint, is based on the following steps:

- & According to AS, a first part is fixed and the second is considered as movable (Fig. [6a](#page-5-0). F_m and F_f are the realistic faces to be in contact of the movable and fixed parts respectively.
- Project Q_i points on a plan P according to AS direction, such as P is a tangent plan to F_f and Q_i ($i = 1$ to $n; n$ is the total number of points) are the triangulation vertices of F_m .
- Determine the closest points Q_m , among Q_i , to P according to AS direction. According to the type of coincident constraint, Q_m are three, two, or one vertices. Q_m are used to apply a coincident constraint with F_f .
- Evaluate the contact between components by measuring the distance between Q_m and F_f . In other words, Q_m must belong to the face F_f .

3.7 Check the respect of FR

This step allows the assembly tolerance analysis by measuring the value of FR in each realistic assembly configurations. If FR is not respected in one realistic configuration, then an optimization step must be carried out to correct initial component tolerances values.

3.8 Search for optimal tolerance values

In this step, the designer chooses the tolerance to be modified and an increment Δt . Generally, it is the less expensive tolerance. An iterative sub-algorithm is developed to optimize the tolerance values of parts. For each iteration, the FR is tested. The optimal tolerance allows the respect of FR in all realistic configurations.

Fig. 5 Sub-algorithm used to obtain the axis of a non-ideal cylindrical hole

4 Case study

4.1 Assembly with rigid joint

To validate the approach already developed, a first case study without allowed motion is illustrated in this section. An assembly, named RGB (Fig. [7\)](#page-6-0), is considered and composed of three planar parts:

- Part B in blue color considered as rigid perfect (without defects).
- Part R in red color considered as rigid with positional defect $(Tr = 0.2$ mm).
- Part G in green color considered as non-rigid part with positional defect (Tg = 0.3 mm).
- Two lateral locking parts assumed to be rigid and fixed on part B. Both lateral faces F1 and F2 of locking parts are in contact with faces Gl and Gr respectively.

A functional requirement $(J = 40^{\pm 0.25}$ mm) is defined between two faces Gb and B1. According to geometrical tolerances values and SDT, all realistic configurations with defects of parts G and R are obtained using Solidworks Application Programming Interface (API). The first column of Table [1](#page-6-0) shows initial mating constraints.

The most stressed part G is isolated and subjected to a FE study (elastic deformation) in order to simulate part loads. Nodal displacements of deformed faces G′f and G′b (corresponding to Gf and Gb respectively) are deduced. A sub-algorithm is developed using Solidworks API to automate the FE simulation while considering boundary conditions and loads (Table [2](#page-6-0)).

After the FE computation, the deformed faces Gf′ and Gb′ are reconstructed as described in steps 4 and 5 of proposed approach. Thirty-six assembly realistic configurations are deduced with the update of mating constraints. For example, the second column of Table [1](#page-6-0) shows the AS and constraints in the 21st realistic configurations. The coincident constraint initially between faces Rb and Gf is replaced either by a constraint Rb′&3V, Rb′&2V, or Rb′&V according to realistic configurations of parts, such as Rb′ is the realistic configuration of Rb and V is a vertex from Gf (V can be one, two $(2V)$, or three (3V) vertices).

4.1.1 Results analysis

The tolerance analysis, using the initial tolerance values ($Tg =$ 0.3 mm and $Tr = 0.2$ mm) and considering G part deformation, shows that J is not respected for some realistic configurations. This result validates our initial assumption considering the deformation impact of the tolerances attributed especially to non-rigid parts on the assembly operation. The new tolerance (Tg opt = 0.29 mm) of G part, computed using the subalgorithm of tolerances optimization, respects J with consideration of deformation factor and positional defects (Fig. [8\)](#page-7-0). In this case, the correction is equal to 0.01 mm. In the case of an assembly with a large number of components, the corrected error will certainly be more significant.

Fig. 6 a Detection of interferences between (R/NR) parts; b contact establishment

Fig. 7 Nominal RGB assembly

4.2 Assembly with parts motion

The second case study consists on an assembly comprising a set of cylindrical and planar parts (Fig. [9\)](#page-7-0).

The bolt is considered as non-rigid with coaxiality defect $(Tc = 0.6$ mm), the support part is assumed to be rigid with perpendicularity defect $(Td = 0.3 \text{ mm})$, and the wheel, fixed with the bolt, is considered as a rigid part without defects.

The FR of the assembly consist of keeping the clearances($e_1 > 0$ and $e_2 > 0$) between the wheel and the support in order to avoid all risk of contact or friction during the rotation of the wheel. The AS and the constraints of the assembly are illustrated in Table [3](#page-8-0).

The assembly used in this case study is dynamic: The bolt rotation causes the wheel rotation. The bolt is considered as the most stressed component in the assembly. Before applying the FE calculation, a stable static position of the bolt according to each specific geometric defect is required to predict the direction of the force due to the weight effect of the wheel on the non-rigid bolt (Fig. [10\)](#page-8-0). The restraints and loads used for the FE are follows: the face 8 is considered as a fixed feature and a force $(F = 200 \text{ N})$ is applied as shown in Fig. [10.](#page-8-0)

After the FE computation, the point's cloud of the deformed face 5 of the bolt are extracted and triangulated in order to reconstruct the realistic face 5′ as presented in Steps 5 and 6. The new axis L'_{R} of 5' is generated based on the OBB tool (Step 6). Sixteen realistic configurations are deduced by updating the mating constraints. The second column of

AS N°.	Constraints in nominal configuration	Constraints in 21st realistic configuration
	Co: Rbo&B9	Co: Rho&B9
$\mathfrak{D}_{\mathfrak{p}}$	$Co: R1\&F1$	Co: R1&F1
$\mathbf{3}$	Co: Rr&B8	Co: Rr&B8
4	Co: Gbo&B9	Co: Gho&B9
5	Co: Gl&F1	Co: Gl&F1
6	Co: Gf&Rb	Co: V&Rb'

Table 2 Boundary conditions and loads

Fig. 8 J values with initial and optimal tolerances.

Table [3](#page-8-0) illustrates the AS and the new constraints in the 10th realistic configuration, such as L'_{R} and L'_{B} are the realistic configurations of the axes L_R and L_B respectively.

For each worst case configuration of faces 4 and 5, deduced from SDT, e_1 and e_2 are computed during the wheel rotation. Table [4](#page-9-0) illustrates the values of e_1 min

Fig. 9 Drawing of the wheel—support assembly

Table 3 AS and constraints in nominal and 10th realistic configurations

$AS N^{\circ}$.	Constraint in nominal configuration	Constraints in 10th realistic configuration
	1.Co: $L_R & L_R$	1.Co: $L'_{R}\&L'_{R}$
2	$2.C_0$: 1&7	2.Co: 1&Vertex(V) ϵ 7
3	$3.Co: L_M&L_N$	$3.Co: L_M&L_N$
4	4.Co: 11&9	4.Co: $11\&9$
5.	5. Relative fixation (wheel & bolt)	5. Relative fixation (wheel & bolt)

and e_2 min corresponding the most critical rotation angle of the wheel.

4.2.1 Results analysis

The tolerance analysis, using the initial tolerance values ($Tc =$ 0.6 mm and $Td = 0.3$ mm) and considering the deformation effect of the non-rigid bolt, shows that FR ($e_1 > 0$ and $e_2 > 0$) is not respected for the majority of the realistic configurations (Table [4](#page-9-0)).

By applying the iterative process, the tolerance value Tc is modified and becomes equal to 0.30 mm. Using the above tolerance, the new values of clearances $(N.e₁min$ and N.e₂min) are computed for each worst case configurations of components. Table [4](#page-9-0) shows that the FR is respected for all configurations with consideration of deformation factor and geometrical defects.

5 Conclusion

In this paper, a new CAD approach for considering non-rigid parts in tolerance analysis is presented. Geometrical defects are taken into account by the determination of the worst case

Fig. 10 Determination of the force direction applied to the bolt according to each initial geometric defect in the worst case

Table 4 Checking the respect of FR (Tc = 0.6 mm and $Td = 0.3$ mm) and N.FR $(Tc = Td = 0.3$ mm)

configurations of assembly components. The deformation simulation, using a model with geometrical deviations, allows to estimate the tolerances impact on part displacements. The reconstruction of deformed part faces contributes to obtain deformed models with geometrical defects. The determination of assembly realistic configurations requires the development of a new strategy to update mating constraints, while respecting assembly sequences. The assembly of the above parts permits the quantification of the effects of both tolerances and deformations on function requirement during the assembly operation. An iterative algorithm is developed to obtain adequate tolerances. The proposed model is a decision support tool integrated into DMU commonly used in industry. The majority of the steps are automated contributing to a simple use of the method, in spite of the fact that the runtime increases according to parts and specifications number. The approach is being improved to be applied on complex assemblies inspired from the industrial environment. Future research works will be interested in the consideration of the form defects on the CAD model through another type of tolerancing approach.

Publisher's Note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

References

- 1. Tsai JC (2007) Stiffness variation of compliant devices due to geometric tolerancing, in Proceedings of CIRP conference on computer aided Tolerancing , Erlange,Germany
- 2. Benichou S, Anselmetti B (2011) Thermal dilatation in functional tolerancing. J Mech Mach Theory 16:1575–1587
- 3. Tlija M, Louhichi B, Benamara A (2013) A new method for tolerance integration in CAD model. In: Proceedings of the International Conference on Control Engineering and Information Technology, Sousse,Tunisia, pp. 46–51
- 4. Pino L (2000) Modeling and kinematic analysis of geometric tolerances for the assembly of mechanical systems, Ph.D Thesis, The Central school of Nantes ,France
- 5. Sobh TM, Henderson TC, Zana F (1999) Tolerance representation and analysis in industrial inspection. Journal of Intelligent Robot System Theory Appl 24:387–401
- 6. Sellakh R, Sellem E, Riviere A (2000) Specification and simulation of geometric imperfections in CAD/CAM. Mech Ind 1:365–372
- 7. Davidson JK, Shah JJ (2013) Using Tolerance-Maps® to represent material condition on both a feature and a datum, The 8th International CIRP Seminar on Computer Aided Tolerancing , Charlotte, North Carolina ,USA , , pp 92–101
- 8. Franciosa P (2009) Modelling and simulation of variational rigid and compliant assembly for tolerance analysis, Ph.D Thesis, The university Naples Federico II ,Italia
- 9. Louhichi B, Tlija M, BenAmara A, Tahan A (2015) An algorithm for CAD tolerancing integration: generation of assembly configurations according to dimensional and geometrical tolerances. Comput Aided Des 62:259–274
- 10. Shen Z, Ameta G, Shah JJ, Davidson JK (2005) A comparative study of tolerance analysis methods. J Inf Sci Eng 5: 247–256
- 11. Prisco U, Giorleo G (2002) Overview of current CAT systems: review article. Integr Comput-Aid E 9:373–387
- 12. Schleich B, Anwer N, Zhu Z, Qiao L, Mathieu L, Wartzack S (2014) Comparative study on tolerance analysis approaches. The International Symposium on Robust Design, Copenhagen, pp 29– 39
- 13. Zhu Z, Qiao L, Anwer N (2016) An improved tolerance analysis method based on skin model shapes of planar parts. The 9th CIRP conference on Digital Enterprise Technology - Intelligent Manufacturing in the Knowledge Economy Era, Nanjing, China, pp 237–242
- Anselmetti B (2006) Generation of functional tolerancing based on positioning features. Comput Aided Des 38:902–919
- Monte Carlo simulation. Comput Aided Des 41:1–12 16. Tlija M, Louhichi B, BenAmara A (2013) Evaluating the effect of tolerances on the functional requirements of assemblies. Mech Ind 14:191–206
- 17. Jbira I, Tlija M, Louhichi B, Tahan A (2017) CAD/tolerancing integration: mechanical assembly with form defects. Adv Eng Softw 114:312–324
- 18. Liu SC, Hu SJ, Woo TC (2007) Tolerance analysis for sheet metal assemblies. J Mech Des 118:62–67
- 19. Camelio J, Hu SJ, Ceglarek D (2003) Modeling variation propagation of multi-station assembly systems with compliant parts. J Mech Des 125:759–790
- 20. Hu SJ, Camelio J, Arbor A (2006) Modeling and control of compliant assembly systems. CIRP Ann Manuf Technol 55(1):19–22
- 21. Söderberg R, Wärmefjord K, Lindkvist L, Berlin R (2012) The influence of spot weld position variation on geometrical quality. CIRP Ann Manuf Technol 61(1):13–16
- 22. Rosenqvist M, Falck A, Lindkvist L, Söderberg R (2014) Geometrical robustness analysis considering manual assembly complexity. The 5th CIRP Conference on Assembly Technologies and Systems, Dresden, Germany, pp 98–103
- 23. RD&T webpage 2013–10–09. [Online]. Available: [http://www.](http://www.rdnt.se) [rdnt.se](http://www.rdnt.se)
- 24. Wärmefjord K, Carlson JS, Söderberg R (2016) Controlling geometrical variation caused by assembly fixtures. J Comput Inf Sci Eng 16(1):11007
- 25. Lee J, Choi W, Kang M, Chung H (2015) Tolerance analysis and diagnosis model of compliant block assembly considering welding deformation. World Maritime Technology Conference, Korea
- 26. Hermansson T, Carlson J, Björkenstam S, Söderberg R (2012) Geometric variation simulation and robust design for flexible cables and hoses, In Proceedings of 12th CIRP Conference on Computer Aided Tolerancing, Huddersfield, UK
- 27. Samper S, Giordan M (1998) Taking into account elastic displacements in 3D tolerancing: models and applications. J Mater Process Technol 78:156–162
- 28. Mazur M, Leary M, Subic A (2011) Computer aided tolerancing (CAT) platform for the design of assemblies under external and internal forces. Comput Aided Des 43:707–719
- 29. Mazur M, Leary M, Subic A (2015) Application of polynomial chaos expansion to tolerance analysis and synthesis in compliant

assemblies subject to loading, J Mech Des vol. 137, Paper No: MD-14-300, <https://doi.org/10.1115/1.4029283>

- 30. Geetha K, Ravindron D, Siva Kumar M, Islam MN (2013) Multiobjective optimization for optimum tolerance synthesis with process and machine selection using a genetic algorithm. Int J Adv Manuf Technol 67:2439–2457
- 31. Stuppy J, Meerkamm H (2009) Tolerance analysis of a crank mechanism by taking into account different kinds of deviations. In: Proceedings of the 11th CIRP international seminar on computer aided tolerancing , Annecy, France, pp 26–27
- 32. Jeang A, Hwan CL, Chen TK (2002) A statistical dimension and tolerance design for mechanical assembly under thermal impact. Int J Adv Manuf Technol 20:907–915
- 33. Pierre L, Teissandier D, Nadeau JP (2009) Integration of thermomechanical strains into tolerancing analysis. Int J Interact Des Manuf 3:247–263
- 34. Irfan AM, Neal PJ (2004) Framework of an integrated tolerance synthesis model and using FE simulation as a virtual tool for tolerance allocation in assembly design. J Mater Process Technol 150: 182–193
- 35. Jayaprakash G, Thilak M, Sivakumar K (2014) Optimal tolerance design for mechanical assembly considering thermal impact. Int J Adv Manuf Technol 73:859–873
- 36. Benichou S, Anselmetti B (2011) Thermal dilatation in functional tolerancing. Mech Mach Theory 46:1575–1587
- 37. Ting L, Yanlong C, Jing W, Jiangxin Y (2016) Assembly error calculation with consideration of part deformation. The 14th CIRP Conference on Computer Aided Design, Gothenburg, Sweden, pp 58–63
- 38. Guo J, Li B, Liu Z, Hong J, Wu X (2016) Integration of geometric variation and part deformation into variation propagation of 3-D assemblies. Int J Prod Res 54:5708–5721
- 39. Sivasankar S, Jeyapaul R, Kolappan S, Shaahid N (2012) Procedural study for roughness, roundness and waviness measurement of EDM drilled holes using image processing technology. Comput Model New Technol 16:49–63
- 40. Srinivasan V (2001) An integrated view of geometrical product specification and verification. In Proceedings of the 7th CIRP Intenational seminars on computer aided tolerancing, Cachan, France, pp. 1–11
- 41. Jacquelin J (2011) 3-D Linear Regression [Online]. Available: <https://fr.scribd.com/doc/31477970/Regressions-et-trajectoires-3D>