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Minimization of turning time for high-strength steel with a given surface roughness using the Edgeworth–Pareto optimization method

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Abstract High-strength steels are used in various civilian and military products. The initial cost of the raw materials for these products is very high. The surface roughness of these products is extremely important during the finishing pass to be accepted during the final inspection. The surface roughness should conform to the required values stated on the design drawing. The paper presents the results of experiments in turning of high-strength steel featuring three factors—cutting speed *V*, feed rate

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f, and depth of cut t—on five levels (125 specimens). These were divided into 25 groups. Each of the five groups was subjected to one common machining speed. Each group was machined using five levels of cutting depth. Each depth was processed using five levels of feed rate. Tessa was used for examination of surface roughness. There is little modern research on machining high-strength steel. The high cost of this material compels us to look for the optimum turning conditions to provide for the specified roughness of surface Ra and the minimum machining time of unit volume T_m . As a result of our study, an artificial neural network was designed in Matlab on the basis of the MLP 3-10-1 multilayer perceptron that allows us to predict Ra of the workpiece with $\pm 2.14\%$ accuracy within the range of the experimental cutting speed, depth of cut, and feed rate values. For the first time, a Pareto frontier was obtained for Ra and T_m of the finished workpiece from high-strength steel using the artificial neural network model that was later used to determine the optimum cutting conditions. It is possible to integrate the suggested optimization algorithms into computer-aided manufacturing using Matlab.

Keywords Artificial neural network · High-strength steel · Turning operation · Optimization · Edgeworth–Pareto method · Surface roughness · Data mining

Nomenclature

d	Diameter of cut (mm)
l	Length of parts (mm)
α	Back angle (⁰)
k _r	Cutting edge angle $(^{0})$
r _o	Nose radius (mm)
V	Cutting speed (m/min)
t	Depth of cut (mm)
f_z	Feed rate (mm/rev)

DM	Decision maker
ΜA	number of criteria
$I = \{1, 2, \dots, m\}$	A set of criteria numbers
X	A set of possible decisions
$f = (f_1, f_2, \dots, f_m)$	Vector-valued criterion
$Y = \mathbf{f}(X)$	A set of possible vectors (estimates)
R_m	Euclidean space of m-dimensional
	vectors with real components
$\succ X$	Preference relation of DM specified
	in the set X
$\succ Y$	Preference relation of DM, induced
	on the set with $\succ X$ ratio and specified
	in the set Y
\succ	Relation $\succ Y$ continued in the entire
	space R_m
\succ SelX	A set of selected decisions
SelY	A set of selected vectors (estimates)
NdomX	A set of non-dominated decisions
<i>N</i> dom <i>Y</i>	A set of non-dominated vectors (estimates)
$P_f(X)$	A set of Pareto optimal decisions
P(Y)	A set of Pareto optimal vectors
	(Pareto optimal estimates)
$f_1(Ra)$	Surface roughness (µm)
$f_2(Tm)$	Machining time of unit volume in
	one cutting tool pass (min/cm ³)
Ra _i	Surface roughness for current V, t and
	f_z parameter combinations (µm)
Ra max	Maximum surface roughness value of
	all the V, t and f_z combinations (µm)
Tm_i	Machining time of unit volume for current
	V, t and f_z parameter combinations
	(min/cm ³)
Tm_{max}	Maximum machining time of unit volume
	value of all the <i>V</i> , <i>t</i> and f_z combinations
	(min/cm ³)

1 Introduction

Turning is commonly used to produce parts in many industries, such as machinery, automobiles, and machine tools. One of the main indicators of the surface quality of finish turning is surface roughness. High-strength steels are used in the production of high-pressure vessels that require ultra-precision turning. Examples of these high-pressure products include gun barrels, food sterilization equipment, high-precision sintering dies, hypersonic (up to Mach 16) wind tunnels, water jet cutting nozzles, and turbine casings for efficient power generation. Due to the limited resources in the modern world, efficient and rational utilization of resources stands out as an urgent task. Thus, developing resource-saving technologies, including for turning operations, is a crucial point of interest. In the case of machining essential components fabricated from high-strength steel, minimizing the surface roughness Ra and maximizing the machining time of unit volume is a very important task to ensure the production of products with better surface quality using the minimum resources. In anticipation of the next sixth technology revolution, it is becoming an increasingly important technique for processing large data sets using artificial intelligence and the integration of artificial intelligence algorithms in automated production.

Many previous investigations have been devoted towards developing prediction models for rough turning [1-19]. Risbood et al. [1] researched and produced models for forecasting roughness and dimensional deviation for dry and wet turning of mild steel rods. Bajić et al. [2] investigated the effect of cutting speed, feed rate, and depth of cut on the surface roughness and cutting force components in longitudinal turning. For the model predictions of surface roughness, regression analysis and neural networks were used. Muthukrishnan and Davim [3] anayzed the turning of Al/SiC-MMC using ANOVA and artificial neural networking (ANN) to develop prediction models of surface roughness. In a study by Ali and Dhar [4] and with the help of artificial neural networks, a prediction model of surface roughness and tool wear was derived. Pontes et al. [5] provided an overview on the use of artificial neural networks to simulate the surface roughness for various types of machining. Natarajan et al. [6] reported the turning of brass C26000 material and the deduced prediction model of surface roughness using artificial neural network (ANN) based on Matlab. Svalina et al. [7] analyzed the effect of the depth of cut, feed rate, and speed on the surface roughness, which is predicted by using neural networks. Abdullah et al. [8] reported a model for predicting surface roughness obtained by turning AISI 4140 steel using ANN and the Taguchi method. Pontes et al. [9] presented a study on the applicability of the radial basis function (RBF) neural networks to predict surface roughness (Ra) in the process of turning SAE 52100 hardened steel, using orthogonal arrays, where Taguchi was implemented as a tool for the development of the network parameters. Asiltürk [10] proposed a model with a standard error of 0.002917120% for predicting the surface roughness of AISI 1040 steel material using artificial neural networks (ANN) and multiple regression model (MRM). Upadhyay et al. [11] used vibration signals to predict surface roughness during turning of Ti-6Al-4 V by applying multiple regression and an artificial neural network model. Ahilan et al. [12] developed a model predicting power consumption and

surface roughness when turning workpieces of AISI 304. Azam et al. [13] investigated the relationship of average surface roughness and processing parameters (feed, speed and depth of cut) for turning highstrength low-alloy steel (AISI 4340). Acayaba and Escalona [14] developed a model for predicting surface roughness in low speed turning of AISI316 austenitic stainless steel using multiple linear regression and artificial neural network techniques. Al Bahkali et al. [15] studied the effect of feed, cutting depth, radius of curvature of the tool tip and the cutting speed on surface roughness in turning cast iron. Mia and Dhar [16] developed an artificial neural network (ANN) model to predict the average surface roughness in turning hardened steel EN 24 T. Jurkovic et al. [17] compared three machine learning methods for predicting the high-speed turning observed parameters (surface roughness (Ra), cutting force (Fc), and the tool life (T)). Tootooni et al. [18] reported surface roughness using a noncontact measurement method during the turning process. Abbas [19] analyzed the effect of the feed rate, depth of cut and cutting speed on the surface roughness in turning high-strength steel. Though all the previously mentioned research [1–19] provided prediction models of surface roughness, they failed to solve the problem of determining the optimal cutting parameters for the minimum surface roughness and maximum production rate.

However, many other previous works have focused on the determination of the optimal cutting conditions for different objectives [20-27]. Zuperl and Cus [20] described a method for optimizing multi-purpose turning cutting conditions with the help of neural networks aimed at increasing productivity and reducing costs, and providing an acceptable surface roughness. Senthilkumaar et al. [21] derived a mathematical model and ANN model for tool wear and surface roughness Ra for turning heatresistant super alloy Inconel 718 material. Optimal processing parameters were selected using the Pareto chart. Zinati and Razfar [22] derived prediction models for cutting conditions that ensure minimal surface roughness for longitudinal turning (turning long parts) of X20Cr13. Jafarian et al. [23] investigated three separate neural networks in order to minimize the surface roughness and maximize tool life in the turning. Mokhtari Homami et al. [24] reported optimal values of flank wear and surface roughness with the use of neural networks for turning Inconel718 superalloy components. Tamang and Chandrasekaran [25] used artificial neural networks for optimal cutting conditions, ensuring minimum values of surface roughness and tool wear on the rear surface for turning Al/SiCp MMC. Sangwan et al. [26] used artificial neural networks (ANN) and genetic algorithm (GA) to

obtain the optimum processing parameters leading to minimal surface roughness when turning a titanium alloy Ti-6Al-4 V. Gupta et al. [27] focused on the optimization of the process parameters of turning operations, namely surface roughness, the back surface of tool wear and power consumption. However, in the abovementioned research [20–27] the task of finding the optimum cutting conditions is one-sided, taking into account only the surface roughness without its relationship to the productivity and machining time of unit volume, which does not present the optimum handling of an expensive material such as high-strength steel.

Now, we consider the work focused on the determination of optimal parameters for turning with multi-objective optimization [28-31]. Basak et al. [28] discussed two types of Pareto optimization: minimizing the production time and minimizing the cost of processing, while the surface roughness was considered as a limiting parameter. Karpat and Özel [29] used neural networks based on multi-objective Pareto optimization modes for longitudinal turning of hardened AISI H13 steel. Two optimization criteria were investigated: the minimization of surface roughness values and maximization of performance in terms of longer tool life and material removal rate, while the second criterion was devoted to minimizing the processing-induced stress on the surface and minimum surface roughness. Yue et al. [30], based on multiobjective Pareto optimization for hard turning of die steel Cr12MoV, established a relationship between surface roughness, thickness of the plastic deformation zone, and cutting modes. Abbas et al. [31] studied the turning parameters for a heat-treated steel alloy (J-Steel) through multi-criteria optimization with the help of Pareto optimization. The work reported the cutting parameters that provided the minimum surface roughness and machining time needed to remove a unit volume. It can be concluded that the most effective approach to solving multiobjective optimization is the Pareto method. However, of the references mentioned here [28-31], none have considered multi-criteria optimization for the turning of highstrength steel, which is a material that is widely used in critical applications where there are stringent requirements on surface quality. Besides, due to the high cost of this material, it should be guaranteed to ensure the desired machined surface roughness value along with the minimum amount of processing time to promote productivity.

Thus, the aim of this study is to determine the turning conditions for high-strength steel while providing the minimum machining time of unit volume T_m and the required value of surface roughness Ra by using an artificial neural network-based model for prediction of these parameters.

2 Materials and methods

The chemical composition and mechanical properties of highstrength steel used in the current study are shown in Tables 1 and 2, respectively. This type of steel belongs to British Military of Defense (defense standard number:10–13/3 (2012)). The heat treatment for the material involved austenitizing at 900 °C for 5 h, air cooling, heating at 880 °C for 5 h, quenching in oil, and finally tempering at 590–600 °C for 8 h, followed by air cooling. The hardness measured was about HV 410 ± 10.

The test specimen had an initial diameter d of 50 mm and a length of 120 mm. Thirty millimeters was used for chuck clamping and 10 mm for clearance grooving and 60 mm will be used for applying the test experiment. A standard conical center was created for supporting the center of the tail stock.

The EMCO Concept Turn lathe 45 CNC equipped with Sinumeric 840-D was used to conduct the experimental work (Fig. 1).

The uncoated tungsten carbide insert was clamped with the tool holder to carry out this experiment. The specifications for the insert and tool holder are SVJCL2020K16 and VCMT160404 (back angle $\alpha = 7^{\circ}$, cutting edge angle $k_r = 75^{\circ}$, nose radius $r_o = 0.4$ mm). The surface roughness was measured and reported for a length of 50 mm, and evaluated using the surface roughness tester Tessa (Fig. 2). All the cutting parameters were controlled via the CNC part program [19].

To ensure a richly dense exploration of the adjustable space of the cutting parameters, a five-level full factorial design of experiments (total of 125 test conditions for three study parameters) was adopted. Listing of the factor levels for the study parameters is provided in Table 3.

For efficient experimentation, the 125 samples were divided into five primary groups (with the same cutting speed for each primary group), each of which was divided into five sub-groups (each having the same depth of cut). A full listing of all the resulting measured surface roughness values is provided in the Section 4.

3 The strategy for determining the optimum conditions

To achieve our objective, it is necessary to build an artificial neural network-based model of turning based on experimental data [32–34] and solve the optimization

 Table 1
 Chemical composition of the high-strength steel material

Element	С	Si	Mn	Ni	Cr	Mo	V	S	Р
%	0.32	0.23	0.64	3.02	0.96	0.48	0.12	0.002	0.004

 Table 2
 Mechanical properties of the high-strength steel work piece

Elastic modulus, <i>E</i> , GPa	0.2% yield strength, MPa	Ultimate tensile strength, MPa	Area reduction, %	Elongation, %
206	1114	1195	59	9.3

problem in a multi-criteria environment using the Edgeworth and Pareto method [28–31, 35–38].

The strategy for determining the optimum conditions is realized in five steps:

Step one

Set the optimization criteria, define the limitations and boundary conditions. Define the vector space of the problem being solved.

• Step two

Using the data mining approach [39–42], carry out three variables functions approximation based on experimental data with the help of the neural network.

• Step three

Determine the Pareto frontier: the set of Pareto optimal decisions and the set of Pareto optimal estimates.

• Step four

Using the expert assessment method, narrow the scope of Pareto optimality to Pareto non-dominated decisions.

• Step five



Fig. 1 Test rig for machining samples



Fig. 2 Test rig measuring surface roughness

Apply the decision-maker's direct questioning to establishing a set of selected decisions that may only contain a single optimum decision with a single estimates vector.

The strategy for decision-making in a multi-criterion selection problem is presented in Fig. 3 and the correlation of vector estimate sets is presented in Fig. 4. The nomenclature used in the charts and later on is the same as in [43]: DM—decision maker; *m*—the number of criteria; I = $\{1, 2, ..., m\}$ —a set of criteria numbers; X - a set of possible decisions; $f = (f_1, f_2, ..., f_m)$ - vectorvalued criterion; Y = f(X)—a set of possible vectors (estimates); R^m —Euclidean space of m-dimensional vectors with real components; \succ_X —preference relation of DM specified in the set X; \succ_{Y} —preference relation of DM, induced on the set with \succ_X ratio and specified in the set Y; \succ -relation $\succ_{\rm Y}$ continued in the entire space R^m; Sel X—a set of selected decisions; Sel Y—a set of selected vectors (estimates); Ndom X-a set of nondominated decisions; Ndom Y-a set of non-dominated vectors (estimates); P_f (X)—a set of Pareto optimal decisions; P(Y)-a set of Pareto optimal vectors (Pareto optimal estimates).

 Table 3
 Factor levels of the full factorial experimentation

Factor/factor level	Cutting speed, V (m/min)	Depth of cut, <i>t</i> (mm)	Feed rate, f_z (mm/rev)
1	75	0.1	0.025
2	100	0.2	0.050
3	125	0.3	0.100
4	150	0.4	0.150
5	175	0.5	0.200

4 Results and discussion

Besides surface quality, the problem of minimizing resource consumption becomes very important in finish turning of expensive high-strength steel. It is crucial to provide the minimum machining time of unit volume T_m and minimum surface roughness Ra at the same time. That is why these two criteria are the most important for finding the optimum machining parameters.

The results of experiments are presented in Tables 4, 5, 6, 7, and 8. Surface roughness (Ra, μ m) was established experimentally, and the second criterion (machining time of unit volume, Tm, min/cm³) was calculated with the following formula:

$$T_m = \frac{1000}{V \cdot t \cdot f_z} \cdot \tag{1}$$

Thus, on the researcher level, the first three steps were implemented.

The optimization problem was solved using the five-step strategy presented earlier.

4.1 Formulation of the optimization problem—step 1

Based on the research objective, the following criteria in turning of the cylindrical workpiece were established: f_1 —surface roughness, Ra, μm ; f_2 —machining time of unit volume in one cutting tool pass, T_m , min/cm³, that is, m = 2. Relatively, a set of possible Y estimates in the two-dimensional space R^2 forms the vectors $f = (f_1, f_2)$. The search is performed for a set of estimates having the minimum sum of vector lengths throughout the entire range of the criteria values changes. For this purpose, it makes sense to present them in a dimensionless form with the index "1" assigned to the maximum actual numbers.

Variable parameters and limitations of the optimization problem were set in accordance with the table of experimental data (see Table 3): $x_1 = [75-175]$ —cutting speed, V, m/min; $x_2 = [0.1-0.5]$ —depth of cut, t, mm; $x_3 = [0.025-0.20]$ —feed per revolution, f_z , mm per rev.

For the optimization procedure, dimensionless surface roughness f_1 (Ra^*) and machining time of unit volume f_2 (T_m^*) (Tables 4, 5, 6, 7, and 8) were calculated using the following formulae:

$$Ra^* = \frac{Ra_i}{Ra_{\max}};$$
(2)

Fig. 3 The decision tree in the multi-criterion selection problem

 $T_m^* = \frac{T_{mi}}{T_{mmax}},$

where Ra_i —surface roughness for current V, t and f_z parameter combinations; Ramax-maximum surface roughness value of all the V, t and f_z combinations; $T_{mi}T_{mi}$ -machining time of unit volume for current V, t and f_z parameter combinations; T_{mmax} —maximum machining time of unit volume value of all the V, t and f_z combinations. The length of estimates vector f was established with the Pythagorean theorem using dimensionless criteria f_1 and f_2 .

(3)

The problem boundary condition was that all variables can take any non-negative values.

Since the criterion of the machining time of unit volume T_m^* was calculated, in the second stage of our strategy, the function of surface roughness $Ra^* = f(x_1, x_2, x_3)$ needed

hree-dimensional surface built on t ۱t r e h f

At the stage of performing a regression analysis of the experimental data, a non-linear association has been established represented by a four-dimensional paraboloid with determination coefficient $R^2 = 0.957$ (with $\pm 4.21\%$ accuracy):



$$Ra = -0.15 + 0.09V + 0.12t + 0.17f_r + 0.25V^2 + 0.29t^2 + 0.17f_r^2 \cdot$$
(4)

Using this non-linear function helped us establish that increasing the coded value of V by 0.1 points leads to an 0.036point increase of surface roughness (0.137 μ m); increasing the coded value of t leads to a 0.047-point increase in surface roughness (0.177 μ m), and increasing the coded value of fr by 0.1 points leads to a 0.037-point (0.140 µm) increase in surface roughness. So, as compared with the influence of Von surface roughness, depth of cut t has a 25.9% greater effect on it, and feed rate f_r has a 1.9% greater effect.

Considering the complicated and non-linear nature of the emergence of this parameter, we had to employ the capacities of the SKIF Aurora-SUSU supercomputer cluster (South Ural State University, Chelyabinsk, Russia) [44].

4.2 Creation of a surface roughness prediction model using an artificial neural network—step 2

Among the most popular packages-Maple, Mathematica, Mathcad, and Matlab-only Matlab today is intended for fundamental, high quality and versatile numeric calculations. The toolbox for creating, training and modeling of neural networks (the Neural Network Toolbox) in Matlab makes it much simpler to



he basis of the experimental points (see Table 8) that
effects the non-linear changes in surface roughness given the changing cutting speed V and feed rate fr with
fixed depth of cut
$$t = 0.5$$
 mm.

Variable parameters			Optimization criteria				
			Results of experiment		Dimensionless criteria		
x_1 Cutting speed, V (m/min)	x_2 Depth of cut, t (mm)	x_3 Feed rate, f_z (mm/rev)	Surface roughness, Ra (µm)	Machining time of unit volume, T_m (min/cm ³)	Surface roughness f_1 (Ra^*), unit	Machining time of unit volume $f_2(T_m^*)$, unit	Estimated vector length, <i>f</i> , unit
75	0.1	0.025	0.602	5.333	0.16	1	1.013
75	0.1	0.05	0.202	2.667	0.054	0.5	0.503
75	0.1	0.1	0.827	1.333	0.219	0.25	0.332
75	0.1	0.15	1.616	0.889	0.428	0.167	0.459
75	0.1	0.2	2.924	0.667	0.775	0.125	0.785
100	0.1	0.025	0.348	4	0.092	0.75	0.756
100	0.1	0.05	0.287	2	0.076	0.375	0.383
100	0.1	0.1	0.957	1	0.254	0.188	0.316
100	0.1	0.15	1.746	0.667	0.463	0.125	0.48
100	0.1	0.2	2.393	0.5	0.634	0.094	0.641
125	0.1	0.025	0.458	3.2	0.121	0.6	0.612
125	0.1	0.05	0.375	1.6	0.099	0.3	0.316
125	0.1	0.1	0.703	0.8	0.186	0.15	0.239
125	0.1	0.15	1.795	0.533	0.476	0.1	0.486
125	0.1	0.2	3.212	0.4	0.851	0.075	0.854
150	0.1	0.025	0.47	2.667	0.125	0.5	0.515
150	0.1	0.05	0.563	1.333	0.149	0.25	0.291
150	0.1	0.1	1.068	0.667	0.283	0.125	0.309
150	0.1	0.15	1.675	0.444	0.444	0.083	0.452
150	0.1	0.2	2.502	0.333	0.663	0.062	0.666
175	0.1	0.025	0.662	2.286	0.175	0.429	0.463
175	0.1	0.05	0.629	1.143	0.167	0.214	0.271
175	0.1	0.1	0.821	0.571	0.218	0.107	0.243
175	0.1	0.15	1.581	0.381	0.419	0.071	0.425
175	0.1	0.2	2.435	0.286	0.645	0.054	0.647

Table 4 Optimization criteria values for variable workpiece turning parameters at the depth of cut t = 0.1 mm

Variable parameter:			Optimization criteria				
			Results of experiment		Dimensionless criteria		
x_1 Cutting speed, V (m/min)	x_2 Depth of cut, t (mm)	x_3 Feed rate, f_z (mm/rev)	Surface roughness, Ra (µm)	Machining time of unit volume, T_m (min/cm ³)	Dimensionless surface roughness f_1 (Ra^*), unit	Dimensionless machining time of unit volume $f_2(T_m^*)$, unit	Estimated vector length, f, unit
75	0.2	0.025	0.141	2.667	0.037	0.5	0.501
75	0.2	0.05	0.266	1.333	0.07	0.25	0.26
75	0.2	0.1	0.807	0.667	0.214	0.125	0.248
75	0.2	0.15	1.599	0.444	0.424	0.083	0.432
75	0.2	0.2	3.774	0.333	1	0.062	1.002
100	0.2	0.025	0.228	2	0.06	0.375	0.38
100	0.2	0.05	0.314	1	0.083	0.188	0.206
100	0.2	0.1	0.771	0.5	0.204	0.094	0.225
100	0.2	0.15	1.622	0.333	0.43	0.062	0.434
100	0.2	0.2	2.789	0.25	0.739	0.047	0.74
125	0.2	0.025	0.515	1.6	0.136	0.3	0.329
125	0.2	0.05	0.842	0.8	0.223	0.15	0.269
125	0.2	0.1	1.981	0.4	0.525	0.075	0.53
125	0.2	0.15	2.025	0.267	0.537	0.05	0.539
125	0.2	0.2	2.778	0.2	0.736	0.038	0.737
150	0.2	0.025	0.671	1.333	0.178	0.25	0.307
150	0.2	0.05	0.378	0.667	0.1	0.125	0.16
150	0.2	0.1	0.965	0.333	0.256	0.062	0.263
150	0.2	0.15	1.636	0.222	0.433	0.042	0.435
150	0.2	0.2	2.225	0.167	0.59	0.031	0.591
175	0.2	0.025	0.832	1.143	0.22	0.214	0.307
175	0.2	0.05	0.365	0.571	0.097	0.107	0.144
175	0.2	0.1	0.857	0.286	0.227	0.054	0.233
175	0.2	0.15	1.67	0.19	0.443	0.036	0.444
175	0.2	0.2	2.649	0.143	0.702	0.027	0.703

Table 5 Optimization criteria values for variable workpiece turning parameters at the depth of cut t = 0.2 mm

Variable parameters			Optimization criteria				
			Results of experiment		Dimensionless criteria		
x_1 Cutting speed, V (m/min)	<i>x</i> ₂ Depth of cut, <i>t</i> (mm)	x_3 Feed rate, f_z (mm/rev)	Surface roughness, Ra (µm)	Machining time of unit volume, T_m (min/cm ³)	Surface roughness f_1 (Ra^*), unit	Machining time of unit volume $f_2(T_m^*)$, unit	Estimated vector length, f, unit
75	0.3	0.025	0.277	1.778	0.073	0.333	0.341
75	0.3	0.05	0.297	0.889	0.079	0.167	0.185
75	0.3	0.1	0.996	0.444	0.264	0.083	0.277
75	0.3	0.15	1.703	0.296	0.451	0.056	0.454
75	0.3	0.2	2.907	0.222	0.77	0.042	0.771
100	0.3	0.025	0.402	1.333	0.107	0.25	0.272
100	0.3	0.05	0.437	0.667	0.116	0.125	0.171
100	0.3	0.1	0.775	0.333	0.205	0.062	0.214
100	0.3	0.15	1.386	0.222	0.367	0.042	0.369
100	0.3	0.2	3.223	0.167	0.854	0.031	0.855
125	0.3	0.025	1.063	1.067	0.282	0.2	0.346
125	0.3	0.05	0.588	0.533	0.156	0.1	0.185
125	0.3	0.1	1.575	0.267	0.417	0.05	0.42
125	0.3	0.15	2.054	0.178	0.544	0.033	0.545
125	0.3	0.2	2.65	0.133	0.702	0.025	0.702
150	0.3	0.025	0.547	0.889	0.145	0.167	0.221
150	0.3	0.05	0.345	0.444	0.091	0.083	0.123
150	0.3	0.1	0.855	0.222	0.227	0.042	0.231
150	0.3	0.15	1.45	0.148	0.384	0.028	0.385
150	0.3	0.2	2.458	0.111	0.651	0.021	0.651
175	0.3	0.025	0.665	0.762	0.176	0.143	0.227
175	0.3	0.05	0.374	0.381	0.099	0.071	0.122
175	0.3	0.1	0.808	0.19	0.214	0.036	0.217
175	0.3	0.15	1.753	0.127	0.464	0.024	0.465
175	0.3	0.2	2.059	0.095	0.546	0.018	0.546

Table 6 Optimization criteria values for variable workpiece turning parameters at the depth of cut t = 0.3 mm

Variable parameters			Optimization criteria				
			Results of experiment		Dimensionless criteria		
<i>x</i> ₁ Cutting speed, <i>V</i> (m/min)	<i>x</i> ² Depth of cut, <i>t</i> (mm)	x_3 Feed rate, f_z (mm/rev)	Surface roughness, Ra (µm)	Machining time of unit volume, T_m (min/cm ³)	Surface roughness f_1 (Ra^*), unit	Machining time of unit volume $f_2(T_m^*)$, unit	Estimates vector length, <i>f</i> , unit
75	0.4	0.025	0.232	1.333	0.061	0.25	0.257
75	0.4	0.05	0.252	0.667	0.067	0.125	0.142
75	0.4	0.1	0.88	0.333	0.233	0.062	0.241
75	0.4	0.15	1.996	0.222	0.529	0.042	0.531
75	0.4	0.2	3.068	0.167	0.813	0.031	0.814
100	0.4	0.025	0.237	1	0.063	0.188	0.198
100	0.4	0.05	0.257	0.5	0.068	0.094	0.116
100	0.4	0.1	0.64	0.25	0.17	0.047	0.176
100	0.4	0.15	1.398	0.167	0.37	0.031	0.371
100	0.4	0.2	2.446	0.125	0.648	0.023	0.648
125	0.4	0.025	0.393	0.8	0.104	0.15	0.183
125	0.4	0.05	0.636	0.4	0.169	0.075	0.185
125	0.4	0.1	1.365	0.2	0.362	0.038	0.364
125	0.4	0.15	1.713	0.133	0.454	0.025	0.455
125	0.4	0.2	2.375	0.1	0.629	0.019	0.629
150	0.4	0.025	0.495	0.667	0.131	0.125	0.181
150	0.4	0.05	0.269	0.333	0.071	0.062	0.095
150	0.4	0.1	0.866	0.167	0.229	0.031	0.231
150	0.4	0.15	1.715	0.111	0.454	0.021	0.454
150	0.4	0.2	2.317	0.083	0.614	0.016	0.614
175	0.4	0.025	0.358	0.571	0.095	0.107	0.143
175	0.4	0.05	0.423	0.286	0.112	0.054	0.124
175	0.4	0.1	0.869	0.143	0.23	0.027	0.232
175	0.4	0.15	1.786	0.095	0.473	0.018	0.473
175	0.4	0.2	2.635	0.071	0.698	0.013	0.698

Variable parameters			Optimization criteria				
			Results of experiment		Dimensionless criteria		
<i>x</i> ₁ Cutting speed, <i>V</i> (m/min)	<i>x</i> ₂ Depth of cut, <i>t</i> (mm)	x_3 Feed rate, f_z (mm/rev)	Surface roughness, Ra (µm)	Machining time of unit volume, T_m (min/cm ³)	Surface roughness f_1 (Ra^*), unit	Machining time of unit volume $f_2(T_m^*)$, unit	Estimated vector length, <i>f</i> , unit
75	0.5	0.025	0.32	1.067	0.085	0.2	0.217
75	0.5	0.05	0.298	0.533	0.079	0.1	0.127
75	0.5	0.1	0.984	0.267	0.261	0.05	0.266
75	0.5	0.15	1.71	0.178	0.453	0.033	0.454
75	0.5	0.2	2.996	0.133	0.794	0.025	0.794
100	0.5	0.025	0.147	0.8	0.039	0.15	0.155
100	0.5	0.05	0.247	0.4	0.065	0.075	0.099
100	0.5	0.1	0.753	0.2	0.2	0.038	0.204
100	0.5	0.15	1.5	0.133	0.397	0.025	0.398
100	0.5	0.2	2.31	0.1	0.612	0.019	0.612
125	0.5	0.025	0.367	0.64	0.097	0.12	0.154
125	0.5	0.05	0.633	0.32	0.168	0.06	0.178
125	0.5	0.1	1.135	0.16	0.301	0.03	0.302
125	0.5	0.15	1.721	0.107	0.456	0.02	0.456
125	0.5	0.2	2.436	0.08	0.645	0.015	0.645
150	0.5	0.025	0.332	0.533	0.088	0.1	0.133
150	0.5	0.05	0.307	0.267	0.081	0.05	0.094
150	0.5	0.1	0.91	0.133	0.241	0.025	0.242
150	0.5	0.15	1.644	0.089	0.436	0.017	0.436
150	0.5	0.2	2.337	0.067	0.619	0.013	0.619
175	0.5	0.025	0.441	0.457	0.117	0.086	0.145
175	0.5	0.05	0.477	0.229	0.126	0.043	0.133
175	0.5	0.1	0.745	0.114	0.197	0.021	0.198
175	0.5	0.15	1.92	0.076	0.509	0.014	0.509
175	0.5	0.2	2.487	0.057	0.659	0.011	0.659

Table 8 Optimization criteria values for variable workpiece turning parameters at the depth of cut t = 0.5 mm



Fig. 5 Three-dimensional surface built on the basis of the experimental points reflecting the non-linear changes in surface roughness given the changing cutting speed V and feed rate fr with fixed depth of cut t = 0.5 mm

create neural networks. An undeniable advantage of Matlab is its language, which allows users to create their own algorithms and applications. The multi-purpose nature of the language provides opportunities for accomplishing a number of tasks such as collecting, analyzing and structuring data, developing algorithms, modeling systems, object-oriented programming, development of a graphical user interface, debugging and converting Matlab applications to C or C++ codes. That is why a parallel version of Matlab R2010b was chosen as the programming environment for this study.

The controlled feedforward neural network was trained based on a multilayer perceptron (MLP) using the Levenberg–Marquardt algorithm. The network structure included a hidden layer of sigmoid neurons and a linear layer of output neurons, because this is the best structure for multidimensional mapping problems.

The preliminary processing of data, which consisted in normalization of the values similar to the normalization of dimensionless criteria (see formulae 2 and 3), provided for compliance of the input values with the [0,1] range and was carried out with the aim of improving the efficiency of the network training process.

The overfitting problem was solved by improving the generalization performance of the network. To do that, two data sets were used: the training set for updating weights and offsets; and the validation set for stopping the training if an undesirable event occurs.

The final configuration (the number of neurons in the hidden layer) of the network was established based on the lowest mean squared error in the validation set.

To begin with, the multilayer perceptrons were trained with nine, ten, and 11 neurons in the hidden layer, with 15% of the tabular data allocated to the validation set. The lowest error values for MLP 3-9-1, MLP 3-10-1, and MLP 3-11-1 are presented in Figs. 6, 7, and 8 respectively.

Analysis of the graphical functions presented in Figs. 6, 7 and 8 showed that the lowest error of 0.61% in the validation set was provided by the MLP 3-10-1 network structure. The coefficient of determination of the obtained model was 0.978,



Fig. 6 The lowest mean squared error for the validation set in MLP 3-9-1configuration (calculated in Matlab)

Fig. 7 The lowest mean squared error for the validation set in MLP 3–10-1 configuration (calculated in Matlab)



which reflects its high accuracy in predicting surface roughness ($\pm 2.14\%$). The same structure appeared to give the best generalization performance in the cases of allocating 10 or 20% in the validation set of tabular data (Fig. 9). In the first training variant, the error was 0.86% (see Fig. 9b) and in the second variant, it was 1.00% (see Fig. 9c).

4.3 Establishing a Pareto frontier—step 3

The third step of the strategy involved calculating the values of Ra^* for the experimental values x_1 , x_2 , x_3 (see Tables 4, 5,

Fig. 8 The lowest mean squared error for the validation set in MLP 3-11-1 configuration (calculated in Matlab) 6, 7, and 8) with the help of the network and plotting charts of dimensionless criteria relations taking into account the T_m^* values (Fig. 10).

Intercept AB for cutting depth t = 0.5 mm with varying V = 150...175 m/min and $f_z = 0.025...0.085$ mm/rev was plotted between the tangency points of the line and the lowest curves (Fig. 11). The coordinates of the intercept ends were A (0,113; 0,034) and B (0,204; 0,022).

Considering the downward trend of the target function f, there are six reference points of the Pareto frontier (Fig. 12). In the new numbering, point A is given number 4 and point B—number 5.





Fig. 9 The lowest mean squared error in generalizing experimental data in MLP 3–10-1(a) with various validation sets: b –10%, c–20% (calculated in Matlab)



Fig. 10 Graphs showing the relation of dimensionless machining time of unit volume T_m^* with dimensionless surface roughness Ra^* for fixed depth of cut t and cutting speed V with varying feeds per revolution (with increasing feed, Ra^* increases and T_m^* decreases)

Analysis of the Pareto curve allowed us to establish five sections. Section I between points 1 and 2 corresponds to t = 0.4 mm and V = 70 m/min. Section II between points 2 and 3 corresponds to t = 0.5 mm and V = 100 m/min. Section III between points 3 and 4 corresponds to t = 0.5 mm and V = 150 m/min. Section IV between points 4 and 5 has been presented before (see Fig. 11). Section V between points 5 and 6 corresponds to t = 0.5 mm and V = 175 m/min. Points 1 and 6 are the end points of relations t = 0.4 mm at V = 75 m/min and t = 0.5 mm at V = 175 m/min, respectively.

4.4 Establishment of Pareto non-dominated decisions—*step 4*

In accordance with the strategy, step four involved narrowing the set of Pareto optimal decisions to a set of Pareto non-dominated decisions. For this purpose, the method of expert assessments was used to establish greater importance of the dimensionless criterion of the machining time of unit volume T_m^* over the





dimensionless criterion of surface roughness Ra^* . As a result, Pareto non-dominated estimates are presented by all vectors located below the blue one, taking into account the equivalence of f_1 and f_2 and plotted at 45° angle to the reference axes (Fig. 13). The end point of this vector with the coordinates (0.054, 0.054) (point 7 in the Pareto frontier) became the global minimum in the case of unconditional optimization with equivalent criteria f_1 and f_2 . In the actual coordinates, the global minimum in the case of equivalent criteria of the machining time of unit volume T_m^* and roughness Ra^* corresponds to the following values: $T_m = 0.287$ min/ cm³, $Ra = 0.203 \mu$ m, V = 150 m/min, t = 0.5 mm and $f_z = 0.043$ mm/rev.

4.5 Establishment of the optimum cutting conditions—*step* 5

In the fifth and final step of the implemented optimization strategy, direct questioning of the decision-maker (chief designer) set the maximum allowable roughness value. It is $Ra = 0.8 \ \mu\text{m}$ or the eighth point on the Pareto frontier curve, with the coordinates (0.212, 0.021), as shown in Fig. 14. In this case (the green estimates vector in Fig. 12), the valid relation of the importance of the optimization criteria was estimated at $T_m^*/Ra^* = 1/9$, i.e. T_m^* has a ninefold differential



Fig. 12 Six reference points of the Pareto frontier



Fig. 13 The global minimum vector of the Pareto optimality function in the case of equivalent machining time of unit volume T_m^* and surface roughness Ra^* (the actual parameters of the global minimum are reflected by the blue vector: $T_m = 0.287 \text{ min/cm}^3$, $Ra = 0.203 \text{ }\mu\text{m}$, V = 150 m/min, t = 0.5 mm and $f_z = 0.043 \text{ mm/rev}$)



Fig. 14 Vector of the global minimum of Pareto optimal function in the case of machining time of unit volume Tm* being nine times as important as surface roughness Ra^* (the actual parameters of the global minimum are presented by the green vector: $T_m = 0.111 \text{ min/cm}^3$, $R_a = 0.8 \text{ }\mu\text{m}$, V = 150 m/min, t = 0.5 mm and $f_z = 0.112 \text{ mm/rev}$)

over R7 and 8 and a valid preference is $y_8 \succ_Y y_7$ and induced $x_8 \succ_X x_7$.

As a result, the set of selected estimates Sel Y became limited to the green vector with the end actual coordinates (0.212, 0.021) and the set of selected decisions Sel X to the three-dimensional vector of the optimum cutting conditions ($f_z = 0.112$, t = 0.5, V = 150).

To sum up, it should be noted that accurate values of the points on the Pareto curve and the coordinates of the presented vectors have been obtained automatically in Matlab using a neural network model as a custom function. In particular, estimates vector f has been chosen as the optimization criteria, the limitation is the ratio of $T_m *: Ra^* = 9: 1$, and the boundary conditions are positive values of cutting speed *V*, cutting depth *t* and feed rate f_z . The non-linear constrained optimization problem was solved using the Newton method with quadratic convergence. The program implementation of the presented strategy in Matlab allows the quick calculation of the local optimum parameters of cutting conditions with various computer-aided manufacturing complexes for the whole range of cutting speeds and depths.

5 Conclusions

- (1) A five-step methodology for optimizing multifactorial systems has been presented to find the best solution for the set of experimental data.
- (2) For the first time for turning of high-strength steel, the Edgeworth-Pareto methodology of searching for the

optimum in a multi-criterion environment was used and made it possible to find the best conditions in the ndimensional decision space clearly and promptly using a neural network-based model.

- (3) An artificial neural network was created in the Matlab programming environment based on the MLP 3-10-1 multilayer perceptron, which predicts the surface roughness of a cylindrical workpiece with a diameter of \emptyset 50 and length of 120 mm manufactured from high-strength steel after finish turning in the following ranges of parameters: cutting speed from 75 through 175 m/min, depth of cut from 0.1 to 0.5 mm and feed per revolution of 0.025 to 0.20 mm with the accuracy of ±2.14%.
- (4) The global optimum for turning high-strength steel with the required surface roughness of the end workpiece was established: the required value of surface roughness $Ra = 0.8 \ \mu\text{m}$ and the minimum machining time of unit volume $T_m = 0.111 \ \text{min/cm}^3$ correspond to the optimum conditions of finish turning: cutting speed $V = 174 \ \text{m/min}$, cutting depth $t = 0.55 \ \text{mm}$ and feed $f_z = 0.112 \ \text{mm/rev}$.
- (5) Using Matlab, conditions were created for automating the design of the optimum turning conditions in the turning of high-strength steel and for integrating artificial intelligence into the CNC machine management system.

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