ORIGINAL ARTICLE



# Research on tool change time and the dynamic reliability of the machining process based on sensitivity analysis

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Abstract Tool changing is on the basis of tool wear failure and breakage failure. Utilization rate of the tool is low, which cannot guarantee the reliability of the whole machining system. In machining process, as the number of parts produced increases, tool wear is constantly increasing, which will contribute to the reduction of the reliability of the cutting tool. That account for processing of substandard products. Combining the moment estimation with the maximum likelihood estimation with the dynamic reliability analysis method, the study builds a mathematical model of the dynamic reliability for machining process under the premise of regarding ting parameters as random variables. The reliability of overall machining process is lower than a given target the proposed model can identify the tool which has the biggest failure rate quickly and accurately. The failure rate **formula** of each tool involved in each operation is deduced as well. Based on failure rate, an algorithm for defining the critical tool and its corresponding tool change time  $i$ ,  $p_i$ , and  $p_i$ , beyond that, for maximizing the utilization of every tool, the given model can pick up the cutting **parameter which has the largest sensi**tive degree to the relation via sensitivity analysis method. Then, the selection of relevant stock removal should be changed so as to  $im_k$  ve the reliability of cutting tool and the whole process system, as well as enabling the cutter continue to  $\mathbf{v}_n$  and delaying tool change time finally. Ultimately,  $\iota$  manufacturing process can maximize the **Xingang Wang<sup>1</sup> • Baoyan Wang<sup>2</sup> • Chunmei LV<sup>1</sup> • Xiaoming Chen<sup>2</sup> • Yimin Zhang<sup>1</sup><br>
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cutters' potential and thus reduce the number of tool changes, as well as the production costs.

Keywords Cutting  $\lambda$  Reliability . Sensitivity . Tool change tin

# 1 **h** oduction

W<sub>ith</sub> the high-precision automation technology being widely used nowadays, the machinery industry gives a higher request to the reliability of the product machining processes. Usually, the reliability of an operation depends greatly on such three factors as machine tool, cutting tool and operator, of which the reliability of the tool is the most important element. Therefore, it is extremely crucial to do research on the reliability and sensitivity of cutting tools. Poor reliability of a tool will induce more tool changes and raise reject rate, which thus results in longer completion time and more manufacturing costs.

Ramalingam and Watson [1] make research on the tool reliability by constructing tool life probabilistic models. Wang et al. [2] established a mathematical model of tool wear reliability, taking attenuation into consideration. Akturk et al. [3, 4] build a heuristic model based on simple scheduling rules and generic searches. Oral and Cakir [5] define computer-aided optimum method for rotational parts, which is characterized by a minimum number of tool changes and minimum tool travel time. Rodriguez et al. [6] set up a mathematical model for calculating critical tool life, which lowers the impact on the reliability of a part manufacturing process. Astakhov [[7\]](#page-8-0) introduces the assessment of cutting tool wear. Those scholars at home and abroad focus mainly on minimizing the total completion time by reasonable machine schedule and planning,

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<span id="page-1-0"></span>without taking into account the tool reliability, which imposes great effect on the tool change time and overall manufacturing process.

What is more, the parameters are changing randomly due to such factors as mechanical vibration and the distribution of material texture. The random variables are closer to the real operating condition. However, there is no literature on cutting parameters that cause effect on tool reliability sensitivity, tool change time and the reliability of the machining process. Salonitis and Kolios [8] proposed a novel approach for the efficient reliability assessment of cutting tool wear based on the combinations of stochastic response surface and surrogate modeling methods, coupled with Monte Carlo simulations and FORM for the estimation of reliability indices. Application of the approach in cutting tool wear with indicative statistical values has illustrated its efficiency and simplicity in implementation since each step can be executed individually potentially using specialized tools and incorporating results from experiments. The methodology employed herein can be extended to take into account more than two variables (cutting speed and feed rate), increasing the number of variables stochastically modeled. distinguished State and color into the set of the color lifeting parameters. But the constrained and color the set of the set of the color into the set of the set of

In this paper, we incorporate machine scheduling, reliability, and dynamics knowledge together. We build a mathematical model based on reliability sensitivity of cutting tools for defining the critical tool and its corresponding tool change time. The sensitivity analysis technique can enable us to pick out and control the cutting part ters with the largest sensitive degree before to failure tool change occurs. Then, the reliability of cutting tools and the whole process system are improved to maximize the utilization of every cutter and to requee the production costs finally.

# 2 Establishment of  $\mathcal{L}$  'vnamic reliability model for a machining process

The whole process reliability depends closely on reliability of each operational sequence, which is also influenced by the reliability  $\sim$  cutting tool, operator, and machine tool. The machine tool **but the top of the machine archi**to the and design, including degree of automation, the operatio. Venvironment. It also has great relationship with the mainte, ance policy made by the manager. That data is usually pre-estimated according to experience. That means the reliability of one machine tool can be experimentally obtained through the time between failure database [[9](#page-8-0)]. The operator reliability can also be obtained by an experiment based on the register recording the number of errors that occur during a specific period of observation. This paper focuses on the

cutting tool reliability and assumes that the machine reliability and the operator reliability remain unchanged.

As for a manufacturing process system, it is made up of three independent components: operator, machine tool, and cutting tool. These components are in series, and then the reliability of any manufacturing process can be calculated by Eq. (1).

$$
R_b(t) = R_m(t) \times R_o(t) \times R_t(t)
$$
\n(1)  
\n
$$
R_b(t)
$$
 is the reliability of a given manufacturer, as a

 $R_b(t)$  is the reliability of a given manufacturing progiven time t,  $R_m(t)$  is the reliability of the machine at a given time t,  $R_o(t)$  is the reliability of the operator a given time t, and  $R_t(t)$  the reliability of the cutting tool at a given time t.

The basic hypothesis here is the both machine tool and operator do not malfunction  $y$  ben producing continuously a batch of parts, and then the machine tool reliability and the operator reliability are always fully restored, which can be predefined as 1, thus Eq. (2)

$$
R_b(t) = R_t(t) \tag{2}
$$

The cutting tool riability at a given time  $t$  lies on its actual working  $\epsilon$  ment, and usually, the tool life t is subject to the two-parameter Weibull distribution. The tool reliability can be calculated as  $Eq.(3)$ .

$$
= \exp\left[-\left(\frac{t}{\eta}\right)^{\beta}\right]
$$
 (3)

where  $\beta$  is the shape parameter and  $\eta$  is scale parameter. When the tool life is subject to the two-parameter Weibull distribution, the basic failure rate can be calculated as Eq. (4).

$$
h_0(t) = \frac{\beta}{\eta} \left(\frac{t}{\eta}\right)^{\beta - 1} = \frac{\beta}{\eta^{\beta}} t^{\beta - 1}
$$
 (4)

If 
$$
\lambda = \frac{\beta}{\eta^{\beta}}
$$
,  $\alpha = \beta - 1$ , then Eq.(5)

 $h_0(t) = \lambda t$  $\alpha$  (5)

The reliability of cutting tool is mainly influenced by the cutting parameters. Based on the Taylor tool life index equation, all cutting parameters are considered. It is reasonable that Weibull proportional hazard model is used to predict the reliability of cutting tool. Therefore, the failure rate of cutting tool can be expressed as [10] in the following.

$$
h(t) = h_0(t) \exp\left(\ln v^{-\beta_1} + \ln f^{-\beta_2} + \ln d^{-\beta_3}\right)
$$

$$
= \lambda t^{\alpha} \exp(W)
$$
(6)

where  $W = -\beta_1 \ln v - \beta_2 \ln f - \beta_3 \ln d$ , the parameter v is the cutting speed (mm/min),  $f$  is the feed rate (mm/r), and  $D$  is the cutting depth (mm).  $\lambda$ , a,  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  are constants, which can be obtained by maximum likelihood estimation

<span id="page-2-0"></span>





 $\mathbf{1}$ 



<span id="page-3-0"></span>

For the convenience of description, we generally regard the number of parts  $N$  as the time unit. Assuming that the manufacturing process is composed of  $n$  jobs and that the time of the job *i* is  $t_i$  and that the tool reliability of the job *i* is  $R_{t_i}$ , then the manufacturing process can be seen as a series system composed of n dependent subsystems. From Eqs. (2) and (8), the cutting tool reliability  $i$  after  $N$  parts production can be calculated in Eq. (9).

$$
R_{t_i}(t) = \exp\left(-\left(\lambda/(\alpha+1)\right) \times (N \times t_i)^{(\alpha+1)} \times v_i^{\beta_1} \times f_i^{\beta_2} \times d_i^{\beta_3}\right)
$$
 (9)  
  $i = 1, 2, 3, \dots, n$ 

And then the reliability of the manufacturing process calculated as indicated in Eq. (10)

$$
R_b(N) = \prod_{i=1}^n R_{t_i}(N) = \prod_{i=1}^n
$$
  
\n
$$
\left\{ \exp\left[-\left(\lambda/(\alpha+1)\right) \times (N \times t_i)^{(\alpha+1)} \times \nu_i^{\beta_1} \times \mathcal{F}_i \times d_i^{\beta_3} \right] \right\}
$$
\n(10)

Especially when  $n$  equals 1, Eq. (10) defines the reliability of a manufacturing process which contains only one job.

# 3 Research on  $t^{\text{h}}$  reliability sensitivity analysis of cutting too's

The paper assumes  $\chi$  different cutting parameters are independent  $o_1$  eq.  $\qquad$  then, and then according to existing theories [13, 14], their mean value and variance is obtained via the ment estimation method. Finally, the reliability sensitivity of  $e$  v basic random variable including cutting speed  $v$ , feed te f, and cutting depth  $d$  can be calculated through the inte $g<sub>r</sub>$  method [15].

The cutters' reliability sensitivity on cutting speed  $\nu$  can be calculated according to Eq.(11) derived from Eq.(8).

$$
\frac{DR_t(t)}{Dv} = \frac{\partial R_t(t)}{\partial v}
$$
  
=  $\exp\left(-\left(\lambda/(\alpha+1)\right) \times t^{(\alpha+1)} \times v^{\beta_1} \times f^{\beta_2} \times d^{\beta_3}\right)$   
 $\times \left(-\lambda/(\alpha+1)\right) \times t^{(\alpha+1)} \times \beta_1 v^{(\beta_1-1)} \times f^{\beta_2}$   
 $\times d^{\beta_3}$  (11)





 $\Phi$  feature diameter,  $L$  feature length

<span id="page-4-0"></span>Table 2 Relationship among the specific operation, the type of cutting tool, the process number and the cutting tool number of each processing stage

Stage	Operation	Process number	Tool number	
	End milling	Process 1	Tool 1	
$\mathfrak{D}_{1}$	Rough milling	Process <sub>2</sub>	Tool 2	
$\mathcal{E}$	Drilling	Process 3	Tool 3	
	Drilling	Process 4	Tool 4	
$\overline{\mathcal{L}}$	Hole milling	Process 5	Tool 5	
6	Rough reaming	Process 6	Tool 6	
	Finish reaming	Process <sub>7</sub>	Tool 7	

The same procedure can be adopted to obtain the sensitivity on feed rate f and cutting depth  $d$ , as shown in Eqs. (12) and (13).

$$
\frac{DR_t(t)}{Df} = \frac{\partial R_t(t)}{\partial f}
$$
  
=  $\exp\left(-\left(\lambda/(\alpha+1)\right) \times t^{(\alpha+1)} \times v^{\beta_1} \times f^{\beta_2} \times d^{\beta_3}\right)$   
 $\times \left(-\lambda/(\alpha+1)\right) \times t^{(\alpha+1)} \times v^{\beta_1} \times \beta_2$   
 $\times f^{(\beta_2-1)} \times d^{\beta_3}$ 

$$
\frac{DR_i(t)}{Dd} = \frac{\partial R_i(t)}{\partial d}
$$
  
=  $\exp\left(-\left(\lambda/(\alpha+1)\right) \times t^{(\alpha+1)} \times v^{\beta_1} \times f^{\beta_2} \times d^{\beta_3}\right)$   
 $\times \left(-\lambda/(\alpha+1)\right) \times t^{(\alpha+1)} \times v \times f^{\beta_2} \times \beta_3$   
 $\times d^{(\beta_3-1)}$  (13)

Table 3 Precedence from operations

Table 4 Associated parameters for cutting tool reliability analysis

Stage	Operation	$\lambda$	aa	$\beta_1$	$\beta_2$	$\beta_3$
1	End milling	$1.752e - 26$	9.833	11.279	2.116	1.794
2	Rough milling	$1.752e - 36$	8.763	12.378	2.209	1.803
3	<b>Drilling</b>	$1.752e - 25$	16.410	14.308	1.786	1.816
4	Drilling	$1.752e - 23$	14.723	11.347	2.011	1.699
5	Hole milling	$1.752e - 25$	7.898	10.708	2.10 <sup>2</sup>	1.794
6	Rough reaming	$1.752e - 23$	6.729	11.279	2514	1.967
7	Finish reaming	$1.752e - 22$	12.998	10.346		1.833

If we regard the number of parts  $N$  as the time unit and assume that time for job i is  $t_i$ , the sensitivity varying tendency with the number of parts produced is shown from Eqs.  $(14)$  to (15).

$$
\frac{DR_t(N)}{Dv} = \frac{\partial R_t(N)}{\partial v} = \exp\left(-\left(\lambda / \frac{1}{N}\right)\right) \times (N \times t_i)^{(\alpha+1)} \times v^{\beta_1} \times f^{\beta_2} \times d^{\beta_3})
$$
\n
$$
\times \left(-\lambda / \frac{1}{N}\right) \times (N \times t_i)^{(\alpha+1)} \times \beta_1 \times v^{(\beta_1-1)} \times f^{\beta_2} \times d^{\beta_3}
$$
\n
$$
\frac{DR_t(N)}{Df} = \frac{\partial R_t(N)}{\partial f} = \exp\left(-\left(\lambda / (\alpha+1)\right) \times (N \times t_i)^{(\alpha+1)} \times v^{\beta_1} \times f^{\beta_2} \times d^{\beta_3}\right)
$$
\n
$$
\times \left(\lambda / (\alpha+1)\right) \times (N \times t_i)^{(\alpha+1)} \times v^{\beta_1} \times \beta_2 \times f^{(\beta_2-1)} \times d^{\beta_3}
$$
\n
$$
(15)
$$

$$
\frac{\partial R_i(\lambda)}{\partial d} = \frac{\partial R_i(N)}{\partial d} = \exp\left(-\left(\lambda/(\alpha+1)\right) \times (N \times t_i)^{(\alpha+1)} \times \nu^{\beta_1} \times f^{\beta_2} \times d^{\beta_3}\right) \times \left(-\lambda/(\alpha+1)\right) \times (N \times t_i)^{(\alpha+1)} \times \nu^{\beta_1} \times f^{\beta_2} \times \beta_3 \times d^{(\beta_3-1)} \tag{16}
$$

If the reliability sensitivity of a certain parameter shows positive, it means the cutting tool tends to be more reliable along with the increase of the average value. On the contrary, if the reliability sensitivity shows negative, the cutting tool tends to be more likely to fail along with the increase of the average value. If the absolute value of the reliability sensitivity is large, the cutter is more sensitive to the change of this parameter. So the cutter should be controlled so as to

Stage. Features Operation Specifications (mm) Feed rate  $f$  (mm/r) Depth  $d$  (mm) Speed v (mm/min) Machining time  $t_i$  (min)  $\mu_f$   $\delta_f^2$  $\mu_d$   $\delta_d^2$  $\mu_v$   $\delta_v^2$  $\mu_{ti}$   $\delta_{ti}$  $\delta_{ti}^{\;\;2}$ 1 1 End milling L = 1.5 1 2.1e−3 1.5 3.2e−3 4.8 4.2e−3 1.8 3.1 2 2,3,4 Rough milling  $\Phi = 80; L = 10$  0.3 3.1e−3 1.1 3.5e−2 40 7.8e−3 2.9 1.3 3 5,6,7,8 Drilling  $\Phi = 8; L = 30$  0.2 6.5e–3 5.5 2.6e–3 12 5.4e–3 0.2 0.05 4 9,10,11,12 Drilling  $\Phi = 12; L = 8$  0.3 4.5e-3 4 6.7e-3 6 1.8e-3 0.2 0.03 5 13 Hole milling  $\Phi = 19; L = 30$  0.3  $3.6e-3$  5 7.1e-3 45 6.3e-3 0.3 0.08 6 13 Rough reaming  $\Phi = 19.6$ ;  $L = 30$  0.6 5.1e−3 0.7 9.6e−3 16 4.2e−3 0.8 0.6 7 13 Finish reaming Φ = 20; L = 30 0.4 1.7e−3 0.3 1.1e−3 4 3.4e−3 0.8 0.6 **Photos 4 Total Control interview of the strengthening 1782–25 1788 in North Language (1982–28 1798 in the strengthening Process 6 Total Strengthening Process 6 Total Strengthening Process 6 Total Strengthening Process 6** 

 $\binom{1}{1}$ 

 $\Phi$  feature diameter, L feature length,  $\mu$  mean,  $\delta_2$  variance



<span id="page-5-0"></span>

guarantee the reliability of the productions and the whole machining process.

# 4 Research on tool change time in the machining process

The manufacturing reliability is calculated by Eq.  $(10)$ , when it is lower than the required minimum value  $(0.80$  here), which can be adjusted according to the actual processing requirements, some tool must be changed, or the number of nonconforming parts and the entire production costs will inevitably increase. At this time,  $t^1$  ime and way to change the tool becomes extremely important. In the following part, specific study on tool change time vresented.



Fig. 5 Process reliability when manufacturing 100 parts with tool changes Fig. 6 The sensitivity change curve of cutting parameters for tool 1

4.1 The machining process is composed of only one job

When the machining process is composed by only one job, the liab ity can be calculated by Eq.  $(9)$ , and the change curve be ween the machined parts  $N$  and the reliability is shown in Fig. 1.

When the process reliability is lower than the allowable value 0.80, some tool must be changed, and this procedure will be repeated until all parts required by the production planning are produced. Assuming that the time of this process is t, then the tool change time  $T_c$  is shown in Eq.(17).

$$
T_c = N \times t \tag{17}
$$

After each replacement, the process reliability is changed and improved according to Fig. 2.



<span id="page-6-0"></span>

Fig. 7 The sensitivity change curve of cutting parameters for tool 2

 $N_1$ ,  $N_2$ ,  $N_3$  and  $N_4$  in Fig. 2 represent the number of parts produced when changing tools. It is assumed that manufacturing process reliability cannot be lower than 0.80. When the tool change happens at  $N_1$ , manufacturing process reliability rises from 0.80 to about 0.97. When the tool change happens at  $N_2$ , manufacturing process reliability rises from 0.82 to about 0.95. The reason why the second change occurs when manufacturing process reliability is higher than 0.80 is that if one more part is produced, manufacturing process reliability may be lower than 0.80, then rejected products will be generated or the shutdown happens. So the tool change should be conducted beforehand. Figure 1 presents that the proper change of the tool can ensure that process reliability is  $\frac{1}{2}$  igherthan the threshold value. **PERIOD RETRACTED ARTICLE RETRACTED ARTICLE IS CONSULTER AN EXAMPLE ARTICLE CONSULTER AN EXAMPLE ARTICLE CONSULTER AN EXAMPLE CONSULTER AN EXAMPLE CONSULTER ARTICLE CONSULTER ARTICLE CONSULTER ARTICLE CONSULTER ARTICL** 

### 4.2 The machining process is composed of a series  $\gamma$ jobs

A real manufacturing process usually  $\chi$  contains multiple operations, and we assume that different operations use different tools. When the manufacturing process reliability  $R_b(N)$  calculated by Eq.(10) is lower  $\triangle$  an the minimum allowable value, the tool must be changed.  $\lambda$  s different operations and tools are involved, how to select the right tool to change becomes



Fig. 8 The sensitivity change curve of cutting parameters for tool 3



extremely critical. This paper  $p_{\text{r}}$  oses  $\ldots$  method for selecting the right tool based on failure rate and defines that a cutter who has the largest failure ate is called critical tool, which must be replaced first when necessary.

For the convenience of presentation, we use the number of machined parts.  $X_{\text{as}}$  as the time unit. Assuming that the manufacturing process is composed of  $n$  jobs and that the time of the job is the definition with Eqs. (6) and (9), the failure rate of cutters after N parts produced can be calculated in Eq.(18).

$$
\lambda \times v_i^{\beta_1} \times f_i^{\beta_2} \times d_i^{\beta_3} \times (N \times t_i)^{\alpha} \quad i = 1, 2, 3, \dots, n \quad (18)
$$

#### 4.3 Computational model

 $h(N)$ 

A case study is used to illustrate the application of the abovementioned methodology. We cut a 90 mm × 90 mm steel plate out of a Q235 steel plate with thickness of 34 mm. The specific sizes, shapes, and tolerances are obtained using milling, drilling, and reaming operations. The part is presented in Fig. 3, the specific requirements are shown in Table 1, and all dimensions are expressed in millimeters.



Fig. 10 The sensitivity change curve of cutting parameters for tool 5

<span id="page-7-0"></span>

Fig. 11 The sensitivity change curve of cutting parameters for tool 6

In Fig. 3, the part is subdivided into 13 pieces with surfaces of different characteristics, which require different machining operations using different cutting tools. Those features can determine the order of precedence of the machining operations. It is assumed that the operator does not make mistakes and all the on of the variables as an example, the calculation, and analysis are carried out. Each operational sequence and the corresponding working time are obtained in Mastercam simulation, in which we adopt proper processing technology and use the preset parameters. Table 2 can illustrate the corresponding relationship among the specific operation, the type of cutting tool, the process number, and the cutting tool number of each processing stage clearly. Table 3 presents cu parameters are random variables which can  $b^*$  models by normal distributions. In this paper, taking the normal distributi the order of precedence and machining imes for each operation. Precedence oper tion is calculated according to Mastercam diagnosis me **[R](#page-4-0)ETARBLE CONFIRMATION CONTINUOUS CONFIRMATION CONFI** 

To estimate the following neces  $x$  parameters  $\lambda$ ,  $a$ ,  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$ , the maximum likelihood estimation is used [[11](#page-9-0)]. With the data presented in Table 3, the likelihood function lognormal function established on the basis of the proposed



Fig. 12 The sensitivity change curve of cutting parameters for tool 7



Fig. 13 Machining process reliability change  $c<sub>u</sub>$  with tool change delay

mathematical model in this study is  $\mathbf{r}_i$  is  $\mathbf{r}_i$  in the following formula.

$$
\ln L(\lambda, \alpha, \beta_1, \beta_2, \beta_3)
$$
\n
$$
= \sum_{i=1}^{10} \left[ \ln(\lambda t_i^{\alpha}) \cdot \frac{\ln(1 - \beta_3 \ln(f_i) + \beta_3 \ln(d_i) - \frac{\lambda}{\alpha + 1} t_i^{\alpha + 1} v_i^{\beta 1} f_i^{\beta 2} d_i^{\beta 3} \right] \tag{19}
$$

where the parameters  $f_i$ ,  $d_i$ ,  $v_i$ , and  $t_i$  are the mean of feed rate, deptively, cutting speed, and the machining time, respectively, as hown in Table 3.

anish the partial derivative function about the  $\lambda$ ,  $a$ ,  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$ , and then five non-linear equations about  $\lambda$ ,  $a$ ,  $\beta_1$ ,  $\beta_2$ , and  $\beta_3$  are obtained. In order to obtain the associated parameters for cutting tool reliability analysis as shown in Table 4, the method of numerical analysis is used to solve these equations by programming in the mathematics software Matlab.

Reliability for this part operation is calculated with Eq. (9), where the machining time and the cutting parameters of each operation are presented in Table 4. The manufacturing process reliability is eventually calculated with Eq. (11). We assume that the allowed reliability of manufacturing process is 0.80 [16]. Tool replacement happens when reliability of manufacturing process is lower than 0.80. For each tool using Eq. (18), the one who has the biggest failure rate must be changed, and the corresponding operation is selected as well. Figure 4 shows the change cure of each tool's failure rate along with N parts produced.

Figure 5 presents the variation trend of the manufacturing process reliability before and after tool change along with the number of parts produced. For example, in Fig. 5, when the 18th part is produced, it is calculated that manufacturing process reliability is 0.7684, lower than minimum allowable value, 0.80. It shows that tool change should be conducted when 17 parts are produced, which is the first tool change in the whole procedure. Figure [4](#page-5-0) can show which tool should be replaced. Milling cutter used in the fifth job presents the <span id="page-8-0"></span>biggest failure rate when the eighteenth part is produced, so it has to be changed. After the tool change, the manufacturing process reliability is recalculated and the value comes to 0.9984. The manufacturing process reliability is improved and the processing is running normally until the reliability is lower than 0.80. Then, tool change happens again until all the work is completed.

# 5 Influence of cutting parameters on tool change time and the machining process reliability

The sensitivity change curves of cutting parameters for every tool involved in every job can be obtained from Eqs. (14) to (16), as is shown from Figs. 6, 7, 8, 9, 10, 11, and 12.

As shown in Fig. 6, the sensitivity value of cutting speed  $\nu$ for the cutter in job 1 appears the largest, which means it has the largest sensitive degree. Similarly, the sensitivity value of feed rate  $f$  for the cutter from job 2 to job 6 appears the largest and that value of cutting depth  $d$  for the cutter in job 7 appears the largest. It can also be found that all the reliability sensitivity value are negative, which means all of the cutters tend to fail along with the increase of the average value. Therefore, the stock removal of the most sensitive parameter must be reduced appropriately before tool failure or tool change occurs so as to improve the reliability value and maximize the utilization of every cutter, and hence reduce the production costs finally.

When the critical tool has been selected via the presented method after a certain number of parts are produced, we easily get its sensitive parameter through Figs.  $6, 7, 8, 9, 10$ 11 and 12. We cut the mean value into half  $a_n d$  increase the working time so as to improve the reliability. When the same tool needs to be changed again,  $\sqrt{e}$  replace it instead of lowering the cutting parameters. Taking the part in Fig. 3 as a case study, the process reliability change curve with tool changes is shown in Fig. 13.

Comparing Fig.  $13$  with  $\sim$  5, we can find that the milling cutter in job 5 must be  $\log$  anged when manufacturing the seventeenth part as is  $s'$  wn in Fig. 5. While in Fig. 13, we only cut the mean value  $\epsilon$  the most sensitive parameter, feed rate, in half based on reliability sensitivity analysis, which means there is no need to change the tool before manufacturing the 18th part. Even the ugh the working time is increased, tool change will not occur until the 26th part is produced. Time for changing tool 3 will extend from when 20 parts are produced to when 37 parts are produced. The same procedure can be ada<sub>p</sub> ed to other tools. Thus, it can be seen that all tool changes are put off to different degrees compared with previous ones, which can reduce the number of tool change and production costs while ensuring the machining process reliability at the same time.

This proposed algorithm does apply to solving the reliability of manufacturing process composed of drilling, turning, milling, and grinding, which can be used in product life cycle management. It is also of certain guiding significance to determining the tool change interval and making reasonable operation precedence.

#### 6 Conclusions

This paper builds a mathematical model of the dynamic reliability for the machining process based on tool reliability, and the sensitivity formulas of cutting parameters are derived as well. The sensitive degree of cutting  $s_{\mathcal{P}}$ , and cutting depth to the cutting tool reliability is  $\epsilon$  in along with a theoretical basis for controlling  $\epsilon$  itting parameters reasonably. Moreover, a failure rate-based odel for selecting a critical tool and tool change time is proposed. It helps to ensure the required process reliability before reaching the maximum wear limit. Finally, a sensit vity-sed algorithm about tool change time and the reliability of the machining process is presented in this study. The sensitive parameters of the specific cutter which is going to lose  $\epsilon$  acy must be changed so as to improve the reliability of both  $\infty$  and the overall process, as well as to delay tool change time and reduce production costs. **S** Influence of certring parameters on tool change time  $\frac{1}{2}$  this proper builds a mathematical model of the symming reduced.<br>The sensitivity change carve of certain time of the certain of the mathematical care of ce

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