# ORIGINAL ARTICLE

# Investigation of the effect of machining parameters on the surface quality of machined brass (60/40) in CNC end milling—ANFIS modeling

Ibrahem Maher  $\cdot$  M. E. H. Eltaib  $\cdot$  Ahmed A. D. Sarhan  $\cdot$ R. M. El-Zahry

Received: 25 December 2013 /Accepted: 28 May 2014 /Published online: 7 June 2014  $\oslash$  Springer-Verlag London 2014

Abstract Brass and brass alloys are widely employed industrial materials because of their excellent characteristics such as high corrosion resistance, non-magnetism, and good machinability. Surface quality plays a very important role in the performance of milled products, as good surface quality can significantly improve fatigue strength, corrosion resistance, or creep life. Surface roughness (Ra) is one of the most important factors for evaluating surface quality during the finishing process. The quality of surface affects the functional characteristics of the workpiece, including fatigue, corrosion, fracture resistance, and surface friction. Furthermore, surface roughness is among the most critical constraints in cutting parameter selection in manufacturing process planning. In this paper, the adaptive neuro-fuzzy inference system (ANFIS) was used to predict the surface roughness in computer numerical control (CNC) end milling. Spindle speed, feed rate, and depth of cut were the predictor variables. Experimental validation runs were conducted to validate the ANFIS model. The predicted surface roughness was compared with measured data, and the maximum prediction error for surface roughness was 6.25 %, while the average prediction error was 2.75 %.

Keywords Brass . ANFIS . Surface roughness . CNC . End milling

I. Maher  $\cdot$  A. A. D. Sarhan ( $\boxtimes$ ) Centre of Advanced Manufacturing and Material Processing, Department of Mechanical Engineering, Faculty of Engineering, University of Malaya, 50603 Kuala Lumpur, Malaysia e-mail: ah\_sarhan@yahoo.com

#### I. Maher

Department of Mechanical Engineering, Faculty of Engineering, Kafrelsheikh University, Kafrelsheikh 33516, Egypt

M. E. H. Eltaib : A. A. D. Sarhan : R. M. El-Zahry Department of Mechanical Engineering, Faculty of Engineering, Assiut University, Assiut 71516, Egypt

# 1 Introduction

Brass is one of the first two metals most widely used by humans, copper and its alloy (brass) and gold [\[1](#page-5-0)]. Brass is specified because of the unique combination of properties, it is stronger and harder than copper, easy to form into various shapes, a good conductor of heat, and is generally resistant to corrosion from salt water. Owing to these properties, brass is usually a first-choice material for many components in equipment made in general. In the electrical and precision engineering industries, brass is also used to make pipes and tubes, weather stripping, and other architectural trim pieces, screws, radiators, musical instruments, and cartridge casting for firearms [[2\]](#page-5-0).

In the milling process, surface roughness plays a vital role in how products perform, and it is also a factor with great influence on manufacturing cost. It describes the geometry of the machined surface, and combined with surface texture, it can play an important role on the operational characteristics of the part (e.g., fatigue, corrosion, fracture resistance, and surface friction). To achieve a desirable surface quality value, the part must be machined more than once. Therefore, the desired surface finish is usually specified, and appropriate processes are selected to attain the required quality [\[3\]](#page-5-0).

To achieve a desired surface finish, a good predictive model is required for stable machining. The number of surface roughness prediction models available in literature is very limited [[4\]](#page-5-0). Most surface quality prediction models are empirical and generally based on laboratory experiments. In addition, it is practically very difficult to control all factors as required to obtain reproducible results [\[5,](#page-5-0) [6\]](#page-5-0).

Actual surface roughness monitoring can be accomplished either by intensive post-process inspection, an in-process surface roughness measuring device, or a surface roughness prediction system. Although post-process inspection is the easiest to implement, it cannot prevent the parts from being

<span id="page-1-0"></span>processed before a defective batch is discovered. In-process measurement of surface roughness requires adding sensitive sensors to a hostile environment. Ultimately, the surface roughness prediction system can be used to determine the surface roughness indirectly [\[7](#page-5-0)–[9\]](#page-5-0).

Several techniques including multiple regression, Taguchi, fuzzy logic, artificial neural network (ANN), and adaptive neuro-fuzzy inference system (ANFIS) have been used to predict surface roughness in various cutting processes [\[10](#page-5-0)–[16\]](#page-6-0).

The criterion variable is surface roughness and the predictor variables are controllable machining parameters, such as spindle speed, feed rate, and depth of cut and their interactions. These techniques were used in turning [[17,](#page-6-0) [18](#page-6-0)], milling [\[19,](#page-6-0) [20\]](#page-6-0), and drilling processes [\[21](#page-6-0), [22](#page-6-0)].

ANFIS is a fuzzy inference system implemented in the framework of an adaptive neural network. By using a hybrid learning procedure, ANFIS can be used to construct an input– output mapping based on human knowledge as fuzzy if-then rules as well as predetermined input–output data pairs for neural network training. It provides a means for fuzzy modeling to learn information about the data set in order to compute the membership function parameters that best allow the associated fuzzy inference system to track the given input–output data [[23,](#page-6-0) [24\]](#page-6-0).

Recently, ANFIS has been applied to predict workpiece surface roughness in end-milling operation, yielding accuracy as high as 96  $\%$  [\[25](#page-6-0)] and average error up to 0.522  $\%$  [\[26](#page-6-0)]. It has also been used to predict surface roughness in turning operation, producing average error up to 0.38 % [\[27](#page-6-0)]. Lee et al. [[28\]](#page-6-0) employed ANFIS to establish the relationship between actual surface roughness and texture features of the surface image. Accurate surface roughness modeling can facilitate the effective estimation of surface roughness. The input parameters of a training model are spatial frequency, arithmetic mean value, and standard deviation of gray levels from the surface image, without involving cutting parameters (cutting speed, feed rate, and depth of cut). Experiments

Table 1 Measured Ra in microns (trained data set)

demonstrate the validity and effectiveness of fuzzy neural networks for modeling and estimating surface roughness. Empirical results also show that the proposed ANFIS-based method outperforms the existing polynomial-network-based method in terms of training and test accuracy of surface roughness. Hence, the aim of this work is to obtain optimal milling parameters (cutting speed, feed rate, and depth of cut) for minimal surface roughness while milling brass (60/40). ANFIS modeling is used to accomplish this objective.

# 2 Experimental setup

Surface roughness is the dependent variable, while cutting speed (*n*) in the range of  $750-1,750$  rpm, feed rate (*f*) ranging from 50 to 250 mm/min, and depth of cut  $(t)$  in the range of 0.3–0.7 mm were used as predictor variables, which were selected based on the tool manufacturer's recommendations (Table 1).

The experiments were performed using a ProLight2000 computer numerical control (CNC) end-milling machine. A high-speed steel four-flute end-milling cutter with a diameter of 7/16 in. (11.1 mm) was used for dry machining slots of brass (60/40) blocks under specific machining conditions (speed, feed, and depth of cut), as shown in Fig. [1](#page-2-0). Brass (60/40) with Vickers hardness of 125 and a chemical composition of 60 % copper and 40 % zinc served as a workpiece material with  $40 \times 40 \times 20$  mm dimensions (Fig. [1\)](#page-2-0). The surface roughness Ra (μm) was measured with a stylus-based profilometer (Surtronic 3+, 99 % accuracy).

## 3 Experimental results

A slot-milling test was carried out using the proposed experimental setup to investigate the surface quality. The average surface roughness Ra was calculated for three different measurements under the same conditions with a sampling length



<span id="page-2-0"></span>

Fig. 1 Cutting geometry

of Lc=2.5 mm at a specific area of the workpiece. The measurements' direction was parallel to the cutting direction and perpendicular to the lay of surface anomalies. A total of 75 sets of data were selected for training ANFIS from a total of 100 sets obtained in the end-milling experiments, as summarized in Table [1](#page-1-0). The remaining 25 sets were used for testing once training was completed to verify the accuracy of the predicted surface roughness values. All data in this research is in the steady-state region of tool wear.

#### 4 ANFIS prediction model

The ANFIS architecture is shown in Fig. 2. Five network layers were used by ANFIS to perform the following fuzzy inference steps: (1) input fuzzification, (2) fuzzy set database construction, (3) fuzzy rule base construction, (4) decisionmaking, and (5) output defuzzification. ANFIS was constructed through MATLAB, and 75 readings comprised the training data set as listed in Table [1](#page-1-0).

Fig. 2 ANFIS architecture for a three-input Sugeno fuzzy model

Different membership functions were used in training ANFIS to predict surface roughness. The generalized bell membership function (gbellmf) gives the lowest training error, so it was adopted for the ANFIS training process in this study. The fuzzy rule architecture of ANFIS when gbellmf is adopted consists of 27 fuzzy rules generated from the input–output data set based on the Sugeno fuzzy model [\[29](#page-6-0)–[31\]](#page-6-0). During training, the 75 Ra values (training data set) were used to conduct 300 cycles of learning with an average error of 0.10.

The membership functions of every input parameter within the architecture can be divided into three areas, i.e., small (S), medium (M), and large (L). Figure [3](#page-3-0) shows the initial and final membership functions of the three end-milling parameters derived from training via gbellmf.

In Fig. [3a, b](#page-3-0), the initial and final membership functions of speed only undergo minor changes in the medium and large areas, and major changes in the small area. Figure [3c, d](#page-3-0) illustrates the initial and final membership functions of the feed rate. It appears that the final membership function after training experiences smaller variation in the small and large areas but slightly greater variation in the medium area. Figure [3e, f](#page-3-0) shows the initial and final membership functions of the depth of cut. There is obviously a small change in the final membership function's shape after training, regardless of area size. The large changes in the small area in Fig. [3b](#page-3-0) indicate that the lower speed value has greater effect on surface roughness than the medium and large values. The minor changes in the small, medium, and large areas in Fig. [3d](#page-3-0) indicate that all ranges of feed rate and depth of cut have the same effect on surface roughness. Also, Fig. [3](#page-3-0) shows that among the three endmilling parameters studied, speed had the greatest impact on surface roughness, followed by feed rate, and finally depth of cut, which was the least significant factor of all.

According to Fig. [4a, b](#page-3-0), speed and feed rates had considerable effect on surface roughness, while an increase in speed led to a decrease in surface roughness and an increase in feed rate resulted in an increase in surface roughness, but depth of cut had a minor effect on surface roughness. Lower depth of cut and feed rate values are recommended for smaller surface



<span id="page-3-0"></span>

(e) Initial membership functions of depth of cut

Fig. 3 Initial membership and final membership functions of speed, feed, and depth of cut. a Initial membership functions of speed. b Final membership functions of speed. c Initial membership functions of feed.

roughness. That is because the combination of feed rate and depth of cut determines the undeformed chip section and hence the amount of cutting forces required to remove a specified volume of material. By decreasing the feed rate and depth of cut, less material has to be cut per tooth per revolution; thus, the energy required is lower. Consequently, this would reduce the cutting forces, leading to lower surface roughness, while the high depth of cut and feed rate would



d Final membership functions of feed e Initial membership functions of depth of cut. f Final membership functions of depth of cut

 $0.28$ 

*t*

lead to a contact overload between the cutting tool and the workpiece, which would cause inferior surface quality.

On the other hand, the effect of cutting speed should also be taken into consideration. The results of cutting speed are shown in Fig. 4a, and they suggest that higher spindle speed would result in lower surface roughness. This could be explained in terms of the chip formation process, which is influenced by the shear







(a) Surface roughness *Ra* in relation to change of Speed (n) and feed rate (f)

(b) Surface roughness *Ra* in relation to change of feed rate (f) and depth of cut (t)

<span id="page-4-0"></span>

Fig. 5 Chip formation process

length (ls) in the shear zone. The shear length (ls) is given as  $ls=t/sin \varphi$ , where t is undeformed chip thickness, and  $\varphi$  is the shear angle [[32](#page-6-0)]. Shear angle ( $\varphi$ ) is large at high cutting speeds; therefore, the shear length (ls) is small, as shown in Fig. 5 [[33](#page-6-0)]. As a result, the chip will break away with less material deformation at

Table 2 The error of the ANFIS

the tool tip, which will in turn preserve the machined surface properties leading to less edge chipping.

## 5 Model verification

Twenty-five random readings were used as the testing data set (Table 2). The plot of 25 measured Ra values versus predicted Ra using the ANFIS model is shown in Fig. [6](#page-5-0). This figure presents a comparison of the measured Ra and predicted Ra of the testing data set of 25 following training using ANFIS. Appropriate assent is evident between the measured and ANFIS-predicted surface roughness values. This close assent obviously displays that the ANFIS model can be used to predict the surface roughness under consideration. Thus, the proposed ANFIS model offers a promising solution to predicting roughness values in the specific range of parameters.

Table 2 and Fig. [6](#page-5-0) show a big difference in surface roughness from 625 to 875 rpm and small change between 875 and 1,375 rpm. There is also a big difference in surface roughness



<span id="page-5-0"></span>

Fig. 6 Measured Ra versus predicted Ra

between 90 and 150 mm/min feed rates and small change from 150 to 270 mm/min. Thus, it is recommended to machine brass (60/40) materials using 90 mm/min feed rate, 875 rpm cutting speed, and a small depth of cut range.

To evaluate the ANFIS model, the percentage error  $E_i$  and average percentage error  $E_{\text{av}}$  defined in Eqs. (1) and (2), respectively, were used. e percentively, w<br>Ra<sub>i</sub>−Ra<sub>i</sub>

$$
E_i = \frac{\left| \text{Ra}_i - \hat{\text{Ra}}_i \right|}{\text{Ra}_i} \times 100 \tag{1}
$$

$$
E_{av} = \frac{1}{m} \sum_{i=1}^{m} E_i
$$
 (2)

where  $E_i$  is the percentage error of sample number i; Ra<sub>i</sub> is the measured Ra of sample number i;  $\hat{R}a_i$  is the predicted Ra generated by the ANFIS model;  $i=1,2,3,...; m$  is the sample number; and  $E_{av}$  is the average percentage error of m sample data.

Table [2](#page-4-0) and Fig. 7 show that the average percentage error for surface roughness prediction is 2.75 %. Figure 7 presents the percentage error between the predicted and measured Ra. The highest percentage of error for ANFIS model prediction is 6.25 %. The low error level signifies that the surface roughness results predicted by ANFIS are very close to the actual experimental results. The error and accuracy values mean that the proposed model can predict surface roughness satisfactorily.



Fig. 7 The error percentage

#### 6 Conclusion

ANFIS was used to develop an empirical model for predicting the surface roughness of machined brass in CNC end milling. Spindle speed, feed rate, and depth of cut were used as predictor variables. Seventy-five measured Ra values, under different cutting conditions, comprised the training data set, and 25 random values were used as the testing data set. The model was verified with test data, and the average percentage accuracy achieved was 97.25 %. These results indicate that the ANFIS model with gbellmf is accurate and can be used to predict surface roughness in end-milling operation.

# References

- 1. Zronik J (2005) Metals shaping our world. Crabtree, Canada
- 2. Cheremisinoff NP (1996) Materials selection deskbook. Noyes, New Jersey
- 3. Benardos PG, Vosniakos GC (2002) Prediction of surface roughness in CNC face milling using neural networks and Taguchi's design of experiments. Robot Comput Integr Manuf 18(5–6):343–354. doi[:10.](http://dx.doi.org/10.1016/S0736-5845(02)00005-4) [1016/S0736-5845\(02\)00005-4](http://dx.doi.org/10.1016/S0736-5845(02)00005-4)
- 4. Suresh PVS, Venkateswara Rao P, Deshmukh SG (2002) A genetic algorithmic approach for optimization of surface roughness prediction model. Int J Mach Tools Manuf 42(6):675–680. doi[:10.1016/](http://dx.doi.org/10.1016/S0890-6955(02)00005-6) [S0890-6955\(02\)00005-6](http://dx.doi.org/10.1016/S0890-6955(02)00005-6)
- 5. Wang X, Feng C (2002) Development of empirical models for surface roughness prediction in finish turning. Int J Adv Manuf Technol 20(5):348–356
- 6. Sayuti M, Sarhan AAD, Tanaka T, Hamdi M, Saito Y (2012) Cutting force reduction and surface quality improvement in machining of aerospace duralumin AL-2017-T4 using carbon onion nanolubrication system. Int J Adv Manuf Technol 65(9-12):1493–1500
- 7. Chen J, Huang B (2003) An in-process neural network-based surface roughness prediction (INN-SRP) system using a dynamometer in end milling operations. Int J Adv Manuf Technol 21(5):339–347
- 8. Chang H-K, Kim J-H, Kim IH, Jang DY, Han DC (2007) In-process surface roughness prediction using displacement signals from spindle motion. Int J Mach Tools Manuf 47(6):1021–1026. doi:[10.1016/j.](http://dx.doi.org/10.1016/j.ijmachtools.2006.07.004) [ijmachtools.2006.07.004](http://dx.doi.org/10.1016/j.ijmachtools.2006.07.004)
- 9. Singh D, Rao PV (2006) A surface roughness prediction model for hard turning process. Int J Adv Manuf Technol 32(11-12):1115-1124. doi[:10.1007/s00170-006-0429-2](http://dx.doi.org/10.1007/s00170-006-0429-2)
- 10. Asiltürk İ, Çunkaş M (2011) Modeling and prediction of surface roughness in turning operations using artificial neural network and multiple regression method. Expert Syst Appl 38(5):5826–5832. doi: [10.1016/j.eswa.2010.11.041](http://dx.doi.org/10.1016/j.eswa.2010.11.041)
- 11. Asiltürk İ (2012) Predicting surface roughness of hardened AISI 1040 based on cutting parameters using neural networks and multiple regression. Int J Adv Manuf Technol 63(1–4):249–257. doi[:10.1007/](http://dx.doi.org/10.1007/s00170-012-3903-z) [s00170-012-3903-z](http://dx.doi.org/10.1007/s00170-012-3903-z)
- 12. Sayuti M, Sarhan AAD, Fadzil M, Hamdi M (2012) Enhancement and verification of a machined surface quality for glass milling operation using CBN grinding tool—Taguchi approach. Int J Adv Manuf Technol 60(9–12):939–950. doi:[10.1007/s00170-011-3657-z](http://dx.doi.org/10.1007/s00170-011-3657-z)
- 13. Bagci E, Aykut Ş (2005) A study of Taguchi optimization method for identifying optimum surface roughness in CNC face milling of cobalt-based alloy (stellite 6). Int J Adv Manuf Technol 29(9–10): 940–947. doi:[10.1007/s00170-005-2616-y](http://dx.doi.org/10.1007/s00170-005-2616-y)
- <span id="page-6-0"></span>14. Zalnezhad E, Sarhan AAD, Hamdi M (2013) A fuzzy logic based model to predict surface hardness of thin film TiN coating on aerospace AL7075-T6 alloy. Int J Adv Manuf Technol 68(1–4):415–423. doi[:10.1007/s00170-013-4738-y](http://dx.doi.org/10.1007/s00170-013-4738-y)
- 15. Kohli A, Dixit US (2004) A neural-network-based methodology for the prediction of surface roughness in a turning process. Int J Adv Manuf Technol 25(1–2):118–129. doi[:10.1007/s00170-003-1810-z](http://dx.doi.org/10.1007/s00170-003-1810-z)
- 16. Abdel Badie S (2011) Prediction of surface roughness in end milling process using intelligent systems: a comparative study. Appl Comput Intel Soft Comput. doi[:10.1155/2011/183764](http://dx.doi.org/10.1155/2011/183764)
- 17. Asiltürk İ, Akkuş H (2011) Determining the effect of cutting parameters on surface roughness in hard turning using the Taguchi method. Measurement. doi[:10.1016/j.measurement.2011.07.003](http://dx.doi.org/10.1016/j.measurement.2011.07.003)
- 18. Hasçalık A, Çaydaş U (2007) Optimization of turning parameters for surface roughness and tool life based on the Taguchi method. Int J Adv Manuf Technol 38(9–10):896–903. doi[:10.1007/s00170-007-](http://dx.doi.org/10.1007/s00170-007-1147-0) [1147-0](http://dx.doi.org/10.1007/s00170-007-1147-0)
- 19. Hamdan A, Sarhan AAD, Hamdi M (2012) An optimization method of the machining parameters in high-speed machining of stainless steel using coated carbide tool for best surface finish. Int J Adv Manuf Technol 58(1–4):81–91. doi[:10.1007/s00170-011-3392-5](http://dx.doi.org/10.1007/s00170-011-3392-5)
- 20. Dweiri F, Al-Jarrah M, Al-Wedyan H (2003) Fuzzy surface roughness modeling of CNC down milling of Alumic-79. J Mater Process Tech 133(3):266–275. doi:[10.1016/S0924-0136\(02\)00847-6](http://dx.doi.org/10.1016/S0924-0136(02)00847-6)
- 21. Kilickap E, Huseyinoglu M, Yardimeden A (2010) Optimization of drilling parameters on surface roughness in drilling of AISI 1045 using response surface methodology and genetic algorithm. Int J Adv Manuf Technol 52(1–4): 79–88. doi:[10.1007/s00170-010-2710-7](http://dx.doi.org/10.1007/s00170-010-2710-7)
- 22. Kumar BS, Baskar N (2012) Integration of fuzzy logic with response surface methodology for thrust force and surface roughness modeling of drilling on titanium alloy. Int J Adv Manuf Technol 65(9–12): 1501–1514. doi:[10.1007/s00170-012-4275-0](http://dx.doi.org/10.1007/s00170-012-4275-0)
- 23. Dong M, Wang N (2011) Adaptive network-based fuzzy inference system with leave-one-out cross-validation approach for prediction of surface roughness. Applied Mathematical Modelling 35(3):1024– 1035. doi[:10.1016/j.apm.2010.07.048](http://dx.doi.org/10.1016/j.apm.2010.07.048)
- 24. Zalnezhad E, Sarhan AD, Hamdi M (2013) Investigating the effects of hard anodizing parameters on surface hardness of hard anodized aerospace AL7075-T6 alloy using fuzzy logic approach for fretting fatigue application. Int J Adv Manuf Technol 68(1–4):453–464. doi: [10.1007/s00170-013-4743-1](http://dx.doi.org/10.1007/s00170-013-4743-1)
- 25. Lo S-P (2003) An adaptive-network based fuzzy inference system for prediction of workpiece surface roughness in end milling. J Mater Process Tech 142(3):665–675. doi[:10.1016/S0924-0136\(03\)00687-3](http://dx.doi.org/10.1016/S0924-0136(03)00687-3)
- 26. Kumanan S, Jesuthanam CP, Ashok Kumar R (2008) Application of multiple regression and adaptive neuro fuzzy inference system for the prediction of surface roughness. Int J Adv Manuf Technol 35(7–8): 778–788. doi:[10.1007/s00170-006-0755-4](http://dx.doi.org/10.1007/s00170-006-0755-4)
- 27. Ho S-Y, Lee K-C, Chen S-S, Ho S-J (2002) Accurate modeling and prediction of surface roughness by computer vision in turning operations using an adaptive neuro-fuzzy inference system. Int J Mach Tools Manuf 42(13):1441–1446. doi:[10.1016/S0890-6955\(02\)](http://dx.doi.org/10.1016/S0890-6955(02)00078-0) [00078-0](http://dx.doi.org/10.1016/S0890-6955(02)00078-0)
- 28. Lee K-C, Ho S-J, Ho S-Y (2005) Accurate estimation of surface roughness from texture features of the surface image using an adaptive neuro-fuzzy inference system. Precision Eng 29(1):95–100. doi: [10.1016/j.precisioneng.2004.05.002](http://dx.doi.org/10.1016/j.precisioneng.2004.05.002)
- 29. Jang J-SR, Sun C-T, Mizutani E (1997) Neuro-fuzzy and soft computing : a computational approach to learning and machine intelligence. MATLAB curriculum series. Prentice Hall, Inc, U.S.A.
- 30. Kasabov NK (1997) Foundations of neural networks, fuzzy systems, and knowledge engineering, vol. 33. MIT, Cambridge. doi[:10.1016/](http://dx.doi.org/10.1016/S0898-1221(97)84600-7) [S0898-1221\(97\)84600-7,](http://dx.doi.org/10.1016/S0898-1221(97)84600-7) Computers & Mathematics with Applications, vol 7
- 31. Zalnezhad E, Sarhan AAD, Hamdi M (2012) Prediction of tin coating adhesion strength on aerospace AL7075-T6 alloy using fuzzy rule based system. Int J Precis Eng Manuf 13(8):1453–1459
- 32. Ghani JA, Choudhury IA, Hassan HH (2004) Application of Taguchi method in the optimization of end milling parameters. J Mater Process Tech 145(1):84–92. doi:[10.1016/S0924-0136\(03\)00865-3](http://dx.doi.org/10.1016/S0924-0136(03)00865-3)
- 33. Philip PK (1971) Built-up edge phenomenon in machining steel with carbide. Int J Mach Tools Des Res 11(2):121–132. doi[:10.1016/0020-](http://dx.doi.org/10.1016/0020-7357(71)90021-7) [7357\(71\)90021-7](http://dx.doi.org/10.1016/0020-7357(71)90021-7)