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Multi-objective optimization in single-row layout design using a genetic algorithm

N. Lenin · M. Siva Kumar · M. N. Islam · D. Ravindran

Abstract This paper presents the development of a genetic algorithm for determining a common linear machine sequence for multi-products with different operation sequences and facilities with a limited number of duplicate machine types available for a job. This work aims to minimize the total flow distance traveled by products, reduce the number of machines arranged in the final linear sequence, and decrease the total investment cost of the machines used in the final sequence. We assume that product flow runs only in the forward direction, either via insequence or bypass movement. We demonstrate the effectiveness of the proposed algorithm by solving a typical layout design problem taken from literature, and several randomly generated problems. Results indicate that the proposed algorithm serves as a practical decision support tool for resolving layout problems in manufacturing facilities.

Keywords Facility layout · Linear sequencing · Genetic algorithm · Flow distance · Machine investment

1 Introduction

Modern product lifecycles have become shorter in recent years given rapid technological development. Manufacturing

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companies have responded to this problem by enhancing their production processes, giving rise to the concept of multi-product flow lines in manufacturing systems. The application of this concept to multiple product manufacturing has become a challenge among researchers and enterprises. Multi-product flow lines enable the simultaneous production of different commodities in a single flow line setup, thereby maximizing the manufacturing process [1]. Machine layout or flow line design involves determining the relative positions of machines (i.e., the layout) in facilities where a given product is manufactured.

Assembly cell layouts can be classified as a (a) unidirectional network loop layout, (b) linear single-row layout, (c) linear double-row layout, (d) circular layout, and (e) cluster layout [2, 3]. A linear machine sequence is the most commonly used in production systems because of its simplicity and efficient flow structure [4, 5], and because it lends itself to the arrangement of machines in a variety of flow configurations, such as a straight line, U-shaped line, serpentine line, or loop for a conveyor or automated guided vehicle system [6]. It presents the advantages of shorter flow distance, easier control of the production process, and easier material handling. It is also the most prevalent layout form in cellular manufacturing systems and flexible manufacturing systems (FMSs) [5, 7]. In this work, therefore, we choose a linear machine sequencing method.

2 Literature review

Many researchers have discussed the linear sequencing of machines for solving flow layout problems. Houshyar and McGinnis [8] introduced a heuristic for assigning facilities to locations for the purpose of minimizing the travel distance traversed during work progress in a straight track. The established heuristic exhibited better performance than did the modified and classical lower bound methods.
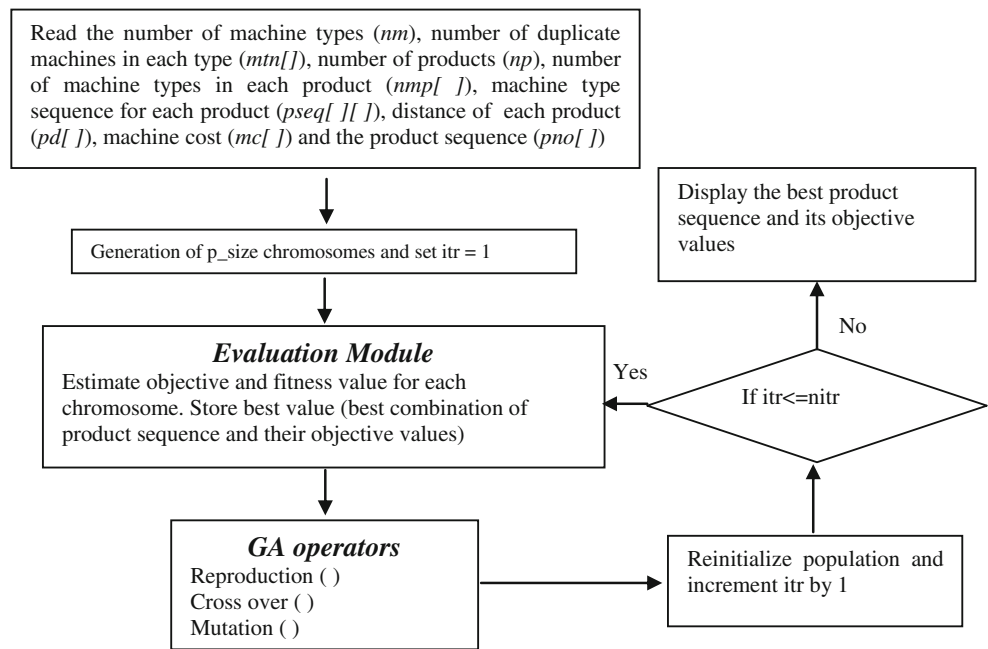
Fig. 1 General schematic diagram of genetic algorithm

The triangle assignment algorithm was used by Heragu and Kusiak [4] in solving the machine layout problems in an FMS. The computational time of the proposed algorithm was comparable to that of existing methods. The authors [9] also presented two efficient models, namely, a linear continuous and linear mixed integer, for facility layout problems. The models do not necessitate prior knowledge of site locations. The authors showed that the continuous models are more useful for solving facility layout problems than are other models presented in literature.

Heragu and Alfa [3] experimentally analyzed simulated annealing-based algorithms, namely, a modified penalty algorithm, the simulated annealing algorithm, and a hybrid simulated annealing algorithm for single-row layout problems in facilities of unequal areas and for multi-row layout problems in facilities of equal areas. The authors concluded that the hybrid algorithm produces better quality solutions than do the first two algorithms, although the former involves slightly longer computational time.

Kouvelis and Chiang [10] implemented a simulated annealing procedure to determine a flow line (or single-row layout) under the assumptions that the number of machines is fixed and backtrack movements are allowed. The authors aimed to determine a machine sequence with minimum total backtrack distance.

Ho et al. [11] proposed two flow analysis methods for a multi-flow line layout design to realize shorter flow distances: The first method features a traditional line structure for analysis, whereas the second implements a network structure. The authors also developed a heuristic pattern-matching method for single-row layout problems in FMSs, in which a linear machine sequence is initially constructed for the product that entails the largest number of operations.

Braglia [12] regarded the linear machine sequencing problem as a non-polynomial hard combinatorial problem. The number of possible sequences grows exponentially because the use of duplicate machines is allowed. Moreover, the set of all feasible sequences is not merely a set of simple permutations of a fixed number of machines given that the sequences must satisfy the different operation sequences of all products. The author determined a linear machine sequence with minimum expected movement of the machine handling device located between machines in a machine cell. The expected movement is determined by the frequency of part displacements between machines.

Table 1 Details of machine, its availability and cost

M. no.	1	2	3	4	5	6	7	8	9
Availability of duplicate machines	2	1	2	2	1	1	2	2	2
Machine cost (Rs.)	24,121	4,546	25,742	27,159	26,738	18,822	21,612	979	12,257

Table 2 Details of machine sequence and demand of individual product

P. no.	Machine sequence	Demand in units
1	4-6-8-1	8
2	7-1-8-2	15
3	5-6-9-8-3	32
4	3-5-1-8	50
5	5-9-8-1-7	42
6	4-6-2-9	29

Wang et al. [13] formulated a model for minimizing the total material handling distance on a shop floor in both inter- and intra-cell facility layouts for cellular manufacturing systems. The authors used an improved simulated annealing algorithm to solve this problem.

Using a simulated annealing algorithm, Ho and Moodie [14] investigated a machine layout problem with a linear single-row flow line for an automated manufacturing system. The authors also investigated the effect of flow line characteristics on machine layouts. They provided vital information on selecting appropriate flow line analysis methods and determining appropriate evaluation criteria for different layout problems.

Chen et al. [15] addressed the problem of determining a common linear machine sequence for multi-products that have different operation sequences and facilities with a limited number of duplicate machine types. The authors intended to minimize the total flow distance traveled by products on this linear flow line by using a modified simulated annealing algorithm.

Diponegoro and Sarker [16] presented a two-stage solution methodology that simplifies computation and generates better solutions for reducing travel distances in production processes that involve sets of identical machines. This problem is often formulated as a tertiary assignment problem because of its combinatorial nature.

Table 3 Initial population

C. no.—chromosome number	Chromosomes
1	1-3-4-5-2-6
2	2-3-1-5-6-4
3	2-3-5-4-6-1
4	2-6-3-4-5-1
5	3-4-1-5-6-2
6	6-1-2-3-4-5
7	2-3-1-6-5-4

According to Hicks [17], layouts produced by a genetic algorithm-based optimization method significantly minimize material movement for a given work schedule in both greenfield and brownfield scenarios. A model for designing an FMS in one or multiple rows with genetic algorithms was discussed by Ficko et al. [18], who established the most favorable number of rows and the sequence of devices in an individual row by using genetic algorithms.

Chrysostomos and Vlachos [1] used the linear programming model for minimal backward flow to determine the optimal linear machine sequence in a manufacturing cell. They applied a modified ACS algorithm to the conditions and parameters of the linear machine layout problem. To determine the optimal linear placement of facilities with varying dimensions on a straight line, Anjosa et al. [19] introduced a semi-definite programming approach for the one-dimensional space-allocation problem, also known as the single-row facility layout problem.

Pillai et al. [20] identified a linear sequence that minimizes the total distance traveled by multiple items with different operation sequences. The authors regarded each type of machine available as limited, and adopted a simulated annealing algorithm in determining the best solution. Solimanpur et al. [21] formulated the single-row machine layout problem as a non-linear 0–1 programming model, in which the distance between the machines is sequence dependent. They developed an ant colony algorithm to solve this problem.

To minimize the total cost of material handling and maximize the requirements of adjacent resources, Gengui et al. [2] developed a multiple objective genetic algorithm approach with a local search method. On the basis of previously developed formulations, solution methodologies, and software packages, Singh et al. [22] discussed the current and future trends of research on facility layout problems. The authors observed a trend toward multi-objective approaches by developing facility layout software using meta-heuristics, such as simulated annealing, genetic algorithm, and concurrent engineering for facility layouts.

Andre and Amaral [23] proposed a mixed 0–1 linear program for the one-dimensional facility layout problem to minimize the weighted sum of distances, while Teo and Ponnambalam [24] proposed a hybrid ACO/PSO heuristic to solve single-row layout problems. For apparel manufacturing, Lin [25] proposed a hierarchical order-based genetic algorithm to minimize the moving distance among cutting pieces in a U-shaped single-row machine layout.

Ramazan et al. [26] and Jannat et al. [5] both considered the same two objectives in solving flow layout problems: minimizing material handling costs and maximizing closeness rating scores. Ramazan et al. proposed a simulated annealing algorithm to identify the non-dominated solution

Fig. 2 Evaluation of chromosome
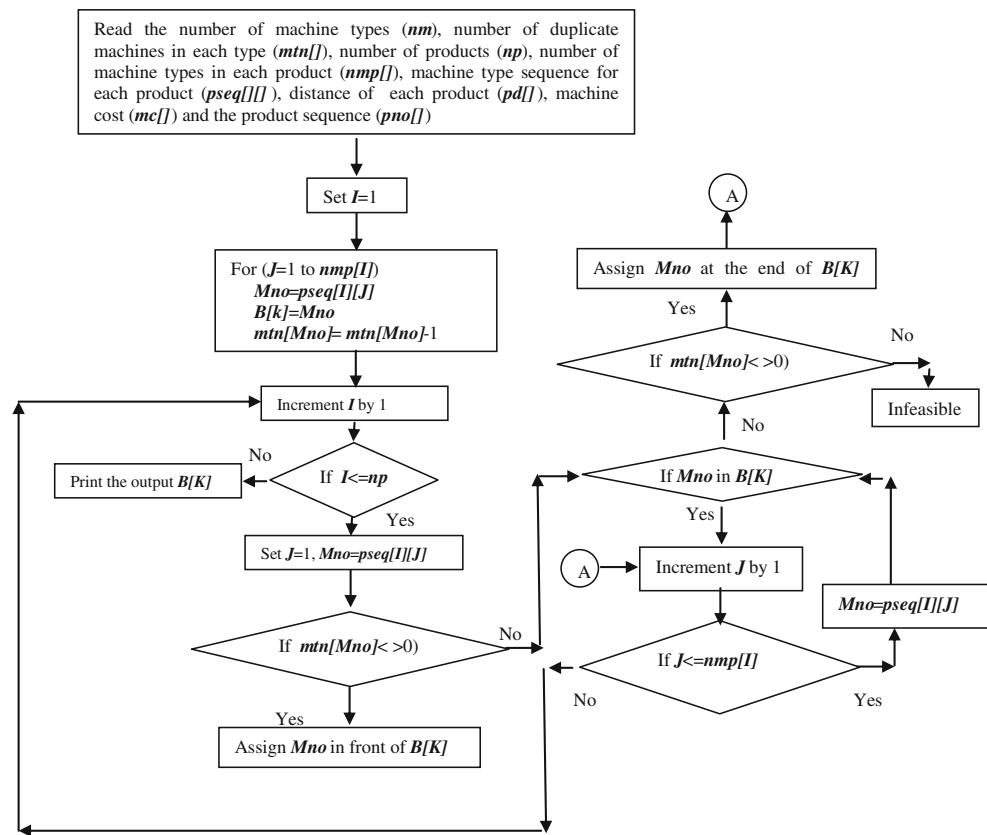
(Pareto optimal) set, while Jannat et al. developed a genetic algorithm for the multi-objective facility layout problem and determined the optimal facility location for a particular problem.

Satheesh Kumar et al. [27] employed an artificial immune system algorithm to minimize material handling costs both in single-row and loop layout problems in FMSs. Siva Kumar et al. [28] developed a simple heuristic to determine the optimal linear sequence that minimizes the flow distance traveled by products.

Dilip Datta et al. [29] developed a permutation based genetic algorithm for arranging the facilities in a line with minimum cost. Giuseppe Aiello et al. [30] proposed a new multi-objective genetic algorithm based on slicing structure encoding for solving unequal area facility layout problems. Amir Sadrzadeh [31] proposed a genetic algorithm with the heuristic procedure to solve the multi-line layout problem.

Despite the considerable effort directed toward solving flow layout problems, most of these studies focused on the optimization of a single parameter only—flow distance. In practice, however, the total number of machines in a layout and the total investment cost of machines are equally important factors. In this work, we aim to determine the linear sequence of machine arrangement that minimizes total flow distance in units;

total number of machines in the final linear sequence; and total investment cost of machines.

3 Problem definition

The locations and number of machines in a linear machine sequence of a single-row layout design are keys to determine the flow distance of multi-products and total investment cost of machines. In facilities with duplicate machines and multiple products, the single-row layout design is considered a non-polynomial hard problem [12].

We present the following assumptions in the proposed method:

a. The number of products, demand for products, machine type sequences, and individual costs of machines are known, along with the availability of duplicate machines.
b. The products always enter the first machine to which they are assigned in the final linear machine sequence.
c. The products' flow distances extend to the end of the respective machine types of the products without affecting the preceding flow.
d. The machines have sufficiently large capacities.
e. Backtracking is prohibited.

Table 4 Final machine sequence for the product sequence 1-3-4-5-2-6

P No.	Product's machines sequence	Machine types / Machines available in stock after assignment (1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	Existing machine sequence	Remarks
		Machine type numbers: 1	2	3	4	5	6	7	8	9		
		Available machines type in stock: 2	1	2	2	1	1	2	2	2		
1	4 6 8 1	1	1	2	1	1	0	2	1	2	4 6 8 1	All machine types are available in stock ie. Mtn[mno] <> 0
3	5 6 9 8 3	1	1	2	1	0	0	2	1	2	5 4 6 8 1	Machine 5 is available in stock. Add this machine in front of the existing sequence. Machine 6 is unavailable in stock. Hence, search the machine 6 in existing sequence. It is available in the existing sequence and take the next machine 9.
	9 8 3	1	1	1	1	0	0	2	0	1	5 4 6 8 1 9 8 3	Machine 9 is unavailable in existing sequence after machine 6 but available in stock. Hence, add it at the end of existing sequence. Similarly, add machine 8 and 3 at the end of existing sequence since, it is available in stock.
4	3 5 1 8	1	1	0	1	0	0	2	0	1	3 5 4 6 8 1 9 8 3	Machine 3 is available in stock. But machine 5 is unavailable in stock and available in existing sequence. Similarly, machine 1 and 8 are also available in the existing sequence after machine 5.
5	5 9 8 1 7	1	1	0	1	0	0	2	0	1	3 5 4 6 8 1 9 8 3	Machine 5 is unavailable in stock. But available in the existing sequence. Similarly, machine 9 and 8 are also available in the existing sequence after machine 5.
	1 7	0	1	0	1	0	0	1	0	1	3 5 4 6 8 1 9 8 3 1 7	Machine 1 is not available in the existing sequence after machines 9 and 8. But machines 1 and 7 are available in stock. Add these machines at the end of existing sequence.
2	7 1 8 2	0	1	0	1	0	0	0	0	1	7 3 5 4 6 8 1 9 8 3 1 7	Machine 7 is available in stock. Add the machine 7 in front of the existing sequence.
	1 8 2	0	0	0	1	0	0	0	0	1	7 3 5 4 6 8 1 9 8 3 1 7 2	Machines 1 and 8 are unavailable in stock. But available in the existing sequence. Machine 2 unavailable in existing sequence after machines 1 and 8, but available in stock, Hence add at the end of existing sequence.
6	4 6 2 9	0	0	0	0	0	0	0	0	1	4 7 3 5 4 6 8 1 9 8 3 1 7 2	Machine 4 is available in stock. Add the machine 4 in front of the existing sequence.
	6 2 9	0	0	0	0	0	0	0	0	0	4 7 3 5 4 6 8 1 9 8 3 1 7 2 9	Machines 6 and 2 are unavailable in stock. But available in the existing sequence. Machine 9 is unavailable after machines 6 and 2 in the existing sequence but available in stock, hence add machine 9 at the end of existing sequence.

[gray]	Product number	[hatched]	Machines available in stock after assignment
[vertical lines]	Assigned machine before the existing machine sequence	[grid]	Machine type already available in the existing sequence
[horizontal lines]	Assigned machine after the existing machine sequence		

4 Mathematical model

The total flow distance of a product in units (td) is determined using Eq. 1. The constraints are presented in Eqs. 2–6:

$$td = \sum_{i=1}^{np} d_i (L_{il} - L_{if}) \qquad (1)$$

where

td   Total flow distance
d_i ith product flow distance
L_{il} ith product's last machine location in the final machine sequence

L_{if} ith product's first machine location in the final machine sequence
np   Number of products

$$L_{ij+1} > L_{ij} \qquad (2)$$

$$L_{ij} > L_{i1} \qquad (3)$$

$$nm_k \leq ndm_k \qquad (4)$$

where

L_{ij+1} ith product's $j+1$th machine location in the final machine sequence

Table 5 Determination of flow distance for the final machine sequence of product sequence 1-3-4-5-2-6

P. no.	Product's machine sequence	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	L_{if}	L_{il}	d_i	fd_i
	Location of final machine sequence	4	7	3	5	4	6	8	1	9	8	3	1	7	2	9				
	List of machines involved in final machine sequence for the individual product's machine sequence	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15				
1	4 6 8 1					4	6	8	1								5	8	8	24
2	7 1 8 2		7	3	5	4	6	8	1	9	8	3	1	7	2		2	14	15	180
3	5 6 9 8 3				5	4	6	8	1	9	8	3					4	11	32	224
4	3 5 1 8			3	5	4	6	8	1	9	8						3	10	50	350
5	5 9 8 1 7				5	4	6	8	1	9	8	3	1	7			4	13	42	378
6	4 6 2 9					4	6	8	1	9	8	3	1	7	2	9	5	15	29	290
Total flow distance																				1,446

fd_i flow distance of ith product

L_{ij} ith product's jth machine location in the final machine sequence

nm_k Number of kth machines available in the final linear machine sequence

ndm_k Number of duplicate kth machine types available for use

$$tm = \sum_{k=1}^{nmt} ndm_k \qquad (5)$$

where

tm   Total number of machines available for use

nmt   Number of machine types

k Index that represents machine type $k=1,2,3,\ldots nmt$.

$$nms \leq tm \qquad (6)$$

where

nms   Total number of machines available in the final linear sequence.

Equation 2 shows that the location of the $j+1$th machine should always be larger than the location of the jth machine in the linear machine sequence. Equation 3 indicates that the location of the $j+1$th machine in the individual product machine sequence should always be larger than the location of the

first machine in the linear machine sequence. According to Eq. 4, the number of kth machines types available in the final linear machine sequence should be less than or equal to the number of duplicate kth machine types available for use. The total number of machines is equal to the sum of the duplicates of individual machine types; this total is given in Eq. 5. Equation 6 shows that the total number of machines in the linear sequence must be less than or equal to the total number of machines available for use, including the duplicate machines.

4.1 Total number of machines in the final linear sequence

The minimum number of machines in the final linear sequence (nms) of the single-row layout design reduces both flow distance and initial investment. This reduction can be expressed using

$$nms = \text{count}(b[\ldots\ldots]), \qquad (7)$$

where $b[\ldots\ldots]$ represents the final linear machine sequence.

4.2 Investment cost of machines

Companies prefer to reduce not only their operation/manufacturing costs but also their initial investment. In the single-

Table 6 Determination of total investment cost of machines for the final machine sequence of product sequence 1-3-4-5-2-6

Machine type	1	2	3	4	5	6	7	8	9	Total investment cost of machines in Rs.
No. of machine type available in final sequence	2	1	2	2	1	1	2	2	2	
Cost of machine type in Rs.	24,121	4,546	25,742	27,159	26,738	18,822	21,612	979	12,257	
Investment cost of each machine types in Rs.	48,242	4,546	51,484	54,318	26,738	18,822	43,224	1,958	24,514	273,846

Table 7 Evaluation result of chromosomes

C no.	Machine sequence	Total investment cost of machines (Z1)	Total number of machines (Z2)	Total flow distance in units (Z3)
1	4-7-3-5-4-6-8-1-9-8-3-1-7-2-9	273,846	15	1,446
2	3-4-5-6-9-8-3-7-1-8-2-7-9	222,566	13	1,376
3	4-3-5-6-9-8-3-7-1-8-2-7-9	222,566	13	1,363
4	4-3-5-4-6-7-1-8-2-9-8-3-1-7	261,589	14	1,341
5	7-1-4-3-5-6-9-8-3-1-8-7-2-9	246,687	14	1,327
6	3-5-7-1-8-4-6-2-9-8-1-3-7	*234,430*	*13*	*1,184*
7	3-4-5-6-9-8-3-7-1-8-2-9-7	222,566	13	1,389
Minimum		222,566	13	1,184
Maximum		273,846	15	1,446

Italics indicate that the machine sequence (3-5-7-1-8-4-6-2-9-8-1-3-7) will produce the optimum objective values of Total investment cost of machines (234430), Total number of machines (13) and Total flow distance in units (1184)

row layout design, the investment cost of machines is expressed by

$$tc = \sum_{k=1}^{nmt} c_k nm_k \qquad (8)$$

where

tc Total investment cost of machines in the final linear sequence
c_k Cost of the kth machine type.

4.3 Average fitness factor

The total flow distance in units, total number of machines in the final linear sequence, and total investment cost of machines are at different ranges or levels. Summing up the above-mentioned values of different levels will not produce the best result. We therefore apply the average fitness factor method [32] to derive values within the range of 0 to 1. The normalized values of total flow distance, total number of machines, and investment cost of machines are determined using Eqs. 9–11.

$$ntd_l = \frac{td_{max} - td_l}{td_{max} - td_{min}} \qquad (9)$$

$$nnms_l = \frac{nms_{max} - nms_l}{nms_{max} - nms_{min}} \qquad (10)$$

$$ntc_l = \frac{tc_{max} - tc_l}{tc_{max} - tc_{min}} \qquad (11)$$

where

ntd_l	Normalized value of the total flow distance of multi-products for the lth sequence of products
$nnms_l$	Normalized value of the total number of machines in the final linear machine sequence for the lth sequence of products
ntc_l	Normalized value of the total investment cost of machines for the lth sequence of products
td_{min} and td_{max}	Minimum and maximum values of the total flow distance for 1,2,3, … l number of sequences of products
nms_{min} and nms_{max}	Minimum and maximum number of machines in the final linear sequence for 1,2,3, …l number of sequences of products
tc_{min} and tc_{max}	Minimum and maximum values of the total investment cost of machines for 1,2,3, …l number of sequences of products
td_l	Total flow distance of multi-products for the lth sequence of products

Table 8 Probability and cumulative probability of the chromosomes

C. no.	nZ1	nZ2	nZ3	*f(x)*	nf(x)	Pro	cum_pro
1	0	0	0	0	1	0.18387	0.18387
2	1	1	0.267176	2.267176	0.711716	0.130863	0.314733
3	1	1	0.316794	2.316794	0.706439	0.129893	0.444625
4	0.239021	0.5	0.400763	1.139784	0.842849	0.154974	0.599599
5	0.529622	0.5	0.454198	1.48382	0.800457	0.14718	0.746779
6	0.768643	1	1	2.768643	0.660145	0.121381	0.868159
7	1	1	0.217557	2.217557	0.717033	0.131841	1

nZ1, *nZ2*, and *nZ3* normalized objective values of Z1, Z2 and Z3; *f(x)* fitness value; *nf(x)* new fitness value; *Pro* probability; *cum_pro* cumulative probability

Table 9 Selected chromosomes for reproduction

C. no.	r_{srp}	O.C. no.	R.C. no.	Selected chromosomes for reproduction
1	0.6300	5	1′	3-4-1-5-6-2
2	0.4100	3	2′	2-3-5-4-6-1
3	0.1250	1	3′	1-3-4-5-2-6
4	0.8300	6	4′	6-1-2-3-4-5
5	0.260	2	5′	2-3-1-5-6-4
6	0.7300	6	6′	6-1-2-3-4-5
7	0.3250	3	7′	2-3-5-4-6-1

r_{srp} random number for selection for reproduction; *O.C. no.* old chromosome number; *R.C. no.* selected chromosomes for reproduction

nms_l	Total number of machines in the final sequence of the *l*th sequence of products
tc_l	Total investment on machines for the *l*th sequence of products.

The average fitness factor value is determined by Eq. 12. In the minimization problem, the maximum value of the average fitness factor is considered.

$$ndmc_l = \frac{ntd_l + nnms_l + ntc_l}{3} \qquad (12)$$

where

$ndmc_l$ Average fitness factor for the *l*th sequence of products.

The corresponding linear machine sequence of the aforementioned maximum average fitness factor value is the optimum sequence among the *l* number of sequences of products.

5 Genetic algorithm

The basic concept of genetic algorithms is explained in Gengui et al. [2]. In the present work, the product numbers

Table 10 Chromosomes before and after cross-over

R.C. no.	Chromosomes before cross-over	r_{co}	Selected	r_{cp}	Chromosomes after cross-over	C.C. no.
1′	3-4-1-5-6-2	0.32	Yes	4	6-2-3-4-1-5	1″
2′	2-3-5-4-6-1	0.76	No		2-3-5-4-6-1	2″
3′	1-3-4-5-2-6	0.08	Yes	1	3-4-5-2-6-1	3″
4′	6-1-2-3-4-5	0.019	Yes	2	2-3-4-5-6-1	4″
5′	2-3-1-5-6-4	0.89	No		2-3-1-5-6-4	5″
6′	6-1-2-3-4-5	0.28	Yes	3	3-4-5-6-1-2	6″
7′	2-3-5-4-6-1	0.92	No		2-3-5-4-6-1	7″

r_{co} random number for cross-over; r_{cp} cutting point; *C.C. no.* chromosome number after cross-over

are considered as genes, the product sequences are regarded as chromosomes, and the number of products is viewed as chromosome length. The general schematic of the genetic algorithm proposed in the current paper is shown in Fig. 1.

The proposed algorithm yields consistent solutions with minimum total flow distance, minimum number of machines, and minimum total investment cost of machines with acceptable computational time. A detailed numerical illustration is provided in the succeeding section.

6 Numerical illustration

The following example problem is considered to illustrate the effectiveness of the proposed genetic algorithm. Table 1 shows the number of machine types (M. no.), their availability, and their individual costs.

The product number (P. no.), individual product's machine type sequences, and demand for the product in units (flow distance) are listed in Table 2.

The product numbers (e.g., 1, 2, 3, 4, 5, 6) are genes, whereas the product sequences (e.g., 1-3-4-5-2-6) are chromosomes. The chromosome length is the number of products involved in the problem. The roulette wheel selection is used for the selection of reproduction. The single-point cross-over technique is adopted for the search of new strings in the search space. Based on the sensitivity analysis, the cross-over and mutation probabilities are considered as 0.5 and 0.02, respectively [33]. The complete replacement policy is implemented since; it yields better results [33].

The C program developed for this purpose terminates automatically when no further change occurs in the previously derived best solutions, and it operates for an additional 50 iterations to ascertain the best solution obtained in continuous mode. The number of iterations required (e.g., 1,000) may be incorporated into the developed program. Table 3 shows the initial population and Fig. 2 presents the flow chart of chromosome evaluation. The detailed procedure for calculating the final machine sequence for product sequence 1-3-4-5-2-6 is presented in Table 4. The flow distance and total investment cost of machines for the aforementioned product sequence are listed in Tables 5 and 6, respectively. The final machine sequence, total investment cost of machines, total number of machines, and total flow distance of the individual chromosomes are presented in Table 7.

The calculated values of total flow distance in units, total number of machines in the final linear sequence, and total investment cost of machines are at different levels. To obtain the same level for all three, we introduce an average fitness factor method (Table 8) [25]. The fitness function is considered the sum of all the normalized values of Z1, Z2, and Z3, and the new fitness values are calculated on the basis of the

Table 11 Chromosomes before and after mutation

C.C. no.	Chromosomes before mutation	r_m						Chromosomes after mutation	M.C. no
1″	6-2-3-4-1-5	0.31	0.49	0.74	0.92	0.84	0.04	6-2-3-4-1-5	1‴
2″	2-3-5-4-6-1	0.1	0.43	0.21	0.85	0.012	0.54	2-3-5-4-1-6	2‴
3″	3-4-5-2-6-1	0.01	0.56	0.67	0.89	0.005	0.45	4-3-5-2-1-6	3‴
4″	2-3-4-5-6-1	0.008	0.003	0.61	0.07	0.09	0.12	3-4-2-5-6-1	4‴
5″	2-3-1-5-6-4	0.4	0.21	0.006	0.32	0.007	0.38	2-3-5-1-4-6	5‴
6″	3-4-5-6-1-2	0.05	0.003	0.002	0.07	0.94	0.12	3-4-6-5-1-2	6‴
7″	2-3-5-4-6-1	0.1	0.43	0.21	0.85	0.012	0.54	2-3-5-4-1-6	7‴

r_m Random number for mutation; *M.C. no.* chromosome number after mutation

expression given below. Equation 14 is used to determine the probability of the chromosomes. The probability and cumulative probability of the individual chromosomes are listed in Table 8.

$$nf(x_i) = E^{-0.15f(x_i)} \qquad (13)$$

$$pro_i = \frac{nf(x_i)}{\sum\limits_{i=1}^{cno} nf(x_i)} \qquad (14)$$

where

$f(x_l)$	Fitness value
$nf(x_l)$	New fitness value
pro_l	Probability
cno	Number of chromosomes

A random number (r_{srp}) is generated for each chromosome to select the reproduction process. From Table 8, we choose the chromosomes that correspond to the cumulative probability value, which is the next highest value after r_{srp}. Table 9 lists the chromosomes selected for reproduction. The cross-over probability (p_cro) is assumed to be 0.5, and a random number (r_{co}) is generated for each

chromosome selected for reproduction. The chromosome is chosen for cross-over operation only if r_{co} is less than or equal to p_cro.

A random number (r_{cp}) is generated within the number of products (np) for each chromosome selected for cross-over. The genes after and before the cutting point (r_{cp}) are interchanged and presented in Table 10.

To avoid local minima, mutation is carried out using the genetic algorithm. Based on the sensitivity analysis, a value of 0.02 is assumed as the mutation probability (p_mut), and a random number (r_m) is generated for each gene of all the chromosomes. If r_m is less than or equal to p_mut, then the corresponding gene is mutated with a neighbor gene (Table 11).

A complete replacement strategy is assumed, which replaces the initial population with the mutated chromosomes. Table 12 shows the chromosomes generated after the first iteration. The above-mentioned steps are repeated until a specific number of iterations (about 1,000 iterations) is reached. The fitness factor values for all the iterations are shown in Fig. 3.

7 Computational results and discussion

We use the proposed algorithm to solve additional problems; the ones discussed in this paper are the first five problems solved by Pillai et al. [20], Chen et al. [15], and

Table 12 Chromosomes after first iteration/new population chromosomes

| M.C. no.	Chromosomes after mutation	C. no.	Machine sequence	Total machine cost (Z1)	Total number of machines (Z2)	Total flow distance (Z3)
1‴	6-2-3-4-1-5	1	4-3-5-7-1-8-4-6-2-9-8-3-1-7	261,589	14	1,160
2‴	2-3-5-4-1-6	2	4-3-5-6-9-8-3-7-1-8-2-7-9	222,566	13	1,363
3‴	4-3-5-2-1-6	3	4-7-3-5-1-8-6-9-8-3-1-7-2-9	246,687	14	1,300
4‴	3-4-2-5-6-1	4	4-7-1-3-5-6-9-8-3-1-8-2-7-9	246,687	14	1,413
5‴	2-3-5-1-4-6	5	4-3-4-5-6-9-8-3-7-1-8-2-7-9	249,725	14	1,376
6‴	3-4-6-5-1-2	6	7-1-4-3-5-6-9-8-3-1-8-2-9-7	246,687	14	1,367
7‴	2-3-5-4-1-6	7	4-3-5-6-9-8-3-7-1-8-2-7-9	222,566	13	1,363
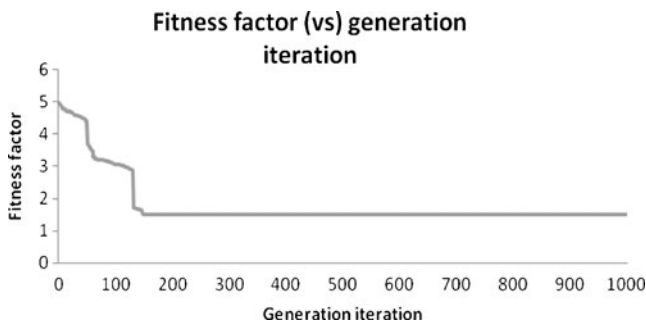
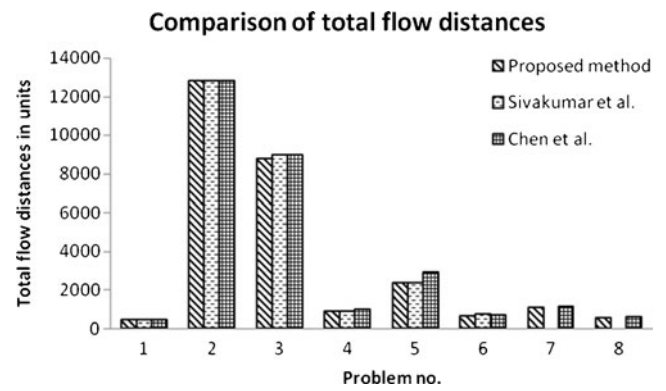Fig. 3 Fitness factor (vs) generation iteration

Fig. 4 Comparison of total flow distances

Siva Kumar et al. [28], as well as problems that are randomly generated. Input data, such as the number of products and their machine type sequences and product demand, are listed in Table 14 of the Appendix. The number of machine types and their duplicate numbers are listed in Table 15 of the Appendix. The cost of individual machine types is listed in

Table 16 of the Appendix. The final linear machine sequence, product sequence, total flow distance, total machine cost, and total number of machines in the final linear sequence are presented in Table 13.

Table 13 Computation results

Problem no.	No. of machine types	No. of products	Method	Total flow distance in units	Total machine cost in Rs.	Total no. of machines in the sequence	Product's sequence	Optimal final linear sequence
1	14	4	Proposed	475	73,567	14	1-3-2-4	1-14-2-3-4-6-8-9-7-13-5-10-11-12
			Siva Kumar et al.	475	73,567	14	1-3-2-4	1-14-2-3-4-6-8-9-7-13-5-10-11-12
			Pillai et al. + Chen et al.	475	73,567	14	1-3-2-4	14-1-2-3-4-6-8-9-7-13-5-10-11-12
2	10	5	Proposed	12800	1,151,057	10	1-2-3-4-5	5-3-2-7-1-8-9-6-4-10
			Siva Kumar et al.	12800	1,151,057	10	1-2-3-4-5	5-3-2-7-1-8-9-6-4-10
			Pillai et al.	12800	1,151,057	10	1-5-3-4-2	5-3-2-7-1-8-9-6-4-10
3	14	5	Proposed	8800	101,000	8	1-4-3-2-5	4-1-3-2-6-5-1-7
			Siva Kumar et al.	9000	114,000	9	1-2-3-4-5	4-6-1-7-1-3-2-6-5
			Pillai et al.	9000	114,000	9	1-2-3-4-5	4-6-1-7-1-3-2-6-5
4	15	4	Proposed	890	58,562	12	3-4-1-2	2-10-12-14-13-7-11-15-5-3-1-4
			Siva Kumar et al.	890	58,562	12	3-4-1-2	2-10-12-14-13-7-11-15-5-3-1-4
			Chen et al.	989	58,562	12	3-4-1-2	2-10-12-14-13-7-11-15-5-1-4-3
5	14	6	Proposed	2388	296,406	14	5-3-4-1-6-2	2-4-8-5-3-11-13-14-7-12-9-1-10-6
			Siva Kumar et al.	2388	296,406	14	5-3-4-1-6-2	2-4-8-5-3-11-13-14-7-12-9-1-10-6
			Chen et al.	2939	296,406	14	5-3-4-1-6-2	4-2-8-5-3-11-13-14-1-10-7-12-9-6
6	13	5	Proposed	640	269,198	17	1-5-2-3-4	12-3-7-1-11-4-8-6-5-8-2-10-9-6-5-7-2
			Siva Kumar et al.	776	314,687	19	5-4-1-3-2	4-8-6-1-11-4-5-8-2-12-3-7-1-10-9-5-7-2-6
			Chen et al.	694	269,198	17	5-4-1-3-2	12-3-7-1-11-4-8-6-5-8-2-10-9-5-7-2-6
7	9	6	Proposed	1080	234,430	13	6-1-4-5-2-3	7-3-5-1-8-4-6-2-9-8-1-7-3
			Siva Kumar et al.	Infeasible solution				
			Chen et al.	1174	234,430	13	4-5-3-6-2-1	3-5-7-1-8-4-6-2-9-8-1-7-3
8	7	7	Proposed	558	186,514	13	2-3-5-1-4-6-7	4-2-1-3-5-7-1-2-4-6-7-5-6
			Siva Kumar et al.	Infeasible solution				
			Chen et al.	606	206,368	14	5-2-4-3-7-6-1	4-2-1-3-5-4-6-7-1-3-7-2-5-6

Fig. 5 Comparison of total investment cost of machines
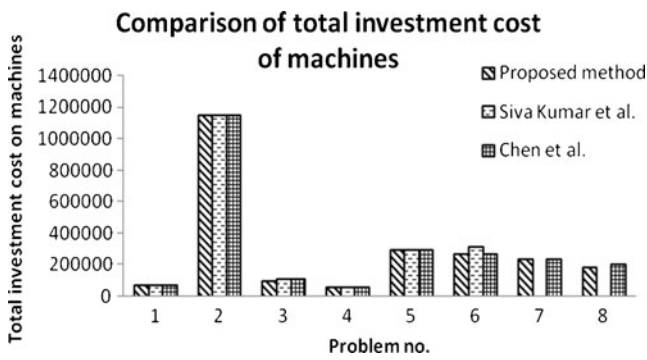

Fig. 7 Comparison of combined objectives

In Figs. 8–10, the Y axis value is the sum of flow distance (considered in 1,000), investment cost of machines (considered in 100,000) and number of machines in the final machine sequence.

The computational results of the proposed method (i.e., total flow distance, total investment cost of machines, and total number of machines in the final linear sequence) are compared with the findings of Siva Kumar et al. [28] and Chen et al. [15]. The comparisons of the individual objective functions are illustrated in Figs. 4, 5, 6, which show that the proposed method is superior to the other two methods. In all the problems, the proposed method generates lower objective values. In the first two problems, the three methods derive equal objective values. In problem numbers 7 and 8, the method proposed by Siva Kumar et al. [28] produces an infeasible solution. The comparison of the combined objectives of the above-mentioned methods is illustrated in Fig. 7, which shows that the proposed method produces a minimum objective value. Figures 8, 9, 10 demonstrate that the proposed method not only produces lower values of individual objective functions, but also yields minimum combined objective values compared with the other approaches. From these illustrations, we conclude that the proposed algorithm yields the best linear sequence
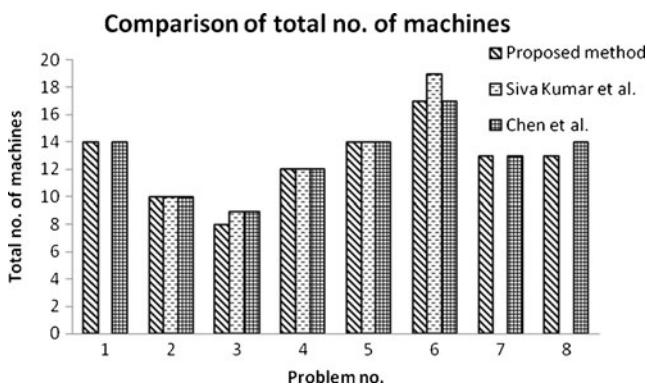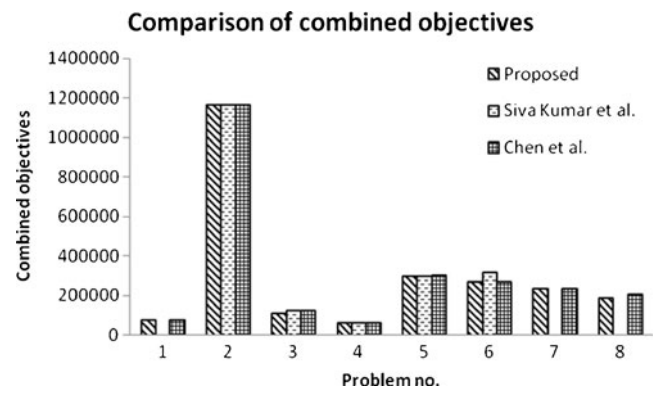
of machines; it minimizes the total flow distance in units, total investment cost of machines, and total number of machines.

The proposed algorithm yields minimum flow distance, minimum number of machines, and minimum investment cost of machines because of the following reasons:

a   Machines are assigned not on the basis of the descending order of the flow distance of a product's sequence.
b   The number of machines used in every machine type in the final linear machine sequence is reduced.
c   The unassigned machine types are incorporated at the front or back flow of the existing machine sequence, depending on availability.
d   If one of the machine types is assigned and it is available in the existing sequence, its availability in this sequence is verified even if the remaining machine types are unassigned. If any of the remaining machine types are unavailable in the existing sequence and are unassigned, then the machine type is incorporated at the back flow of the existing sequence without affecting the previous product machine type sequences.
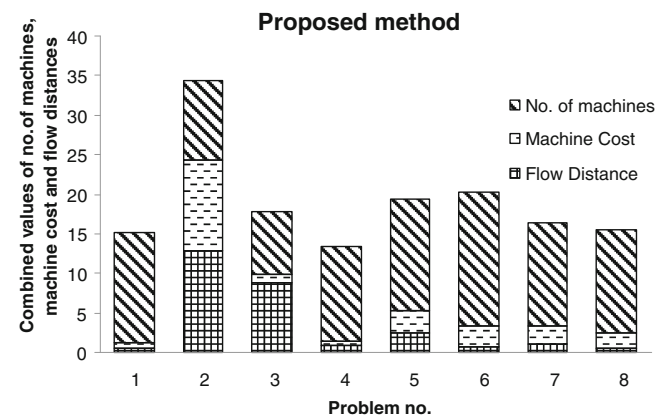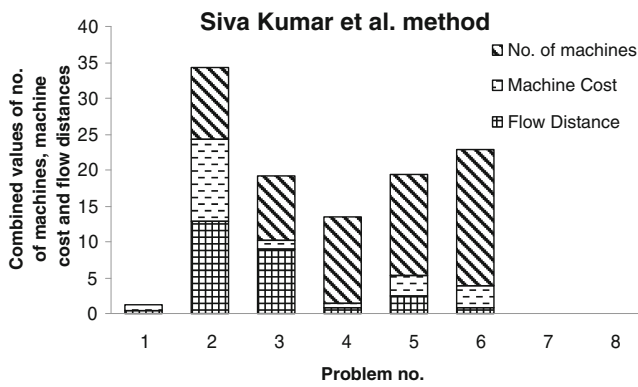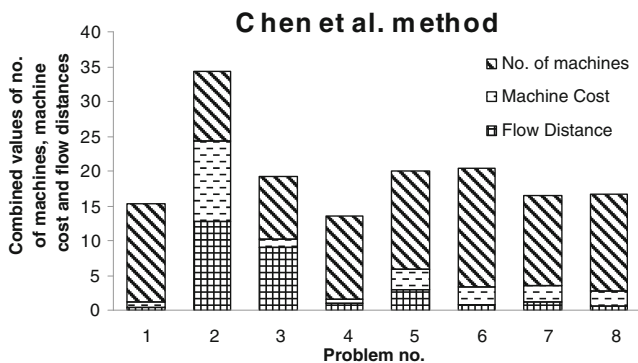

Fig. 6 Comparison of total number of machines

Fig. 8 Problem number versus combined values of number of machines, machine cost, and flow distances for the proposed method

Fig. 9 Problem number versus combined values of number of machines, machine cost, and flow distances for the method of Siva Kumar et al.

8 Conclusion

The linear sequence of machines in a layout design determines the flow distance and investment cost of machines for multi-products of different operation sequences with a single or limited number of duplicate machines of each type. In this work, a genetic algorithm is proposed for constructing a linear sequence of machines that minimizes total flow distance in units, total investment cost of machines, and total number of machine types arranged in the final linear sequence. It is concluded that the proposed method is highly efficient both in individual objective functions and in combined objective functions. Other than the problems discussed in literature, several other problems were generated and experimented on using the proposed algorithm. Compared with previous approaches, our method generates more favorable results. As an extension to this work, we will consider the material handling costs of machine types. Optimization techniques such as PSO and Tabu Search may also be used to solve problems.

Fig. 10 Problem number versus combined values of number of machines, machine cost, and flow distances for the method of Chen et al.

Appendix

Table 14 Operation sequences and product demand of example problems

Problem no	Products	Operation sequence	Product demand
1 Pillai et al. + Chen et al.	1	2-3-4-6-8-9-7	20
	2	14-2-3-4-5-10-11-12	10
	3	2-4-6-8-9-13	15
	4	1-2-3-5-11-12	10
2 Pillai et al.	1	1-8-9-6-4	700
	2	5-3-2-7	600
	3	5-3-2-9	500
	4	3-7-6-4	400
	5	3-2-7-9-10	300
3 Pillai et al.	1	1-3-2-6-5	800
	2	4-6-1-7	400
	3	4-1-6-5	300
	4	4-3-2-5	200
	5	4-1-3-2	100
4 Chen et al.	1	14-13-7-15	34
	2	2-10-12-13	29
	3	11-15-5-3	94
	4	15-5-1-4	89
5 Chen et al.	1	4-5-3-9	69
	2	5-3-7-6	13
	3	13-7-12-9	113
	4	8-5-3-14	72
	5	11-13-14-7	131
	6	2-5-1-10	36
6	1	8-2-10-9-6	34
	2	4-8-6-5	2
	3	1-11-4-5	30
	4	12-3-7-1	36
	5	10-9-5-7-2	48
7	1	4-6-8-1	8
	2	7-1-8-2	15
	3	5-6-9-8-3	32
	4	3-5-1-8	50
	5	5-9-8-1-7	42
	6	4-6-2-9	29
8	1	1-3-5-7	12
	2	2-4-6-7	18
	3	3-5-7-1	15
	4	4-2-3-7	16
	5	7-2-5-6	20
	6	1-3-2-6	13
	7	5-4-7-6	14

Table 15 Machine types and its duplicates for the example problems

Problem no.	Machines types														
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
2	1	1	1	1	1	1	1	1	1	1					
3	2	1	1	1	1	2	1								
4	1	1	1	2	1	2	2	2	2	2	1	2	1	1	1
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
6	2	2	2	2	2	2	2	2	2	1	2	1	2		
7	2	1	2	2	1	1	2	2	2						
8	2	2	2	2	2	2	2								

Table 16 Machine types and its cost for the example literature problems

Machines types	Problem no.							
	1	2	3	4	5	6	7	8
1	8,788	84,565	10,000	8,788	21,011	20,831	24,121	12,315
2	6,589	74,325	15,000	6,589	28,752	12,380	4,546	14,445
3	3,512	59,874	16,000	3,512	26,354	22,658	25,742	19,854
4	6,541	39,998	12,000	6,541	17,655	24,658	27,159	16,547
5	3,254	47,775	11,000	3,254	21,357	17,230	26,738	15,487
6	9,874	22,225	13,000	9,874	16,554	16,660	18,822	13,221
7	6,547	14,411	14,000	6,547	11,357	12,557	21,612	11,315
8	8,541	15,455		8,541	30,699	6,088	979	
9	3,256	134,545		3,256	19,220	10,912	12,257	
10	1,111	657,884		1,111	12,632	27,943		
11	2,222			2,222	10,228	24,234		
12	3,333			3,333	24,998	8,132		
13	4,445			4,445	27,111	20,831		
14	5,554			5,554	28,478			
15				6,666				

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