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Discrete Element Modeling of Stick-Slip Instability and Induced Microseismicity

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Abstract-Using Particle Flow Code, a discrete element model is presented in this paper that allows direct modeling of stick-slip behavior in pre-existing weak planes such as joints, beddings, and faults. The model is used to simulate a biaxial sliding experiment from literature on a saw-cut specimen of Sierra granite with a single fault. The fault is represented by the smoothjoint contact model. Also, an algorithm is developed to record the stick-slip induced microseismic events along the fault. Once the results compared well with laboratory data, a parametric study was conducted to investigate the evolution of the model's behavior due to varying factors such as resolution of the model, particle elasticity, fault coefficient of friction, fault stiffness, and normal stress. The results show a decrease in shear strength of the fault in the models with smaller particles, smaller coefficient of friction of the fault, harder fault surroundings, softer faults, and smaller normal stress on the fault. Also, a higher rate of displacement was observed for conditions resulting in smaller shear strength. An increase in *b*-values was observed by increasing the resolution or decreasing the normal stress on the fault, while bvalues were not sensitive to changes in elasticity of the fault or its surrounding region. A larger number of recorded events were observed for the models with finer particles, smaller coefficient of friction of the fault, harder fault surroundings, harder fault, and smaller normal stress on the fault. The results suggest that it is possible for the two ends of a fault to be still while there are patches along the fault undergoing stick-slips. Such local stickslips seem to provide a softer surrounding for their neighbor patches facilitating their subsequent stick-slips.

Key words: Stick-slip, Particle flow code (PFC), microseismic, fault instability.

1. Introduction

It is believed that the mechanism of fault instability involves multiple local on and off slips of patches referred to as "stick-slip" along the fault (BRACE and BYERLEE 1966). Such small stick-slips may be recorded as "foreshocks" leading to "main shocks" and followed by "aftershocks" each releasing different levels of acoustic energy. Various aspects of fault instability have been already studied by laboratory experiments (BRUNE *et al.* 1993; BYERLEE and BRACE 1968; DIETERICH 1981; JULIAN *et al.* 1998; OHNAKA 1973) as well as numerical continuum models (DALGUER and DAY 2006; DAY *et al.* 2005; GALIS *et al.* 2008; XING *et al.* 2004) and numerical discontinuum models (FINCH *et al.* 2003; MORA and PLACE 1994; MORGAN 2004; PLACE *et al.* 2002).

Compared to continuum models, the discrete element method (DEM) has the capability to model geometrical heterogeneity by size distribution of particles as well as looking into the rupture process of rocks with more details. Using Particle Flow Code (PFC3D) v.5.0 in this research, a discrete representation of the fault is modeled, and release of acoustic energy due to its stick-slip instability is studied. For this purpose, a large scale laboratory experiment conducted on granite with a single fault originally reported by DIETERICH (1979) and recently repeated with microseismic recording by MCLASKEY and KILGORE (2013) was numerically simulated.

Traditionally, the approach for modeling microseismicity with PFC has been to consider each bond breakage (crack) as a single AE event with the further possibility of clustering the events to form more realistic magnitudes (HAZZARD 1998). This approach has been successfully used in modeling the intact rock problems where the events are believed to have a compressive induced crack nature (HAZZARD and YOUNG 2002, 2004; YOUNG and DEDECKER 2005; YOUNG *et al.* 2001; ZHAO and YOUNG 2011). However, in the present research, new routines have been developed for recording slip-induced microseismic

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events. The results have been compared with the experimental data. A parametric study has been conducted to study the effect of various factors on a fault's behavior.

This knowledge could also be useful for problems other than earthquake studies where there is likelihood of two planes sliding on each other such as in landslides (PENG and GOMBERG 2010), basal gliding of ice glaciers (JANSEN 2006; ROUX *et al.* 2008), and microseismic monitoring of a sedimentary rock mass in petroleum projects (FAIRHURST 2013; KRISTIANSEN *et al.* 2000).

2. Theory of Slip

The basics of how slip occurs in physics are briefly explained using Fig. 1 (left). As the applied driving force to the block, f_d , is increased, the resistive frictional force (solid red line) is also increased until at point *a*, f_d reaches the maximum static frictional resistance, the frictional resistance drops to lower values known as kinetic friction (or as simplified by the dotted blue curve), the spring unloads following a line with the slope equal to its stiffness (dashed green line), *K*, and the block starts to move.

The spring's unloading continues even after the applied force is equal to the kinetic friction at point c,

meaning deceleration of the block until the final stop at point *e* where the excess energy is dissipated (Δ abc equals Δcde) (SCHOLZ 2002). In reality, once the motion eventually stops (point e), there has to be a "healing" mechanism for friction to regain its static value so that further slips can happen. This process of multiple slips and stops is called "stick-slip" and is believed to be the mechanism of earthquakes (BRACE and Byerlee 1970). RABINOWICZ (1951, 1958) first suggested that if two surfaces are in contact in a stationary condition under load for time t, the coefficient of static friction increases approximately as logt. He also proposed that a minimum displacement of D_c , "critical slip distance", is required for transition from static friction state to kinetic friction state. With regard to Fig. 1 (left), the condition required for the onset of instability can be mathematically expressed by Eq. (1):

$$\left|\frac{\partial f_{\rm f}}{\partial u}\right| = \frac{(\mu_s - \mu_k)N}{D_{\rm c}} > K \tag{1}$$

where $|{}^{Of}f_{Ou}|$ is variations of resistive frictional force, f_f , for increments of displacement, u. The parameters μ_s and μ_k are static and kinetic coefficients of friction, respectively, N is the normal stress on the block, D_c is critical slip distance, and K is the stiffness of spring.

The physical implication of the stiffness of spring, K, in this model can be thought of as the



Figure 1

(*Left*) solid red line is variations of the resistive frictional force. The simplified change in friction is shown in *dotted blue*. The *dashed green* line shows variations of the driving force once the block starts to move until it stops. (*Right*) horizontal section of a more realistic model for the fault. The masses, stiffness of springs, and normal stress on each block are not necessarily equal due to heterogeneity. Three arbitrary patches are shown with *dotted red*, *solid purple*, and *dashed green*. The *red* and *green* patches can slide simultaneously

elastic conditions of the vicinity of a fault in nature or the stiffness of the loading machine in the laboratory. From Eq. (1), it is obvious that instability depends on the normal stress, elastic properties of the medium surrounding the fault, and roughness of the fault. The major microseismic events in the field are believed to be the result of stress drop followed by slip on fractures and consequently release of energy (DAMJANAC et al. 2010). However, if the stress drop is not large enough to impose excess energy to the system, i.e., after point "a" in Fig. 1 (left), the drop in resistive frictional force (solid red line) is such that it is placed above the unloading line (dashed green line), the slip would be aseismic. Therefore, in reality not every slip is the source of instability and considered seismic.

The assumption behind the model explained by Fig. 1 (left) is that the block can be regarded as a single mass point. PERSSON and TOSATTI (1999) suggest that for this assumption to be valid, the dimension of block, $L_{\rm B}$, has to be smaller than a characteristic "elastic coherence length", ξ , otherwise, the block has to be discretized to smaller cells with the size, ξ , connected to each other by elastic springs. Therefore, it is necessary to take into account heterogeneity and nonuniform geometry of faults (NIELSEN et al. 1995, 2000). A more realistic model for the fault is shown in Fig. 1 (right). In this model, the mass, stiffness of springs, and normal stress on each block is different, and thus different patches may form and slide at different times or simultaneously.

3. Description of the Experiment

DIETERICH (1979) studied the scale dependence of the fault instability process through a large scale biaxial laboratory experiment. A large specimen of Sierra white granite with dimensions $1.5 \times 1.5 \times 0.419$ m was sawed diagonally at the quarry and roughened in the laboratory by lapping the two surfaces together with 30 grit silicon carbide abrasive to represent the fault with peak-to-trough surface roughness of 0.08 mm (DIETERICH 1981). He concluded that a minimum fault length was required so that confined shear instability could occur along a preexisting fault. Although strain gauges and velocity transducers were mounted on the model, no types of acoustic emission sensors were used during his experiment. The scalar seismic moments were later calculated from the general formula as:

$$M_0 = \mu DA \tag{2}$$

where μ is the shear modulus, D is the average local seismic displacement and A is the area of the fault. A similar experiment on the same specimen was conducted by McLASKEY et al. (2014) and MCLASKEY and KILGORE (2013) at the USGS, California, with 14 piezoelectric sensors recording the microseismic events during the test. This large model would allow the fault to be studied realistically so that some parts of it could slide while the rest was not slipping. In this way, individual stickslips can occur during the loading with the possibility that they might trigger other slides. However, since this specimen had been used for 25 years resulting in many stick-slip events and cumulative without additional surface preparation, slips MCLASKEY et al. (2014) believed that the present surface was smoother than it was in 1981.

The test setup was a steel frame with four flatjacks between the frame and the specimen as shown in Fig. 2. The model was loaded in σ_2 direction and unloaded in σ_1 direction by increasing and decreasing the pressures slowly along the 1 and 2 directions, respectively, with the same rate of 0.001 MPa/s. This way, the normal pressure on the fault was kept constant while the fault was shearing. They tried to model the earthquake cycle by loading, resetting and holding at four stages. Slip sensors were installed on top of the fault to measure relative slips from one side of the fault to the other. Piezoelectric sensors were also installed on top and bottom of the fault. The sensors would respond to the vertical component of motion in frequency ranges of $\sim 100-1$ MHz and were installed 200 mm off the fault. The onset of instability was observed at 3.7 MPa of shear stress. At this point, the fault would experience several small falls and rises in the shear stress each accompanied by a small displacement along the fault. These small displacements have been reported to range from 0.08 to 0.15 mm (G. McLASKEY, personal communication, 2013). The



(*Left*) McLaskey's experimental setup. (*Right*) slip sensors and piezoelectric sensors. Piezoelectic sensors are mounted on the top and bottom of the sample. Flatjacks are marked FJ1 to FJ4. Strain gages are shown by S1 to S15. (McLaskey and Kilgore 2013)

shear modulus and critical slip distance of the Sierra white granite were estimated to be around 20 GPa and 5 μ m, respectively (G. McLASKEY, personal communication, 2013).

4. Numerical Model

In this research, Particle Flow Code (PFC3D) v.5.0 is used to model the experiment reported by McLASKEY and KILGORE (2013). PFC3D is an explicit implementation of the distinct element method (DEM) developed by Itasca, and despite continuum models, does not require mesh generation. In this code, it is assumed that the particles are rigid (non-deformable). In a PFC3D model, particles are bonded by models such as the parallel bond model and smooth joint model. Parallel bonds can transmit both forces and moments and can be envisioned as a short length beam or a "set" of elastic springs uniformly distributed over a circular cross-section at the contact point (POTYONDY and CUNDALL 2004).

The smooth joint model is used to simulate interfaces. The traditional way to model an interface is to change the properties such as strength of the bonds along the interface to those representing the real interface. The problem with this approach is bumpiness of the boundaries that can affect the behavior of the system. The effect of these bumpy boundaries could become more important, when it comes to modeling joints or weak planes. A possible solution is to use smaller size particles along the interface which is not practical in large models. In order to solve this problem, another type of bond that simulates an "interface" regardless of the orientation of the particles along it is the "smooth joint contact model" (MAS IVARS et al. 2008). This model can be assigned to all the contacts between particles that lie on or along the opposite sides of the interface. This model overcomes the drawback of bumpy boundaries. The reason for calling it "smooth" is because of the constitutive behavior that allows particles bonded by this contact model to overlap and to "slide" on each other instead of moving around one another. Once a smooth joint model is created, the already existing contact or parallel bond models are deleted automatically for the contacts along the interface. Figure 3 shows the behavior of smooth joint model compared to the usual parallel bond model.

In PFC3D, it is assumed that due to small time steps, a disturbance cannot propagate farther than neighbor particles, and therefore, velocities and accelerations can be considered constant during each cycle. Once a force is applied to the model, integrating twice the Law of Motion using the time step, velocities and then displacements are calculated that result in the updated position of each particle. The



a Standard contact model with relative normal and tangential forces with regard to their orientation, b displacement of the particles bonded by standard contact model assuming the *bottom ball* is fixed, c normal and tangential forces on the particles whose contact is located along the smooth joint regarding their orientation with respect to the joint, d displacement of particles bonded by smooth joint model (MAS IVARS 2008)

updated positions are then used by the Force–Displacement Law to calculate the new forces, and so on. This process of cycling is continued until a predefined criterion is met.

4.1. Algorithm for Recording Slip-Induced Microseismicity

The numerical representation of the fault is composed of all the contact points whose at least one of the particles is located along the fault. Once a slip occurs at any of these contacts, if the normal stress of that contact is greater than 0.1 MPa, an "event" is created and the time at which slip started is recorded. The reason for this threshold can be explained using Fig. 1 (left). According to this figure, if the simple static-dynamic friction law (dotted blue curve) is used instead of the realistic frictional resistance curve (solid red), the rate of decrease in frictional resistance during slip will always be faster than the rate of decrease in driving force, and thus every slip will be seismic. It is known that low stiffness, high normal stress, and small D_c facilitate the unstable slip (DIETERICH 1979). Based on Eq. (1), assuming the frictional properties and the stiffness of the surroundings are constant along the fault, normal stress will be the only controlling factor for the onset of instability, and thus a low normal stress results in the fault sliding stably. Therefore, it is necessary to set a minimum normal stress for the slips to be considered seismic. In practice, this threshold has the advantage of reducing the number of recorded events and faster computation time (HAZZARD and PETTITT 2013). However, it will be shown in Sect. 4.3.2 of this paper that the models presented in this study are not sensitive to this threshold.

According to laboratory stick-slip friction data reported by McGARR (1994), the dynamic friction in this study has been assumed equal to 80 % of the static friction. Therefore, once a slip passes the normal stress criterion, the coefficient of friction of that contact is dropped to 80 % of its original value. Once the contact stops sliding, the coefficient of friction is readjusted to its static value. This is implemented to take into account the healing phenomenon (due to processes such as creep in the field or thermal mechanism in the lab causing the microasperities to weld together) that is believed to be a necessary component for generation of earthquakes in nature (McLASKEY et al. 2012). For each seismic slip, the start and end times as well as displacement of the contact are recorded. Considering each slip as one event, results in all the magnitudes are assumed to be almost equal. A good practice is to assume a group of slips close in time and space forming a slip patch and clustering them to form a single event. Therefore, the events have been clustered if they had two conditions: they were within a space window and their duration of slip would overlap for at least one cycle. Another criterion has also been implemented for duration of each slip. Assuming the shear can propagate as slowly as 0.5 times the shear wave velocity of the material (HAZZARD and YOUNG 2000), the minimum duration of a slip to be considered seismic is calculated as:

$$T_{\min} = \operatorname{int}\left(\frac{\operatorname{space_window}}{0.5 \times \operatorname{ae_svel}}\right)$$
(3)

where T_{\min} is the time required for the shear wave to propagate the space window, space_window is considered to be 0.42 m in this study, and ae_svel is the shear wave velocity equal to 2,700 m/s for Sierra granite as reported by McLASKEY *et al.* (2014). Equation (3) shows that not only does the choice of space window affect the size of clusters and, therefore, distribution of event magnitudes, but also it affects the minimum lifetime of a slip to be considered seismic.

Therefore, choosing an appropriate space window can be considered part of the model's calibration. For a similar clustering algorithm, but for crack-induced events, HAZZARD (1998) showed that the space window of five particle diameters would yield the best results in a 2D model, and above this value, the *b*-values were not dependent on the size of window, while for a 3D model a smaller space window would be more reasonable. Later in a study of unstable fault slip in Lac Du Bonnet granite, HAZZARD et al. (2002) showed that three particle diameters would result in a realistic b-value. In the present model, considering the maximum diameter of the particles is 0.14 m, a space window equal to 0.42 m (three particle diameters) has been used. Comparison of the results with data reported by McLASKEY et al. (2014) and McLASKEY and KILGORE (2013) will be shown in the next sections and confirms that this is an appropriate choice.

At the end of the test, all the slips that occurred within the space window and with the durations overlapping at least one cycle are clustered together. The area of each clustered event is calculated assuming the event as an ellipse. The largest and smallest radii of the ellipse are calculated based on the farthest and closest particles to the center of the event, respectively.

In order to calculate the centroid of each event, the number of contacts forming that event has been used. However, it has to be emphasized that the number of "contacts" forming an event is not necessarily the same as the number of "slips" forming that event. As an example, the clustering process for three smooth joint contacts, A, B, and C, is schematically illustrated in Fig. 4.

In this figure, imagine contact A starts slipping from 0.10 to 0.15 s. At 0.13 s contact B starts slipping within the space window of contact A, and therefore, these two slips constitute one event. The contact B slips until 0.20 s. At 0.15 s contact C starts slipping until 0.16 s at which point contact A starts slipping



A section of the fault illustrating the clustering process for three contacts, *A*, *B*, and *C*. It's assumed that no other contacts within the space window slipped from 0.10 to 0.20 s. Size of the elliptic event is determined based on the closest and farthest contacts to the center of the event (i.e. *B* and *A*, respectively)

"again" until 0.20 s. No other contacts slipped within the space window of contact A from 0.10 to 0.20 s. In this example, although there are four slips forming one event, there are only three contacts involved, and therefore, the location of contact A is used once for calculating the centroid (although it slipped twice). The centroid is simply calculated as the average of the locations of the contacts forming the event. Average displacement is calculated as the sum of all displacements associated to all the slips, four slips in this example, forming one event divided by the number of contacts in that event/cluster. Having the area of the event and the average displacement of all the contacts forming the cluster, seismic scalar moment, M_0 , is calculated using Eq. (2). Eventually, magnitudes are calculated using Eq. (4):

$$M_w = \frac{2}{3} \log M_0 - 6.0 \tag{4}$$

The whole idea of clustering is justified considering the fact that in nature, most seismic events are made up of small ruptures and shearing of asperities (SCHOLZ 2002).

4.2. Results

A discrete element model of the experiment reported by McLASKEY *et al.* (2014) and McLASKEY and KILGORE (2013) is made by PFC3D as shown in Fig. 5. There are six walls surrounding the model. The wall on the face is not shown in this figure to make the balls visible. The balls are bonded together by parallel bond model. In order to resemble the fault, smooth joint model has been installed in all the contacts of all the particles located along the diagonal fault extending from top right to the bottom left of the model.

There is no direct one-to-one correspondence between the micro-parameters of a discrete element model and macro parameters of the real rock. Therefore, the calibration process involves some trial and error attempt of varying the micro-parameters until the desired macro response is observed (ITASCA 1999). However, in the present model, in order to eliminate the effect of possible bond breakages (cracks) on the fault's behavior, the strength properties of parallel bonds were set to high values so that they would not control the results, and therefore, such calibration for the parallel bond properties was no longer necessary. The fault (smooth joint) parameters were chosen so that the expected stick-slip behavior would be observed at the onset of instability at about 3.7 MPa as reported by MCLASKEY and KILGORE (2013). In order to keep the normal stress on the fault constant at 5 MPa during the test, the top and bottom



Figure 5 The PFC3D model. The fault extends from the *top right* to the *bottom left*

walls were moving inwards while the right and left walls were moving outwards, all four with the same velocity. The two walls on the back and front were not moving during the test. However, it has to be kept in mind that due to complete symmetry in the fault's location and loading scheme of this test, as well as high strength properties of the parallel bonds, there will be practically no damage in any part of the model other than slip along the fault. The PFC3D parameters of the model are summarized in Table 1.

As the first pass to validate the model, the normal stress along the fault has been obtained during the test. In PFC3D, it is possible to record the stress and strain values in three different ways: wall-based, measurement sphere-based, and particle-based. The wall-based stresses are calculated as the sum of outof-balance forces of all the particles in contact with the wall divided by the wall's area. Measurement spheres (or "circles" in 2D) are representative volumes in which an average value for the stress or strain is calculated. They can be defined at arbitrary places in the specimen. Particle-based measurements represent the value of stress at one particular point.

In order to ensure that the normal stress remains constant on the fault, the wall-based stresses (shown in dashed red and purple in Fig. 6) were monitored. Considering the whole model as one big element, the normal stress on the fault, however, is calculated using a 2D transformation matrix as shown in Eq. (5):

$$\sigma_n^{\text{fault}} = \frac{\sigma_x + \sigma_y}{2} - \frac{\sigma_x - \sigma_y}{2} \cos 2\theta - \tau_{xy} \sin 2\theta \quad (5)$$

where θ is 45°, τ_{xy} is assumed to be negligible and σ_x and σ_y are wall-based stresses along the *x* and *y* directions, respectively. As another measure of assurance, the normal stress on the fault is also determined by summing up all the normal forces of all the contacts with the smooth joint model assigned to them divided by their area. The wall-based and directly measured normal stresses along the fault, as well as the wall-based stresses along the *x* and *y* directions, are plotted in Fig. 6. As can be observed in this figure, if the onset of instability is assumed as the point at which the increase in shear stress stops (i.e. 3.7 MPa), this point corresponds to about 0.22 s past the start of the test. Despite the laboratory

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meto parameters used in 1105D model of Sterra granite				
Ball parameters		Smooth joint parameters		
Average radius (m)	Young's modulus (GPa)	Normal stiffness (N/m ³)	Shear stiffness (N/m ³)	Coefficient of static friction
md_ravg 0.056	ba_Ec 2.1E10	sj_kn 2.1E10	sj_ks 2.1E10	sj_fric 1.05

 Table 1

 Micro-parameters used in PFC3D model of Sierra granite





Stress measurements during the test. *Dotted blue curve* starting at 5 MPa is the direct measurement of normal stress from the particles along the fault. The *solid green curve* at 5 MPa is the normal stress along the fault determined from the wall based stresses by the transformation matrix. The *solid black curve* starting at 0 MPa is shear stress along the fault directly measured from the smooth joint contacts. The *two dashed symmetrical red* and *purple curves* are the wall-based stresses along the x and y directions, respectively

experiment which has practical limitations for how much the fault can slip, in this PFC3D model, there is really no criterion for when the test should stop. Therefore, the test was stopped once 0.1 % total displacement of the fault (i.e. 2 mm) was reached. Total displacement of the fault is calculated mathematically from the wall-based strains in the *x* and *y* directions.

As can be observed in Fig. 6, the normal stress directly measured from the balls is a little bit smaller than the wall-based measurement, which is as expected since the fault is modeled as a discontinuum surface. Other than that, the normal stress along the fault has been kept constant during the test. The overall shear stress along the fault versus time as well as a magnified section of the final stick-slip behavior is plotted in Fig. 7.

As can be observed in this figure, the stick-slips have been successfully modeled by the numerical model. Prior to the onset of instability at 3.7 MPa, McLASKEY and KILGORE (2013) observed a linearly increasing shear stress throughout the test. An interesting observation from this figure is that three stages in the slip behavior of the fault can be identified. The first stage is from 0 to about 3.2 MPa where the shear increases linearly with no major stick-slips. The second stage starts from 3.2 MPa until about 3.7 MPa with minor stick-slips while the



Figure 7

The average shear stress along the fault versus time. Shear force is a vector with three components. Average shear stress of all the contacts with smooth joint model along the x and y directions are calculated by summing up their respective forces divided by their areas. Then the average shear stress along the 45° fault is calculated by the stress transformation matrix

shear is still increasing, but non-linearly (i.e. the strength is still mobilizing). The final stage starts from 3.7 MPa where the falls and rises of shear stress become more significant and the overall trend of shear stress becomes almost constant while the fault is sliding.

Location of the slips at two sides of the fault recorded in the PFC3D model is shown in Fig. 8. As can be observed in this figure, the events are uniformly spread along the fault. This is in agreement with the observation of McLASKEY *et al.* (2014).

In the PFC3D model, 223 slips have been recorded with the majority of magnitudes around –6 and some –7. As was previously mentioned, a reasonable approach would be to cluster the slips close in time and space to represent more realistic events. After clustering, the number of events is reduced to 131. As can be observed from the clusters shown in Fig. 9, the largest events have occurred at the central section of the fault which is in agreement with MCLASKEY and KILGORE (2013). Because of difficulties in plotting ellipses, all the events in Fig. 9 are illustrated with circles with diameters equal to the major axis of ellipses; otherwise, as mentioned before, the area of each event has been calculated assuming it has an elliptic shape in general. It has to

be emphasized that the number of events in a PFC model is a function of model's resolution, and therefore, it is not reasonable to compare the number of PFC events directly with the real number of events recorded in the experiment.

In their experiment, McLaskey and Kilgore (2013) reported that the normal stress along the fault was kept constant at 5 MPa. However, in their recent 2014 publication, the test was repeated with 4 and 6 MPa normal stresses along the fault. MCLASKEY et al. (2014) were able to locate 16 and 32 events accurately for the test with 4 and 5 MPa normal stresses, respectively. In order to determine the mechanism of events, they performed a moment tensor inversion technique and reported that the majority of the events could be modeled by a doublecouple mechanism resulting from frictional slips. The average displacement of each dynamic slip event (DSE) was reported to be about 50-150 µm occurring in about 3–5 ms with a source radii of about 3–6 mm. A few larger foreshocks (M > -5.0) were not reported due to difficulty in analyzing them. In the PFC3D model, there are 98 smooth joint contacts forming the fault. The stick-slip behavior of a group of them during the test is shown in Fig. 10.



The *top figure* shows the location of events reported by (MCLASKEY *et al.* 2014). Foreshocks and aftershocks are shown by *circles* and *diamonds*, respectively. They have not reported the events near the fault ends. The *two figures* at the *bottom* with *blue background* are the location of slips in the PFC3D model at both sides of the fault. The *figure* between these two is a side view of the fault with the location of events around it. No clustering is shown in this figure



Figure 9 The clustered events in PFC3D model. A bigger radius shows a larger patch. *Concentric circles* represent consecutive slips on the same contact

Although a general trend of increase in the shear stress followed by stick slips is observed for the fault in Fig. 7, it can be observed from Fig. 10 that different contacts do not necessarily follow the same stick-slip pattern. In other words, for the small patches along the fault, not every drop in shear stress corresponds to a drop in the normal stress. This suggests the likelihood of the existence of another process responsible for generation of local stick-slips. It is in agreement with McLASKEY and KILGORE (2013) that some aseismic slips can possibly trigger repeated earthquakes in their vicinity.

4.3. Parametric Study

A parametric study is presented in this section to investigate the effect of various parameters on the shear behavior of the fault as well as on generation of microseismic events.

4.3.1 Studying the Effect of Space Window's Size

A model with the same properties as mentioned in Table 1 is repeated with different space window sizes of 0.14, 0.28 and 0.42 m (equal to one, two, and three times the maximum diameter size of the balls,



Variations of stick-slip behavior in different contacts along the fault. Normal and shear forces are shown with *solid blue* and *dashed red*, respectively



Figure 11 b-value plots as well as frequency of the number of events recorded during the tests for three different sizes of space windows

0.14 m). In order to calculate the magnitudes, the shear modulus of 2 MPa has been used for the slipping patch in all the tests. The *b*-value plots as well as variations in the number of events for the three tests are shown in Fig. 11.

As can be observed in this figure, an increase in the size of space window causes an increase in the appearance of magnitudes larger than -6 while for the smaller magnitudes, a reverse effect is observed. A comparison between the numerical *b*-value plots with the experiment is not accurate for three reasons: (a) McLaskey's data belong to the tests with 4 and 6 MPa normal stress (not 5 MPa). (b) The loading in this study was continuous, while in order to simulate the earthquake cycle, their experiments would include loading, resetting, and holding at four stages. (c) Some magnitudes greater than -5 have not been reported by them. However, for the sake of comparison and considering the *b*-values, regardless of *a*-values, the size of space window equal to three times the maximum diameter of the balls, 0.42 m, seems to provide the best match with reality, and therefore, it has been used for the other tests presented in the paper.

Also, a fewer number of clusters have been observed for greater sizes of space window which is as expected.

4.3.2 Studying the Effect of Normal Stress Threshold for Seismic Events

A model with the same properties as mentioned in Table 1 is repeated with three normal stress

thresholds of 0.0 MPa (i.e. no threshold), 0.1, and 3 MPa for the slips to be considered seismic (Fig. 12). As was mentioned in Sect. 4.1, although the coefficient of friction is decreased to 80 % of the static friction for the slips that pass the normal stress threshold, thus affecting the shear strength as well, no significant difference in shear-displacement and displacement–time plots was observed, and therefore, they are not included in the paper. However, as was expected, a lower threshold would result in a greater number of smaller events and also earlier appearance of events in the shear process. The *b*-values do not seem sensitive to this threshold.

In nature, the overall normal stress on the fault would depend on the in situ stresses as well as orientation of the fault, while for the local patches along the fault, heterogeneity would also play a role. Therefore, this threshold would be more important if faults with different resolutions and/or faults in different stress regimes were being compared. However, for the conditions tested in this section, the behavior of the model does not seem sensitive to the choice of this threshold, and thus 0.1 MPa has been used for the other tests presented in next sections.

4.3.3 Studying the Effect of Discretization (Size of Particles)

A model with the same properties as listed in Table 1 has been repeated with finer and coarser particles. The average radii of the particles in the three tests were 0.081 m (199 balls), 0.056 m (649 balls), and 0.029 m



Figure 12 Variations of model behavior for different normal stress thresholds for the slips to be considered seismic

(5,164 balls). As shown in Fig. 13, coarser balls would result in higher strengths, greater stress drops during stick-slip, slower rate of displacements and smaller *b*-values. Although the events appear earlier in the finer model and the number of events are higher, the second stage in transitioning from elastic linear increase in shear strength to the final instability where the shear stress becomes constant, from 85 % to peak strength, is less obvious in the finer model. This could be observed both in the shear-displacement plots and in frequency of events versus time plots where the slope of getting to the peak number of events is very steep for the finest model (Fig. 13).

4.3.4 Studying the Effect of the Coefficient of Friction of the Fault (sj_fric)

A model with the same properties as mentioned in Table 1 is repeated with different coefficients of friction of the fault (1.05, 0.85 and 0.55) which is within the range of 0.6 to 1 as suggested by BYERLEE (1978). The results shown in Fig. 14 indicate a decrease in overall shear strength as well as an increase in the rate of displacements for smaller coefficients of friction. The number of magnitudes larger than -5.5 are not much sensitive to the fault's coefficient of friction while an increase in the greater number of events smaller than -5.5 is observed for smaller coefficients which is consistent with the greater number of events observed for these faults.

4.3.5 Studying the Effect of Particle Elasticity (ba_Ec)

A model with the same properties as mentioned in Table 1 is repeated with varying Young's moduli of the balls (2.1e9, 2.1e10, and 2.1e11). This would represent the stiffness of the medium surrounding the fault. As shown in Fig. 15, for the softest model (ba Ec = 2.1e9), small stick-slip instability was observed as early as 0.1 mm displacements were reached. This behavior continued until about 7 mm displacements (at 3.7 MPa shear stress) that could be considered the onset of the second stage. The peak shear strength, 4.4 MPa, was reached after 9.6 mm displacements and 1.9 s after the start of the test. This is much longer compared to previous cases where the maximum shear strength was reached in a fraction of a second. The overall pattern of shear-displacement for the fault with the softest surrounding (i.e. ba Ec = 2.1e9) included three stages in shear process similar to the model with Young's modulus of balls equal to 2.1e10, but only the portion until 2 mm displacement is shown in Fig. 15.

For the model with the surrounding region harder than the fault itself, a softening behavior is observed with almost no second stage in the shear process. With regard to the number of events, a softer surrounding has not resulted in more emissions for the same amount of displacement, and its only contribution has been to delay the process of displacements. An overall shift in the *a*-values



Figure 13 Variations of the model's behavior for different resolutions

towards larger magnitudes is also observed for the faults with softer surrounding while the *b*-values are not much sensitive.

4.3.6 Studying the Effect of the Fault's Elasticity (sj_kn and sj_ks)

A model with the same properties as mentioned in Table 1 is repeated with varying elastic properties of the smooth joint. As shown in Fig. 16, higher shear strengths are observed for harder faults. The rate of deformations and *b*-value plots, however, do not seem to be much affected. A lower number of events is observed for softer faults.

4.3.7 Studying the Effect of Normal Stress

A model with the same properties as mentioned in Table 1 is repeated with normal stresses along the

fault equal to 3, 5, and 7 MPa. The plots in Fig. 17 show an increase in the shear strength as well as a decrease in the rate of deformations for higher normal stresses. Also, for the same amount of deformation, higher normal stresses generate fewer emissions. An overall decrease in the b-value can be observed for higher normal stresses as well.

5. Discussion

As expected, the behavior of the numerical model was sensitive to the elastic properties of the medium surrounding the fault as well as the fault's properties and the size of particles. It is in agreement with the fundamental mechanism shown in Fig. 1. Sensitivity of the numerical model to the frictional parameters is also in agreement with the observation of McLASKEY *et al.* (2014) who believed that the recorded events



Figure 14 Variations of the model's behavior for different coefficients of friction

were not due to factors such as grain crushing or fracturing of the fresh rock. The majority of events were believed to have a double-couple mechanism indicating a shear dislocation along the fault. The ones with a non-double-couple mechanism were expected not to exceed 20 % of all the events (McLASKEY *et al.* 2014).

They observed no specific difference between the focal mechanisms and magnitudes or even stress drop of the foreshocks and aftershocks. Both types of events were broadly distributed along the fault. This is consistent with the results of numerical modeling presented in this study. The results show that largest magnitudes appear mostly in the last stage of unstable stick-slip once the peak shear strength of the fault is already reached.

According to the model shown in Fig. 1 (left), whether or not a slip is seismic (or aseismic) would

depend on the elasticity of the medium (i.e. stiffness of spring in this model) as well as the amount of stress drop due to unloading the normal stress or frictional properties of the surface. In Fig. 15, it was shown that stickslips would occur much earlier in the shear process for the fault with softer surrounding. This is in agreement with the fact that low stiffness facilitates unstable slips (DIETERICH 1979). Also, it has been suggested that local stick-slips could trigger or facilitate other slips in their vicinity (McLaskey and KILGORE 2013). A possible mechanism for this could be the fact that local slips (or in other words, local unloading normal stress conditions) provide a softened surrounding for their neighbor patches and thus, similar to what was shown in Fig. 15, facilitating their instability. The amount of how much of either seismic or aseismic slips would contribute to this could be the subject of another study.



Figure 15

Variations of the model's behavior for different Young's moduli of the particles. Distribution of magnitudes for the softest model are plotted based on the events recorded until 2 and 9.6 mm displacements

6. Conclusion

This paper presented applicability of the discrete element modeling to reproduce stick-slips successfully on a large scale, which takes a lot of time and effort in laboratory to be studied. Once the model is calibrated with one set of experiments, it can be used to expand our knowledge to the cases that cannot be easily tested.

In this research, the microseismic release along preexisting faults during shearing was studied numerically. For this purpose, the experiment reported by McLASKEY and KILGORE (2013) was modeled using PFC3D. PFC inherently allows modeling of stick-slips; however, an algorithm is also developed in this research to record the slip-induced acoustic emissions. Some advantages of the present model are as follows: (1) The three-dimensional and discrete

nature of model allows taking into account the geometrical heterogeneity and make the simulations more realistic. (2) Focusing on the fault's behavior by use of a smooth joint model allows eliminating the bond breakages affecting the results. (3) The algorithm developed for recording the stick-slip induced microseismic events.

Once the results compared well with real laboratory data, the model was then expanded upon to study the difference in shear and microseismic behavior in faults with different properties. A summary of the results is presented here:

 A decrease in shear strength was observed for the models with smaller particles, smaller coefficient of friction of the fault, harder surroundings of the fault (higher Young's modulus for the particles), softer faults (smaller elasticity moduli of the fault), and



Figure 16

Variations of the model's behavior for different elastic properties of the fault. Distribution of magnitudes for the model with softest fault properties are plotted based on the events recorded until 2 and 3.8 mm displacements

smaller normal stress on the fault. Also, a softer behavior (i.e. decrease in the initial slope of sheardisplacement curve) was observed for the softer faults as well as faults with softer surrounding.

- 2. A higher rate of displacements was observed for the faults with finer particles, smaller coefficient of friction, harder surrounding, and smaller normal stress. The fault's elastic properties did not seem to have much effect on the rate of displacements; however, a small increase in this rate was observed for the softest fault. A comparison between displacement–time and shear-displacement curves suggests that higher rate of displacements are observed for weaker conditions (i.e. conditions resulting in smaller peak strength) while this conclusion seems less obvious for the softer faults (Fig. 16).
- 3. With regard to the magnitudes, a greater size of space window resulted in an increase in the events larger than -6 while a reverse effect was observed for the smaller events. The *b*-values were not sensitive to the normal stress threshold of slips to be seismic. Increasing the resolution or decreasing the normal stress on the fault both caused an increase in the *b*-values. Decreasing the coefficient of friction did not have much effect on the magnitudes larger than -5.5 while for the smaller magnitudes, a decrease in this coefficient caused an increase in the number of events. Increasing the particles' elasticity caused a decrease in the avalues, but the *b*-values were not much affected. The *b*-values were not sensitive to the elastic properties of the fault.



Variations of the model's behavior for different normal stresses. Distribution of magnitudes for the model with 7 MPa normal stress are plotted based on the events recorded until 2 and 2.8 mm displacements

4. A larger number of recorded events were observed for the models with smaller size of space window, smaller normal stress threshold, finer particles, smaller coefficient of friction, harder fault surrounding region, harder fault, and smaller normal stress on the fault. An obvious observation is that for the same amount of slip, the emissivity would depend on several factors affecting the release of microseismic energy. It was also suggested that there are three stages in the slip behavior of a fault: (1) linear increase in the shear stress until 85 % of the peak strength with no or very few stick-slips, (2) stable slip from 85 % of the peak shear strength until the maximum shear strength is reached, (3) unstable continuation of slip until for some reason the fault stops. An exception was observed for the case with the fault's surrounding being harder than the fault itself (Fig. 15), where right after the first elastic stage in the shear process, the third stage started with a post-peak softening pattern. However, among these three stages, the last one which is unstable has the greatest number of stick-slips, and therefore, a comparison between the number of events versus time and shear versus displacement plots suggests that for the same amount of displacement, the conditions at which the third stage is reached earlier would be the most emissive ones.

The results suggest that in reality it is quite possible for the two ends of a fault to be still while there are patches along the fault undergoing stick-slips; however, due to the geometry of the fault and loading scheme used in this research it was not investigated. Also, local stick-slips seem to provide a softer surrounding for their neighbor patches favoring their subsequent stick-slips.

With regard to the calibration of model for stickslip behavior, the onset of instability (peak shear strength) as well as *b*-value seems to be the two most controlling parameters that need to be taken into account.

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